

It is important that you read the assignment submission instructions and suggestions available on LEARN.

1. (3 marks) Let  $\vec{u}, \vec{v} \in \mathbb{C}^3$  with

$$\vec{u} = \begin{bmatrix} 1+j \\ 2-3j \\ 6+2j \end{bmatrix} \quad \text{and} \quad \vec{v} = \begin{bmatrix} 2j \\ 4 \\ -2+j \end{bmatrix}$$

- (a) Compute  $\vec{u} \cdot \vec{v}$
- (b) Compute  $\vec{v} \cdot \vec{u}$
- (c) Compute  $\|\vec{u}\|$  and  $\|\vec{v}\|$ .

2. (6 marks) Let

$$\vec{x} = \begin{bmatrix} -1 \\ 3 \\ 2 \end{bmatrix}, \quad \vec{y} = \begin{bmatrix} 4 \\ 1 \\ 2 \end{bmatrix} \quad \text{and} \quad \vec{z} = \begin{bmatrix} 3 \\ 1 \\ -2 \end{bmatrix}$$

- (a) Evaluate  $\vec{x} \times \vec{y}$ .
- (b) Compute the area of the triangle determined by  $\vec{x}$  and  $\vec{y}$ .
- (c) Find volume of the parallelepiped determined by  $\vec{x}$ ,  $\vec{y}$  and  $\vec{z}$ .
- (d) Compute  $\text{proj}_{\vec{x}} \vec{y}$ .
- (e) Compute  $\text{perp}_{\vec{x}} \vec{y}$ .

3. (4 marks) Let

$$\vec{u} = \begin{bmatrix} 1 \\ -1 \\ -1 \end{bmatrix} \quad \text{and} \quad \vec{v} = \begin{bmatrix} 2 \\ 1 \\ t \end{bmatrix}$$

For what values of  $t \in \mathbb{R}$  does the parallelogram determined by  $\vec{u}$  and  $\vec{v}$  have area equal to  $\sqrt{26}$ ?

4. (4 marks)

- (a) Find a *vector* equation for the line passing through the point  $(1, -1, 3)$  and parallel to the line that passes through the points  $A(1, 1, 2)$  and  $B(3, 2, -4)$ .
- (b) Find a *scalar* equation of the plane passing through the point  $(2, 7, 6)$  and parallel to the plane  $2x_1 - 3x_3 = 6$

5. (5 marks) Determine the coordinates of the point(s) of intersection of the line  $L$  with the plane  $T$  where  $L$  has vector equation

$$\begin{bmatrix} x \\ y \\ z \end{bmatrix} = \begin{bmatrix} -1 \\ 2 \\ 1 \end{bmatrix} + t \begin{bmatrix} 3 \\ 1 \\ 2 \end{bmatrix}, \quad t \in \mathbb{R}$$

and  $T$  has vector equation

$$\begin{bmatrix} x \\ y \\ z \end{bmatrix} = \begin{bmatrix} 4 \\ 1 \\ 6 \end{bmatrix} + s \begin{bmatrix} 1 \\ 1 \\ 2 \end{bmatrix} + r \begin{bmatrix} 1 \\ 3 \\ -1 \end{bmatrix}, \quad s, r \in \mathbb{R}$$

6. (5 marks) Find the shortest distance from the point  $P(1, 5, -2)$  to the line  $L$  passing through

$P_0(4, 3, 2)$  with direction vector  $\vec{d} = \begin{bmatrix} 3 \\ 3 \\ 2 \end{bmatrix}$ . Also, find the point  $Q$  on  $L$  that is closest to  $P$ .

**Total: 27 marks.**