

ALTERNATING CURRENT «دوائر التيار المتردد (AC)» «CIRCUITS (AC)»

«AC CIRCUITS» دوائر التيار المتردد

* An AC Circuit consists of a combination of circuit elements and a power source.
تتكون دائرة التيار المتردد من مجموعة من عناصر الدائرة ومصدر طاقة.

- The Power Source provide an alternating Voltage, ΔV
- Notation note: $(V(t))$ * يوفّر مصدر الطاقة جهداً متردداً
- Lower Case symbols will indicate instantaneous values
- Capital letters will indicate fixed values.

* The output of an (AC) power source is sinusoidal and varies with time according to the following equation:

يكون خرج مصدر طاقة التيار المتردد جيبيًا ويتغير مع الوقت...

$$\Delta V = \Delta V_{\max} \sin \omega t$$

«الجهد اللحظي» ← «سعة الجهد»

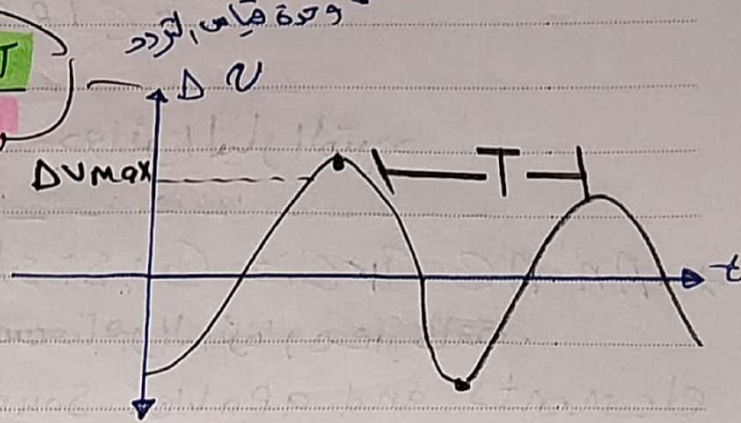
- ΔV is The instantaneous Voltage
- ΔV_{\max} is The maximum output voltage of The Source «أقصى جهد»
- Also Called The Voltage amplitude «سعة الجهد»
- ω is The angular frequency of The (AC) Voltage.

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The angular frequency is:

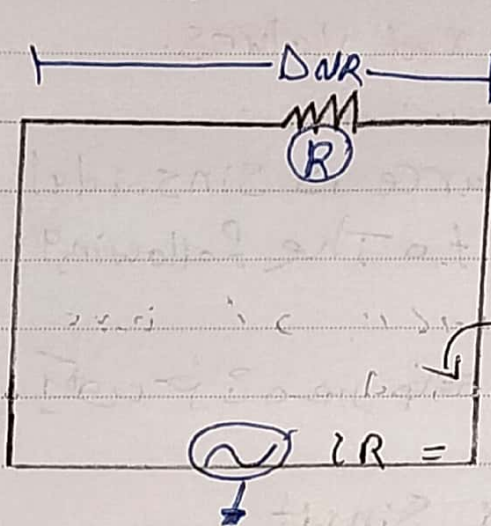
$$f = \frac{1}{T} = \text{Hz}$$

$$\omega = 2\pi f = \frac{2\pi}{T}$$



"RESISTORS IN AN AC CIRCUIT"

APPLY Kirchhoff's loop rule Therefore



قانون كيرشوف

$$\Delta V + \Delta V_R = \text{Zero}$$

$$\Delta V - iR = \text{Zero}$$

قانون كيرشوف عبارة عن
مجموع الجهود في الدائرة
المغلقة = صفر

$$\Delta V_{\max} \sin(\omega t) - iR = \text{Zero}$$

$$iR = \frac{\Delta V_{\max} \sin \omega t}{R} = I_{\max} \sin(\omega t)$$

$$\Delta V = \Delta V_{\max} \sin \omega t \quad \text{where } \therefore I_{\max} = \frac{\Delta V_{\max}}{R}$$

$$\Delta V_R = I_{\max} \sin \omega t \cdot R$$

"RMS CURRENT AND VOLTAGE"

The average current in one cycle is zero

- Resistors experience a temperature increase which depends on the magnitude of the current, but not the direction of the current

$$I_{rms} = \frac{I_{max}}{\sqrt{2}} = 0.707 I_{max}$$

- Alternating voltages can also be discussed in terms of RMS values

$$V_{rms} = \frac{V_{max}}{\sqrt{2}} = 0.707 V_{max}$$

"POWER"

- The rate at which electrical energy is delivered to a resistor in the circuit is given by

$$P = I^2 R$$

- The average power delivered to a resistor that carries an alternating current is

$$P_{av} = I_{rms}^2 R$$

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Kirchhoff's loop rule can be applied and gives

$$\Delta V + \Delta V_L = 0 \text{ or}$$

$$\Delta V - L \frac{di}{dt} = \text{Zero}$$

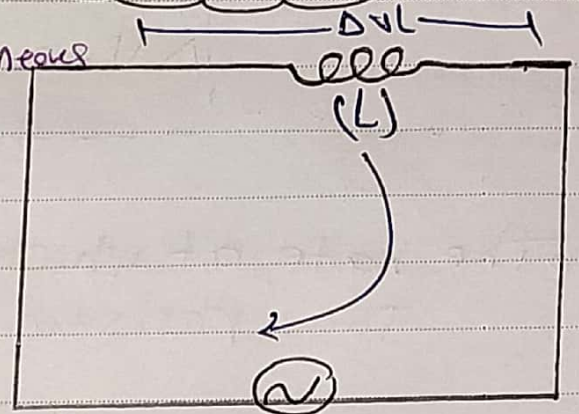
$$\Delta V = L \frac{di}{dt} = \Delta V_{\max} \sin \omega t$$

$$\# i_L = \frac{\Delta V_{\max}}{L} \int \sin \omega t \, dt = -\frac{\Delta V_{\max}}{\omega L} \cos \omega t$$

$$i_L = \frac{\Delta V_{\max}}{\omega L} \sin \left[\omega t - \frac{\pi}{2} \right] \quad \text{---} \quad I_{\max} = \frac{\Delta V_{\max}}{\omega L}$$

This shows that the instantaneous

current i_L in the inductor
and the instantaneous voltage
 ΔV_L across the
inductor are
out of phase by $(\pi/2) \text{ rad} = 90^\circ$



$$\Delta V = \Delta V_{\max} \sin \omega t$$

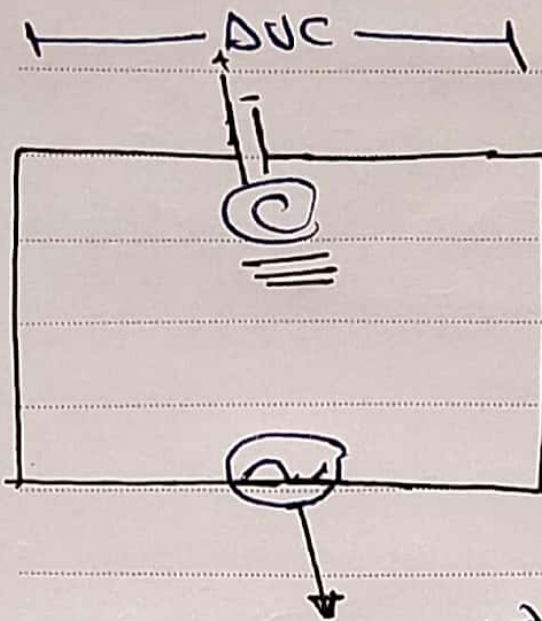
The instantaneous voltage across the inductor is

$$\left(\begin{aligned} \Delta V_L &= -L \frac{di}{dt} \\ &= -\Delta V_{\max} \cdot \sin \omega t \\ &= -I_{\max} \cdot X_L \sin \omega t \end{aligned} \right)$$

||الحل||

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The circuit contains a capacitor and an AC Source.



$\Delta V + \Delta V_C = \text{Zero and so}$

$$i_C = \frac{dq}{dt} = \omega C \Delta V_{\max} \cos \omega t$$

$$\text{or } i_C = \omega C \Delta V_{\max} \sin(\omega t + \frac{\pi}{2})$$

$$i_C = \omega C \Delta V_{\max} \sin(\omega t + \frac{\pi}{2})$$

The Current is $\pi/2$ rad = 90° out Phase

($\Delta V = \Delta V_{\max} \sin \omega t$) with The voltage