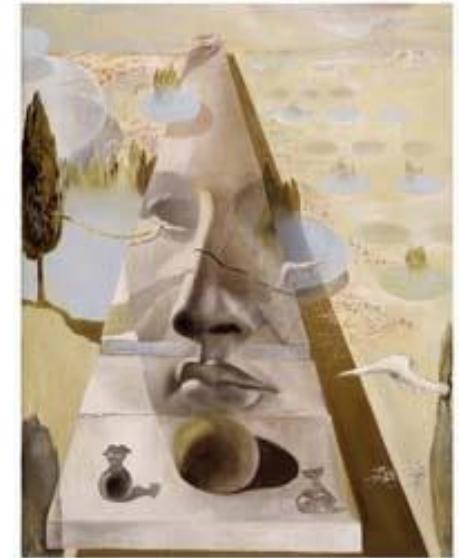


# CS231A

## Computer Vision: From 3D Reconstruction to Recognition

1891

Representation & Representation Learning

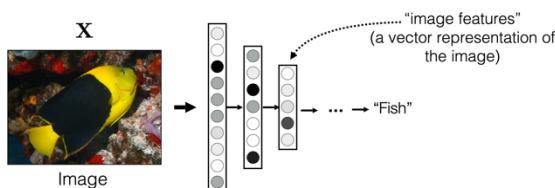


# How to reach me?

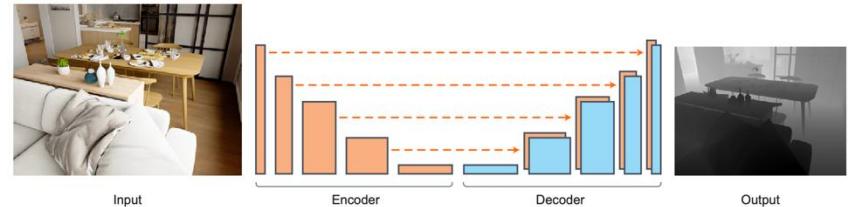
- Jeannette Bohg, CS, Assistant Professor in Robotics
- Office hours, Wednesdays 9am, Gates 244 or on zoom

# Learning Goals for Upcoming Lectures

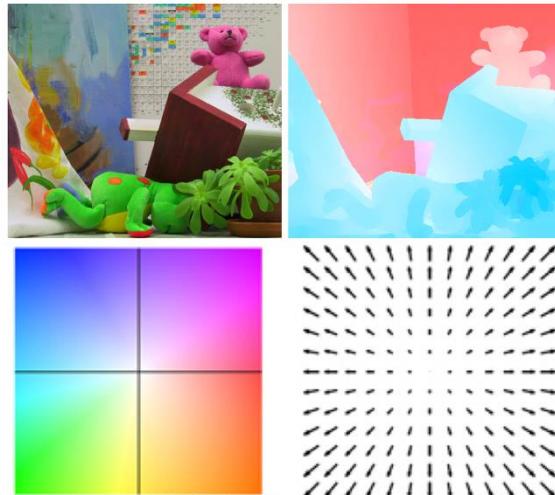
## Representations & Representation Learning



## Monocular Depth Estimation, Feature Tracking

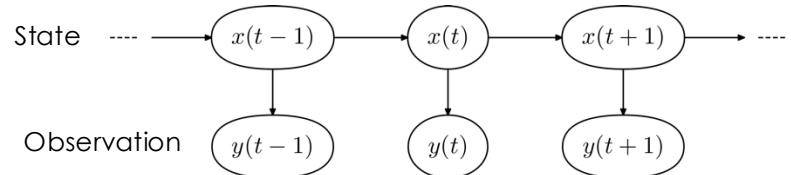


## Optical & Scene Flow

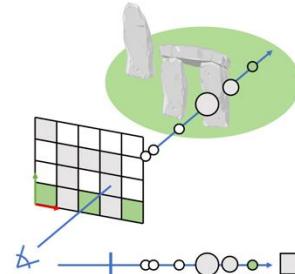


A Database and Evaluation Methodology for Optical Flow.  
Baker et al. IJCV. 2011

## Optimal Estimation



## Neural Radiance Fields



# Exercise

- Use an to manipulate (pen, water bottle, a mask, ...)
- What information do you need to solve a manipulation task, i.e., to make decision?
- How do you get this information?

## Representations for Manipulation Tasks

0 surveys completed



0 surveys underway



Start the presentation to see live content. For screen share software, share the entire screen. Get help at [pollev.com/app](https://pollev.com/app)

## How do you get this information? (Be concise)

Join by Web

[PollEv.com/jeannetteboh707](https://PollEv.com/jeannetteboh707)

Join by QR code

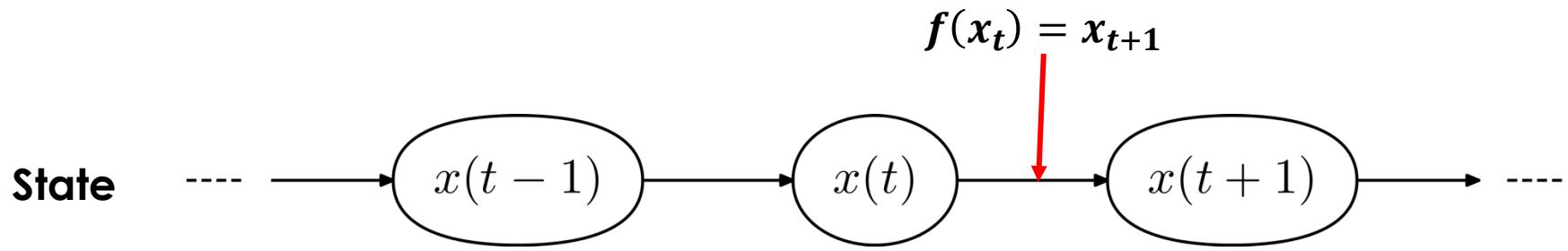
Scan with your camera app



# Outline of this lecture

- What is a state? What is a representation?
- What are the different kinds of representations?
- How can we extract state from raw sensory data?
- How can we learn good representations from data?

# What is a state? What is a representation?



Markov Model



Sparse Cartpole



Acrobot Swingup



Hopper Hop



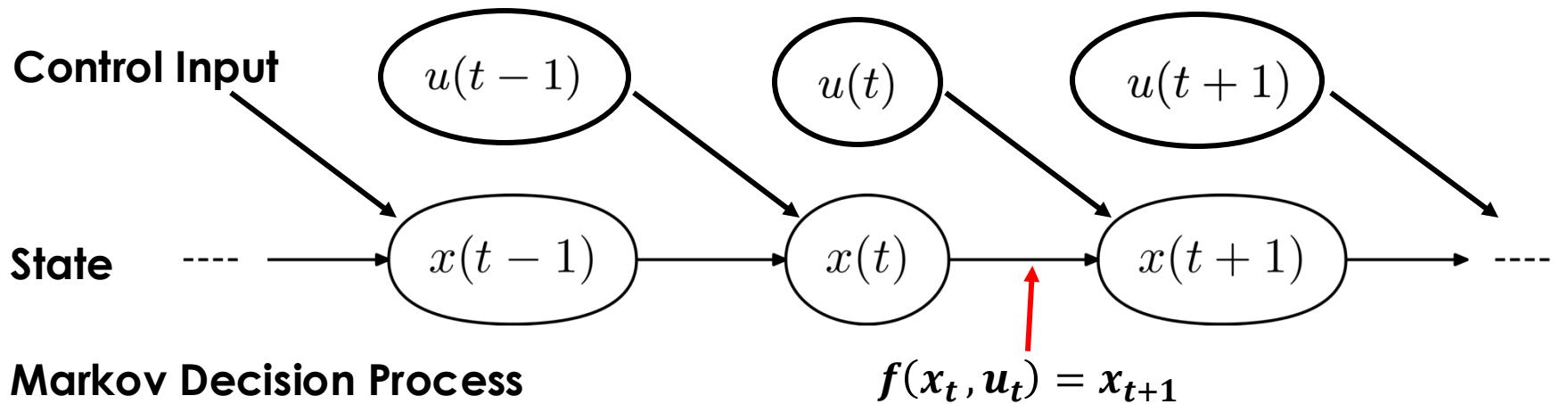
Walker Run



Quadruped Run

DeepMind Control Suite. Tassa et al. 2018

# What is a state? What is a representation?



Sparse Cartpole



Acrobot Swingup



Hopper Hop



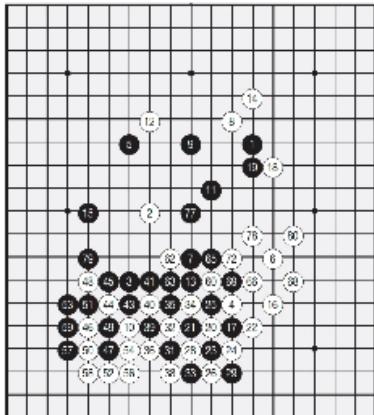
Walker Run



Quadruped Run

DeepMind Control Suite. Tassa et al. 2018

# What is a state? What is a representation?



$3^{361}$  states?

## Game of Go

- an exponentially large number of states?
- infeasible to enumerate, memorize, or search



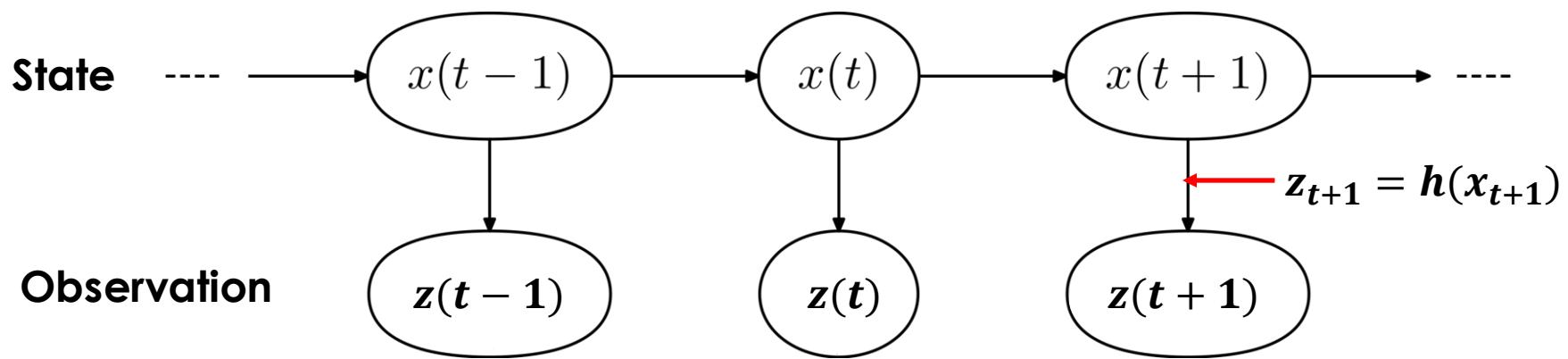
$256^{3 \times 500 \times 500}$ ?

## Images

Image space has exponentially more states than Go.

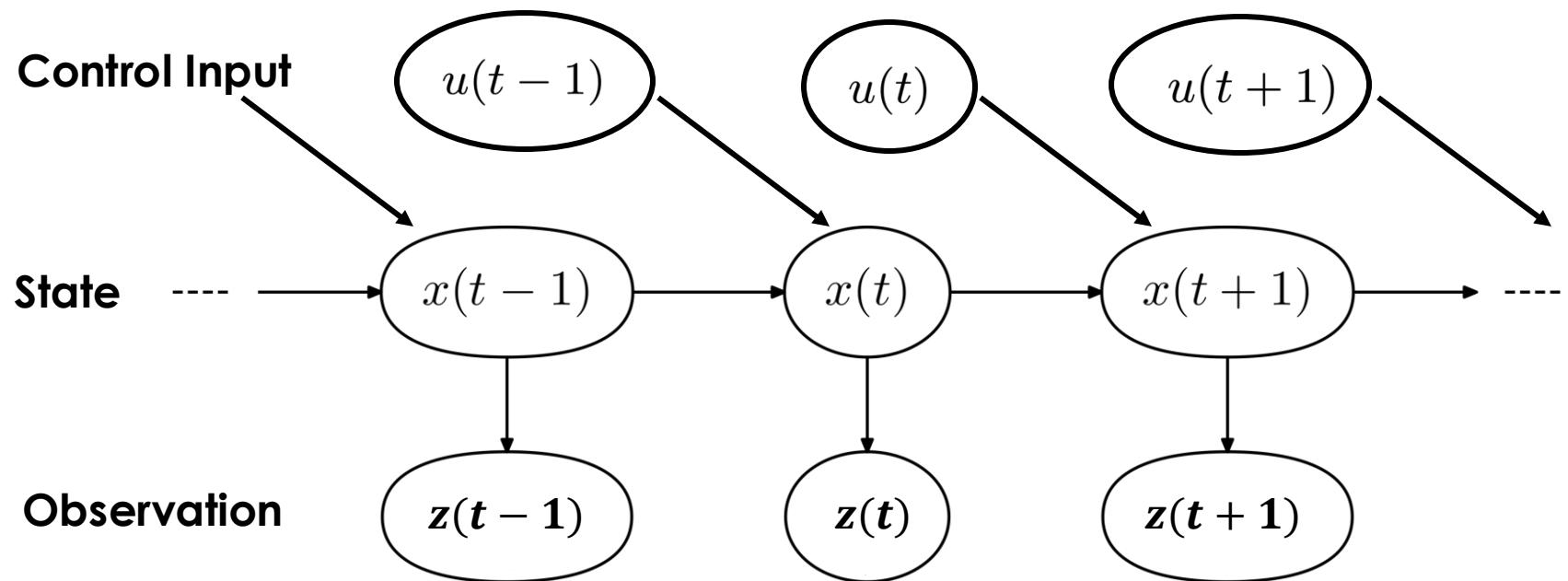
Examples from MIT - 6.8300/1 Advances in Computer Vision

# What is a state? What is a representation?



## Hidden Markov Model

# What is a state? What is a representation?



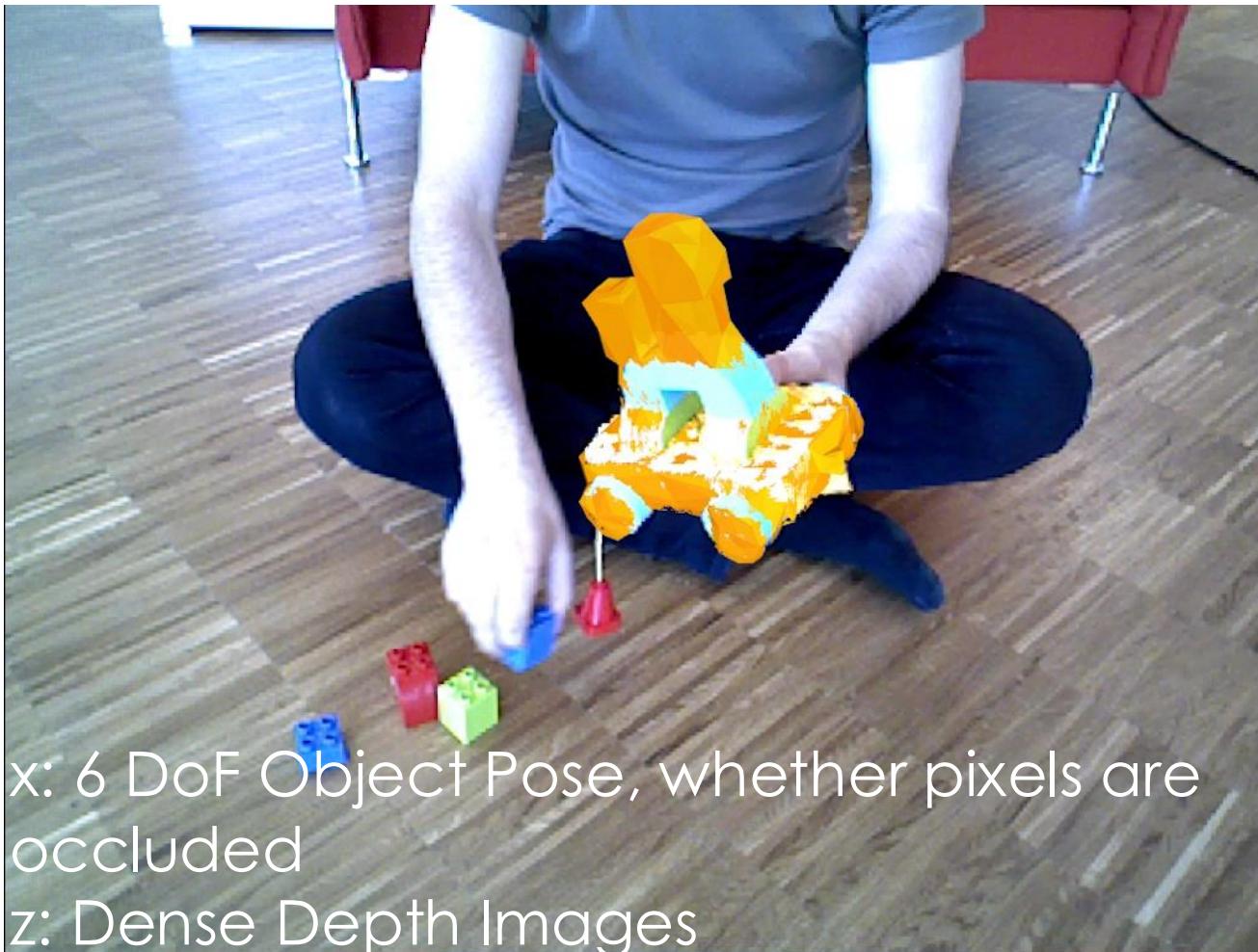
**Partially Observable Markov Decision Process**

# Representations for Autonomous Driving



Image adapted from NuScenes by Motional. [nuscenes.org](https://nuscenes.org)

# Representations for Manipulation



Manuel Wüthrich et al. "Probabilistic Object Tracking using a Depth Camera", IROS 2013

# Meaning in English

“the way that someone or something is shown or described:”

“a sign, picture, model, etc. of something”

- Cambridge Dictionary

# Representations in Cognitive Science

## Symbolic View

“[...] a hypothetical internal cognitive symbol that represents external reality” (Morgan '14)

“[...] a formal system for making explicit certain entities or types of information [...]” (Marr '10)

“[...] intermediaries between the observing subject and the objects, processes or other entities observed in the external world. These intermediaries [...] represent to the mind the objects of that world.” (Wikipedia - Mental Representations - Representationalism )

## Embodied View

“... actions are directly triggered by stimuli in the environment without the need for internal representations” (Gibson '66, Zech '19 on Embodied Cognition)

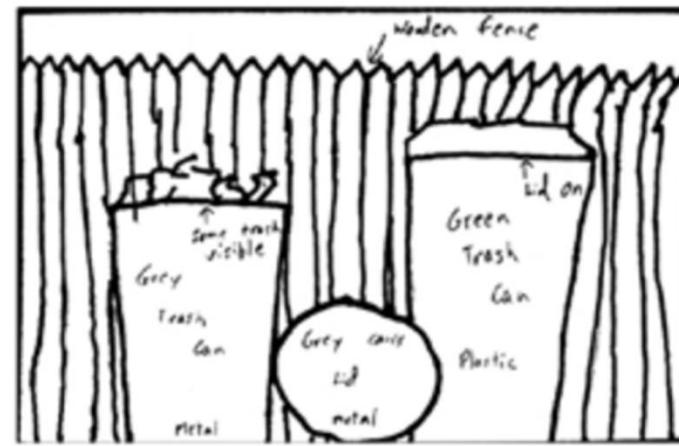
“... actions are represented by their anticipated effect, that is, action representations essentially entail a mental model of a needed future environmental state” (Jeannerod '06, Zech '19)

# Representations in Cognitive Science

Observed image



Drawn from memory



[Bartlett, 1932]

[Intraub & Richardson, 1989]

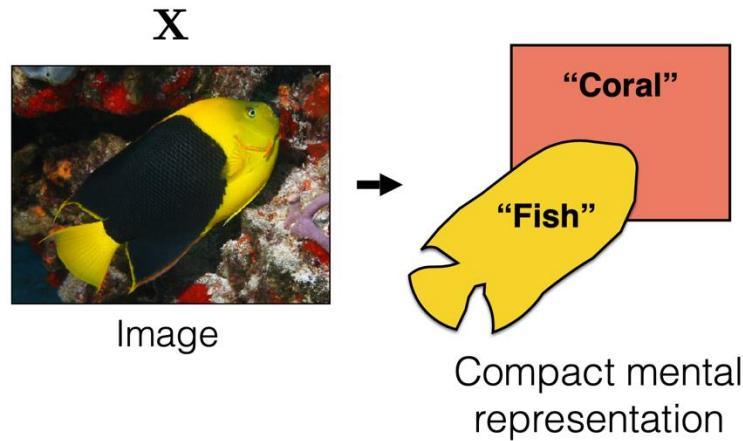
# Representations in Machine Learning

“Features”, “A good representation is also one that is useful as input to a supervised predictor.” (Bengio ’14)

“create a representation of the data to provide the model with a useful vantage point into the data's key qualities. [...] to train a model, you must choose the set of features that best represent the data.” (Google Crash Course of ML Concepts)

“ [...] world models, internal models of how the world works.”; “(1) estimate missing information about the state of the world not provided by perception, (2) predict plausible future states of the world.” (YLC ’22)

# Representations in Computer Vision



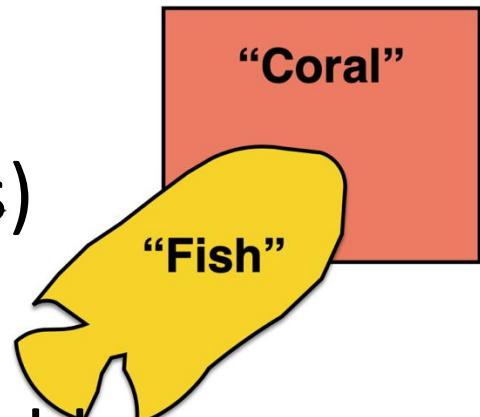
**Input:** grey scale, color, depth image, point cloud – Sensor measurements of the world

**Output:** Symbols, abstract shapes, 6D pose – Often Representation for Decision-Making

**Intermediate Representations:** Compact summary of the sensory information

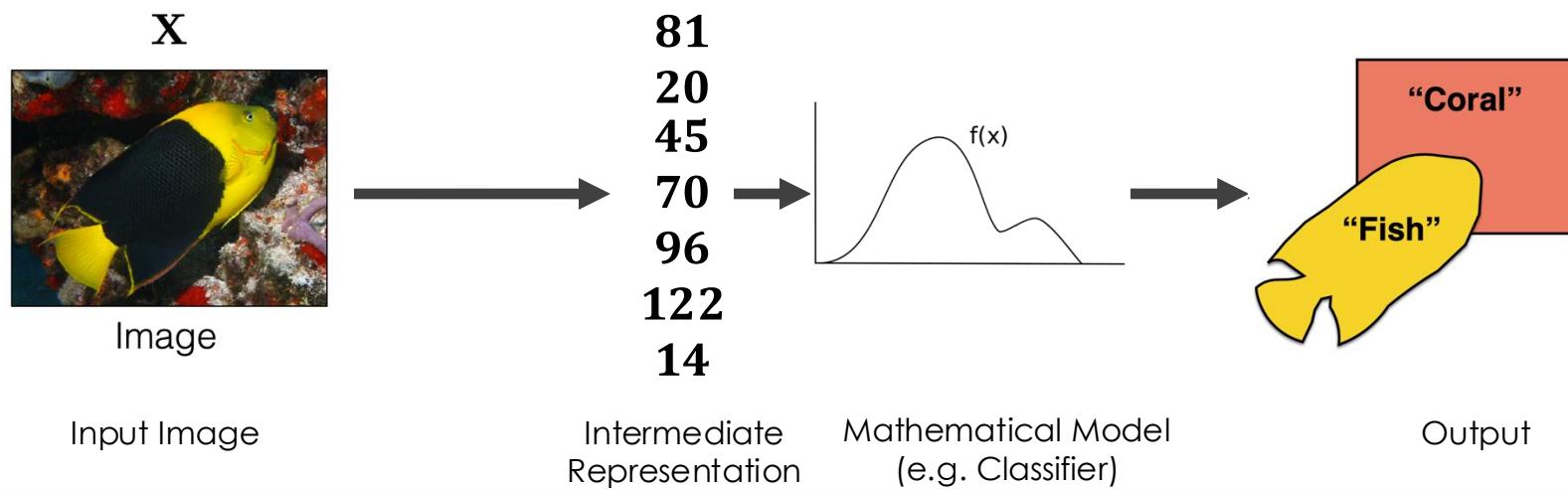
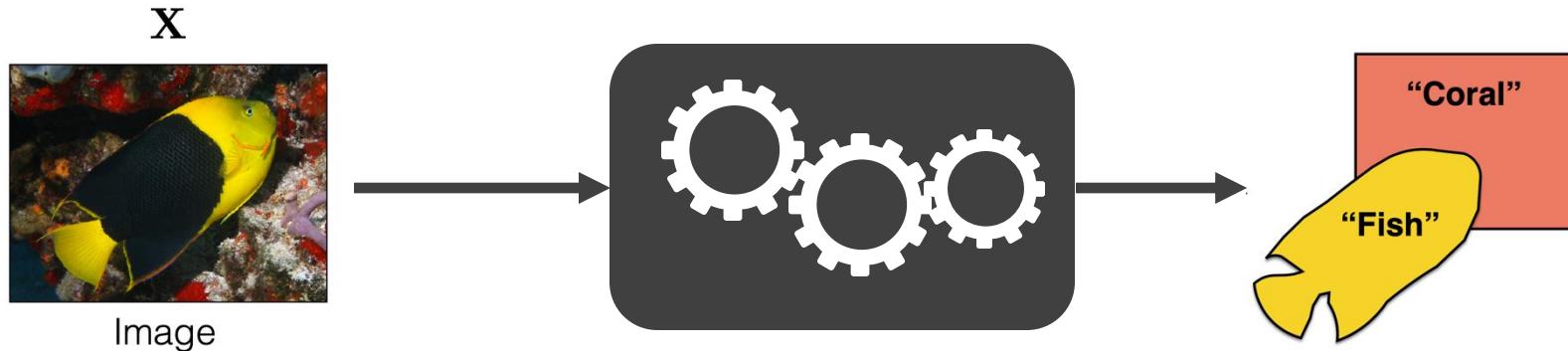
# Requirements for Good Representations

- Compact (minimal)
- Explanatory (sufficient)
- Disentangled (independent factors)
- Hierarchical (feature reuse)
- Makes downstream perception problem easier
- Generalizes over many tasks

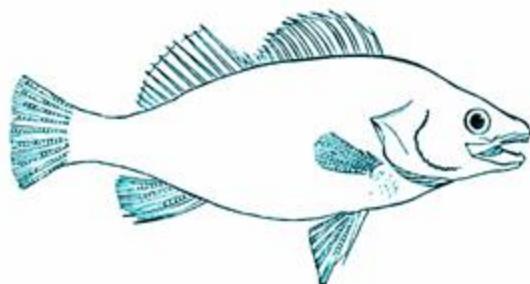


[See “Representation Learning”, Bengio 2013, for more commentary]

# Typical CV Pipeline



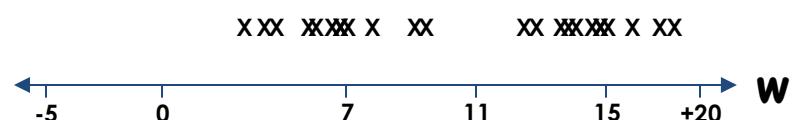
# Example



**~12 lbs**

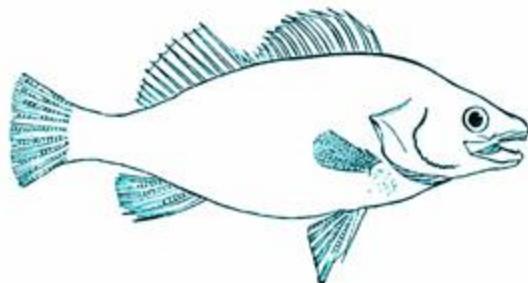


**~8 lbs**

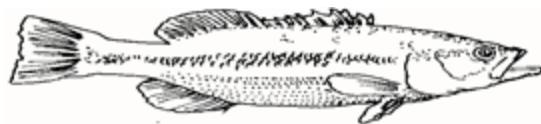


Example from CS331B: Representation Learning in Computer Vision

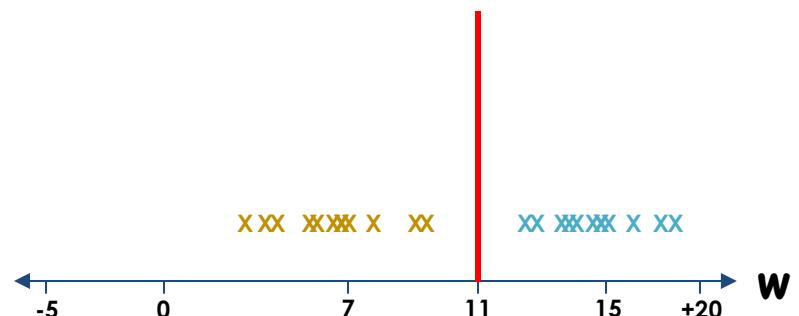
# Example



**~12 lbs**

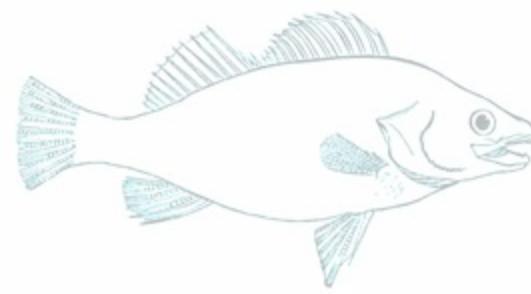


**~8 lbs**



Example from CS331B: Representation Learning in Computer Vision

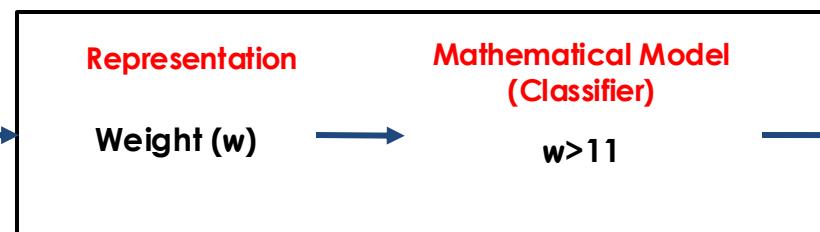
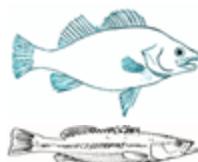
# Example



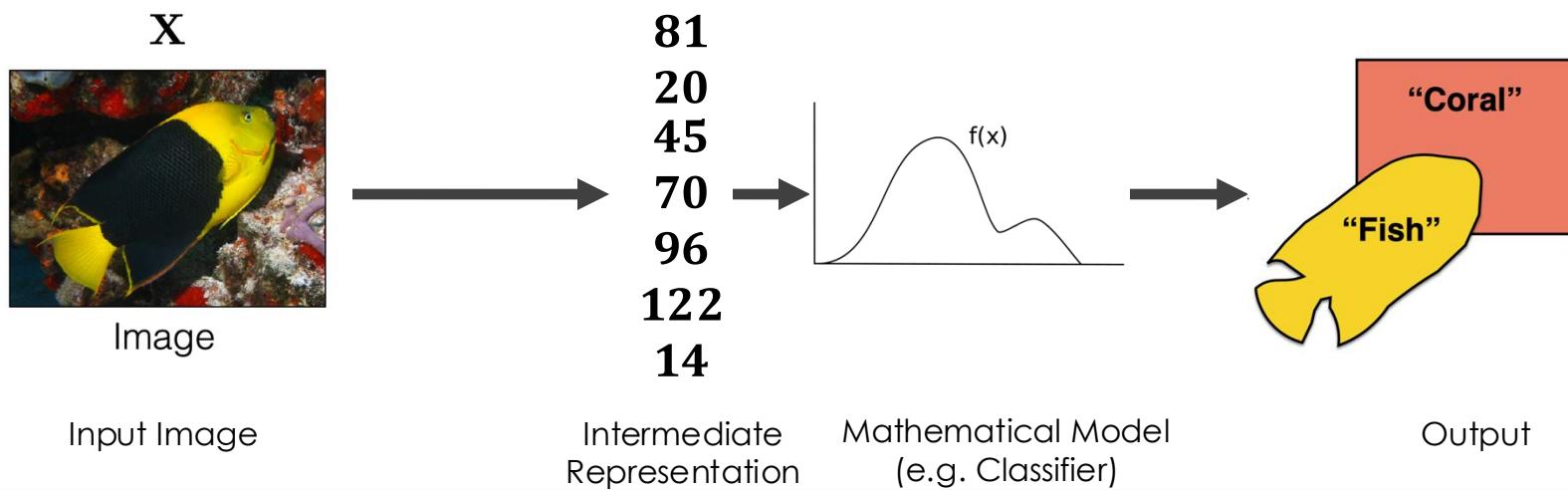
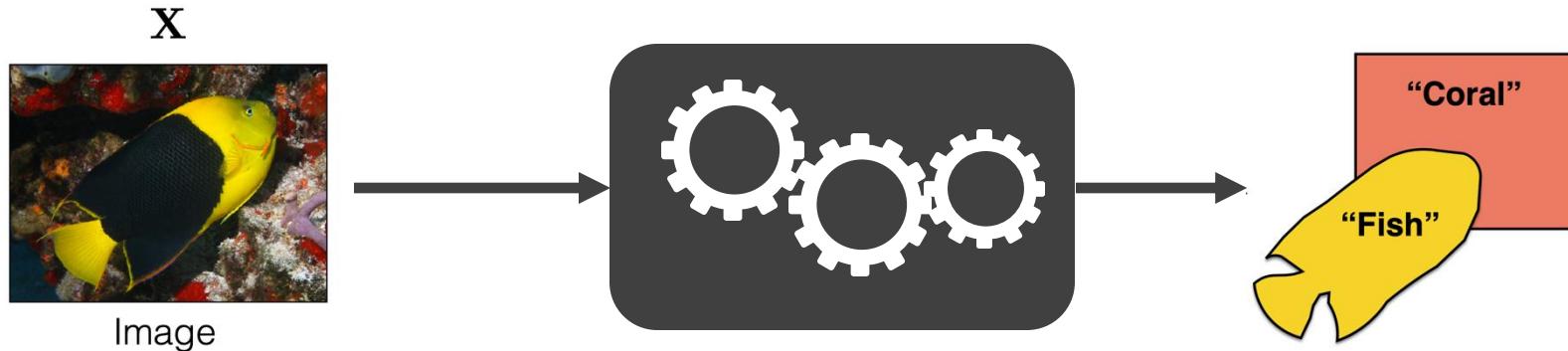
~12 lbs



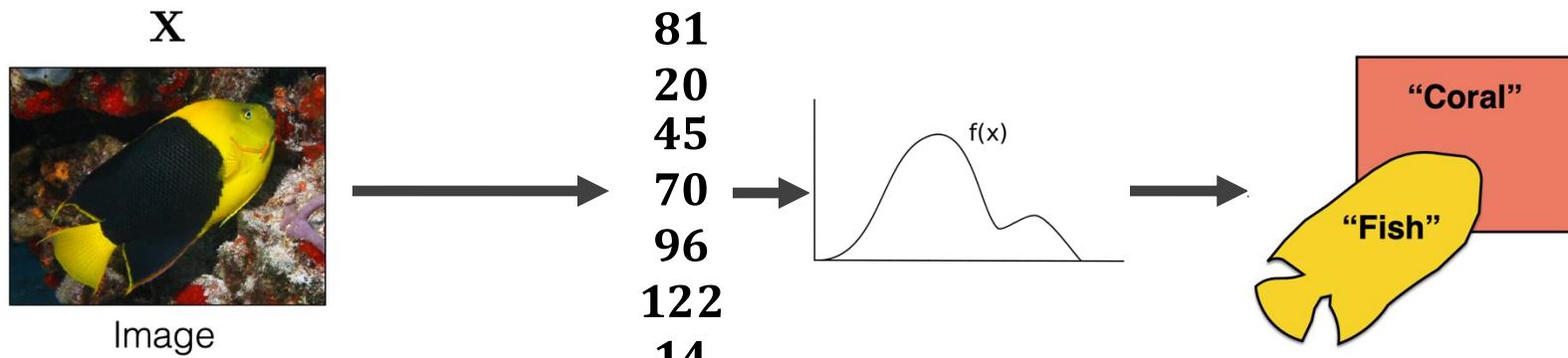
~8 lbs



# Typical CV Pipeline



# Traditional CV Pipeline



Input Image

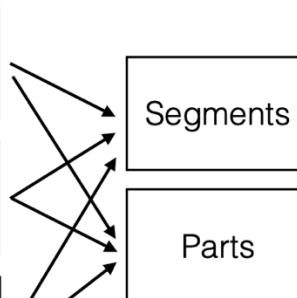
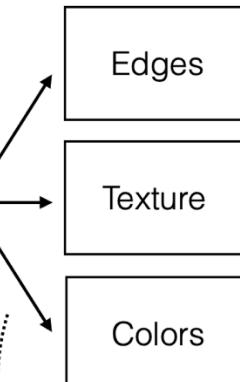
81  
20  
45  
70  
96  
122  
14

Intermediate Representation  
(e.g. Classifier)

Output



Feature extractors

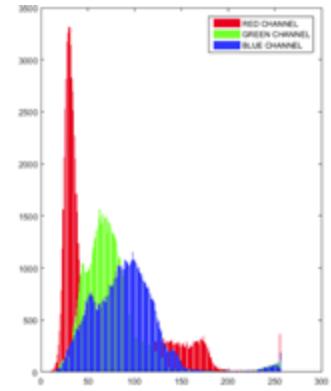


"clown fish"

Classifier

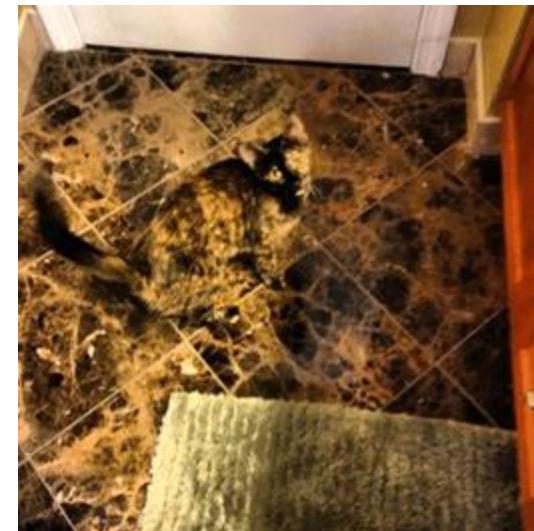
Example from Advances in Computer Vision – MIT – 6.869/6.819

# Represent these cats with a cat detector!



Example from CS331B: Representation Learning in Computer Vision

# Represent these cats with a cat detector! (II)



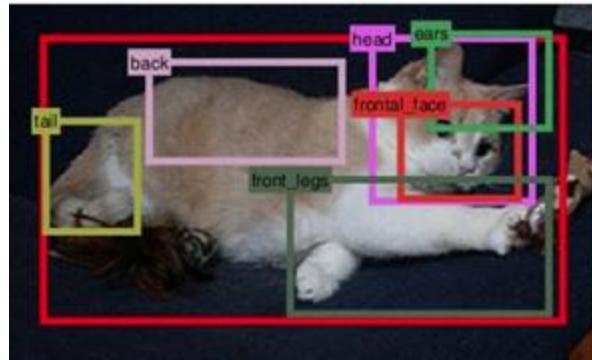
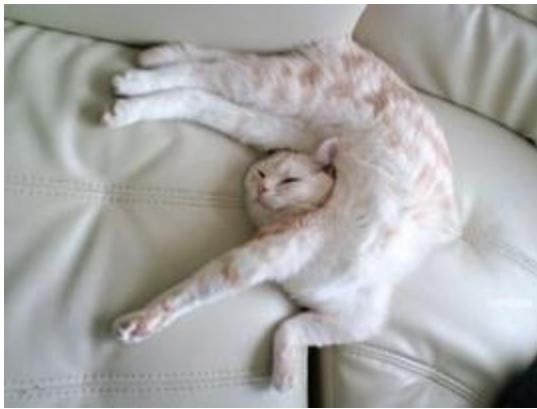
Example from CS331B: Representation Learning in Computer Vision

# Represent these cats with a cat detector! (II)



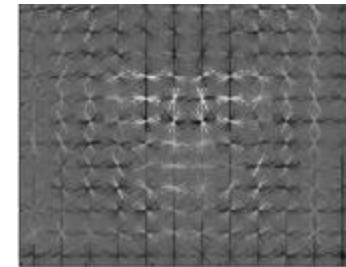
Example from CS331B: Representation Learning in Computer Vision

# Represent these cats with a cat detector! (III)



Example from CS331B: Representation Learning in Computer Vision

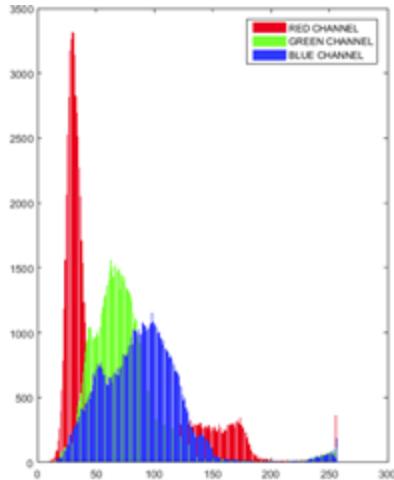
# Represent these cats with a cat detector! (IV)



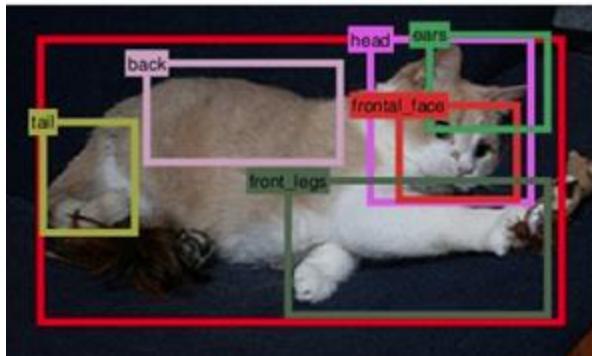
Example from CS331B: Representation Learning in Computer Vision

# Summary of Traditional Components

Color  
Histograms



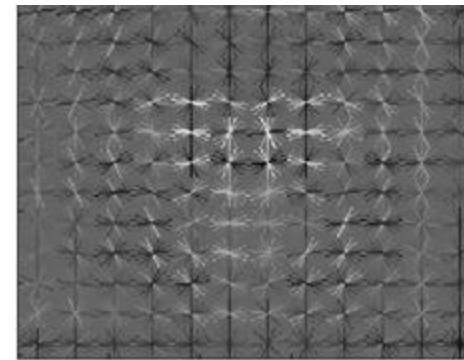
Deformable  
Part based  
Models  
(DPM)



Felzenszwalb et al. 2010.  
Dalal and Triggs, 2005.  
Beis and Lowe, 1997.



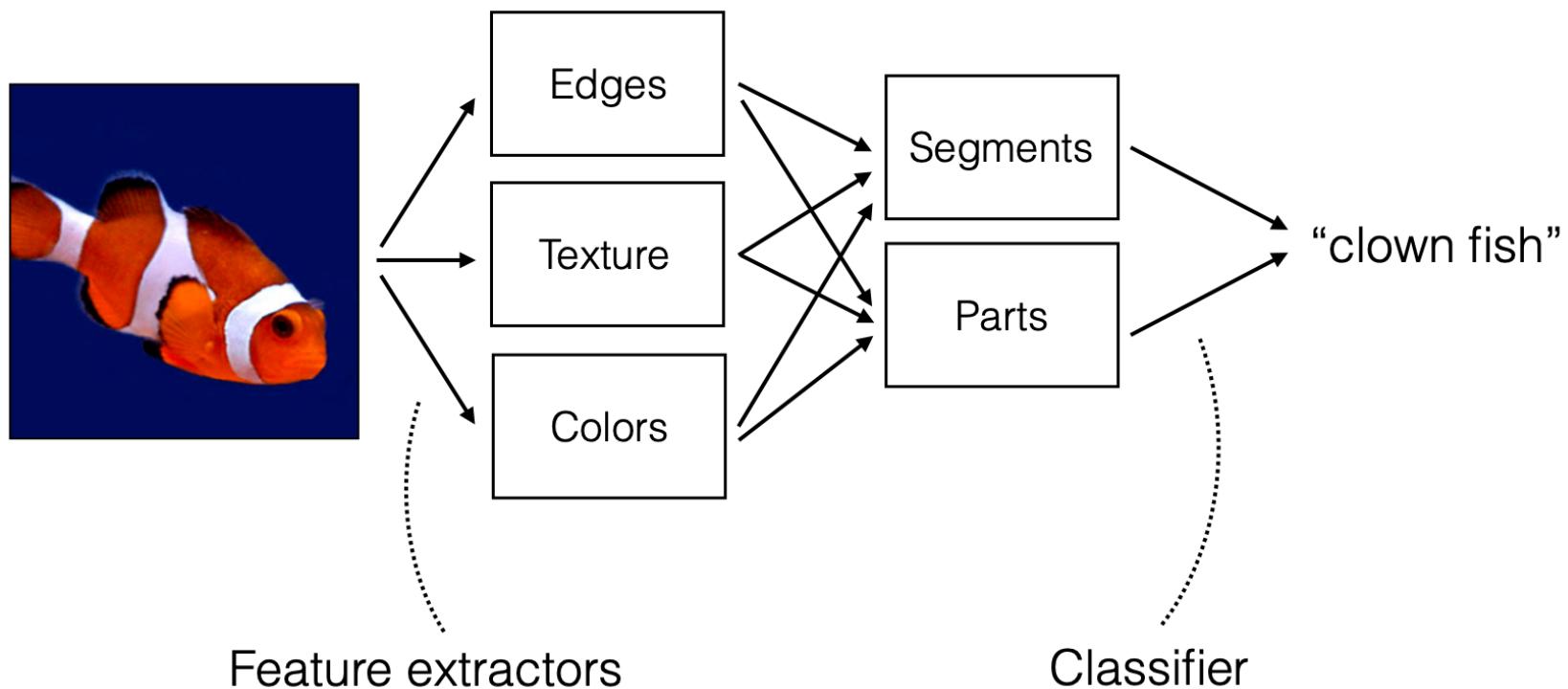
Model  
based  
Shapes



Histogram  
of  
Gradients  
(HOG)

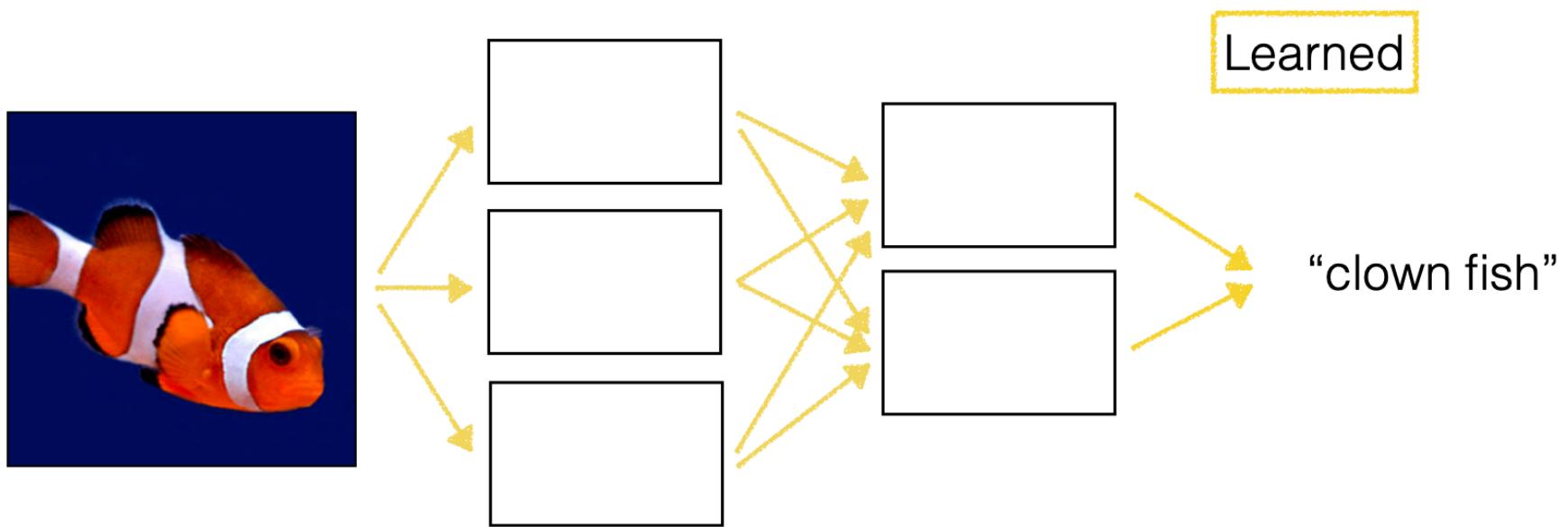
Example from CS331B: Representation Learning in Computer Vision

# Traditional CV Pipeline



Example from Advances in Computer Vision – MIT – 6.869/6.819

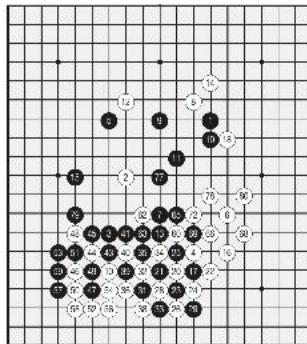
# Learned CV Pipeline



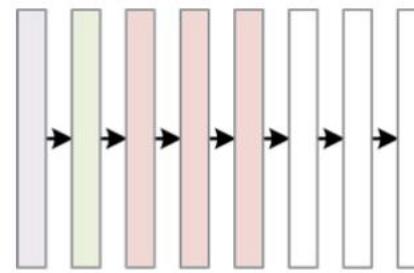
Example from Advances in Computer Vision – MIT – 6.869/6.819

# Learned CV Pipeline

Go playing can be solved in representation space.



$3^{361}$  states?



*Good representation*



$256^{3 \times 500 \times 500}$ ?

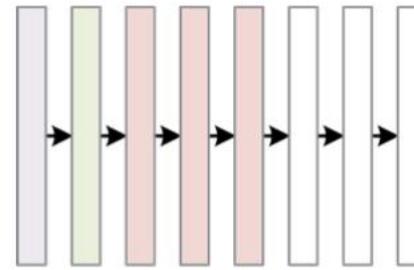
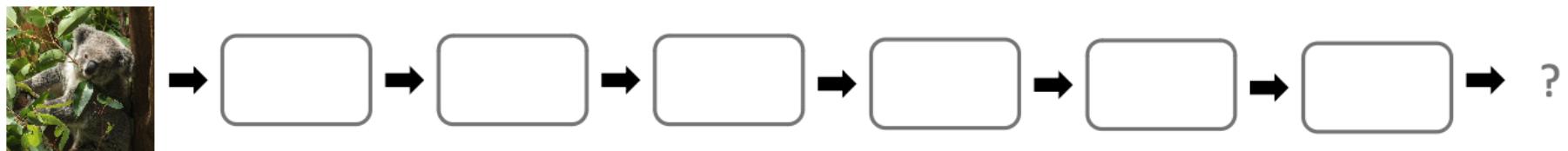


Image recognition is solved in representation space.

Examples from MIT - 6.8300/1 Advances in Computer Vision

# Learned CV Pipeline

general modules (instead of specialized features)



**compose simple modules into complex functions**

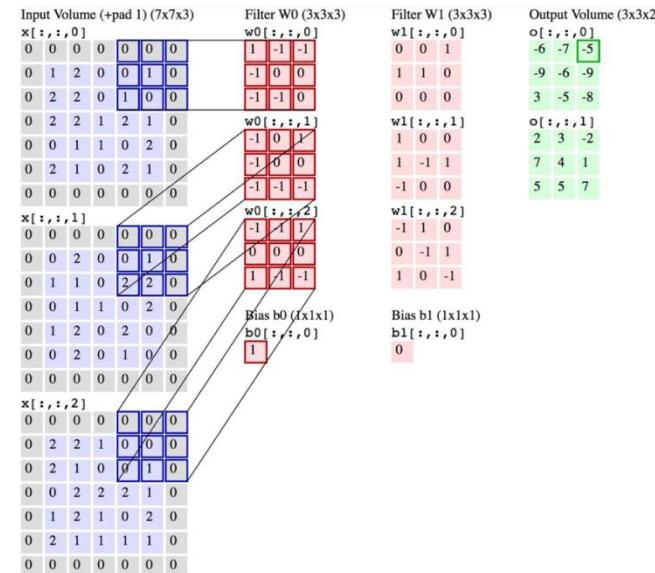
- build multiple levels of abstractions
- learn by back-prop
- learn from data
- reduce domain knowledge and feature engineering

# Introduction to Neural Networks and CNNs

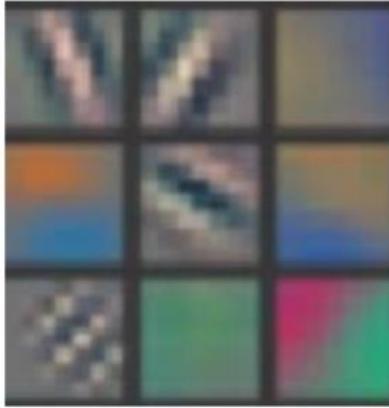
- Check Friday's CA Session (5/9)

## Components

- Each convolutional “layer” is represented by a 3D tensor of shape  $[h \times w \times n_{\text{channels}}]$
- Between two convolutional layers, the weights are of the shape [relative x-position, relative y-position, input channels, output channels]
- “Convolve” operation consists of 4 hyperparameters:
  - Number of filters, or *depth* (each channel also called an “activation map”)
  - *Spatial extent*, or *receptive field*
  - The stride
  - Amount of zero-padding
- With this, the shape of layer  $i$  convolved from layer  $i - 1$  is:
  - $[(W - F + 2P)/S + 1, (H - F + 2P)/S + 1, K]$



# Multiple Levels of Representations



features

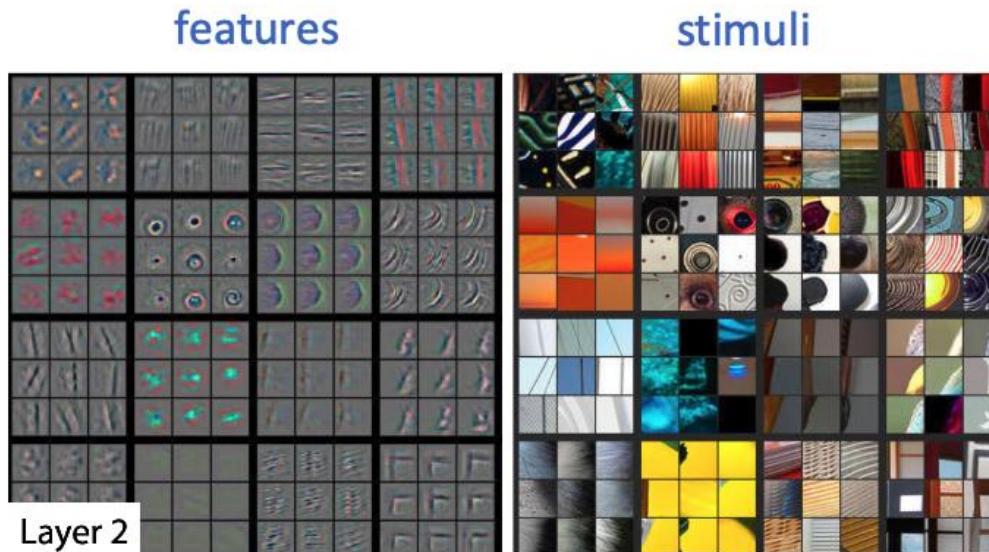


stimuli  
(patches with the highest  
1-hot activations)

"Visualizing and Understanding Convolutional Networks", Zeiler & Fergus. ECCV 2014

Examples from MIT - 6.8300/1 Advances in Computer Vision

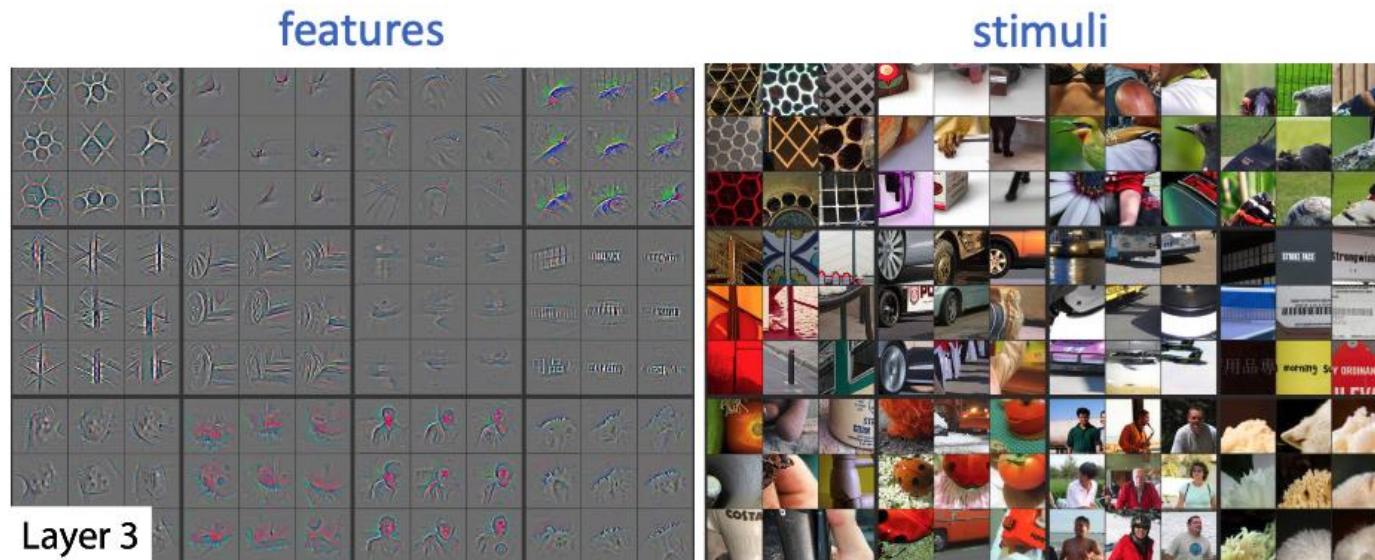
# Multiple Levels of Representations



"Visualizing and Understanding Convolutional Networks", Zeiler & Fergus. ECCV 2014

Examples from MIT - 6.8300/1 Advances in Computer Vision

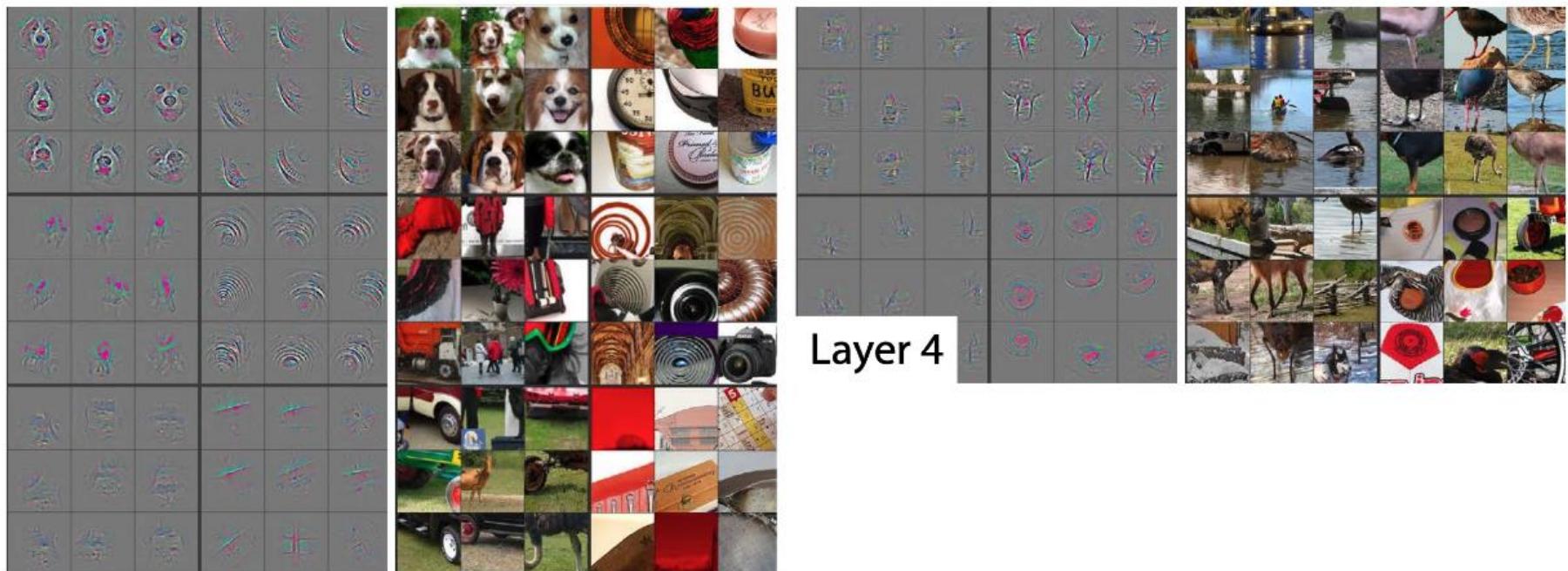
# Multiple Levels of Representations



"Visualizing and Understanding Convolutional Networks", Zeiler & Fergus. ECCV 2014

Examples from MIT - 6.8300/1 Advances in Computer Vision

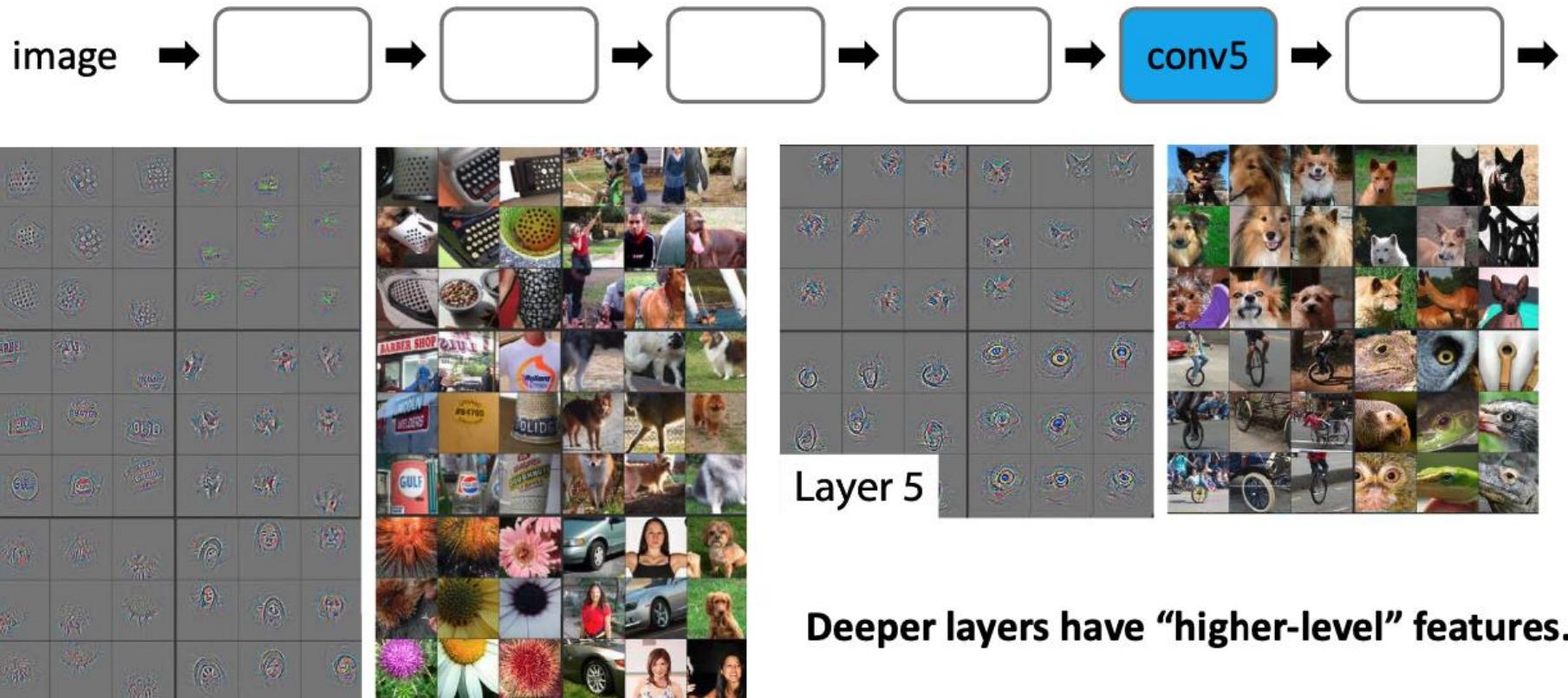
# Multiple Levels of Representations



"Visualizing and Understanding Convolutional Networks", Zeiler & Fergus. ECCV 2014

Examples from MIT - 6.8300/1 Advances in Computer Vision

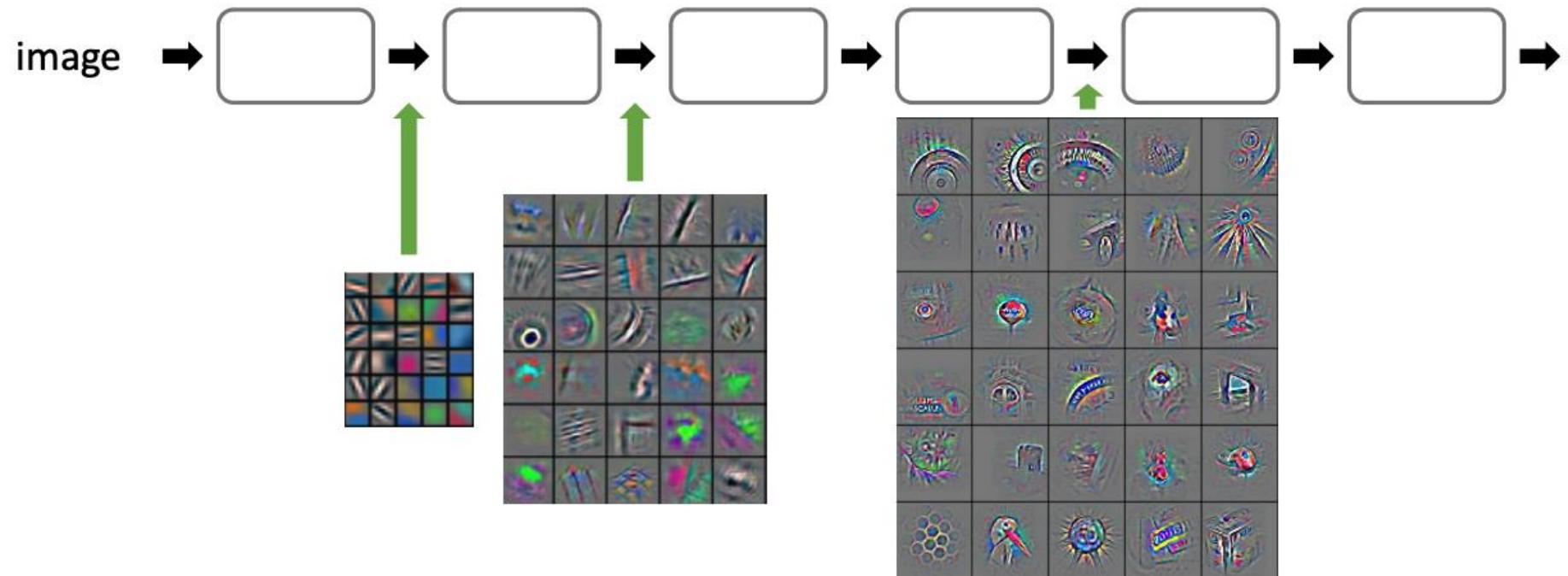
# Multiple Levels of Representations



“Visualizing and Understanding Convolutional Networks”, Zeiler & Fergus. ECCV 2014

Examples from MIT - 6.8300/1 Advances in Computer Vision

# Multiple Levels of Representations



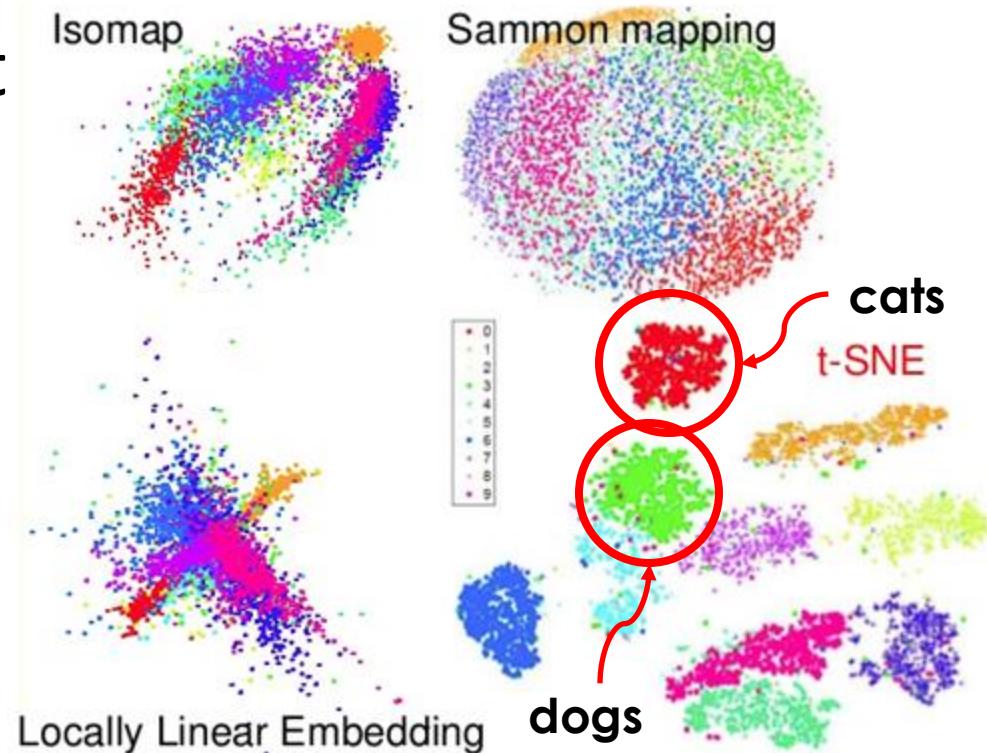
**Deeper layers have “higher-level” features.**

“Visualizing and Understanding Convolutional Networks”, Zeiler & Fergus. ECCV 2014

Examples from MIT - 6.8300/1 Advances in Computer Vision

# Understanding representations through low-dimensional embeddings

- 6000 MNIST Digit
  - tSNE
  - Isomap
  - Sammon M
  - LLE



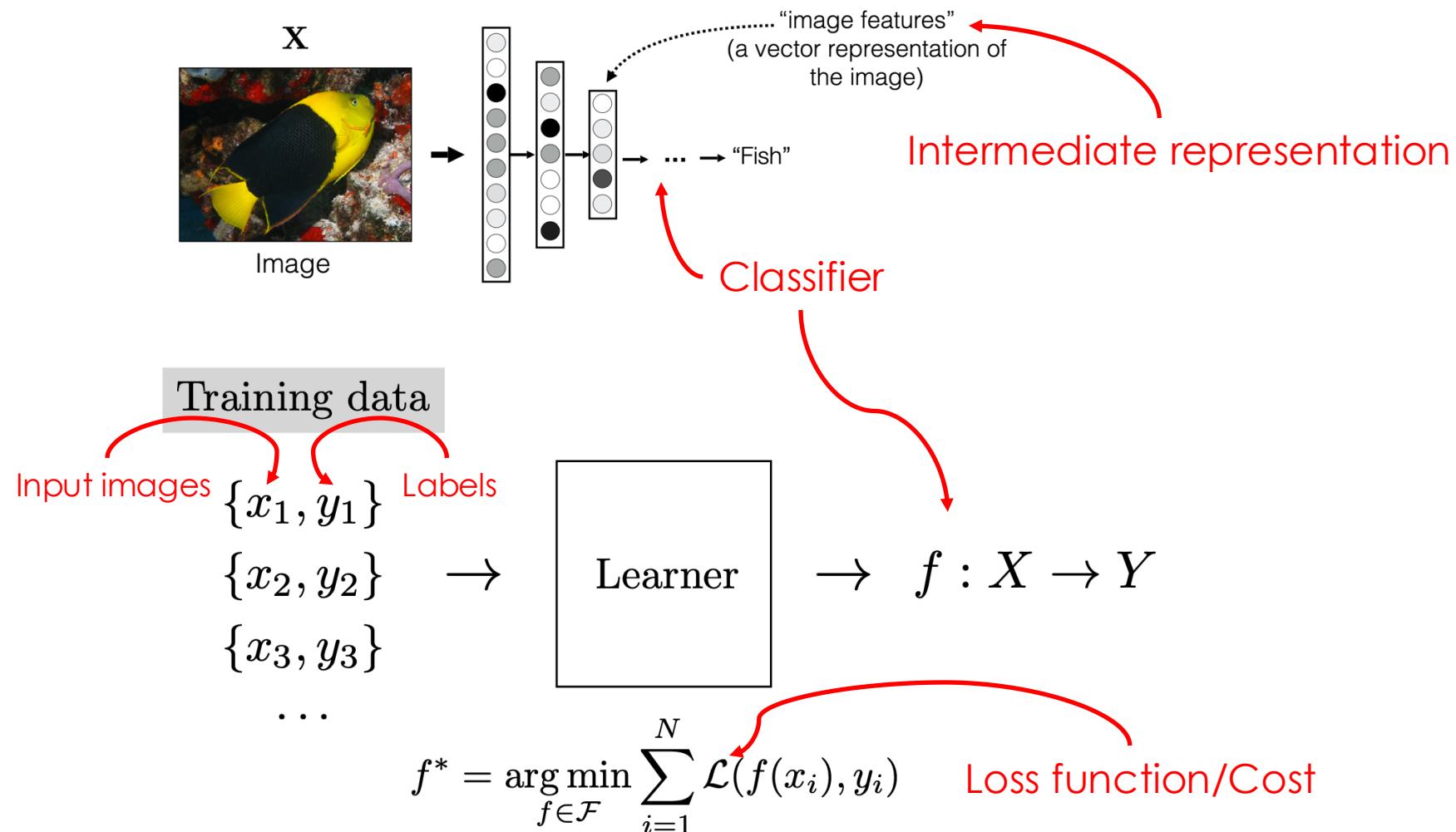
# Understanding representations through low-dimensional embeddings

- tSNE



Van der Maaten & Hinton. 2008

# How do you learn a representation?

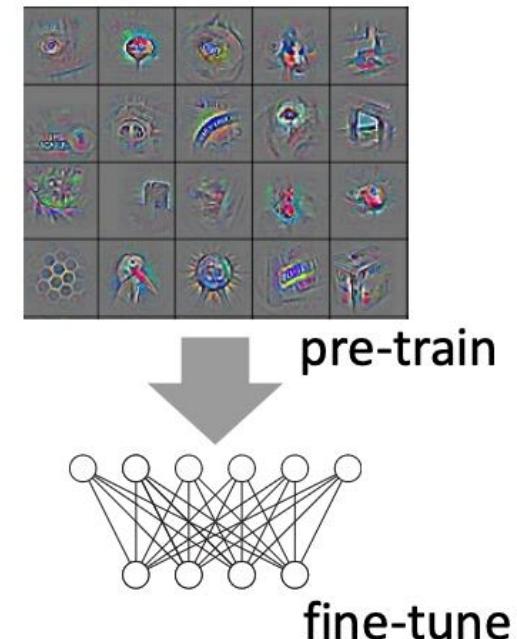


# Learned Representations are Transferable

The single most important discovery in DL revolution

Transfer learning:

- pre-train on large-scale data
- fine-tune on small-scale data
- enable DL for small datasets
- revolutionize computer vision
- data: engine for general representation
- GPT: a similar principle



"DeCAF: A Deep Convolutional Activation Feature for Generic Visual Recognition", Donahue et al. arXiv 2013

"Visualizing and Understanding Convolutional Networks", Zeiler & Fergus. arXiv 2013

"CNN Features off-the-shelf: an Astounding Baseline for Recognition", Razavian. arXiv 2014

# Transfer learning: Pre-training & Fine-tuning

## Pre-training



### Pre-training:

- to learn **general** representations
- on **large-scale** data
- train for a **long** time
- with **large** models

# Transfer learning: Pre-training & Fine-tuning

## Pre-training



## Fine-tuning



## Fine-tuning:

- transfer weights to **specific** tasks
- on **small-scale** data
- train for a **short** time, **lower** learning rate
- enable **large** models with lower risk of overfitting

# Transfer learning: Pre-training & Fine-tuning

## Pre-training



## Fine-tuning



## Partial transfer

- pre-train and target domains may differ
- highest-level features are too adapted to pre-training
- randomly initialize new layers

# Transfer learning: Pre-training & Fine-tuning

## Pre-training



## Fine-tuning



## Frozen weights

- freeze some/all pre-trained weights
- reduce overfitting if data is too little
- save memory, speed up training

# Transfer learning: Pre-training & Fine-tuning

## Pre-training



## Fine-tuning



## Network surgery

- re-purpose the model for other tasks (detect, segment)
- general features + task-specific predictions

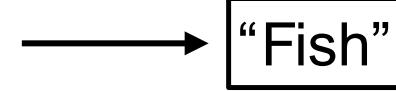
# How can we (pre-)train good representations?

- **Model** (network architecture)
  - scaling: deep, wide, large
  - inductive bias: convolution, recurrency, attention
- **Data**
  - scaling
  - curating, cleaning, filtering, ...
- **Learning objective**
  - supervised
  - unsupervised
  - self-supervised

# Supervised Object Recognition



image X

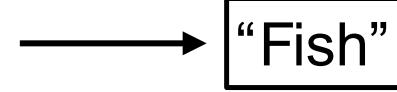


label Y

# Supervised Object Recognition



image X

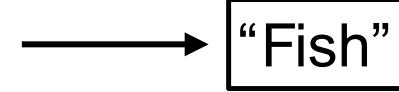


label Y

# Supervised Object Recognition

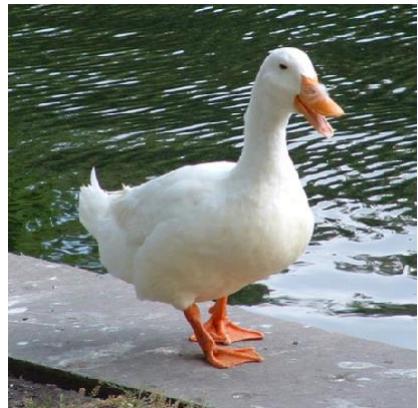


image X



label Y

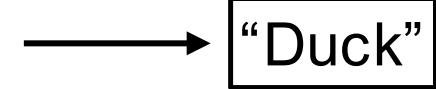
# Supervised Object Recognition



⋮

A vertical ellipsis indicating multiple inputs.

image X



label Y

# Learning in the wild



Time lapse of a baby playing with toys. Francis Vachon. YouTube

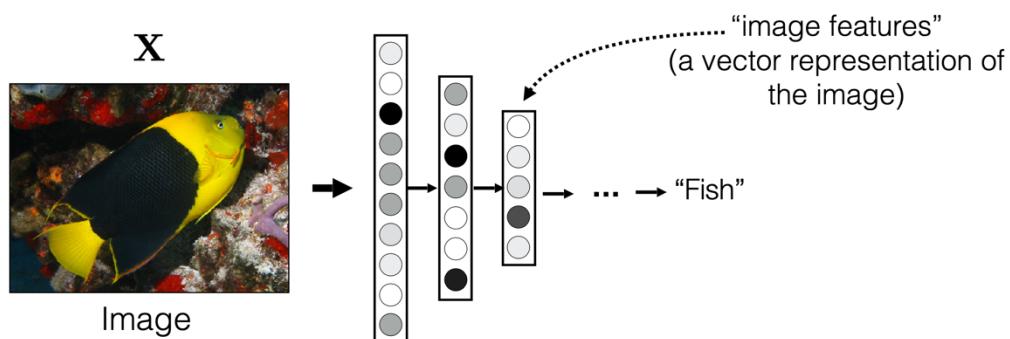
## **Supervised Computer Vision**

- Informative
- Expensive
- Limited to teacher knowledge

## **Vision in Nature**

- Cheap
- Noisy
- Harder to interpret

# Learning without Labels



Training data

$$\{x_1, y_1\}$$

$$\{x_2, y_2\}$$

$$\{x_3, y_3\}$$

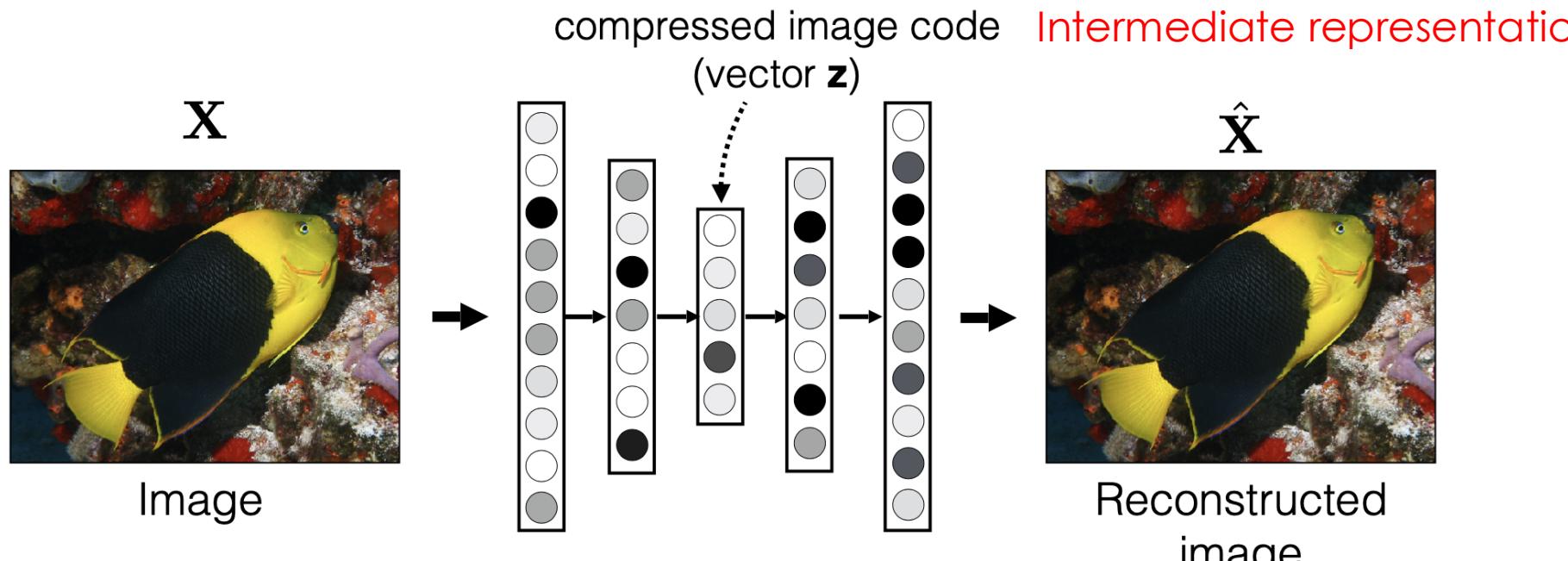
...

$$f^* = \arg \min_{f \in \mathcal{F}} \sum_{i=1}^n \mathcal{L}(f(x_i), y_i)$$

A large red 'X' is overlaid on the training data and function mapping components. To the right of the 'X', the function mapping is shown as  $f : X \rightarrow Y$ .

# Unsupervised Representation Learning

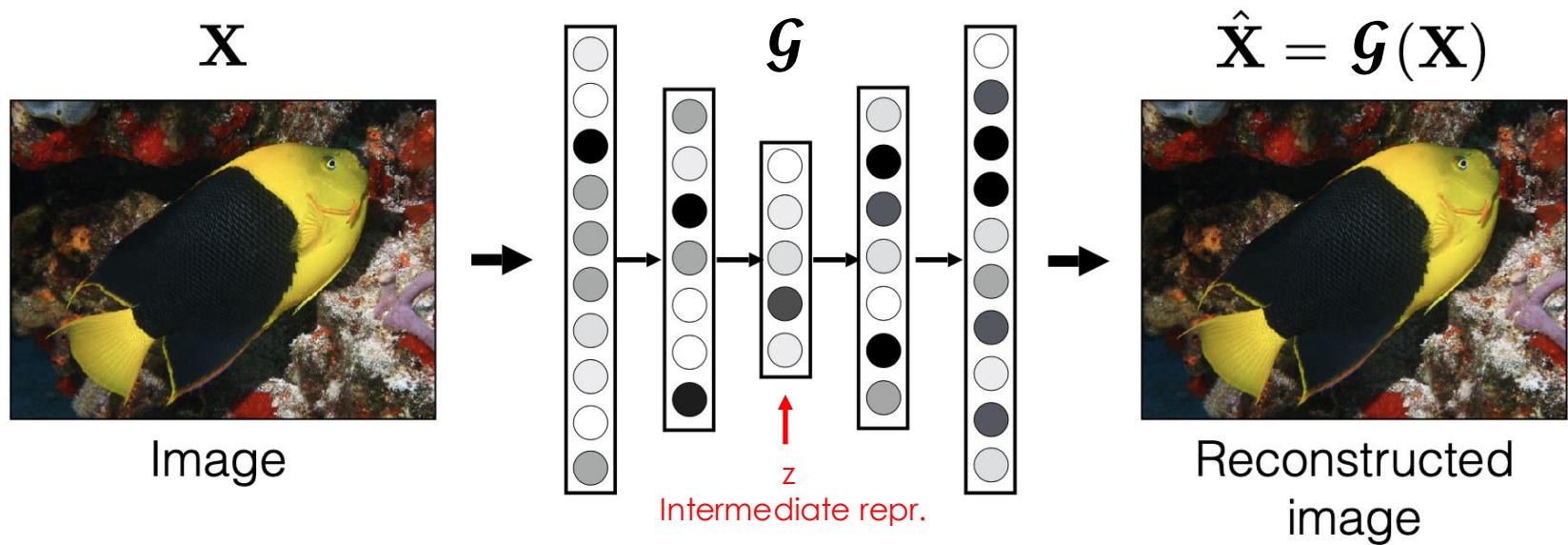
No category or symbolic label. Instead: learn to reconstruct.



One kind of unsupervised model: “Autoencoder”

[e.g., Hinton & Salakhutdinov, Science 2006]

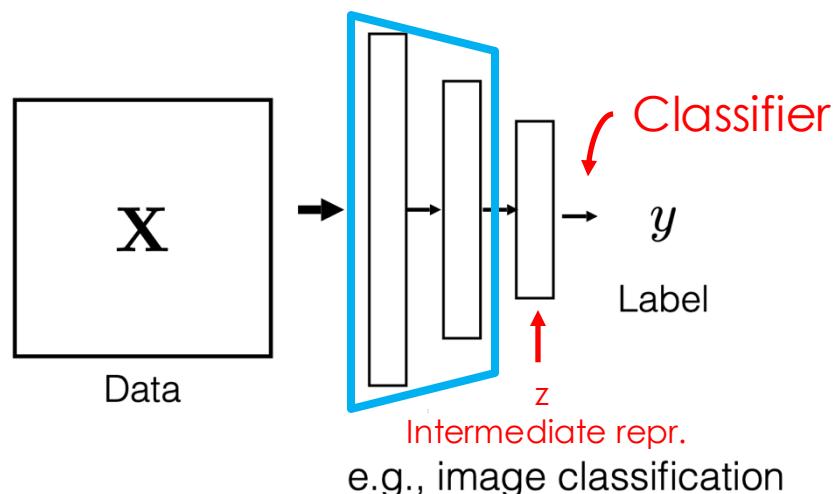
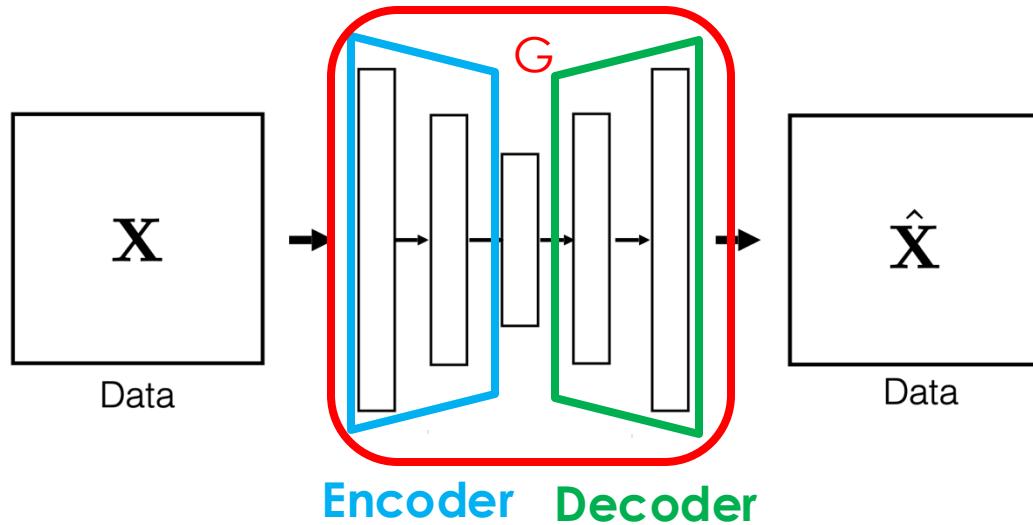
# Autoencoder



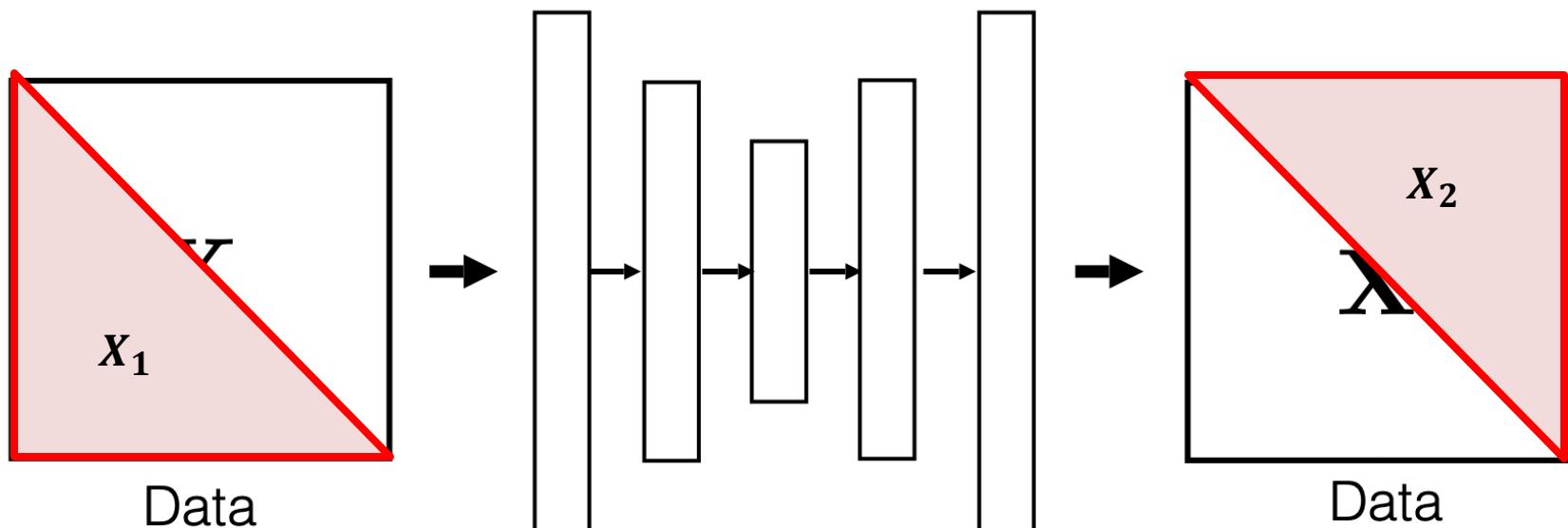
$$\arg \min_{\mathcal{F}} \mathbb{E}_{\mathbf{X}} [|| \mathbf{g}(\mathbf{X}) - \mathbf{X} ||]$$

Reconstruction loss to  
minimize by finding  
optimal G

# Data Compression & Task Transfer



# Self-Supervision



$$G(X) = \hat{X}$$
$$G(X_1) = \hat{X}_2$$

# Predictive Learning: Language Models

## Next word prediction (GPT)

- Predict the next word (token) given a prefix



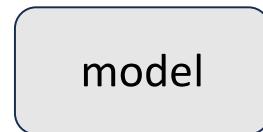
Radford, et al., "Improving Language Understanding by Generative Pre-Training", 2018

# Predictive Learning: Language Models

## Masked language modeling (BERT)

- Predict the masked words (tokens) in a text

The \_\_\_ opened their \_\_\_ and began to \_\_\_



students .. books .. read

Devlin, et al., “BERT: Pre-training of Deep Bidirectional Transformers for Language Understanding”, 2018

# Predictive Learning: Computer Vision

## Masked image modeling (Context Encoders)

- Predict the masked regions using ConvNets

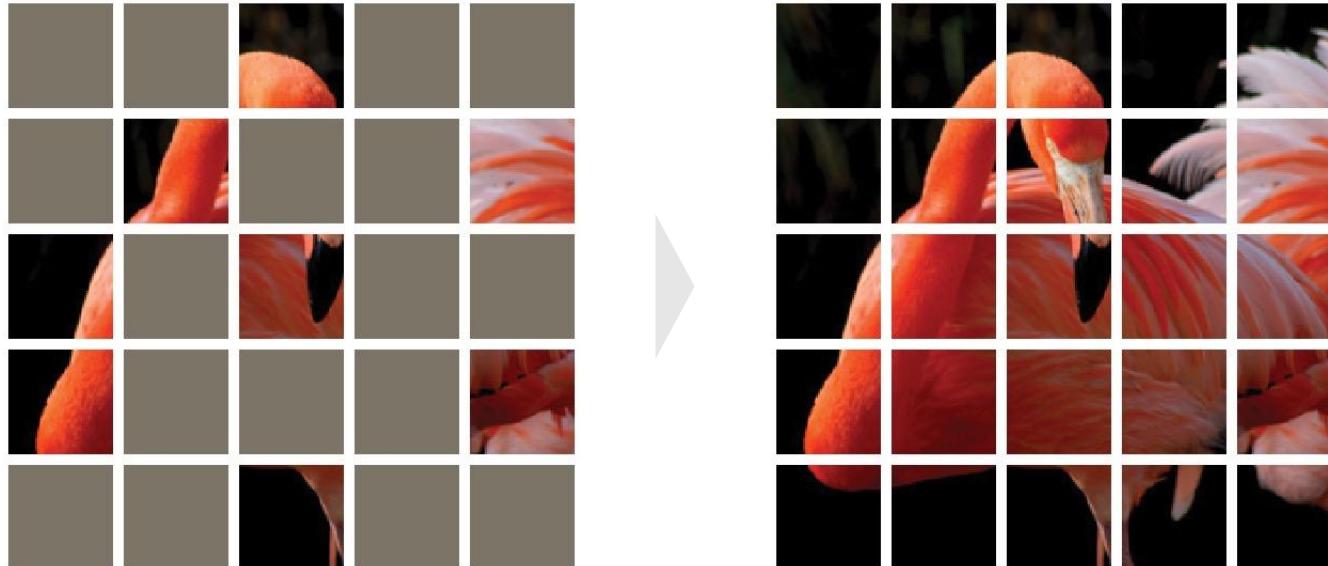


Pathak, et al., "Context Encoders: Feature Learning by Inpainting", CVPR 2016

# Predictive Learning: Computer Vision

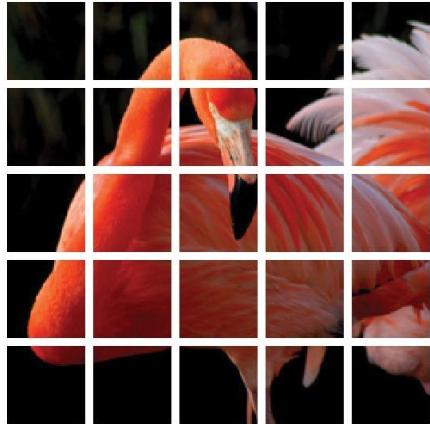
## Masked image modeling (Masked Autoencoder)

- Predict the masked patches using Transformers



He, et al., "Masked Autoencoders Are Scalable Vision Learners", CVPR 2022

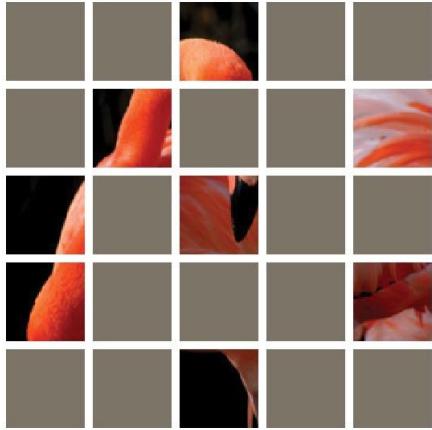
# Masked Autoencoder (MAE)



patches as visual tokens  
(Vision Transformer)

He, et al., "Masked Autoencoders Are Scalable Vision Learners", CVPR 2022

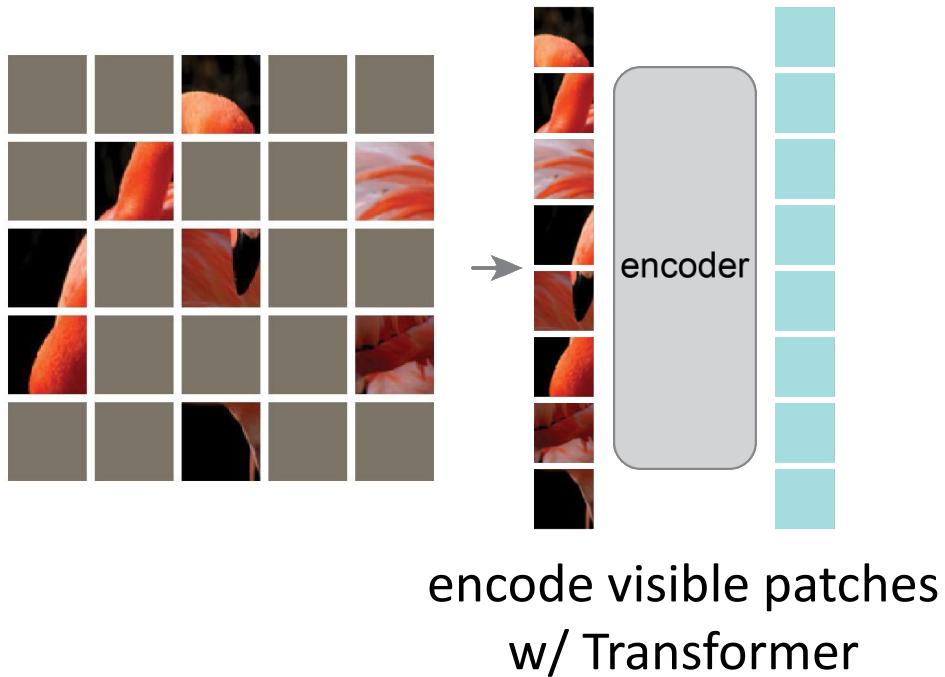
# Masked Autoencoder (MAE)



random masking

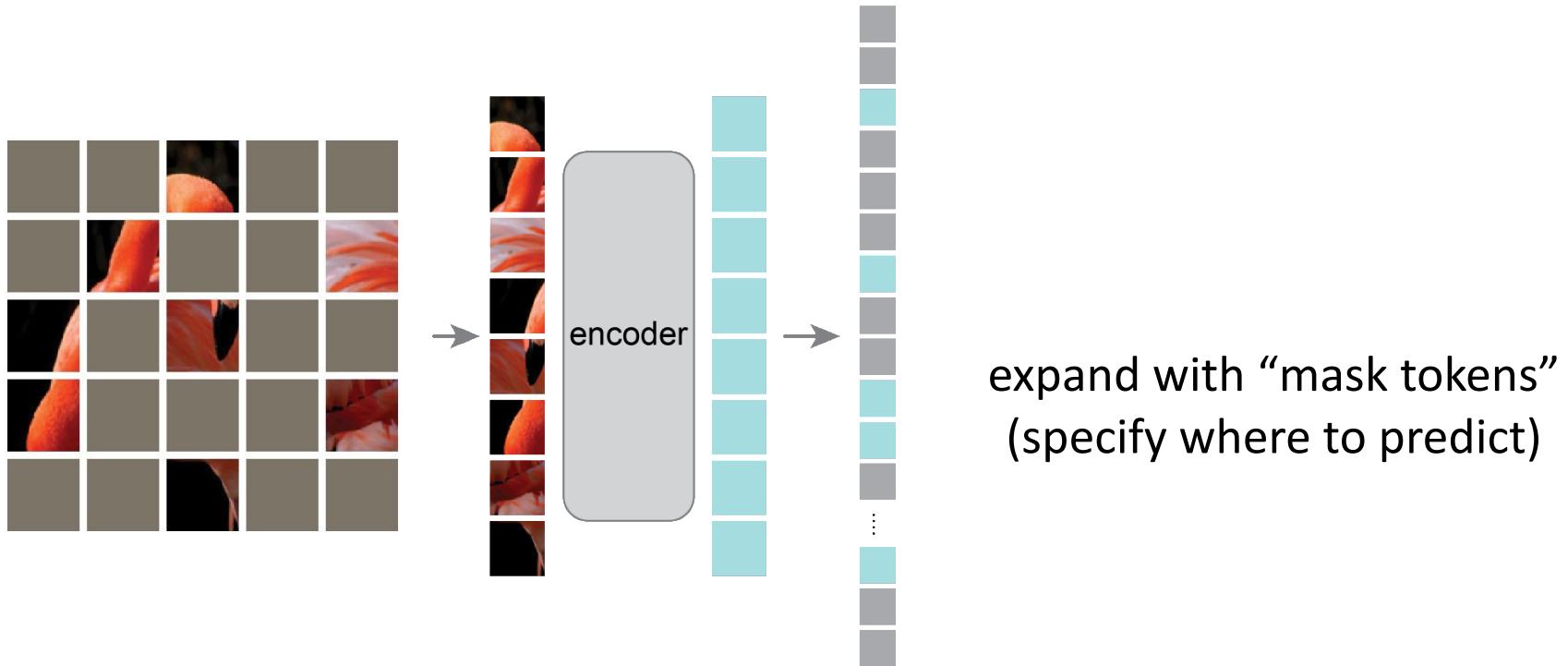
He, et al., "Masked Autoencoders Are Scalable Vision Learners", CVPR 2022

# Masked Autoencoder (MAE)



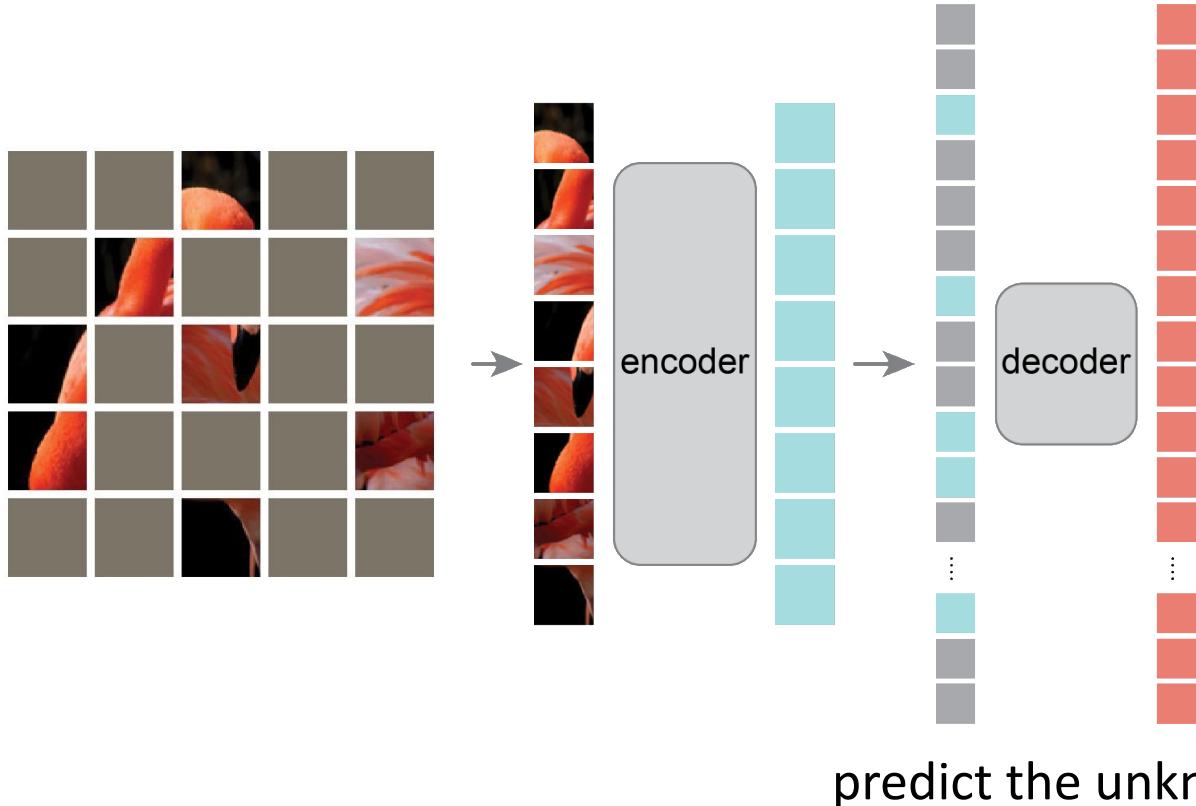
He, et al., "Masked Autoencoders Are Scalable Vision Learners", CVPR 2022

# Masked Autoencoder (MAE)



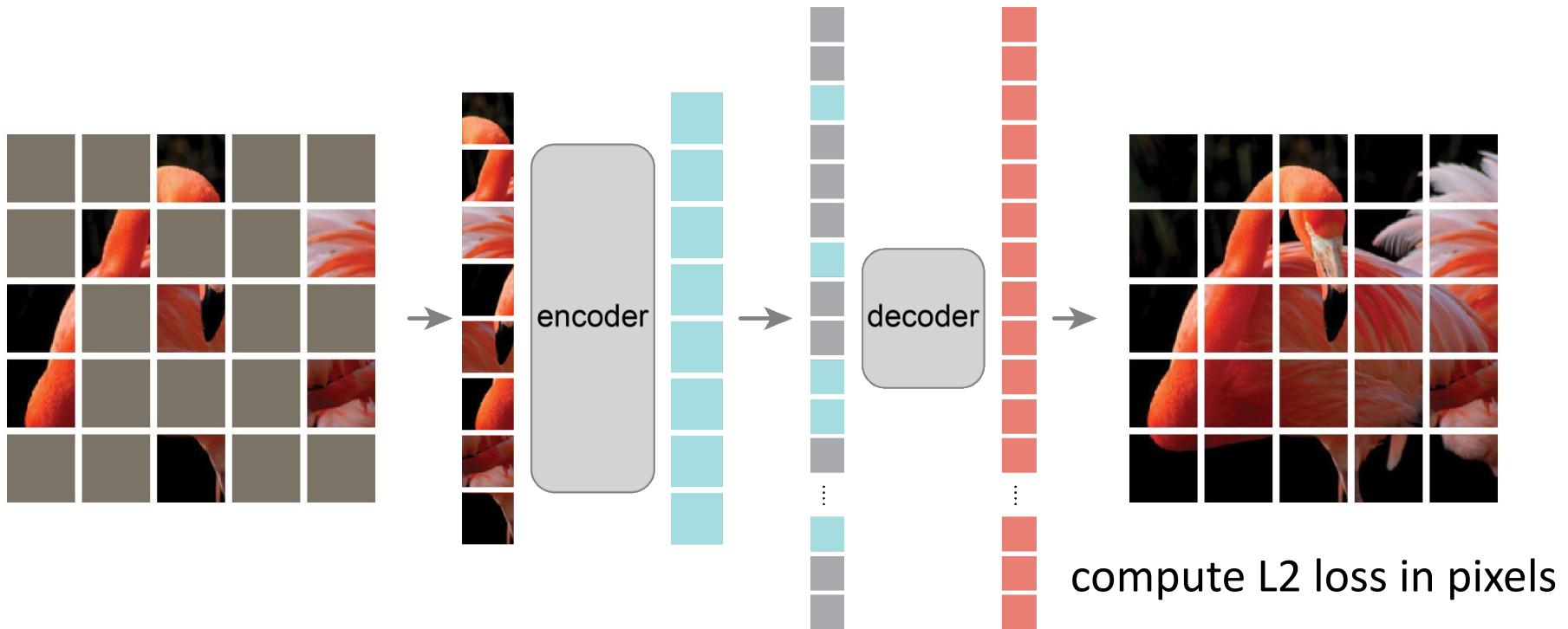
He, et al., “Masked Autoencoders Are Scalable Vision Learners”, CVPR 2022

# Masked Autoencoder (MAE)



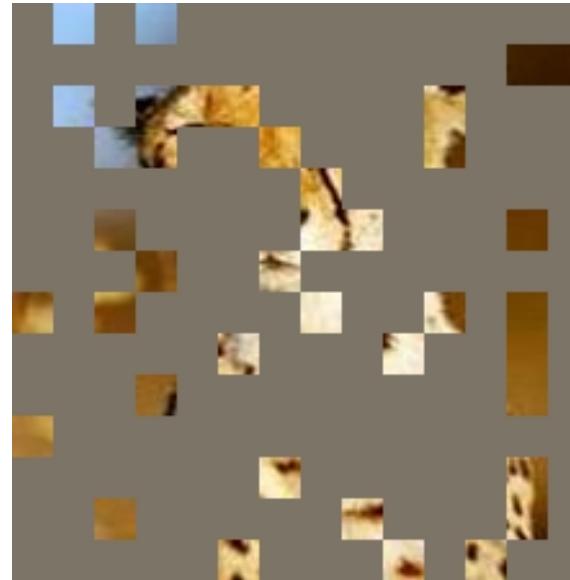
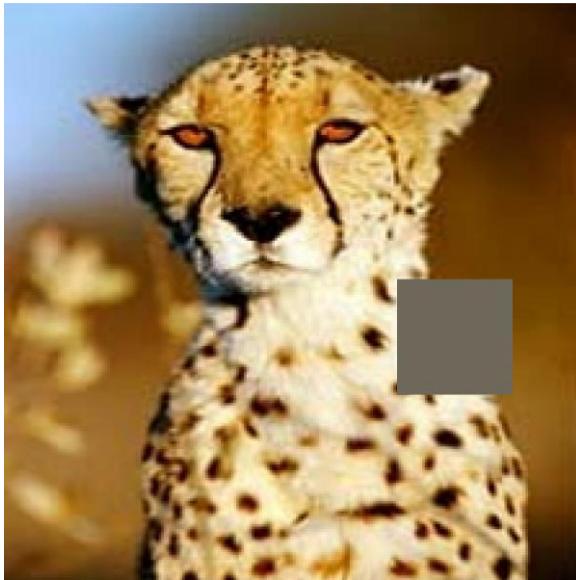
He, et al., "Masked Autoencoders Are Scalable Vision Learners", CVPR 2022

# Masked Autoencoder (MAE)



He, et al., "Masked Autoencoders Are Scalable Vision Learners", CVPR 2022

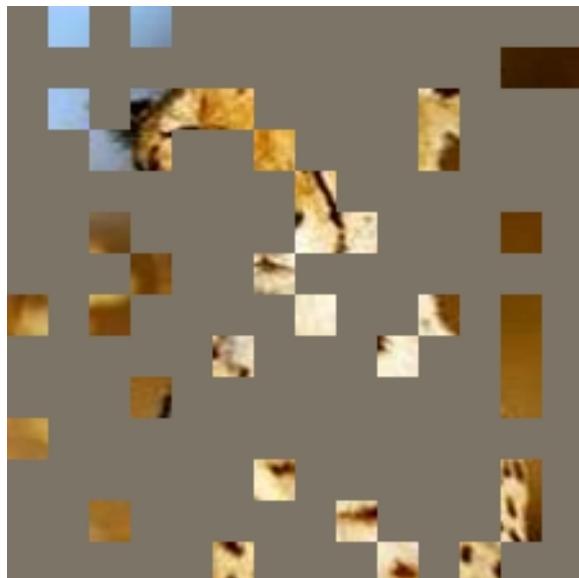
# How to learn good representations by predicting?



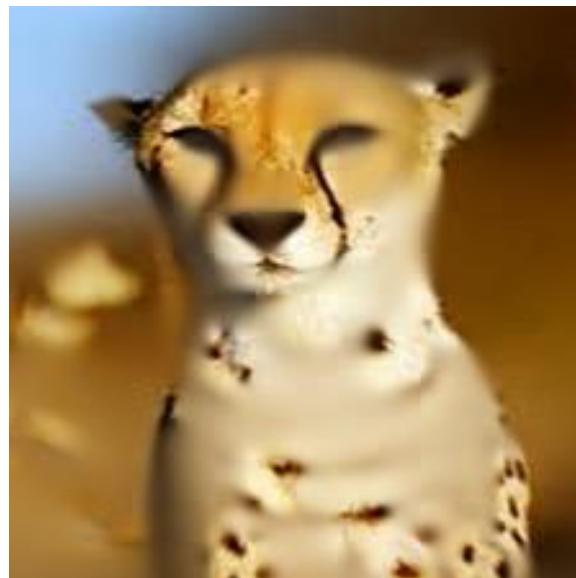
- predicting a small portion may not require high-level understanding
- predicting a large portion of unknown patches encourages to learn semantic features

He, et al., "Masked Autoencoders Are Scalable Vision Learners", CVPR 2022

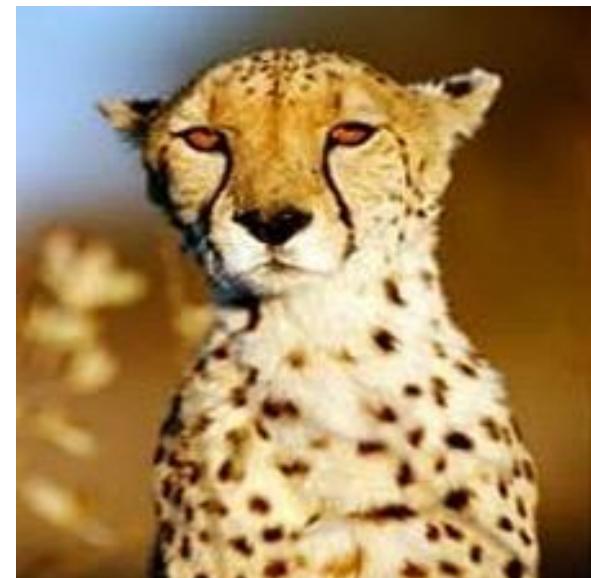
# How to learn good representations by predicting?



input



MAE prediction



original

He, et al., "Masked Autoencoders Are Scalable Vision Learners", CVPR 2022

# Representation Learning

## Reinforcement Learning (Cherry)

Predicting a scalar reward given once in a while  
A few bits for some samples

## Supervised Learning (Chocolate Coat)

Predicting category or vector of scalars per input as provided by human labels.  
10-10k bits per sample

## Unsupervised / Self-Supervised Learning (Cake)

Predicting parts of observed input or predicting future observations or events  
Millions of bits per sample



Visualisation Idea by Yann LeCun  
Photo by [Kristina Paukshtite](#) from [Pexels](#)

# Summary of what you learned today

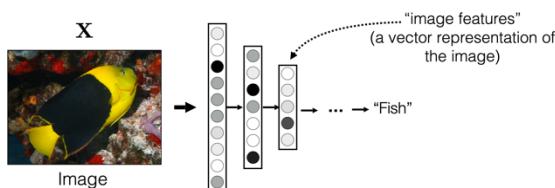
- **State:** Quantity that describes the most important aspect of a dynamical system at time t
- **Representation:** data format of input or output including a low-dimensional representation of sensor data

# Summary of what you learned today

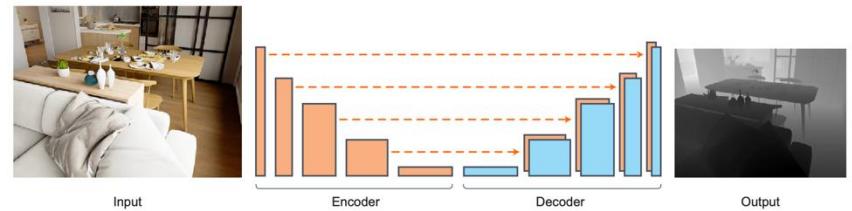
- Learned versus interpretable representations
- Visualize learned representations
- How to learn representations?
  - Supervised
  - Unsupervised
  - Self-supervised

# Next Lectures

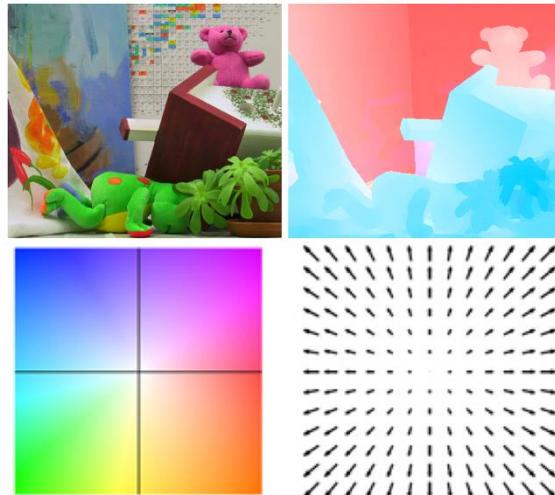
## Representations & Representation Learning



## Monocular Depth Estimation, Feature Tracking

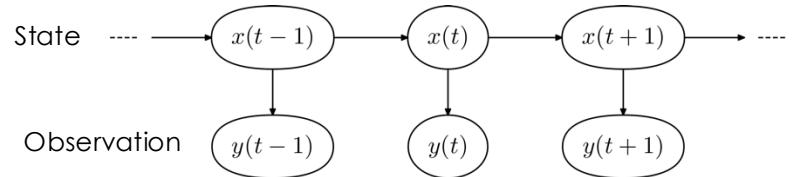


## Optical & Scene Flow

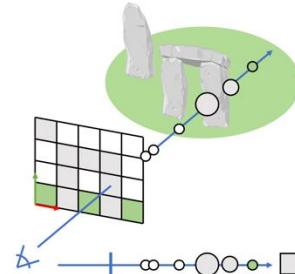


A Database and Evaluation Methodology for Optical Flow.  
Baker et al. IJCV. 2011

## Optimal Estimation



## Neural Radiance Fields



# CS231

## Computer Vision: From 3D Reconstruction to Recognition



Next lectures:

Midterm (Monday)

Monocular Depth Estimation & Feature  
Tracking (Wednesday)