

Cost analysis of the algorithm (c_2 → problem_1.py)

```
def knapsackProblem(itemValues, itemWeights, maxCapacity):
    n = len(itemValues)                                     #c1=1
    dpTable = [[0 for _ in range(maxCapacity+1)] for _ in range(n+1)]
    #c2=n.m

    for i in range(1, n+1):                                 #c3=n
        for capacity in range(1, maxCapacity+1):           #c4=n.m
            dpTable[i][capacity] = dpTable[i-1][capacity] #c5=n.m

            if itemWeights[i-1] <= capacity:                #c6=n.m
                items = itemValues[i-1] + dpTable[i-1][capacity -
itemWeights[i-1]]                                         #c7=n.m
                if items > dpTable[i][capacity]:           #c8=n.m
                    dpTable[i][capacity] = items          #c9=n.m

    maxValue = dpTable[n][maxCapacity]                     #c10=1
    selectedItems = []                                     #c11=1
    capacity = maxCapacity                                 #c12=1

    for i in range(n, 0, -1):                               #c13=n
        if dpTable[i][capacity] != dpTable[i-1][capacity]: #c14=n
            selectedItems.append(i-1)                     #c15=n
            capacity = capacity - itemWeights[i-1]         #c16=n

    selectedItems.reverse()                                 #c17=n
    return maxValue, selectedItems                         #c18=1
```

- Basic operation:

$$c_4, c_5, c_6, c_7, c_8, c_9 = n.m$$

- Time complexity calculation:

$$T(n) = (c_4 + c_5 + c_6 + c_7 + c_8 + c_9) \cdot (n.m)$$

$$T(n) = 6(n.m)$$

$$T(n) = n.m$$

$$T(n) \in O(n.m)$$

- Solving the recurrence:

$$T(n) = T(n-1) + 6m, \quad n \geq 1, \quad T(0) = 0$$

$$T(1) = T(1-1) + 6m = T(0) + 6m = 0 + 6m = 6m$$

$$T(2) = T(2-1) + 6m = T(1) + 6m = 6m + 6m = 12m$$

$$T(3) = T(3 - 1) + 6m = T(2) + 6m = 12m + 6m = 18m$$

$$T(4) = T(4 - 1) + 6m = T(3) + 6m = 18m + 6m = 24m$$

$$T(n) = \sum_{i=1}^n 6.m$$