

Analytical Geometry First Semester 2023-2024 Date: 18/1/2024

Answer The following questions:

Q1: Choose the correct answer: [1.5 Marks for a point]

1.	If the value of eccentri	icity $e = 0$, then what is th	e name of the conic?		
	A. ellipse	B. parabola	C. hyperbola	D. none	
2.	If the distance from a	point to the focus is 3 unit	ts and the distance from the	directrix is 3 units, then the	
	conic section called				
	A. ellipse	B. parabola	C. circle	D. hyperbola	
3. The equation of the line whose intercepts on the x and y axes are respectively 5 and -3 is					
	A. $3x + 5y + 15$	B. $3x + 5y - 15$	C. $3x - 5y + 15$	D. $3x - 5y - 15$	
4.	The midpoint of two	points (7,1) and (-1,5)			
	A. (3,3)	B. (4,-2)	C. (-4,2)	D. None	
5. Slope of the segment between two points (7,1) and (-1,5)					
	A2	B2/3	C3/2	D1/2	
6.	If $p = 5$, $\omega = \pi/6$, th	en equation of normal fo	rm of straight line		
	A. $x + \sqrt{3} y - 10 = 0$	B. $\sqrt{3} x + y + 10 = 0$	C. $\sqrt{3} x + y - 10 = 0$	D. $x + \sqrt{3} y + 10 = 0$	
7. The distance from the line $8x+15y - 24 = 0$ to point $(-2,-3)$					
	A. 4	B. 5	C. 8	D. 1/5	
8. If $A x^2 + B xy + C y^2 = 0$ represents equation of two straight lines, then the angle between two lines					
	A. $\pm \frac{2\sqrt{B^2 - AC}}{A + C}$	B. $\pm \frac{2\sqrt{A^2 - AB}}{B + C}$	$C. \pm \frac{\sqrt{B^2 - AC}}{A + C}$	D. $\pm \frac{\sqrt{A^2 - AB}}{B + C}$	
9.	Equation $x^2 + 2hxy$	$+by^2 + 2gx + 2fy + c =$	= 0, represents two straigh	t lines if	
		В.	C.	D.	
	$\begin{vmatrix} a & b & c \\ b & h & f \\ c & f & g \end{vmatrix} = 0$	$\begin{vmatrix} a & g & h \\ g & b & f \\ h & f & c \end{vmatrix} = 0$	$\begin{vmatrix} a & f & g \\ f & b & h \\ g & h & c \end{vmatrix} = 0$	$\begin{vmatrix} a & h & g \\ h & b & f \\ g & f & c \end{vmatrix} = 0$	
10). The formulas for the r	otation of the axes through	n an angle θ are		
A.	$x = x' \cos \theta - y' \sin \theta$	B. $x = x' \cos \theta + y' \sin \theta$	C. $x = x' \cos \theta + y' \sin \theta$	D. $x = x' \cos \theta - y' \sin \theta$	
	$y = x' \sin \theta + y' \cos \theta$	$y = x' \sin \theta + y' \cos \theta$	$y = x' \sin \theta - y' \cos \theta$	$y = x' \sin \theta - y' \cos \theta$	

11. The center of circle $2x^2 + 2y^2 - Ax - By + C = 0$ is

D.
$$(A/2, B/2)$$

The radius in the previous circle is

A.
$$r = \sqrt{\frac{A^2}{4} + \frac{B^2}{4} - C}$$
 B. $r = \sqrt{\frac{A^2}{2} - \frac{B^2}{2} + C}$ C. $r = \sqrt{\frac{A^2}{16} + \frac{B^2}{16} - C}$ D. $r = \sqrt{A^2 + B^2 - C}$

13. The vertices in conic section $9x^2 - 16y^2 = 144$ are

Δ	(0,	$\pm 4)$
\neg .	(υ,	ユエノ

B.
$$(\pm 3,0)$$

C.
$$(\pm 4.0)$$

D.
$$(0, \pm 3)$$

14. In the previous conic section

A.
$$e = \frac{5}{4}$$

A.
$$e = \frac{5}{4}$$
 B. $e = \frac{4}{5}$

C.
$$e = \frac{3}{4}$$

D.
$$e = \frac{4}{3}$$

15. Then, two foci are

A.
$$(\pm 5,0)$$

B.
$$(0, \pm 5)$$

C.
$$(\pm 16/5,0)$$

D.
$$(0, \pm 16/3)$$

16. And two directrixes equations are:

A.
$$x = \pm \frac{16}{5}$$
 B. $x = \pm \frac{5}{16}$

B.
$$x = \pm \frac{5}{16}$$

c.
$$y = \pm 5$$

D.
$$y = \pm \frac{16}{5}$$

17. And equation of two Asymmptites equations are......

A.
$$x = \pm \frac{3}{4}$$

B.
$$y = \pm \frac{3}{4} x$$

C.
$$y = \pm \frac{4}{3} x$$

D.
$$y = \pm \frac{3}{4}$$

18. The parabola $(x + 3)^2 = -16(y - 5)$

A. Symmetrical about x – axis and opens to left B. Symmetrical about y – axis and opens downward

C. Symmetrical about x – axis and opens to right D. Symmetrical about y – axis and opens upward

19. The equation of a parabola having the origin as its vertex and focus (-4/3,0) is:

A.
$$x^2 = -\frac{4}{3}y$$

B.
$$y^2 = -\frac{16}{3}x$$
 C. $y^2 = +\frac{16}{3}x$ D. $x^2 = +\frac{4}{3}y$

C.
$$y^2 = +\frac{16}{3}x$$

D.
$$x^2 = +\frac{4}{3}y$$

20. The equation $4x^2 + 9y^2 - 48x + 72y + 144 = 0$ represents a....

A. circle

B. parabola

C. hyperbola

D. ellipse

21. The center of the previous question is

22. An ellipse having foci at (0,1) and (4,1), then the center is

C.
$$(2,1)$$

23. If the eccentricity e = 0, then the conic section is......

A. ellipse

B. parabola

C. hyperbola

D. none

24. Equation of circle with diameter points A = (5,-1), B = (-3,7)

A.
$$(x+1)^2 +$$

B.
$$(x-1)^2 +$$

B.
$$(x-1)^2 +$$
 C. $(x+1)^2 +$

D.
$$(x-1)^2 +$$

$$(y+3)^2 = 25$$

$$(y-3)^2=25$$

$$(y+3)^2 = 32$$

$$(y-3)^2 = 32$$

Q2 [14 marks]: Prove that the equation of parabola whose vertex is at the origin symmetrical about x axis is $y^2 = 4 a x$ and the focal width = |4a|.

Q3 [10 marks]: Find the length of tangent of circle $x^2 + y^2 + 2fx + 2gy + c = 0$ drown from a point (x_1, y_1) .

Q4 [10 marks]: Determine the equation of the curve $2x^2 + 3y^2 - 8x + 6y = 7$ when the origin is translated to the point (2,-1). (explain the new curve).

With best wishes

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