

# Random Stuff

$$\log(x) := \ln(x) := E^{-1}(x) \quad (x \in (0, \infty))$$

$$\log(1) = 0, \quad \log(e) = 1$$

$$\log(xy) = \log(x) + \log(y)$$

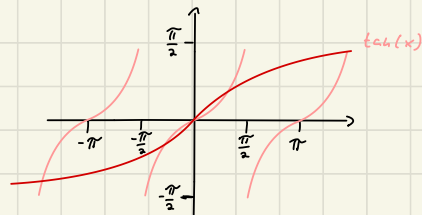
$$\log\left(\frac{x}{y}\right) = \log(x) - \log(y)$$

$$\log_a(x) = \frac{\log_b(x)}{\log_b(a)}$$

$$\log(x^m) = m \cdot \log(x)$$

$$\tanh(x) := \frac{\sinh(x)}{\cosh(x)}$$

$$\operatorname{arctan}(x) := \tan^{-1}(x)$$

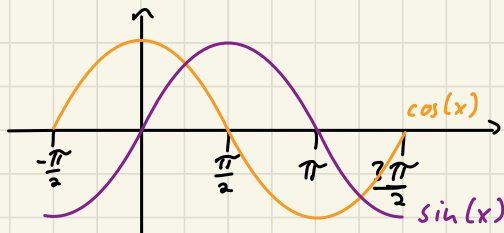


$$a^x = e^{x \cdot \log(a)}$$

$$a^{x+y} = a^x \cdot a^y$$

$$\log(a^x) = \log(e^{x \cdot \log(a)}) = x \cdot \log(a)$$

$$(a^x)^y = a^{x \cdot y}$$



$$\sin\left(x + \frac{\pi}{2}\right) = \cos(x)$$

$$\sin(x + \pi) = -\sin(x) \quad \cos(x + \pi) = -\cos(x)$$

$$\sin(x + 2\pi) = \sin(x) \quad \cos(x + 2\pi) = \cos(x)$$

## geometrische Summenformel

$$\sum_{k=0}^n z^k = \frac{1 - z^{n+1}}{1 - z} \quad (z \in \mathbb{C}, z \neq 1)$$

$$(\sin(x))' = \cos(x)$$

$$(\cos(x))' = -\sin(x)$$

$$(\tanh(x))' = \frac{1}{\cosh^2(x)}$$

$$(\operatorname{arctan}(x))' = \frac{1}{1+x^2}$$