

# Lecture 8

## Active stereo & Volumetric stereo



- Active stereo
  - Structured lighting
  - Depth sensing
- Volumetric stereo:
  - Space carving
  - Shadow carving
  - Voxel coloring

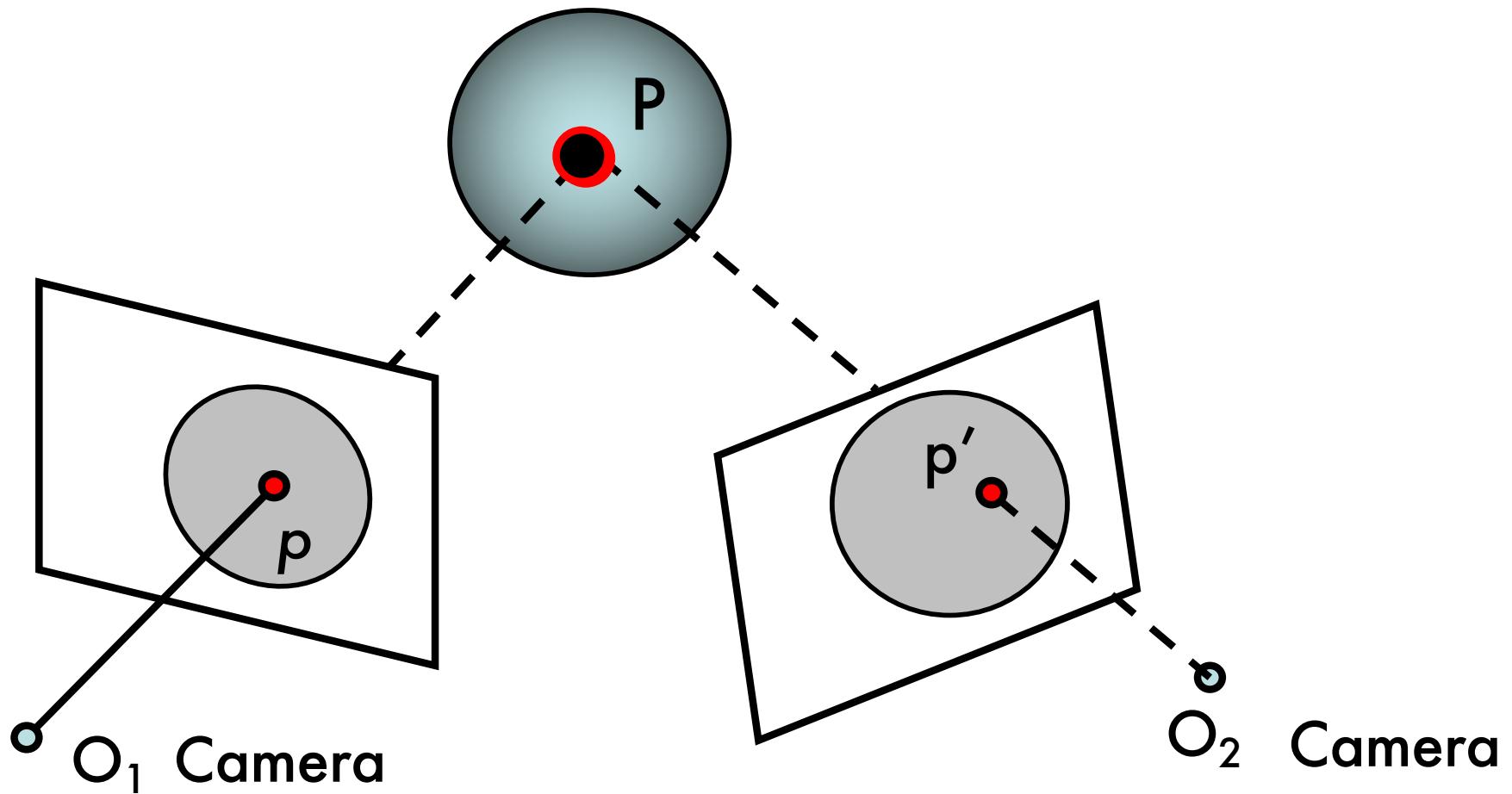
### Reading:

[Szeliski] Chapter 11 “Multi-view stereo”

S. Savarese, M. Andreetto, H. Rushmeier, F. Bernardini and P. Perona, 3D Reconstruction by Shadow Carving: Theory and Practical Evaluation, International Journal of Computer Vision (IJCV) , 71(3), 305-336, 2006

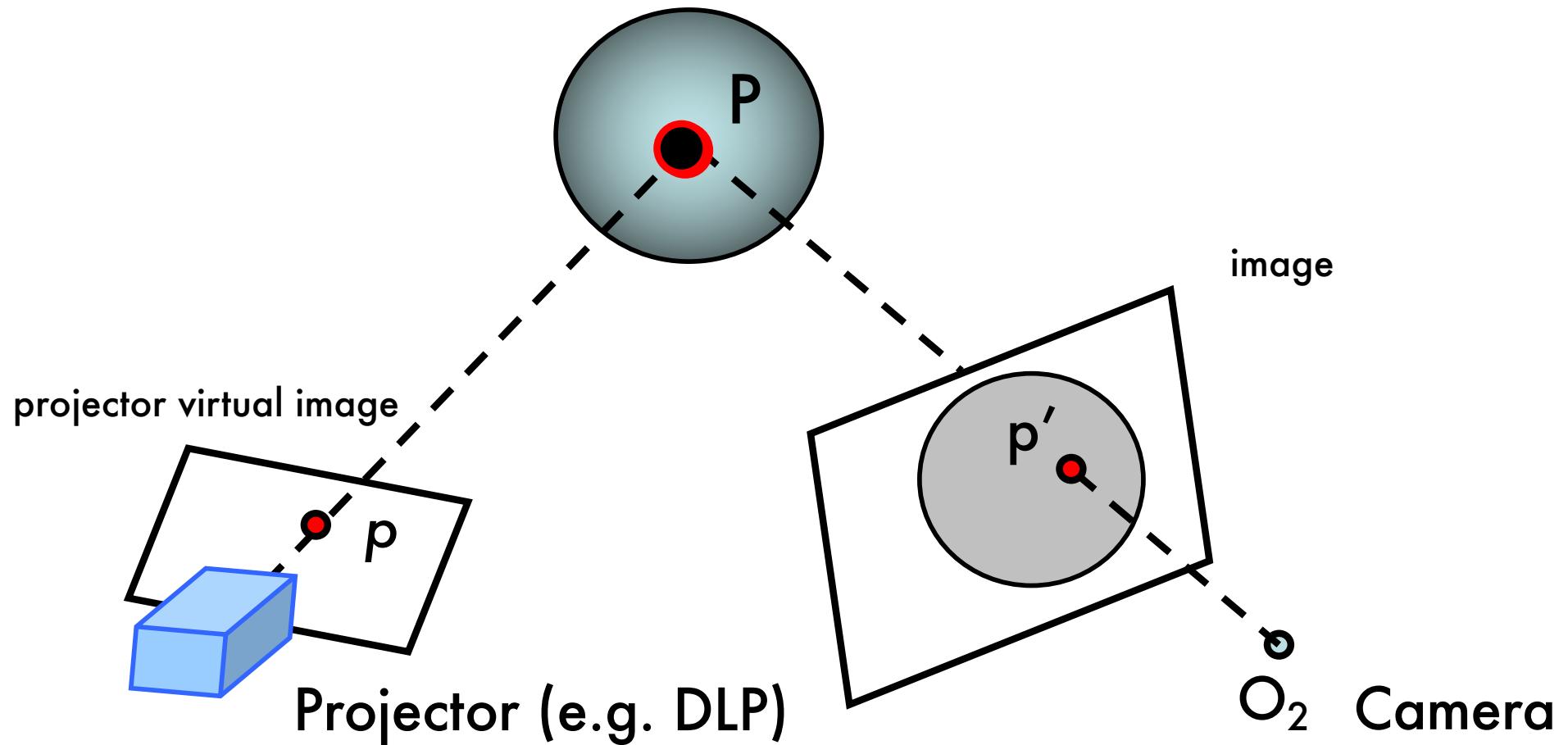
Seitz, S. M., & Dyer, C. R. (1999). Photorealistic scene reconstruction by voxel coloring. *International Journal of Computer Vision*, 35(2), 151-173.

# Traditional stereo



What's the main problem in traditional stereo?  
We need to find correspondences!

# Active stereo (point)

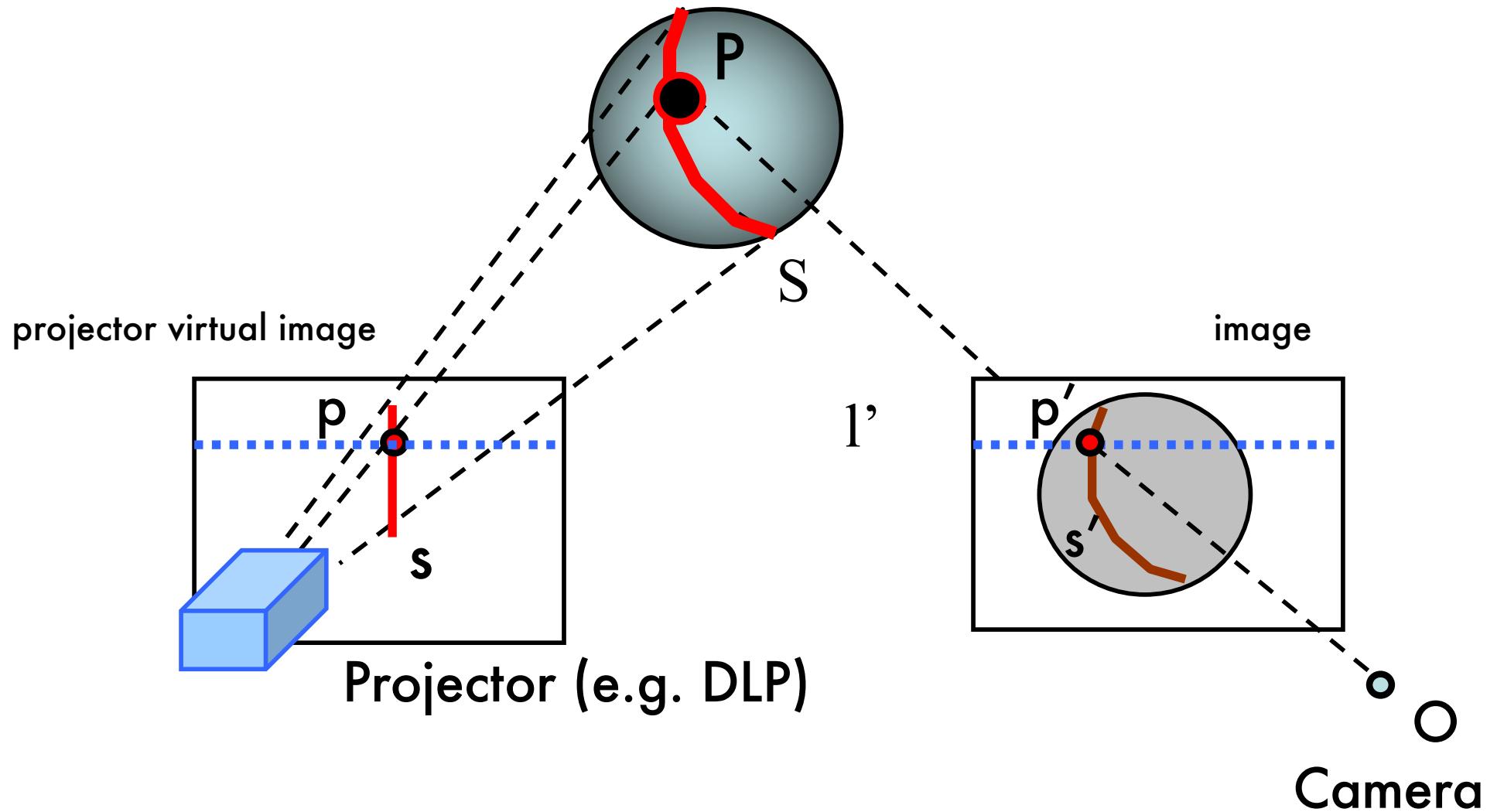


Replace one of the two cameras by a projector

- Projector geometry calibrated
- What's the advantage of having the projector? Correspondence problem solved!

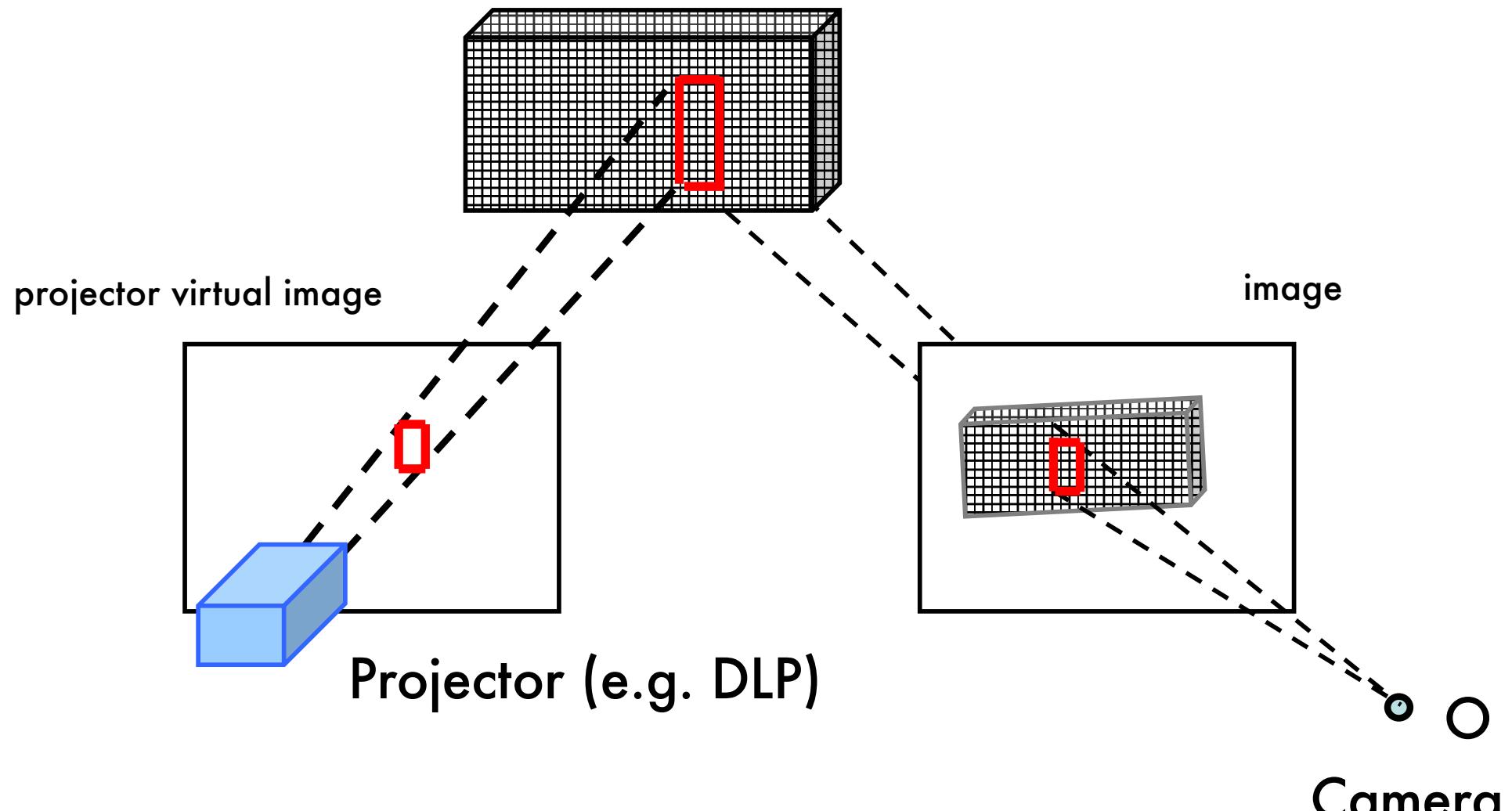
Any limitation??

# Active stereo (stripe)



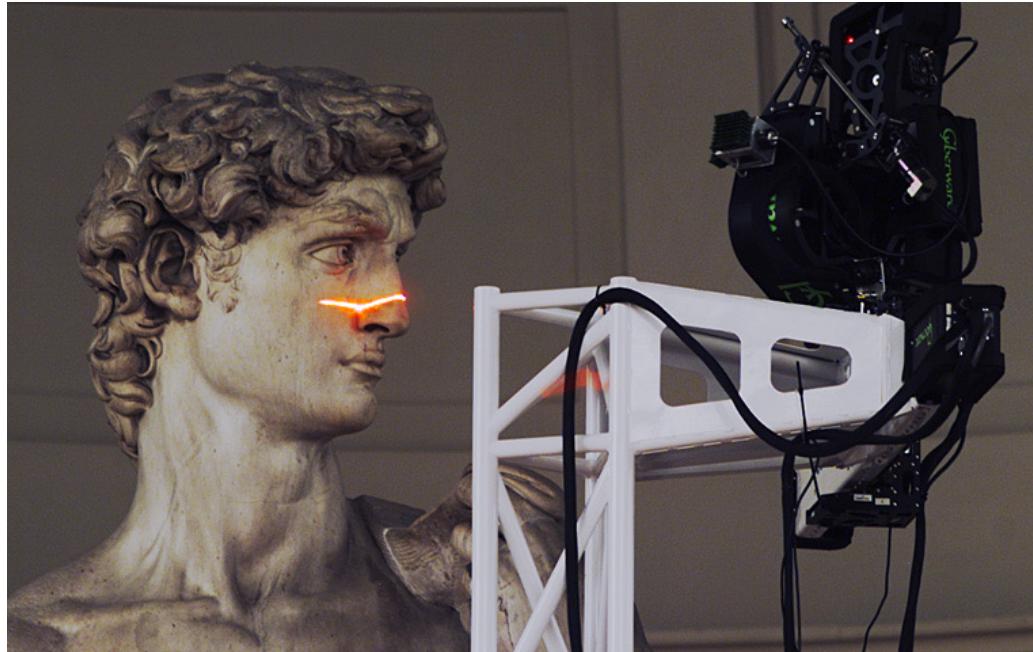
- Projector and camera are parallel
- Correspondence problem is solved!

# Calibrating the system



- Use calibration rig to calibrate camera and localize rig in 3D
- Project patterns on rig and calibrate projector

# Laser scanning



Digital Michelangelo Project (1990)  
<http://graphics.stanford.edu/projects/mich/>

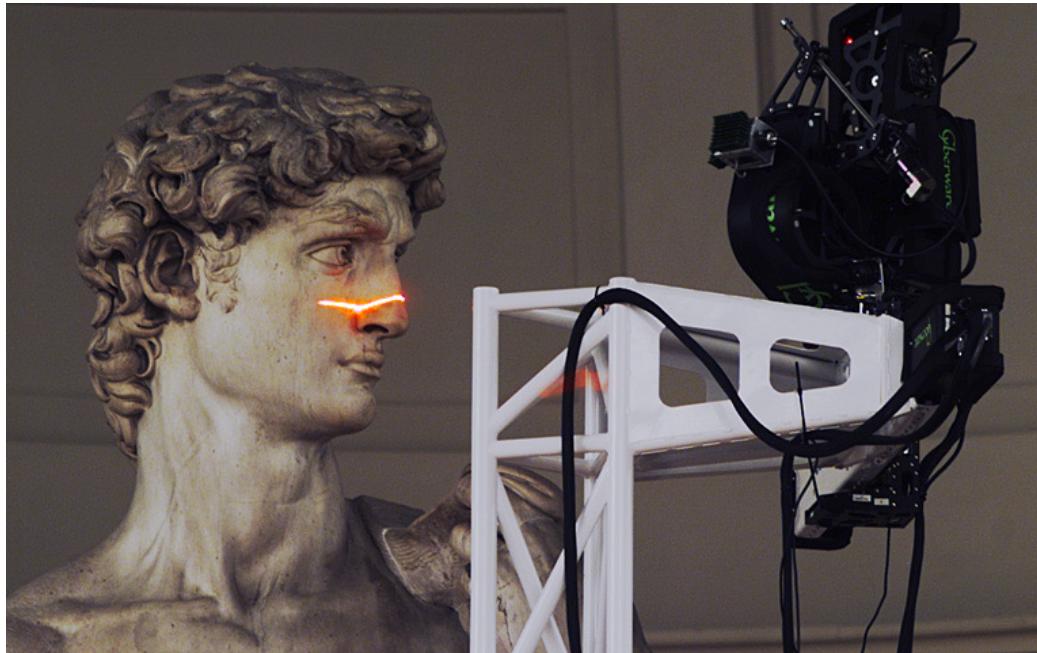
- **Optical triangulation**
  - Project a single stripe of laser light
  - Scan it across the surface of the object
  - This is a very precise version of structured light scanning

# Laser scanning



The Digital Michelangelo Project, Levoy et al.

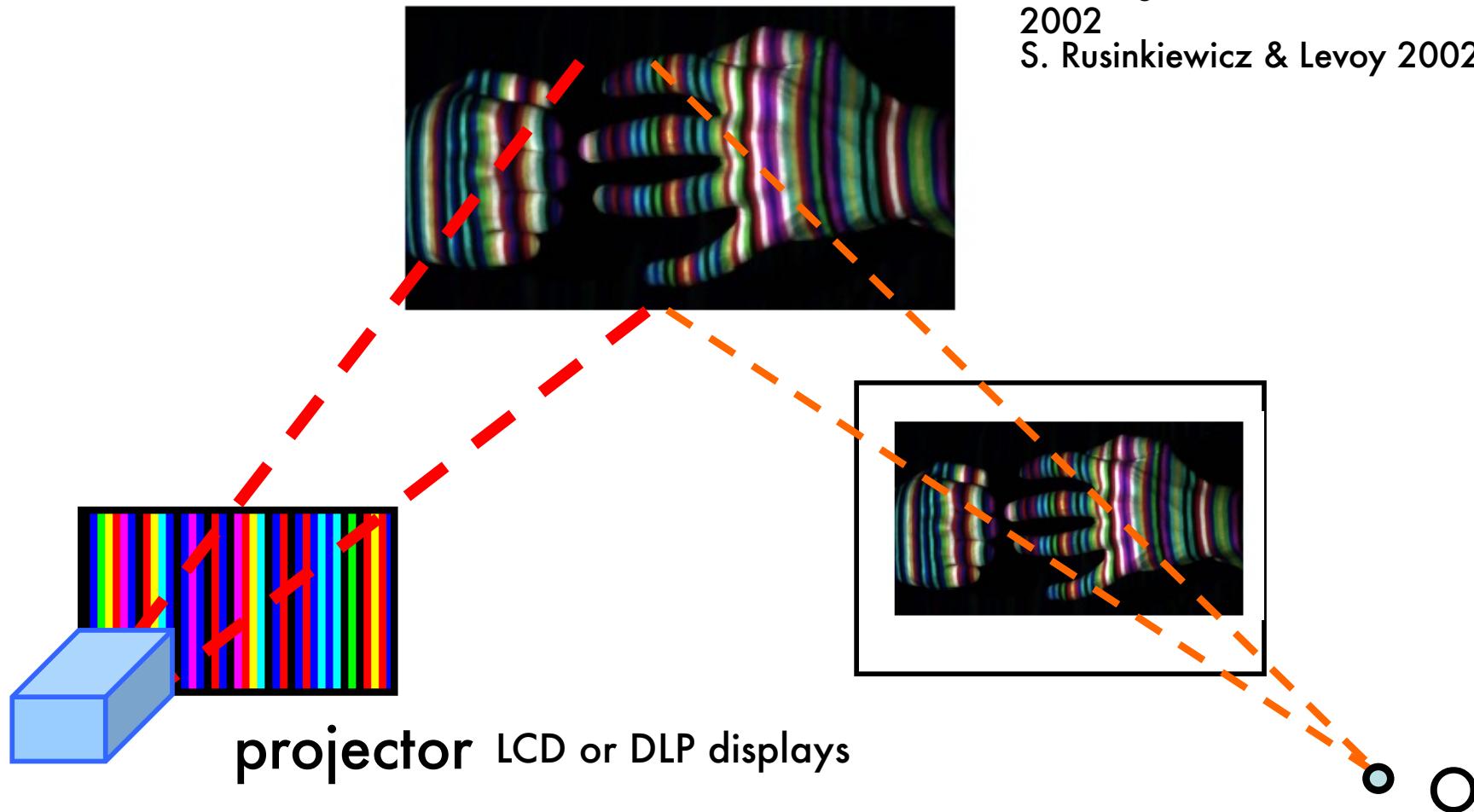
# Limitations of Laser scanning



- Slow
- Cannot capture deformations in time

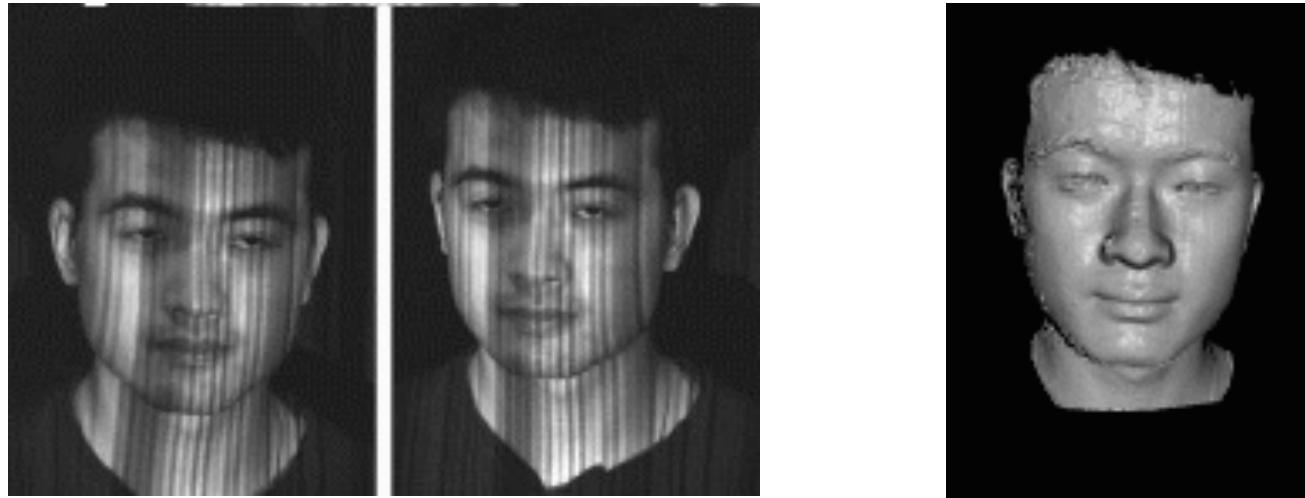
# Active stereo (color-coded stripes)

L. Zhang, B. Curless, and S. M. Seitz  
2002  
S. Rusinkiewicz & Levoy 2002



- Dense reconstruction
- Correspondence problem again
- Get around it by using color codes

# Active stereo (color-coded stripes)



Rapid shape acquisition: Projector + stereo cameras



L. Zhang, B. Curless, and S. M. Seitz. Rapid Shape Acquisition Using Color Structured Light and Multi-pass Dynamic Programming. 3DPVT 2002

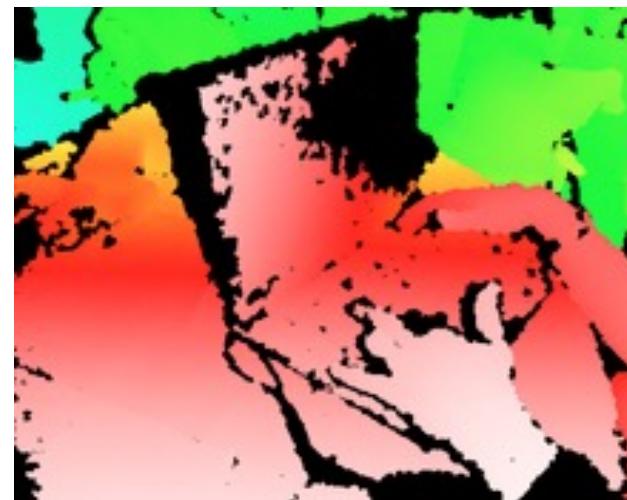
# Active stereo - depth sensors



- Infrared projector combined with an IR camera
- Captures video data in 3D under any ambient light conditions.



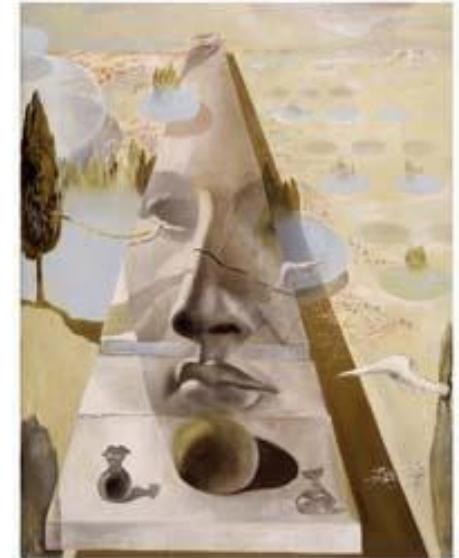
Pattern of projected infrared points to generate a dense 3D image



Depth map

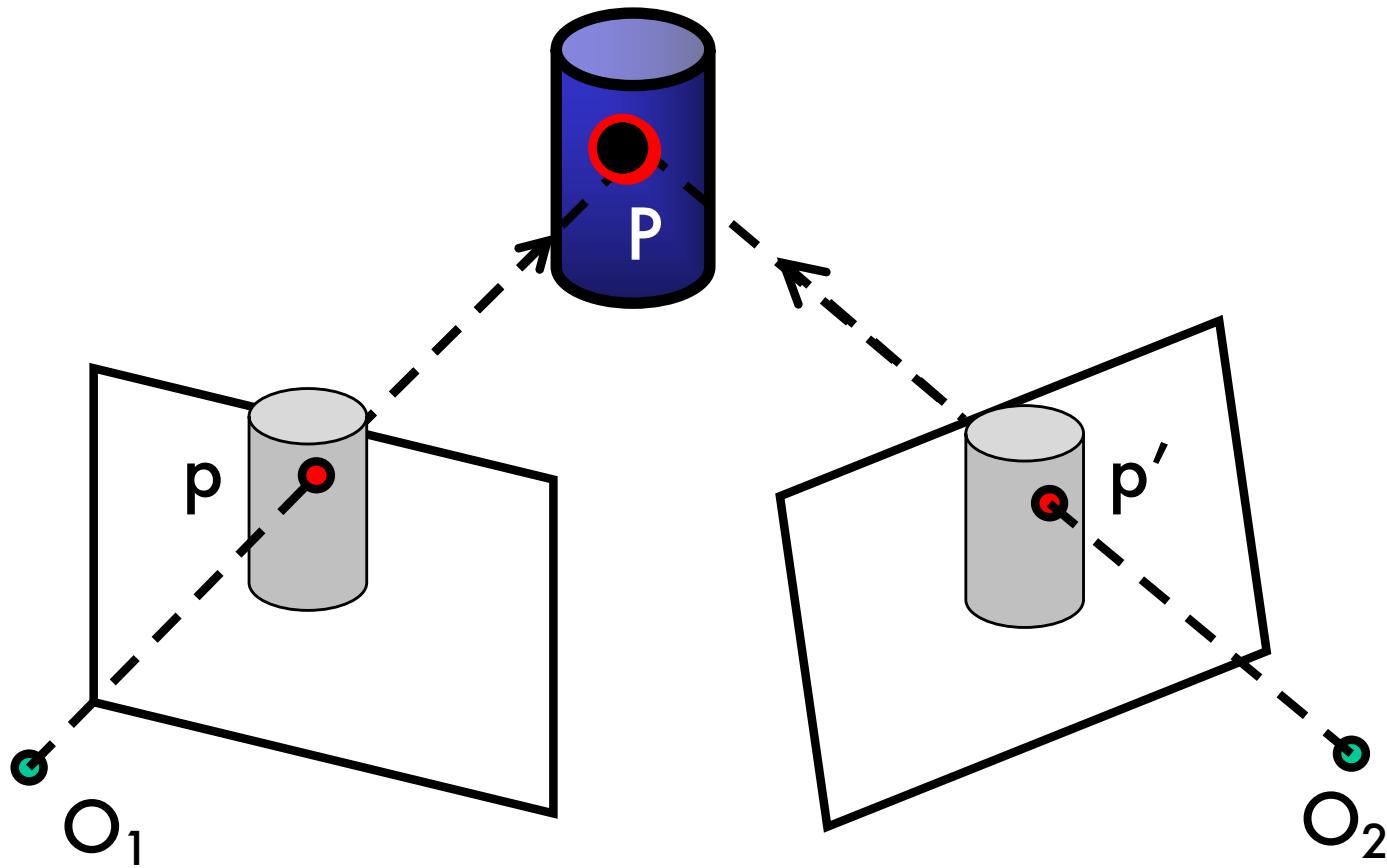
# Lecture 8

## Active stereo & Volumetric stereo



- Active stereo
  - Structured lighting
  - Depth sensing
- Volumetric stereo:
  - Space carving
  - Shadow carving
  - Voxel coloring

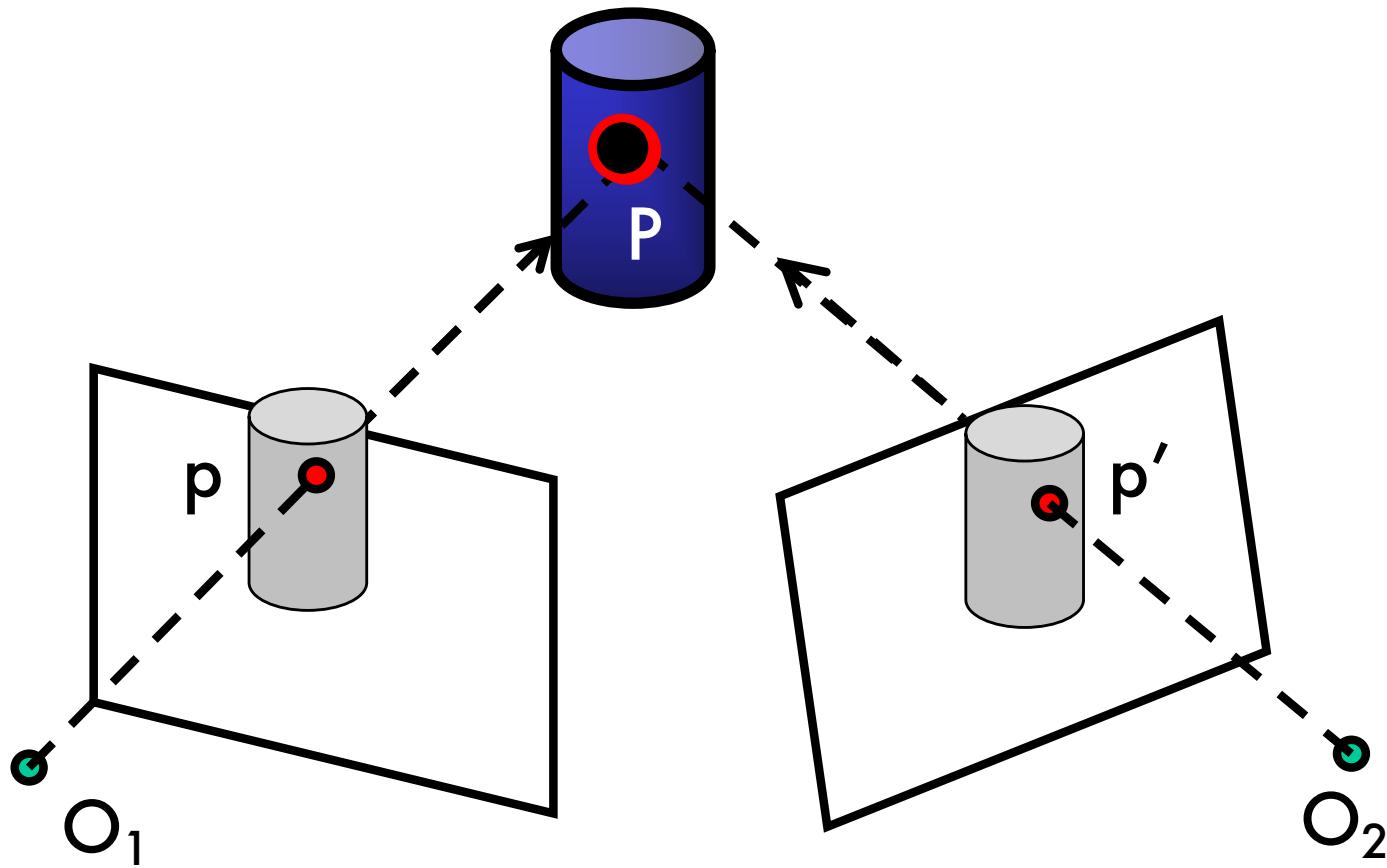
# “Traditional” Stereo



**Goal:** estimate the position of P given the observation of P from two view points

**Assumptions:** known camera parameters and position ( $K, R, T$ )

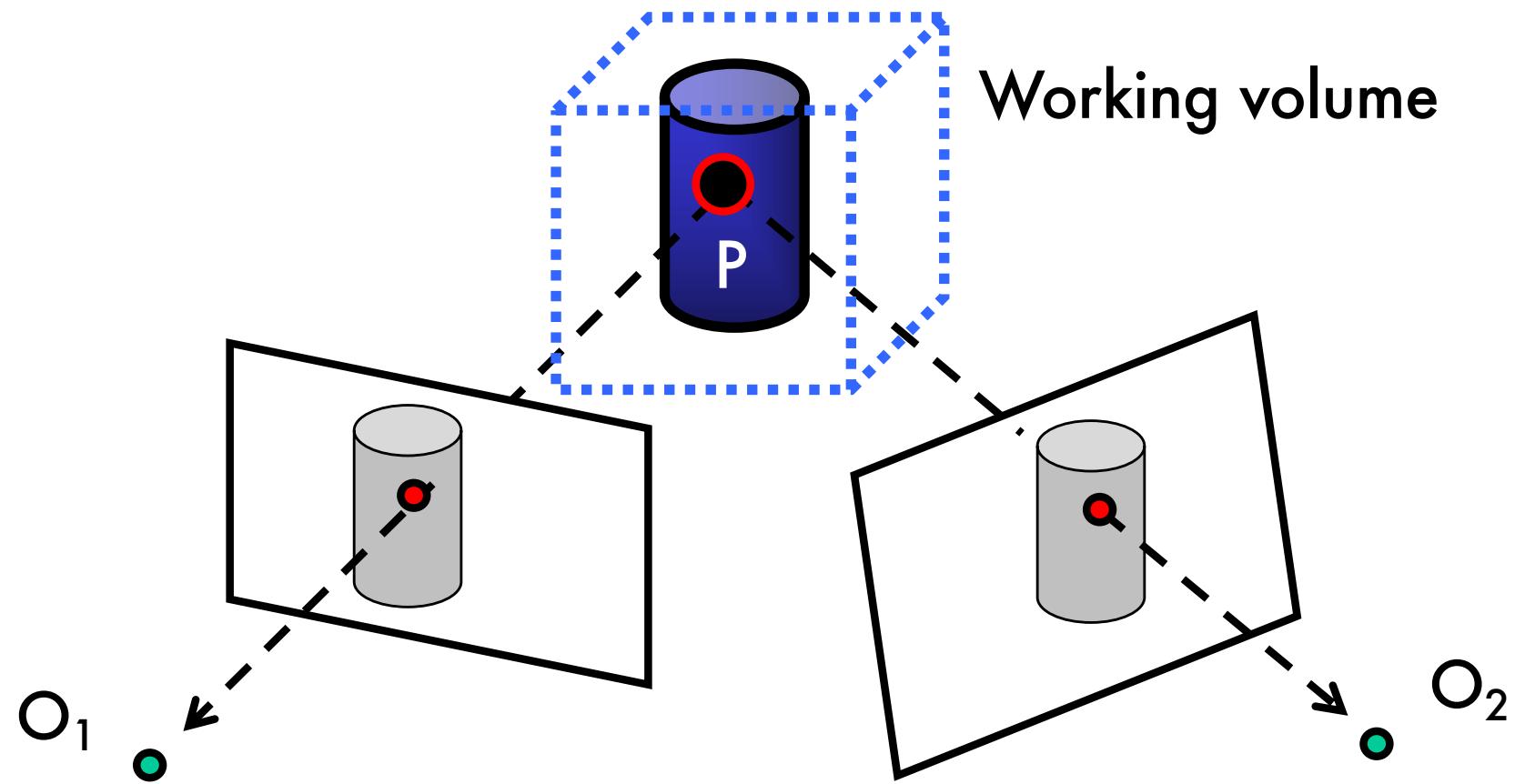
# “Traditional” Stereo



**Subgoals:**

1. Solve the correspondence problem
2. Use corresponding observations to triangulate

# Volumetric stereo



1. Hypothesis: pick up a point within the volume
2. Project this point into 2 (or more) images
3. Validation: are the observations **consistent?**

**Assumptions:** known camera parameters and position ( $K, R, T$ )

# Consistency based on cues such as:

- Contours/silhouettes → Space carving
- Shadows → Shadow carving
- Colors → Voxel coloring

# Lecture 8

## Active stereo & Volumetric stereo



- Active stereo
- Structured lighting
- Depth sensing
- Volumetric stereo:
  - Space carving
  - Shadow carving
  - Voxel coloring

**Reading:**

[Szelisky] Chapter 11 “Multi-view stereo”

# Contours/silhouettes

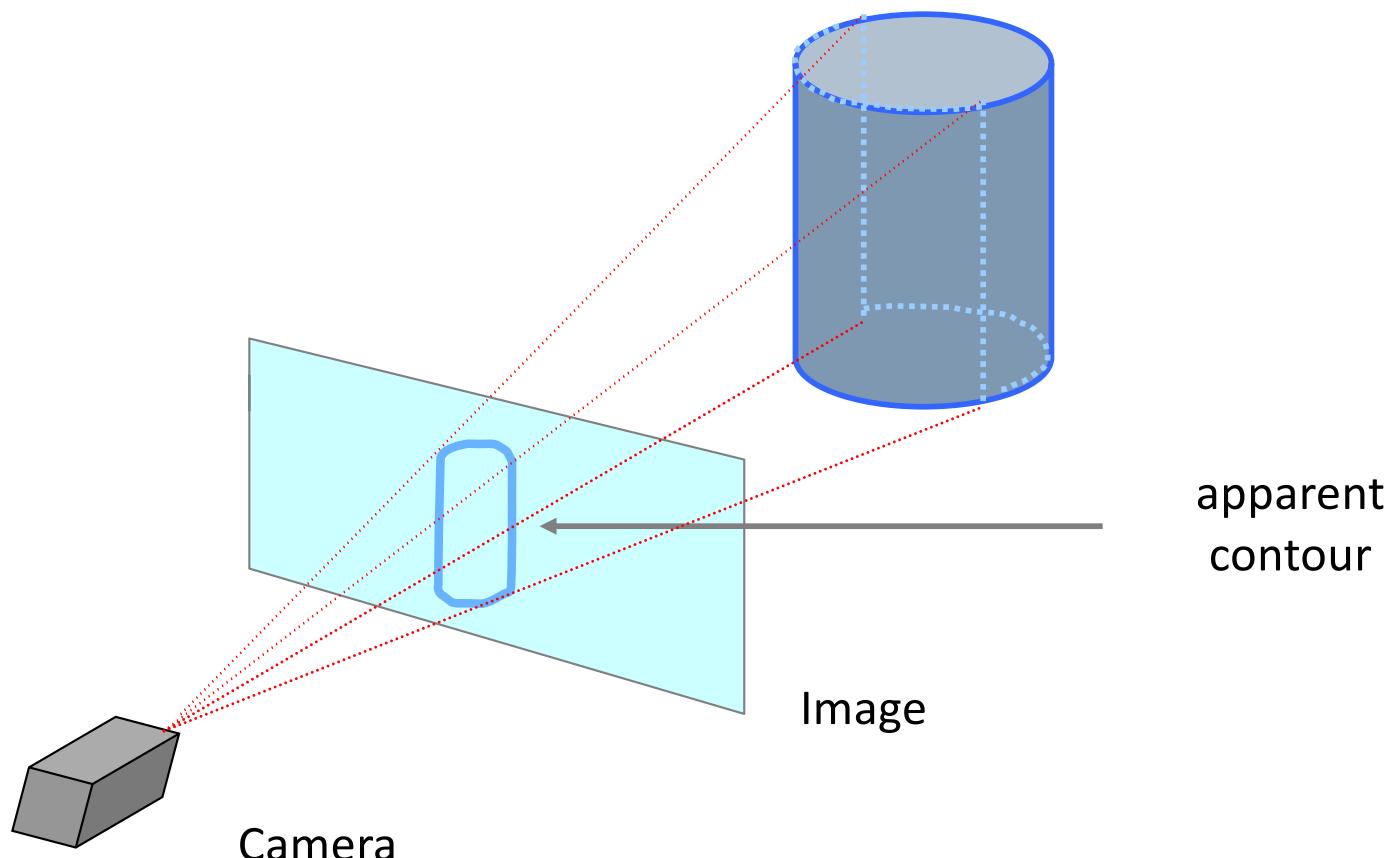
- Contours are a rich source of geometric information



# Apparent Contours

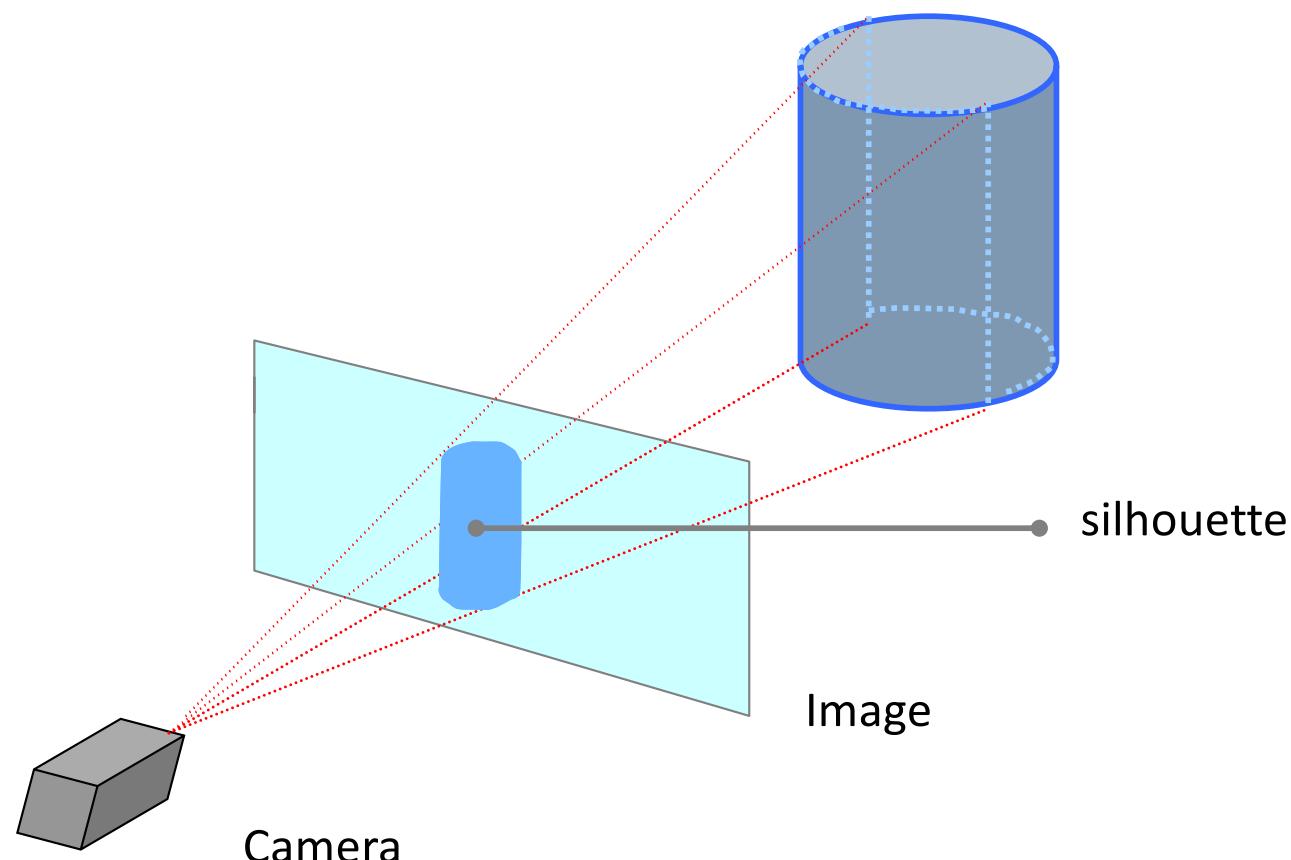
- Projection of the locus of points on the object surface which separate the visible and occluded parts on the surface

[sato & cipolla]

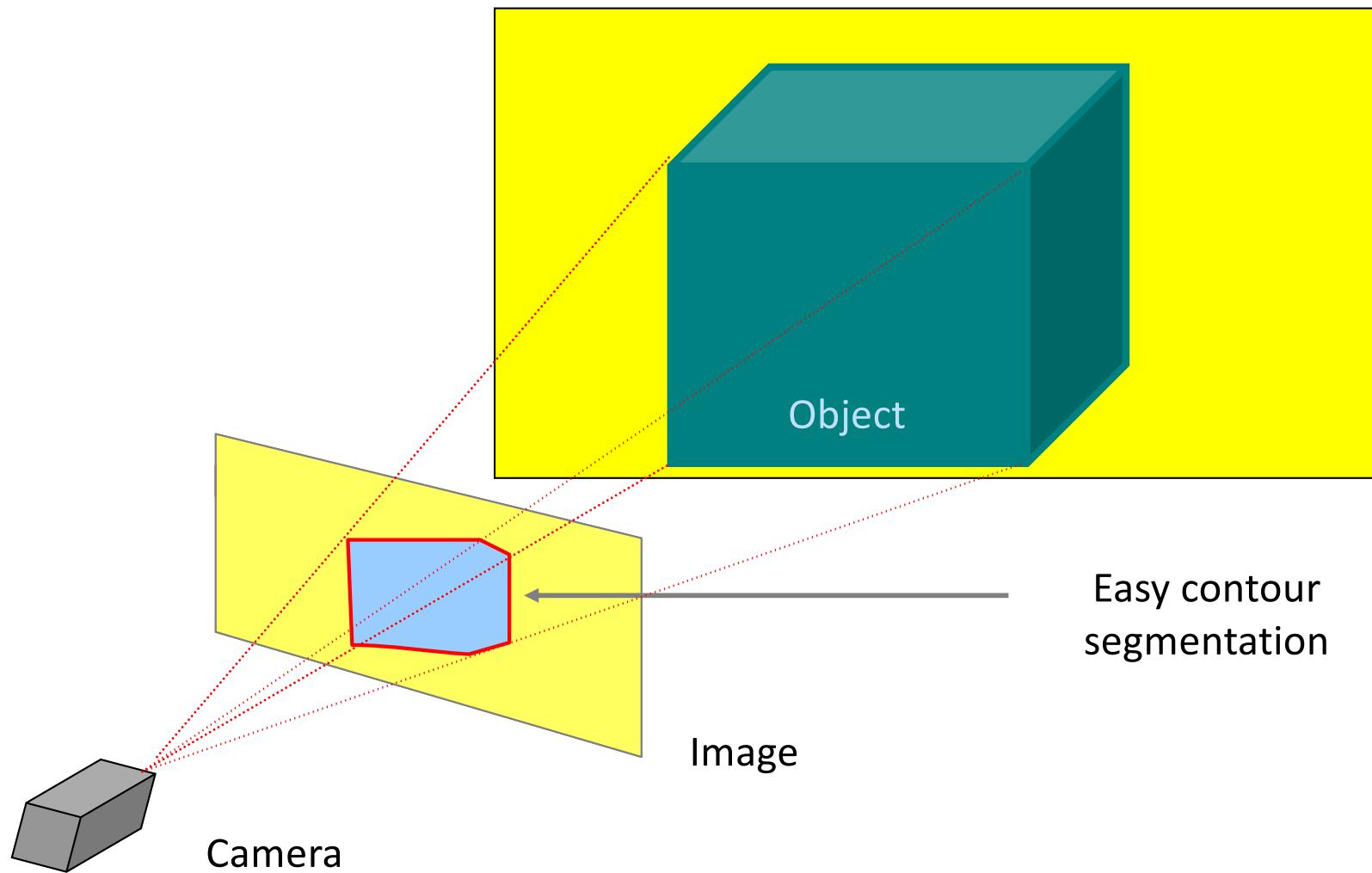


# Silhouettes

A silhouette is defined as the area enclosed by the apparent contours



# Detecting silhouettes



# Detecting silhouettes

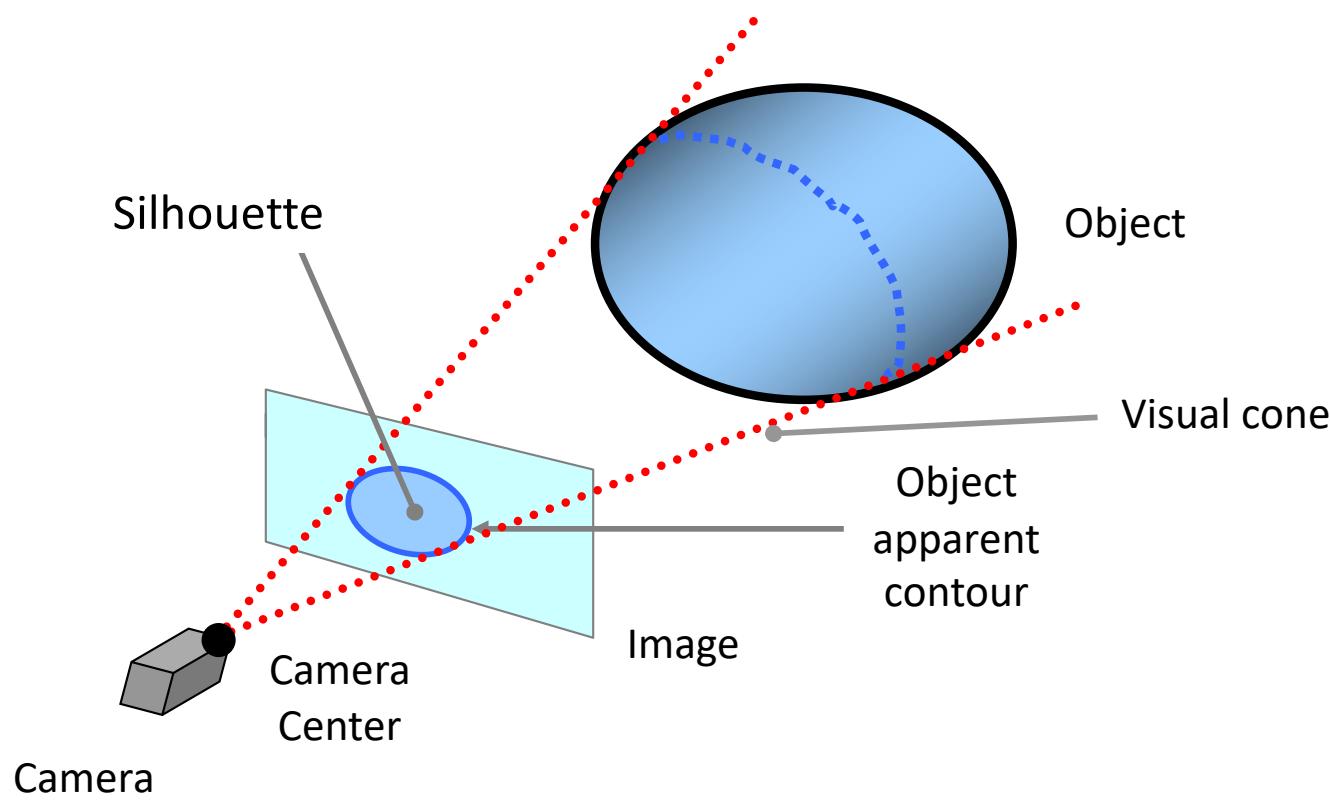
Original Image



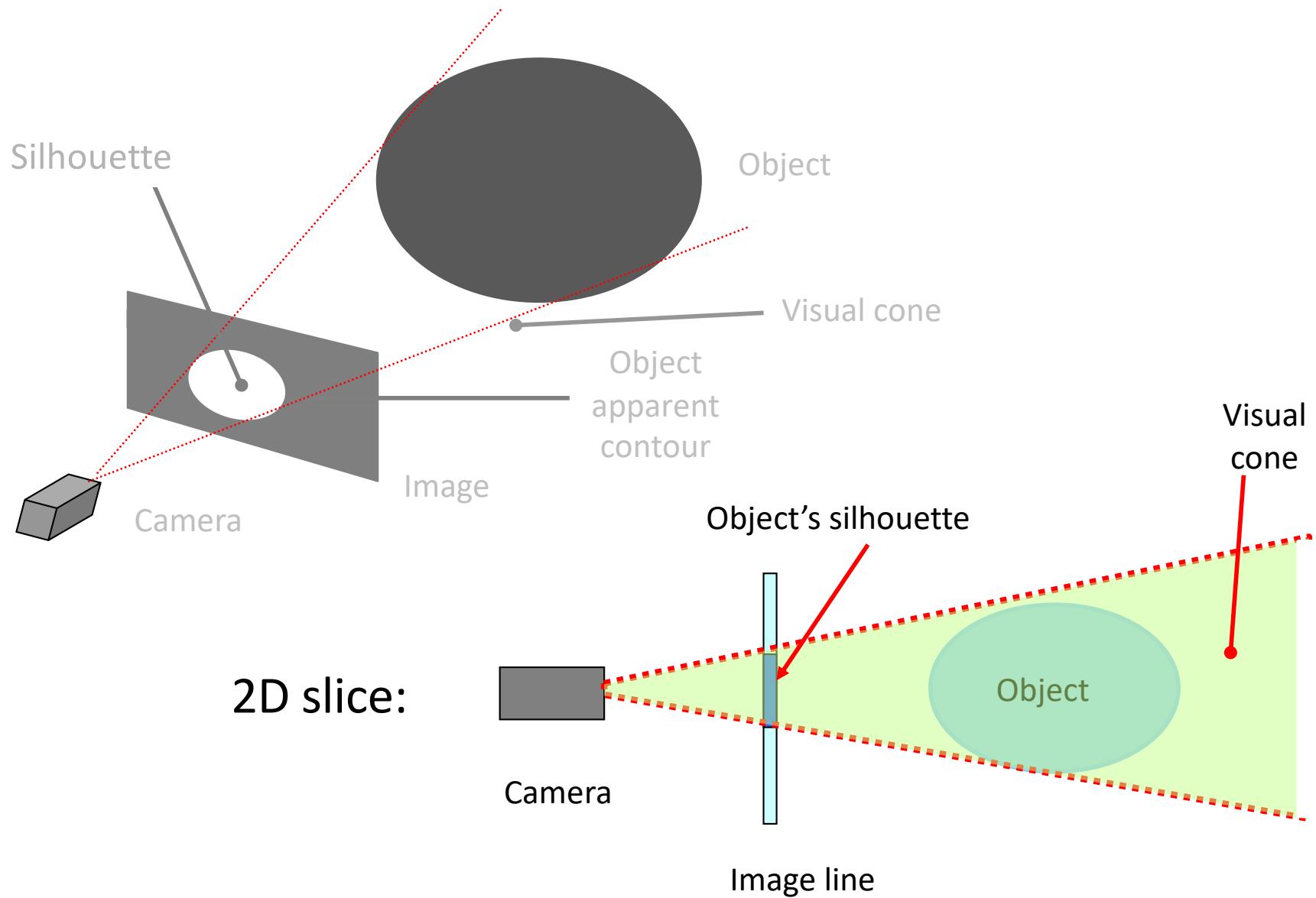
Silhouette



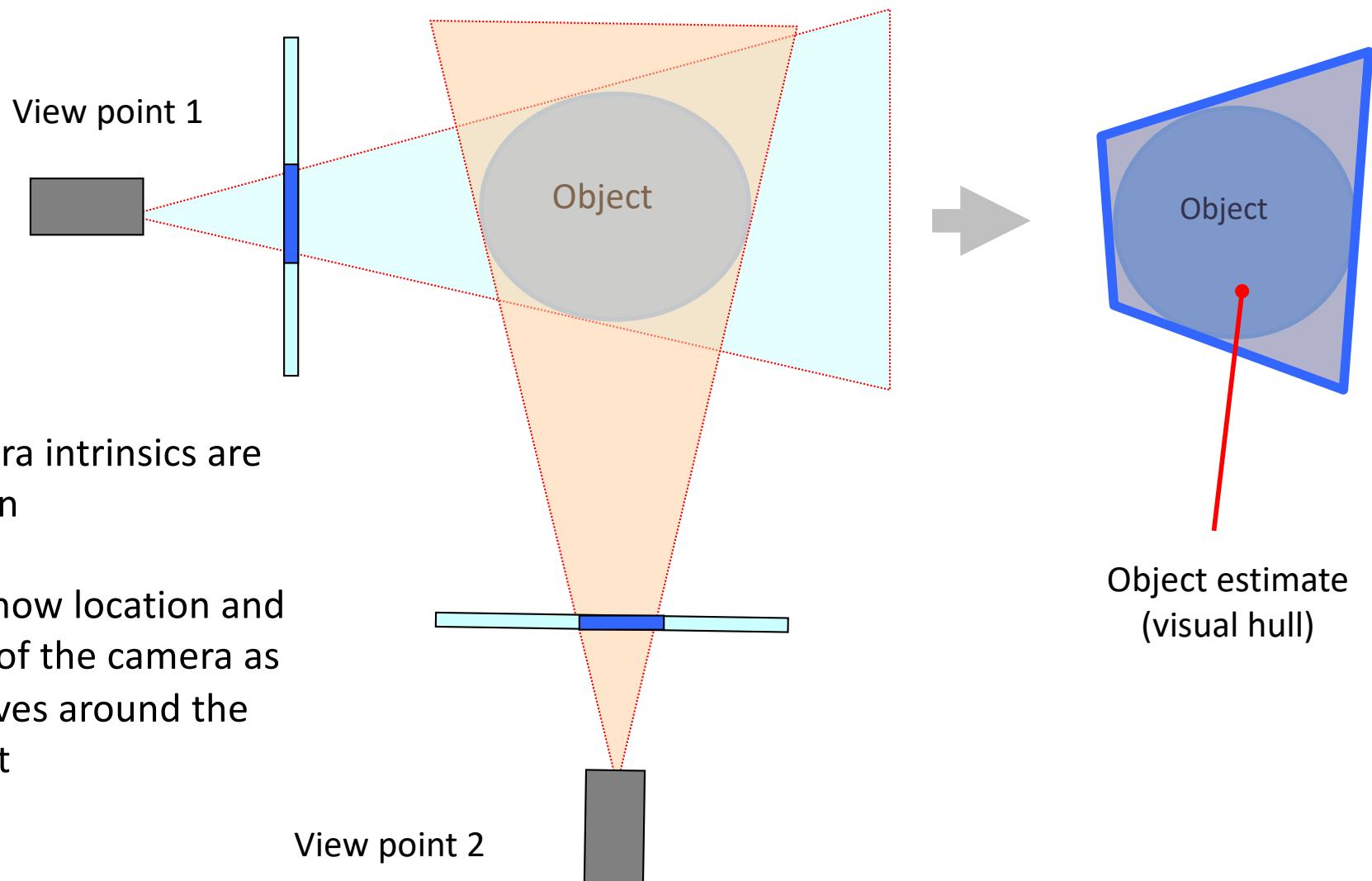
# How can we use contours?



# How can we use contours?



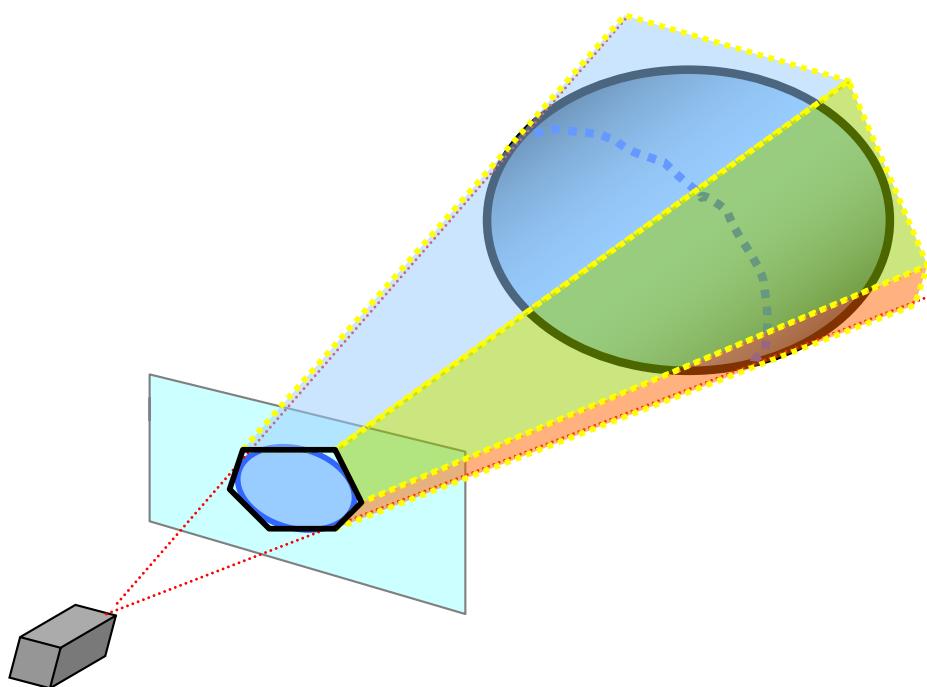
# How can we use contours?



- Camera intrinsics are known
- We know location and pose of the camera as it moves around the object

# How to perform visual cones intersection?

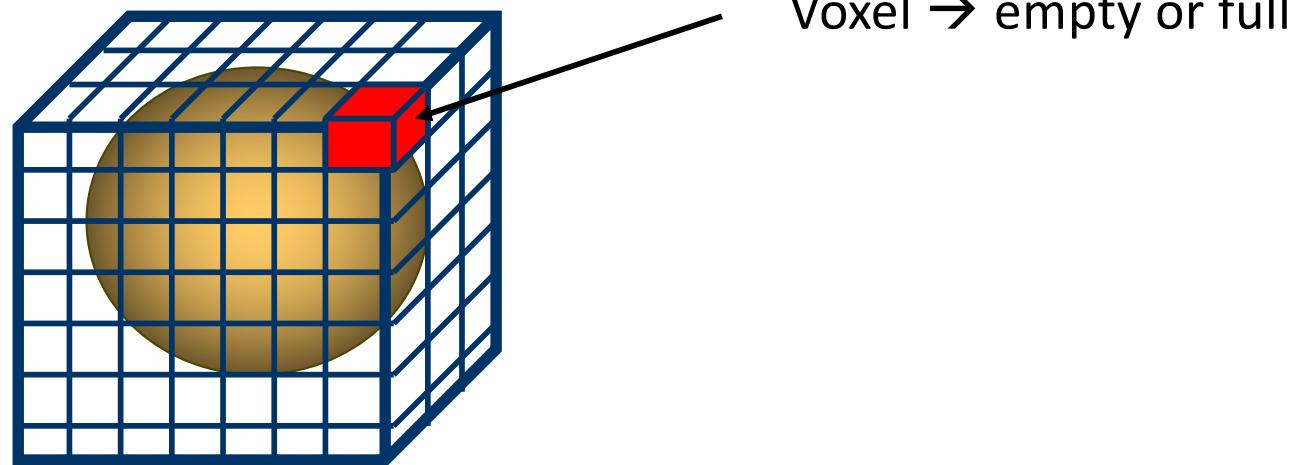
- Decompose visual cone in polygonal surfaces  
(among others: Reed and Allen '99)



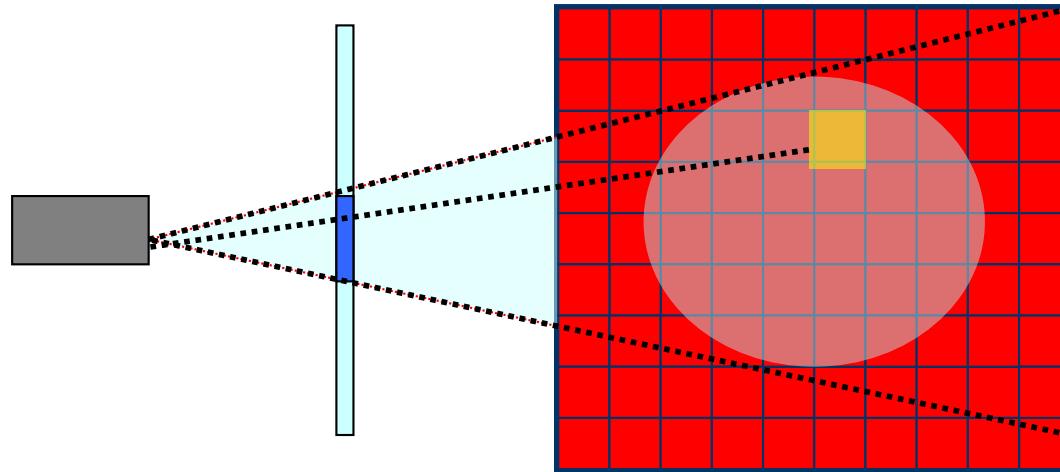
# Space carving

[ Martin and Aggarwal (1983) ]

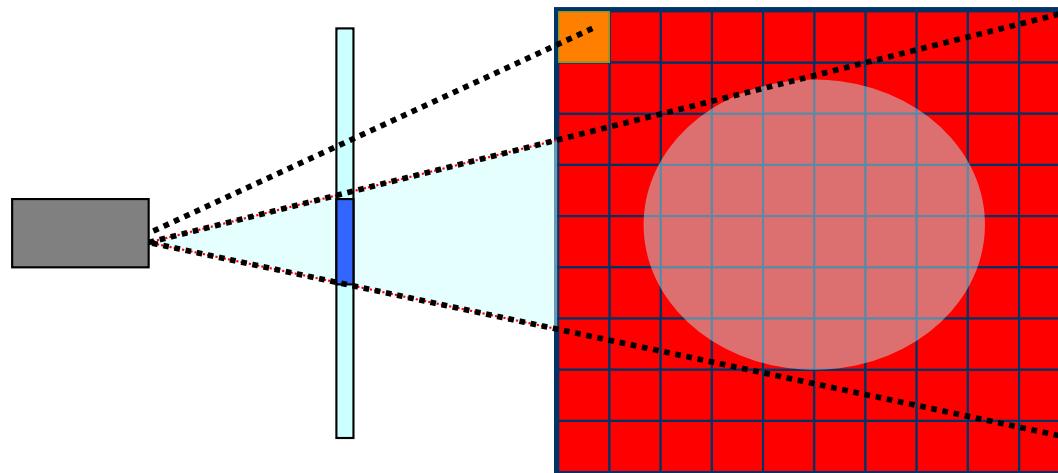
- Using contours/silhouettes in volumetric stereo, also called **space carving**



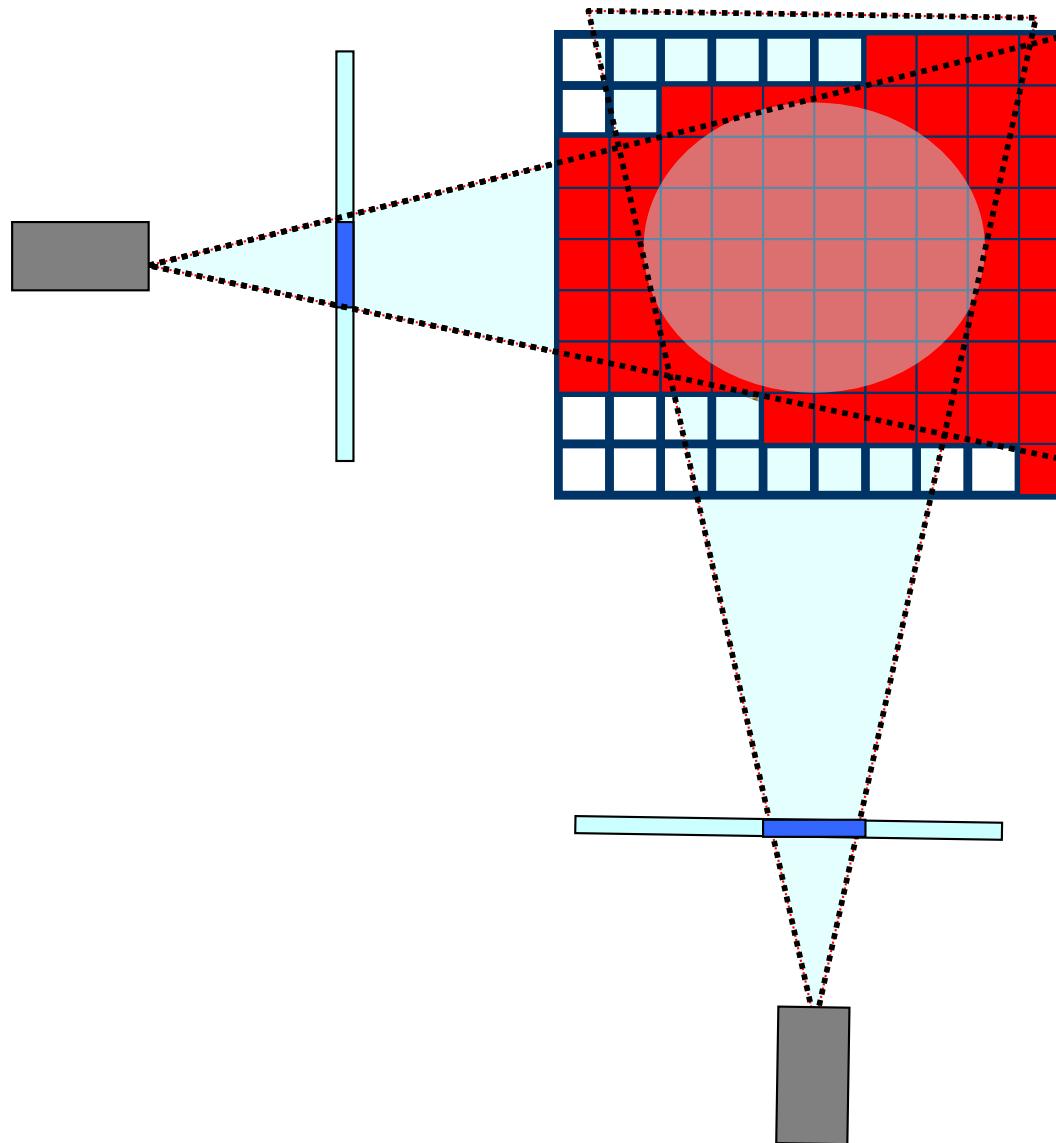
# Computing Visual Hull in 2D



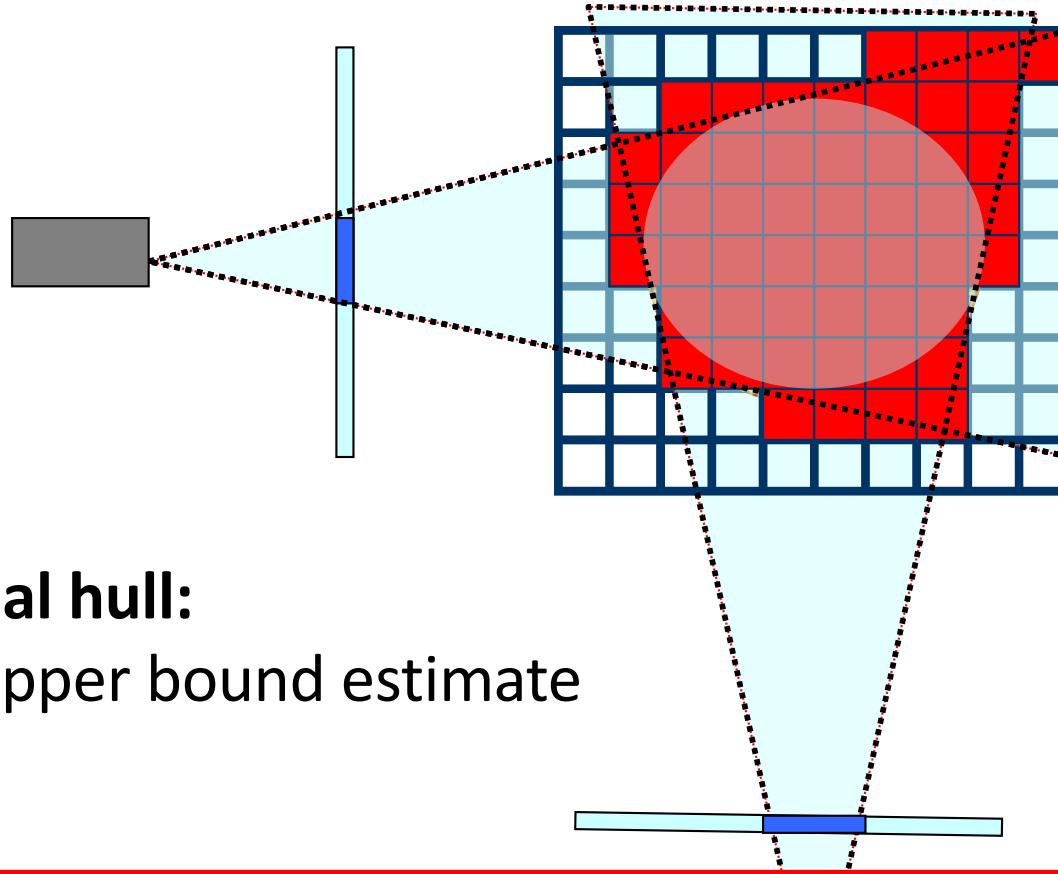
# Computing Visual Hull in 2D



# Computing Visual Hull in 2D



# Computing Visual Hull in 2D

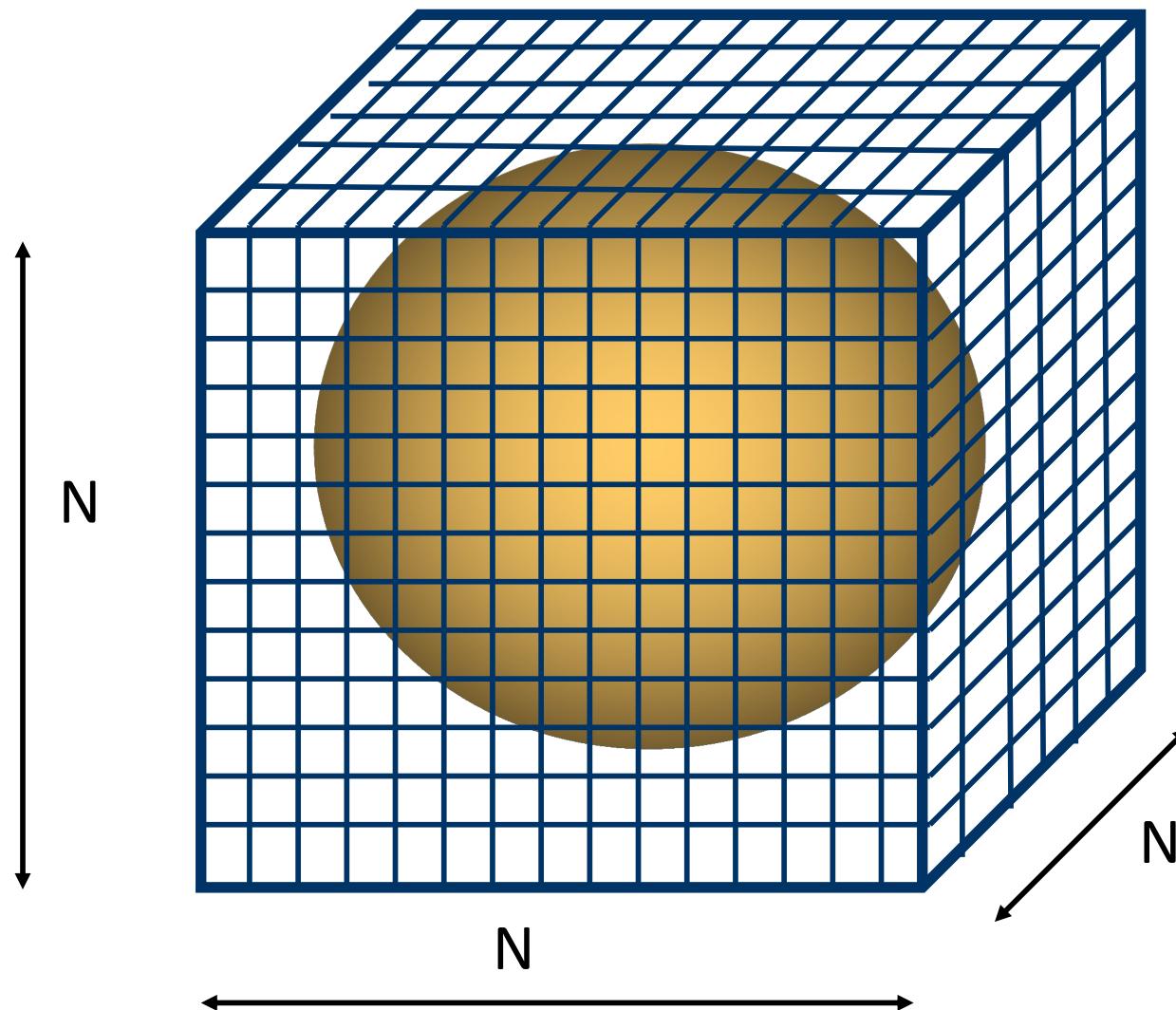


**Visual hull:**  
an upper bound estimate

**Consistency:**

A voxel must be projected into a silhouette in each image

# Space carving has complexity ...

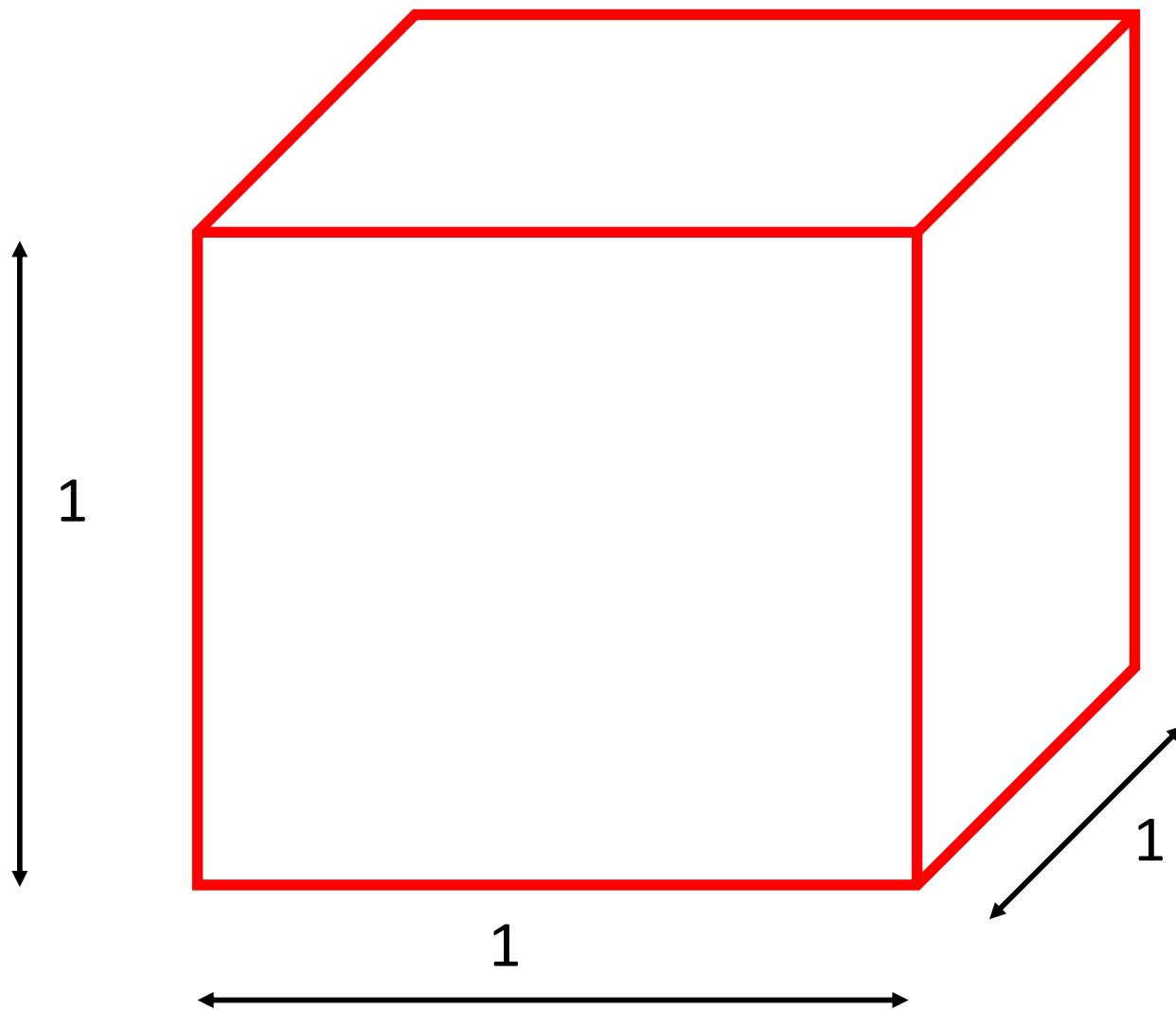


$O(N^3)$

Any suggestion  
for speeding this  
process up?

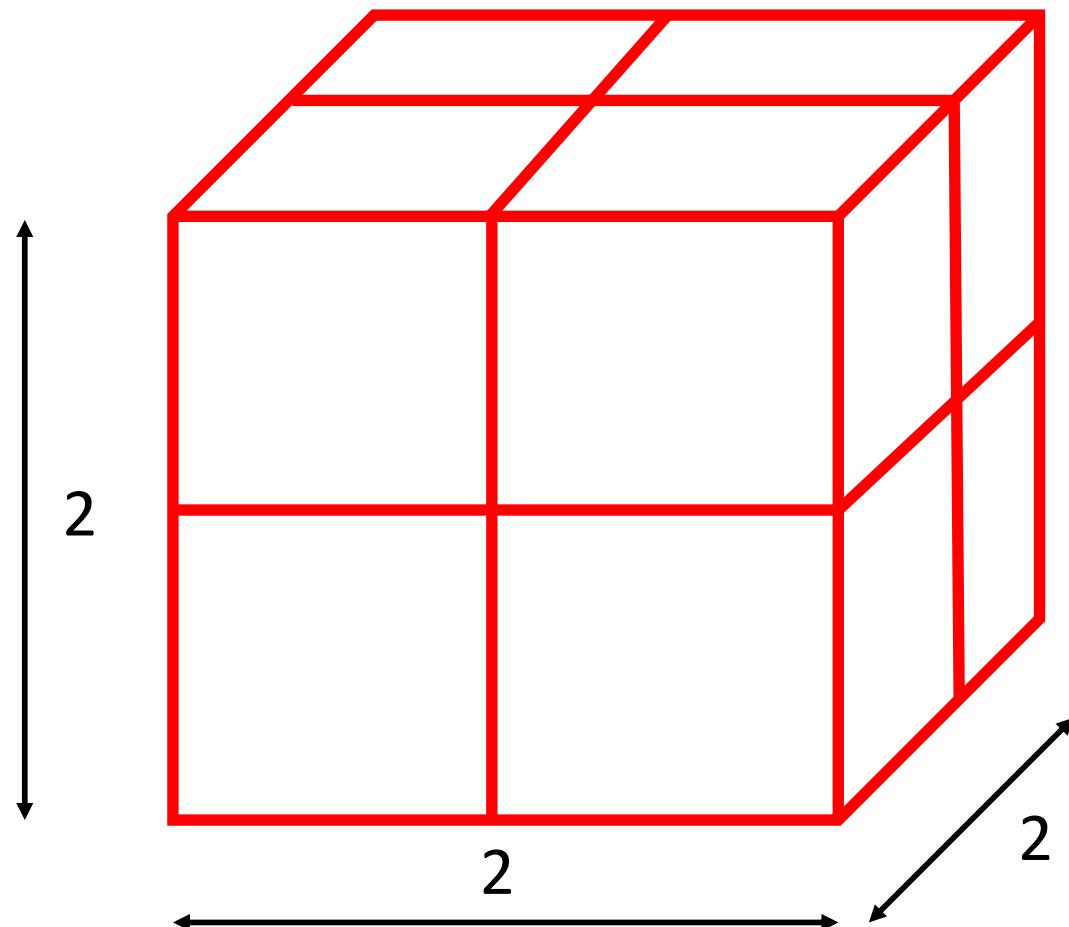
Octrees!  
(Szeliski '93)

# Complexity Reduction: Octrees

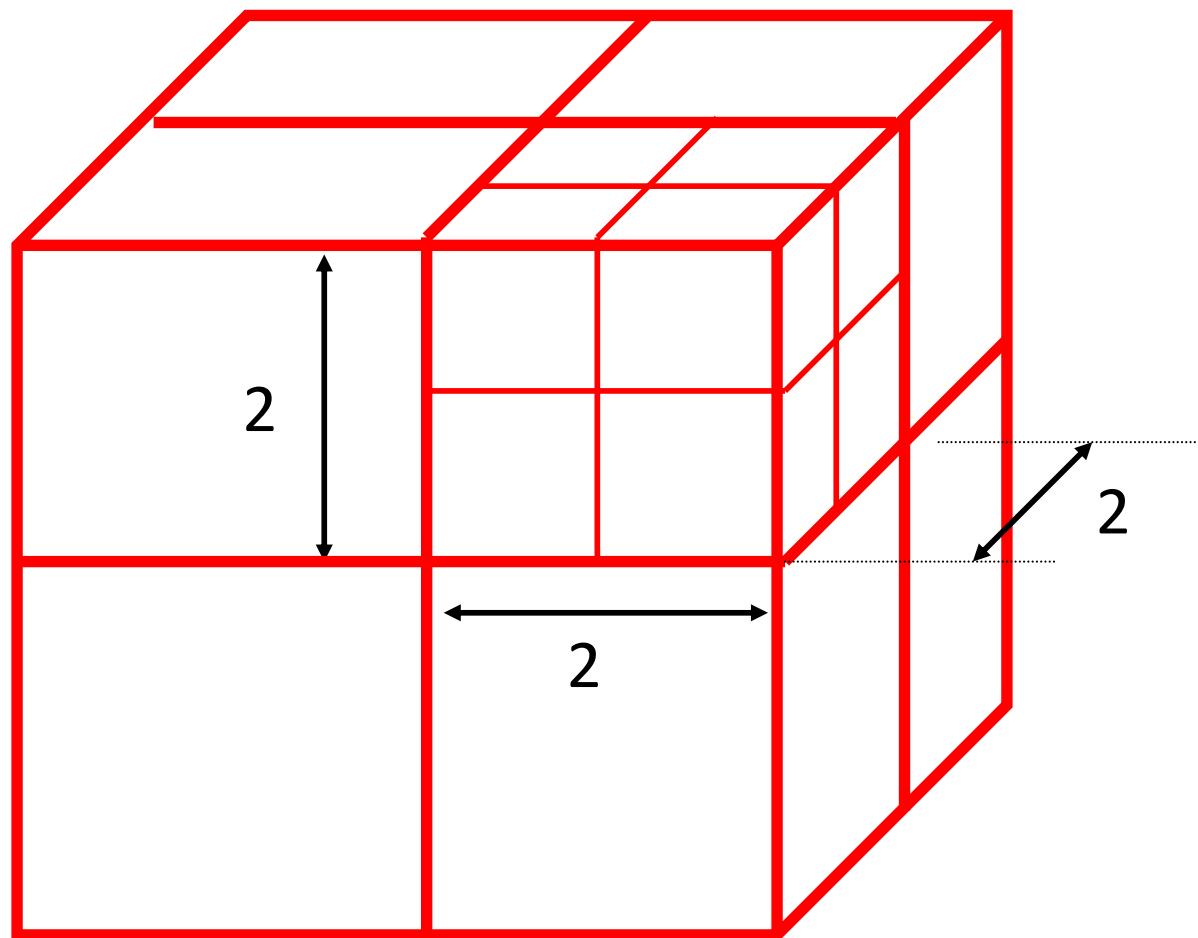


# Complexity Reduction: Octrees

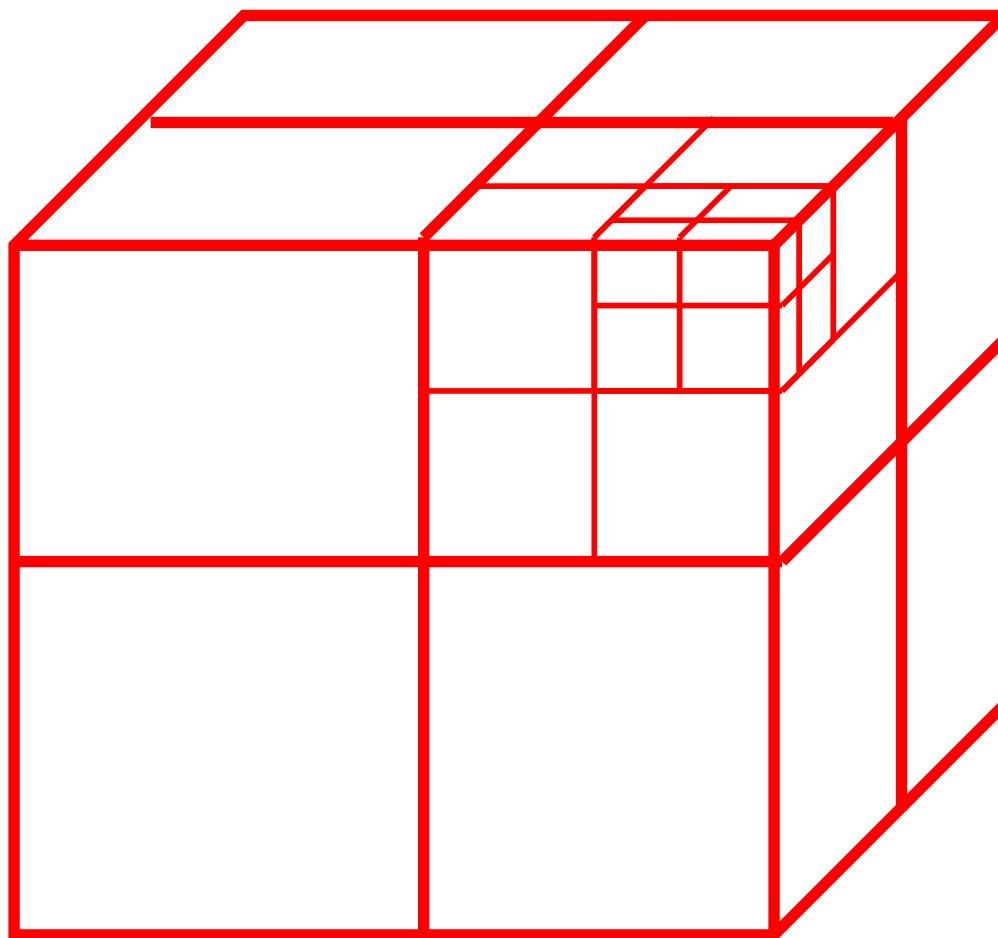
- Subdividing volume in sub-volumes of progressive smaller size



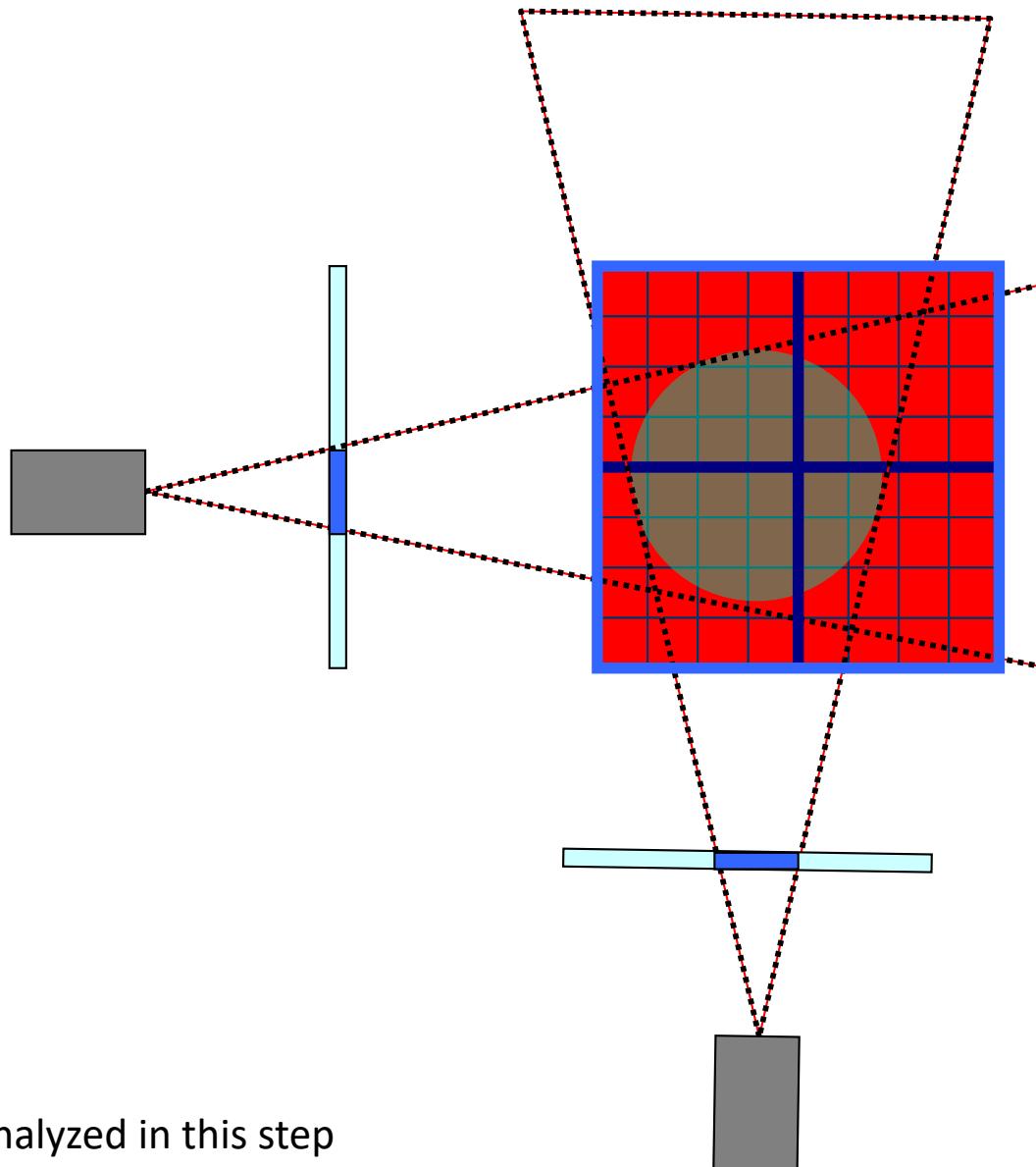
# Complexity Reduction: Octrees



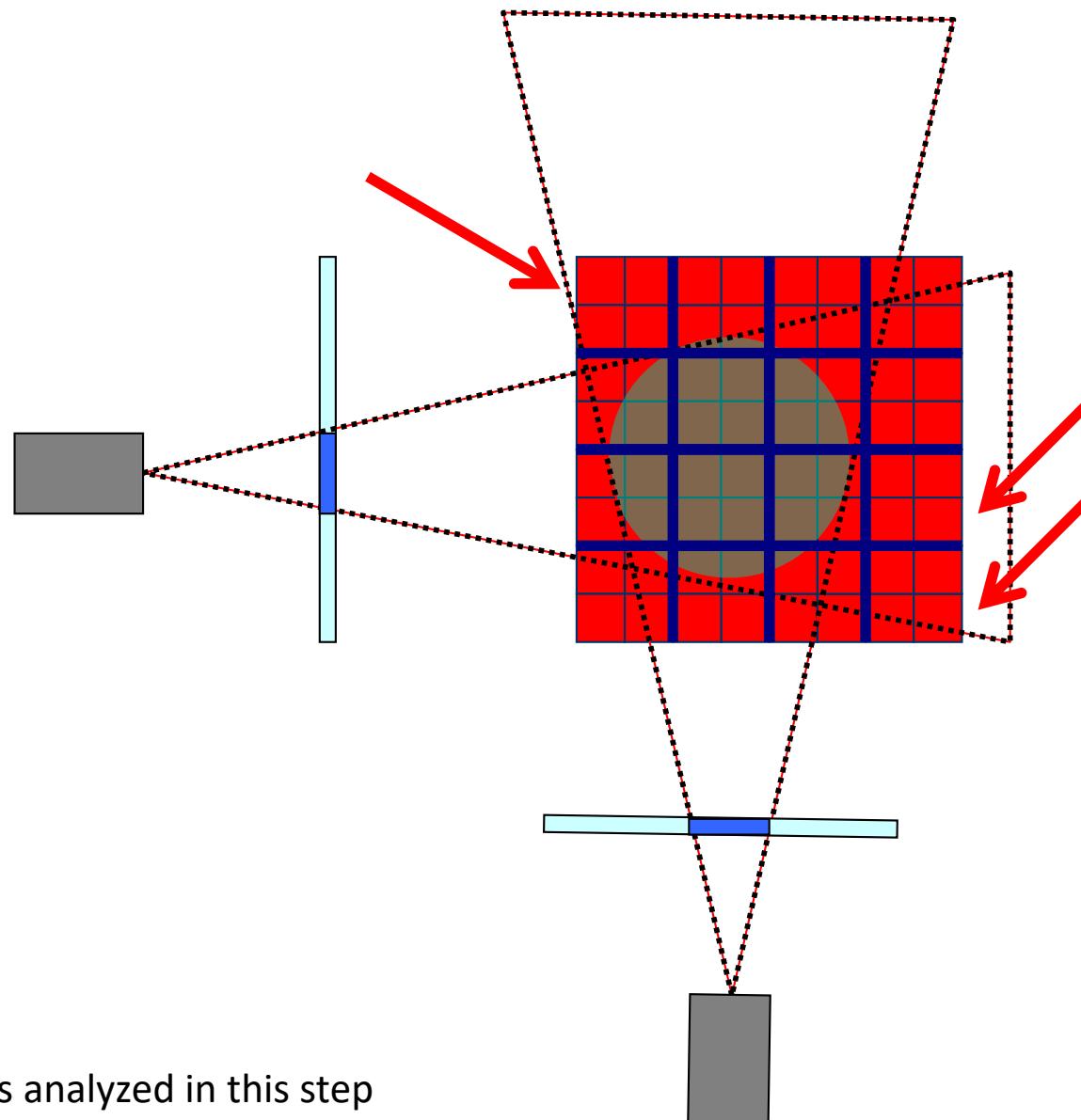
# Complexity Reduction: Octrees



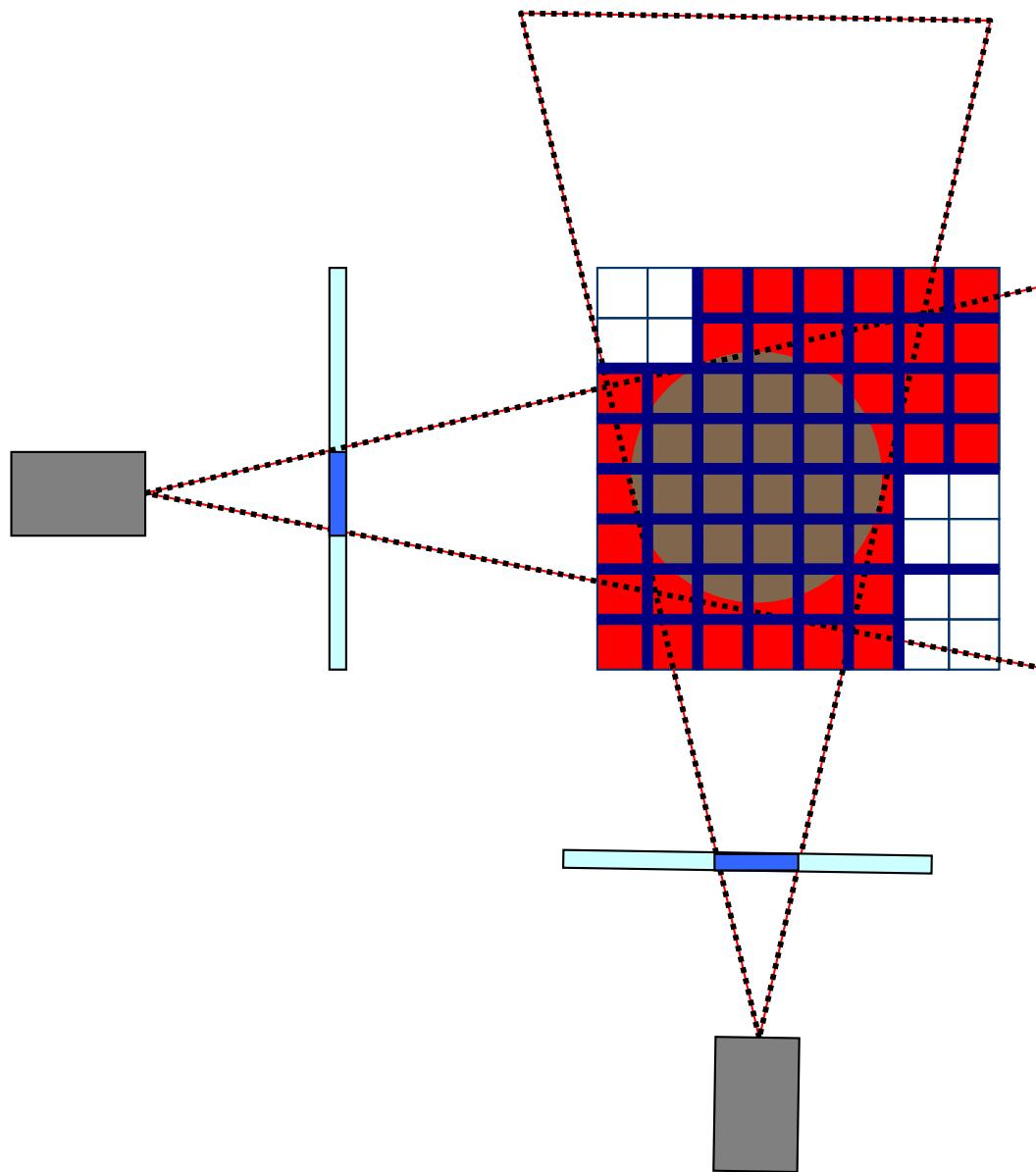
# Complexity reduction: 2D example



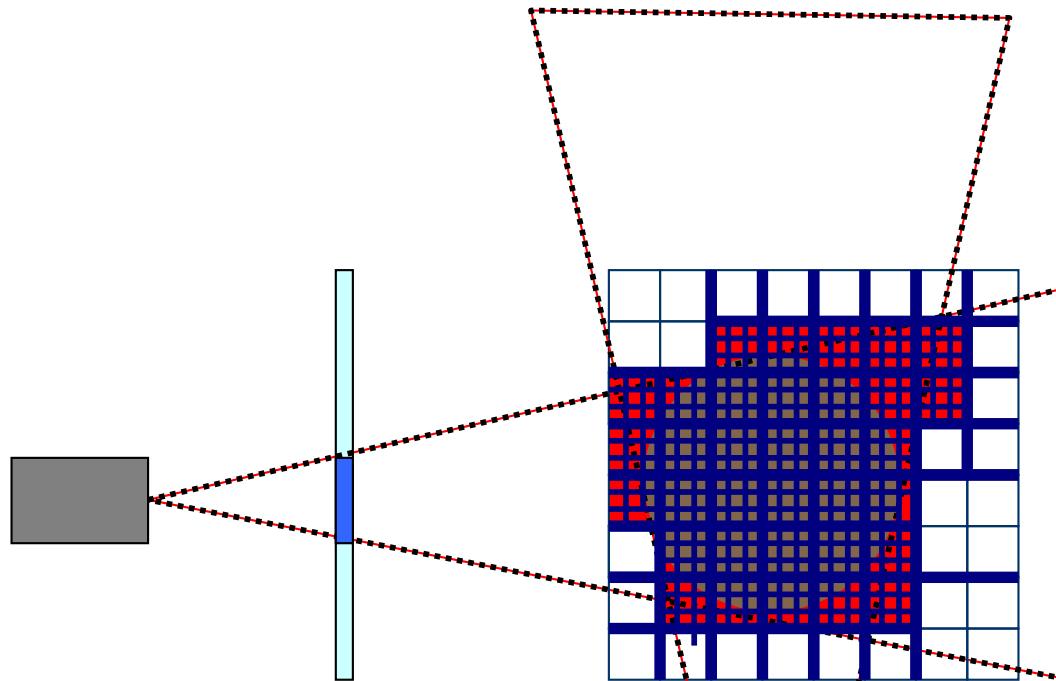
# Complexity reduction: 2D example



# Complexity reduction: 2D example



# Complexity reduction: 2D example



52 elements are analyzed in this step

$16 \times 34 = 544$  voxels are analyzed in  
this step

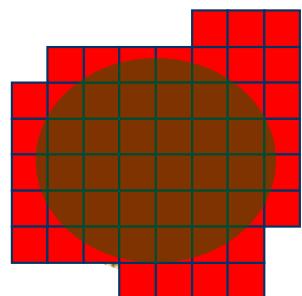
$1 + 4 + 16 + 52 + 544 = 617$  voxels have  
been analyzed in total  
(rather than  $32 \times 32 = 1024$ )

# Advantages of Space carving

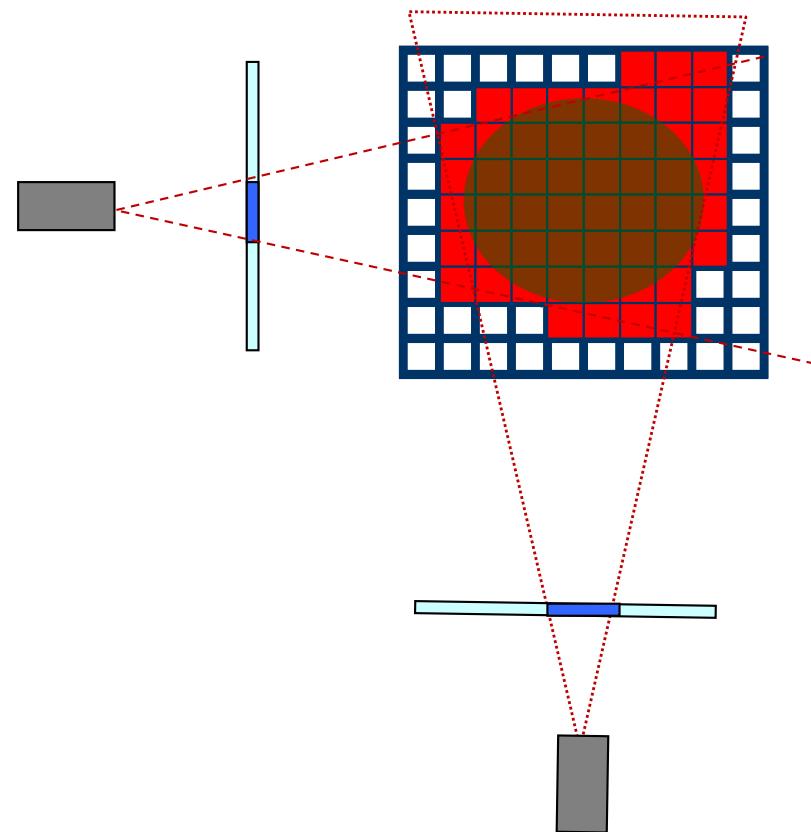
- Robust and simple
- No need to solve for correspondences

# Limitations of Space carving

- Accuracy function of number of views



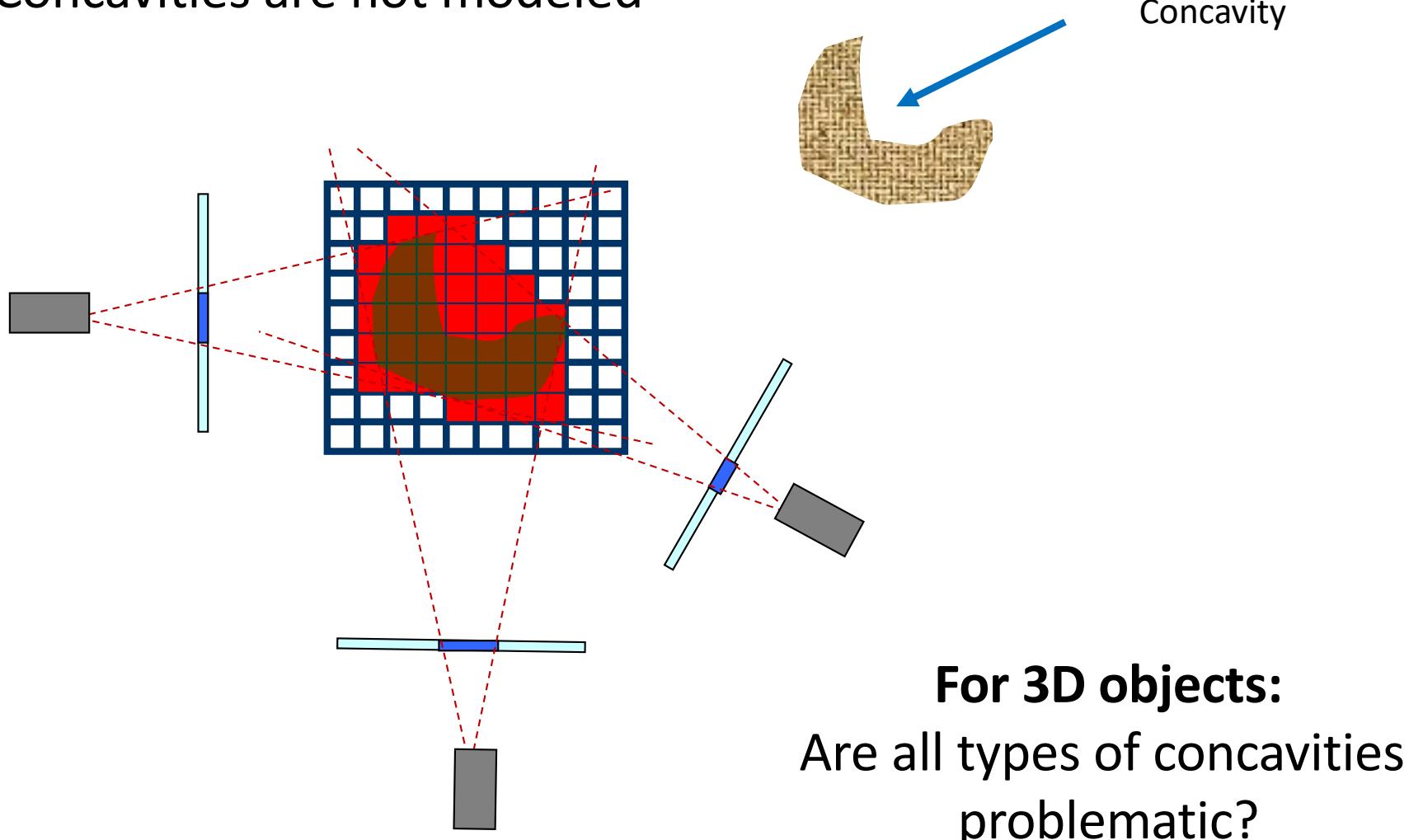
Not a good estimate



What else?

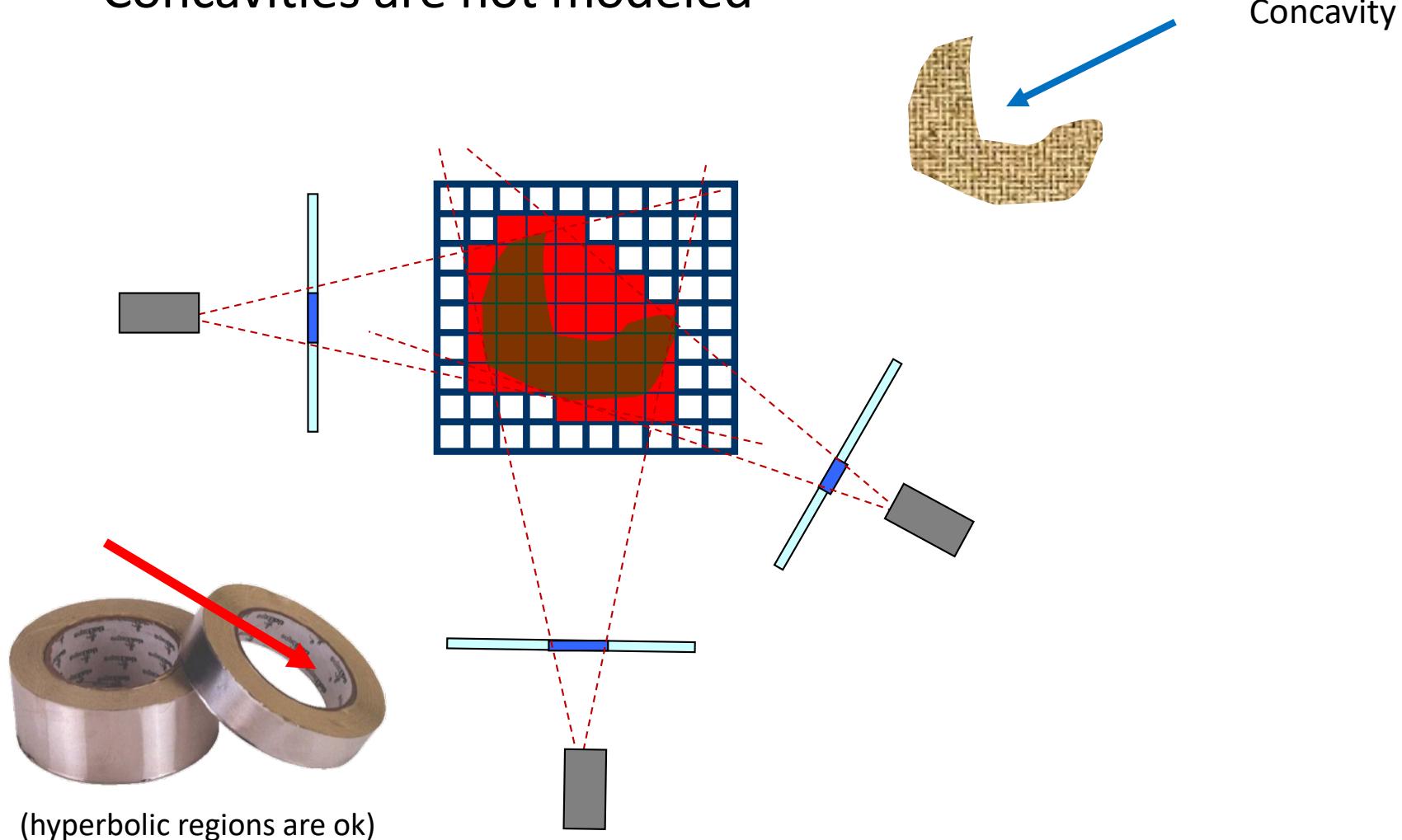
# Limitations of Space carving

- Concavities are not modeled



# Limitations of Space carving

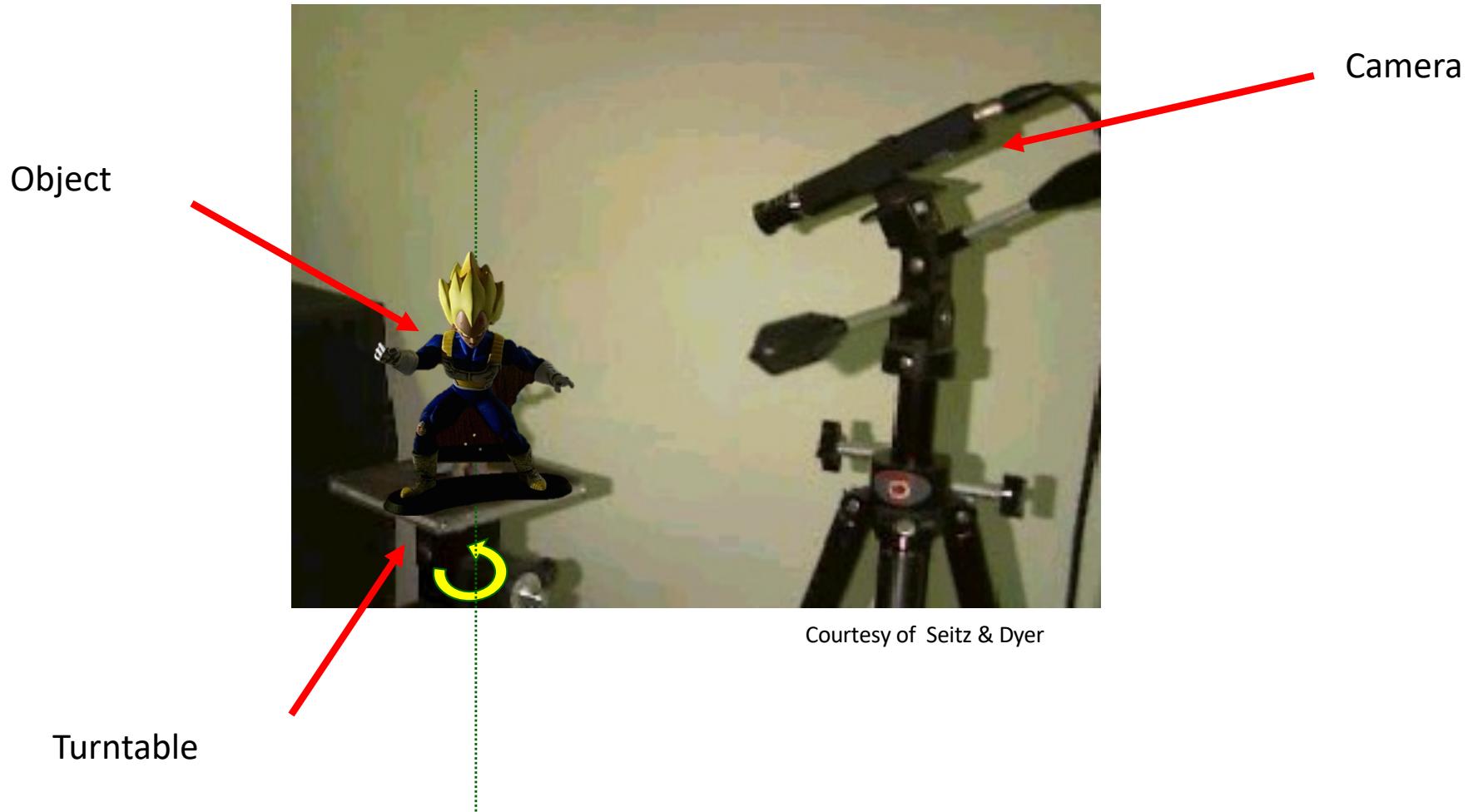
- Concavities are not modeled



(hyperbolic regions are ok)

-- see Laurentini (1995)

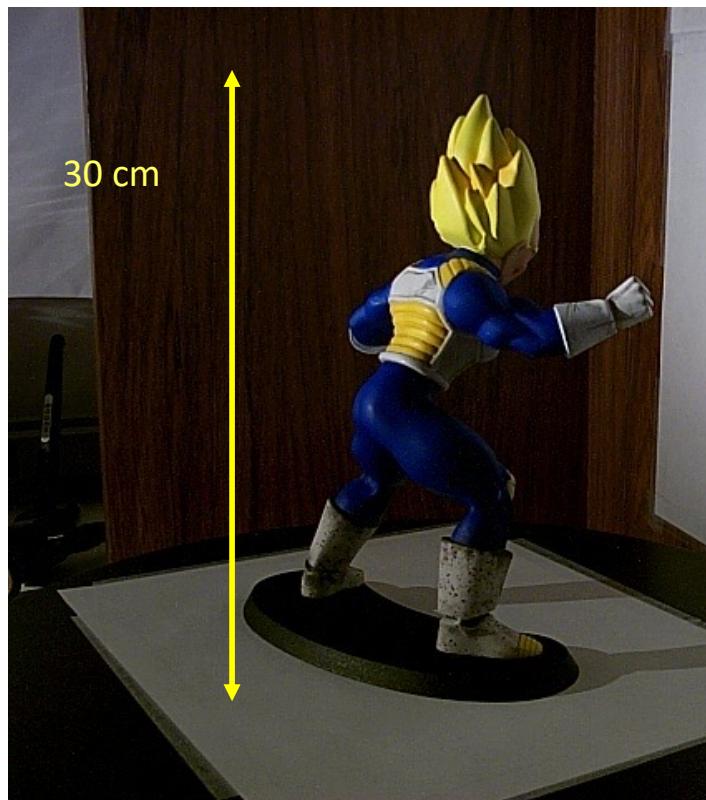
# Space carving: A Classic Setup



# Space carving: A Classic Setup

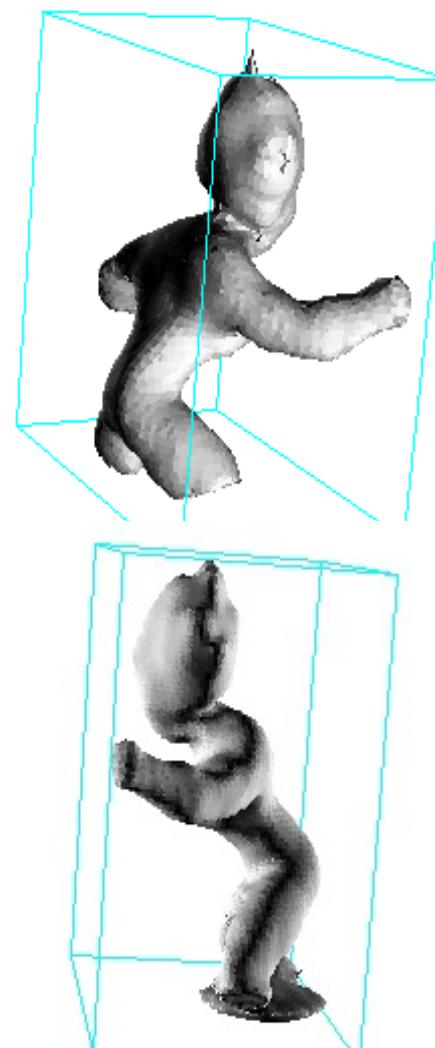


# Space carving: Experiments

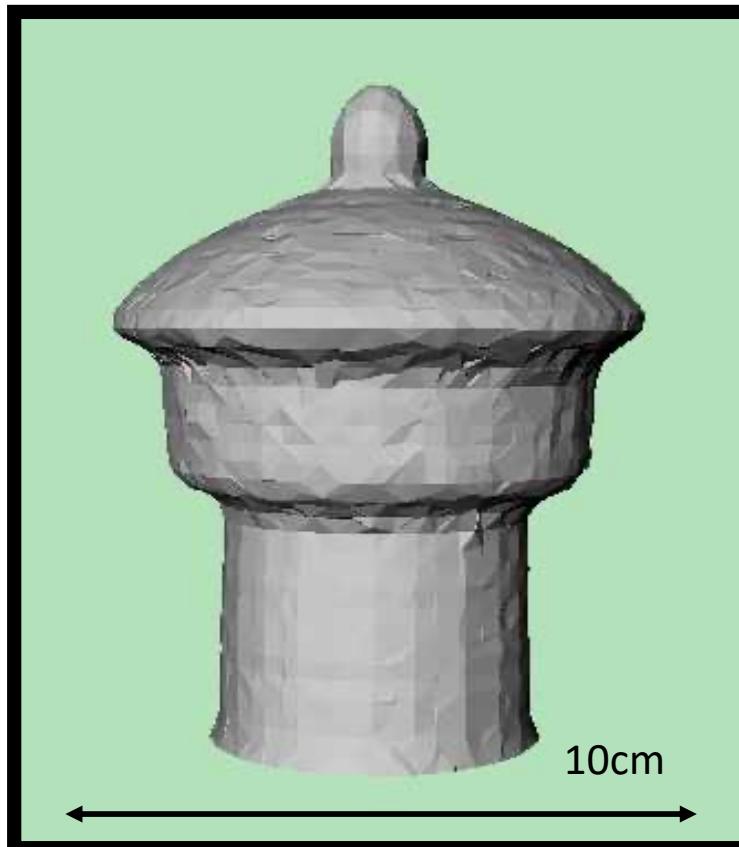


24 poses ( $15^\circ$ )

voxel size = 1mm

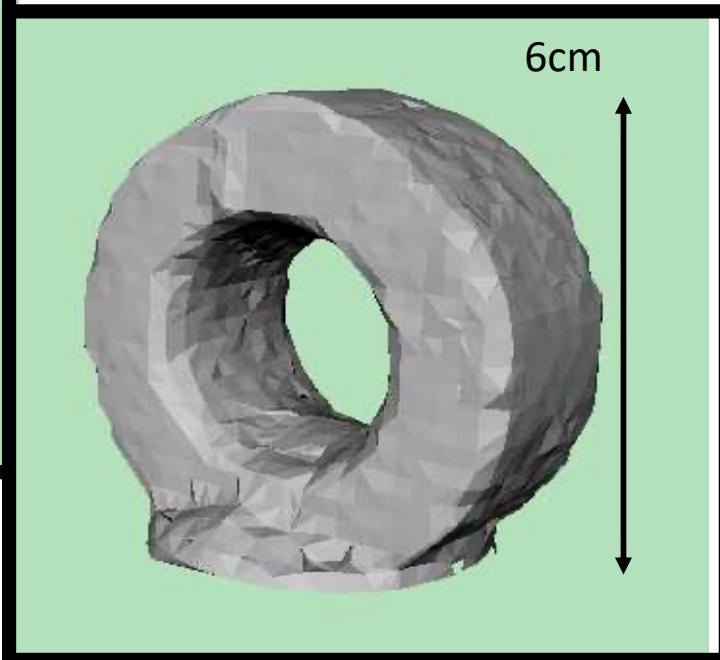


# Space carving: Experiments



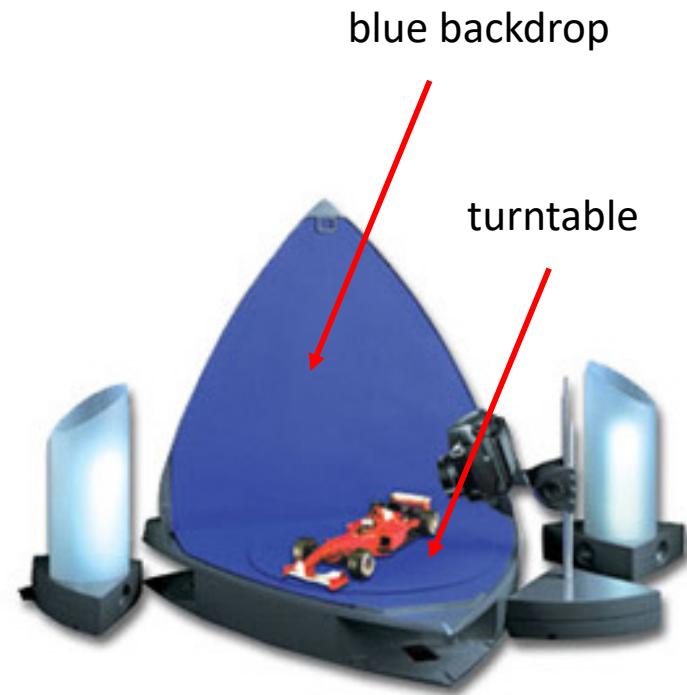
24 poses ( $15^\circ$ )

voxel size = 2mm



# Space carving: Conclusions

- Robust
- Produce conservative estimates
- Concavities can be a problem
- Low-end commercial 3D scanners



# Lecture 8

## Active stereo & Volumetric stereo



- Active stereo
  - Structured lighting
  - Depth sensing
- Volumetric stereo:
  - Space carving
  - Shadow carving
  - Voxel coloring

# Shape from Shadows

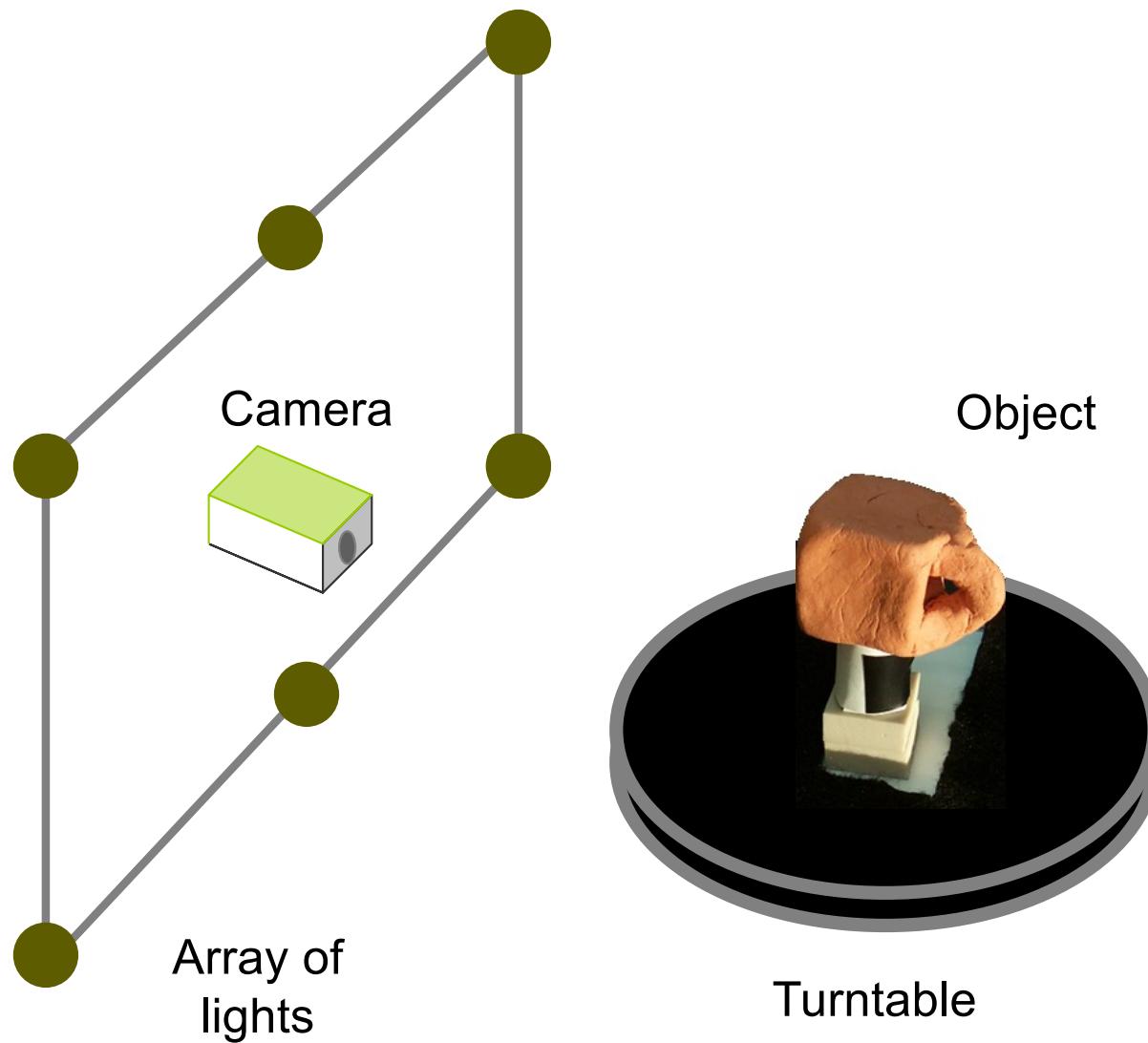
- Self-shadows are visual cues for shape recovery



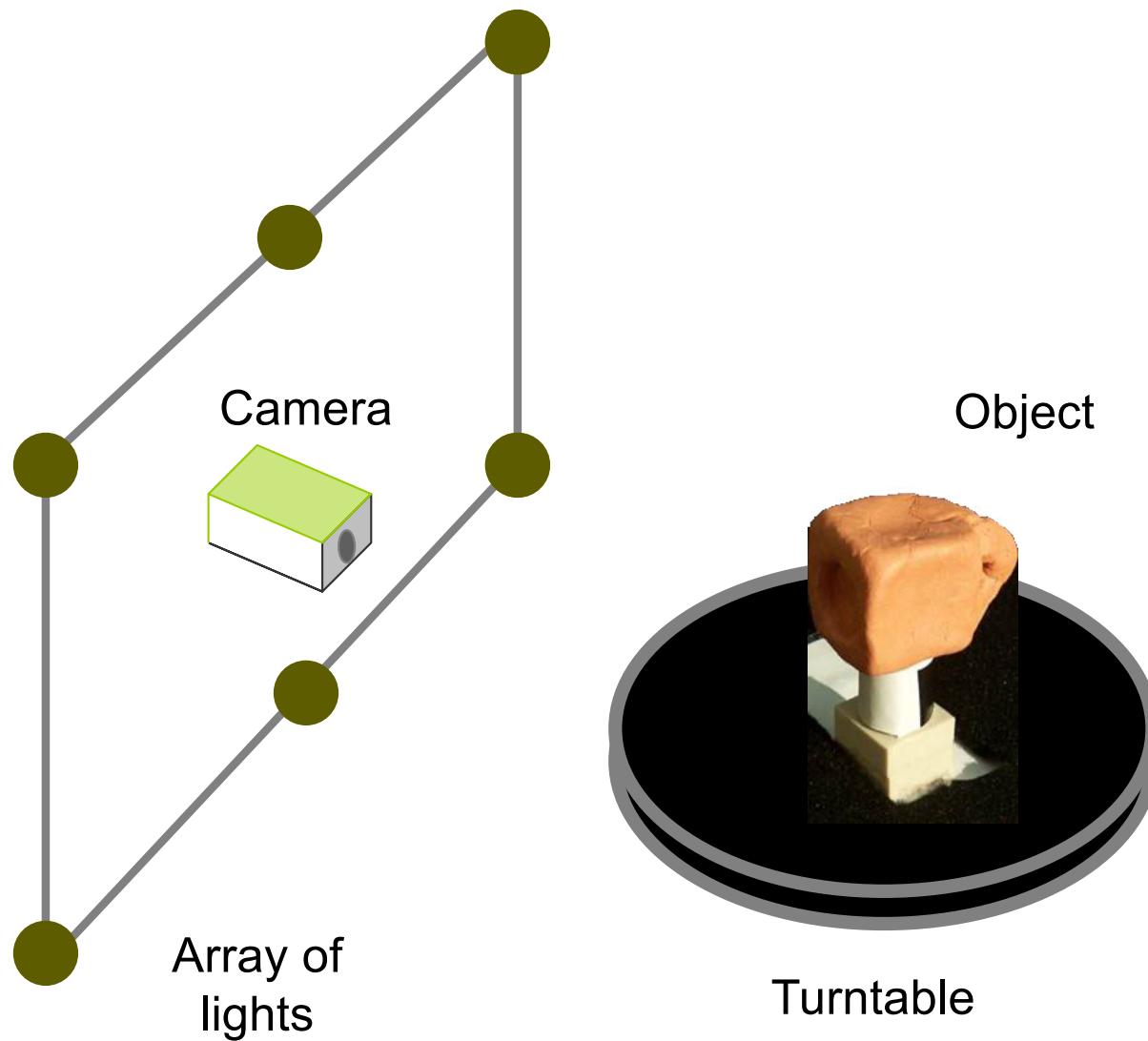
Self-shadows indicate concavities  
(no modeled by contours)



# Shadow carving: The Setup

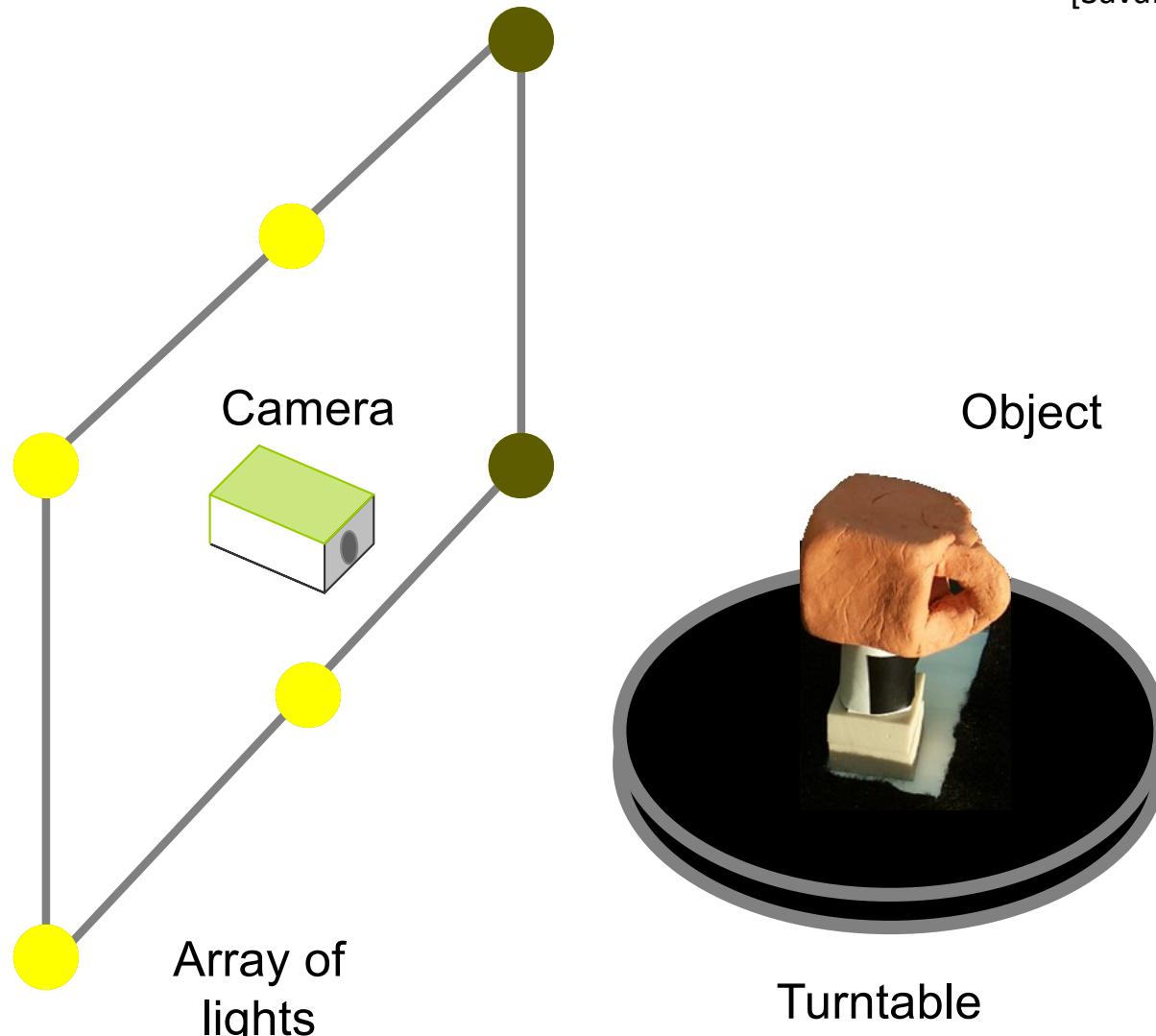
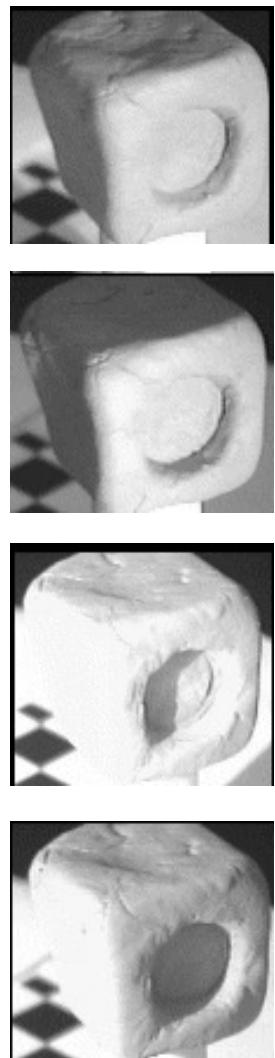


# Shadow carving: The Setup



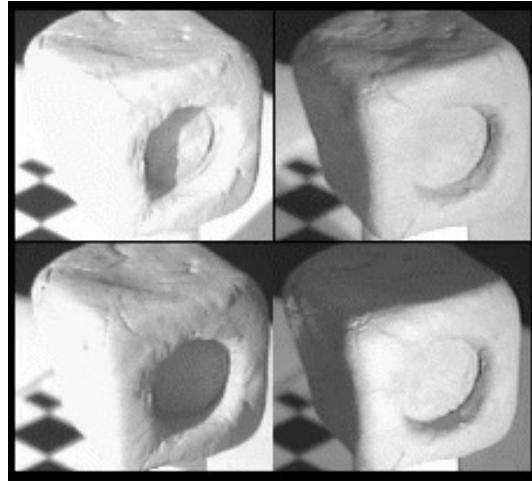
# Shadow carving: The Setup

[Savarese et al '01]



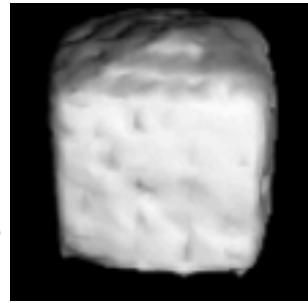
# Shadow carving

[Savarese et al. 2001]

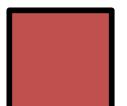
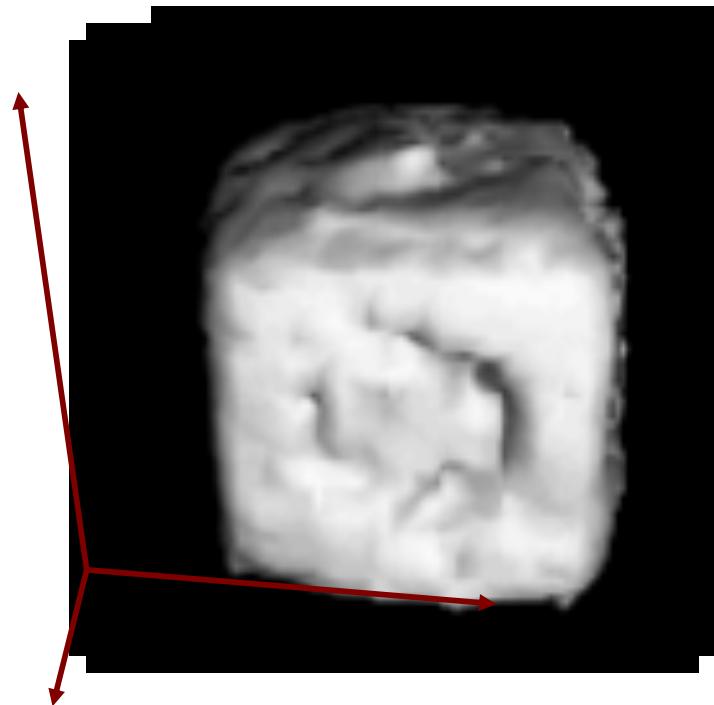
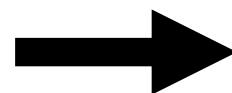


Self-shadows

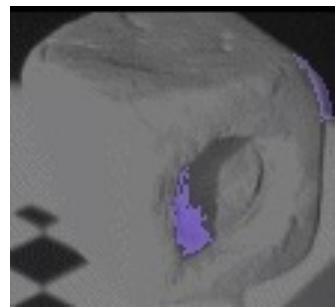
+



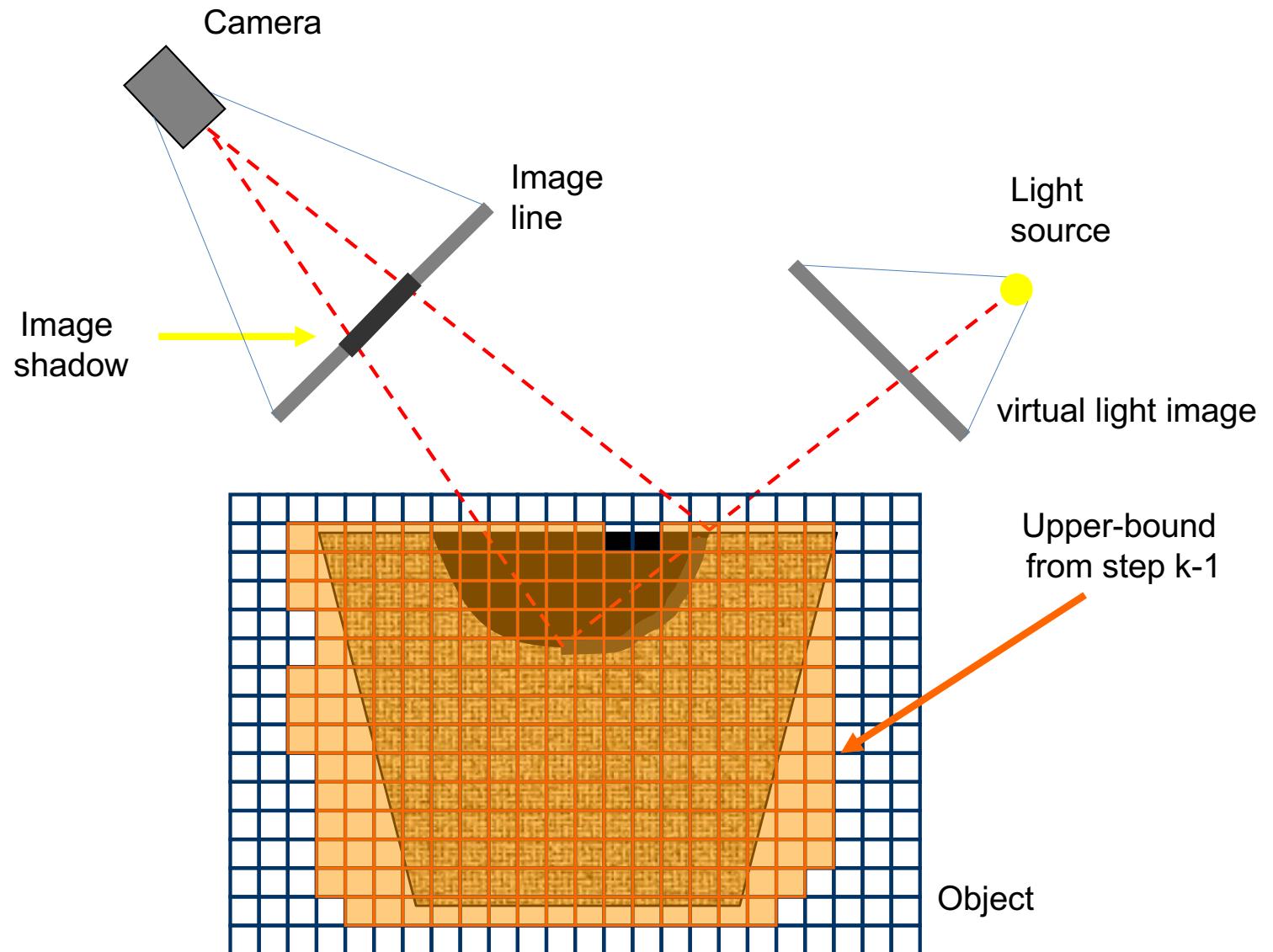
Object's upper bound



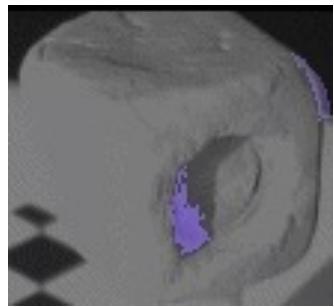
# Algorithm: Step k



Image

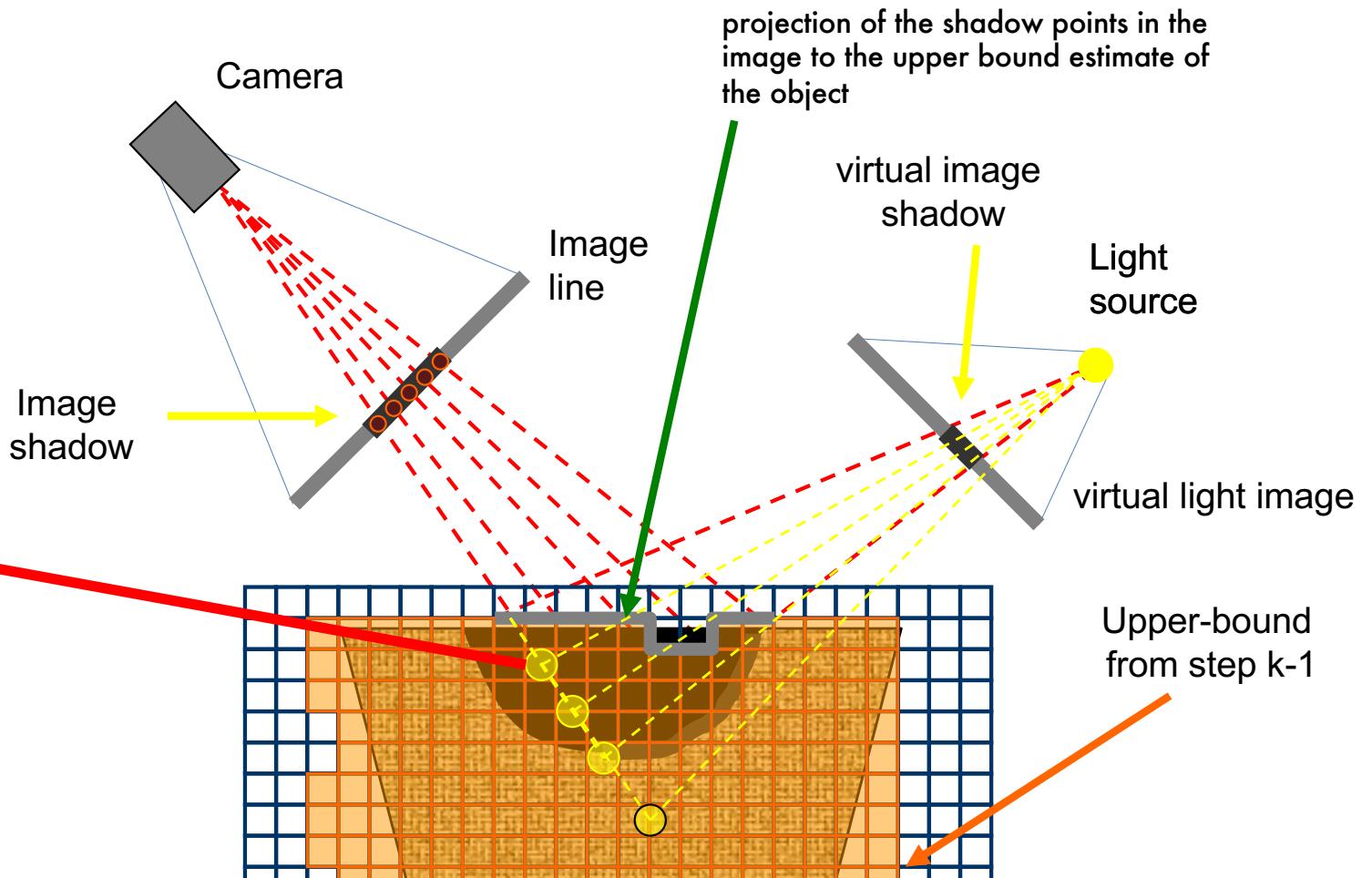


# Algorithm: Step k



Image

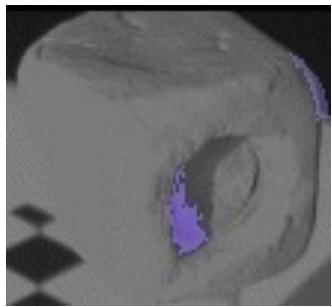
?



## Theorem:

A voxel that projects into an image shadow AND an virtual image shadow cannot belong to the object.

# Algorithm: Step k

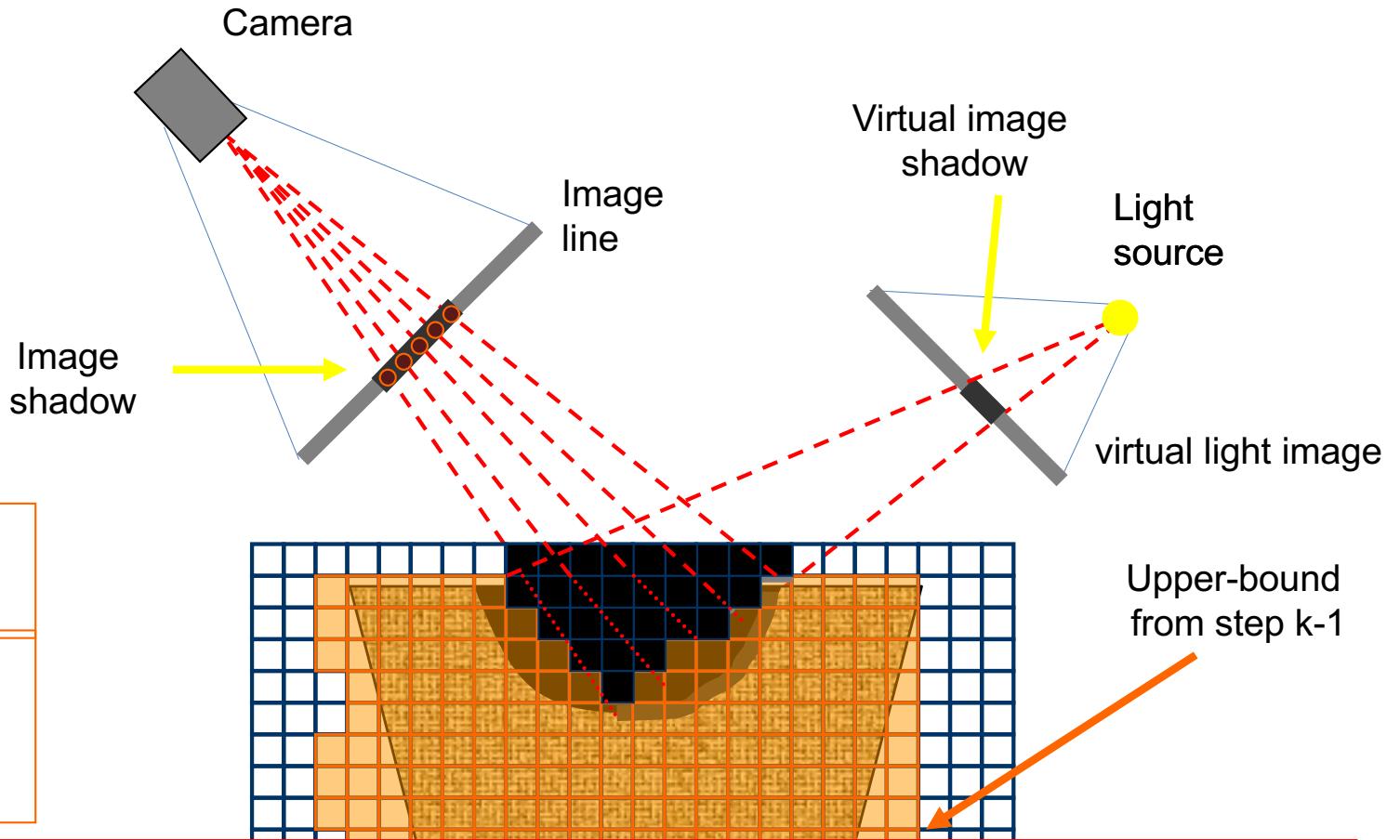


Image

Properties:

No further volume can be removed

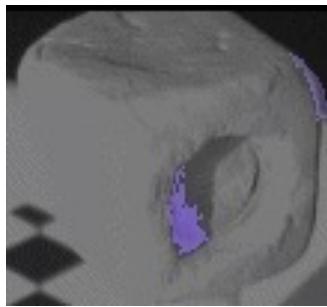
Carving process  
always  
conservative



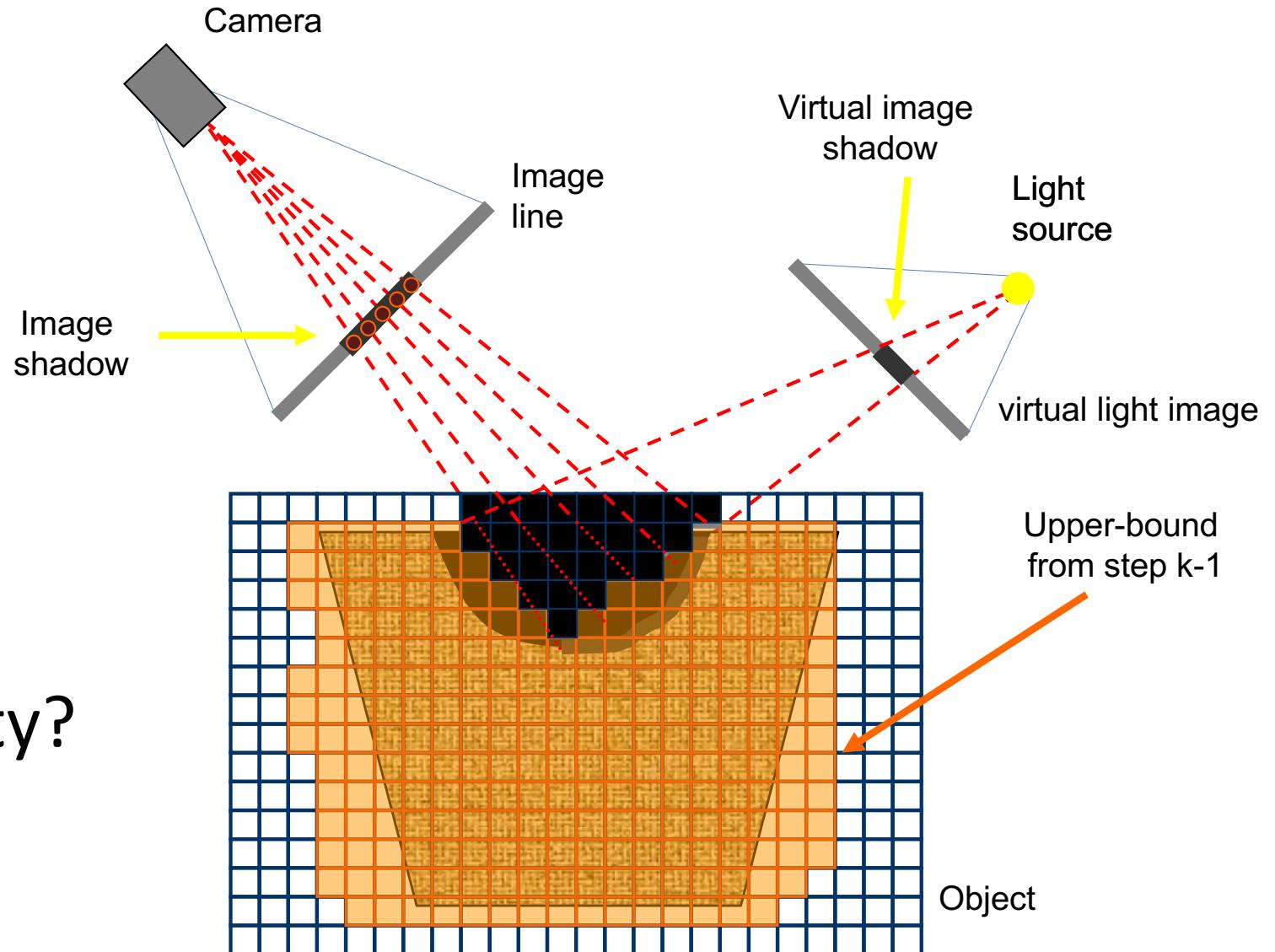
Consistency:

In order for a voxel to be removed it must project into both  
image shadow and virtual image shadow

# Algorithm: Step k



Image

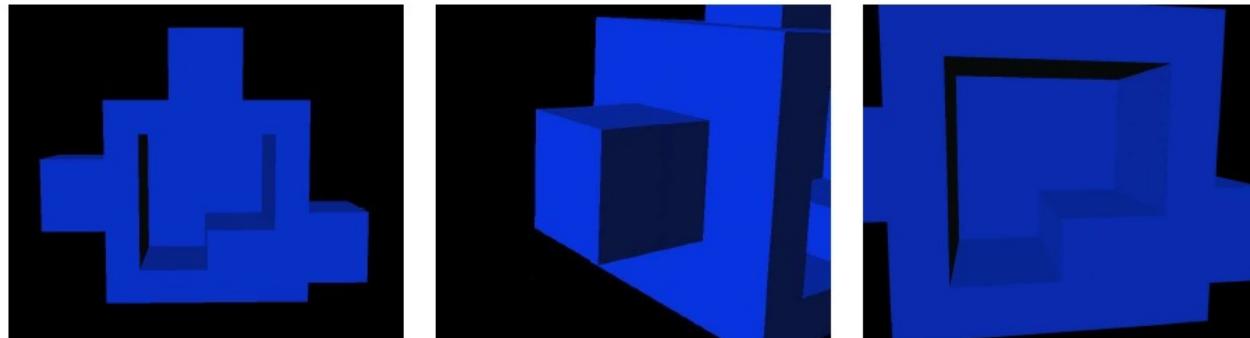


Complexity?

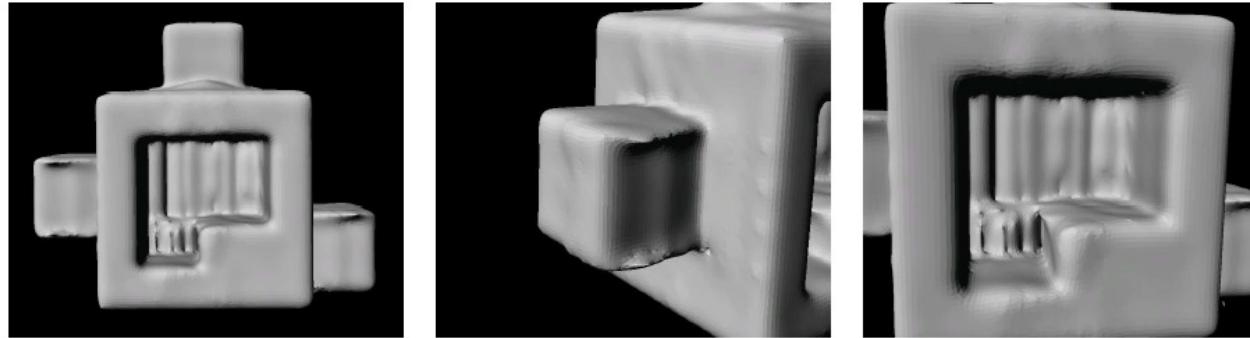
$$O(2N^3)$$

# Simulating the System

- 24 positions
- 4 lights

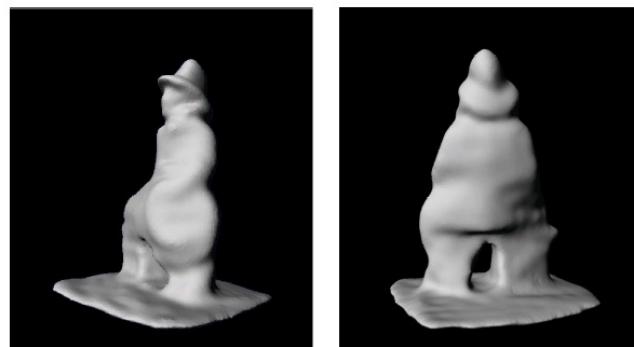


- 72 positions
- 8 lights

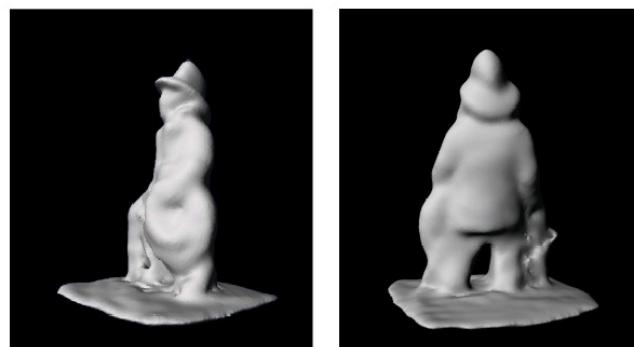


# Results

- 16 positions
- 4 lights



**Space carving**



**Shadow carving**

# Results



Space carving



Shadow carving

# Shadow carving: Summary

- Produces a conservative volume estimate
- Accuracy depending on view point and light source number
- Limitations with reflective & low albedo regions

# Lecture 8

## Active stereo & Volumetric stereo



- Active stereo
  - Structured lighting
  - Depth sensing
- Volumetric stereo:
  - Space carving
  - Shadow carving
  - Voxel coloring

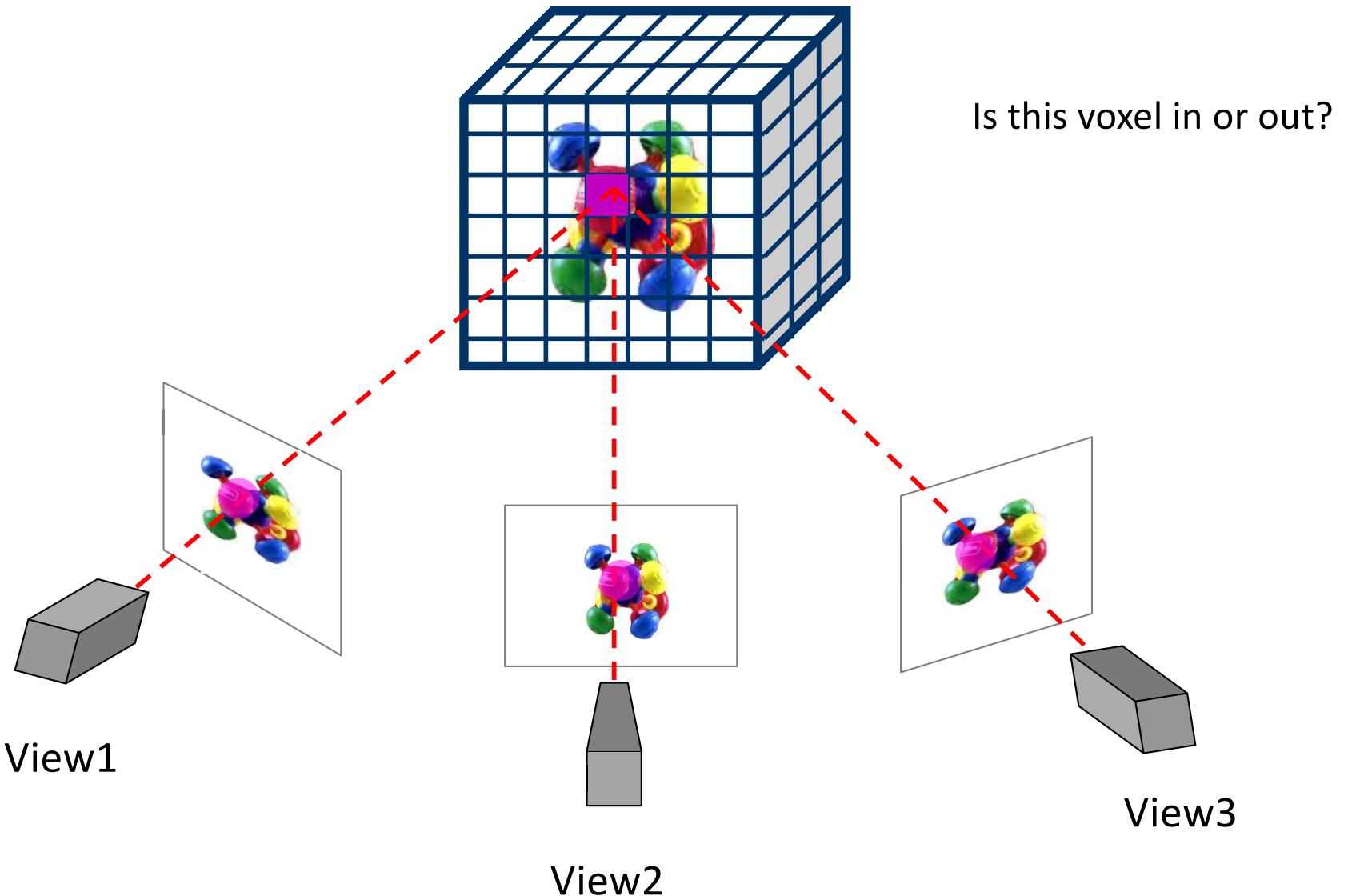
# Voxel Coloring

[Seitz & Dyer ('97)]  
[R. Collins (Space Sweep, '96)]

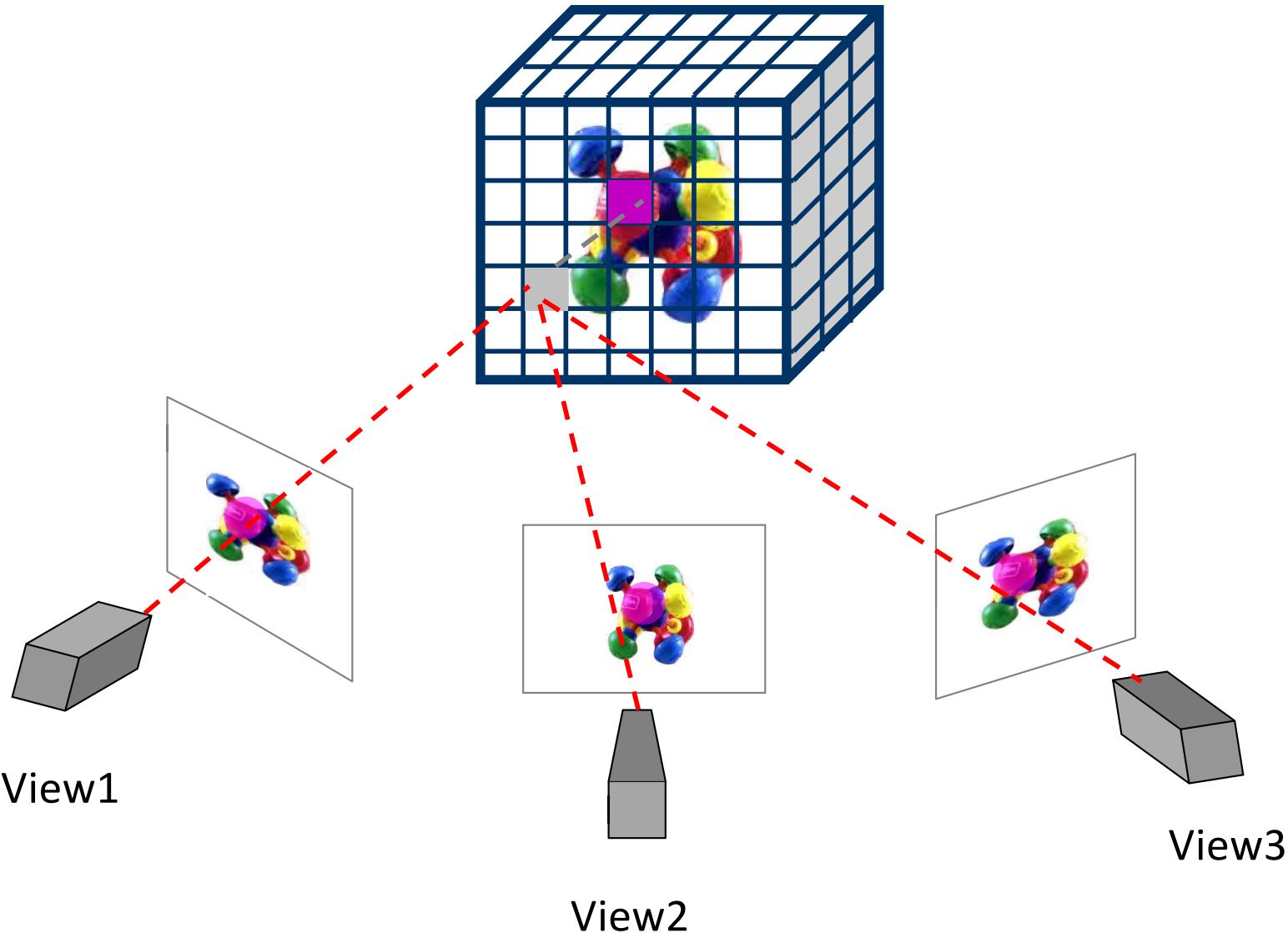


- Color/photo-consistency
- Jointly model structure and appearance

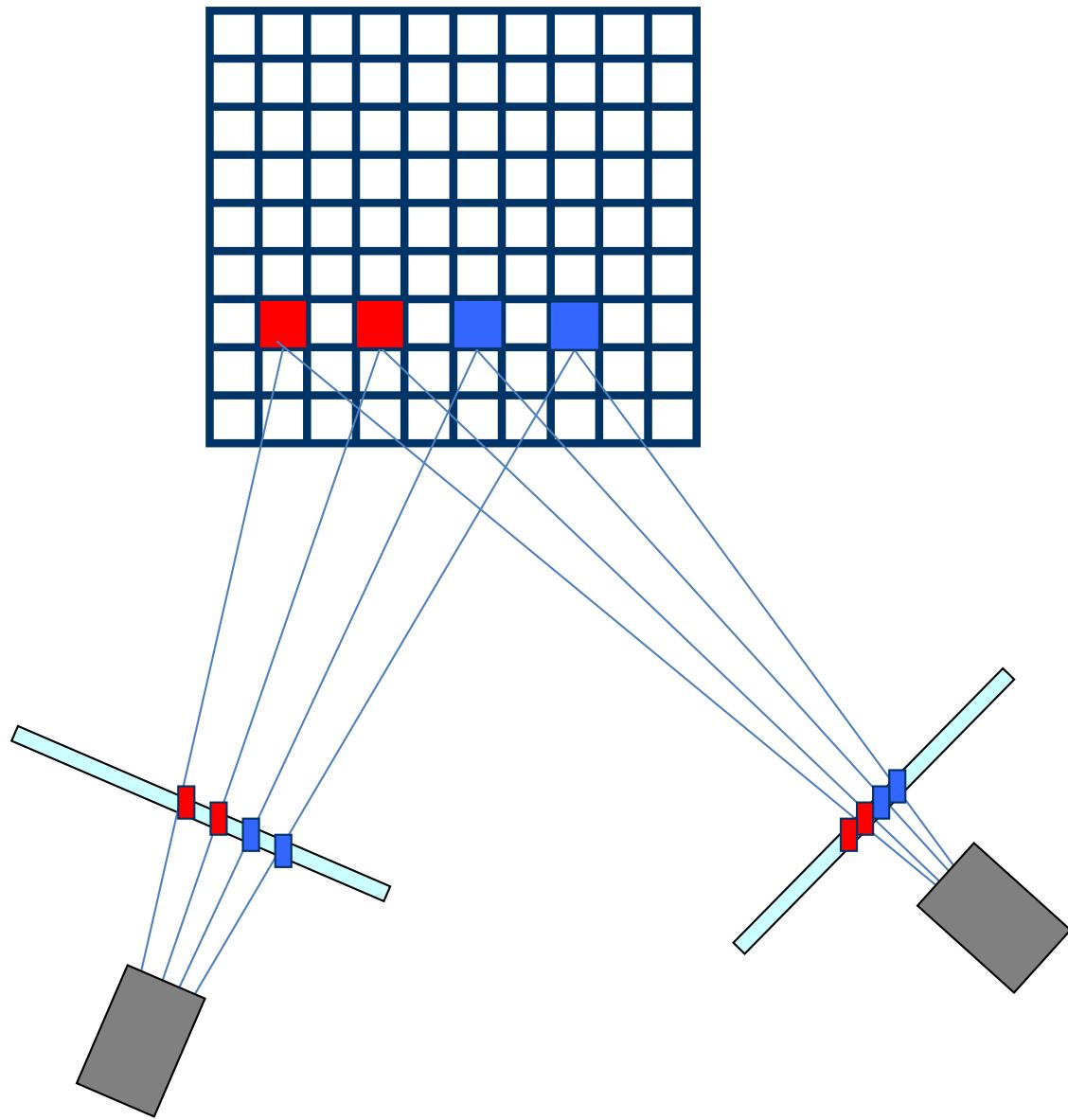
# Basic Idea



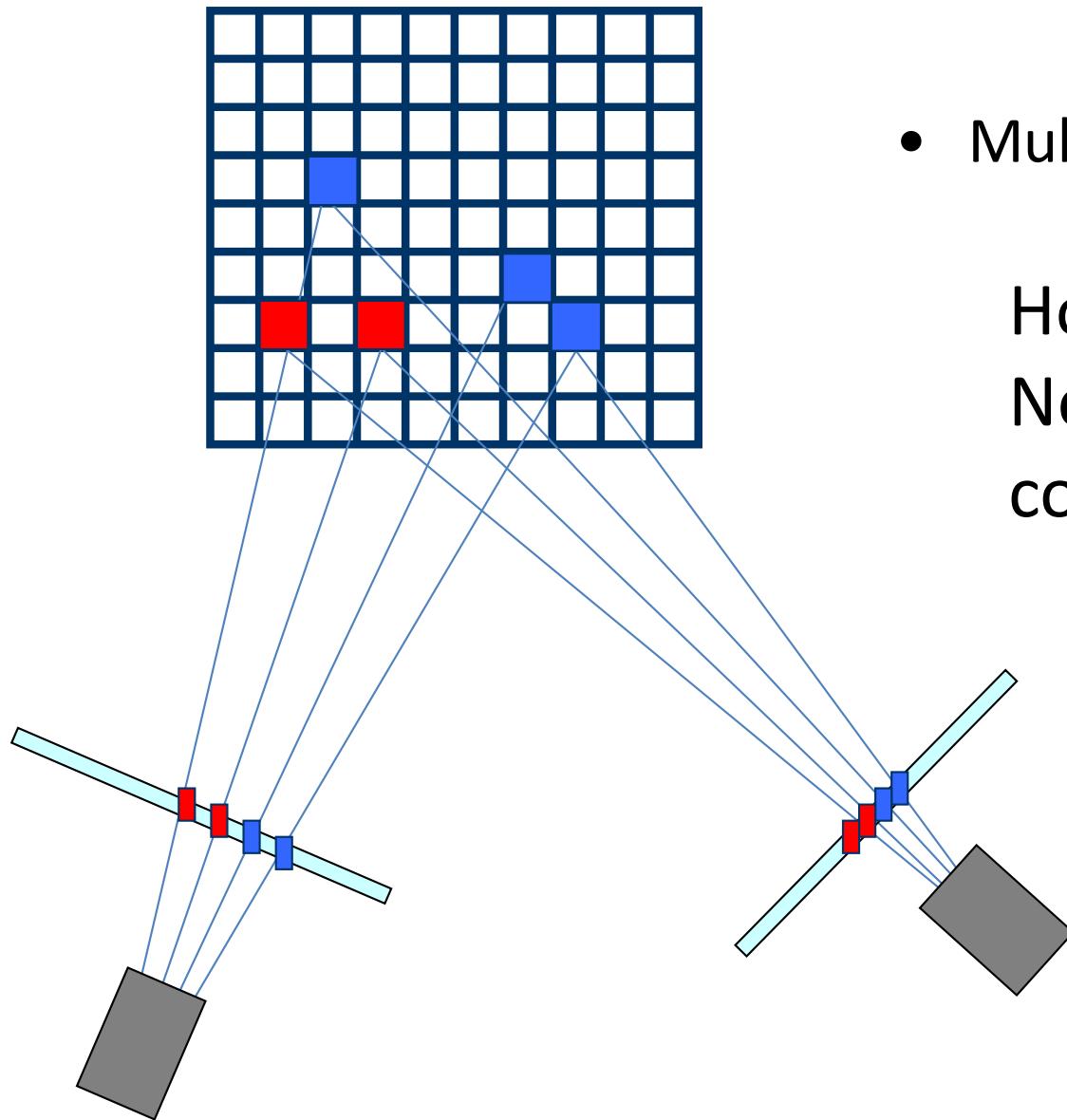
# Basic Idea



# Uniqueness



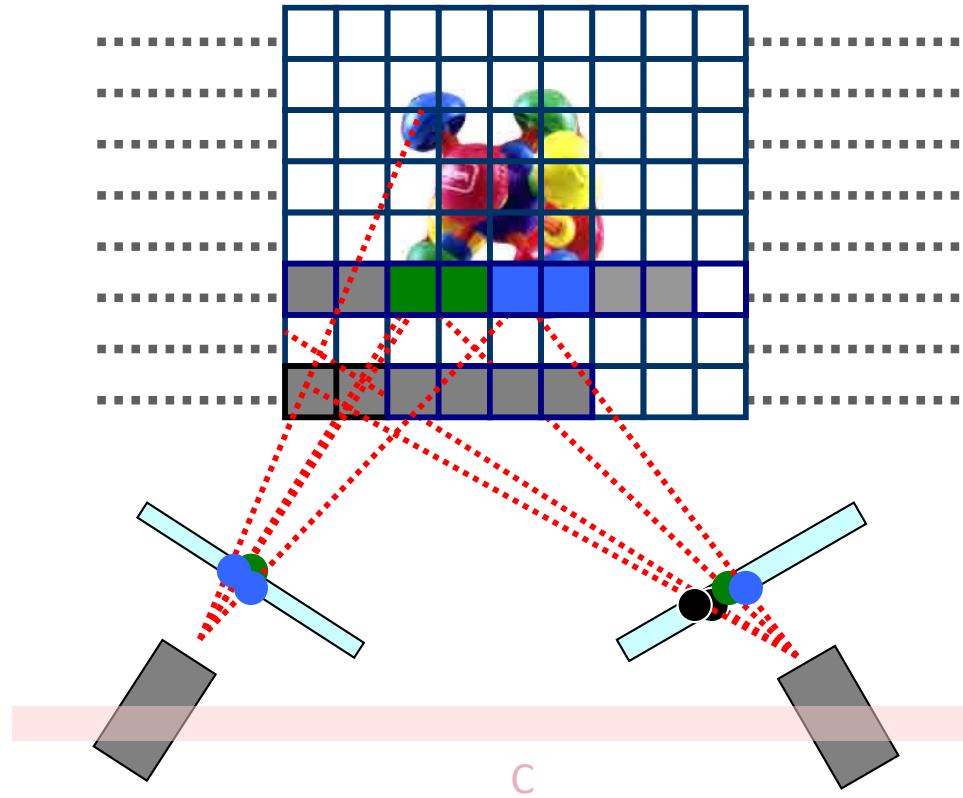
# Uniqueness



- Multiple consistent scenes

How to fix this?  
Need to use a visibility  
constraint

# Algorithm for enforcing visibility constraints



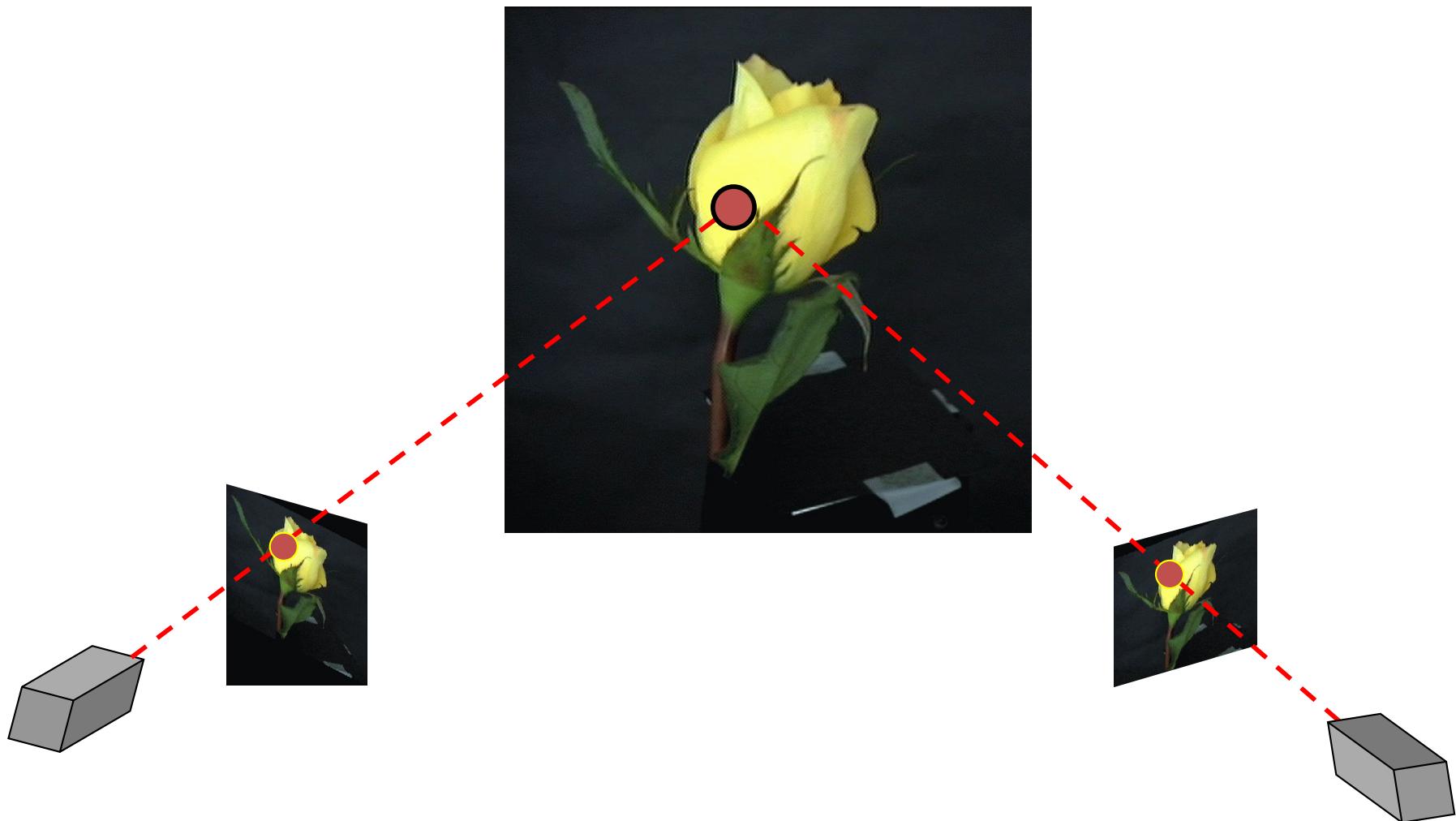
# Algorithm Complexity

- Voxel coloring visits each  $N^3$  voxels only once
- Project each voxel into  $L$  images

$$\rightarrow O(L N^3)$$

NOTE: not function of the number of colors

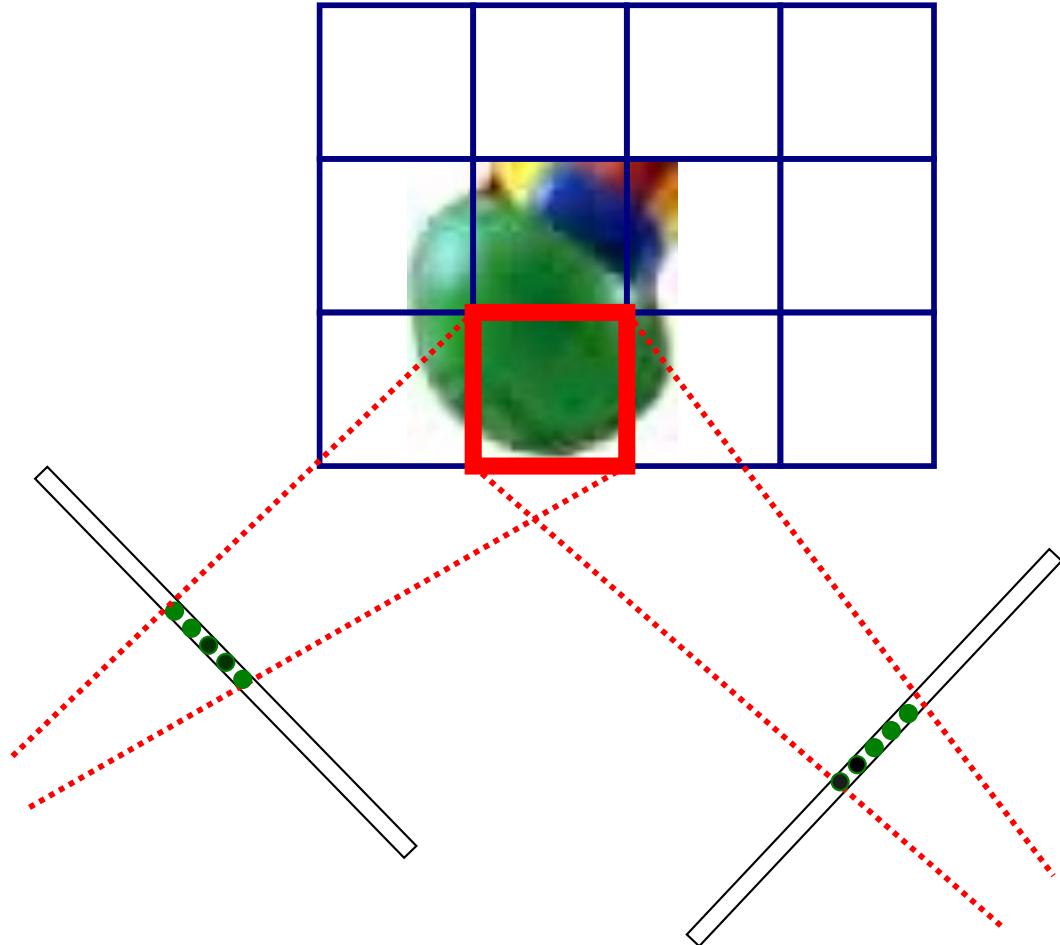
# A Critical Assumption: Lambertian Surfaces



# Non Lambertian Surfaces



# Photoconsistency Test



$$C = \text{corr} ( \begin{array}{c} \bullet \\ \bullet \\ \bullet \\ \bullet \\ \bullet \end{array}, \begin{array}{c} \bullet \\ \bullet \\ \bullet \\ \bullet \\ \bullet \end{array} ) \\ w \quad w'$$

$$C = \frac{(w - \bar{w})(w' - \bar{w}')}{\|(w - \bar{w})\| \|(w' - \bar{w}')\|}$$

$$\bar{w} = \text{mean}(w)$$

$$\bar{w}' = \text{mean}(w')$$

If  $C > \lambda = \text{threshold} \rightarrow \text{voxel consistent}$

# Experimental Results



Dinosaur



72 k voxels colored  
7.6 M voxels tested  
7 min to compute on a 250MHz



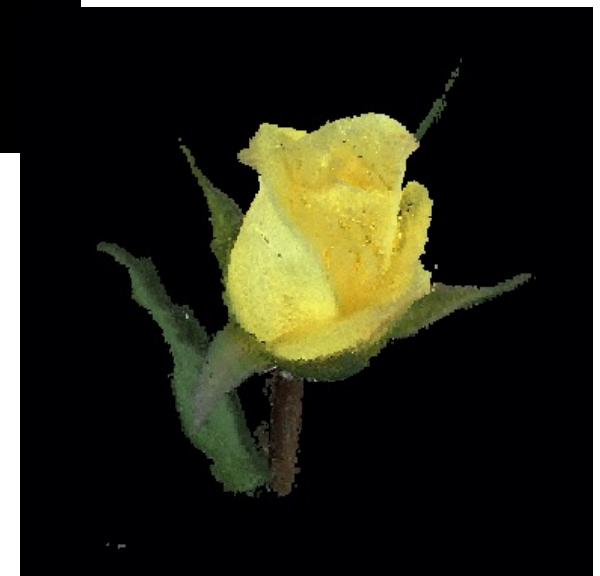
# Experimental Results



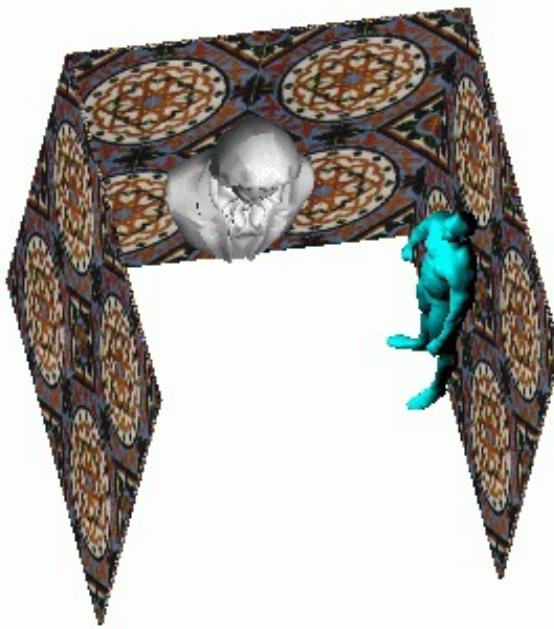
Flower



70 k voxels colored  
7.6 M voxels tested  
7 min to compute on a 250MHz



# Experimental Results



Room + weird people

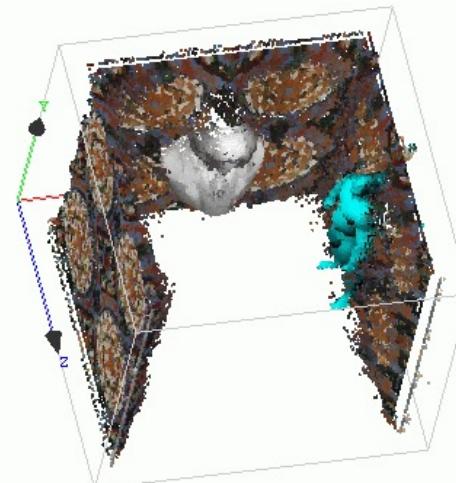
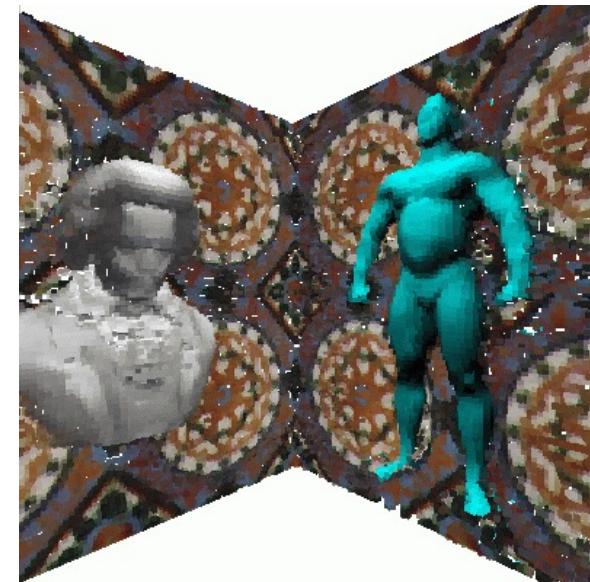


Image source: <http://www.cs.cmu.edu/~seitz/vcolor.html>

# Voxel Coloring: Conclusions

- Good things
  - Model intrinsic scene colors and texture
  - No assumptions on scene topology
- Limitations:
  - Constrained camera positions
  - Lambertian assumption

# Further Contributions

- A Theory of Space carving [Kutulakos & Seitz '99]
  - Voxel coloring in more general framework
  - No restrictions on camera position
- Probabilistic Space carving
  - [Broadhurst & Cipolla, ICCV 2001]
  - [Bhotika, Kutulakos et. al, ECCV 2002]
- CNN & voxel coloring
  - Incorporate reprojection error in the loss function for estimating object shape

Next lecture...

Fitting and Matching