Centre No.					Pape	r Refer	ence			Surname	Initial(s)
Candidate No.			6	6	6	5	/	0	1	Signature	

Paper Reference(s

6665/01

Edexcel GCE

Core Mathematics C3 Advanced Level

Monday 23 January 2006 – Afternoon

Time: 1 hour 30 minutes

Materials	reg	uired	for	exam	ination

Mathematical Formulae (Green)

Items included with question papers

Nil

Candidates may use any calculator EXCEPT those with the facility for symbolic algebra, differentiation and/or integration. Thus candidates may NOT use calculators such as the Texas Instruments TI 89, TI 92, Casio CFX 9970G, Hewlett Packard HP 48G.

Instructions to Candidates

In the boxes above, write your centre number, candidate number, your surname, initial(s) and signature.

Check that you have the correct question paper.

You must write your answer for each question in the space following the question.

When a calculator is used, the answer should be given to an appropriate degree of accuracy.

Information for Candidates

A booklet 'Mathematical Formulae and Statistical Tables' is provided.

Full marks may be obtained for answers to ALL questions.

The marks for individual questions and the parts of questions are shown in round brackets: e.g. (2).

There are 8 questions in this question paper. The total mark for this paper is 75.

There are 20 pages in this question paper. Any blank pages are indicated.

Advice to Candidates

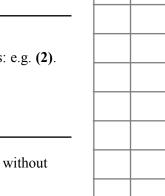
You must ensure that your answers to parts of questions are clearly labelled.

You must show sufficient working to make your methods clear to the examiner. Answers without working may gain no credit.

This publication may be reproduced only in accordance with Edexcel Limited copyright policy. ©2006 Edexcel Limited.

 $\begin{array}{c} {\rm Printer's\ Log,\ No.} \\ N23495A \\ {\rm W850/R6665/57570} \\ \end{array} \\ {\rm 7/7/3/3/3/3/3} \end{array}$





Examiner's use only

Team Leader's use only

2

3

4

5

6

8

Turn over



1.



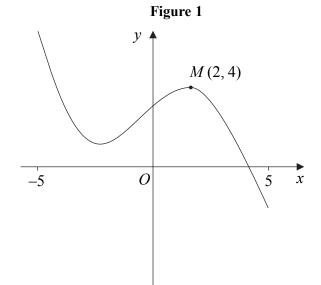


Figure 1 shows the graph of y = f(x), $-5 \le x \le 5$. The point M(2, 4) is the maximum turning point of the graph.

Sketch, on separate diagrams, the graphs of

(a)
$$y = f(x) + 3$$
,

(2)

(b)
$$y = |f(x)|$$
,

(2)

(c)
$$y = f(|x|)$$
.

(3)

Show on each graph the coordinates of any maximum turning points.

		Leave blank
Question 1 continued		
		Q1
	(Total 7 marks)	

		L
2. I	Express	
	$\frac{2x^2+3x}{(2x+3)(x-2)} - \frac{6}{x^2-x-2}$	
а	as a single fraction in its simplest form. (7)	
_		

Question 2 continued	I
destion 2 continued	
	 Q

•	The point P lies on the curve with equation $y = \ln\left(\frac{1}{3}x\right)$. The x-coordinate of P is 3.
	Find an equation of the normal to the curve at the point P in the form $y = ax + b$, where a and b are constants.
	(5)
_	
_	
_	

	l l
uestion 3 continued	
	_
	_
	_
	_
	_
	_
	_
	_
	_
	_
	_
	_
	_
	_
	_
	_
	_
	Q

		Leav
4.	(a) Differentiate with respect to x	blan
т.		
	(i) x^2e^{3x+2} ,	
	(4)	
	(ii) $\frac{\cos(2x^3)}{2}$.	
	$(11) \frac{3x}{3x}.$	
	(b) Given that $x = 4 \sin(2y + 6)$, find $\frac{dy}{dx}$ in terms of x.	
	(5)	
_		
_		
_		
_		
_		
_		
_		
_		
_		
_		
_		
_		
_		
_		
_		
_		
_		
_		
_		
_		
_		
_		
_		

	Leave blank
Question 4 continued	
	Q4
(Total 13 marks)	

5.

$$f(x) = 2x^3 - x - 4.$$

(a) Show that the equation f(x) = 0 can be written as

$$x = \sqrt{\left(\frac{2}{x} + \frac{1}{2}\right)}.$$

(3)

Leave blank

The equation $2x^3 - x - 4 = 0$ has a root between 1.35 and 1.4.

(b) Use the iteration formula

$$x_{n+1} = \sqrt{\left(\frac{2}{x_n} + \frac{1}{2}\right)},$$

with $x_0 = 1.35$, to find, to 2 decimal places, the values of x_1 , x_2 and x_3 .

(3)

The only real root of f(x) = 0 is α .

(c) By choosing a suitable interval, prove that $\alpha = 1.392$, to 3 decimal places.

(3)

Question 5 continued	Leav blan
	Q5
(Total 9 marks)	

•	$f(x) = 12\cos x - 4\sin x.$	
(Given that $f(x) = R \cos(x + \alpha)$, where $R \ge 0$ and $0 \le \alpha \le 90^{\circ}$,	
((a) find the value of R and the value of α .	(4)
	(b) Hence solve the equation	
	$12\cos x - 4\sin x = 7$	
	for $0 \le x < 360^{\circ}$, giving your answers to one decimal place.	(5)
	(c) (i) Write down the minimum value of $12 \cos x - 4 \sin x$.	(1)
	(ii) Find, to 2 decimal places, the smallest positive value of x for which minimum value occurs.	
		(2)

	Leav blan
Question 6 continued	
	Q
(Total 12 marks)	

Leave blank

- 7. (a) Show that
 - (i) $\frac{\cos 2x}{\cos x + \sin x} \equiv \cos x \sin x, \quad x \neq (n \frac{1}{4})\pi, n \in \mathbb{Z},$

(2)

(ii) $\frac{1}{2}(\cos 2x - \sin 2x) \equiv \cos^2 x - \cos x \sin x - \frac{1}{2}$.

(3)

(b) Hence, or otherwise, show that the equation

$$\cos\theta \left(\frac{\cos 2\theta}{\cos\theta + \sin\theta}\right) = \frac{1}{2}$$

can be written as

$$\sin 2\theta = \cos 2\theta$$
.

(3)

(c) Solve, for $0 \le \theta \le 2\pi$,

$$\sin 2\theta = \cos 2\theta,$$

giving your answers in terms of π .

(4)

Question 7 continued	eave lank



		Leave blank
Question 7 continued		
	_	
	-	
	-	
	_	
	_	
	_	
	_	
	_	
	_	
	_	
	_	
	-	
	-	
	-	
	_	
	_	
	_	
	_	
	_	
	_	
	_	
	_	
	_	
	_	
	-	
	-	
	-	
	-	Q 7
	-	
(Total 12 mark	s) [

Leave

1 N6	e functions f and g are de	enned by			
		$f: x \to 2x + \ln 2$	$x \in \mathbb{R}$		
		$g: x \to e^{2x}$,	$x \in \mathbb{R}$.		
(a)	Prove that the composit	te function gf is			
		$gf: x \to 4e^{4x},$	$x \in \mathbb{R}$.		(4)
(b)	In the space provided o				nd show
	the coordinates of the p	ooint where the cu	irve cuts the y-ax	118.	(1)
(c)	Write down the range of	of gf.			
		d			(1)
(d)	Find the value of x for figures.	r which $\frac{d}{dx}[gf(x)]$	[c)]=3, giving yo	our answer to 3 sig	nificant
	figures.				(4)

	Leave blank
	blank
Question 8 continued	
Question & continued	



(Tota	al 10 marks)