

# Fitted Models

Loïc Pages

2025-06-25

## Seedlings survival

Models selected by AIC

```
ASurvglm11 <- fitme(Survie ~ 1+ bs(Size0Mars,df=4,degree=2) + (Size0Mars|year),
                    family=binomial,
                    data=survdata1,
                    method="PQL/L")

ASurvglm12 <- fitme(Survie ~ 1+ bs(Size0Mars,df=4,degree=2) + (Size0Mars|year)+ (1|Pop),
                    family=binomial,
                    data=survdata1,
                    method="PQL/L")

ASurvglm13 <- fitme(Survie ~ 1+ bs(Size0Mars,df=4,degree=2) + (1|year) + (1|Pop),
                    family=binomial,
                    data=survdata1,
                    method="PQL/L")

ASurvglm14 <- fitme(Survie ~ 1+ bs(Size0Mars,df=4,degree=2) + (1|year),
                    family=binomial,
                    data=survdata1,
                    method="PQL/L")

ASurvglm15 <- fitme(Survie ~ 1+ bs(Size0Mars,df=5,degree=3) + (Size0Mars|year),
                    family=binomial,
                    data=survdata1,
                    method="PQL/L")
```

Models selected by BIC

```
BSurvglm11 <- fitme(Survie ~ 1+ Size0Mars + (1|year) + (1|Pop),
                    family=binomial,
                    data=survdata1,
                    method="PQL/L")

BSurvglm12 <- fitme(Survie ~ 1+ Size0Mars + (1|year),
                    family=binomial,
                    data=survdata1,
                    method="PQL/L")
```

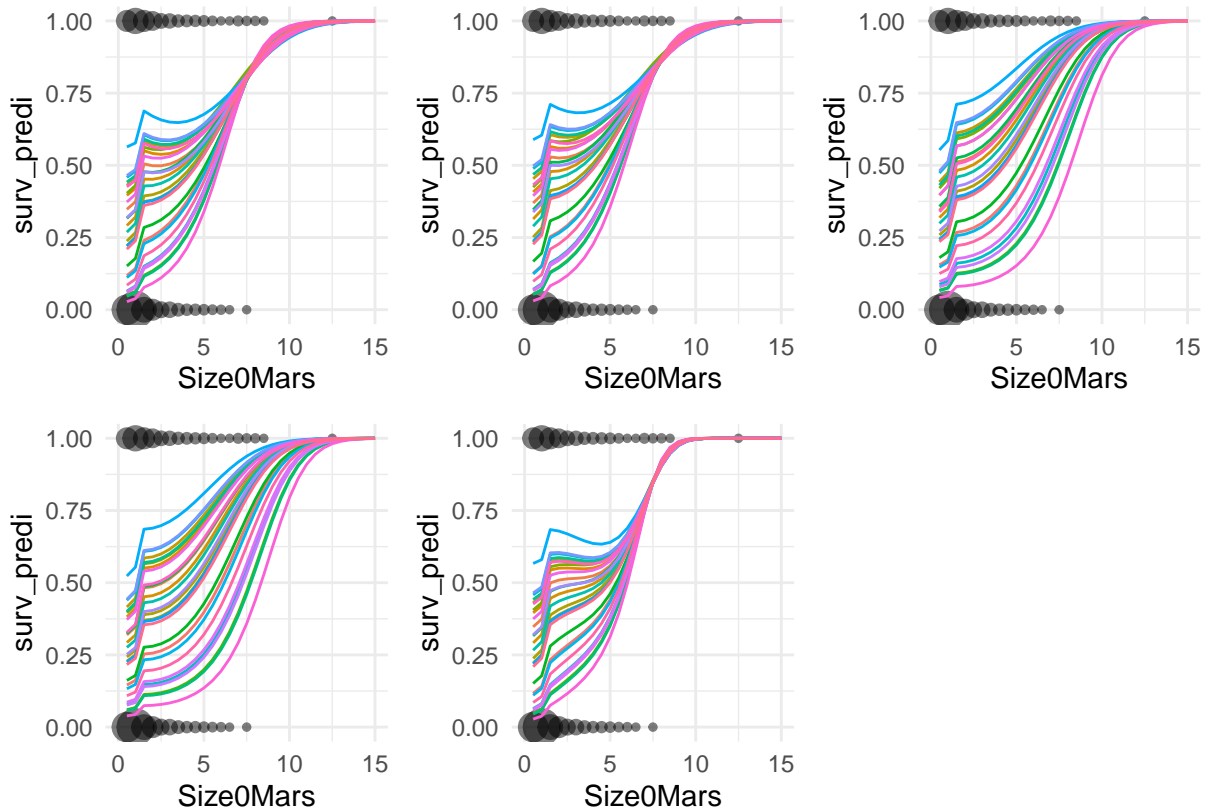
```
BSurvglm13 <- fitme(Survie ~ 1 + Size0Mars + (Size0Mars|year) + (1|Pop),
  family=binomial,
  data=survdata1,
  method="PQL/L")

BSurvglm14 <- fitme(Survie ~ 1+ Size0Mars + (Size0Mars|year),
  family=binomial,
  data=survdata1,
  method="PQL/L")

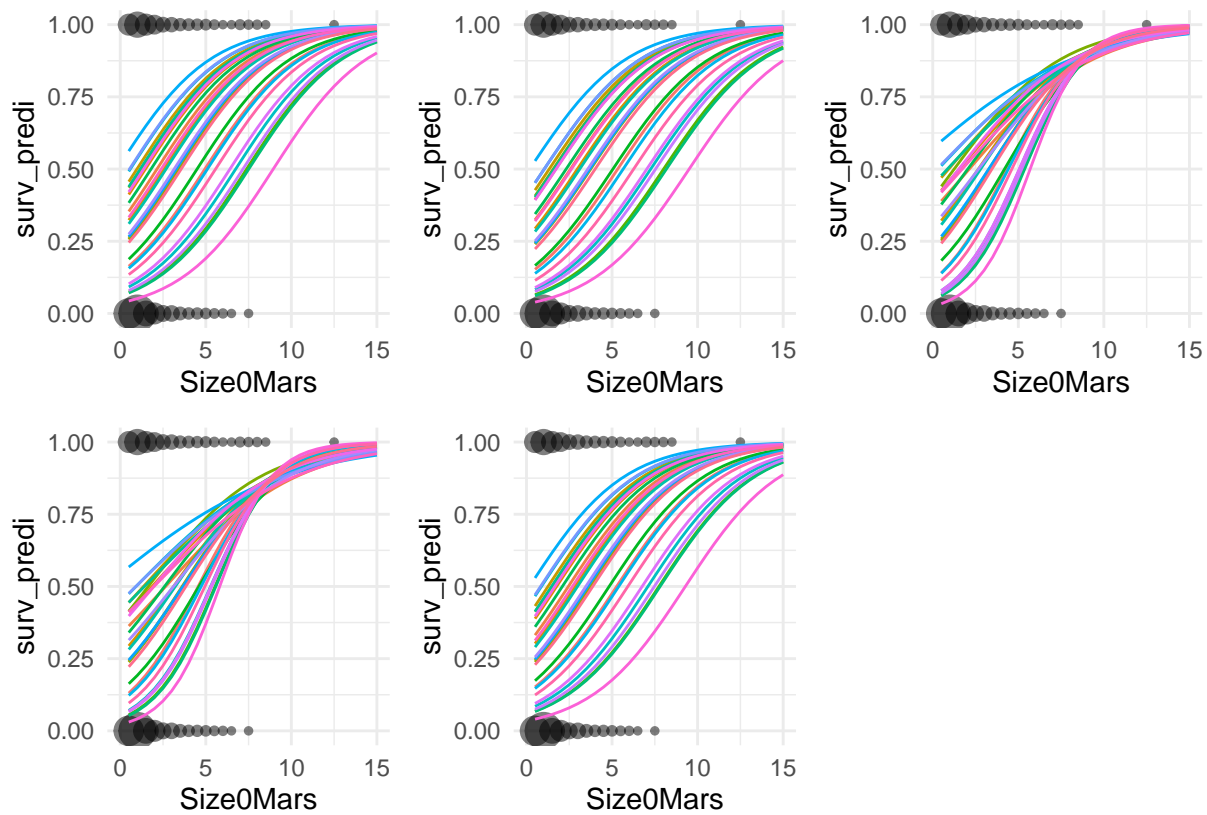
BSurvglm15 <- fitme(Survie ~ 1+ Size0Mars + (1|year) + (Size0Mars|Pop),
  family=binomial,
  data=survdata1,
  method="PQL/L")
```

As a function of size

See year effect (population fixed)

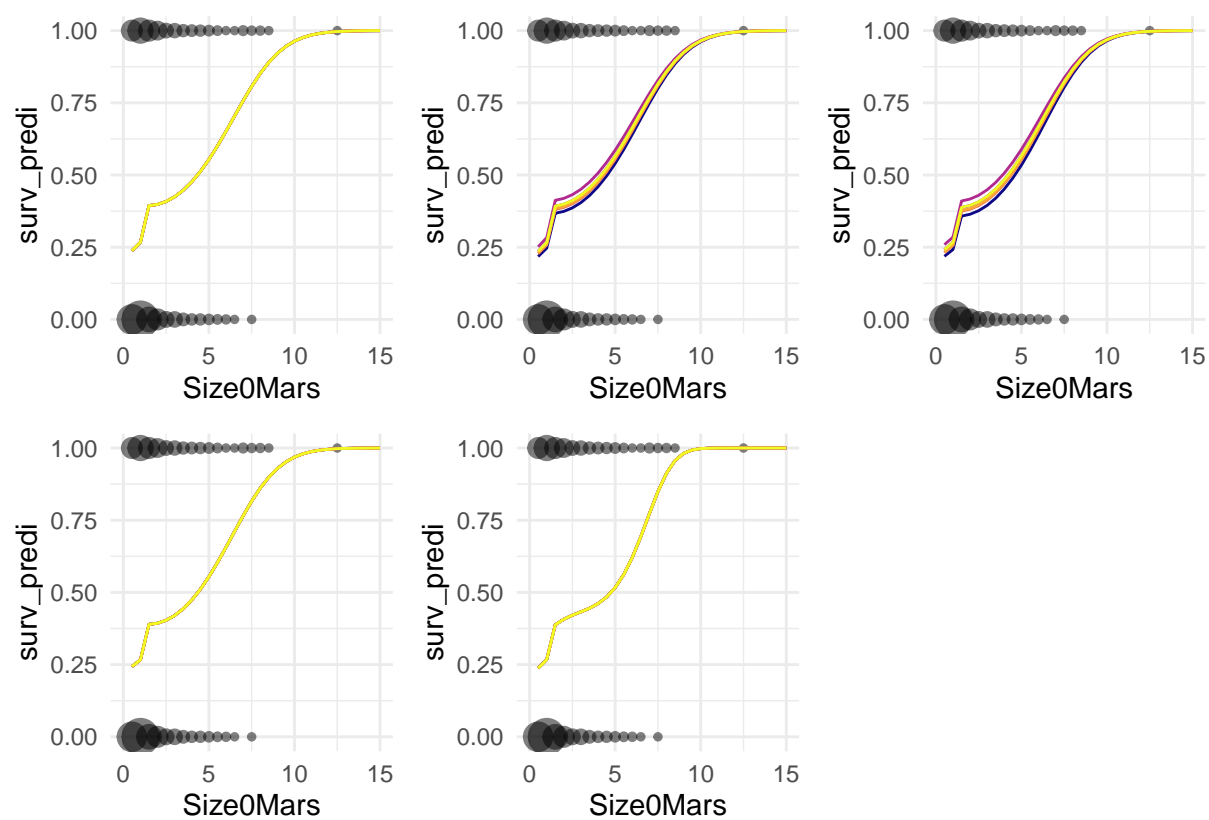


AIC

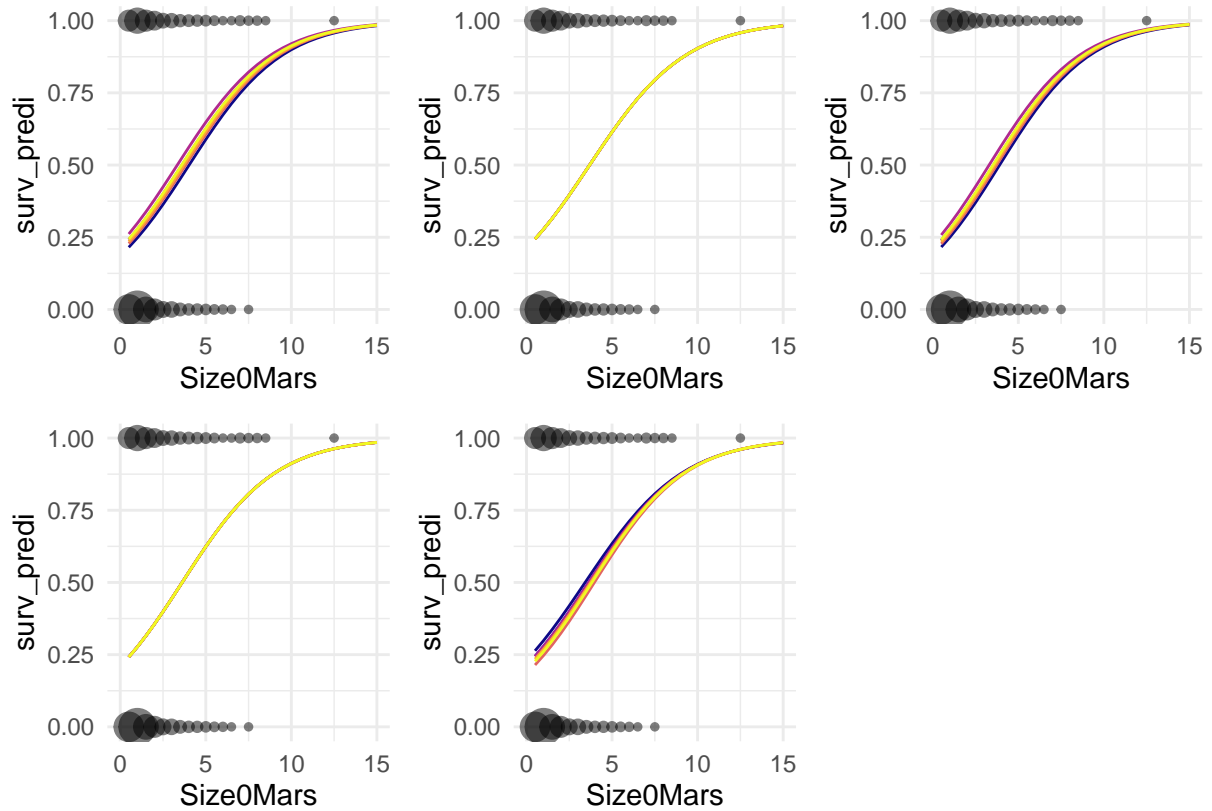


BIC

See population effect (year fixed)



AIC



BIC

## Rosette survival

AIC

```
ASurvglm21 <- fitme(Survie ~ 1+ bs(Size0Mars,df=3,degree=2) +
  bs(Age,degree=3,knots=6.5) + (Age|year) + (1|Pop),
  family=binomial,
  data=survdata2,
  method="PQL/L")

ASurvglm22 <- fitme(Survie ~ 1+ bs(Size0Mars,df=3,degree=2) +
  bs(Age,degree=3,knots=6.5) + (1|year) + (1|Pop),
  family=binomial,
  data=survdata2,
  method="PQL/L")

ASurvglm23 <- fitme(Survie ~ 1+ bs(Size0Mars,df=4,degree=2) +
  bs(Age,degree=3,knots=6.5) + (Age|year) + (1|Pop),
  family=binomial,
  data=survdata2,
  method="PQL/L")

ASurvglm24 <- fitme(Survie ~ 1 + poly(Size0Mars,4) + bs(Age,degree=3,knots=6.5)
  + (Age|year) + (1|Pop),
```

```

        family=binomial,
        data=survdata2,
        method="PQL/L")

ASurvglm25 <- fitme(Survie ~ 1+ bs(Size0Mars,df=4,degree=2) +
                    bs(Age,degree=3,knots=6.5) + (1|year) + (1|Pop),
                    family=binomial,
                    data=survdata2,
                    method="PQL/L")

```

BIC

```

BSurvglm21 <- fitme(Survie ~ 1+ bs(Size0Mars,df=3,degree=2) + (Age|year) +
                    (1|Pop),
                    family=binomial,
                    data=survdata2,
                    method="PQL/L")

BSurvglm22 <- fitme(Survie ~ 1+ poly(Size0Mars,3) + (Age|year) + (1|Pop),
                    family=binomial,
                    data=survdata2,
                    method="PQL/L")

BSurvglm23 <- fitme(Survie ~ 1 + bs(Size0Mars,df=3,degree=2) + (Age|year) +
                    (Size0Mars|Pop),
                    family=binomial,
                    data=survdata2,
                    method="PQL/L")

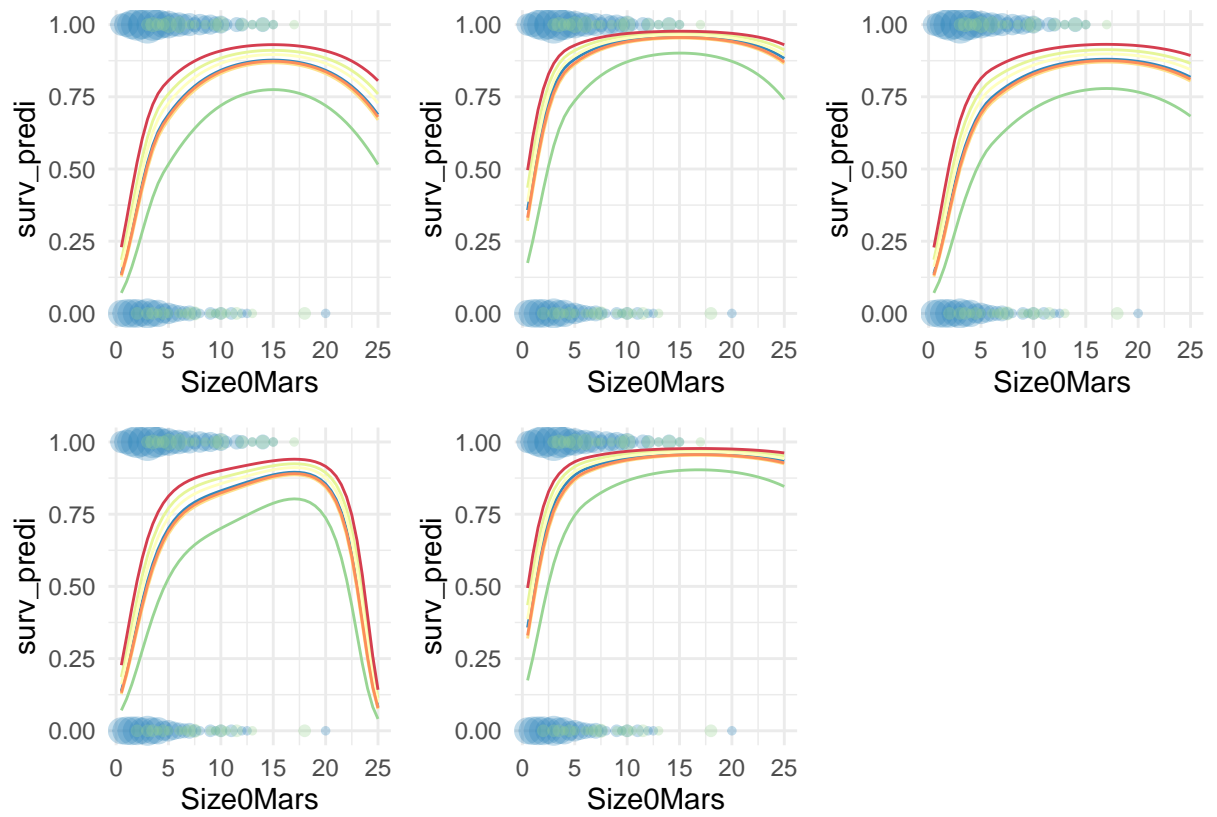
BSurvglm24 <- fitme(Survie ~ 1+ bs(Size0Mars,df=3,degree=2) + (Age|year) +
                    (Age|Pop),
                    family=binomial,
                    data=survdata2,
                    method="PQL/L")

BSurvglm25 <- fitme(Survie ~ 1+ poly(Size0Mars,2) + (Age|year) + (1|Pop),
                    family=binomial,
                    data=survdata2,
                    method="PQL/L")

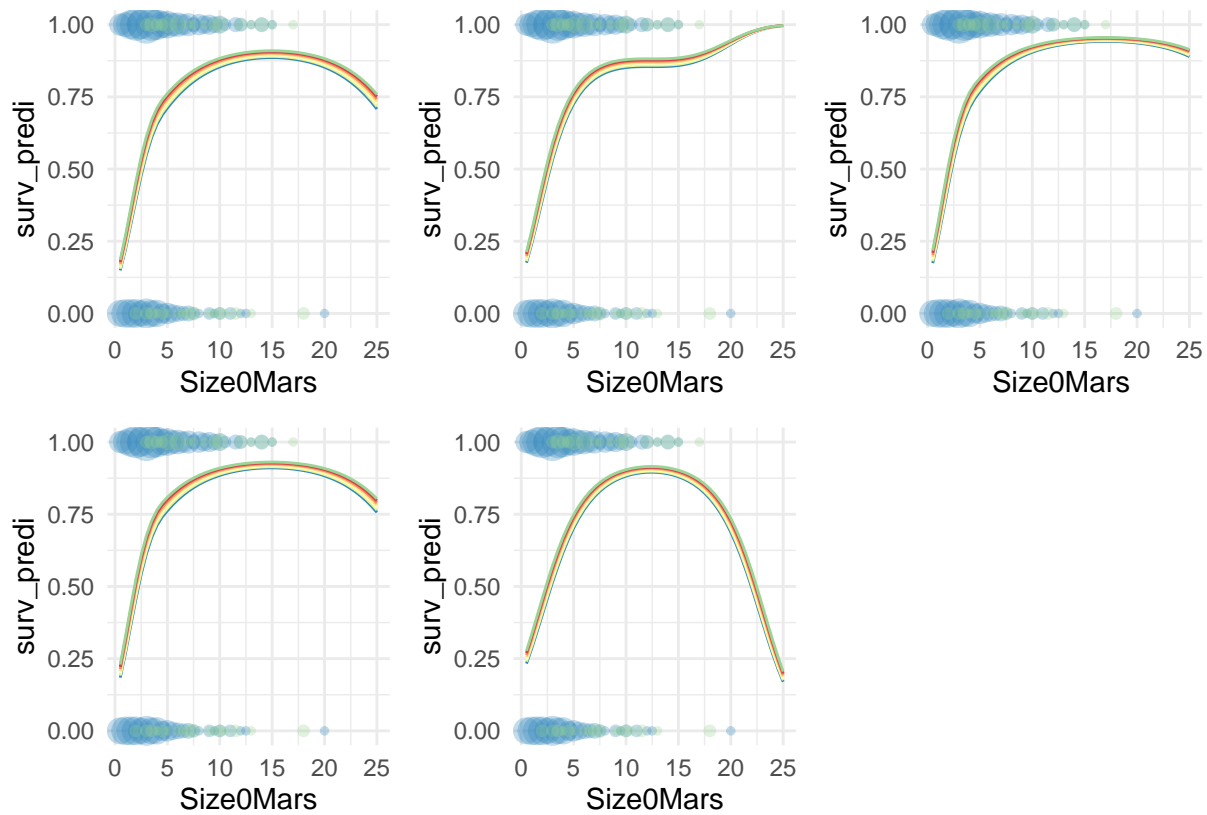
```

As a function of size

See effect of age (population and year fixed)



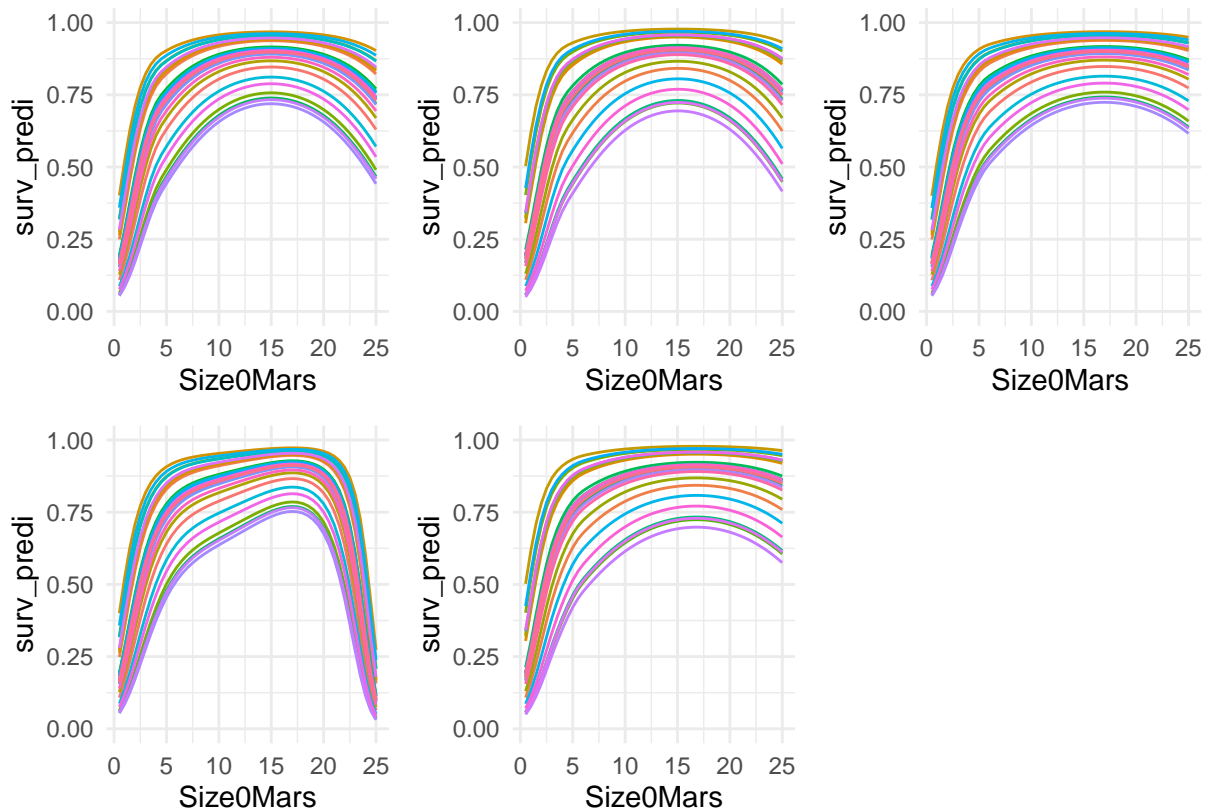
AIC



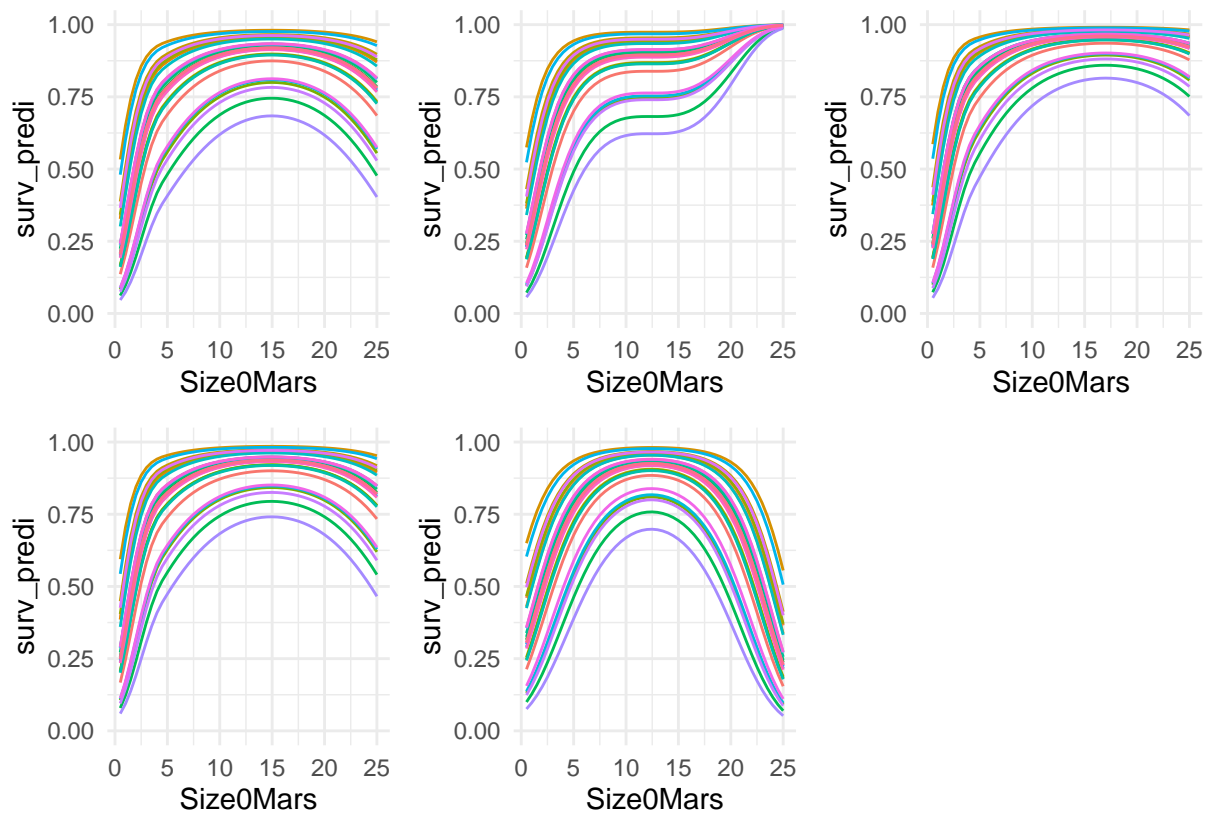
BIC



See year effect (population fixed and age=5)

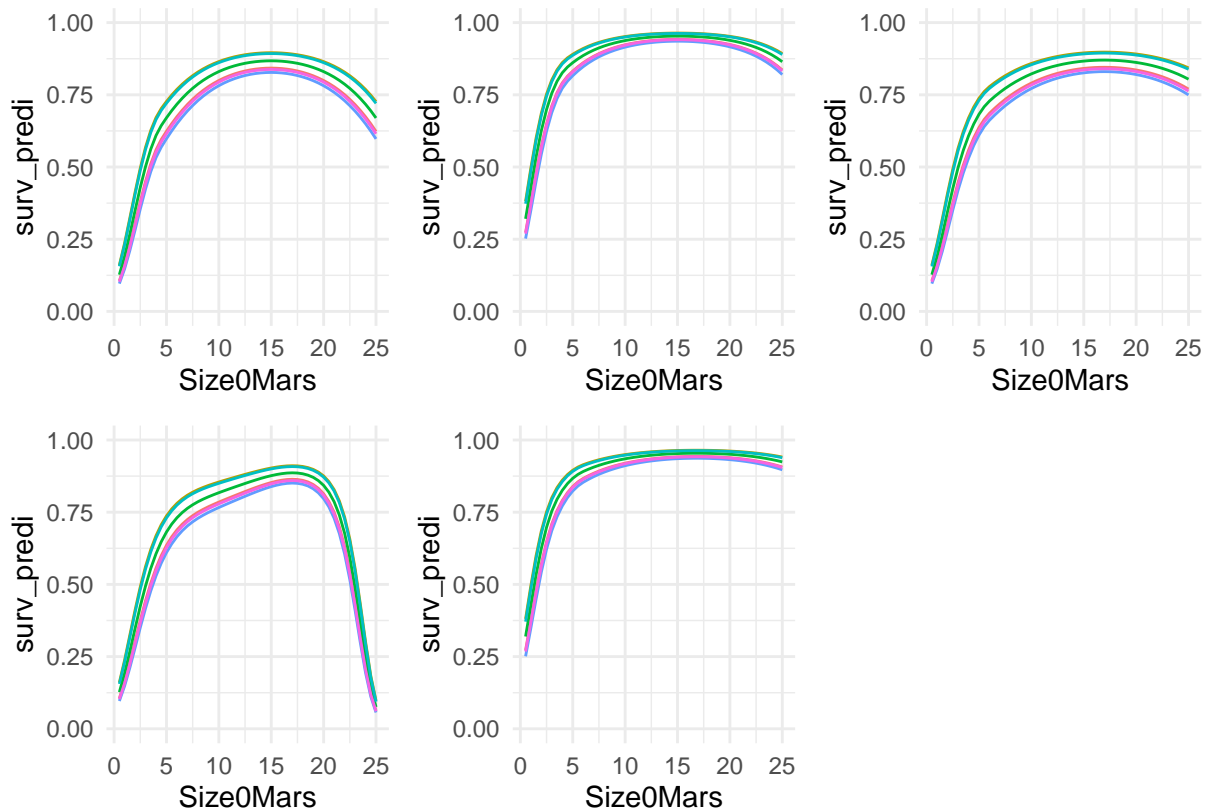


AIC

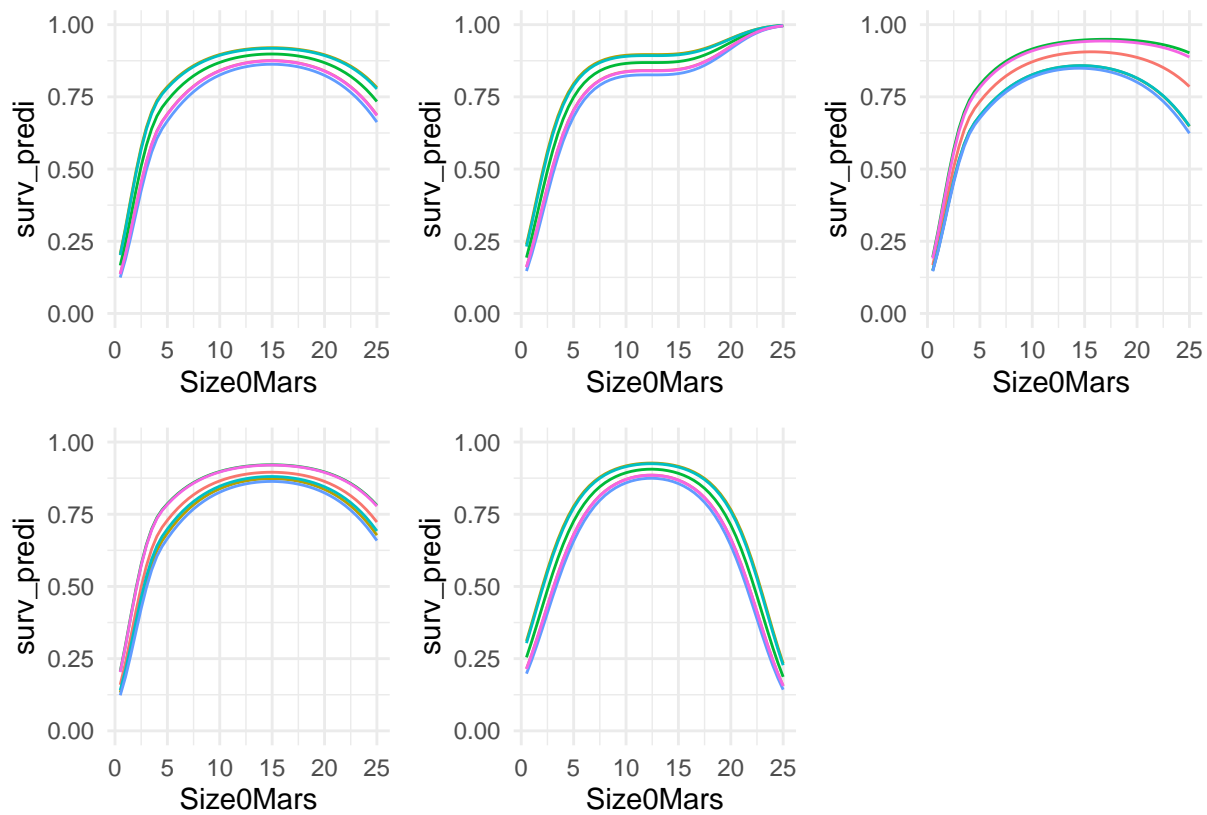


BIC

See population effect (year fixed and age=5)



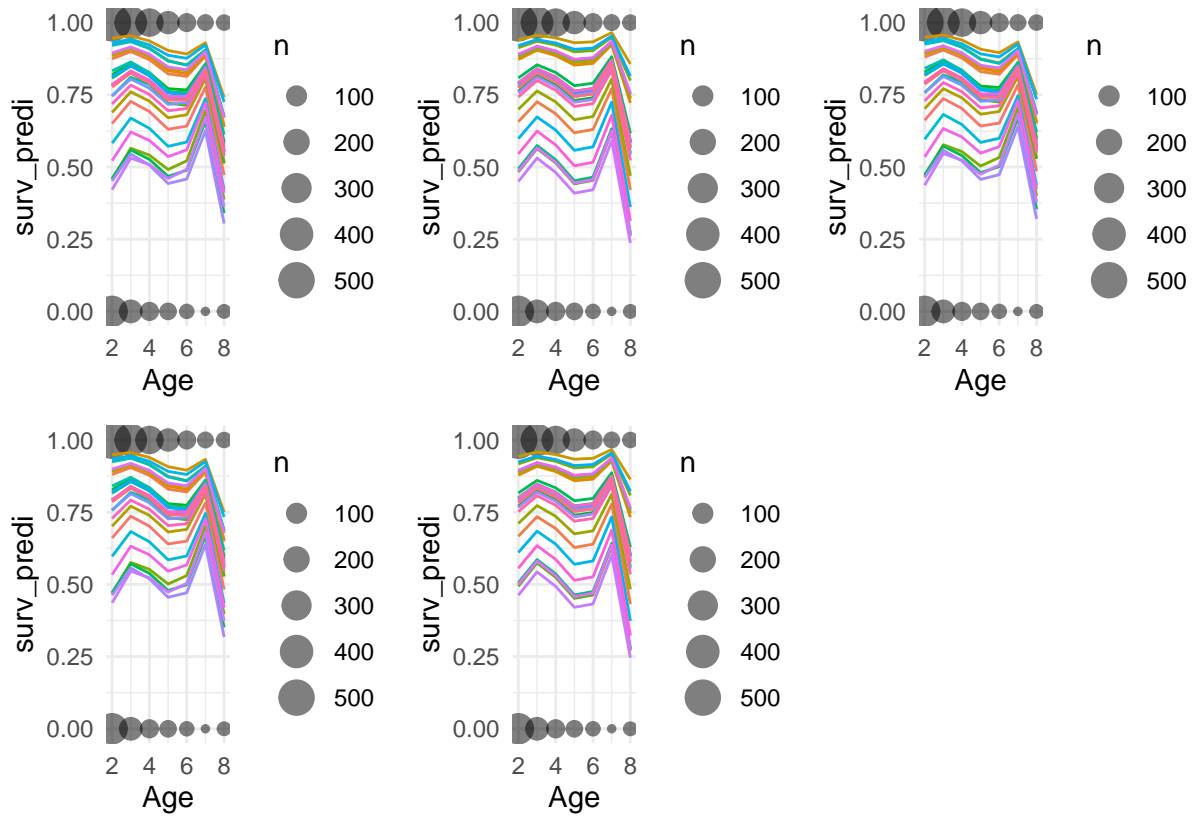
AIC



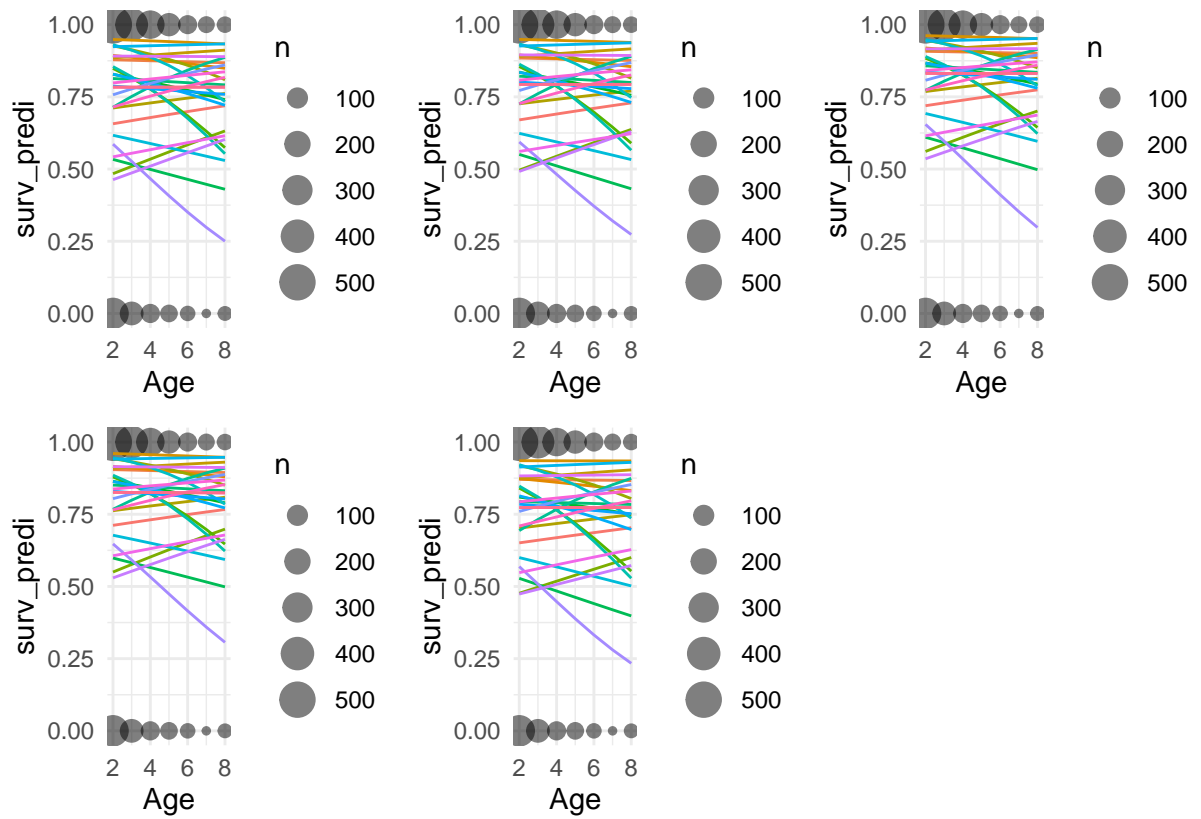
BIC

As a function of age (size=5)

See year effect (population fixed)



AIC



BIC

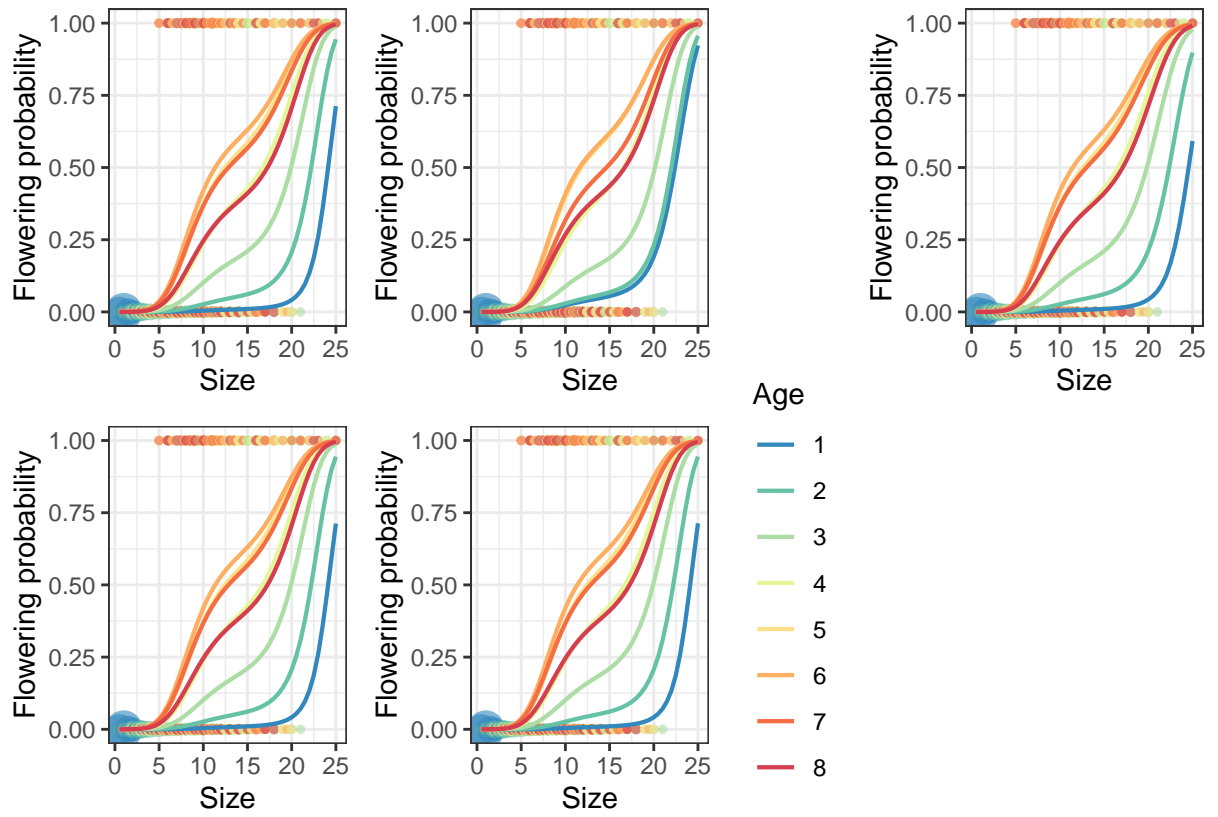
## Flowering probability

AIC

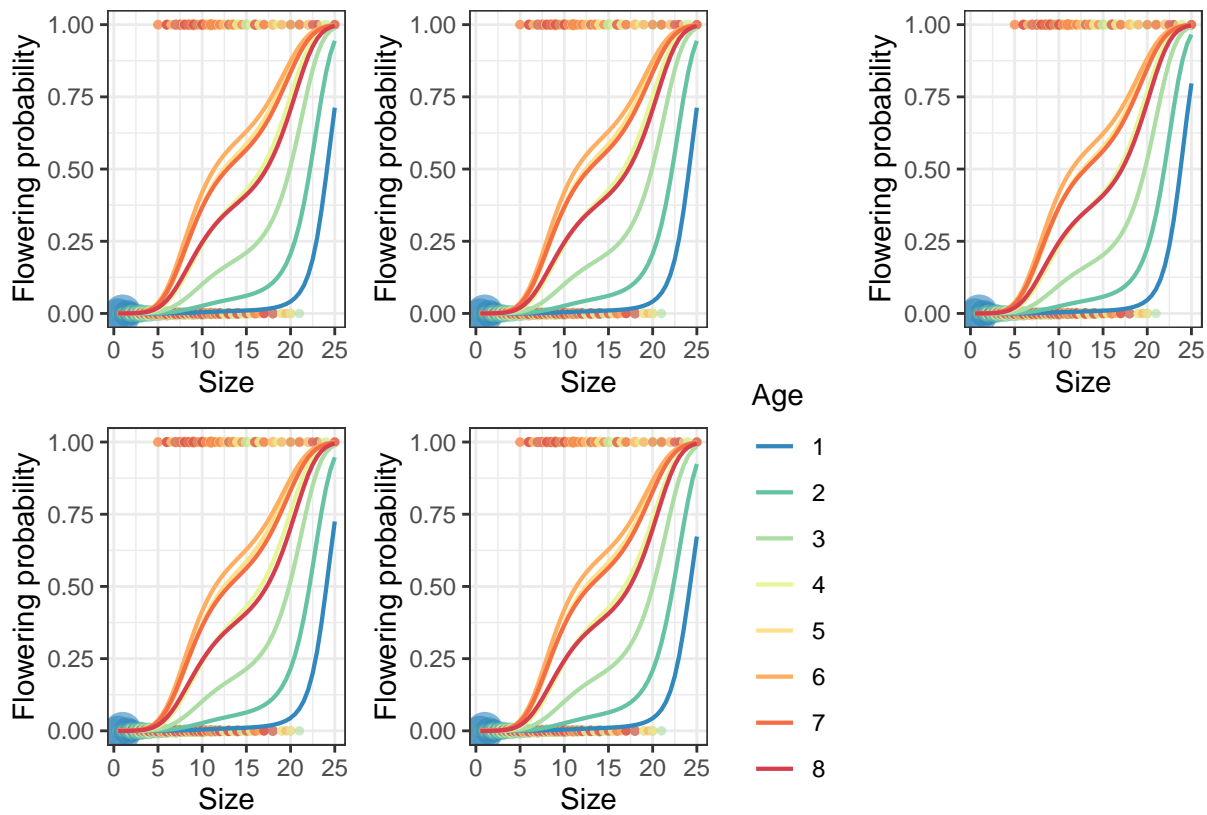
BIC

As a function of size

See effect of age



AIC

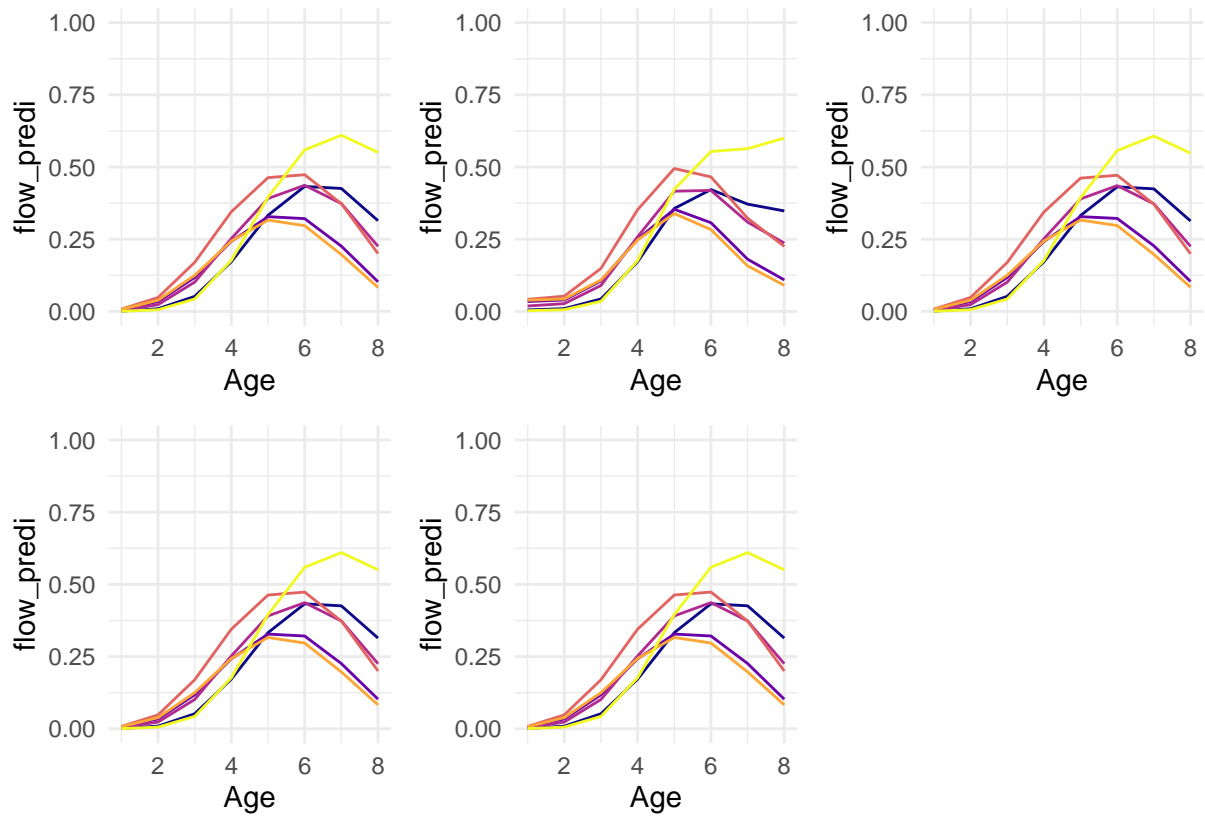


BIC

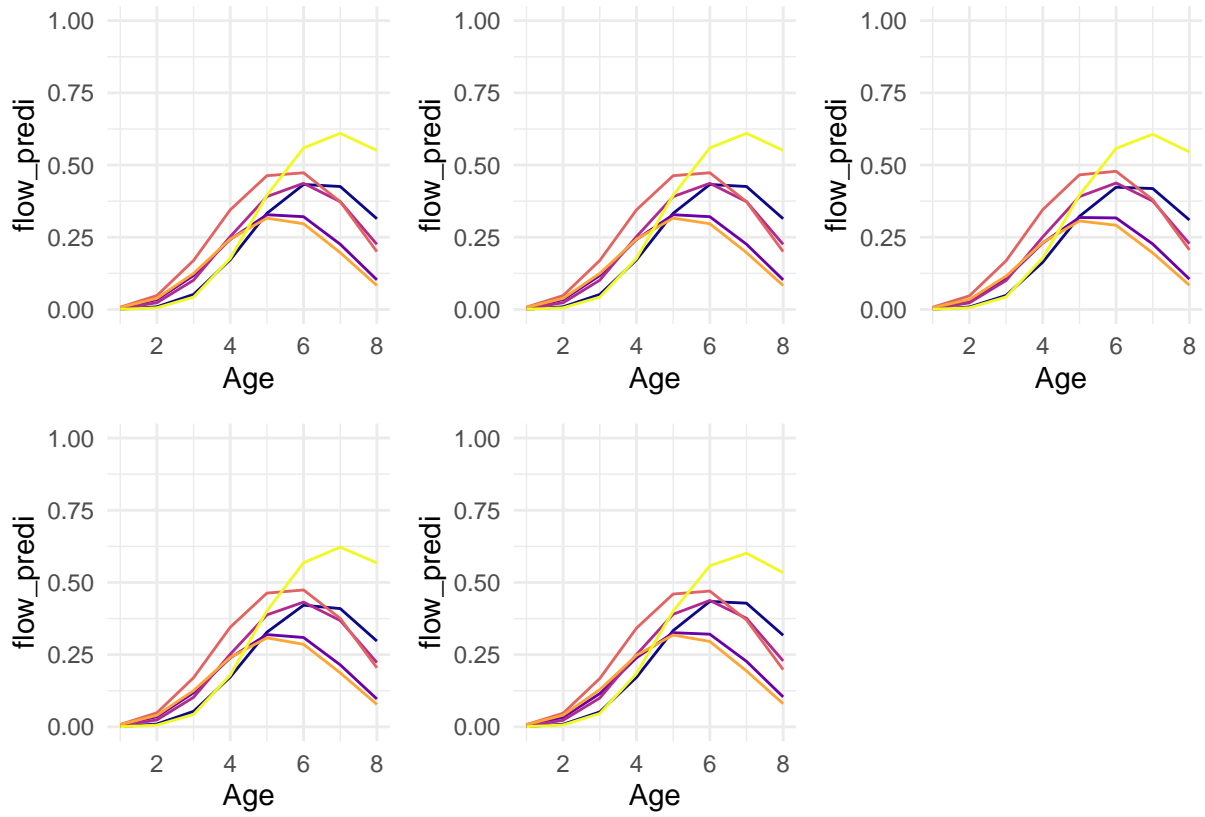


As a function of age (size fixed)

See population effect (mean over the years)

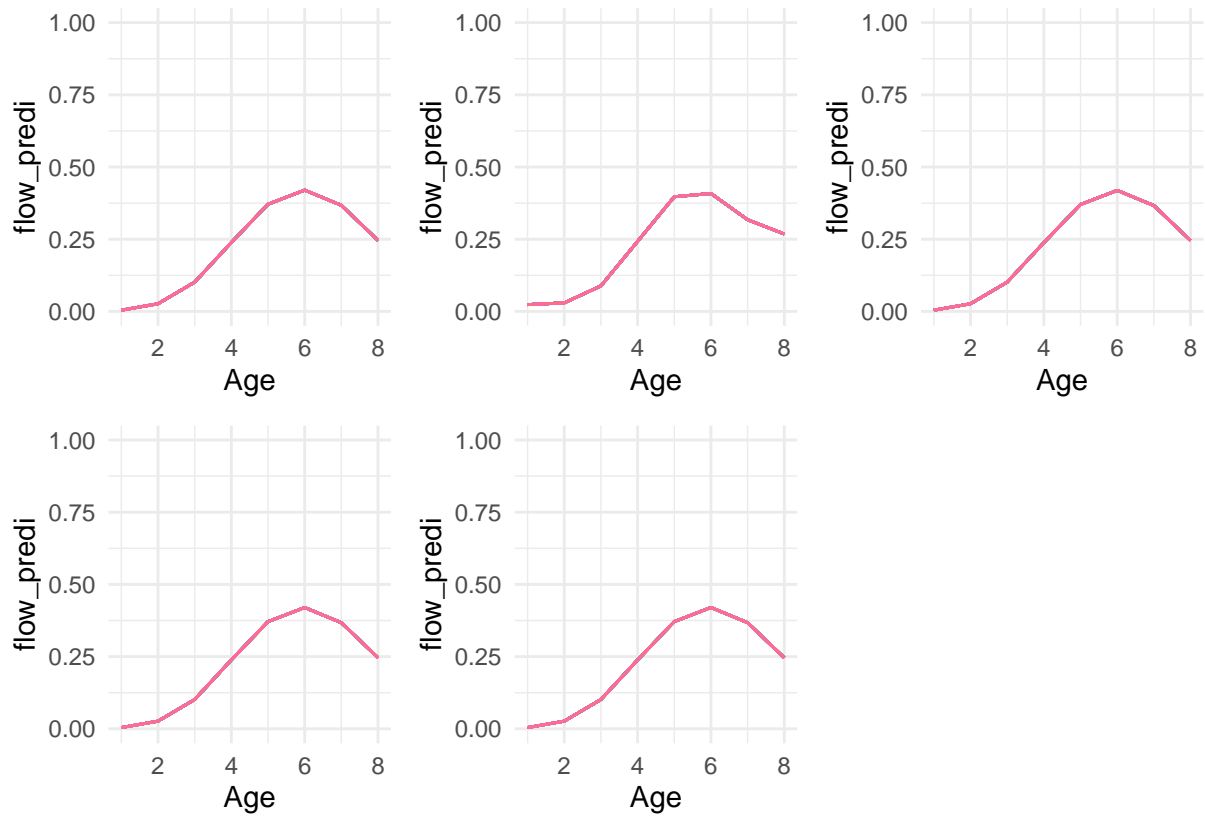


AIC

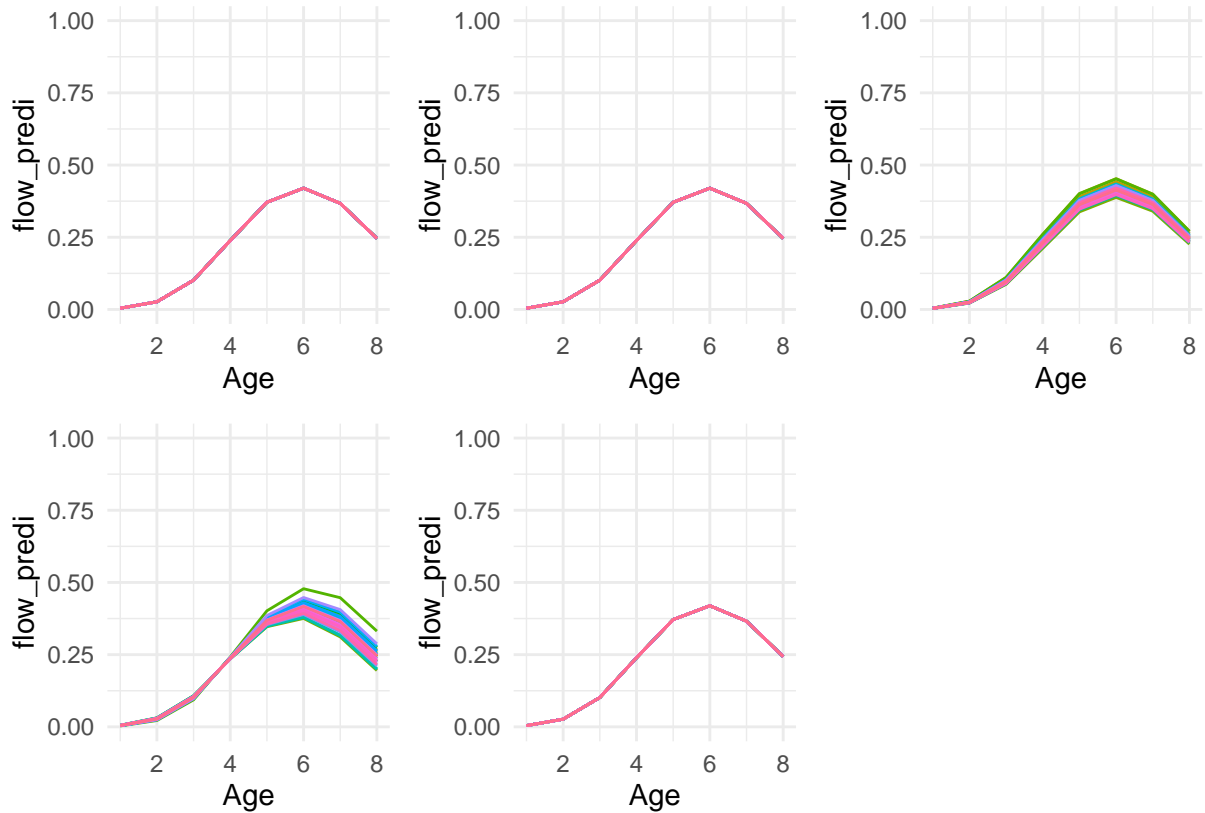


BIC

See year effect (mean over the populations)



AIC



BIC

## Growth

AIC

```
AGrowthglm1 <- fitme(Size1Mars ~ 1 + poly(Size0Mars,3) +
  bs(Age,degree=2,knots=6.5) + (Size0Mars+Age|year) +
  (1|Pop),
  resid.model = ~ log(Size0Mars)+log(Age),
  data=growthdata)

AGrowthglm2 <- fitme(Size1Mars ~ 1 + poly(Size0Mars,3) +
  bs(Age,degree=2,knots=6.5) + (Size0Mars+Age|year) +
  (Size0Mars|Pop),
  resid.model = ~ log(Size0Mars)+log(Age),
  data=growthdata)

AGrowthglm3 <- fitme(Size1Mars ~ 1 + poly(Size0Mars,3) +
  bs(Age,degree=2,knots=6.5) + (Size0Mars+Age|year) +
  (Size0Mars+Age|Pop),
  resid.model = ~ log(Size0Mars)+log(Age),
  data=growthdata)

AGrowthglm4 <- fitme(Size1Mars ~ 1 + bs(Size0Mars,df=5,degree=3) +
  bs(Age,degree=2,knots=6.5) + (Size0Mars+Age|year) +
```

```

      (1|Pop),
      resid.model = ~ log(Size0Mars)+log(Age),
      data=growthdata)

AGrowthglm5 <- fitme(Size1Mars ~ 1 + bs(Size0Mars,df=5,degree=3) +
      bs(Age,degree=2,knots=6.5) + (Size0Mars+Age|year) +
      (Size0Mars|Pop),
      resid.model = ~ log(Size0Mars)+log(Age),
      data=growthdata)

```

BIC

```

BGrowthglm1 <- fitme(Size1Mars ~ 1 + poly(Size0Mars,3) + poly(Age,2) +
      (Size0Mars+Age|year) + (1|Pop),
      resid.model = ~ log(Size0Mars)+log(Age),
      data=growthdata)

BGrowthglm2 <- fitme(Size1Mars ~ 1 + poly(Size0Mars,3) + poly(Age,2) +
      (Size0Mars+Age|year) + (Size0Mars+Age|Pop),
      resid.model = ~ log(Size0Mars)+log(Age),
      data=growthdata)

BGrowthglm3 <- fitme(Size1Mars ~ 1 + bs(Size0Mars,df=3,degree=2) + poly(Age,2) +
      (Size0Mars+Age|year) + (1|Pop),
      resid.model = ~ log(Size0Mars)+log(Age),
      data=growthdata)

BGrowthglm4 <- fitme(Size1Mars ~ 1 + bs(Size0Mars,df=3,degree=2) + poly(Age,2) +
      (Size0Mars+Age|year) + (Size0Mars|Pop),
      resid.model = ~ log(Size0Mars)+log(Age),
      data=growthdata)

BGrowthglm5 <- fitme(Size1Mars ~ 1 + bs(Size0Mars,df=3,degree=2) + poly(Age,2) +
      (Size0Mars+Age|year) + (Size0Mars+Age|Pop),
      resid.model = ~ log(Size0Mars)+log(Age),
      data=growthdata)

```

```

plot_growth1 <- function(data = fake_data, prediction, var, c1, c2, valc1=1, fact) {
  data %>%
    mutate(size1predi = prediction) %>%
    group_by(!!sym(var),!!sym(fact)) %>%
    filter(!!sym(c1) == valc1) %>%
    summarise(size1predi = mean(size1predi),
      .groups = "drop") %>%
    ggplot(aes(x = .data[[var]], y = size1predi)) +
    geom_line(aes(color = as.factor(.data[[fact]])),show.legend = FALSE) +
    geom_abline()+
    theme_minimal()
}

```

```

plot_growth2 <- function(data = fake_data, prediction, var, c1, c2, valc1=1, fact) {
  data %>%
    mutate(size1predi = prediction) %>%

```

```

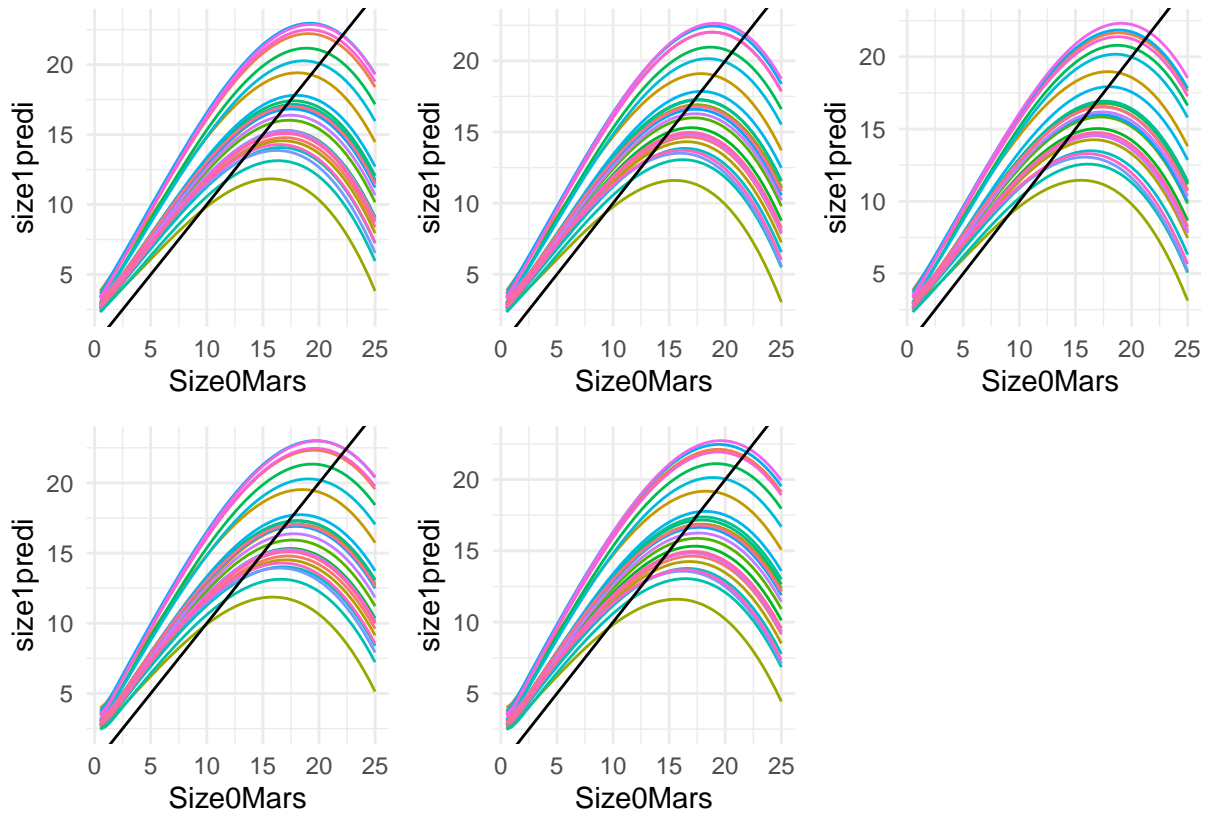
    group_by(!!sym(var),!!sym(fact)) %>%
    filter(!!sym(c1) == valc1) %>%
    summarise(size1predi = mean(size1predi),
              .groups = "drop") %>%
    ggplot(aes(x = .data[[var]], y = size1predi)) +
    geom_line(aes(color = as.factor(.data[[fact]])),show.legend = FALSE) +
    geom_abline()+
    theme_minimal()+
    scale_color_viridis_d(option = "plasma")
}

plot_growth3 <- function(data = fake_data, prediction, var, c1, c2, valc1=1, fact) {
  data %>% mutate(sdgrow = prediction) %>%
  group_by(Size0Mars, Age) %>%
  summarise(sd_predi = mean(sdgrow),
            .groups = "drop") %>%
  ggplot(aes(x = Size0Mars, y = sd_predi)) +
  geom_line(aes(color = as.factor(Age))) +
  theme_bw()+
  labs(x = "Size(t)",
       y = "Growth residual variance",
       fill = "Age",
       color = "Age")+
  scale_color_brewer(palette = "Spectral", direction = -1)
}

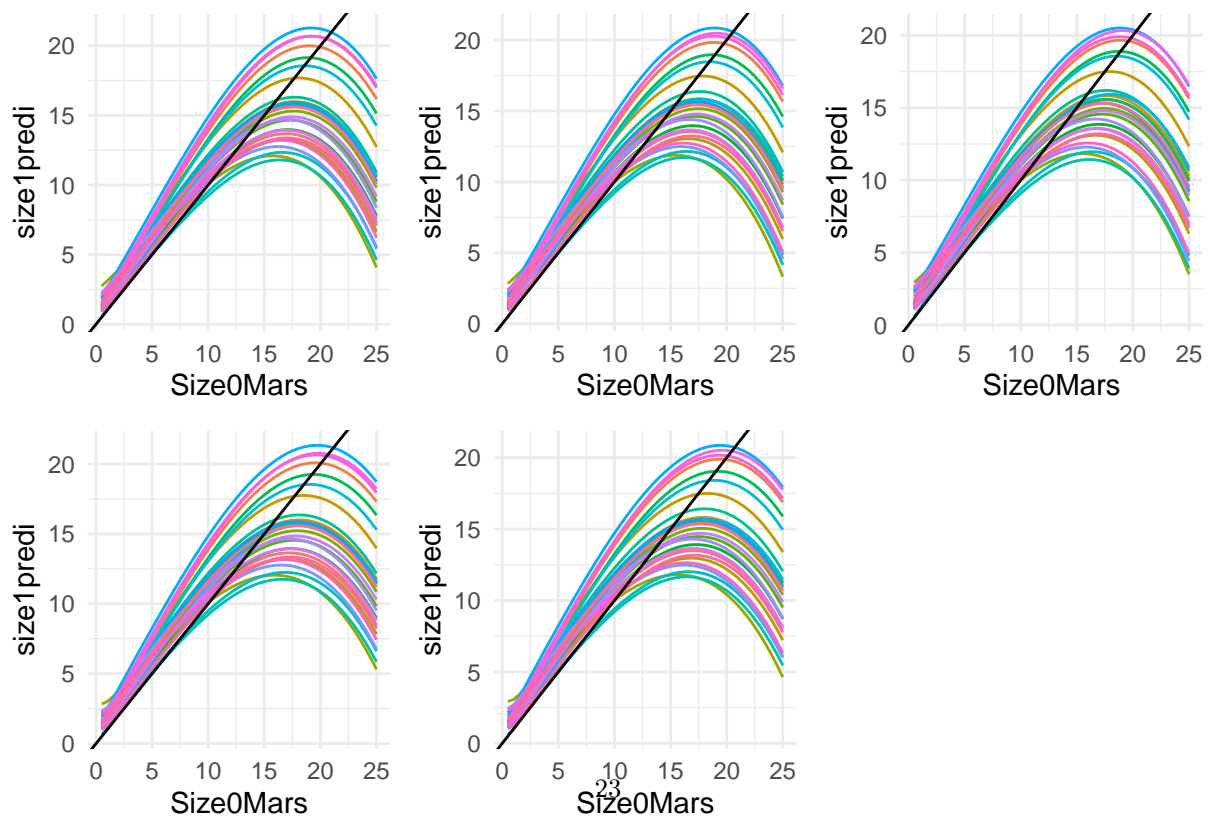
```

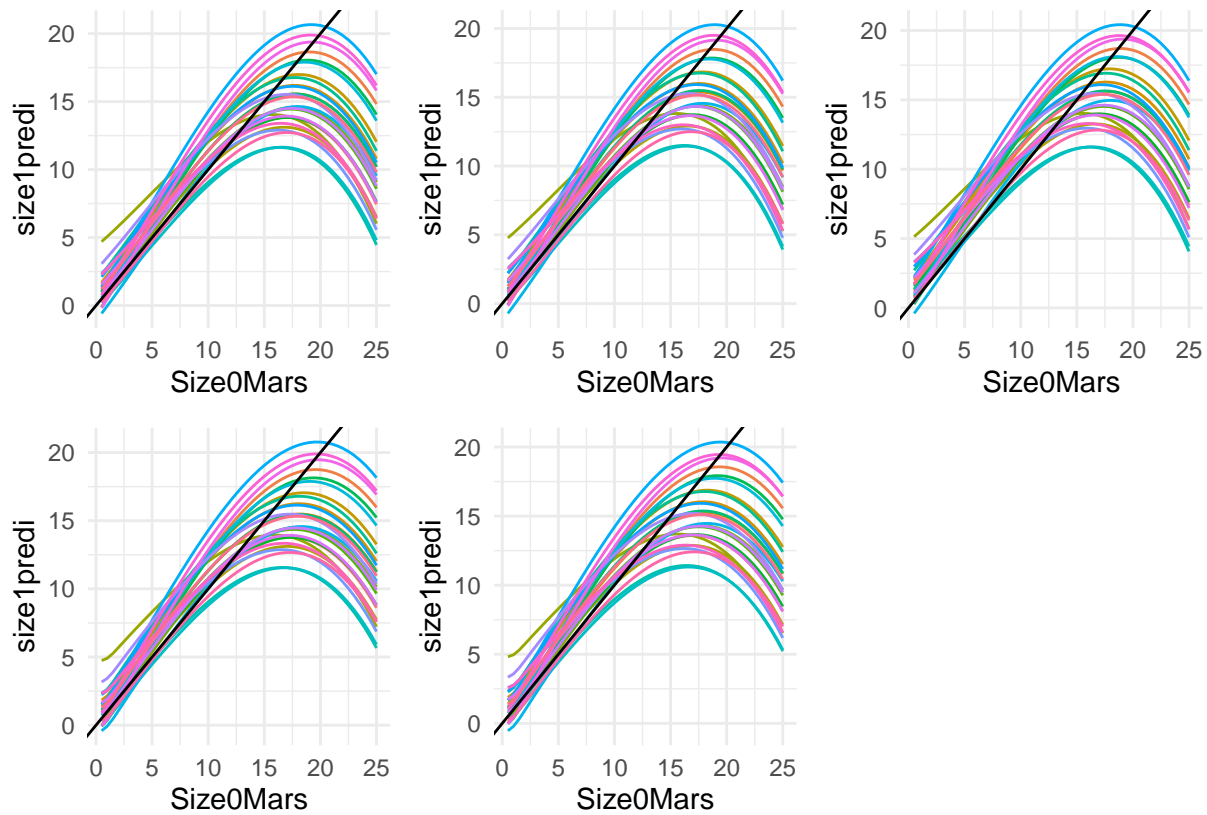
Size at  $t+1$  as a function of size at  $t$  (age 1, 4, 8)

See year effect (population fixed)

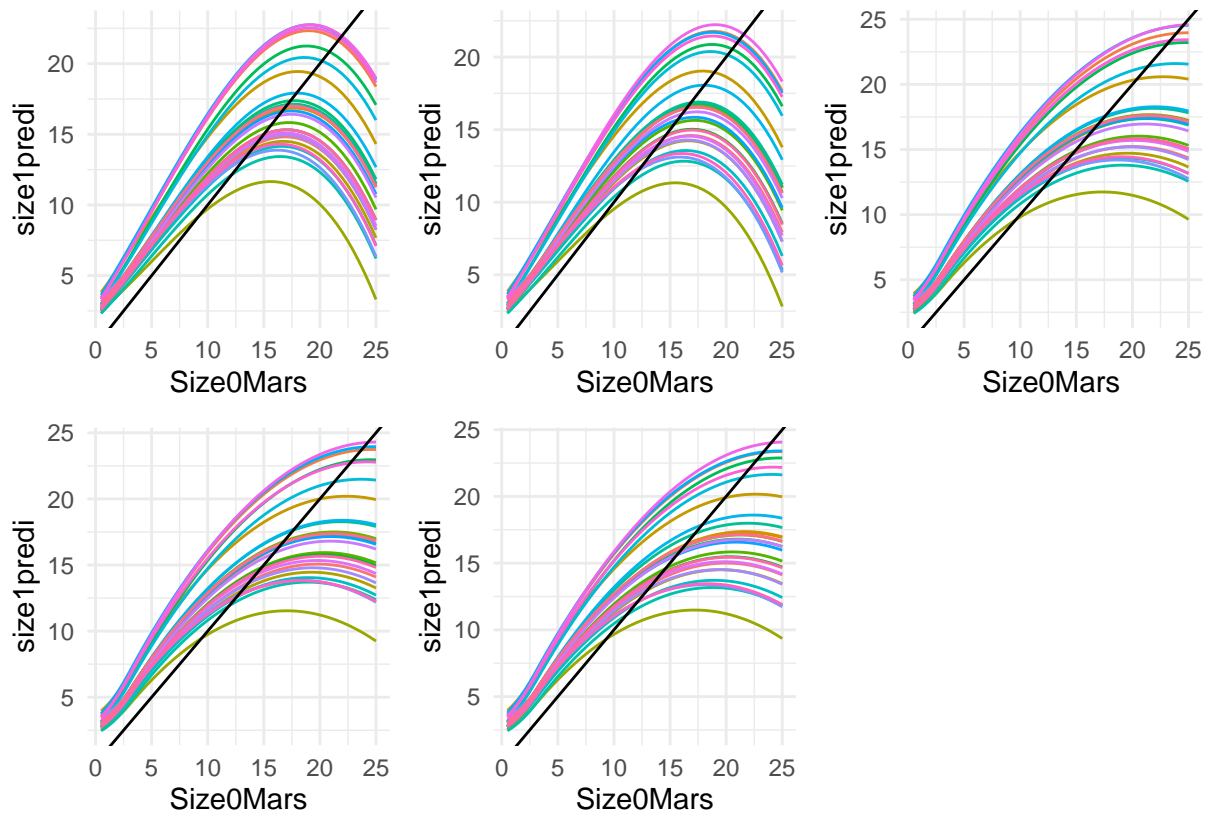


AIC

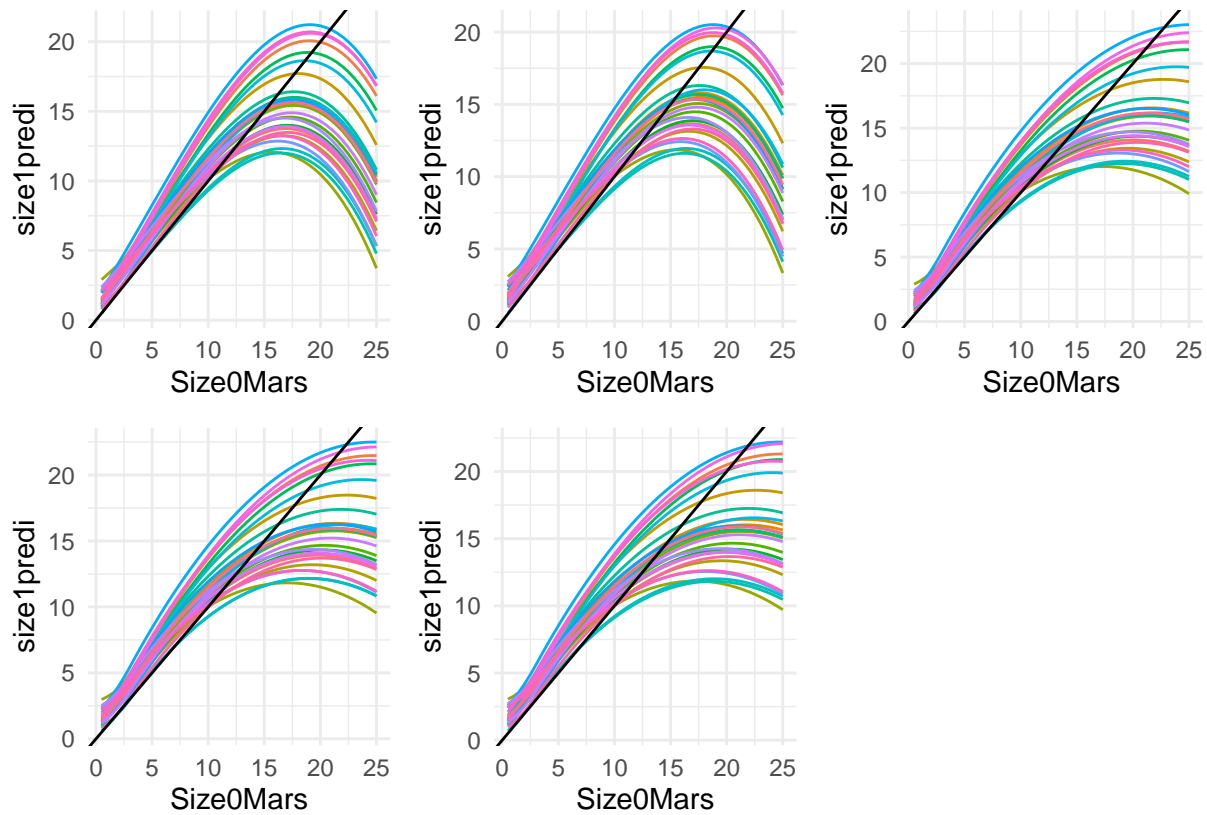


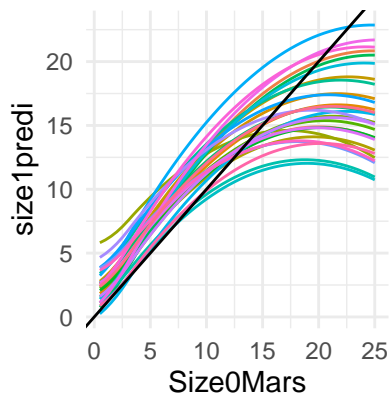
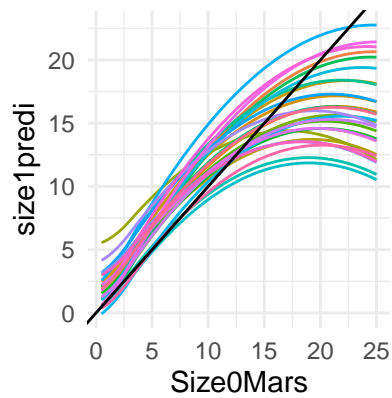
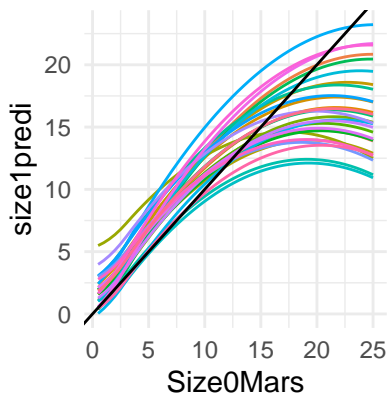
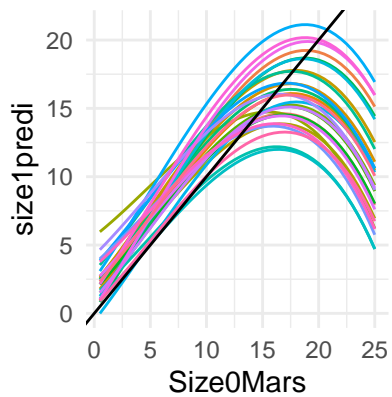
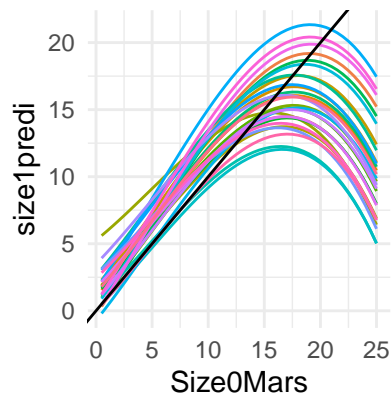




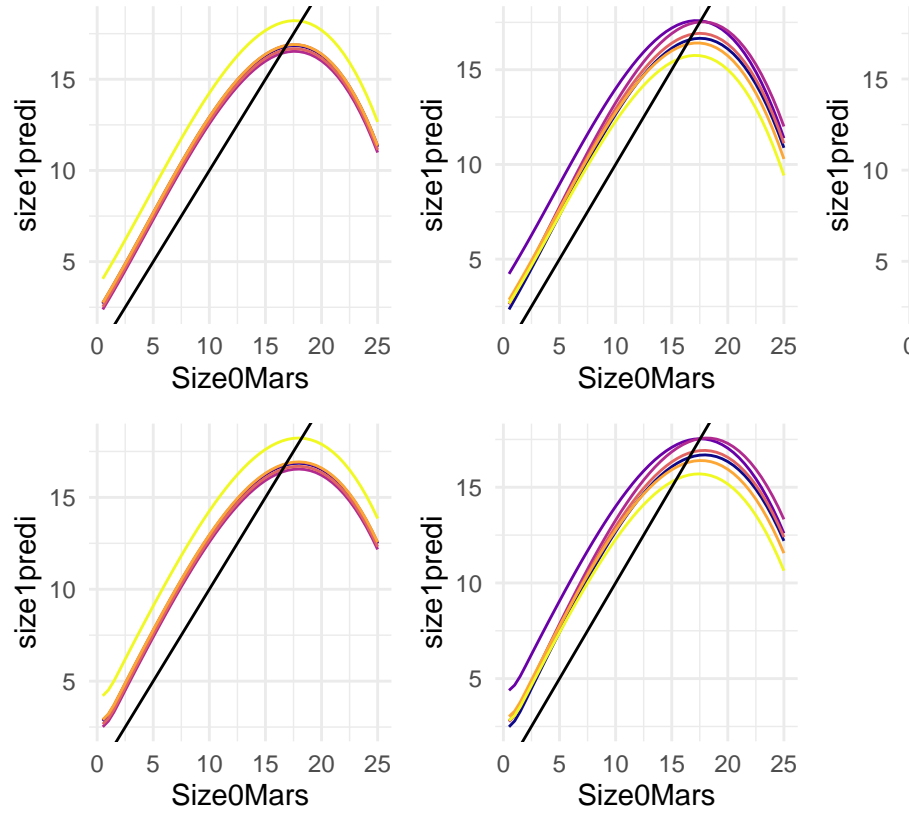


BIC

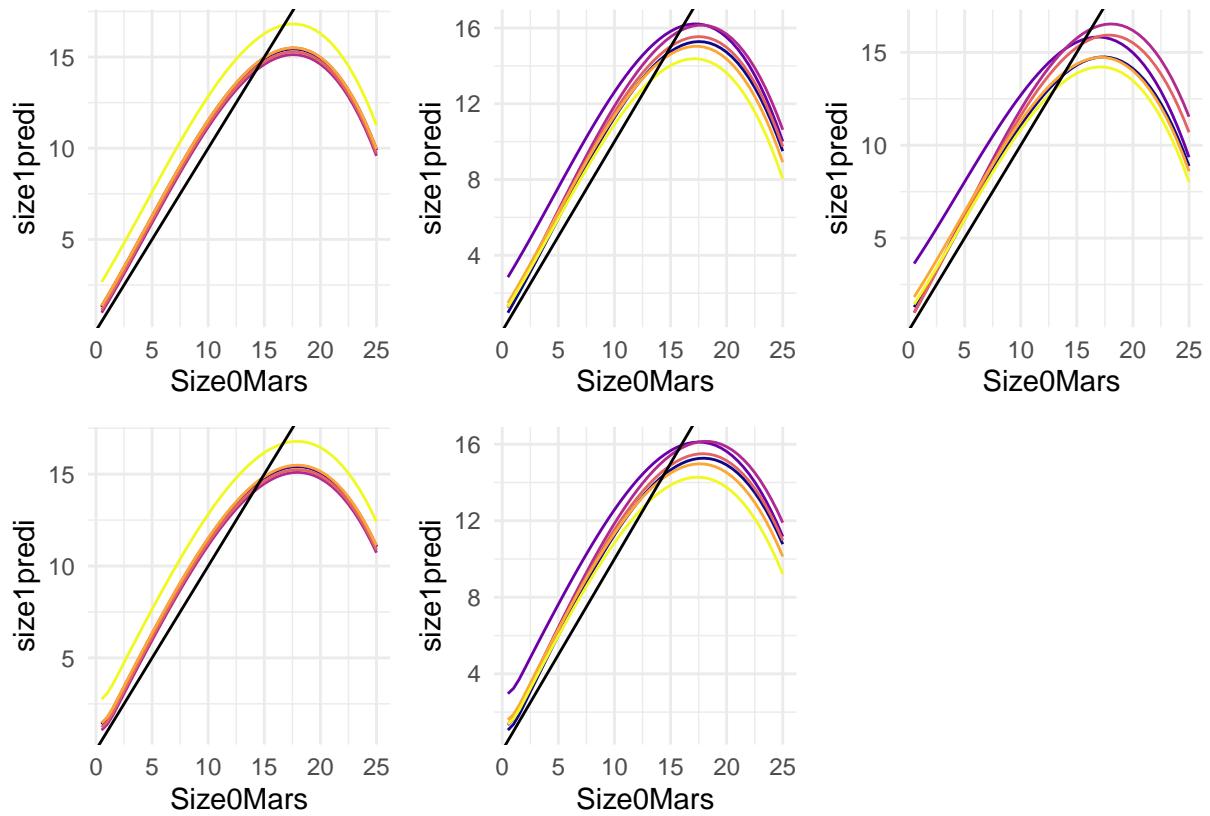


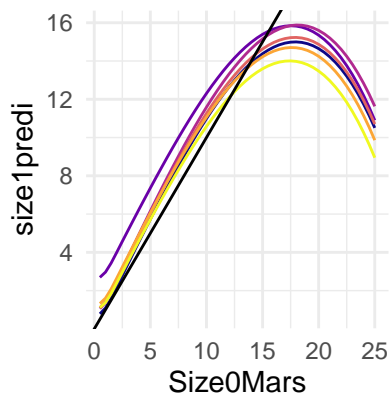
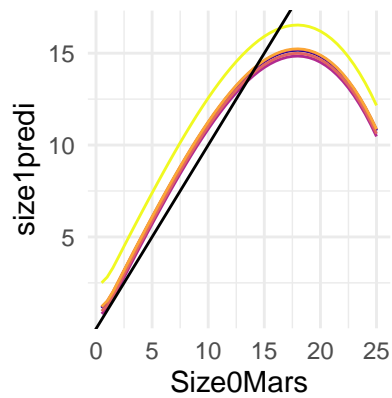
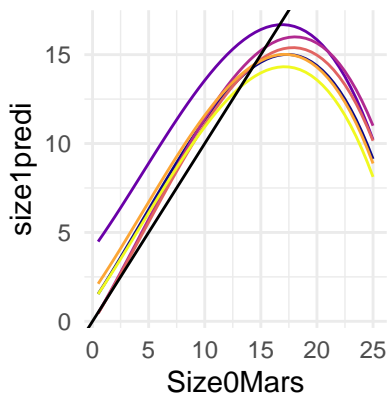
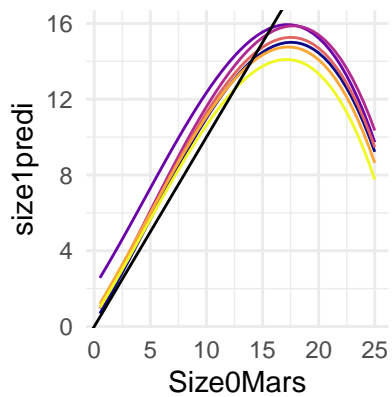
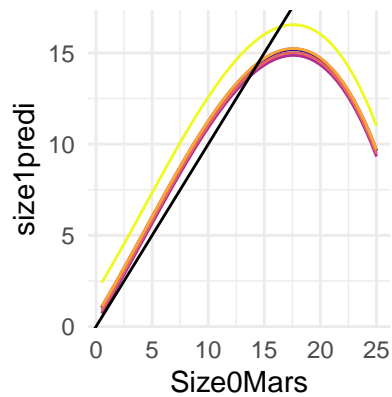


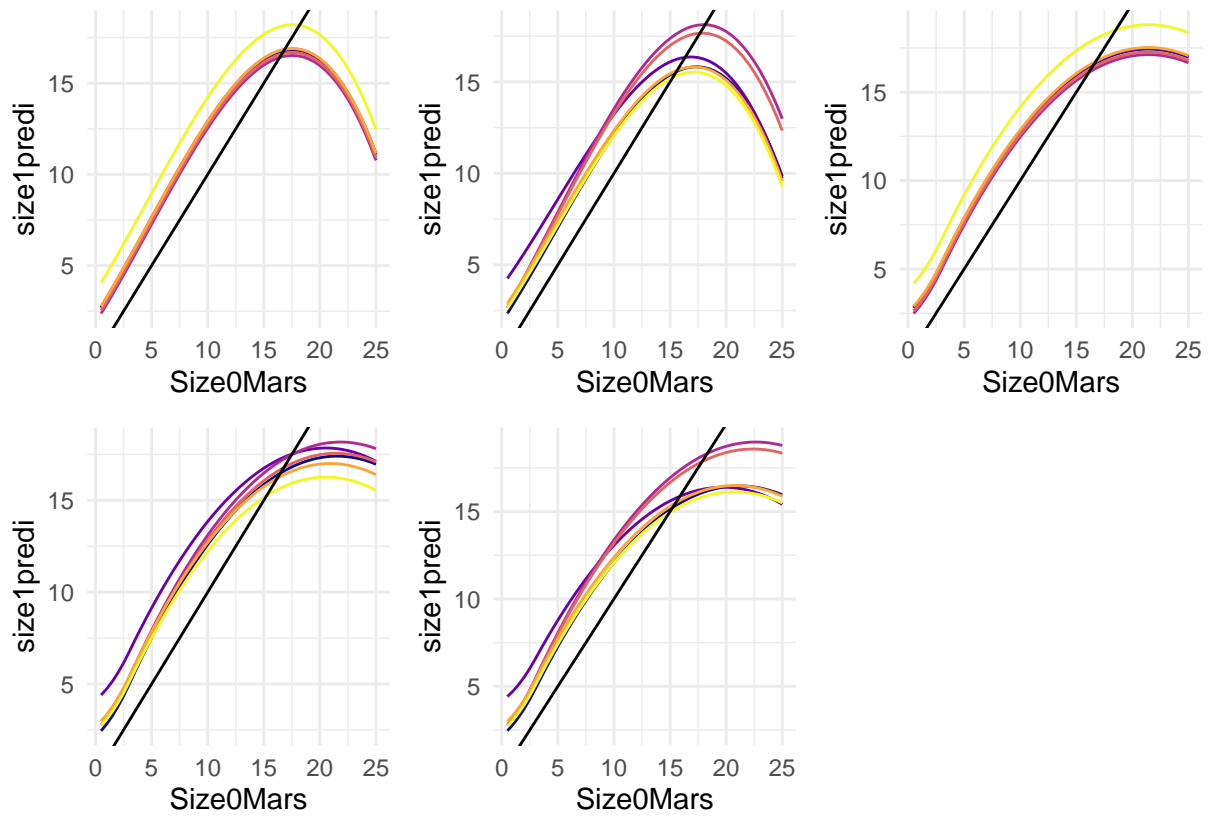




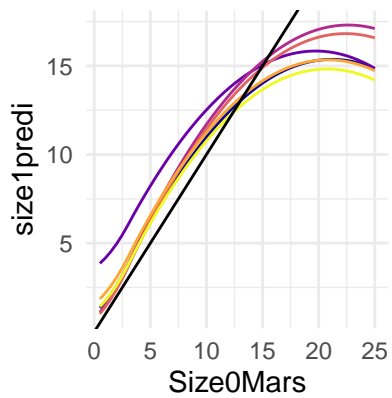
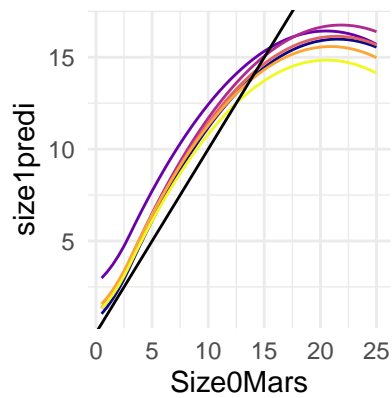
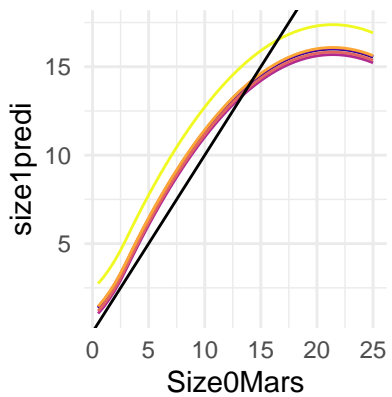
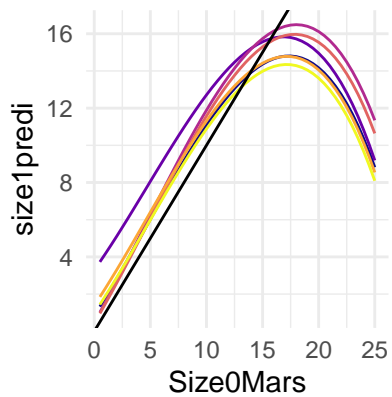
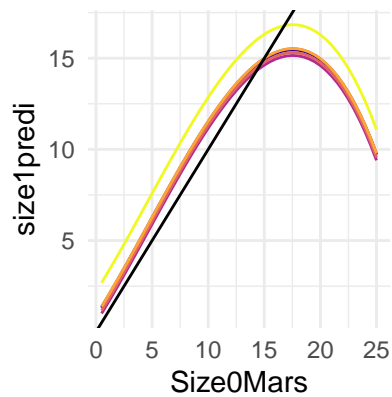
See population effect (year fixed) AIC



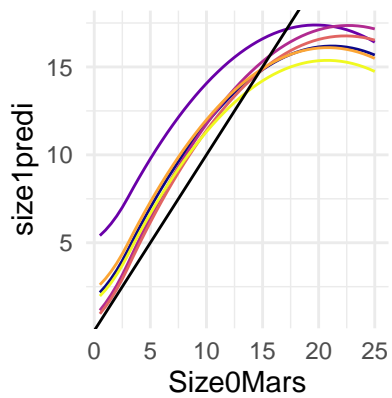
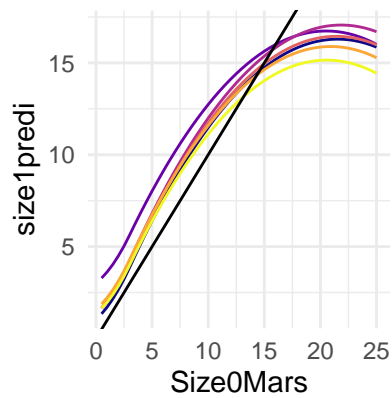
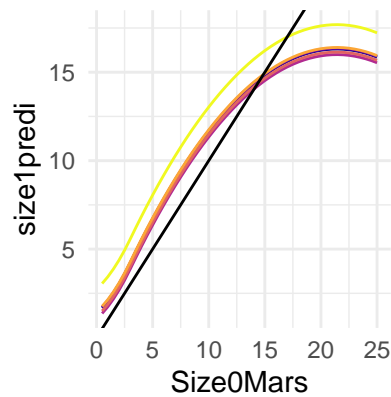
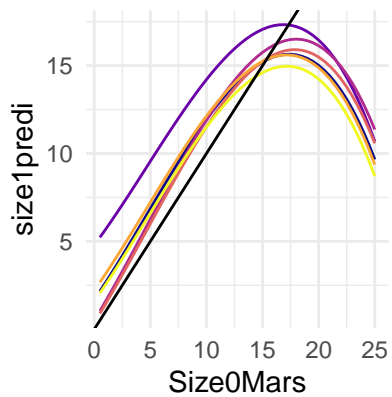
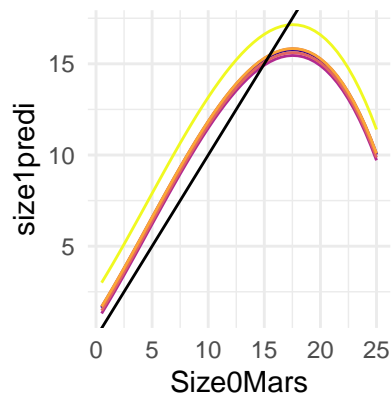




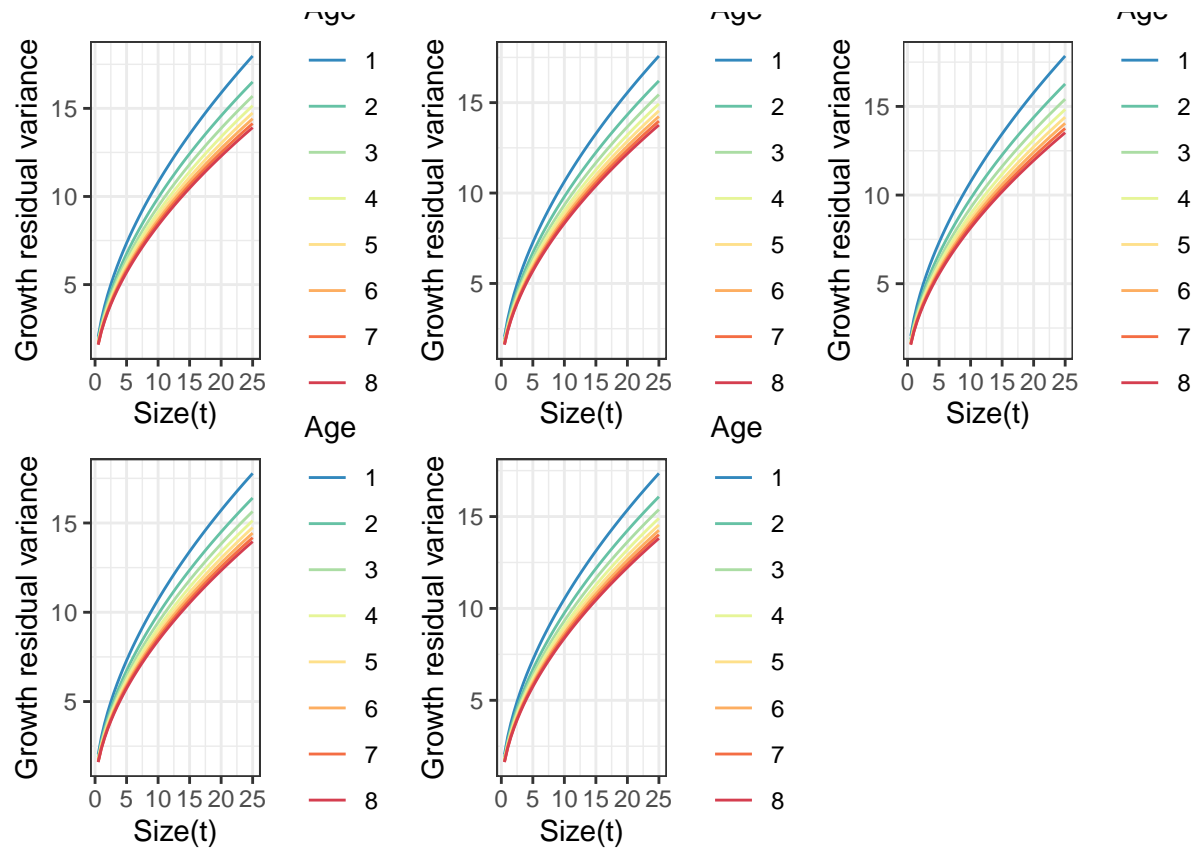
BIC



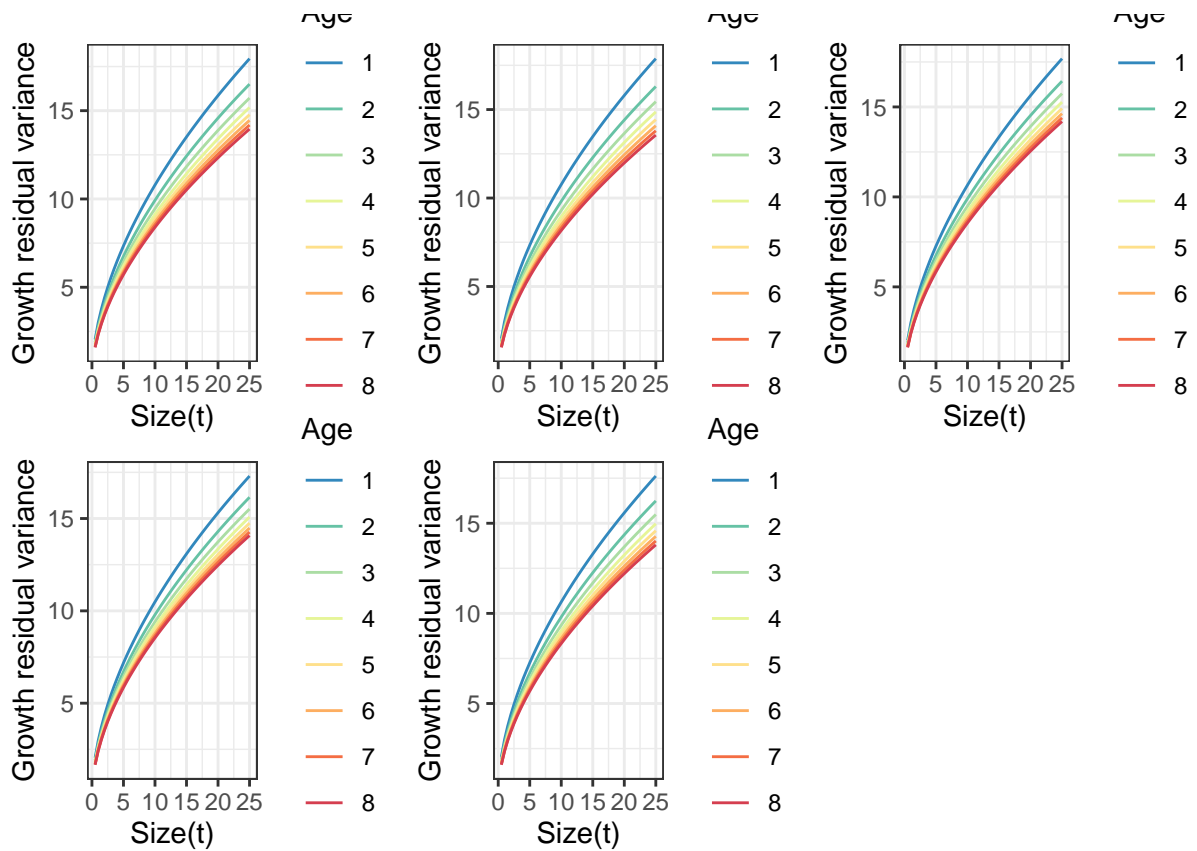




Residual variance



AIC



BIC

## Number of capitula (fecundity)

AIC

```
ACptlglm1 <- fitme(log(Capitule) ~ 1 + Size0Mars + (Age|year),
  data=cptldata)

ACptlglm2 <- fitme(log(Capitule) ~ 1 + Size0Mars + (Age|year) + (1|Pop),
  data=cptldata)

ACptlglm3 <- fitme(log(Capitule) ~ 1 + poly(Size0Mars,2) + (Age|year),
  data=cptldata)

ACptlglm4 <- fitme(log(Capitule) ~ 1 + Size0Mars + Age + (Age|year),
  data=cptldata)

ACptlglm5 <- fitme(log(Capitule) ~ 1 + Size0Mars + (1|year),
  data=cptldata)
```

BIC

```
BCptlglm1 <- fitme(log(Capitule) ~ 1 + Size0Mars + (Age|year),
  data=cptldata)
```

```
BCptlglm2 <- fitme(log(Capitule) ~ 1 + Size0Mars + (Age|year) + (1|Pop),
  data=cptldata)

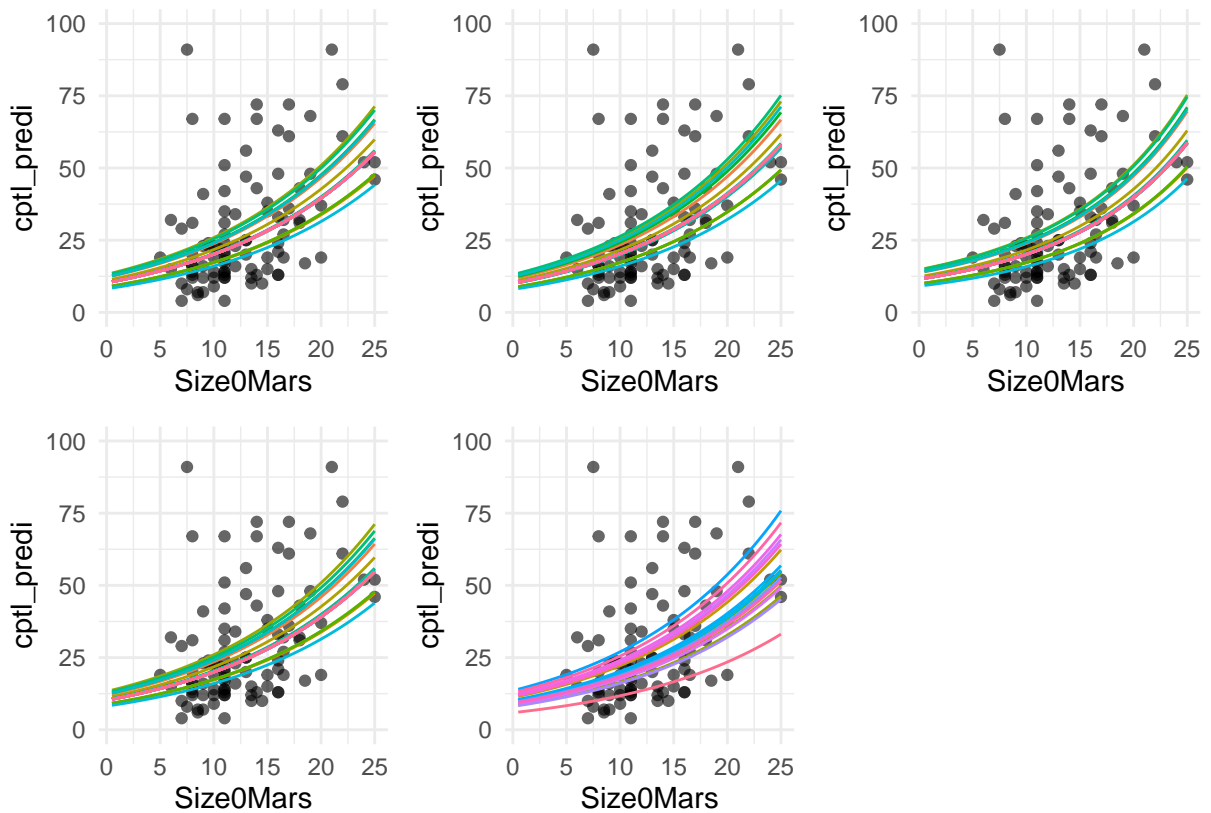
BCptlglm3 <- fitme(log(Capitule) ~ 1 + Size0Mars + (1|year),
  data=cptldata)

BCptlglm4 <- fitme(log(Capitule) ~ 1 + Size0Mars,
  data=cptldata)

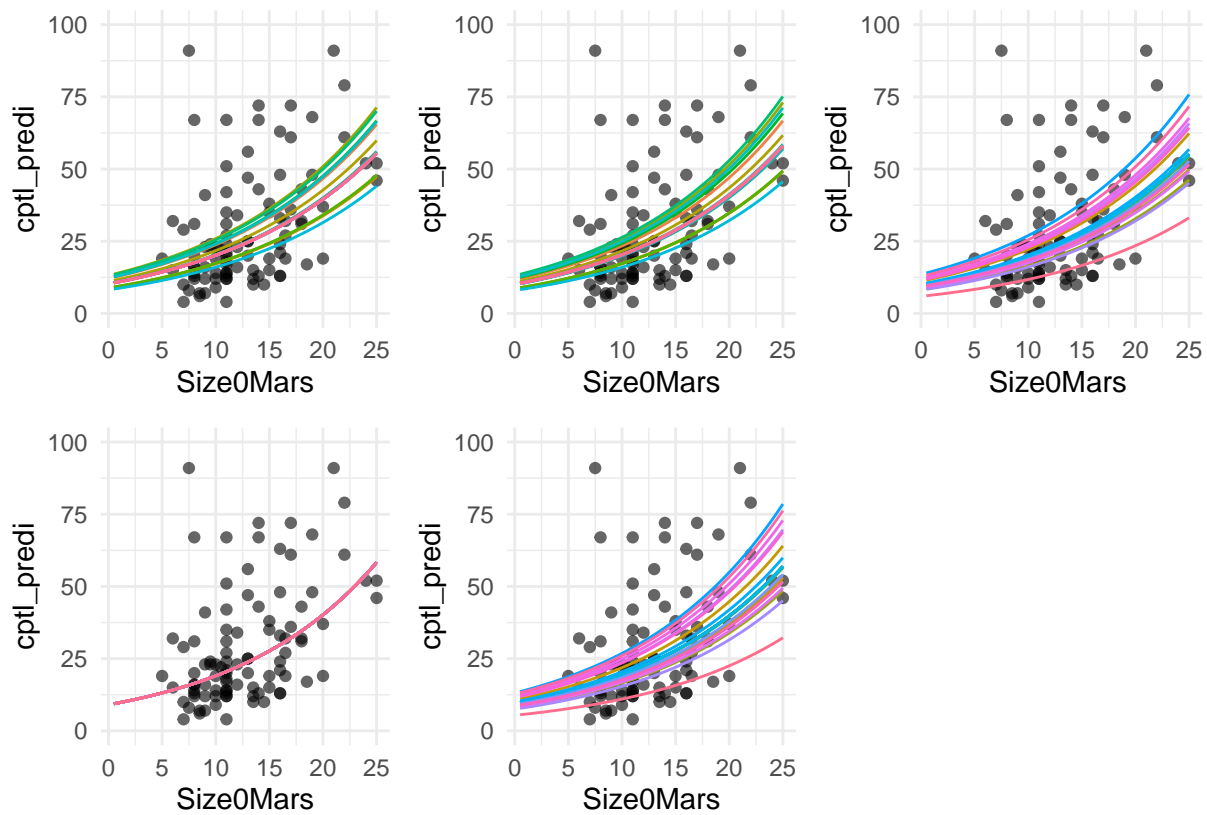
BCptlglm5 <- fitme(log(Capitule) ~ 1 + Size0Mars + (1|year) + (1|Pop),
  data=cptldata)
```

As a function of size

See year effect

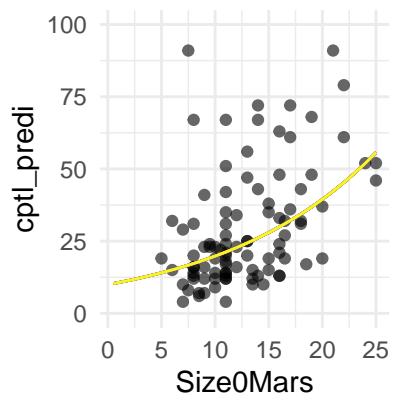
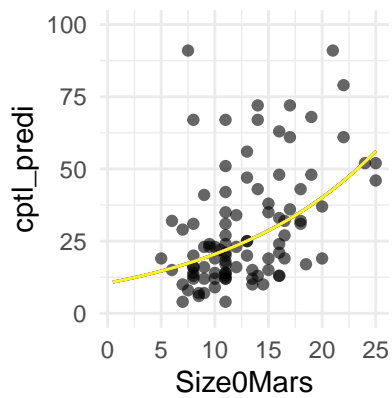
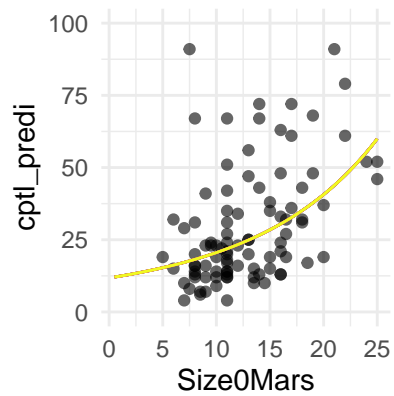
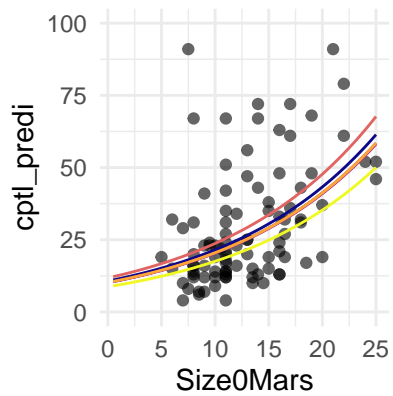
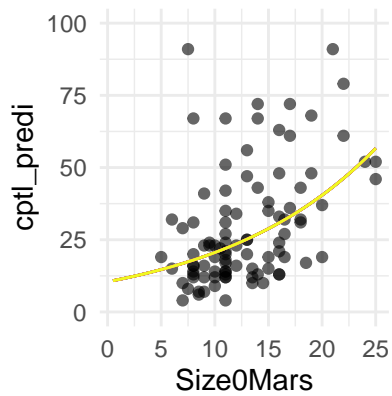


AIC

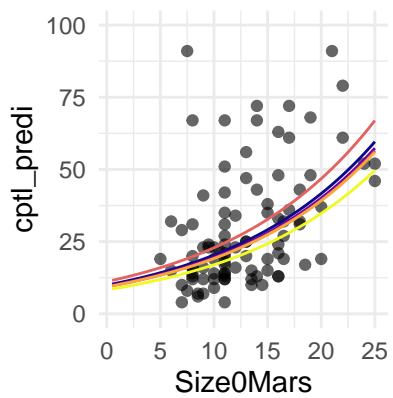
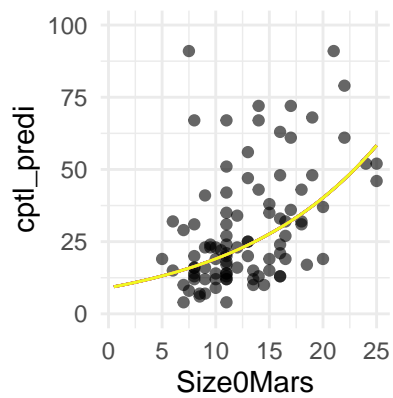
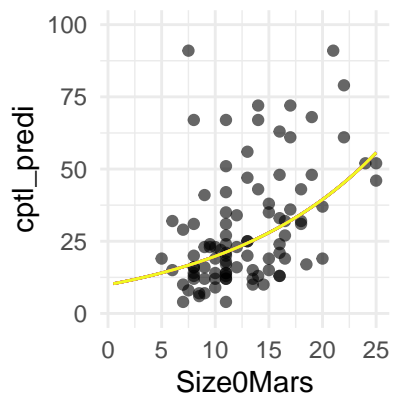
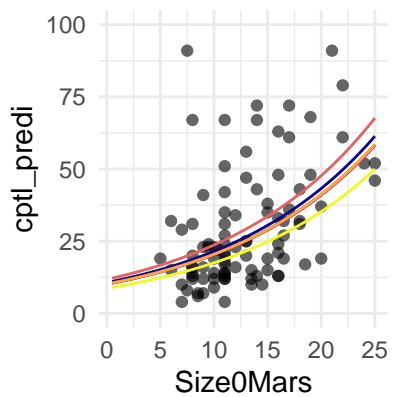
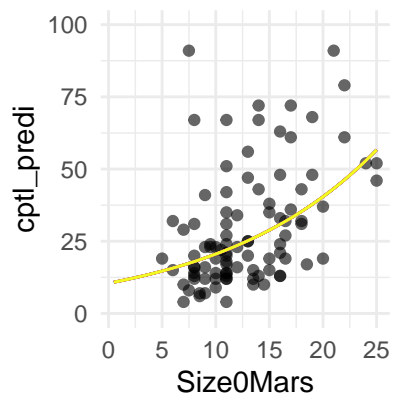


BIC

See population effect



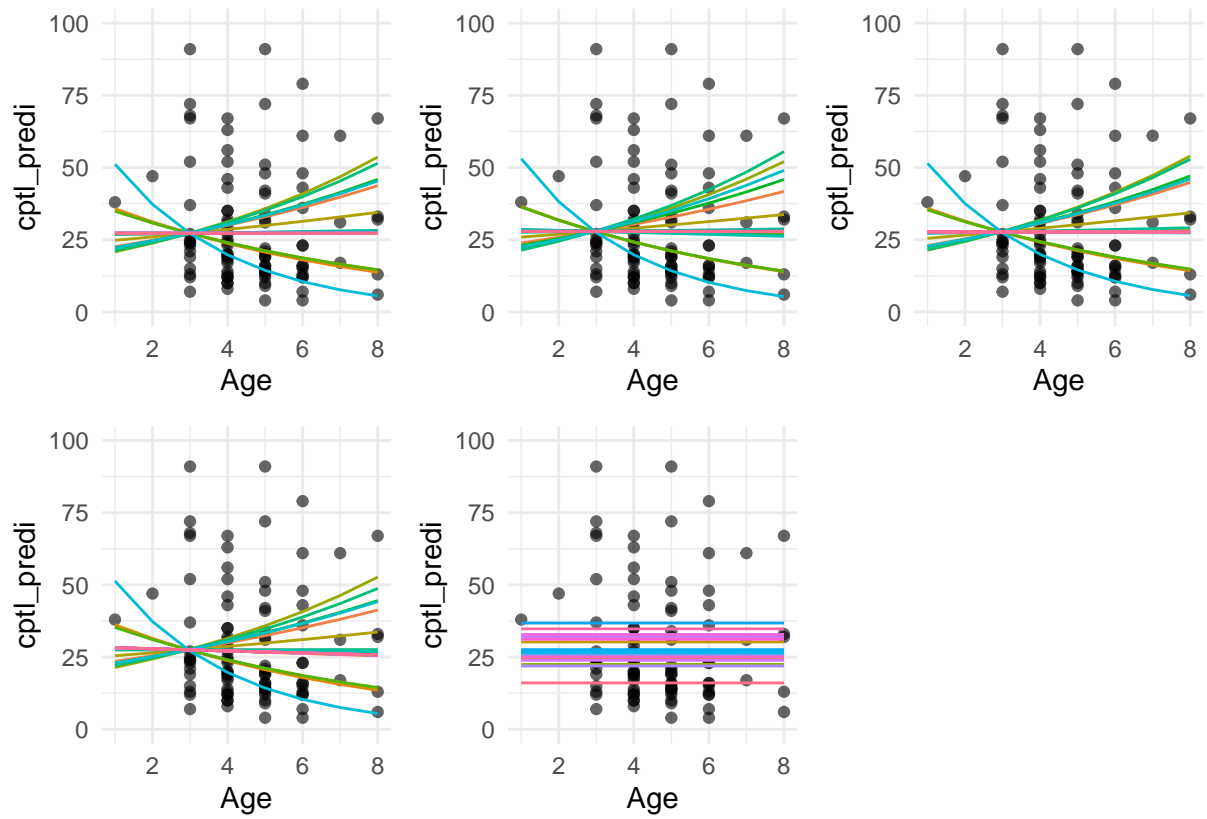
AIC



BIC

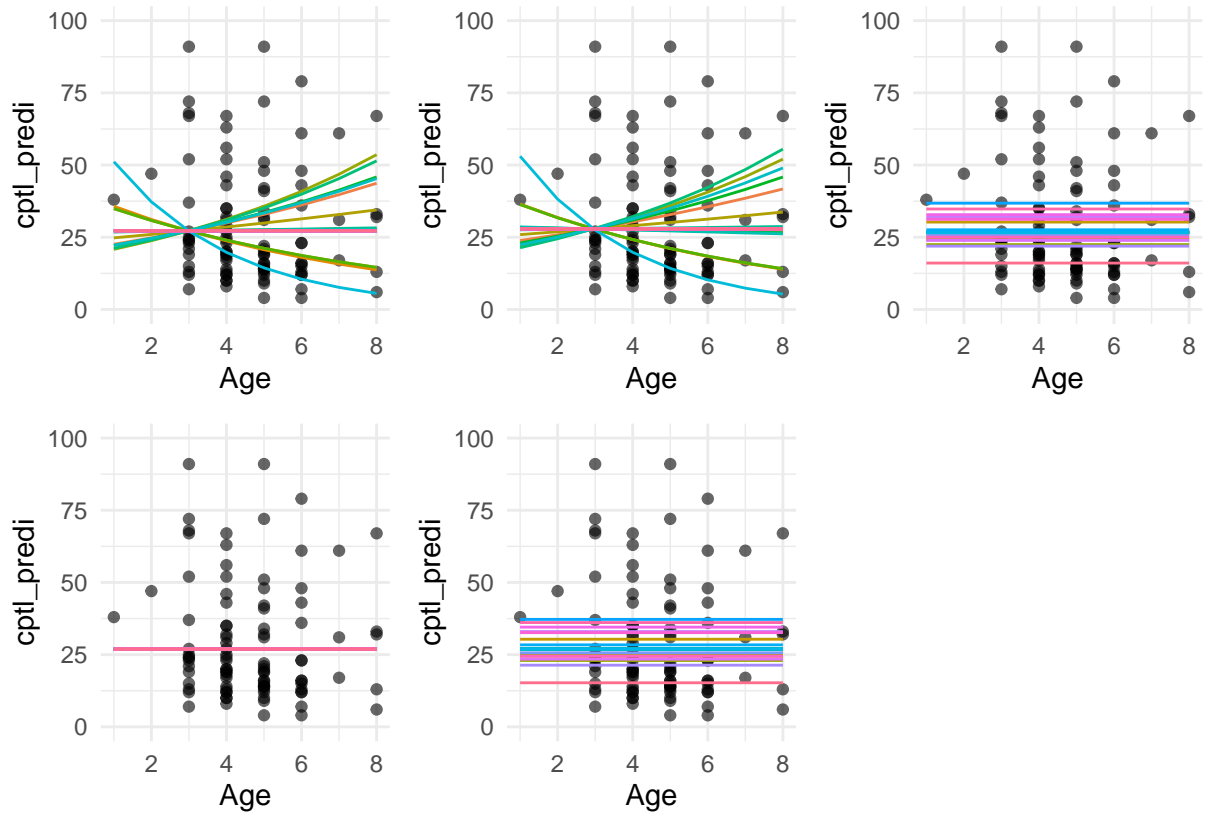
As a function of age

See year effect



AIC



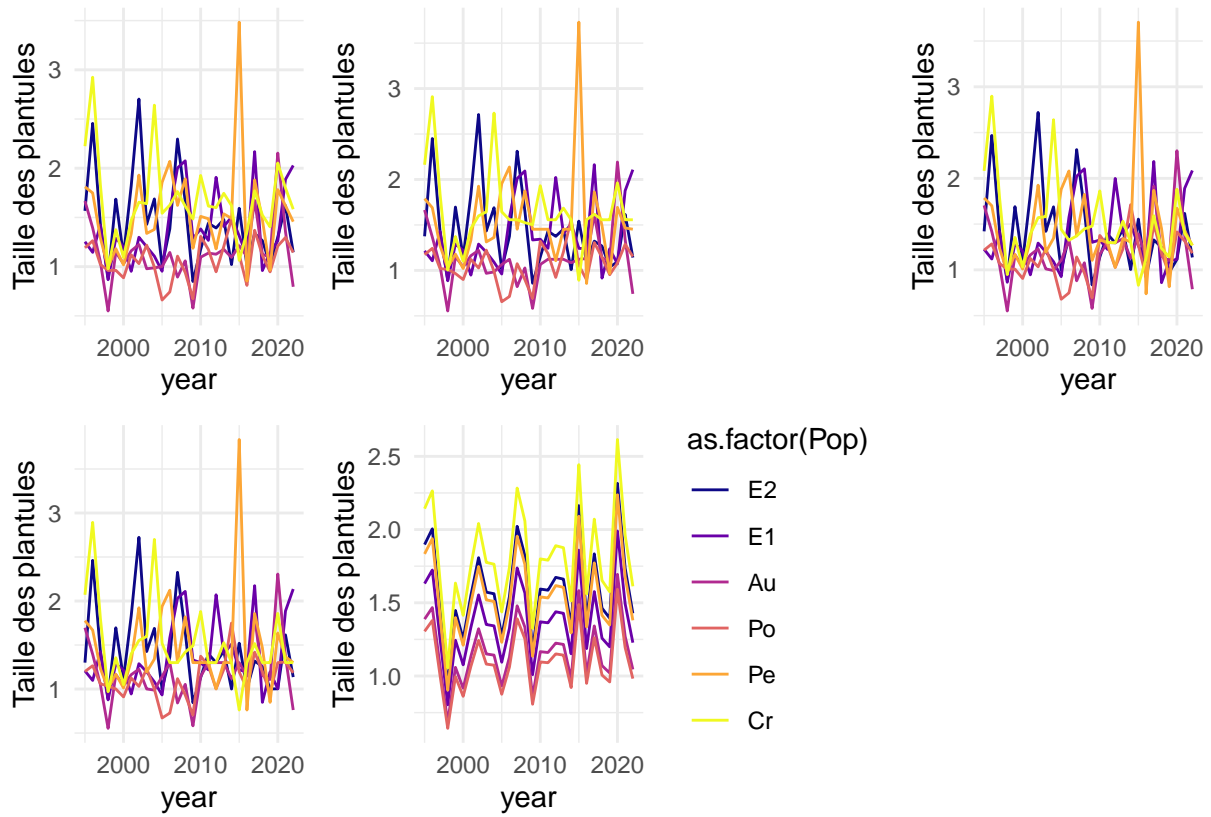


BIC

## Seedling size

Same with AIC and BIC

As a function of year



## Density

