

## « Applications of integration »

$$F'(x) = m$$

$$y = x^2 + 3 \quad \therefore y' = 2x$$

$$y_1 = x^2 - \pi \quad \therefore y_1' = 2x$$

$$* \int 2x \, dx = x^2 + C \rightarrow \text{عائلة المنحنيات}$$

$x = s$  distance

$v$  velocity

$f = a$  acceleration

مشتقها

مشتقها

بالنسبة لـ  $t$

$$v = \frac{ds}{dt}$$

$$a = f = \frac{dv}{dt} = \frac{d^2s}{dt^2}$$

$$\text{Ex}_1] M = -2x$$

$$\frac{dy}{dx} = \frac{df(x)}{dx} = -2x$$

$$y = f(x) = -2 \int x \, dx = -x^2 + C$$

$$\text{at } [1, 1] \quad 1 = -1 + C \quad \therefore C = 2$$

$$y = -x^2 + C \Rightarrow y = -x^2 + 2$$

$$\text{Ex}_2] M = 4x, (1, 5)$$

$$\frac{dy}{dx} = \frac{df(x)}{dx} = 4x$$

$$y = f(x) = 4 \int x \, dx = 2x^2 + C$$

at (1, 5)

$$5 = 2 \times 1 + C \quad \therefore C = 3 \Rightarrow y = 2x^2 + 3$$



$$Ex_3] m = \sqrt{x}, (9, 18)$$

$$\frac{dy}{dx} = \frac{df(x)}{dx} = \sqrt{x}$$

$$y = f(x) = \int \sqrt{x} dx = \int x^{\frac{1}{2}} dx = \frac{2}{3} x^{\frac{3}{2}} + C$$

at (9, 18)

$$18 = \frac{2}{3} \times 9^{\frac{3}{2}} + C \Rightarrow C = 0 \Rightarrow y = \frac{2}{3} x^{\frac{3}{2}}$$

$$Ex_4] m = \frac{x}{y}, (4, 2)$$

$$\frac{dy}{dx} = \frac{df(x)}{dx} = \frac{x}{y}$$

$$y dy = x dx \quad \text{« يتكامل الطرفين »}$$

$$\int y dy = \int x dx + C$$

$$\frac{y^2}{2} = \frac{x^2}{2} + C$$

at (4, 2)

$$\frac{4}{2} = \frac{16}{2} + C \Rightarrow C = -6 \Rightarrow y^2 = x^2 - 12 \quad \text{[مربعين 2]}$$

$$Ex_5] m = \frac{x}{1+x^2}, (3, 5)$$

$$\frac{dx}{dx} = \frac{df(x)}{dx} = \frac{x}{1+x^2}$$

$$y = f(x) = \int \frac{x}{1+x^2} dx = \frac{1}{2} \int \frac{2x}{1+x^2} dx$$

$$y = \frac{1}{2} \ln |1+x^2| + C \quad \text{at (3, 5)} \quad 5 = \frac{1}{2} \ln |1+3^2| + C \Rightarrow C = \frac{\ln 10}{2}$$

$$\therefore y = \frac{1}{2} \ln |1+x^2| + 5 - \frac{1}{2} \ln 10$$



Partical moves along ----  $(0,0)$   $t=0$

$$V = 4t, (0,4)$$

$$V = 6T + 3, (1,3)$$

$$V = 3T^2 + 2T, (2,4)$$

$$V = \sqrt{T} + 5, (4,9)$$