

算法

- 辗转相减法
 - 通过不断的两数相减并将结果移给被减数，然后不断重复相减的过程，直到两数相等，则停止，两个数都是最大公约数
 - 若 $a > b$, 则 $(a, b) = (a-b, b)$
 - 若 $a < b$, 则 $(a, b) = (a, -(a-b))$;
 - 若 $a = b$, 则最大公约数即 a

写代码

```
                .ORIG x3000
                LD R0, Data0
                LD R1, Data1
LOOP            NOT R2, R1
                ADD R2, R2, #1 ; R2 <- -R1
                ADD R2, R0, R2 ; R2 <- R0-R1
                BRz Done
                BRp Positive ; (R0 > R1)?(R0 <- R2):(R1 <- -R2) (R0 != R1)
                NOT R2, R2
                ADD R1, R2, #1 ; R1 <- -R2
                BRnzp LOOP
Positive        ADD R0, R2, #0 ; R0 <- R2
                BRnzp LOOP
Done            HALT
Data0           .FILL x0018
Data1           .FILL x0020
                .END
```

1. 由算法,R0-R1是一个共同操作，如果R0-R1=0则已经找到结果，直接跳转到**HALT**，否则，判断R0-R1>0，如果成立，则将结果(储存在R2中)赋给R0，否则应将-R2赋给R1，所以整体看来，就是将差的绝对值赋给R0，R1中较大的那个

测试数据

Example (3, 12)

Registers			Memory		
R0	x0003	3	!	▶	x3000 x200C 8204 <i>LD R0, Data0</i>
R1	x0003	3	!	▶	x3001 x220C 8716 <i>LD R1, Data1</i>
R2	x0000	0	!	▶	x3002 x947F -27521 <i>LOOP NOT R2, R1</i>
R3	x0000	0	!	▶	x3003 x14A1 5281 <i>ADD R2, R2, #1</i>
R4	x0000	0	!	▶	x3004 x1402 5122 <i>ADD R2, R0, R2</i>
R5	x0000	0	!	▶	x3005 x0406 1030 <i>BRz Done</i>
R6	x0000	0	!	▶	x3006 x0203 515 <i>BRp Positive</i>
R7	x0000	0	!	▶	x3007 x94BF -27457 <i>NOT R2, R2</i>
PSR	x8002	-32766 CC: Z	!	▶	x3008 x12A1 4769 <i>ADD R1, R2, #1</i>
PC	x300C	12300	!	▶	x3009 x0FF8 4088 <i>BRnzp LOOP</i>
MCR	x0000	0	!	▶	x300A x10A0 4256 <i>Positive ADD R0, R2, #0</i>
			!	▶	x300B x0FF6 4086 <i>BRnzp LOOP</i>
			!	▶	x300C xF025 -4059 <i>Done HALT</i>
			!	▶	x300D x0003 3 <i>Data0 .FILL x0003</i>
			!	▶	x300E x000C 12 <i>Data1 .FILL x000C</i>
			!	▶	x300F x0000 0
			!	▶	x3010 x0000 0
			!	▶	x3011 x0000 0
			!	▶	x3012 x0000 0
			!	▶	x3013 x0000 0
			!	▶	x3014 x0000 0
			!	▶	x3015 x0000 0
			!	▶	x3016 x0000 0

Console (click to focus)

```

--- Halting the LC-3 ---


```

反过来 (12, 3)

Registers

R0	x0003	3
R1	x0003	3
R2	x0000	0
R3	x0000	0
R4	x0000	0
R5	x0000	0
R6	x0000	0
R7	x0000	0
PSR	x8002	-32766 CC: Z
PC	x300C	12300
MCR	x0000	0

Console (click to focus)

--- Halting the LC-3 ---

[]

Memory

!	▶	x3000	x200C	8204	LD R0, Data0
!	▶	x3001	x220C	8716	LD R1, Data1
!	▶	x3002	x947F	-27521	LOOP NOT R2, R1
!	▶	x3003	x14A1	5281	ADD R2, R2, #1
!	▶	x3004	x1402	5122	ADD R2, R0, R2
!	▶	x3005	x0406	1030	BRz Done
!	▶	x3006	x0203	515	BRp Positive
!	▶	x3007	x94BF	-27457	NOT R2, R2
!	▶	x3008	x12A1	4769	ADD R1, R2, #1
!	▶	x3009	x0FF8	4088	BRnzp LOOP
!	▶	x300A	x10A0	4256	Positive ADD R0, R2, #0
!	▶	x300B	x0FF6	4086	BRnzp LOOP
!	▶	x300C	xF025	-4059	Done HALT
!	▶	x300D	x000C	12	Data0 .FILL x000C
!	▶	x300E	x0003	3	Data1 .FILL x0003
!	▶	x300F	x0000	0	
!	▶	x3010	x0000	0	
!	▶	x3011	x0000	0	
!	▶	x3012	x0000	0	
!	▶	x3013	x0000	0	
!	▶	x3014	x0000	0	
!	▶	x3015	x0000	0	
!	▶	x3016	x0000	0	

1,1较为特殊 (1, 1)

Registers

R0	x0001	1
R1	x0001	1
R2	x0000	0
R3	x0000	0
R4	x0000	0
R5	x0000	0
R6	x0000	0
R7	x0000	0
PSR	x8002	-32766 CC: Z
PC	x300C	12300
MCR	x0000	0

Console (click to focus)

--- Halting the LC-3 ---

[]

Memory

!	▶	x3000	x200C	8204	LD R0, Data0
!	▶	x3001	x220C	8716	LD R1, Data1
!	▶	x3002	x947F	-27521	LOOP NOT R2, R1
!	▶	x3003	x14A1	5281	ADD R2, R2, #1
!	▶	x3004	x1402	5122	ADD R2, R0, R2
!	▶	x3005	x0406	1030	BRz Done
!	▶	x3006	x0203	515	BRp Positive
!	▶	x3007	x94BF	-27457	NOT R2, R2
!	▶	x3008	x12A1	4769	ADD R1, R2, #1
!	▶	x3009	x0FF8	4088	BRnzp LOOP
!	▶	x300A	x10A0	4256	Positive ADD R0, R2, #0
!	▶	x300B	x0FF6	4086	BRnzp LOOP
!	▶	x300C	xF025	-4059	Done HALT
!	▶	x300D	x0001	1	Data0 .FILL x0001
!	▶	x300E	x0001	1	Data1 .FILL x0001
!	▶	x300F	x0000	0	
!	▶	x3010	x0000	0	
!	▶	x3011	x0000	0	
!	▶	x3012	x0000	0	
!	▶	x3013	x0000	0	
!	▶	x3014	x0000	0	
!	▶	x3015	x0000	0	
!	▶	x3016	x0000	0	

(1, 8)

Registers			Memory		
R0	x0001	1	!	▶	x3000 x200C 8204 <i>LD R0, Data0</i>
R1	x0001	1	!	▶	x3001 x220C 8716 <i>LD R1, Data1</i>
R2	x0000	0	!	▶	x3002 x947F -27521 <i>LOOP NOT R2, R1</i>
R3	x0000	0	!	▶	x3003 x14A1 5281 <i>ADD R2, R2, #1</i>
R4	x0000	0	!	▶	x3004 x1402 5122 <i>ADD R2, R0, R2</i>
R5	x0000	0	!	▶	x3005 x0406 1030 <i>BRz Done</i>
R6	x0000	0	!	▶	x3006 x0203 515 <i>BRp Positive</i>
R7	x0000	0	!	▶	x3007 x94BF -27457 <i>NOT R2, R2</i>
PSR	x8002	-32766 CC: Z	!	▶	x3008 x12A1 4769 <i>ADD R1, R2, #1</i>
PC	x300C	12300	!	▶	x3009 x0FF8 4088 <i>BRnzp LOOP</i>
MCR	x0000	0	!	▶	x300A x10A0 4256 <i>Positive ADD R0, R2, #0</i>
			!	▶	x300B x0FF6 4086 <i>BRnzp LOOP</i>
			!	▶	x300C xF025 -4059 <i>Done HALT</i>
			!	▶	x300D x0001 1 <i>Data0 .FILL x0001</i>
			!	▶	x300E x0008 8 <i>Data1 .FILL x0008</i>
			!	▶	x300F x0000 0
			!	▶	x3010 x0000 0
			!	▶	x3011 x0000 0
			!	▶	x3012 x0000 0
			!	▶	x3013 x0000 0
			!	▶	x3014 x0000 0
			!	▶	x3015 x0000 0
			!	▶	x3016 x0000 0

Console (click to focus)

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--- Halting the LC-3 ---


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两个偶数，且最大公约数不是这两个数 (24, 32)

Registers

R0	x0008	8
R1	x0008	8
R2	x0000	0
R3	x0000	0
R4	x0000	0
R5	x0000	0
R6	x0000	0
R7	x0000	0
PSR	x8002	-32766 CC: Z
PC	x300C	12300
MCR	x0000	0

Memory

!	▶	x3000	x200C	8204	LD R0, Data0
!	▶	x3001	x220C	8716	LD R1, Data1
!	▶	x3002	x947F	-27521	LOOP NOT R2, R1
!	▶	x3003	x14A1	5281	ADD R2, R2, #1
!	▶	x3004	x1402	5122	ADD R2, R0, R2
!	▶	x3005	x0406	1030	BRz Done
!	▶	x3006	x0203	515	BRp Positive
!	▶	x3007	x94BF	-27457	NOT R2, R2
!	▶	x3008	x12A1	4769	ADD R1, R2, #1
!	▶	x3009	x0FF8	4088	BRnzp LOOP
!	▶	x300A	x10A0	4256	Positive ADD R0, R2, #0
!	▶	x300B	x0FF6	4086	BRnzp LOOP
!	▶	x300C	xF025	-4059	Done HALT
!	▶	x300D	x0018	24	Data0 .FILL x0018
!	▶	x300E	x0020	32	Data1 .FILL x0020
!	▶	x300F	x0000	0	
!	▶	x3010	x0000	0	
!	▶	x3011	x0000	0	
!	▶	x3012	x0000	0	
!	▶	x3013	x0000	0	
!	▶	x3014	x0000	0	
!	▶	x3015	x0000	0	
!	▶	x3016	x0000	0	

Console (click to focus)

--- Halting the LC-3 ---

--- Halting the LC-3 ---

□

一个偶数，一个奇数，但不互质 (33, 24)

Registers

R0	x0003	3
R1	x0003	3
R2	x0000	0
R3	x0000	0
R4	x0000	0
R5	x0000	0
R6	x0000	0
R7	x0000	0
PSR	x8002	-32766 CC: Z
PC	x300C	12300
MCR	x0000	0

Memory

!	▶	x3000	x200C	8204	LD R0, Data0
!	▶	x3001	x220C	8716	LD R1, Data1
!	▶	x3002	x947F	-27521	LOOP NOT R2, R1
!	▶	x3003	x14A1	5281	ADD R2, R2, #1
!	▶	x3004	x1402	5122	ADD R2, R0, R2
!	▶	x3005	x0406	1030	BRz Done
!	▶	x3006	x0203	515	BRp Positive
!	▶	x3007	x94BF	-27457	NOT R2, R2
!	▶	x3008	x12A1	4769	ADD R1, R2, #1
!	▶	x3009	x0FF8	4088	BRnzp LOOP
!	▶	x300A	x10A0	4256	Positive ADD R0, R2, #0
!	▶	x300B	x0FF6	4086	BRnzp LOOP
!	▶	x300C	xF025	-4059	Done HALT
!	▶	x300D	x0021	33	Data0 .FILL x0021
!	▶	x300E	x0018	24	Data1 .FILL x0018
!	▶	x300F	x0000	0	
!	▶	x3010	x0000	0	

Console (click to focus)

--- Halting the LC-3 ---

两个奇数，互质 (5, 7)

Registers

R0	x0001	1
R1	x0001	1
R2	x0000	0
R3	x0000	0
R4	x0000	0
R5	x0000	0
R6	x0000	0
R7	x0000	0
PSR	x8002	-32766 CC: Z
PC	x300C	12300
MCR	x0000	0

Memory

!	▶	x3000	x200C	8204	LD R0, Data0
!	▶	x3001	x220C	8716	LD R1, Data1
!	▶	x3002	x947F	-27521	LOOP NOT R2, R1
!	▶	x3003	x14A1	5281	ADD R2, R2, #1
!	▶	x3004	x1402	5122	ADD R2, R0, R2
!	▶	x3005	x0406	1030	BRz Done
!	▶	x3006	x0203	515	BRp Positive
!	▶	x3007	x94BF	-27457	NOT R2, R2
!	▶	x3008	x12A1	4769	ADD R1, R2, #1
!	▶	x3009	x0FF8	4088	BRnzp LOOP
!	▶	x300A	x10A0	4256	Positive ADD R0, R2, #0
!	▶	x300B	x0FF6	4086	BRnzp LOOP
!	▶	x300C	xF025	-4059	Done HALT
!	▶	x300D	x0005	5	Data0 .FILL x0005
!	▶	x300E	x0007	7	Data1 .FILL x0007
!	▶	x300F	x0000	0	
!	▶	x3010	x0000	0	
!	▶	x3011	x0000	0	
!	▶	x3012	x0000	0	
!	▶	x3013	x0000	0	
!	▶	x3014	x0000	0	

Console (click to focus)

--- Halting the LC-3 ---

--- Halting the LC-3 ---

[]

一个偶数，一个奇数，互质 (5, 12)

Registers

R0	x0001	1
R1	x0001	1
R2	x0000	0
R3	x0000	0
R4	x0000	0
R5	x0000	0
R6	x0000	0
R7	x0000	0
PSR	x8002	-32766 CC: Z
PC	x300C	12300
MCR	x0000	0

Console (click to focus)

--- Halting the LC-3 ---

--- Halting the LC-3 ---

Memory

!	▶	x3000	x200C	8204	LD R0, Data0
!	▶	x3001	x220C	8716	LD R1, Data1
!	▶	x3002	x947F	-27521	LOOP NOT R2, R1
!	▶	x3003	x14A1	5281	ADD R2, R2, #1
!	▶	x3004	x1402	5122	ADD R2, R0, R2
!	▶	x3005	x0406	1030	BRz Done
!	▶	x3006	x0203	515	BRp Positive
!	▶	x3007	x94BF	-27457	NOT R2, R2
!	▶	x3008	x12A1	4769	ADD R1, R2, #1
!	▶	x3009	x0FF8	4088	BRnzp LOOP
!	▶	x300A	x10A0	4256	Positive ADD R0, R2, #0
!	▶	x300B	x0FF6	4086	BRnzp LOOP
!	▶	x300C	xF025	-4059	Done HALT
!	▶	x300D	x0005	5	Data0 .FILL x0005
!	▶	x300E	x000C	12	Data1 .FILL x000C
!	▶	x300F	x0000	0	
!	▶	x3010	x0000	0	
!	▶	x3011	x0000	0	
!	▶	x3012	x0000	0	
!	▶	x3013	x0000	0	