

Homework 3 Problem 4

**Programming Problem 4 (10 points):**

The purpose of this problem is to construct a random graph generator for use in other programming problems and to demonstrate an implementation of graphs using adjacency lists.. A random graph generator, given an input parameter  $n$ , picks “at random” a graph with  $n$  vertices. There are multiple different models of random graphs. We will consider the *edge density* model, where a parameter  $p$  gives the probability of each edge being present. This model is referred to as  $\mathcal{G}_p^n$ . The undirected random graph generation problem is: given an integer  $n$  and a real number  $p$  with  $0 \leq p \leq 1$ , construct an undirected graph on  $n$  vertices where each edge  $\{u, v\}$  has probability  $p$  of being in the set of edges  $E$ , and the probability of each edge is independent. Write a generator for  $\mathcal{G}_p^n$  which given inputs  $n$  and  $p$  constructs a random undirected graph in adjacency list representation.

For this problem, write the graph generator and a routine to print the edges and vertices of a graph. Print the results a creating two different random graphs using  $n = 10$  and  $p = 0.2$ .

**Answer:**

```
import java.util.HashMap;
import java.util.ArrayList;
import java.util.Arrays;
import java.util.Random;

public class Graph{
    public int n;
    private int m;
    private double p;
    public HashMap<Integer, ArrayList<Integer>> vertexMap = new HashMap<>();
    public ArrayList<int[]> edgeList = new ArrayList<>();

    public Graph(int n, double p) {
        this.n = n;
        this.p = p;
        m = (int) (n * (n - 1) * p / 2.0);
        //System.out.printf("n:%d, m:%d, p:%.4f\n", n, m, p);
        getRandomGraph();
    }
}
```

```

    }

    void getRandomGraph(){
        Random rand = new Random();
        for (int i = 0; i < n - 1; i++)
            for (int j = i + 1; j < n; j++)
                if (rand.nextDouble() < p){
                    AddEdge(i, j);
                }
    }

    void AddEdge(int i, int j) {
        if(!vertexMap.containsKey(i)){
            vertexMap.put(i, new ArrayList<>());
        }
        vertexMap.get(i).add(j);

        if(!vertexMap.containsKey(j)){
            vertexMap.put(j, new ArrayList<>());
        }
        vertexMap.get(j).add(i);
        edgeList.add(new int[] {i, j});
        edgeList.add(new int[] {j, i});
    }

    public static void main(String[] args){
        Graph g1 = new Graph(10, 0.2);
        Graph g2 = new Graph(10, 0.2);
        System.out.println("g1:␣" + g1.vertexMap);
        for (int[] edge : g1.edgeList){
            System.out.print(Arrays.toString(edge) + '␣');
        }
        System.out.println();
        System.out.println("g2:␣" + g2.vertexMap);

        for (int[] edge : g2.edgeList){
            System.out.print(Arrays.toString(edge) + '␣');
        }
    }
}

```

g1: 0=[6, 9], 1=[7], 2=[6], 3=[4, 8], 4=[3, 9], 5=[9], 6=[0, 2, 7, 9], 7=[1, 6], 8=[3], 9=[0, 4, 5, 6]  
 [0, 6][6, 0][0, 9][9, 0][1, 7][7, 1][2, 6][6, 2][3, 4][4, 3][3, 8][8, 3][4, 9][9, 4][5, 9][9, 5][6, 7][7, 6][6, 9][9, 6]

g2: 0=[5], 1=[4, 5, 6], 2=[9], 3=[6], 4=[1, 8], 5=[0, 1], 6=[1, 3, 7], 7=[6, 8], 8=[4, 7], 9=[2]  
 [0, 5][5, 0][1, 4][4, 1][1, 5][5, 1][1, 6][6, 1][2, 9][9, 2][3, 6][6, 3][4, 8][8, 4][6, 7][7, 6][7, 8][8, 7]