Deep Learning for Natural Language Processing

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23 décembre 2018

2 Multilingual word embeddings

Question

We want to minimize $\|WX - Y\|$ under the constraint that $W \in O_d(\mathbb{R})$.

We notice :

$$\begin{aligned}\|WX - Y\|_F^2 &= \langle WX - Y, WX - Y\rangle \\ &= \|WX\|_F^2 + \|Y\|_F^2 - 2\langle WX, Y\rangle \\ &= \|X\|_F^2 + \|Y\|_F^2 - 2\langle WX, Y\rangle\end{aligned}$$

So minimizing $\|WX - Y\|$ is equivalent to maximizing $\langle WX, Y\rangle$.

Let's write $U\Sigma V^T = SVD(YX^T)$. We have :

$$\begin{aligned}\langle WX, Y\rangle &= \langle W, YX^T\rangle \\ &= \langle W, U\Sigma V^T\rangle \\ &= \langle U^T WV, \Sigma\rangle\end{aligned}$$

Let's denote $Q = U^T WV$. We have :

$$\begin{aligned}\langle Q, \Sigma\rangle &= \text{Trace}(Q^T\Sigma) \\ &= \sum_{k=1}^{d} Q_{kk}\Sigma_{kk}\end{aligned}$$

Because Σ is diagonal.

Notice that $Q = U^T WV \in O_d(\mathbb{R})$ because $O_d(\mathbb{R})$ is a group and U, V, W belong to it. It implies that $Q_{kk} \in [-1, 1]$.

Thus, this expression is maximized when $Q = I$, since we need to choose $Q_{kk} = 1$ for all k because the entries of Σ are non-negative.

So :

$$Q = I \Leftrightarrow U^T WV = I \Leftrightarrow W = UV^T$$

3 Sentence classification with BoV

Question

4 Deep Learning models for classification

Question 1

I used the categorical cross-entropy loss.

Its formula is

$$-\frac{1}{N}\sum_{i=1}^{N}\sum_{c=1}^{C}\mathbf{1}_{\{y_i=c\}}\log(p(\hat{y}_i=c))$$

where N is the number of examples, C is the number of classes, y_i is the true label of example i, and $\hat{y}_i$ is the predicted label of example i.

Question 2

FIGURE 1 – Evolution of train/dev results w.r.t the number of epochs.

Question 3