

1: $p \ll 1$ 位相 $\Phi_c \rightarrow \Phi_c + \Delta\Phi_c$, $\Phi_D \rightarrow \Phi_D + \Delta\Phi_D \in L_2$ とする。 求める。

$$\begin{aligned} \Phi_H &= r t' R r' e^{i\Phi_c} (1 + p e^{i\Delta\Phi_c}) + t' R t t' e^{i\Phi_D} (1 + p e^{i\Delta\Phi_D}) \\ \Phi_0 &= r t' R t e^{i\Phi_c} (1 + p e^{i\Delta\Phi_c}) + t' R t r e^{i\Phi_D} (1 + p e^{i\Delta\Phi_D}) \end{aligned}$$

beam intensities

$$\begin{aligned} I_H &= |t' R|^2 [|r r'|^2 |1 + p e^{i\Delta\Phi_c}|^2 + |t t'|^2 |1 + p e^{i\Delta\Phi_D}|^2 \\ &\quad + 2 \operatorname{Re}(r r'^* t'^* e^{i\Phi_c} (1 + p e^{i\Delta\Phi_c} + p e^{-i\Delta\Phi_D}))] + O(p^2) \end{aligned}$$

$$\begin{aligned} &= |t|^2 |R|^2 [|r|^4 (1 + 2p \cos \Delta\Phi_c) + |t|^4 (1 + 2p \cos \Delta\Phi_D) \\ &\quad - 2 |r|^2 |t|^2 (\cos \Delta\Phi + p \cos(\Delta\Phi + \Delta\Phi_c) + p \cos(\Delta\Phi - \Delta\Phi_D))] \end{aligned}$$

$$I_{Hcd} = |r|^4 |t|^2 |R|^2 (1 + 2p \cos \Delta\Phi_c) \quad (C \text{ 区画の伝わり遅延})$$

$$\begin{aligned} I_0 &\cong |r|^2 |t|^4 |R|^2 [|1 + p e^{i\Delta\Phi_c}|^2 + |1 + p e^{i\Delta\Phi_D}|^2 + 2 \operatorname{Re}(e^{i\Delta\Phi} (1 + p e^{i\Delta\Phi_c} + p e^{-i\Delta\Phi_D}))] \\ &= |r|^2 |t|^4 |R|^2 [2 + 2p \cos \Delta\Phi_c + 2p \cos \Delta\Phi_D + 2 \cos \Delta\Phi + 2p \cos(\Delta\Phi + \Delta\Phi_c) + 2p \cos(\Delta\Phi - \Delta\Phi_D)] \end{aligned}$$

$$I_{0cd} = |r|^2 |t|^4 |R|^2 (1 + 2p \cos \Delta\Phi)$$

$$\therefore \frac{I_H/I_{Hcd} - I_0/I_{0cd}}{I_H/I_{Hcd} + I_0/I_{0cd}}$$

$$\begin{aligned} &= \left[\left(1 + \frac{|t|^4}{|r|^4} \frac{(1 + 2p \cos \Delta\Phi_D)}{(1 + 2p \cos \Delta\Phi_c)} - 2 \frac{|t|^2}{|r|^2} \frac{[\cos \Delta\Phi + p \cos(\Delta\Phi + \Delta\Phi_c) + p \cos(\Delta\Phi - \Delta\Phi_D)]}{(1 + 2p \cos \Delta\Phi_c)} \right) \right. \\ &\quad \left. - \left(1 + \frac{1 + 2p \cos \Delta\Phi_D}{1 + 2p \cos \Delta\Phi_c} + 2 \frac{\cos \Delta\Phi + p \cos(\Delta\Phi + \Delta\Phi_c) + p \cos(\Delta\Phi - \Delta\Phi_D)}{1 + 2p \cos \Delta\Phi_c} \right) \right] / \dots \end{aligned}$$

$$= \frac{\left(\frac{|t|^4}{|r|^4} - 1 \right) \frac{1 + 2p \cos \Delta\Phi_D}{1 + 2p \cos \Delta\Phi_c} - 2 \left(\frac{|t|^2}{|r|^2} - 1 \right) \frac{\cos \Delta\Phi + p \cos(\Delta\Phi + \Delta\Phi_c) + p \cos(\Delta\Phi - \Delta\Phi_D)}{1 + 2p \cos \Delta\Phi_c}}{2 + \dots}$$