

## Exam in Learning Systems (DVA427)

Date 2019-03-28  
Time 8:10 – 11:30  
Allowed material No  
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**Good Luck!!!**

### 1. Decision Tree Learning (6+2p)

Construct the decision tree for the set of training instances in the left table with attributes  $x_1$ ,  $x_2$  and classes A, B.

- 1) Which attribute should be used at the root node and why?
- 2) Show how the examples  $D_1, \dots, D_6$  are sorted down the tree and how they are classified.

Use the right table to look up the entropy for a subset of training instances. Take the entry that is closest to the decimal number for which you want to calculate the entropy (e.g. if you need to calculate the entropy of 0.33, take the entry for 0.3 in the table which is 0.9). It is sufficient to make approximate calculations rounded to one digit behind the decimal.

#### Training examples

No.	$x_1$	$x_2$	$c(x_1, x_2)$
$D_1$	T	T	A
$D_2$	F	F	B
$D_3$	T	F	A
$D_4$	F	F	B
$D_5$	T	F	A
$D_6$	F	T	A

p	entropy(p)
0.0	0.0
0.1	0.5
0.2	0.7
0.3	0.9
0.4	1.0
0.5	1.0
0.6	1.0
0.7	0.9
0.8	0.7
0.9	0.5
1.0	0.0

### 2. Artificial Neural Network (4+2p)

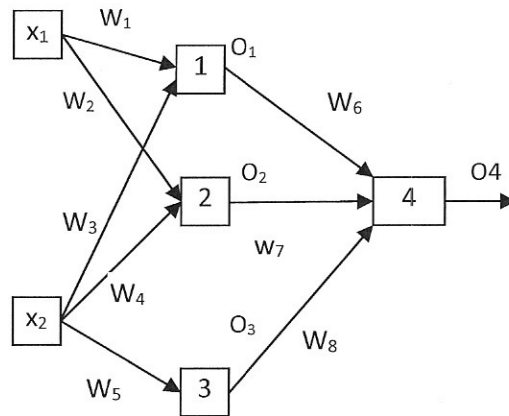
Consider a neural network shown in the following figure. The outputs from the four units are given by

$$O_1 = \text{sigmoid}(w_1x_1 + w_3x_2 + c_1)$$

$$O_2 = \text{sigmoid}(w_2x_1 + w_4x_2 + c_2)$$

$$O_3 = \text{sigmoid}(w_5x_2 + c_3)$$

$$O_4 = \text{sigmoid}(w_6O_1 + w_7O_2 + w_8O_3 + c_4)$$



Now you are given a training example  $(x_{10}, x_{20}, t_0)$ . Suppose that, under this training example, the outputs of the four units are  $O_{10}$ ,  $O_{20}$ ,  $O_{30}$  and  $O_{40}$  respectively, and the current values for weights  $W_6$ ,  $W_7$  and  $W_8$  are  $W_{60}$ ,  $W_{70}$  and  $W_{80}$  respectively. The learning rate is  $\gamma$ .

- 1) Please write out the formulas to calculate  $\Delta W_7$  and  $\Delta W_4$  in terms of the incremental BP algorithm.
- 2) Let  $E = \frac{1}{2} (t_0 - O_{40})^2$ , what are  $\frac{\partial E}{\partial w_1}$  and  $\frac{\partial E}{\partial c_1}$ ?

### 3. Genetic Algorithms (2+2+2+2p)

1) Suppose a population has five individuals whose fitness values are illustrated in the table as follows

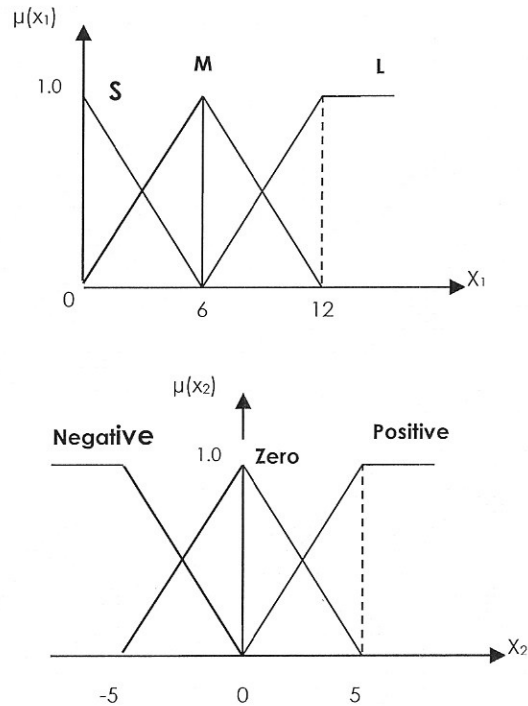
Individual	Fitness
1	12
2	5
3	8
4	15
5	10

What are the probabilities of selection for these individuals?

- 2) Now you need to select an individual from the population based on these selection probabilities. For this purpose a uniform random number from  $[0, 1]$  is created. Suppose this created number is equal to 0.7, which individual in the population will be selected according to the roulette wheel scheme and why?
- 3) What is the risk if a genetic algorithm has no mutation?
- 4) What is the difference between mutations for real-coded string and binary string?

### 4. Fuzzy systems and learning (4+2+1+1p)

Suppose a fuzzy classification system with two inputs  $x_1$  and  $x_2$ . The fuzzy subsets  $S$ ,  $M$ , and  $L$  correspond to input  $x_1$ , and fuzzy subsets *Negative*, *Zero*, and *Positive* correspond to input  $x_2$ . The fuzzy set membership functions of the inputs are depicted in the figures below.



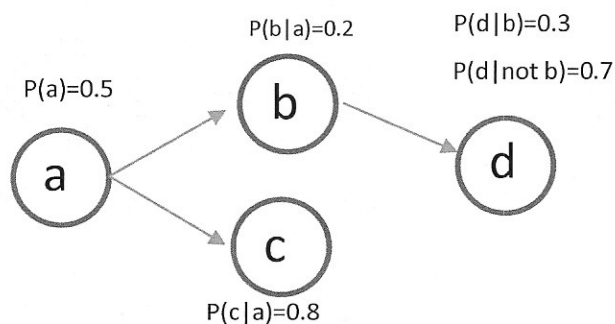
Now suppose that there are four training examples as follows:

$x_1$	$x_2$	Class
8	-2	B
2	-4	B
6	1	C
13	5	A

- 1) Please generate a fuzzy rule set from the above training examples using the Wang-Mendel algorithm.
- 2) What are firing strengths of the generated fuzzy rules given the input situation  $x_1=10$ ,  $x_2=3$ ?
- 3) What are the output fuzzy sets suggested by the generated fuzzy rules in the current situation with  $x_1=10$ ,  $x_2=3$ ?
- 4) How can you make final decision in terms of these fuzzy rules in the current situation with  $x_1=10$ ,  $x_2=3$ ?

## 5. Bayesian Networks (4p)

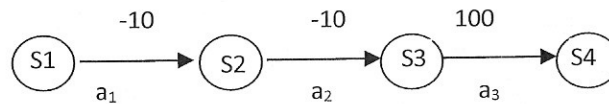
Given a Bayesian Network as follows:



What is the probability of  $d$  to be true when  $a$  is true?

6. Reinforcement learning without model (3+3p)

Given a sequence of the agent's interaction with the environment as shown in the figure as follows, where rewards are indicated above the arrows and actions are indicated below the arrows, and S4 is the terminate state.



Let  $Q$  be the estimate of the optimal action values  $Q^*$ . Assume that the current  $Q$  estimates for all actions at states S1, S2 and S3 are zero.

So far the numbers of visits for the state-actions pairs  $(S1, a_1)$ ,  $(S2, a_2)$ , and  $(S3, a_3)$  are  $N_1=2$ ,  $N_2=5$ , and  $N_3=10$  respectively. The discounting factor is 0.8.

- 1) How can you update the  $Q$  estimates using the  $Q$ -learning rule if the environment is deterministic?
- 2) How can you update the  $Q$  estimates using the  $Q$ -learning rule if the environment is stochastic?