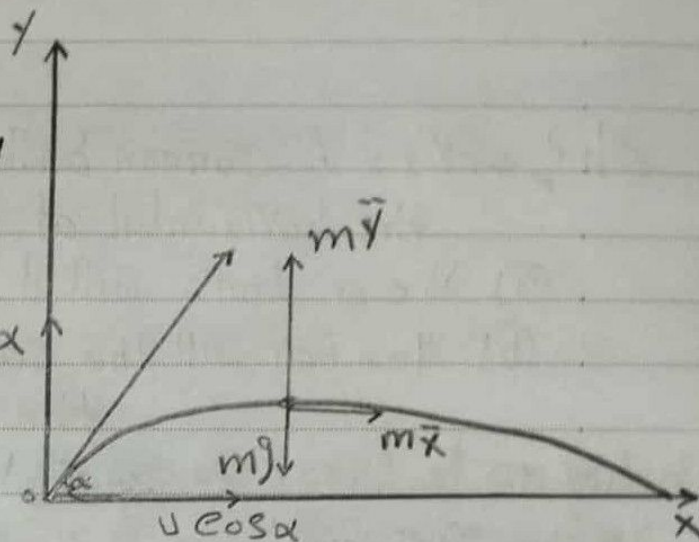


« Projectile motion » [حركة المقذوفات]

$u \Rightarrow$ initial velocity
 $\alpha \Rightarrow$ direction of initial velocity
above the horizontal ox .

!! مقاومة الهواء معدومة
Zero =



$$m \ddot{x} = 0 \quad (1)$$

$$m \ddot{y} = -mg \quad (2)$$

From equation (1) we find that

$$\frac{d\dot{x}}{dt} = 0 \Rightarrow \dot{x} = \text{const} = u \cos \alpha \quad (3)$$

From equation (2) we find that

$$\frac{d\dot{y}}{dt} = -g$$

$$\dot{y} = u \sin \alpha - gt$$

$$x = ut \cos \alpha^*$$

$$y = ut \sin \alpha - \frac{1}{2} gt^2^*$$

$$\text{Flight time} \Rightarrow t = \left(\frac{2u}{g} \right) \sin \alpha$$

$$\{g = 9.8 = 980\}$$

$$\text{Horizontal Range} \Rightarrow R = u \left(\frac{2u}{g} \sin \alpha \right) \cos \alpha$$

$$= \frac{u^2}{g} \sin 2\alpha$$

$$R_{\max} = u^2/g$$

Maximum Height $\Rightarrow h = y_{\max} = \frac{u^2}{2g} \sin^2 \alpha$

$t_h = \left(\frac{u}{g}\right) \sin \alpha$ * زمن الطيران = $\frac{1}{2}$ زمن أقصى ارتفاع

Ch 4 \Rightarrow Ex 3: A cannon ball is fired at an angle of 30° to the horizontal at a speed of 25 m s^{-1}

(a) How long will it be before the impact?

(b) How far will the cannon ball travel before hitting the ground?

« Solu »

$\Rightarrow u = 25 \text{ m s}^{-1}$

$\Rightarrow \alpha = 30^\circ$

$y = ut \sin \alpha - \frac{1}{2} g t^2 \quad y = 0$

$0 = 25T \sin 30 - \frac{1}{2} g T^2 \quad T(25 \sin 30 - \frac{1}{2} g T) = 0$

$50T = 0 \quad \text{or} \quad T = (50 \sin 30) / g = 50 \sin 30 / 9.8$
 $= 2.55 \text{ s} \quad \#$

$X = uT \cos \alpha$

$R = 25 \times 2.55 \times \cos 30 = 55.231 \text{ m} \quad \#$

Ch 4 \Rightarrow Ex 7: A ball is kicked at an angle of 35° with the ground: (a) what should be the initial velocity of the ball so that it hits a target that is 30 meters away at height of 1.8 meters?

(b) what is the time for the ball to reach the target?

« Solu »

$(x, y) = (b, 1.8)$

$$X = v_0 \cos(35^\circ) t$$

$$30 = v_0 \cos(35^\circ) t$$

$$t = 30 / v_0 \cos(35^\circ)$$

$$y = v_0 \sin \alpha - \frac{1}{2} g t^2$$

$$1.8 = v_0 \sin(35^\circ) (30 / v_0 \cos(35^\circ)) - \frac{1}{2} \times 9.8 (30 / v_0 \cos(35^\circ))^2$$

$$v_0 \cos(35^\circ) = 30 \sqrt{9.8 / (2(30 \tan(35^\circ) - 1.8))}$$

$$v_0 = 18.3 \text{ m/s} \quad \#$$

$$\therefore t = X / v_0 (\cos(35^\circ)) = 30 / 18.3 \cos(35^\circ) = 2.0 \text{ s} \quad \#$$

Ex 8: A ball kicked from ground level at an initial velocity of 60 m/s and an angle θ with ground reaches a horizontal distance of 200 meters.

a) What is the size of angle θ ?

b) What is time of flight of the ball?

« Solu »

$$X = v_0 t \cos \theta$$

$$t = \frac{2 v_0 \sin \theta}{g} \quad \text{[1]}$$

$$\hookrightarrow t = X / v_0 \cos \theta \quad \text{[2]}$$

$$X / v_0 \cos \theta = \frac{2 v_0 \sin \theta}{g}$$

$$200 / v_0 \cos \theta = 2 v_0 \sin \theta / g$$

$$2 v_0^2 \cos \theta \sin \theta = 200 g$$

$$v_0^2 \sin 2\theta = 200 g$$

$$\sin(2\theta) = 200 g / v_0^2 = 200 (9.8) / 60^2$$

$$\theta = 16.5^\circ \quad \#$$

$$\text{time of flight} = 200 / v_0 \cos(16.5^\circ) = 3.48 \text{ s} \quad \#$$

$$ch 4 \Rightarrow Exg: E = \frac{1}{2} m v_x^2 = \frac{1}{2} m [v_0 \cos \alpha]^2$$

$$22 = \frac{1}{2} (0.6) (v_0 \cos(35))^2$$

$$v_0 = (1 / \cos(35)) \sqrt{(44 / 0.6)} = 10.4 \text{ m/s} \quad \#$$

$$E_f - E_i = m g H \Rightarrow$$

$$32.4 - 22 = m g H$$

المسافة الرأسية بين البداية والنهاية

$$\therefore H = 10.4 / (0.6 \times 9.8) = 1.8 \text{ m} \quad \#$$

$$ch 4 \Rightarrow Ex 10: v_x = v_0 \cos \theta = 1000 / 40 = 25 \text{ m/s} \quad \textcircled{1}$$

$$\text{time of flight} = 2 v_0 \sin \theta / g = 40 \text{ s}$$

$$v_0 \sin \theta = 20 \times 9.8 = 196 \quad \textcircled{2}$$

$$\text{From 1, 2} \quad \frac{v_0 \sin \theta}{v_0 \cos \theta} = \frac{196}{25} \quad \tan \theta = 196 / 25$$

$$\therefore \theta = 82.7^\circ \quad v_0 \cos \theta = 25 \text{ m/s}$$

$$v_0 = 25 / \cos(82.7^\circ) = 196.8 \text{ m/s} \approx 197 \text{ m/s} \quad \#$$

طريقة أخرى « ② - ① » \Rightarrow جميع وتربيع $v_0^2 [\cos \theta]^2 + v_0^2 [\sin \theta]^2 = 25^2 + 196^2$

$$v_0^2 [\cos^2 \theta + \sin^2 \theta] = 25^2 + 196^2$$

$$v_0^2 = 39041$$

$$v_0 = 197 \text{ m/s} \quad \#$$

ch 4 \Rightarrow Ex 11:

$$y = -0.025x^2 + 0.5x$$

معادلة المسار

$$y = x \tan \alpha - \frac{g}{2u^2} x^2 \sec^2 \alpha$$

$$\tan \alpha = 0.5 \Rightarrow \alpha = 26.5^\circ \quad \#$$

$$-0.025 = -0.5 (9.8 / [v_0 \cos(26.5^\circ)]^2)$$

$$\therefore v_0 = 15.6 \text{ m/s} \quad \#$$

ch 4 \Rightarrow Ex 12:

$$y = ut \sin \alpha - \frac{1}{2} g t^2$$

$$-3 = -\frac{1}{2} g t^2$$

$$t = \sqrt{3 / \frac{1}{2} \times 9.8}$$

$$= 0.78 \text{ s} \quad \#$$

$$x_A = ut \cos \alpha$$

$$= 10 \times 0.78 = 7.8 \text{ m}$$

$$x_B = v_B t \cos \alpha$$

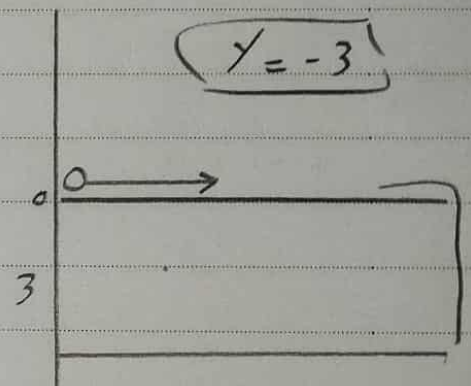
$$= 15 \times 0.78 = 11.7$$

$$|x_B - x_A| = |11.7 - 7.8| = 3.9 \text{ m} \quad \#$$

المسافة بين

الكرة A، الكرة B

B



لأن اتجاه $\alpha = 0^\circ$
تذف الكرة افقى

الكرتان
هيو صلاوا
فبي نفس
النزول
لأن لهم نفس سرعة
الجاذبية الأرضية
ونفس الزمان