逻辑与推理2

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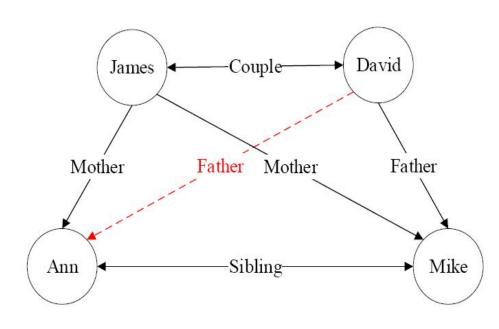
致谢:本课件主要内容来自浙江大学吴飞教授、 南开大学程明明教授

提纲

- 命题逻辑
- 谓词逻辑
- 知识图谱推理
- 因果推理

知识图谱:基本概念

- ●知识图谱可视为包含多种关系的图。
 - ●每个节点是一个实体(如人名、地名、 事件和活动等),任意两个节点之间的 边表示这两个节点之间存在的关系。
- ●可将知识图谱中任意两个相连节点及其 连接边表示成一个三元组(*triplet*)
 - $\mathbb{P}(left_{node}, relation, right_{node})$
 - ●例(David, Father, Mike)



知识图谱:知识工程

- Edward A. Feigenbaum于1977年提出了知识工程的概念
 - 开发了基于知识的系统(knowledge-based systems)。该系统利用计算机程序包含大量知识、规则、和推理机制,为显示生活中的问题提供解决方案。
 - 基于知识的系统主要表现形式是用于模仿专家决策过程的专家系统。
 - Turing Award in 1994

Feigenbaum, E. A., The Art of Artificial Intelligence: Themes and Case Studies of Knowledge Engineering,

Proceedings of the International Joint Conference on Artificial Intelligence(IJCAI),1977

The art of artificial intelligence—Themes and case studies of knowledge engineering

by EDWARD A. FEIGENBAUM Stanford University Stanford, California

INTRODUCTION-AN EXAMPLE

This paper will examine emerging themes of knowledge engineering, illustrate them with case studies drawn from the work of the Stanford Heuristic Programming Project, and discuss general issues of knowledge engineering art and practice.

Let me begin with an example new to our workbench: a system called PUFF, the early fruit of a collaboration between our project and a group at the Pacific Medical Center (PMC) in San Francisco.*

A physician refers a patient to PMC's pulmonary function testing lab for diagnosis of possible pulmonary function disorder. For one of the tests, the patient inhales and exhales a few times in a tube connected to an instrument/computer combination. The instrument acquires data on flow rates and volumes, the so-called flow-volume loop of the patient's lungs and airways. The computer measures certain parameters of the curve and presents them to the diagnostician (physician or PUFF) for interpretation. The diagnosis is made along these lines: normal or diseased; restricted lung disease or obstructive airways disease or a combination of both; the severity; the likely disease type(s) (e.g., emphysema, bronchitis, etc.); and other factors important for diagnosis.

PUFF is given not only the measured data but also certain items of information from the patient record, e.g., sex, age, number of pack-years of eigarette smoking. The task of the PUFF system is to infer a diagnosis and print it out in English in the normal medical summary form of the interpretation expected by the referring physician.

RULE 31

IF

The severity of obstructive airways disease of the patient is greater than or equal to mild, and
 The degree of diffusion defect of the

The degree of diffusion defect of the patient is greater than or equal to mild, and

3) The tlc (body box) observed/predicted of the patient is greater than or equal to 110

 The observed-predicted difference in rv/tlc of the patient is greater than or equal to 10

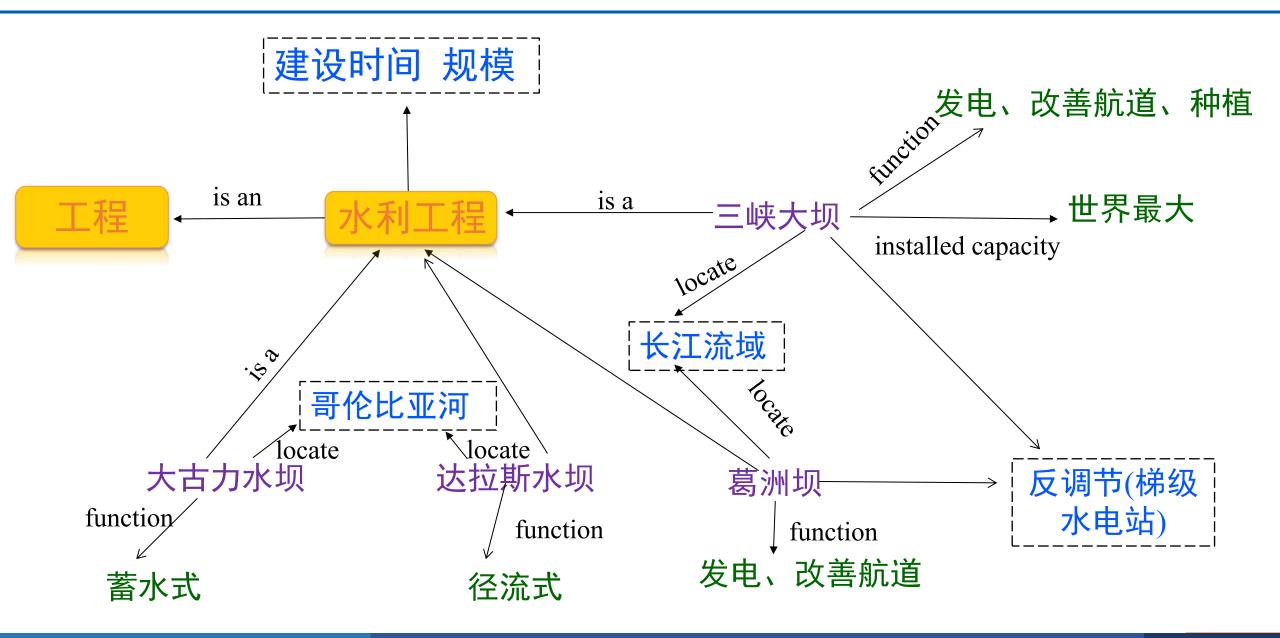
THEN

 There is strongly suggestive evidence (.9) that the subtype of obstructive airways disease is emphysema, and
 It is definite (1.0) that "OAD, Diffusion Defect, elevated TLC, and elevated RV together indicate emphysema." is one of the findings.

One hundred cases, carefully chosen to span the variety of disease states with sufficient exemplary information for each, were used to extract the 55 rules. As the knowledge emerged, it was represented in rule form, added to the system and tested by running additional cases. The expert was sometimes surprised, sometimes frustrated, by the occasional gaps and inconsistencies in the knowledge, and the incorrect diagnoses that were logical consequences of the existing rule set. The interplay between knowledge engineer and expert gradually expanded the set of rules to remove most of these problems.

As cumulation of techniques in the art demands and allows, a new tool was not invented when an old one would do. The knowledge engineers pulled out of their toolkit a version of the MYCIN system (to be discussed later), with the rules about infectious diseases removed, and used it as the inference engine for the PUFF diagnoses. Thus PUFF, like MYCIN, is a relatively simple backward-chaining infer-

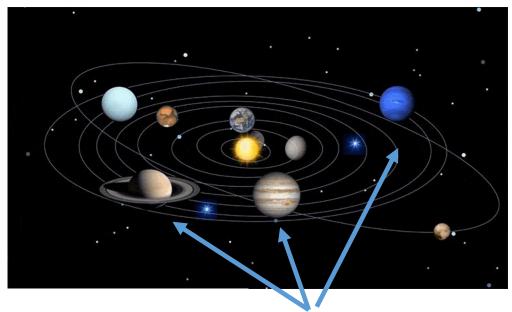
^{*} Dr. J. Osborn, Dr. R. Fallat, John Kunz, Diane McClung.



·概念之间层次化关系(ontology):

- •如:工程→水利工程
- 与Wordnet等早期本体知识构建不同, 现有方法多在传统分类法(Taxonomy) 中结合大众分类(Folksonomy)和机器学 习来构建语义网络分类体系。

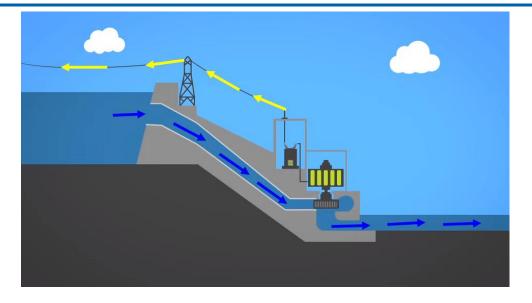
(太阳系→地月系统)



例子或实体

• 概念或实体的属性:

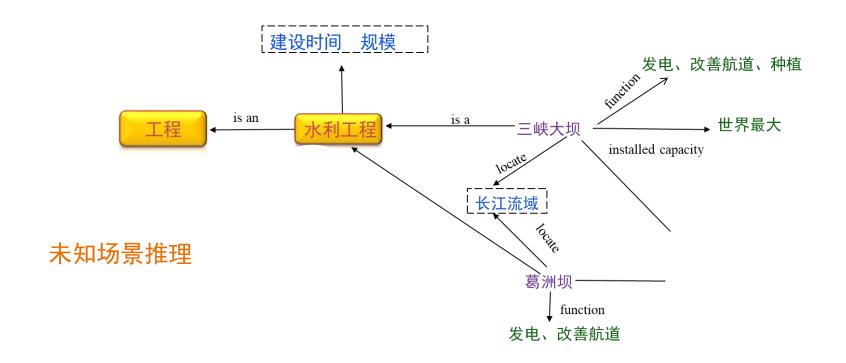
• 属性是对概念或实体内涵的描述。



水利工程可发电

- · 概念或实体的<u>属性描述和关</u> <u>系表达</u>一般通过三元组来表 示:
 - (entity, relation, entity)或 (subject, predicate, object)

- ·知识图谱推理 (inference):
 - 通过机器学习等方法对知识图谱所蕴含关系进行挖掘。



知识图谱的构成

- ·知识图谱一般可通过标注多关系图(labeled multi-relational graph)来表示。
 - 概念: 层次化组织

知识图谱推理

•知识图谱中存在连线的两个实体可表达为三元组形式

- < left_node, relation, right_node >
- 这种三元组也可以表示为一阶逻辑(first order logic, FOL)的形式
- 为基于知识图谱的推理创造了条件
- ·例如从<與巴马,出生地,夏威夷>和<夏威夷,属于,美国>两个三元组,可推理得到<奥巴马,国籍,美国>。

知识图谱推理

• 可利用一阶谓词来表达刻画知识图谱中节点之间存在的关系

知识图谱推理

•问题:如何从知识图谱中推理得到

father(David, Ann)



 $(\forall x)(\forall y)(\forall z)\big(Mother(z, y)$ $\land Couple(x, z) \rightarrow Father(x, y)\big)$

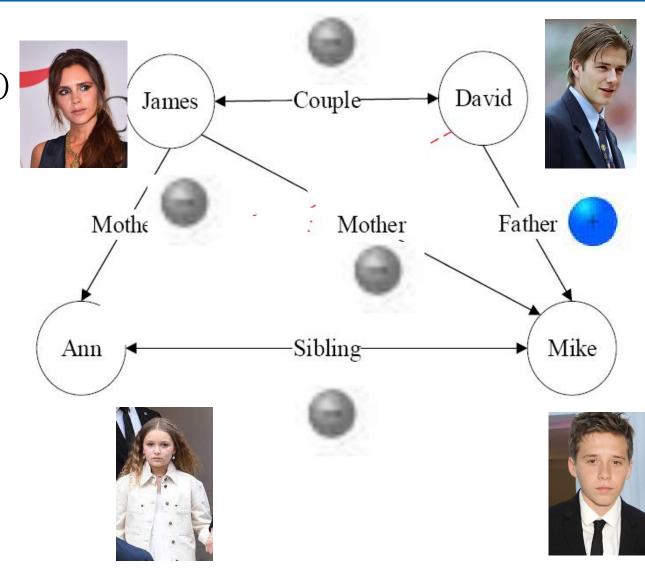
知识图谱推理: 归纳学习

- · 归纳逻辑程序设计 (inductive logic programming, ILP)算法
 - · ILP是机器学习和逻辑程序设计交叉领域的研究内容
 - ILP使用一**阶谓词逻辑**进行知识表示,通过修改和扩充逻辑表达 式对现有知识归纳,完成推理任务。

• 作为ILP的代表性方法,FOIL(First Order Inductive Learner) 通过序贯覆盖实现规则推理。

 推理手段: positive examples + negative examples + background knowledge examples ⇒ hypothesis

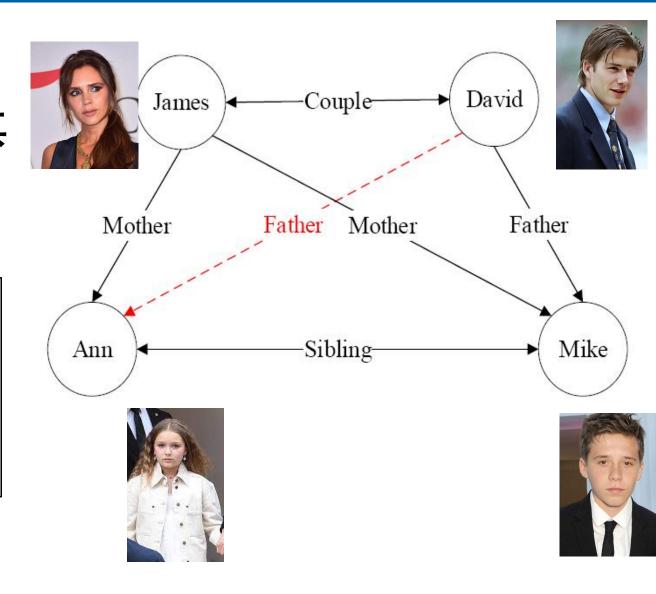
- 目标谓词: Father(x, y)
- 目标谓词只有一个正例Father(David, Mike)

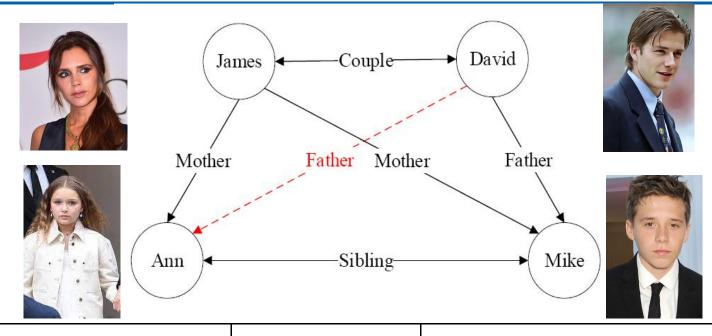


• 目标谓词: Father(x, y)

· 背景知识:目标谓词以外的其 它谓词实例化结果

当景知识 | Couple(David, James) | 样例集合 | Mother(James, Ann) | Mother(James, Mike) |





背景知识 样例集合

Sibling(Ann, Mike) 背景知识 Couple(David, James)

样例集合 | Mother(James, Ann)

Mother(James, Mike)

目标谓词 训练样例 集合 Father(David, Mike)

¬Father(David, James)

¬Father(James, Ann)

¬Father(James, Mike)

¬Father(Ann, Mike)

 $(\forall x)(\forall y)(\forall z)\big(Mother(z, y) \land Couple(x, z) \rightarrow Father(x, y)\big)$



前提约束谓词(学习得到)

目标谓词(已知)

如何推理

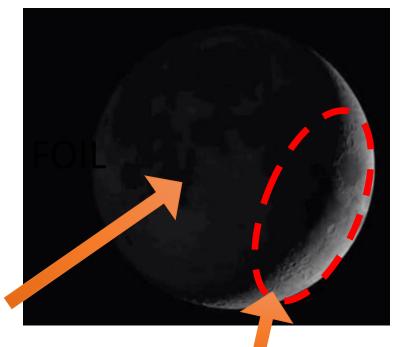


 $(\forall x)(\forall y)(\forall z)(Mother(z, y) \land Couple(x, z) \rightarrow Father(x, y))$

前提约束谓词(学习得到)

推理思路:从一般到特殊,逐步给目标谓词添加前提约束谓词,直到所构成的推理规则不覆盖任何反例。

目标谓词(已知)



前提约束谓词

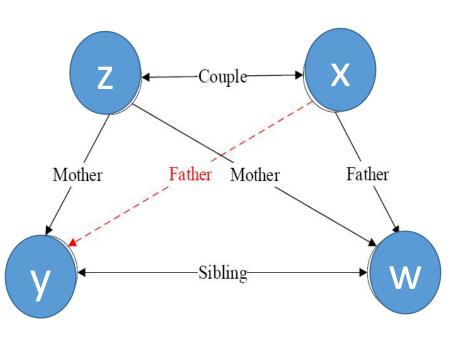
目标谓词

 $(\forall x)(\forall y)(\forall z)\big(Mother(z, y) \land Couple(x, z) \rightarrow Father(x, y)\big)$

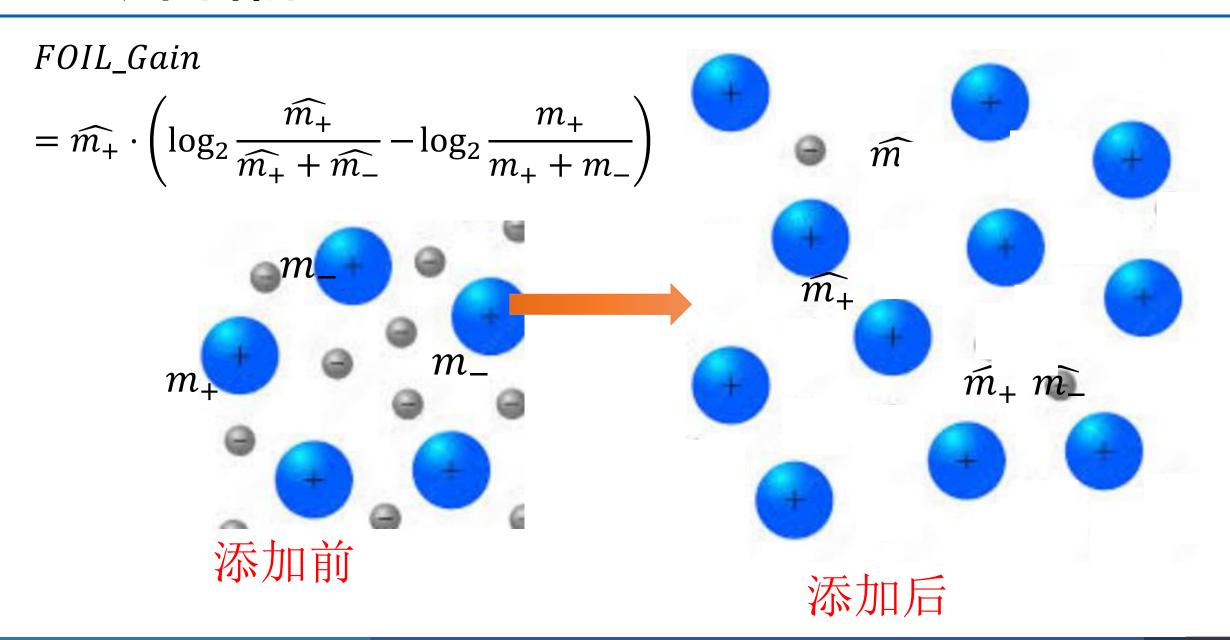


- · 对目标谓词或前提约束谓词中的变量赋 予值具体
 - •如将上例这一推理规则所包含的目标谓词Father(x, y)中x和y分别赋值为David和Ann





- •哪些谓词好呢?可以作为目标谓词的前提约束谓词?
 - FOIL中信息增益值(information gain)



 $(\forall x)(\forall y)(\forall z)(Mother(z, y) \land Couple(x, z) \rightarrow Father(x, y))$



前提约束谓词(学习得到)



- lacktriangle Mother(\cdot , \cdot)
- $Sibling(\cdot, \cdot)$
- \bullet Couple(\cdot , \cdot)

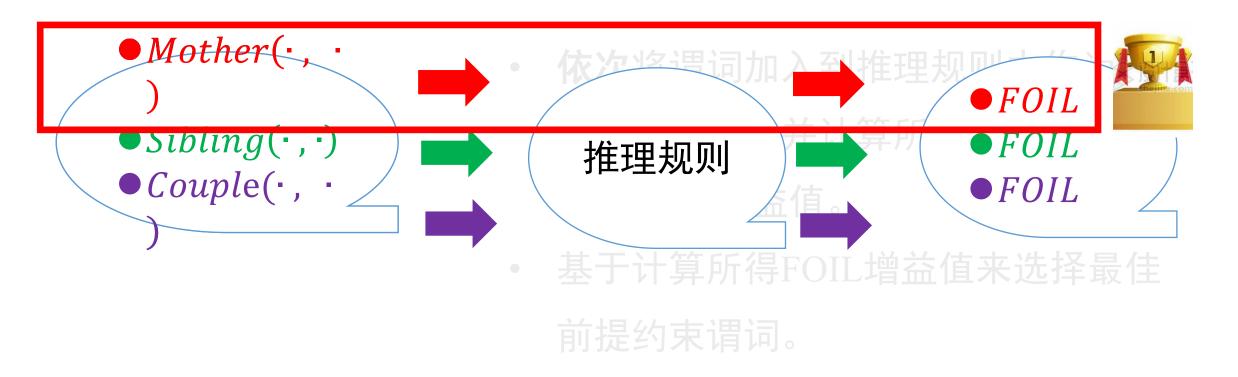
- 依次将谓词加入到推理规则中作为前提约束谓词,并计算所得到新推理规则的FOIL增益值。
- · 基于计算所得FOIL增益值来选择最佳 前提约束谓词。

 $(\forall x)(\forall y)(\forall z)(Mother(z, y) \land Couple(x, z) \rightarrow Father(x, y))$



前提约束谓词(学习得到)

目标谓词(已知)



 $(\forall x)(\forall y)(\forall z)(Mother(z, y) \land Couple(x, z) \rightarrow Father(x, y))$



前提约束谓词(学习得到)



	Cibling(Ann Miles)		Father(David, Mike)
	Sibling(Ann, Mike)	目标谓词	¬Father(David, James)
背景知识	Couple(David, James)	训练样例	¬Father(James, Ann)
样例集合	Mother(James, Ann)		
	Mother(James, Mike)	集合	¬Father(James, Mike)
			¬Father(Ann, Mike)

	FOIL算法
输入:	目标谓词 P , P 的训练样例(正例集合 E^+ 和反例集合 E^-
),其他背景知识
输出:	推导得到目标谓词P的推理规则
1	将目标谓词作为所学习推理规则的结论
2	将其他谓词逐一作为前提约束谓词加入推理规则,计算所得到推理规则的FOIL信息增益值,选取最优前提约束谓词以生成新推理规则,并将训练样例集合中与该推理规则不符的样例去掉
3	重复2过程,直到所得到的推理规则不覆盖任意反例

- · 给定目标谓词,此时推 理规则只有目标谓词
- 因此推理规则所覆盖的 正例和反例的样本数分 别是训练样本中正例和 反例的数量

•
$$m_{+} = 1$$
, $m_{-} = 4$

推理规则		推理规则涵盖的正例 和反例数		FOIL信息 增益值
目标谓词	前提约束谓词	正例	反例	信息增益值
$Father(x, y) \leftarrow$	空集	$m_{+} = 1$	m=4	FOIL_Gain

	Cibling (A Miles)		Father(David, Mike)	
	Sibling(Ann, Mike)	目标谓词	¬Father(David, James)	
背景知识	Couple(David, James)	训练样例	¬Father(James, Ann)	
样例集合	Mother(James, Ann)			
	Mother(James, Mike)	集合	¬Father(James, Mike)	
	Modifer (James, Mike)		¬Father(Ann, Mike)	

- 将Mother(x, y)作为前提约束谓词加入,可得到推理规则
 - $Mother(x, y) \rightarrow Father(x, y)$

推理规!		涵盖的正 反例数	FOIL信息 增益值	
目标谓词	前提约束谓 词	正例	反例	信息増益 值
$Father(x, y) \leftarrow$	空集	$m_{+} = 1$	$m_{-} = 4$	FOIL_Gain
	Mother(x, y)	$\widehat{m_+} = 0$	$\widehat{m}_{-}=2$	NA

 $Father(x, y) \leftarrow$

				Father(David, Mike)
景			目标谓词	¬Father(David, James)
			训练样例	¬Father(James, Ann)
			集合	¬Father(James, Mike)
	Mother(James, Mike)			¬Father(Ann, Mike)
1	景识 例合	Couple(David, James)例 Mother(James, Ann)	京 识 Couple(David, James) 例 Mother(James, Ann)	京 目标谓词 目标谓词 识 Couple(David, James) 训练样例 Mother(James, Ann) 集合

- 将Mother(x, y)作为前提约束谓词加入,可得到推理规则
 - $Mother(x, y) \rightarrow Father(x, y)$
- 背景知识中Mother(x, y)有两个实例
 - *Mother(James, Ann)*
 - Mother(James, Mike)
- •对于Mother(James, Mike)这一实例
 - x = James, y = Mike, 将x 和y 代入Father(x, y), 可知在训练样本中Father(James, Mike)是一个反例

推理规!	推理规则涵盖的正 ① 例和反例数		FOIL信息 增益值	
目标谓词	前提约束谓 词	正例	反例	信息增益 值
$Father(x, y) \leftarrow$	空集	$m_{+} = 1$	$m_{-} = 4$	FOIL_Gain
	Mother(x, y)	$\widehat{m_+} = 0$	$\widehat{m}_{-}=2$	NA

 $Father(x, y) \leftarrow$

		Cibling(Ann Miles)		Father(David, Mike)
	背景	Sibling(Ann, Mike)	目标谓词	¬Father(David, James)
	知识	Couple(David, James)	训练样例	¬Father(James, Ann)
-	样例 集合	Mother(James, Ann)	集合	¬Father(James, Mike)
	/ □	Mother(James, Mike)		¬Father(Ann, Mike)

 $Mother(x, y) \rightarrow Father(x, y)$

• 覆盖正例和反例数量分别为

$$\widehat{m_+}=0$$
, $\widehat{m_-}=2$

由于 n₊ = 0,代入 F O I L _
 G a i n 公式时会出现负无
 穷的情况,此时 F O I L _G
 a i n 记为NA (Not Available)

推理规!	则		涵盖的正 反例数	FOIL信息 增益值
目标谓词	前提约束谓 词	正例	反例	信息增益 值
$Father(x, y) \leftarrow$	空集	$m_{+} = 1$	$m_{-} = 4$	FOIL_Gain
	Mother(x, y)	$\widehat{m_+} = 0$	$\widehat{m}_{-}=2$	NA
	Mother(x, z)	$\widehat{m_+} = 0$	$\widehat{m}_{-}=2$	NA
	Mother(y, x)	$\widehat{m_+} = 0$	$\widehat{m}_{-}=1$	NA
	Mother(y, z)	$\widehat{m_+} = 0$	$\widehat{m}_{-}=1$	NA
	Mother(z, x)	$\widehat{m_+} = 0$	$\widehat{m}_{-}=1$	NA
	Mother(z, y)	$\widehat{m_+} = 1$	$\widehat{m}_{-}=3$	0.32
	Sibling(x, y)	$\widehat{m_+} = 0$	$\widehat{m}_{-}=1$	NA
	Sibling(x, z)	$\widehat{m_+} = 0$	$\widehat{m}_{-}=1$	NA
Eathor(x x)	Sibling(y, x)	$\widehat{m_+} = 0$	$\widehat{m}_{-}=0$	NA
Father $(x, y) \leftarrow$	Sibling(y, z)	$\widehat{m_+} = 0$	$\widehat{m}_{-}=0$	NA
	Sibling(z, x)	$\widehat{m_+} = 0$	$\widehat{m}_{-}=0$	NA
	Sibling(z, y)	$\widehat{m_+} = 1$	$\widehat{m}_{-}=2$	0.74
	Couple(x, y)	$\widehat{m_+} = 0$	$\widehat{m}_{-}=1$	NA
	Couple(x, z)	$\widehat{m_+} = 1$	$\widehat{m}_{-}=1$	1.32
	Couple(y, x)	$\widehat{m_+} = 0$	$\widehat{m}_{-}=0$	NA
	Couple(y, z)	$\widehat{m_+} = 0$	$\widehat{m}_{-}=0$	NA
	Couple(z, x)	$\widehat{m_+} = 0$	$\widehat{m}_{-}=2$	NA
	Couple(z, y)	$\widehat{m_+} = 0$	$\widehat{m}_{-}=1$	NA

- •如果将Couple(x, z)作为前提约束谓词加入,
 - 可得到如下推理规则 $Couple(x, z) \rightarrow Father(x, y)$
- 在背景知识中,Couple(x, z)只有一个实例
 - PPx = David, z = James
 - 将其代入Father(x, y)得到 Father(David, y)

推理规则		推理规则涵盖的正 例和反例数		FOIL信息 增益值	
目	标谓词	前提约束谓 词	正例	反例	信息增益 值
Fathe	$er(x, y) \leftarrow$	空集	$m_{+} = 1$	$m_{-} = 4$	FOIL_Gain
背景 知识 样例 集合	Sibling(Ann Couple(Dav Mother(Jam Mother(Jam	id, James) nes, Ann)	目标谓词 训练样例 集合	¬Father(Ja	avid, James) ames, Ann) ames, Mike)

 $Father(x, y) \leftarrow$

Couple(x, z) $\widehat{m}_{+} = 1$ $\widehat{m}_{-} = 1$ 1.32

• 训练样本中存在正例以及反例

- Father(David, Mike)
- $\neg Father(David, James)$,
- 即 $Couple(x, z) \rightarrow Father(x, y)$ 覆盖正反例数量分别为1和1。
- •信息增益值为:

$$\widehat{m_{+}} \cdot \left(\log_{2} \frac{\widehat{m_{+}}}{\widehat{m_{+}} + \widehat{m_{-}}} - \log_{2} \frac{m_{+}}{m_{+} + m_{-}} \right)$$

$$= 1 \cdot \left(\log_{2} \frac{1}{1+1} - \log_{2} \frac{1}{1+4} \right) = 1.32$$

	推理规则]涵盖的正 反例数	FOIL信息 增益值
	目	标谓词	前提约束谓 词	正例	反例	信息增益 值
	Fathe	$r(x, y) \leftarrow$	空集	$m_{+} = 1$	$m_{-} = 4$	FOIL_Gain
)	背景 知 样例 集合	Sibling(Ann Couple(Dav Mother(Jam Mother(Jam	id, James) es, Ann)	目标谓词 训练样例 集合	Father(Dav ¬Father(D ¬Father(Ja ¬Father(Ja ¬Father(A	avid, James) mes, Ann) mes, Mike)

 $Father(x, y) \leftarrow$

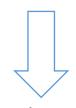
Couple(x, z) $\widehat{m}_{+} = 1$ $\widehat{m}_{-} = 1$ 1.32

Back-ground knowledge	Sibling(Ann, Mike) Couple(David, James) Mother(James, Ann) Mother(James, Mike)
Positive and negative samples	Father(David, Mike) ¬Father(David, James) ¬Father(James, Ann) ¬Father(James, Mike) ¬Father(Ann, Mike)

- Couple(x, z) 加入后信息增益最大
- 将 Couple(x, z) 加入推理规则,得到 $Couple(x, z) \rightarrow Father(x, y)$ 新推理规则
- 将训练样例中与该推理规则不符的样例去掉。 这里不符指当*Couple(x,z)*中*x*取值为David时, 与*Father*(David,)或¬*Father*(David,)无法匹 配的实例。
- 训练样本集中只有正例 Father (David, Mike) 和负例¬Father (David, James)两个实例

$Mother(z, y) \land Couple(x, z)$

 \rightarrow Father(x, y)



已知:

Mother(James, Ann)
Couple(David, James)

于是: x=David, z=James,因此y=Ann 或者Mike.

	推理规则			推理规则涵盖的 正例和反例数		FOIL 信息		
	现有规则	拟加入前提 约束谓词			正例	反例	增益 值	
背景知识 样例 集合	Sibling(Ann, Mik Couple(David, Ja Mother(James, A Mother(James, M	mes) nn)	-			(David, M er(David, J	,	
	Father(x , y) \leftarrow Couple(x , z)	∧ Sibli ∧ Sibli ∧ Sibli ∧ Sibli ∧ Coup ∧ Coup ∧ Coup ∧ Coup ∧ Coup	ing(x, z) $ing(y, x)$ $ing(y, z)$ $ing(z, x)$ $ing(z, y)$ $ole(x, y)$ $ole(x, z)$ $ole(y, z)$ $ole(y, z)$ $ole(z, x)$ $ole(z, y)$		$ \begin{array}{c} k_{+} = 0 \\ k_{+} = 0 \\ $	$ \widehat{m}_{-} = 0 $ $ \widehat{m}_{-} = 1 $ $ \widehat{m}_{-} = 1 $ $ \widehat{m}_{-} = 0 $ $ \widehat{m}_{-} = 0 $ $ \widehat{m}_{-} = 0 $	NA N	

- ●推理Mother(z, y)加入信息增益最大
- ●将Mother(z, y)加入,得到新规则

 $Mother(z, y) \land Couple(x, z)$

- \rightarrow Father(x, y)
- ●当x = David、y = Mike、z = James 时,该推理规则覆盖训练样本集合中 正例 Father (David, Mike)且不覆盖 任意反例,因此算法学习结束。

推理	推理规则 正例和	FOIL 信息		
现有规则	拟加入前提 约束谓词	正例	反例	増益 值
$Father(x, y) \leftarrow$	$m_{+} = 1$	$m_{-} = 1$	1.32	
	\land <i>Mother</i> (x , y)	$\widehat{m_+} = 0$	$\widehat{m}_{-}=0$	NA
	\land <i>Mother</i> (x , z)	$\widehat{m_+} = 0$	$\widehat{m}_{-}=0$	NA
	\land Mother (y, x)	$\widehat{m_+} = 0$	$\widehat{m}_{-}=0$	NA
	\land Mother(y, z)	$\widehat{m_+} = 0$	$\widehat{m}_{-}=0$	NA
	\land Mother(z, x)	$\widehat{m_+} = 0$	$\widehat{m}_{-}=0$	NA
	\land Mother (z, y)	$\widehat{m_+}=1$	$\widehat{m}_{-}=0$	1
	$\land Sibling(x, y)$	$\widehat{m_+} = 0$	$\widehat{m}_{-}=0$	NA
	$\land Sibling(x,z)$	$\widehat{m_+} = 0$	$\widehat{m}_{-}=0$	NA
Father(x, y)	\land Sibling(y, x)	$\widehat{m_+} = 0$	$\widehat{m}_{-}=0$	NA
$\leftarrow Couple(x, z)$	\land Sibling (y,z)	$\widehat{m_+} = 0$	$\widehat{m}_{-}=0$	NA
	$\land Sibling(z, x)$	$\widehat{m_+} = 0$	$\widehat{m}_{-}=0$	NA
	\land Sibling (z, y)	$\widehat{m_+} = 0$	$\widehat{m}_{-}=0$	NA
	$\land Couple(x, y)$	$\widehat{m_+} = 0$	$\widehat{m}_{-}=1$	NA
	$\land Couple(x, z)$	$\widehat{m_+} = 1$	$\widehat{m}_{-}=1$	0
	$\land Couple(y, x)$	$\widehat{m_+} = 0$	$\widehat{m}_{-}=0$	NA
	$\land Couple(y, z)$	$\widehat{m_+} = 0$	$\widehat{m}_{-}=0$	NA
	$\land Couple(z, x)$	$\widehat{m_+} = 0$	$\widehat{m}_{-}=0$	NA
	$\land Couple(z, y)$	$\widehat{m_+} = 0$	$\widehat{m}_{-}=0$	NA

知识图谱推理: FOIL

 $(\forall x)(\forall y)(\forall z)(Mother(z, y) \land Couple(x, z) \rightarrow Father(x, y))$



前提约束谓词(学习得到)

目标谓词(已知)

• 推理手段: examples(positive + negative + background) ⇒ hypothesis

背			
景		目标	Father(David, Mike)
知	Sibling(Ann, Mike)	谓词	 ¬Father(David, James)
识	Couple(David, James)	ると	¬rather(David, James)
 1 '	_ ` `	训练	\neg Father(James, Ann)
样	Mother(James, Ann)	样例	Eathon(Iomas Miles)
例	Mother(James, Mike)	住人	¬Father(James, Mike)
集	inother (sumes, wince)	集合	¬Father(Ann, Mike)
合			,

给定目标谓词,FOIL算法从实例 (正例、反例、背景样例)出发, 不断测试所得到推理规则是否还包 含反例,一旦不包含负例,则学习 结束,展示了"归纳学习"能力。

知识图谱推理: FOIL

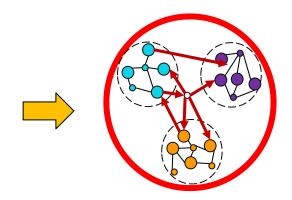
	FOIL算法				
输入:	目标谓词 P , P 的训练样例(正例集合 E^+ 和反例集合 E^-),其他背景知识				
1A -1-	•				
输出:	推导得到目标谓词P的推理规则				
1	将目标谓词作为所学习推理规则的结论				
2	将其他谓词逐一作为前提约束谓词加入推理规则,计算所得到推理规则的FOIL信息增益值,选取最优前提约束谓词以生成新推理规则,并将训练样例集合中与该推理规则不符的样例去掉				
3	重复2过程,直到所得到的推理规则不覆盖任意反例				

知识图谱推理



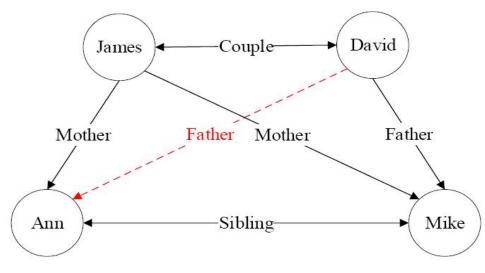
推理机

- 概念
- 实体
- 属性
- 关系



知识图谱的扩充

Score(Father(David, Ann))



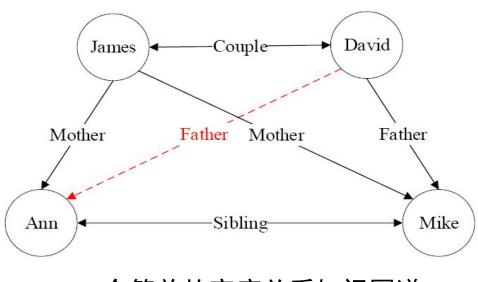
一个简单的家庭关系知识图谱

将实体之间的关联路径作为特征, 来学习目标关系的分类器

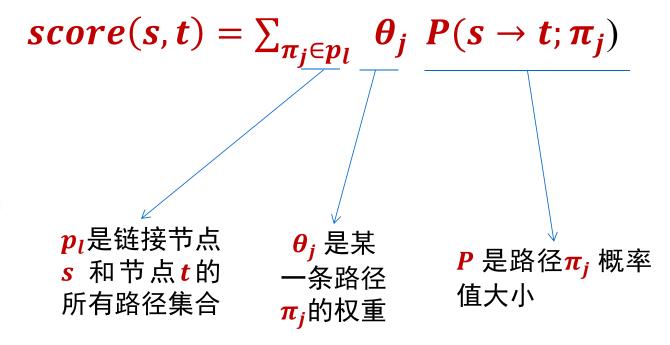
即:判断David和Ann之间的路径关联是否足够支持表述*Father*这一关系。

Ni Lao, William W. Cohen, Relational retrieval using a combination of path-constrained random walks, *Machine learning*, 2010, 81(1): 53-67, 2010

Score(Father(David, Ann))

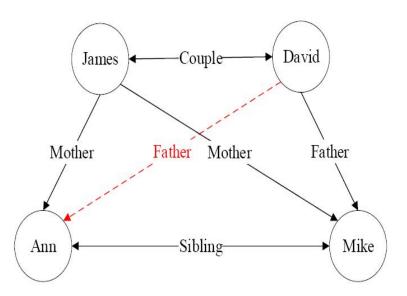


一个简单的家庭关系知识图谱



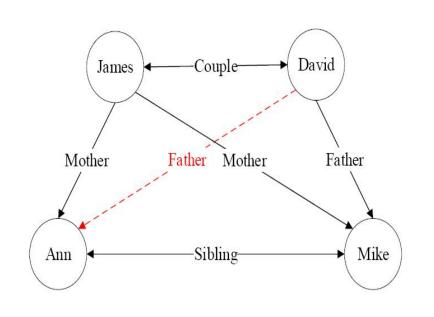
$$score(s,t) = \sum_{\pi_j \in p_l} \theta_j P(s \rightarrow t; \pi_j)$$

Score(Father(David, Ann))



- 特征抽取:生成并选择路径特征集合。生成路径的方式有随机游走(random walk)、广度优先搜索、深度优先搜索等。
- **特征计算**: 计算每个训练样例的特征值 $P(s \to t; \pi_j)$ 。该特征值可以表示从实体节点s出发,通过关系路径 π_j 到达实体节点t的概率;也可以表示为布尔值,表示实体s到实体t之间是否存在路径 π_j ; 还可以是实体s和实体t之间路径出现频次、频率等。
- 分类器训练:根据训练样例的特征值,为目标关系训练分类器。当训练好分类器后,即可将该分类器用于推理两个实体之间是否存在目标关系。

Score(Father(David, Ann))



$$score(s,t) = \sum_{\pi_i \in p_l} \theta_j \ father(s \rightarrow t; \pi_j)$$

给定目标关系: Father(s,t)

1. 对于目标关系Father,生成四组训练样例,一个为

正例、三个为负例:

正例: (David, Mike)

负例: (David, James), (James, Ann), (James, Mike)

2. 从知识图谱采样得到路径,每一路径链接上述每个训

练样例中两个实体:

(David, Mike)对应路径: Couple → Mother

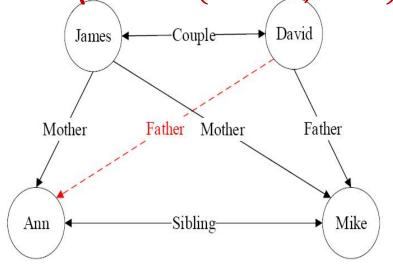
(David, James)对应路径: Father → Mother⁻¹

(Mother⁻¹与 Mother为相反关系)

(James, Ann)对应路径: *Mother* → *Sibling*

(James, Mike)对应路径: Couple → Father

Score(Father(David, Ann))



$$score(s,t) = \sum_{\pi_j \in p_l} \theta_j \ father(s \to t; \pi_j)$$

3. 对于每一个正例/负例,判断上述四条路径可否链接其 包含的两个实体,将可链接(记为1)和不可链接(记为0)作 为特征,于是每一个正例/负例得到一个四维特征向量:

(David, Mike): {[1, 0, 0, 0], 1}

(David, Mike)对应路径: Couple → Mother <<

(David, James)对应路径: Father → Mother →

(Mother⁻¹与 Mother为相反关系)

(James, Ann)对应路径: *Mother* → *Sibling* ←

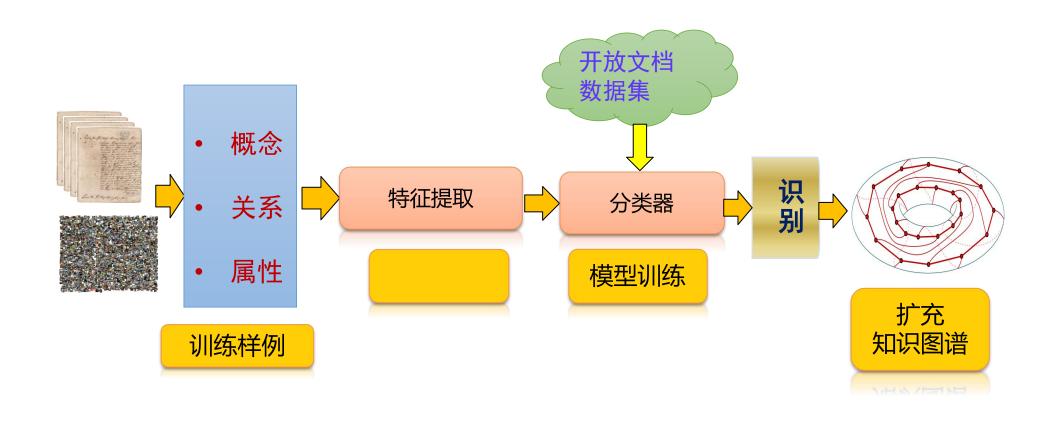
(James, Mike)对应路径: Couple 4. Poths 编样本,训练分类器M

(David, James): $\{[0, 1, 0, 0], -1\}$

Gauss Ann): $\{[0, 0, 1, 0], -1\}$

(Iames, Mike): $\{[0, 0, 1, 1], -1\}$

知识图谱推理: 机器学习



知识图谱构造流程:以Wiki为例子

正文描述

William Henry "Bill" Gates III
(born October 28, 1955) is an
American business magnate,
investor, programmer, inventor and
philanthropist. [2][3][4] Gates is
the former chief executive and
chairman of Microsoft, the
world's largest personal-computer
software company, which he cofounded with Paul Allen.

Gates was born in Seattle, Washington, to William H. Gates, Sr. and Marx Maxwell Gates. His ancestry includes English, German, and Scots-Irish. [15][16] His father was a prominent lawyer, and his mother served on the board of directors for First Interstate BancSystem and the United Way. Gates's maternal grandfather was IW Maxwell, a national bank president. After being named one of Good Housekeeping's "50 Most Eligible Bachelors" in 1985, [71] Gates married Melinda French on January 1, 1994 They have three children: daughters Jennifer Katharine (b. 1996) and Phoebe Adele (b. 2002), and on Rory John (b. 1999). The family resides in



Born William Henry Gates III October 28, 1955 (age 58) Seattle, WA, US Resi dence Medina, WA, US Alma mater Harvard University (dropped out) Children Jennifer, Rory, and Phoebe Parents William H. Gates, Sr. Mary Maxwell Gates William H. Dato III Signature

属性定义 及描述

44个 类别 标签

Categories: Bill Gates | 1955 births | American billionaires | American chairmen of corporations | American computer businesspeople | American computer programmers | American financiers | American humanitarians | American inventors | American investors | American nonprofit chief executives | American people of English descent | American people of German descent | American people of Scotch-Trish descent | American people | American philanthropists | American Roman Catholics | American software engineers | American technology chief executives | American technology chief executives | American technology chief executives | American technology writers | Big History | Bill & Melinda Gates Foundation people | Business people from Seattle | Businesspeople in software | Directors of Berkshire Hathaway | Directors of Microsoft | Fellows of the British Camputer Society | Gates family | Giving Pledgers | Harvard University people | History of Computing | History of Microsoft | Honorary Knights Commander of the Order of the British Empire | Lakeside School alumni | Living people | Members of the United States National Academy of Engineering | Microsoft employees | National Medal of Technology recipients | Personal computing | People from King County, Washington | Placards of the Order of the Atter Easle (Mexico) | Vindows people | Viviters from Seattle, Washington |

Wiki中用户对"Bill Gates"这个实例的标注

知识图谱构造流程:以Wiki为例子

William Henry "Bill" Gates III (born October 28, 1955) is an American business magnate, investor, programmer, inventor and philanthropist. [2][3][4] Gates is the former chief executive and chairman of Microsoft, the world's largest personal-computer software company, which he cofounded with Paul Allen.

Gates was born in Seattle, Washington,

to William H. Gates, Sr. and Mary Maxwell Gates. His ancestry includes English, German, and Scots-Irish. [15][16] His father was a prominent lawyer, and his mother served on the board of directors for First Interstate BancSystem and the United Way. Gates's maternal grandfather was JW Maxwell, a national bank president. After being named one of Good Housekeeping's "50 Most Eligible Bachelors" in 1985, [71] Gates marri Melinda French on January 1, 1994, They have three children: daughters Jennifer Katharine (b. 1996) and Phoebe Adele (b. 2002), and on Rory John (b. 1999). The family resides in



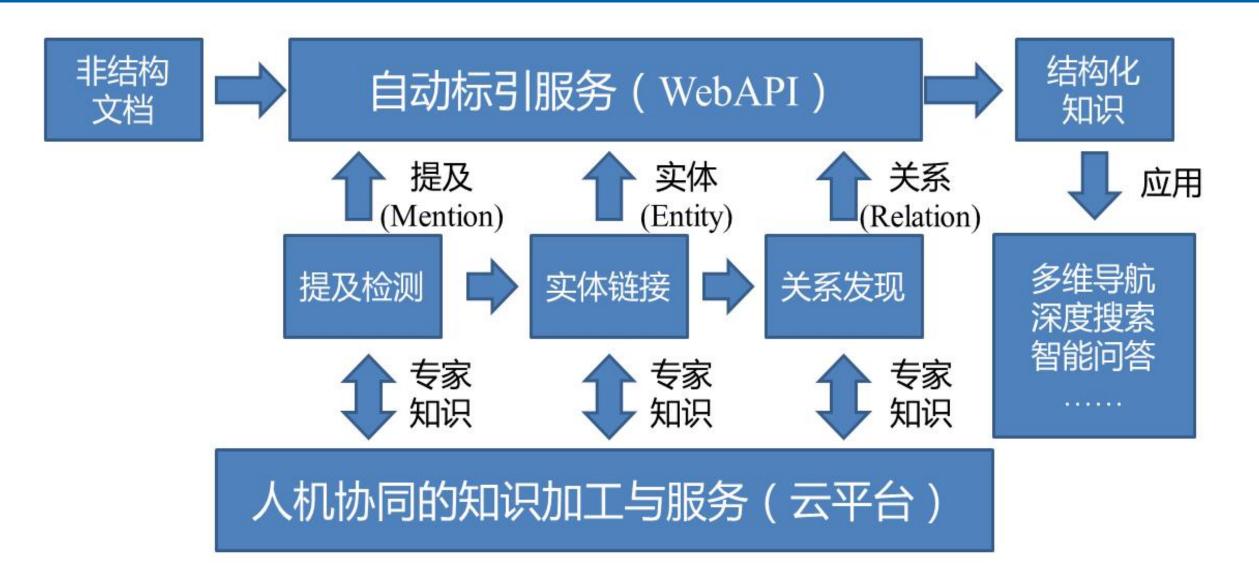
William H. Dato III

Categories: Bill Gates | 1955 births | American billionaires | American chairmen of corporations | American computer businesspeople | American computer programmers | American financiers |
American humanitarians | American inventors | American investors | American nonprofit chief executives | American people of English descent | American people of Gorman descent |
American people of Scotch-Irish descent | American people of Scotch-Irish descent | American people of Scotch-Irish descent | American people of Scotch-Irish descent | American people of Scotch-Irish descent | American people of Scotch-Irish descent | American people of Scotch-Irish descent | American people of Scotch-Irish descent | American people of Scotch-Irish descent | American people of Scotch-Irish descent | American people of Scotch-Irish descent | American people of Scotch-Irish descent | American people of Scotch-Irish descent | American people of Scotch-Irish descent | American people of Scotch-Irish descent | American people of Scotch-Irish descent | American people of Scotch-Irish descent | American people of Scotch-Irish descent | American people of Scotch-Irish descent | American people of Scotch-Irish descent | American people of Scotch-Irish descent | American people of Scotch-Irish descent | American people of Scotch-Irish descent | American people of Scotch-Irish descent | American people of Scotch-Irish descent | American people of Scotch-Irish descent | American people of Scotch-Irish descent | American people of Scotch-Irish descent | American people of Scotch-Irish descent | American people of Scotch-Irish descent | American people of Scotch-Irish descent | American people of Scotch-Irish descent | American people of Scotch-Irish descent | American people of Scotch-Irish descent | American people of Scotch-Irish descent | American people of Scotch-Irish descent | American people of Scotch-Irish descent | American people of Scotch-Irish descent | American people of Scotch-Irish descent | American people of Scotch-Irish descent |

从概念的专业分类(taxonomy)到大众分类(folksonomy),即用户趋向于用自我定义的标签对内容进行组织和分类。

44个类别标签: Bill Gates,1955 births, American billionaires, American chairmen of corporations, American computer, business people, American computer programmers, American financiers, American humanitarians, American inventors, American investors, American nonprofit chief executives, American people of English descent, American people of German descent, American people of Scotch-Irish descent, American people of Scottish descent, American philanthropists, American Roman Catholics, American software engineers, American technology chief executives ,American technology company founders, American technology writers, Big History, Bill & Melinda Gates Foundation, people Business, people from Seattle, Business people in software, Directors of Berkshire Hathaway.....

知识图谱: 从数据到知识、从知识到决策



提纲

- 命题逻辑
- 谓词逻辑
- 知识图谱推理
- 因果推理

相关不意味着因果



致酒行 (唐-李贺)

零落栖迟一杯酒,主人奉觞客长寿。 主父西游困不归,家人折断门前柳。 吾闻马周昔作新丰客,天荒地老无人识。 空将笺上两行书, 直犯龙颜请恩泽。 我有迷魂招不得, 雄鸡一声天下白。 少年心事当拿云, 谁念幽寒坐呜呃。

公鸡打鸣与太阳升起

1973年伯克利本科生录取率

	男生		女	生
	申请数	录取率	申请数	录取率
整体	8442	44%	4321	35%

男生录取率(44%)远高于女生(35%)

	男	男生		生
学院	申请数	录取率	申请数	录取率
A	825	62%	108	82%
В	560	63%	25	68%
С	325	37%	593	34%
D	417	33%	375	35%
Е	191	28%	393	24%
F	373	6%	341	7%

6个最大的院系中,4个院系女生录取率大于男生。如果按照这样的分类,女生实际上比男生的录取率还高一点点。

女生更愿意申请那些竞争压力很大的院系(比如英语系),但是男生却 更愿意申请那些相对容易进的院系(比如工程学系)。

P.J. Bickel, E.A. Hammel, J.W. O'Connell, Sex bias in graduate admissions: Data from Berkeley, *Science*, 187(4175):398-404,1975

- 计算机学院学生的高个率高于文学院(左表)。
 - 分别比较两所学院男生和女生身高时,却发现计算机学院男生和女生的高个率均低于文学院
- 在总体样本上成立的某种关系却在分组样本里恰好相反。

身高(cm)	计算机	文学院
矮个人数	60	80
高个人数	290	270
高个率(%)	82.9	77.1

	计算机学院		文等	学院
身高(cm)	男生	女生	男生	女生
矮个人数	35	25	10	70
高个人数	235	55	80	190
高个率(%)	87	68.9	88.9	73.1

 $\frac{b}{a} < \frac{d}{c}, \frac{b'}{a'} < \frac{d'}{c'}$ $\frac{b}{a + a'} > \frac{d + d'}{c + c'}$

左: 计算机学院和文学院 学生的身高情况 右:以性别分组后的计算机学院 和文学院的学生身高情况

• 右表体现了男生比女生个子高这一现象

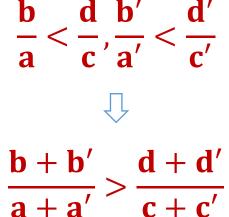
- 如计算机学院和文学院男生高个率都比女生高个率要大
- •性别会影响专业选择,计算机男生多,而文学院女生多。因此, 当计算机学院的样本中包含更多的男生,就会看到左表所呈现 的情况:计算机学院的高个率高于文学院。

身高(cm)	计算机	文学院
矮个人数	60	80
高个人数	290	270
高个率(%)	82.9	77.1

	计算机学院		文学院	
身高(cm)	男生	女生	男生	女生
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左: 计算机学院和文学院 学生的身高情况

右:以性别分组后的计算机学院 和文学院的学生身高情况



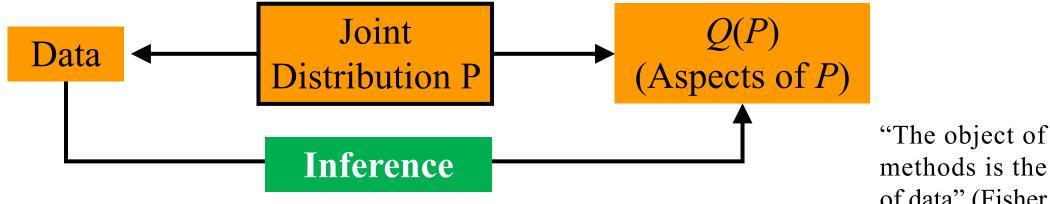
·辛普森悖论表明,在某些情况下,忽略潜在的"第三个变量" (如性别就是专业和身高之外的第三个变量),可能会改变 已有的结论,而我们常常却一无所知。从观测结果中寻找引 发结果的原因,由果溯因,就是本节要介绍的因果推理

不能只满足于数字或图表,必须考虑数据生成

过程——因果模型

因果推理: Causal Inference

• 传统以统计建模为核心的推理手段

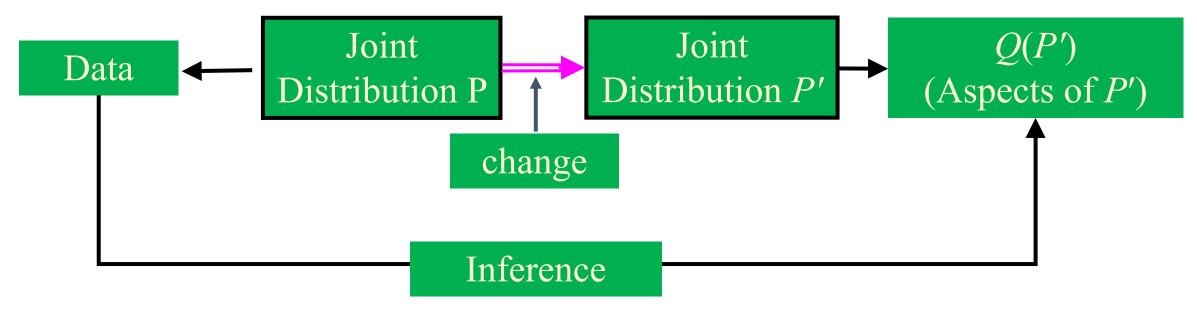


"The object of statistical methods is the reduction of data" (Fisher 1922).

购买了A商品的顾客是否会购买B商品(对A和B的联合分布建模) $Q = P(B \mid A)$

因果推理: Causal Inference

- ●如果商品价格涨价一倍,预测销售量P'(sales)的变化
- ●如果放弃吸烟,预测癌症P'(cancer)的概率



数据分布从 P 变换到 P'

因果推理的层级

- Actions: B will be true if we do A.
- Counterfactuals: B would be different if A were true

可观测性问题 (关联)	What if we see A	P(y A)		
决策行动问题 (干预)	What if we do A	P(y do(A))(如果采取A行为,则B真)		
反事实问题 (Counterfactual)	What if we did things differently	P(y' A) (如果A为真,则B将不同)		
Options: with what probability				

因果推理模型: 结构因果模型和因果图

- 结构因果模型(structural causal model, SCM)
 - 也被称为因果模型(causal model)或Neyman-Rubin因果模型
 - Jerzy Neyman在1923年博士论文中(波兰语)提出的"潜在结果" (potential outcome) 的概念
 - •之后, Donald Rubin发展了"潜在结果"这一概念,并将其和缺失数据的理论联系在一起。
- 因果图(causal diagram)由Judea Pearl于 1995年提出。
- •每个结构因果模型M都与一个因果图G相对应

因果推理: 有向无环图

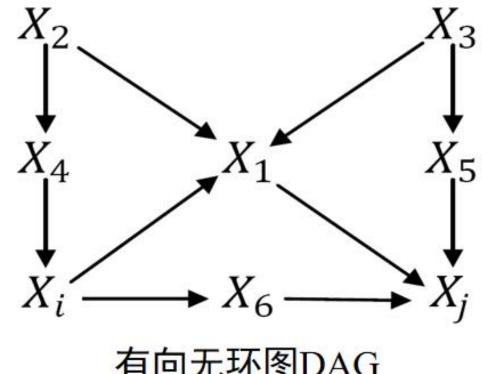
- 有向无环图(directed acyclic graphs, DAG)
 - 一个无回路的有向图,即从图中任意一个节点出发经过任意条边,均无法回到该节点。刻画了图中所有节点之间的依赖关系。
- · DAG 可用于描述数据的生成机制
 - 这样描述变量联合分布或者数据生成机制的模型,被称为"贝叶斯网络"(Bayesian network)

•对于任意的DAG,模型中d 个变量的联合概率分布由每个节点与其父节点之间条件概率P (c h i l d |p a r e n t s) 的乘积给出:

$$P(x_1, x_2, \dots, x_d) = \prod_{j=1}^{n} P(x_j | x_{pa(j)})$$

•其中, $x_{pa(j)}$ 表示节点 x_j 的父节点集合(所有指向 x_j 的节点)

请写出下列有向无环图的联合概率形式,并区分内生变量和外生 变量。

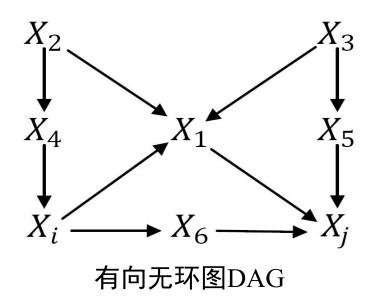


有向无环图DAG

正常使用主观题需2.0以上版本雨课堂

作答

- •一个有向无环图唯一地决定了一个联合分布
- •一个联合分布不能唯一地决定有向无环图
 - 反过来的结论不成立
 - 如联合分布 $P(X_1, X_2) = P(x_1)P(x_2|x_1) = P(x_2)P(x_1|x_2)$



联合分布可表示为:

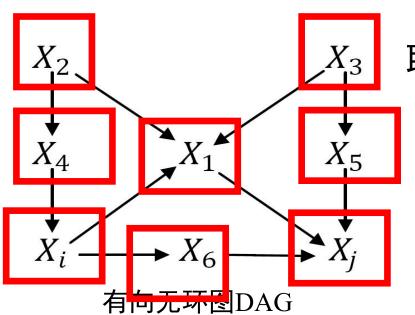
$$P(X_{1}, X_{2}, X_{3}, X_{4}, X_{5}, X_{6}, X_{i}, X_{j})$$

$$= P(X_{2}) \times P(X_{3}) \times P(X_{1}|X_{2}, X_{3}, X_{i})$$

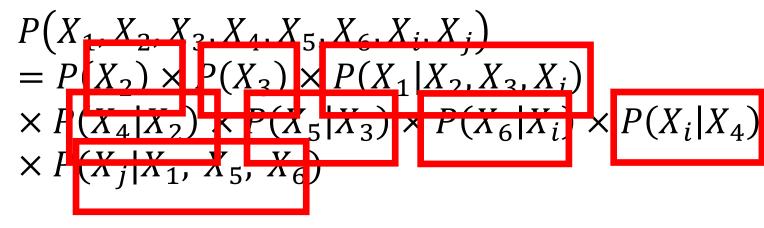
$$\times P(X_{4}|X_{2}) \times P(X_{5}|X_{3}) \times P(X_{6}|X_{i}) \times P(X_{i}|X_{4})$$

$$\times P(X_{j}|X_{1}, X_{5}, X_{6})$$

- •一个有向无环图唯一地决定了一个联合分布
- •一个联合分布不能唯一地决定有向无环图
 - 反过来的结论不成立
 - 如联合分布 $P(X_1, X_2) = P(x_1)P(x_2|x_1) = P(x_2)P(x_1|x_2)$



联合分布可表示为:



- •例:假设某个有向无环图中存在一条依赖路径 $X \to Y \to Z$,其中X表示气候好,Y表示水果产量高,Z表示水果价格低,给出P(气候好,水果产量高,水果价格低)的联合概率。
 - 使用乘积分解规则,将P(气候好,产量高,价格低)转换为: P(气候好)×P(价格低 产量高)

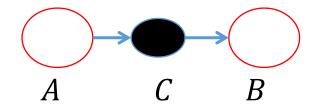
假设:

P(气候好) = 0.5 P(产量高|气候好) = 0.8 P(价格低|产量高) = 0.9 P(气候好,产量高,价格低) = $0.5 \times 0.8 \times 0.9 = 0.36$

• D -分离用于判断集合A 中变量是否与集合B 中变量相互独立(给定集合C),记为 $A \perp B \mid C$ D-分离的例子

(serial connection)

· 当C取值固定(可观测, observed), 有



$$P(A, B|C) = \frac{P(A,B,C)}{P(C)} = \frac{P(A)P(C|A)P(B|C)}{P(C)} = P(A|C)P(B|C)$$

- ·可见A和B在C取值固定情况下,是条件独立的
 - •注:上式利用了P(A)P(C|A)=P(C)P(A|C)

- D -分离用于判断集合A 中变量是否与集合B 中变量相互独立
 - (给定集合C),记为 $A \perp B \mid C$
- ·当C取值固定(observed),有

D-分离的例子 (diverging connection)



$$P(A, B|C) = \frac{P(A,B,C)}{P(C)} = \frac{P(C)P(A|C)P(B|C)}{P(C)} = P(A|C)P(B|C)$$

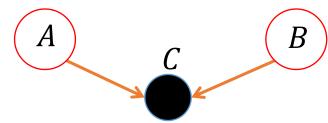
- ·可见A和B在C取值固定情况下,是条件独立的
 - •如果C不固定,则有 $P(A,B) = \sum_{C} P(A|B)P(B|C)P(C)$
 - 由于 $P(A,B) \neq P(A)P(B)$, 因此A和B在条件C下不独立的

• D -分离用于判断集合A 中变量是否与集合B 中变量相互独立

(给定集合C), 记为 $A \perp B \mid C$ $P(A, B, C) = P(A)P(B)P(C \mid A, B)$

· 当C取值固定(observed)

D-分离的例子 (V-structure connection)



$$P(A, B|C) = \frac{P(A, B, C)}{P(C)} = \frac{P(A)P(B)P(C|A, B)}{P(C)} \neq P(A)P(B)$$

· A和B在条件C下是不独立的(是相关的)

• D -分离用于判断集合A 中变量是否与集合B 中变量相互独立

(给定集合C), 记为 $A \perp B \mid C$ $P(A, B, C) = P(A)P(B)P(C \mid A, B)$

· 当C不作为观测点, A和B是独立的

D-分离的例子 (V-structure connection)

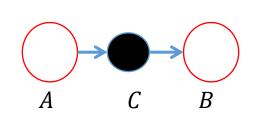
$$P(A,B) = \sum_{C} (P(A)P(B)P(C|A,B)) = P(A)P(B) \sum_{C} P(C|A,B)$$

$$= 1$$

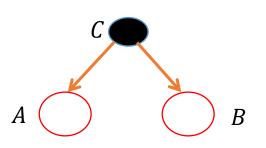
链结构(chain)	分连结构(fork)	汇连(或碰撞)结构 (collider)	
U_1 U_2 X U_3 Z Y	U_2 U_3 X Y	U_1 U_3 Y Z	
Z和X是相关的	X和Z是相关的	Z和X是相关的	
Y和Z是相关的	Y和Z是相关的	Z和Y是相关的	
Y和X很有可能是相关的	Y和X很有可能是相关的	Y和X是相互独立的	
给定Z时, Y和X是条件独立的	给定Z时, Y和X是条件独立的	给定Z时,Y和X是相关的	

- *D*-分离:对于一个DAG图,如果*A、B、C*是三个集合(可以是单独的节点或者是节点的集合),为了判断*A*和*B* 是否是 *C* 条件独立的,在DAG图中考虑所有*A*和*B*之间的路径(不管方向)。对于其中的一条路径,如果满足以下两个条件中的任意一条,则称这条路径是阻塞(block)的:路径中存在节点*X*
 - X是链结构或分连结构节点, 且 $X \in C$
 - · X是汇连结构节点,并且X或X后代不包含在C中

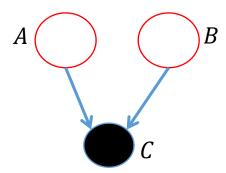
• D-分离:如果A和B之间所有路径都是阻塞的,那么A和B就是关于C条件独立的;否则A和B不是关于C条件独立



链结构



分连结构



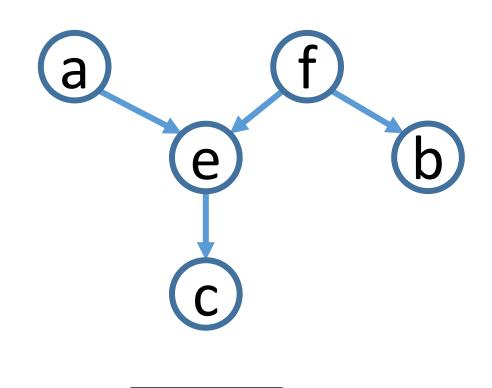
汇连结构 (V结构或冲撞点, collider)



此题未设置答案,请点击右侧设置按钮

下面描述中正确的有

- a和b是条件c下独立的
- a和b是条件e下独立的
- a和b是条件f下独立的



提交

因果推理: D-分离 (directional separation)

- D -分离方法可用于判断因果图上任意变量间相关性和独立性
- •在因果图上,若节点X 和节点Y 之间的每一条路径都是阻塞的
 - · 称节点X 和节点Y 是有向分离的
 - 反之,称节点X 和节点Y 是有向连接的
- 当两个节点是有向分离时,意味着这两个节点相互独立

因果推理: 干预(intervention)和d o 算子(do-calculus

- · DAG中具有链接箭头的节点之间存在某种"因果关系"。
- •要在 DAG 上引入"因果"的概念,需要引进do 算子
 - do-calculus的意思可理解为 "干预" (intervention)
- 在 DAG 中, $do(X_i) = x_i'$, 表示将DAG中指向节点 X_i 的有向 边全部切断,并且将 X_i 的值固定为常数 x_i'
- ·在这样操作后,所得到新的DAG中变量联合分布为:

$$P(x_1, x_2, \dots, x_d | do(X_i) = x_i')$$

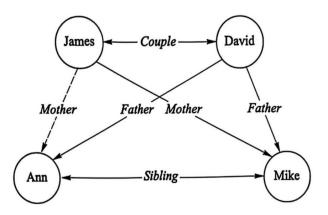
因果推理:反事实推理(counterfactual model)

- · "反事实"框架是科学哲学家大卫·刘易斯(David Lewis)等 人提出的推断因果关系的标准。
- 事实是指在某个特定变量(A)的影响下可观测到的某种状态或结果(B)。 "反事实"是指在该特定变量(A) 取负向值时可观测到的状态或结果(B')
- •条件变量对于结果变量的因果性就是A成立时B的状态与A取负向值时"反事实"状态(B')之间的差异。
- 如果这种差异存在且在统计上是显著的,说明条件变量与结果变量存在因果关系。

推理总结

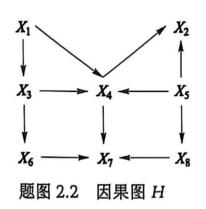
推理方法	推理方式	说明
归纳推理	如果 A_i (i 为若 干取值),那么B	从若干事实出发推理出一般性规律
演绎推理	如果A,那么B	A是B的前提、但不是唯一前提,因此A是B的充分条件。当然,在特殊情况下A也可为B的充分必要条件
因果推理	因为A, 所以B	A是B的唯一前提,因此"如果没有A,那 么没有B"也成立。

小雅课堂最后两题



题图 2.1 家庭关系

10. 如题图 2.1 所示, 试运用路径排序算法推出 James 和 Ann 的 Mother 关系。



- 12. 题图 2.2 给出了不同变量之间的依赖关系。试写出因果图 H中 8 个变量之间的联合概率形式,并区分哪些变量是内生变量、哪些变量是外生变量。
- 13° . 给出 5 个可能的限定集 Z, 使其阻塞题图 2.2 中的结点 X_{6} 和结点 X_{8} 。

谢谢!