Lecture 1: Introduction to PySpark

Distributed computing over a cluster is a widely adopted strategy in the case of many applications both in- and outside academia.

Imagine you are interested in working on a very large dataset, at the scale of hundreds of Terabytes or even Petabytes. As discussed in the Data Management part of the course, a large horizontally scalable storage solution is going to be necessary to host the entire dataset. Even if we assume the storage solution is sorted out, we are left with the issue... how can we deal with all these data in order to produce the "final result" we aim at?

Even if we assume the storage solution is sorted out, we are left with the issue... how can we deal with all this data to produce the "final result" we aim for?

- Data are distributed over many nodes, and collecting all data in one node (e.g., loading the entire dataset into a single computer memory) would be impossible.
- Not all data in the entire dataset is necessarily going to be relevant to solve your problem. You may want to first load all data, explore it, filter it, and preprocess it.
- Then, you may want to move to the actual data analysis phase and possibly apply
 machine learning models on the preprocessed data. However, even the preprocessed
 data may not fit into your local machine's memory, and once again, a distributed system
 is necessary.

What you would like to do is to run the pre-processing on the nodes of the cluster where the data is distributed, and return only the high-level quantities that will be used in the analysis, or even the end result of the entire analysis.

This is the core concept of distributed computing frameworks like Hadoop and Spark: the code/execution goes to the data, rather than the data coming to the machine where the code resides (data locality).

Docker Cluster

For this set of lectures we will work with a standalone Spark cluster deployed on your machine via Docker. This is a mock-up of a larger scale cluster setup, and can also be used to develop and test your application before deploying it on a "production" cluster.

We are using docker compose to create the cluster with multiple Docker containers acting as computing nodes.

The cluster dashboard is exposed at localhost: 8080 and the master is already available at spark: //spark-master: 7077

Spark Session

We can now create the Spark session.

With the following command we are asking the master (and the resource manager) to create an **application** with the required resources and configurations.

In this case, we are using all the default options (e.g. number of cores and number of executors), but we can also specify them by hand with .config("spark.some.config", "value").

The list of available configurations can be found here.

```
# import the python libraries to create/connect to a Spark Session
from pyspark.sql import SparkSession
# build a SparkSession
    connect to the master node on the port where the master node is
listening (7077)
   declare the app name
    configure the executor memory to 512 MB
    either *connect* or *create* a new Spark Context
spark = SparkSession.builder \
    .master("spark://spark-master:7077")\
    .appName("My first spark application")\
    .config("spark.executor.memory", "512m")\
    .get0rCreate()
Setting default log level to "WARN".
To adjust logging level use sc.setLogLevel(newLevel). For SparkR, use
setLogLevel(newLevel).
24/06/06 09:55:42 WARN NativeCodeLoader: Unable to load native-hadoop
library for your platform... using builtin-java classes where
applicable
```

Check the content of the Spark Session spark object.

This is the entry point to the main Spark functionalities.

```
spark
<pyspark.sql.session.SparkSession at 0x7f65c858c610>
```

The **Spark UI** link provided won't work directly, as it refers to the Docker container running the Spark application.

However, port mapping is provided for port 4040, allowing you to access the Spark UI link for the application by pointing your browser to localhost: 4040.

From the Spark Session we can access the Spark Context.

The Spark Context is the driver application program we will use to submit applications to Spark, and it is used to work with RDDs

```
# create a spark context
sc = spark.sparkContext
```

```
# print its status
sc
<SparkContext master=spark://spark-master:7077 appName=My first spark
application>
```

Parallelize!

The main feature of Spark is to distribute data into a number of **partitions**, either using the *memory* or the *disk* available in the executors.

Also, keep in mind the difference between the Worker and the Executor in Spark!

The first command we will use is parallelize().

This is a function of the SparkContext (sc) object and it is used to create a Resilient Distributed Dataset (RDD) from a list collection. In other words, it takes a collection and splits it among the executors.

We will start with a basic example to get familiar with the main functions of Spark RDDs.

Starting from a Python "dataset", we create an RDD, i.e., a distributed dataset residing on the cluster, dist_data, and then operate on it in parallel.

```
# a simple python list, as the starting dataset
data = [1,2,3,4,5,6,7,8]

print(f'{type(data)=}')

type(data)=<class 'list'>

# parallelize it over the available executors!
dist_data = sc.parallelize(data)

print(f'{type(dist_data)=}')

type(dist_data)=<class 'pyspark.rdd.RDD'>
```

Go and check the Spark web UI

- http://localhost:8080 for the Master node web UI
- http://localhost:4040 for the SparkContext web UI (where you application will reside)

In principle, we could expect the application to report something related to our request of parallelizing data over the cluster...

But instead... nothing happened in the Web UI, even though we asked Spark to parallelize our data into a number of partitions!

That's because parallelize is not an action, but a transformation, and thus is *lazy* by nature.

We can trigger it by using an action, for instance, the **count** action, a function used to count the number of elements in the RDD.

```
# count elements of the rdd
dist_data.count()
```

Let's go back and check the Spark web UIs and interpret its content...

If you are using two executors (i.e. two cores of your CPU in this example), in the WebUI you will see two parallel lines for this task.

That's because the RDD consists of two partitions.

Indeed, under the hood, the RDDs are stored and represented as partitions, "small blocks" of the original dataset that will be **unit of parallelism**.

One partition can be processed by one PU (e.g. a core of a CPU) at a time. More PUs can thus operate on multiple partitions at the same time, with the limit of 1 PU per partition.

In other words, if the RDD is composed of one partition, even if we have two total available cores, then only one task at a time will be run.

On the other hand, if the RDD partitions are four and we still have two available cores, only two of the partitions will be processed in parallel.

To split our data in an arbitrary number of partitions we can use numSlices

```
# parallelize using a different number of partitions
sc.parallelize(data, numSlices=8).count()
8
```

We can ask Spark to count the number of partitions of a given RDD with the method getNumPartitions()

```
# sc.parallelize() is itself an RDD
# thus we can call getNumPartitions() on the RDD created via the
parallelize transformation
sc.parallelize(data, numSlices=8).getNumPartitions()
8
```

By default, Spark will try to split the dataset into a number of partitions equal to the number of executors.

Not always successfully, though...

To parallelize your computation effectively, you should make sure what is the number of slices your dataset is parallelized into, and how it compares with the available computing resources.

```
# get the number of partitions of the RDD created previously
dist_data.getNumPartitions()
```

It's important to visualize that **the RDD resides in the worker nodes**, and not in your client/local machine.

If we print the dist_data object from Jupyter we will not see the actual data contained in the RDD, but only that this is a distributed dataset.

```
# print the dist_data object from here
print(dist_data)
ParallelCollectionRDD[3] at readRDDFromFile at PythonRDD.scala:289
```

This is actually a very important concept, as in a distributed system the datasets we are processing are typically much larger than the available memory of the driver (it's one of the main reasons we use a distributed system in the first place).

Returning the content of the whole dataset in a single machine is not a clever idea.

However, a distributed dataset can be collected in the driver with collect().

By issuing this action, all the workers will send back all the blocks of the RDD.

This is generally used to collect only the end results after a computationally heavy processing is first run on the worker nodes, and a slim and manageable result can be retrieved.

This function should be **used with caution** since **it fetches the entire RDD to a single machine** and can cause the driver to run out of memory.

```
# collect the distributed dataset (so far, a mere list)
dist_data.collect()
[1, 2, 3, 4, 5, 6, 7, 8]
```

If we have a massive dataset and we are looking to inspect only a small subset of elements we can use take (num).

take allows to return only the first num number of elements from the RDD, thus limiting the amount of data we are collecting from the cluster.

Under the carpet, Spark will look at one partition's data, and will decide if one is enough to satisfy your request, or it will need to retrieve data from more than one.

```
# retrieve a few elements from the RDD
dist_data.take(3)
[1, 2, 3]
```

Map and Reduce

We can now write our first map-reduce application.

The method map (f) will apply a function f to each *element* of the RDD.

For instance, let's create a simple function to increment by 1 each of the elements of the RDD.

```
[1,2,3,4,5,6,7,8] --> [2,3,4,5,6,7,8,9]
```

The function itself is very simple, we can use a Python lambda function to take care of that:

```
lambda(x: x+1)
```

Remember, **this is a transformation**, not an action. Being a map phase equivalent to the Hadoop Map-Reduce, we have the idea that all partitions will be operated in parallel.

To trigger the transformation, we can chain it with an action, such as collect.

```
# increment each value of the array with map
# and collect the result
dist_data.map(lambda x: x+1).collect()
[2, 3, 4, 5, 6, 7, 8, 9]
```

Differently from plain Hadoop, in Spark we can chain together multiple transformations, without having to strictly follow the Map-then-Reduce pattern.

For instance, we can even run an entire chain of map functions one after the other with no reduce function at all.

Let's chain a +1 increment function with a /2 function to divide the result of the previous multiple map transformations.

We can continue using map and lambda functions to do this, and chain a .map() after other .map() functions.

So far we can see that we have already moved away from the strict pattern of Map-Reduce "a-la-Hadoop", where every operation is a single Map phase followed by a single Reduce phase.

In this example we have instead 2 Map phases, and a single Reduce phase (the collect).

The optimization provided by the DAG scheduler will hide the map functions under the same processing stage, and will take care of running them pipelined as fast as possible.

Another important operation available is an explicit reduce function.

Reduce is an **action** that aggregates all the elements of the RDD using some user-provided function, and returns the result to the driver.

We will see later on another version of reduce, reduceByKey, which performs the reduction for elements with the same key, and we'll reproduce the wordcount example.

For the time being, let's explore a simple reduce implementation.

Reduce actions can take a **function as argument**, which will be applied to *all the elements of the RDD*, to perform some kind of **aggregation**.

For example, we can think about summing the elements of an RDD in pairs with a lambda function.

A schematic view of this simple Map-Reduce application can be seen sketched here:

Please note how the reduce function does not necessarily have to complete its task in a single iteration. In this case, the sum in pairs will continue on until we are left with a single scalar.

Exercise 1

Write a simple reduce function to find the minimum of dist data.

A simple approach is to evaluate the min of pairs of values x and y, by reducing the min(x,y) function.

```
dist_data.reduce(lambda x, y: min(x,y))
1
```

A list of built-in Python functions (including min) are also available, and can be used directly as a reduce-like action:

```
dist_data.reduce(min)
1
```

On top of these, clearly Spark does implement already all basic functionalities we might expect for the RDD objects, including min.

```
dist_data.min()
1
```

Exercise 2

Create a set of 100 points in a 3D space, represented as tuples of randomly generated floats, and calculate the maximum distance of the points from the origin (0,0,0).

- 1. Create the collection of tuples on the client (Python)
- 2. Parallelize the collection in a Spark RDD
- 3. Use Spark to evaluate the Euclidean distance of each point from the origin
- 4. Use Spark reduce to evaluate the maximum distance

```
# 1. Create the collection of tuples on the client (Python)
import random
points = [(random.random(), random.random()) for in
range(100)]
# print(points)
# 2. Parallelize the collection in a Spark RDD
dist points = sc.parallelize(points)
# 3. Use Spark to evaluate the euclidean distance of each point from
the origin
distances = dist points.map(lambda x: (x[0]**2+x[1]**2+x[2]**2)**0.5)
# 4. Use Spark reduce to evaluate the maximum distance
distances.reduce(lambda x, y: max(x,y))
# or
# distances.reduce(max)
1.470280176752061
# The entire set of functions can be implemented in one single
operation:
sc.parallelize(points)\
  .map(lambda x: (x[0]**2+x[1]**2+x[2]**2)**0.5)\
  .reduce(lambda x, y: max(x,y))
1.470280176752061
```

We should keep in mind that every time we move data **from the client to the cluster** or **from the cluster to the client** we are potentially paying a large price:

- moving data from the client to the workers implies a large amount of data transfers, through the driver, and to the executors. If we can read data directly from the worker nodes (we'll see later a couple of examples) this should always be preferred.
- on top of this issue, moving data from the workers to the client implies an additional risk. We might have more data on the cluster than what we can afford to store locally on our client machine. Moving back data (i.e. doing a collect) from the cluster might crash the driver, and crash your application. Refrain from asking Spark to collect an entire GB-, TB- or even PB-sized dataset to your laptop.

Exercise 3 - compute π

Estimate π by simulating random points in the unit square (side length of 1) and counting how many fall in the unit circle.

The probability of one point falling inside the circle is

$$P = \frac{\text{Area circle}}{\text{Area square}} = \frac{\pi}{4}$$

We can estimate this probability by counting the number of simulated points inside the circle

$$P = \frac{\text{#Points in circle}}{\text{#Points}}$$

Thus obtaining

$$\pi \approx 4 \cdot \frac{\text{#Points in circle}}{\text{#Points}}$$

This can be done in Spark by running the computation in parallel with the following steps:

- 1. Create a "dummy RDD" containing placeholders for all the points (e.g. use the value 0 as a placeholder for each data point)
- 2. Generate the points as random (x,y) pairs and check if each of them falls inside/outside the circle
- 3. Count the points inside the circle

Think about which transformations are needed to generate the points and to check if they fall inside the circle. Combine all the transformations and the action in a single pipeline.

```
num_points = 1_000_000

# instantiate a "placeholder RDD"
points_rdd = sc.parallelize([0]*num_points, numSlices=8)

def in_circle(dummy):
    # generate a point randomly and check if
    # it is inside the circle
    # by returning 0 or 1
```

The same result can be achieved using the filter transformation.

filter(f) returns a new RDD containing only the element of source RDD on which the condition/function f is true.

```
# perform the same exercise using filter
points inside = points rdd \
   .map(lambda x: random.random()**2 + random.random()**2) \
   .filter(lambda x: x < 1) \</pre>
   .count()
# or
# points inside = points rdd \
     .map(lambda x: (random.random(), random.random())) \
     .filter(lambda p: p[0]**2 + p[1]**2 < 1)
     .count()
# print result
print ("pi =", 4*points inside/num points)
(5
+ 2) / 8]
pi = 3.1411
```

Reduce by key and flat map

Consider the following dataset where each element consists of a tuple (group, value) (a simple example of a key-value pair).

This can be for example:

- group = product class
- value = revenue

Or readings from a set of sensors:

- group = sensor identifier
- value = reading

We may be interested in operating only on the *values* of the dataset, discarding the *keys*.

We can write a map function to do this, using the Python syntax to access only the [0] (the key) or the [1] element of the tuple.

For instance, we can implement a simple increment of +1 to all values via a map function.

```
# operate only on the values
class_rdd.map(lambda el: (el[0], el[1]+1)).collect()
[('group1', 11), ('group2', 5), ('group3', 2), ('group2', 8),
('group1', 9)]
```

The same result can be achieved using mapValues.

This allows to writing an equivalent map function that applies only to the values of the groups disregarding the keys.

```
# do the same using map values
class_rdd.mapValues(lambda x: x+1).collect()
[('group1', 11), ('group2', 5), ('group3', 2), ('group2', 8),
('group1', 9)]
```

We can perform a reduce function for each class using **reduceByKey**: in this way we are applying the reduce function only to all the elements of the same class.

Despite its name, **reduceByKey** is not an action, but a transformation, since it returns a distributed dataset (the result of an aggregation by key could still give a very large number of items if the number of keys is large).

Let's compute the minimum value of all elements of each group using reduceByKey and collecting the result.

We can further filter our results by using **takeOrdered** to get the first n results sorted by a given field.

By default, take0rdered(n) takes the first n elements of the RDD in ascending order. To get the descending order (or any other arbitrary order) we can specify a function, such as:

```
lambda x: -x
```

Get the maximum value for each group, and return only the 2 with the largest values

```
class_rdd.reduceByKey(lambda x, y: max(x,y)) \
    .takeOrdered(2, key=lambda x: -x[1])
[('group1', 10), ('group2', 7)]
```

If we are not interested in treating the dataset as key-value pairs, or in general we have a non-flat dataset (e.g. each element of the RDD is a list, or another object), we can use flatMap to "explode" each element returning a plain sequence of elements.

This can be extremely useful if you have data stored as arbitrary data structures, but would like to use them as plain lists of items.

Exercise 3: word count

Let's rerun the word-count example seen in class when discussing the Map-Reduce programming paradigm, starting from the following arbitrary text.

```
message = [
   'Three Rings for the Elven-kings under * the sky,',
   'Seven for the Dwarf-lords in $ their halls of stone,',
```

```
'Nine for Mortal # Men doomed to die,',
'One for [ the Dark Lord on his dark throne',
'In the Land of _ Mordor where the Shadows lie.\n',
'One Ring to } rule them all, One @ Ring to find them,',
'One Ring $ to bring them all and in the darkness bind them',
'In the Land of Mordor * where the Shadows lie.\n'

print(''.join(message))

Three Rings for the Elven-kings under * the sky, Seven for the Dwarflords in $ their halls of stone, Nine for Mortal # Men doomed to die, One for [ the Dark Lord on his dark throneIn the Land of _ Mordor where the Shadows lie.

One Ring to } rule them all, One @ Ring to find them, One Ring $ to bring them all and in the darkness bind themIn the Land of Mordor * where the Shadows lie.
```

The goal is to count the occurrence of each word using a map-reduce approach in Spark.

But first, you may want to need to clean-up the dataset by removing all "stray" symbols such as @ and \$.

To avoid double counting the same word when in lower- or upper-case, you may also want to change all the words to lower case.

Hint: use string.punctuation or a regular expression to remove the unwanted characters

```
import string
string.punctuation
'!"#$%&\'()*+,-./:;<=>?@[\\]^ `{|}~'
# parallelize the message
message rdd = sc.parallelize(message)
message rdd.collect()
['Three Rings for the Elven-kings under * the sky,',
 'Seven for the Dwarf-lords in $ their halls of stone,',
 'Nine for Mortal # Men doomed to die,',
 'One for [ the Dark Lord on his dark throne',
 'In the Land of Mordor where the Shadows lie.\n',
 'One Ring to } rule them all, One @ Ring to find them,',
 'One Ring $ to bring them all and in the darkness bind them',
 'In the Land of Mordor * where the Shadows lie.\n'l
# step 1: create the words rdd where each element is a word
# eq: ['one', 'ring', 'to', 'rule', 'them']
def clean row(row):
```

```
# this function should:
    # 1. clean a row from punctuation
        2. put each word in lowercase
       3. and return the list of words
    word list = []
    for word in row.strip().split():
        clean word = ''
        # scan the rows looking for punctuation
        for char in word:
            if char not in string.punctuation:
                clean_word += char
        # lower the words
        if clean word!="":
            word list.append(clean word.lower())
    return word list
# apply transformation
words_rdd = message_rdd.flatMap(clean_row)
# print a few items
words rdd.collect()[:10]
['three',
 'rings',
 'for',
 'the',
 'elvenkings',
 'under',
 'the',
 'sky',
 'seven',
 'for']
# step 2: perform word count!
# -> crate pairs (word, 1)
# -> reduce based on the word and count
word count rdd = words rdd.map(lambda word: (word, 1)) \
                           .reduceByKey(lambda c1, c2: c1+c2)
# print your result
word count rdd.collect()
[('three', 1),
 ('for', 4),
 ('under', 1),
```

```
('sky', 1),
('their', 1),
('halls', 1),
('of', 3),
('nine', 1),
('mortal', 1), ('doomed', 1),
('to', 4),
('die', 1),
('lord', 1),
('his', 1),
('land', 2),
('mordor', 2),
('where', 2),
('shadows', 2),
('find', 1),
('and', 1),
('bind', 1),
('in', 4),
('the', 9),
('lie', 2),
('one', 4),
('ring', 3),
('rule', 1),
('them', 4),
('all', 2),
('bring', 1),
('darkness', 1),
('rings', 1),
('elvenkings', 1),
('seven', 1),
('dwarflords', 1),
('stone', 1),
('men', 1),
('dark', 2),
('on', 1),
('throne', 1)]
```

The method take0 rdered (n, key) allows to collect only the first n elements based on the ordering provided by key. Ordering is by default ascending.

```
# collect the 10 most occurent words
word_count_rdd.takeOrdered(10, key=lambda x: -x[1])

[('the', 9),
    ('for', 4),
    ('to', 4),
    ('in', 4),
    ('one', 4),
```

```
('them', 4),
('of', 3),
('ring', 3),
('land', 2),
('mordor', 2)]
```

Exercise 4 - Distributed linear regression

The files in ../datasets/lecture1/ contain a series of measurements of a sensor. Each measure is in the form

```
Measure N: (t,val)
```

There could be pairs such as (t, None), corresponding to missing values. This measure should be removed.

We are interested in knowing if there is any sort of relation between t and val.

The first task consists of reading each file and creating an RDD containing as elements the pairs (t,val).

We can first inspect the first lines of a file to get a sense of the data:

```
!head ../datasets/lecture1/file_1.txt

Measure 0: (-10.00,0.70)

Measure 1: (-9.95,0.61)

Measure 2: (-9.90,0.47)

Measure 3: (-9.85,None)

Measure 4: (-9.80,0.58)

Measure 5: (-9.75,0.29)

Measure 6: (-9.70,0.35)

Measure 7: (-9.65,0.25)

Measure 8: (-9.60,0.39)

Measure 9: (-9.55,0.52)
```

Imagine that each file contains millions of measurements and there may be thousands of files.

Reading all the files with Python on our local machine (client-side), and then using parallelize should be avoided at all costs. This would be a very inefficient way to read the data, as we would have to read all the files in the driver (possibly getting out of memory), and then split the data in the workers.

Instead, we can parallelize the *list of files* and then read all files in parallel directly from the Spark executors.

```
base_path = '/mapd-workspace/datasets/lecture1/file_{}.txt'
file_list = [base_path.format(i) for i in range(1,5)]
```

```
files_rdd = sc.parallelize(file_list)
files_rdd.collect()

['/mapd-workspace/datasets/lecture1/file_1.txt',
   '/mapd-workspace/datasets/lecture1/file_2.txt',
   '/mapd-workspace/datasets/lecture1/file_3.txt',
   '/mapd-workspace/datasets/lecture1/file_4.txt']
```

Note

In this case we could have used the built-in Spark function textFile, which takes as input the path to the files and reads them directly into an RDD.

To access a file with this function we need to prepend file:// if the file is in the local file system. If the file is in Hadoop the path will be similar to hdfs://namenode.com:8020/path_to_the_file. In the same way, if the file is stored on object stores using the s3 API (such as the one used in CloudVeneto) the path will be s3://.

The Spark function textFile could be used in this case as the input files are stored in a plain text.txt format. In many other cases, however, a custom data loader is required instead, as the data will be stored in a specific format, impossible for Spark to interpret without some instructions. On the other hand, we should try to use the built-in data readout functions as much as possible since they are much more performant than our custom Python code.

```
text_rdd = sc.textFile("file://"+base_path.format('*'))
text_rdd.collect()[:4]
```

In this example we will write a custom data loader, that could be generalized to all kinds of files and data formats.

Starting from the RDD files, write a map function that converts data into an RDD, data_rdd, where each element is a tuple (t, val).

During this preprocessing phase remember to remove points with **None** as their measured value.

The elements of data rdd should finally be something like:

```
[(0.0,9.93), (-1.0,9.02), ...]
```

In order to do this, we can use regular expressions (or regex).

A regular expression is a sequence of characters that allows to identify and select a **pattern** in a string, instead of a specific substring. Most editors (including Jupyter) allow to use of regex to find and replace text based on patterns, and several interesting sites offer a simple interface to learn and experiment with regexp, e.g. https://regex101.com/

All following characters are considered "meta-characters" in regex

```
. ^ $ * + ? { } [ ] \ | ( )
```

In a regular expression, all these symbols will be **not** interpreted as their characters but are used to build up the patterns and search for matches in the text.

The main notable examples are:

[] square brackets meaning exactly 1 character

regexp	interpretation
[a]	the letter a
[ax]	the letter a or x
[a-x]	any letter from a to x
[a-zA-F]	any letter from a to z and from A to F
[0-9]	any number from 0 to 9
^ represents a not	
regexp	interpretation
[^b02]	all charachters but b,0and 2
. represents any character at all	
regexp	interpretation
	all charachters
? makes the preceding character in the regular expression optional	
regexp	interpretation
colou?r	color or colour
st match the preceding character (or combination) zero or more times	
regexp	interpretation
go*gle	ggle,gogle,google,

\t matches a tab

\n matches a new-line

^ (outside of []) matches the start of a line

\$ matches the end of a line

Regex can be used in plain Python with the re module.

Let's use the re module to implement the appropriate regular expression to clean up our data.

We should find all float values possibly starting with a +/- sign and collecting them in pairs.

test the regex pattern with a fake measurement
import re

```
fake meas = 'Measure 0: (.05, 0.70)'
float pattern = '-?[0-9]*\.[0-9]*'
test = re.findall(f'{float pattern},{float pattern}', fake meas)
test
['.05,0.70']
def parse file(file):
    # this function should:
    # 1. open the file and read all lines
        2. apply the regex to extract the values
    # 3. sanify the data by removing all measurement pairs with non-
numerical values
    # 4. create a `points` list where each entry is a tuple of the
two values/coordinates
    points = []
    with open(file, 'r') as fin:
        # load lines
        lines = fin.readlines()
    for line in lines:
        # extract points
        float pattern = '-?[0-9]*\.[0-9]*'
        coordinates = re.findall(f'{float pattern},{float pattern}',
line)
        # check if we have numerical coodinates
        if len(coordinates)!=0:
            coordinates = coordinates[0].split(',')
            # append entries as tuples
            points.append(
                (float(coordinates[0]), float(coordinates[1]))
    # ---
    return points
data rdd = files rdd.flatMap(lambda file: parse file(file))
data rdd.collect()[:10]
[(-10.0, 0.7),
 (-9.95, 0.61),
 (-9.9, 0.47),
 (-9.8, 0.58),
 (-9.75, 0.29),
 (-9.7, 0.35),
 (-9.65, 0.25),
```

```
(-9.6, 0.39),
(-9.55, 0.52),
(-9.5, 0.68)]
```

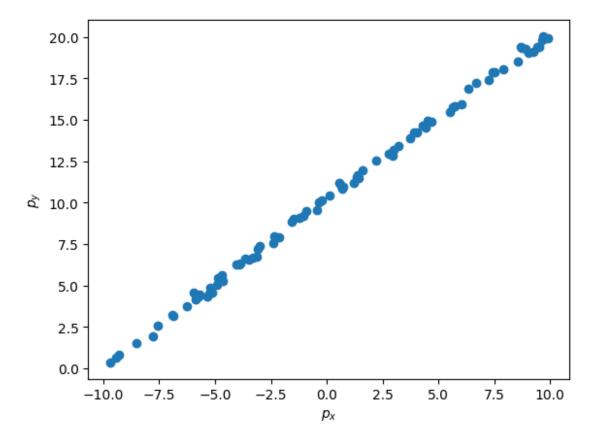
With sample (with_replacement, fraction) we can sample some points from the original RDD.

This is useful if we want to collect only a given **fraction** of our data, without dumping the entire dataset with a collect.

```
import matplotlib.pyplot as plt
import numpy as np

# collect a sub-sample of your data
data = np.array(data_rdd.sample(False,0.2).collect())

plt.scatter(data[:,0], data[:,1]);
plt.xlabel(r'$p_x$');
plt.ylabel(r'$p_y$');
```



We will now implement a distributed gradient descent and use it to find the best parameters for a linear model.

Given an input X the output of the model is

$$Y = W X = w_0 + w_1 x_1 + ... + w_p x_p$$

In our case, we have Y = y(w,x), $W = [w_0, w_1]$ and $X = [1, x]^T$, in other words

$$y(w,x)=w_0+w_1x$$

We are interested in estimating the optimal parameters w^* of the line fitting our data.

To do this we will use **gradient descent**, an iterative procedure that allows us to find a local minumum of a differentiable function.

In our case, we would like to minimize the square residuals, i.e.

$$J(W, X) = \frac{1}{2n} \sum_{i=1}^{n} [Y(W, X) - y_i]^2 = \frac{1}{2n} \sum_{i=1}^{n} [(w_0 + w_1 x) - y_i]^2$$

where y_i is the true value.

In each step of the gradient descent we use the following update rule

$$W_{i+1} = W_i - \gamma \nabla J_W(W_i, X)$$

where y is the learning rate, a variable used to reduce the size of each step.

In other words, we are moving in the opposite direction of the gradient, i.e. towards the minimum of the function.

Recalling that $W = [w_0, w_1]$ and X = [1, x] we have that each component of the gradient, i.e. $\pi = \{v_0, w_1\}$ we have that each component of the gradient, i.e. $\pi = \{v_0, w_1\}$ we have that each component of the gradient, i.e. $\pi = \{v_0, w_1\}$ we have that each component of the gradient, i.e. $\pi = \{v_0, w_1\}$ we have that each component of the gradient, i.e. $\pi = \{v_0, w_1\}$ we have that each component of the gradient, i.e. $\pi = \{v_0, w_1\}$ we have that each component of the gradient, i.e. $\pi = \{v_0, w_1\}$ we have that each component of the gradient, i.e. $\pi = \{v_0, w_1\}$ we have that each component of the gradient, i.e. $\pi = \{v_0, w_1\}$ we have that each component of the gradient, i.e. $\pi = \{v_0, w_1\}$ we have $\pi = \{v_0, w_1\}$ where $\pi = \{v_0, w_1\}$ and $\pi = \{v_0, w_1\}$ where $\pi = \{v_0, w_1\}$ and $\pi = \{v_0, w_1\}$ where $\pi = \{v_0, w_1\}$ and $\pi = \{v_0, w_1\}$ where $\pi = \{v_0, w_1\}$ and $\pi = \{v_0, w_1\}$ and $\pi = \{v_0, w_1\}$ and $\pi = \{v_0, w_1\}$ where $\pi = \{v_0, w_1\}$ and $\pi = \{v_0, w_1\}$ where $\pi = \{v_0, w_1\}$ and $\pi = \{v_0, w_1\}$ an

$$\nabla J(W,X) = \left[\frac{1}{n}\sum_{i=1}^{n} \left[Y(W,X) - y_i\right] \cdot 1, \frac{1}{n}\sum_{i=1}^{n} \left[Y(W,X) - y_i\right] \cdot x_i\right]$$

We can now write a map-reduce job used to estimate the parameters using gradient descent on the full dataset.

We start by defining the weights vector and initializing it to some values, e.g. (10,0.5) is a good guess...

```
# use numpy to create the W weight array
W = np.array([7.5, 0.9])
```

Implement then the functions computing the prediction given as input \boldsymbol{x} and the current weights \boldsymbol{W}

```
# predict y for any given x and weights W
def predict(x, W):
    # return prediction
    return W[0] + W[1]*x
# ---
```

```
# test the function in local
assert predict(1, [10,1]) == 11
# ---
```

Implement the function computing the gradient for one example, given as inputs:

- 1. the point P=(x, y), and
- 2. the current set of weights W.

Remember that the gradient has two components, one per parameter.

Furthermore, the normalization $\frac{1}{n}$ can be omitted since we can apply it afterward, having summed the gradients of all examples.

```
# compute the gradient
def gradient(P, W):
    # return the prediction given the x value of P and the weights W

# and compute gradient
pred = predict(P[0], W)
gradient = np.dot(pred-P[1], [1,P[0]])
# ---

return gradient

# test the function in local
assert not (gradient((1,11), [10,1])).all()
# ---
```

We are now ready to implement the gradient descent and find the optimal line parameters.

Hint: compute the gradient for each point in parallel, and then sum all of them. Finally, use this sum to update the weights vector.

```
# count points based on the partitioned data
num_points = data_rdd.count()

# re-declare the weight vector here:
# this is useful if the cell is run multiple times
W = np.array([10,0.5])

# define the learning rate
lr = 0.01

# define the number of iterations
num_it = 20
```

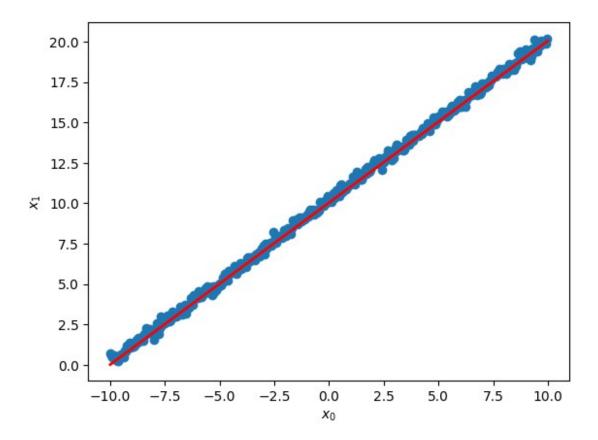
```
for i in range(num_it):
    # run the gradient descent in parallel and then sum the gradients
    grad = data_rdd.map(lambda P: gradient(P,W)).reduce(lambda g1,g2:
g1+g2)
    # ---

# update the weights according to the learning rate and the
gradient
    W = W - (lr/num_points)*grad
    # ---

# print the results
print("Final parameters: x0={:.2f}, x1={:.2f}".format(W[0], W[1]))
Final parameters: x0=10.03, x1=1.00
```

Check out the results by plotting the data points and the resulting best fit line.

```
data = np.array(data_rdd.collect())
plt.scatter(data[:,0], data[:,1]);
x = np.arange(-10,11)
y = W[0] + W[1]*x
plt.plot(x, y, color='red', lw=2);
plt.xlabel(r'$x_{0}$');
plt.ylabel(r'$x_{1}$');
```

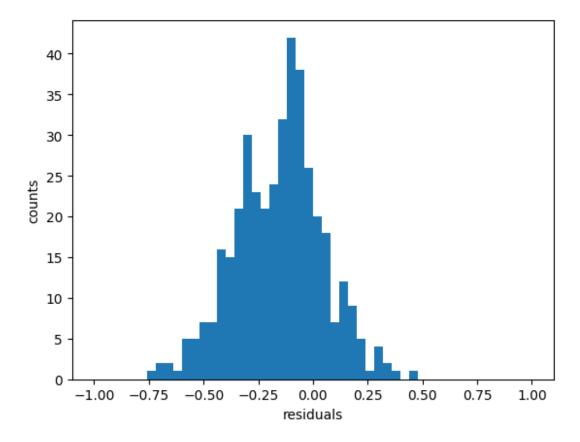


Finish up by computing the residuals using Spark, and plot their distribution in a histogram.

The residual of the point (x_i, y_i) with respect to the model y(x) is simply defined as

$$R_i = y(x_i) - y_i$$

```
# compute the residuals
residuals_rdd = data_rdd.map(lambda x: predict(x[0], W) - x[1])
# plot its distribution
plt.hist(residuals_rdd.collect(), range=(-1,1), bins=50);
plt.xlabel("residuals");
plt.ylabel("counts");
```



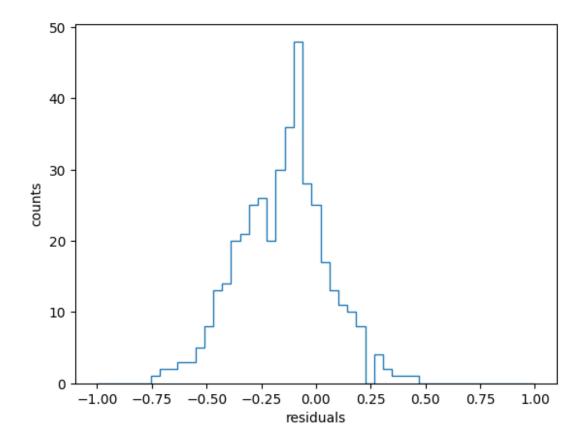
Note

By running the previous cell we asked Spark to return the entire residual RDD object. This is not a sizeable dataset in this specific example, but it might be the case in a real-life scenario, where you may have lots of records stored in a distributed cluster. Returning the entire dataset just to produce a histogram is extremely inconvenient, as it implies large data transfers from the executors to the driver, and finally to the client (possibly resulting in getting out of the driver's memory).

What you should be doing instead is to evaluate the histogram remotely and in parallel, and return the histogram as a set of bins and counts. This way the data transfer from the executors to the driver is minimized, avoiding possible issues.

You should be able to write a Map-Reduce function to create a histogram (consider this an **Extra-exercise**), but Spark is also providing some built-in functions to compute simple histograms remotely.

```
# use the spark RDD histogram method to return the histogram from the
cluster
hist = residuals_rdd.histogram(np.linspace(-1,1,50).tolist())
plt.stairs(hist[1], hist[0]);
plt.xlabel("residuals");
plt.ylabel("counts");
```



Caching

From the WebUI we can see that in each iteration Spark is computing every operation from the very beginning, i.e. starting from reading the list of filenames and running the parallelization of the text files!. This would not be really necessary, as this first operation should not need to be re-executed every time we need to access the dataset.

With persist () we can instruct Spark to put intermediate results into the executors' memory, e.g. after the function parsing the files.

In this way, the same dataset will be loaded in the next iterations much faster, at the cost of having the dataset stored in memory.

Note-1: to be precise, there could be different levels of persistence of data into the executors' memory.

Note-2: one should be very careful not to *abuse* the caching of datasets. Caching itself takes time and resources, and caching all intermediate stages of your dataset might end up taking a toll on the performance (and saturating the available memory of the executors).

```
# persist the original RDD
data_rdd = data_rdd.persist()

# persist is a transformation, it will be triggered
# only once we apply an action on the RDD!
```

```
# run the same code as previously
# and have a look at the spark application webUI
# under the Storage tab
num_points = data_rdd.count()

W = np.array([10,0.5])

lr = 0.01
num_it = 20

for i in range(num_it):
    grad = data_rdd.map(lambda P: gradient(P,W)).reduce(lambda g1,g2:g1+g2)
    W = W - (lr/num_points)*grad

print("Final parameters: x0={:.2f}, x1={:.2f}".format(W[0], W[1]))

Final parameters: x0=10.03, x1=1.00
```

The RDD can (actually, **should**) be removed from memory with **unpersist()**, freeing up the executors' memory when needed.

```
# free up the memory
data_rdd = data_rdd.unpersist()
```

Stop worker and master

```
# stop the running Spark context
sc.stop()
# stop the running Spark session
spark.stop()
```

Finally, use docker compose down to stop and clear all running containers.