* Half_Angle Substitution >> التكامل باستخدام نصف الزارية

* هوطریقت تستخدم فی تکامل الدوال المناشق، خاصه عندما تکون هناك دوال مثلث به مرفوعت لأسس زوجیت أوعبارات نمتوی علی جنور مربعت او ، اذا كان كسر مقامت له : همتوی علی کثرات حدود، و كن دوال مثلث به رای رای به ده وی علی کثرات حدود، و كن دوال

$$y = \tan \frac{x}{2}$$
 $\Rightarrow du = \frac{1}{2} Sec^2 \frac{x}{2} dx$

$$\left(\begin{bmatrix} \frac{1}{2} \left(1 + \upsilon^2\right) \right) \right) \Leftarrow \frac{1}{2} \left(1 + \tan^2 \frac{\chi}{2}\right) d\chi$$

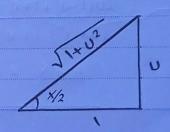
$$\Rightarrow \exists X = \frac{2du}{1+v^2}$$

$$-\sin X = 2 \sin \frac{x}{2} \cos \frac{x}{2}$$

$$= 2 \frac{U}{\sqrt{1+U^2}} \frac{1}{\sqrt{1+U^2}} = \frac{2U}{1+U^2}$$

$$- \left[\cos X \right] = \left[\cos^2 X \right] - \left[\sin^2 X \right]$$

$$= \frac{1}{\sqrt{1+u^2}} - \frac{u^2}{\sqrt{1+u^2}} = \frac{1-u^2}{1+u^2}$$



$$\cos \frac{x}{2} = \frac{1}{\sqrt{1+u^2}}$$

$$\Rightarrow \int \frac{dx}{2 + \cos x} = \int \frac{2 dv}{1 + v^2} = \int \frac{2 d$$

$$\frac{1}{q^{2}+\chi^{2}} = \frac{1}{q^{2}+\chi^{2}} = \frac{1}$$

$$= \int \frac{dx}{\sin x + \tan x} = \int \frac{2 du}{1 + u^2} \frac{2 du}{1 + u^2}$$

$$= \int \frac{2 d u / 1 + u^2}{2 u (1 - u^2 + 1 + u^2)} = \frac{1}{2} \int \frac{(1 - u^2) d u}{u}$$

$$\frac{1}{1+u^2} + \frac{\sin x}{\cos x}$$

$$= \frac{2u}{1+u^2} / \frac{1-u^2}{1+u^2}$$

$$= \frac{2u}{1-u^2}$$

$$\tan \frac{x}{2} = \frac{1}{2} \left[\ln \left| u \right| - \frac{u^2}{2} \right] + e^{-\frac{1}{2} \tan^2 \frac{x}{2}}$$

﴾ تكامل حاصل ضرب الدوال المثلثية ١٠

$$\int \int \sin m \times \cdot \cdot \int \sin n \times \cdot dx = \frac{1}{2} \left(GS(m-n) \times - GS(m+n) \times \right)$$

BISSIN mx - Cos nx
$$dx = \frac{1}{2} \left(Sin (m-n) \times + Sin (m+n) \times \right)$$

صنع الحظارة

$$\Rightarrow \int \sin 3x \cos 5x \, dx = \frac{1}{2} \int (\sin(3-5)x + \sin(3+5)x)$$

$$= \frac{1}{2} \int [-\sin 2x + \sin 8x] \, dx = \frac{1}{2} \left[\frac{1}{2} \cos 2x - \frac{1}{8} \cos 8x \right] + C$$

$$= \frac{1}{4} \cos 2x - \frac{1}{16} \cos 8x + C$$

$$\Rightarrow \int \cos \frac{x}{2} \sin \frac{x}{3} dx =$$

$$= \frac{1}{2} \int (\sin(\frac{1}{2} - \frac{1}{3}) x + \sin(\frac{1}{3} + \frac{1}{2}) x) = \frac{1}{2} \int [\sin \frac{x}{3} + \sin \frac{5x}{3}] dx$$

$$- \int \sin \frac{x}{3} dx = \int \sin \frac{x}{3} dx = -b \cos \frac{x}{3}$$

$$\int \sin \frac{5x}{6} dx = -\frac{6}{5} \cos \frac{5x}{6}$$

$$= \frac{1}{2} \left(-6 \cos \frac{x}{6} - \frac{6}{5} \cos \frac{5x}{6} \right) = -3 \cos \frac{x}{6} - \frac{3}{5} \cos \frac{5x}{6} + C$$

$$= \int \sin 5x \sin 2x \, dx = \frac{1}{2} \int (\cos (5.2)x - \cos (5+2)x) \, dx$$

$$= \frac{1}{2} \int [\cos 3x - \cos 7x] \, dx = \frac{1}{2} \left(\frac{1}{3} \sin 3x - \frac{1}{7} \sin 7x \right) + C$$

$$= \frac{1}{2} \sin 3x - \frac{1}{14} \sin 7x + C$$

ال أخر اتنين الدكتور معلهمين 22999999999