Homework 9, Problem 3

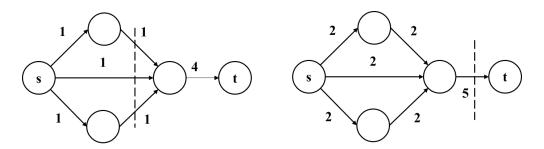
Problem 3 (10 points):

Decide whether you think the following statement is true or false. If it is true, give a short explanation. If it is false, give a counterexample.

Let G be an arbitrary flow network, with a source s, a sink t and a positive integer capacity c_e on every edge e; and let (A, B) be a minimum s - t cut with respect to these capacities $\{c_e : e \in E\}$. Now suppose we add 1 to every capacity; then (A, B) is still a minimum s - t cut with respect to these new capacities $\{1 + c_e : e \in E\}$.

Answer:

false:



Before, minimum cut is 3

After, minimum cut is 5

Figure 1: A counterexample