

$$3. \quad f(t) = B_0(t) P_0 + B_1(t) P_1 + B_2(t) P_2 + B_3(t) P_3$$

$$B_0(t) = (1-t)^3 \quad B_1(t) = 3t(1-t)^2 \quad B_2(t) = 3t^2(1-t) \quad B_3(t) = t^3$$

$$t = u$$

$$f(u) = (1-u)^3 P_0 + 3u(1-u)^2 P_1 + 3u^2(1-u) P_2 + u^3 P_3$$

$$f(u)^2 = f_0$$

$$f_0 = (1-u)S_0 + uS_1 = (1-u)((1-u)\bar{v} + u\tau_1) + u((1-u)\tau_1 + u\tau_2)$$

$$= (1-u) \left[ (1-u) \left( (1-u)P_0 + uP_1 \right) + u \left( (1-u)P_1 + \bar{v}P_2 \right) \right] +$$

$$u \left[ (1-u) \left( (1-u)P_1 + vP_2 \right) + u \left( (1-u)P_2 + vP_3 \right) \right]$$

$$= (1-u)^3 P_0 + u(1-u)^2 P_1 + u(1-u)^2 P_1 + u(1-u)^2 P_1 +$$

$$u^2(1-u)P_2 + u^2(1-u)P_2 + u^2(1-u)P_2 + u^3 P_3$$

$$= (1-u)^3 P_0 + 3u(1-u)^2 P_1 + 3u^2(1-u)P_2 + u^3 P_3 = F(u)$$