Constraint-Based Methods for Bioinformatics Workshop

Identification of Bifurcations in Biological Regulatory Networks using Answer-Set Programming

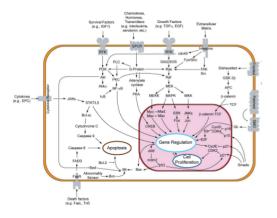
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Joint work with:

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Context

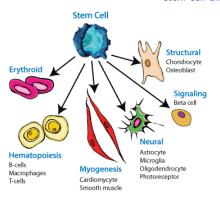


[Liu et al, in Journal of Bioinformatics and Computational Biology, 2012]

- Cellular processes are driven by networks of biological interactions.
- Formal modelling and analysis of Biological Regulatory Network.
- Static analysis of properties.

Motivation

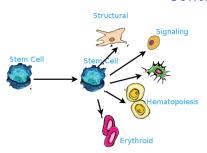
stem cell differentiation



[https://www.systembio.com/stem-cell-research/differentiation-reporters/overview]

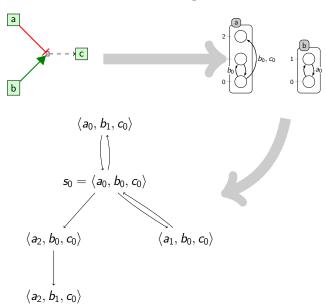
- Loss of capability differentiation
- Which transitions (operations) are responsible of Bifurcations ?
- From which state?

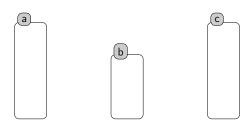
Contribution



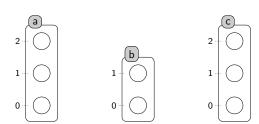
- Bifurcation transitions can be expressed in temporal logic formula
- "Relaxation":
 verification of CTL formula (PSPACE (complete))
 → NP, problem which can be easily expressed in SAT/AS
 - \Rightarrow NP problem which can be easily expressed in SAT/ASP
- Contribution :

Biological networks modelling



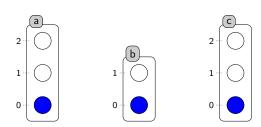


Automata: components a, b, c



Automata: components a, b, c

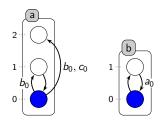
local states: levels of expression c_0 , c_1 , c_2

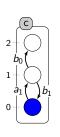


Automata: components a, b, c

local states: levels of expression c_0 , c_1 , c_2

States: sets of active local states $\langle a_0, b_0, c_0 \rangle$





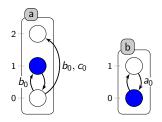
$$s_0 = \langle a_0, b_0, c_0 \rangle$$

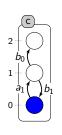
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States: sets of active local states $\langle a_0, b_0, c_0 \rangle$

Transitions: dynamics $t_1=a_0\xrightarrow{b_0}a_1$, $t_2=a_1\to a_0$, $t_3=a_0\xrightarrow{b_0,c_0}a_2$, $t_4=b_0\to b_1$





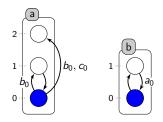
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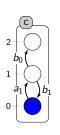
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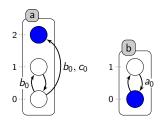
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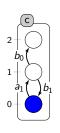
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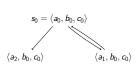
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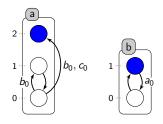


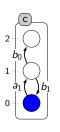
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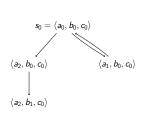
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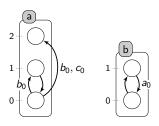


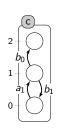
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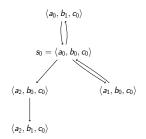
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Automata: components a, b, c

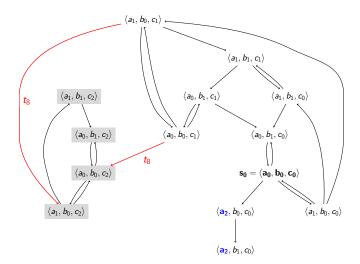
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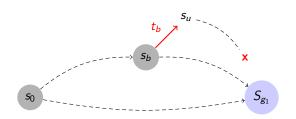
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$$t_4 = b_0 \rightarrow b_1$$

Illustration of bifurcations



Definition of bifurcation



Definition

 t_b is a bifurcation transition from s_0 to g_1 if and only if there exists s_b such that:

(C1)
$$s_u \not\rightarrow^* g_1$$

(C2)
$$s_b \rightarrow^* g_1$$

(C3)
$$s_0 \rightarrow^* s_b$$

Formal approximation of reachability

Static analysis by abstract interpretation

The reachability approximations for ANs introduced in [Paulevé, Magnin, Roux in *Mathematical Structures in Computer Science*, 2012]

$$\mathsf{UA}(s \to^* s') \Rightarrow \mathbf{s} \to^* \mathbf{s}' \Rightarrow \mathsf{OA}(s \to^* s')$$

- OA (over-approximations): necessary conditions for $s \rightarrow^* s'$
- UA (under-approximation): sufficient conditions for $s \to^* s'$ (but the converse does not hold in general)

Interest:

- Avoid state space explosion
- Decide in an efficient way reachability properties

General scheme for identification of bifurcation

concepts and tools



General scheme for identification of bifurcation

concepts and tools



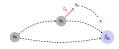
(C1)
$$s_b \cdot t_b \not\rightarrow^* g_1$$

$$(\mathsf{I}\mathsf{1}^\#) \neg \mathsf{OA}(s_u \to^* g_1) \qquad \qquad (\mathsf{I}\mathsf{1}^\#) \Rightarrow (\mathsf{C}\mathsf{1})$$

$$(11^{\#}) \Rightarrow (C1)$$

General scheme for identification of bifurcation

concepts and tools



(C1)
$$s_b \cdot t_b \not\rightarrow^* g_1$$

$$(\mathsf{I}\mathsf{1}^\#) \neg \mathsf{OA}(s_u \to^* g_1)$$

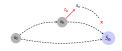
$$(I1^{\#}) \Rightarrow (C1)$$

(C2)
$$s_b \rightarrow^* g_1$$

$$(12^{\#}) \Rightarrow (C2)$$

General scheme for identification of bifurcation

concepts and tools



(C1)
$$s_b \cdot t_b \not\rightarrow^* g_1$$

$$(\mathsf{I}\mathsf{1}^\#) \neg \mathsf{OA}(s_u \to^* g_1)$$

$$(I1^{\#}) \Rightarrow (C1)$$

(C2)
$$s_b \rightarrow^* g_1$$

$$(12^\#)$$
 UA $(s_b \rightarrow^* g_1)$

$$(12^{\#}) \Rightarrow (C2)$$

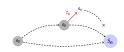
(C3)
$$s_0 \rightarrow^* s_b$$

(13)
$$s_b \in \operatorname{reach}(s_0)$$

(13#)
$$UA(s_0 \rightarrow^* s_b)$$

$$(13^{\#}) \Rightarrow (C3)$$

General scheme for identification of bifurcation



#: sufficient conditions.

(C1)
$$s_b \cdot t_b \not\rightarrow^* g_1$$

$$(\mathsf{I}\mathsf{1}^\#) \neg \mathsf{OA}(s_u \to^* g_1)$$

$$(I1^{\#}) \Rightarrow (C1)$$

(C2)
$$s_b \rightarrow^* g_1$$

$$(12^\#) \quad \mathsf{UA}(s_b \to^* g_1)$$

$$(12^{\#}) \Rightarrow (C2)$$

concepts and tools

$$(\text{C3}) \ s_0 \to^* s_b$$

(13)
$$s_b \in \operatorname{reach}(s_0)$$

(13#)
$$UA(s_0 \rightarrow^* s_b)$$

$$(13^{\#}) \Rightarrow (C3)$$

$$(I1^{\#})$$
 and $(I2^{\#})$ and $((I3)or(I3^{\#})) \Rightarrow t_b$ is a bifurcation.

Automata Network modelling of Biological Networks

Transition-centered specification

- ...in opposition to function-centered of Boolean/Thomas networks
- explicit context/ causality of state changes
- closely related to (safe) Petri nets
- step semantics (purely async, purely sync, mixed)

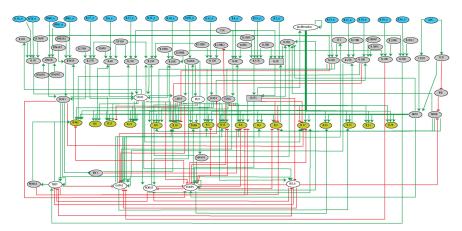
Modelling

- any Boolean/Thomas networks can be encoded;
- in case of logical rules uncertainty: model the union of Boolean/Thomas networks (over-approximation of behaviours)

Case study

Lambda phage: (4 components and 11 interactions); EGF/TNF: (28 components and 55 interactions);

t_helper differentiation: (101 components and 381 interactions).



[Abou-Jaoudé et al, in Frontiers in Bioengineering and Biotechnology, 2015]

Results of identification of bifurcations

Automata Network	Goal	M-C (NuSMV)		(13)		(I3 [#])	
		$ t_b $	Time	$ t_b $	Time	$ t_b $	Time
Lambda phage	${ m CI_2}$	10	0.1 <i>s</i>	6	0.1 <i>s</i>	0	0.2s
$ \Sigma = 4 T = 11$	Cro_2	3	0.1 <i>s</i>	3	0.1 <i>s</i>	2	0.3 <i>s</i>
EGF/TNF	$NFkB_0$	5	0.2 <i>s</i>	4	0.1 <i>s</i>	2	0.1 <i>s</i>
$ \Sigma = 28 T = 55$	IKB_1	5	0.2s	3	0.1 <i>s</i>	2	0.1 <i>s</i>
Th_th17	$RORGT_1$	18	48 <i>s</i>	9	23 <i>s</i>	8	26 <i>s</i>
$ \Sigma = 101 T = 381$	BCL6 ₁	7	26 <i>s</i>	5	23 <i>s</i>	4	24 <i>s</i>
Th_HTG	BCL6 ₁	out-of-time		out-of-time		6	61 <i>s</i>
$ \Sigma = 101 T = 381$	GATA3 ₁					7	34 <i>s</i>

Implemented in ASP (Answer Set Programming) and solve with clingo 4.5.4.

Conclusions & Perspectives

Summary

•

```
 \left\{ \begin{array}{l} \mathsf{AI} \ (\mathsf{Artificial} \ \mathsf{inteligence}) \\ + \\ \mathsf{AI} \ (\mathsf{Abstract} \ \mathsf{interpretation}) \end{array} \right. \Longrightarrow \mathsf{formal} \ \mathsf{approximation} \ \mathsf{of} \ \mathsf{bifurcations}
```

- Tractable on large networks (compared to model-checking)
- Under-approximation: some bifurcations are not returned.

Perspectives

- Over-approximation of bifurcations
- Use bifurcations for the analysis of probability
- Applications for predicting targets for cellular reprogramming.

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Thank you for your attention!