

example 7

if the relation between x and t by
 $x = e^{2t} - 2e^{-2t}$ Prove that $v^2 = 4(x^2 + 8)$

$$F = 4x$$

Solution

$$x^2 = e^{4t} + 4e^{-4t} - 4$$

$$v = 2e^{2t} + 4e^{-2t}$$

$$v^2 = 4e^{4t} + 16e^{-4t} + 16$$

$$= 4[e^{4t} + 4e^{-4t} + 4]$$

$$4[e^{4t} + 4e^{-4t} + 8 - 4]$$

$$v^2 = 4[x^2 + 8] \quad \#$$

← اذلي تامل

$$F = [4e^{2t} - 8e^{-2t}]$$

$$= 4[e^{+2t} - 2e^{-2t}]$$

$$F = 4x \quad \#$$

example 3: 11

11, 10, 11

تابع السك 2

مقرر 1 Chapter

Example 8

A large stone is falling through a layer of mud. At time t seconds, the depth of the stone in metres below the surface is given

$$by \ x(t) = 20(1 - e^{-\frac{1}{2}t})$$

Solution

$$x'(t) = \frac{20}{2} e^{-\frac{1}{2}t}$$

$$x''(t) = -5 e^{-\frac{1}{2}t}$$

$$x'(1) = 10 e^{-\frac{1}{2}} \rightarrow \text{Positive}$$

$$x''(1) = -5 e^{-\frac{1}{2}} \rightarrow \text{Negative}$$

السرعة ايجابيا لا سفل فتنقص
ايضا سرعة الحركة
الحركة لا على
السرعة تنزل
السرعة ايجابيا لا على عاكس ايضا سرعة الحركة - العجلة لا سفل
السرعة تقل

$$** \leftarrow e^{-\frac{t}{2}} = e^{-\frac{\infty}{2}} = e^{-\infty} = \frac{1}{e^{\infty}} = \frac{1}{\infty} = 0$$

$$t \rightarrow \infty$$

$$x = 20$$

$$x' = \text{Zero}$$

$$x'' = \text{Zero}$$

example 9

A Particle moves in a straight line
it is initially at rest at the origin the
the acceleration of the Particle is given

$$x''(t) = \frac{1}{3} \cos 3t.$$

solution

$$x'(t) = 3 \times \frac{1}{3} \sin 3t + A$$

$$x(t) = \frac{1}{9} \sin 3t + A$$

من البداية

$$x_0 = v_0 = t_0 = 0$$

$$0 = \frac{1}{9} \sin 0 + A \rightarrow \text{ناتج الصافي}$$

$$v(t) = \frac{1}{9} \sin 3t$$

$$x(t) = -\frac{1}{27} \cos 3t + C \rightarrow \text{ناتج الصافي}$$

$$\therefore C = \frac{1}{27} \quad \#$$

Finished Chapter 1