January 2005

6677 Mechanics M1

Mark Scheme

Question Number	Scheme	Marks
1	3 \longrightarrow 4 1.5 kg \longrightarrow 2.5 kg 2.5 \longrightarrow \bigvee (a) CLM: $1.5 \times 3 - 2.5 \times 4 = -1.5 \times 2.5 + 2.5 \times \bigvee$ $\Rightarrow \bigvee = -0.7 \text{ m s}^{-1} \text{ so speed} = 0.7 \text{ m s}^{-1}$ (b) Direction of Q unchanged	M1 A1 A1 (3) A1√ (1)
	(c) Impulse = 1.5 (3 + 2.5) = 8.25, Ns	M1 A1, B1 (3)

Question Number		Scheme	Marks
2	τ † _	37	
		40g 20g	
	(a)	$R(\uparrow)$: $T + 3T = 40g + 20g$	M1
		T = 15g, so tension at C is $45g$ or 441 N or 440 N	A1 (2)
	(b)	M(B) 15g x 3 + 45g x d = 40g x 1.5	M1 A2,1,0√ ↓
		Solve: $d = \frac{1/3 \text{ or } 0.33 \text{ or } 0.333 \text{ m}}{}$	M1 A1 (5)

Question Number		Scheme	Marks
3	(a)	Distance = $\frac{1}{2}$ x 4 x 9 + 16 x 9 or $\frac{1}{2}$ (20 + 16) x 9	M1
		= <u>162 m</u>	A1 (2)
	(b)	Distance over last 5 s = $\frac{1}{2}(9 + u) \times 5$	M1
		$162 + \frac{1}{2}(9 + u) \times 5 = 200$	M1 A1√
		$\Rightarrow u = 6.2 \text{ m s}^{-1}$	A1 (4)
	(c)	6.2 = 9 + 5a	M1 A1√
		$a = (-) 0.56 \text{ m s}^{-2}$	A1 (3)

Question Number		Scheme	Marks
4	R 🔪		
,	2.5g (a)	$R = 2.5g\cos 20$	M1
	· · · · ·	$\approx 23.0 \text{ or } 23 \text{ N}$	A1 (2)
	(b)	$X = 0.4 \times 23.0 + 2.5g \sin 20$	M1 A2,1,0√
	() 5	≈ 17.6 or 18 N	A1 (4)
	(c) R F	In equlib. $F = 2.5g \sin 20 \approx 8.38 \text{ or } 8.4 \text{ N}$	B1
	↓ 2.5g	μ R = 0.4 x 2.5 g cos 20 \approx 9.21 or 9.2 N	B1
		8.4 < 9.2 (using ' $F < \mu R$ ' not F	= <i>μR</i>) M1
		Since $F < \mu R$ remains in equilibrium	(cso) A1 (4)

Question Number		Scheme	Marks
5	(a) 's = $ut + \frac{1}{2}at^2$ ' for B	$0.4 = \frac{1}{2} a(0.5)^2$	M1 A1
		$a = 3.2 \text{ m s}^{-2}$	A1 (3)
	(b) N2L for <i>B</i> :	$0.8g - T = 0.8 \times 3.2$	M1 A1√ ↓
		T = 5.28 or 5.3 N	M1 A1 (4)
	(c) A:	$F = \mu \times 0.5g$	B1
	N2L for A:	T - F = 0.5a	M1 A1 ↓
	Sub and solve	$\mu = 0.75 \text{ or } 0.751$	M1 A1 (5)
	(d) Same acceleration	on for A and B.	B1 (1)

Question Number		Scheme	Marks
6	(a)	$16^2 = 20^2 - 2 \times a \times 24 \implies a = 3 \text{ m s}^{-2}$	M1 A1 (2)
	(b)	$v^2 = 20^2 - 2 \times 3 \times 30$	M1 A1√
		$v = \sqrt{220 \text{ or } 14.8 \text{ m s}^{-1}}$	A1 (3)
	(c)	$0.3 = m \times 3 \implies m = 0.1 \text{ kg} (*)$	M1 A1 (2)
	(d)	$0.1(w + \sqrt{220}) = 2.4$	M1 A1√
		w = 9.17	A1 ↓
		$0 = 9,17 - 3 \times t$	M1 A1√
		$t \approx 3.06 \text{ s}$	A1 (6)

Question Number		Scheme	Marks
7	(a)	$\mathbf{v}_P = \{(29\mathbf{i} + 34\mathbf{j}) - (20\mathbf{i} + 10\mathbf{j})\}/3 = (3\mathbf{i} + 8\mathbf{j}) \text{ km h}^{-1}$	M1 A1 (2)
	(b)	p = (20i + 10j) + (3i + 8j)t	M1 A1√
		q = (14i - 6j) + 12tj	M1 A1 (4)
	(c)	$\mathbf{q} - \mathbf{p} = (-6 - 3t)\mathbf{i} + (-16 + 4t)\mathbf{j}$	M1 A1
		$d^2 = (-6 - 3t)^2 + (-16 + 4t)^2$	↓ M1
		$= 36 + 36t + 9t^2 + 16t^2 - 128t + 256$	↓ M1
		$= 25t^2 - 92t + 292 \tag{*}$	A1 (cso) (5)
	(d)	$25t^2 - 92t + 292 = 225$	M1
		$25t^2 - 92t + 67 = 0$	A1 ↓
		(t-1)(25t-67) = 0	M1
		t = 67/25 or 2.68	A1
		time $\approx~161$ mins, or 2 hrs 41 mins, or 2.41 am, or 0241	A1 (5)