

# EL9343 Homework 1

(Due September 29, 2016)

*All problem/exercise numbers are for the third edition of CLRS text book*

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1. Prove the *Transitivity* property of  $\Theta(\cdot)$ , i.e.  $f(n) = \Theta(g(n))$  and  $g(n) = \Theta(h(n)) \Rightarrow f(n) = \Theta(h(n))$ .
2. Problem 3-1 in CLRS Text book;
3. Problem 3-2 in CLRS Text book;
4. Problem 3-4 (a) (b) (g), (h) in CLRS Text book;
5. Use the substitution method to show that the solution to  $T(n) = T(\alpha n) + T((1 - \alpha)n) + 10$ , with  $0 < \alpha < 1$ , is  $\Theta(n)$
6. First use the iteration method to solve the recurrence:

$$T(n) = T\left(\frac{n}{4}\right) + T\left(\frac{3n}{4}\right) + n$$

then use the substitution method to verify your solution.

7. First use the iteration method to solve the recurrence

$$T(n) = T\left(\frac{n}{6}\right) + T\left(\frac{n}{3}\right) + n^2$$

then use the substitution method to verify your solution.

8. Solving the recurrence:

$$T(n) = 9T(n^{\frac{1}{3}}) + \log^2(n).$$

*(Hint: Making change of variable)*

9. Give asymptotic upper and lower bounds for  $T(n)$  in each of the following recurrences. Make your bounds as tight as possible, and justify your answers.
  - (a)  $T(n) = 2T(n/3) + n^{\frac{1}{2}} \log n$
  - (b)  $T(n) = 25T(n/5) + n^2$
  - (c)  $T(n) = 4T(n/2) + n^2 \sqrt{n}$
  - (d)  $T(n) = T(n - 2) + 1/n$