Bandit networks

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Goals of the project

Review the article Ravi Kumar Kolla, Krishna P. Jagannathan, and Aditya Gopalan. "Stochastic bandits on a social network: Collaborative learning with local information sharing". In: *CoRR* abs/1602.08886 (2016). arXiv: 1602.08886. URL: http://arxiv.org/abs/1602.08886

- Understand the proposed framework and algorithms
- Implement them and reproduce the experimental results
- Pinpoint the limitations of the model and try to improve it

Multi-agent stochastic multi-armed bandit (MAB) problem

- Undirected graph G = (V, E) with |V| = m users
- ullet All users are playing the same MAB problem with K arms
- A user v can observe the actions and the respective rewards of itself and its one hop neighbors up to round t, before deciding the action for round (t+1)
- $\mathcal{N}(v)$: node v and its one-hop neighbors
- $m_i^v(t)$: number of times arm i has been chosen by node v and its one-hop neighbors up to round t
- $\hat{\mu}_{m_i^v(t)}$: average reward for playing arm i obtained by node v and its one-hop neighbors up to round t

Upper-Confidence-Bound-Network (UCB-Network) policy

Algorithm 1 Upper-Confidence-Bound-Network (UCB-Network)

Each user in G follows UCB-user policy

UCB-user policy for a user *v*:

Initialization: For $1 \le t \le K$

- play arm t

Loop: For $K \leq t \leq n$

-
$$a^{\mathrm{v}}(t+1) = \operatorname*{argmax}_{j} \hat{\mu}_{m^{\mathrm{v}}_{j}(t)} + \sqrt{\frac{2 \ln t}{m^{\mathrm{v}}_{j}(t)}}$$

Follow Your Leader (FYL) policy

Algorithm 2 Follow Your Leader (FYL) policy

Input: Graph G, a dominating set D and a dominating set partition

Leader - **Each node in** *D*:

Follows the UCB-user policy by using the samples of itself and its neighbors

Follower - Each node in $V \setminus D$:

In round t = 1:

- Chooses an action randomly from ${\mathcal K}$

In round t > 1:

- Chooses the action taken by the leader in its component, in the previous round $\left(t-1\right)$

Issue with the FYL policy

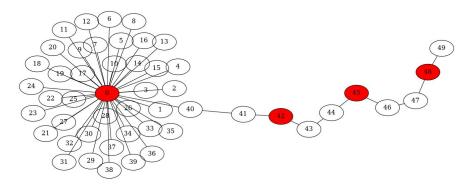


Figure 1: Star-chain graph, with optimal dominating set in red

Nodes 41-49 are missing on a lot of information!

Follow Best Informed (FBI) policy

- FYL policy is myopic
- In addition to their previous action, nodes can output the number of samples (information) they used to compute it
- Nodes can follow their best informed neighbor and use UCB-policy if they are better informed
- Actually, the structure of a graph fully determines the behavior of the nodes (but not their precise actions obviously)

Example of the usefulness of the FBI policy

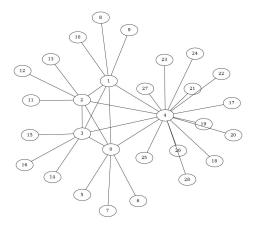


Figure 2: Fully connected stars graph

After first iteration, node 4 has the most information. It can pass it to nodes 0-3, who will then pass it to their children.

Results for a fully connected stars graph

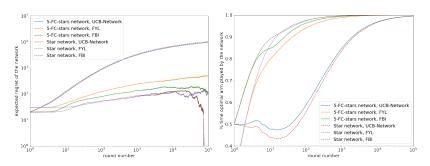


Figure 3: Performance comparison of UCB-Network, FYL, and FBI policies on a 100-nodes star network and on the 100-nodes 5-FC-stars network: 2 arms, Bernoulli rewards with means 0.5 and 0.7 (1000 sample paths).

Results for a star-chain graph

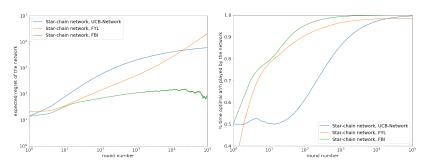


Figure 4: Performance comparison of FYL and FBI policies on the pathological graph structure (star graph with 70 nodes, among which a 20-nodes long chain): 2 arms, Bernoulli rewards with means 0.5 and 0.7 (1000 sample paths).

A deeper look at the FBI policy

- Downside: If one node has more information than the rest, every node is going to follow it (at a delayed rate) ⇒ Strong correlation in the nodes actions
- Further improvements: When a node has multiple
 neighbors informed about in the same way, it may be smart to
 randomly follow one with a probability depending on its
 amount of information. But then the behavior of the nodes is
 not determined by the structure of the graph...

Conclusion

- RL framework very useful to study to study a bandit problem on a graph...
- ... But the naive solution is not very efficient!
- For simple policies, interesting bounds can be computed
- More general types of graphs provide hints to build more robust strategies

Any Questions?

References



Ravi Kumar Kolla, Krishna P. Jagannathan, and Aditya Gopalan. "Stochastic bandits on a social network: Collaborative learning with local information sharing". In: *CoRR* abs/1602.08886 (2016). arXiv: 1602.08886. URL: http://arxiv.org/abs/1602.08886.