EDEXCEL MECHANICS M2 (6678) – JUNE 2002

PROVISIONAL MARK SCHEME

Question Number		Scheme	Marks	3
1.	(a)	Differentiating: $\mathbf{a} = 3\mathbf{i} - 5\mathbf{j}$ (sufficient)	M1A1	(2)
	(<i>b</i>)	Integrating: $\mathbf{r} = (\frac{3}{2}t^2 - 2t)\mathbf{i} - \frac{5}{2}t^2\mathbf{j} \ (+C)$	M1A1	
		Using initial conditions to find C (3i); $\mathbf{r}(t=2) = 5 \mathbf{i} - 10 \mathbf{j}$	M1; A1	
		Distance = $\sqrt{\{5^2 + (10)^2\}}$; = $5\sqrt{5}$ or 11.2 or 11.18 (m)	M1; A1	6)
			(6 ma	rks)
2.	(a)	$0 \le t \le 3$ $v = 2t^2 - \frac{1}{3}t^3 (+C)$ Evidence of integration for M1	M1 A1	
		$t = 3 \implies v = 9 \text{ m s}^{-1}$	A1	(3)
	(<i>b</i>)	$t \ge 3 \qquad \qquad v = -\frac{27}{t} \ \ (+C)$	B1	
		Using $t = 3$ and candidates' $v = 9$ to find C ; $C = 18$	M1; A1 ft	
		Substituting $t = 6$ in expression for v ; $v = 13.5$ m s ⁻¹	M1; A1	(5)
			(8 ma	rks)
3.	(a)	Change in KE: $\frac{1}{2} \times 80 \times (8^2 - 5^2)$ [loss: 2560 – 1000 = 1560 J]	B1	
		Change in PE: $80 \times g \times (20 - 12)$ [loss: $15680 - 9408 = 6272 \text{ J}$]	B1	
		WD by cyclist = 20×500 – (loss in K.E. + P.E.)	M1 A1 ft	
		= 2168 Nm (allow 2170 and 2200)	A1	(5)
	(<i>b</i>)	Equation of motion: $F - 20 = 80 \times 0.5$ [M1 requires three terms]	M1 A1	
		Power = $F_c \times 5$; = 300 W	M1 A1	
			(9 ma	rks)

(ft = follow through mark)

Question Number		Scheme	Marks
4.	(a)	Shape Square Semi-circle Lamina L Relative masses 100 $12\frac{1}{2}\pi(39.3)$ $100 - 12\frac{1}{2}\pi(60.7)$	M1 A1
		Centre of mass from AB $\frac{20}{3\pi}$ (2.12) $\frac{\pi}{x}$	B1 B1
		Moments about AB: $100 \times 5 - 12\frac{1}{2}\pi \times \frac{20}{3\pi} = (100 - 12\frac{1}{2}\pi)^{-\frac{1}{2}}$	M1 A1
		Answer: 6.86 cm	A1 (cao) (7)
	(b)	D_{θ} Correct angle, diagram sufficient	M1
		Method to find θ [or $(90 - \theta)$] $10 - \bar{x} \qquad C$ $\tan \theta = \frac{10 - \bar{x}_c}{10 - \theta}$	M1
		$ \int 10 - \bar{x} \qquad C \qquad \tan \theta = \frac{10 - \bar{x}_c}{5} $	A1 ft
		Answer: 32.1°	A1 (cao) (4)
			(11 marks)
5.	(a)	$x = u \cos \alpha t$; $y = u \sin \alpha t - \frac{1}{2}gt^2$	B1; B1
		Eliminating t : $y = u \sin \alpha \frac{x}{u \cos \alpha} - \frac{1}{2} g \frac{x^2}{(u \cos \alpha)^2}$	M1
		$y = x \tan \alpha - \frac{gx^2}{2u^2 \cos^2 \theta}$	M1
		$y = x \tan \alpha - \frac{gx^2}{2u^2} (1 + \tan^2 \alpha) *$	A1 (5)
	(b)	$-2 = x \tan 45^{\circ} - \frac{9.8 \times x^{2}}{2 \times 14^{2}} (1 + \tan^{2} 45^{\circ})$	M1 A1
		Simplifying "correctly" to quadratic of form $ax^2 + bx + c = 0$ (may be implied, e.g. $x^2 - 20x - 40 = 0$; $-0.05x^2 + x + 2 = 0$; $4.9x^2 - 98x - 196 = 0$	M1
		Solving for t (2.205 s), $x = 14 \cos 45^{\circ} t$, $x = 21.8 \text{ m}$	M1 A1 (5)
	(c)	$21.8_{c} = 14 \cos 45^{\circ} t \; ; \; t = 2.2 \text{ s}$	M1 A1 (cao) (2)
			(12 marks)

(ft = follow through mark; cao = correct answer only; cso = correct solution only; * indicates answer is given on the examination paper)

PROVISIONAL MARK SCHEME

Question Number	Scheme	Marks
6. (a)	CoM: $mu = -mv_1 + 3 mv_2$ $\Rightarrow u = 0$ $\Rightarrow u = -v_1 + 3 v_2$ $\Rightarrow u = -v_1 + 3 v_2$ $\Rightarrow u = v_2 + v_1$ Solving: $v_1 = \frac{1}{4}(3e - 1)u$ $v_2 = \frac{1}{4}(1 + e)u$ Speed of B after hitting wall $= \pm \frac{3}{16}(1 + e)u$ (v_2^*) For second collision $v_2^* > v_1$; $\frac{3}{16}(1 + e)u > \frac{1}{4}(3e - 1)u$ Solving, $e < \frac{7}{9}$ Finding lower bound using $v_1 > 0$; $e > \frac{1}{3}$	M1 A1 M1 A1 M1 A1 A1 (7) B1 ft M1 M1 A1 M1 A1
	Complete range: $\frac{1}{3} < e < \frac{7}{9}$	A1 (cso) (6)
		(13 marks)
7. (a)	F = 0.6R (seen anywhere)	M1
	Moments about B: $R \times 2a \cos \alpha + F \times 2a \sin \alpha = W \times a \cos \alpha$ Using $\cos \alpha = \frac{12}{13}$ and $\sin \alpha = \frac{5}{13}$ Solving for R	M1 A1
	$\frac{24}{13}R + \frac{6}{13}R = \frac{12}{13} W \Rightarrow 30R = 12$	M1
	$\Rightarrow R = \frac{2}{5} W^*$	A1 (6)
(b	Resolve \leftrightarrow : $T \cos \beta = F$; $= 0.6 R = \frac{6}{25} W$	M1 A1
	Resolve \updownarrow : $T \sin \beta + R = W$ $T \sin \beta = \frac{3}{5} W$	M1 A1
	Complete method for β [e.g tan $\beta = 2.5$]; $\beta = 68.2^{\circ}$	M1; A1 (6)
	Complete method for T: substitute for β or $\sqrt{\{(0.6 \text{ W})^2 + (0.24 \text{ W})^2\}}$	M1
	$T = 0.646W \implies k = 0.65 \text{ or } 0.646$	A1 (2)
		(14 marks)