PROVISIONAL MARK SCHEME JANUARY 2003

Question Number		Scheme		Mark	Marks	
1.	inoci	$T_1 \uparrow \uparrow T_2$ $5g$	$T_1 = \frac{175 \times 0.2}{1}$ $175 \times 0.2 \qquad \lambda \times 0.3$	B1		
		↓ 5 <i>g</i>	$\frac{175 \times 0.2}{1} + \frac{\lambda \times 0.3}{0.9} = 49$	M1 A 1		
			$\Rightarrow \lambda = 42$	M1 A1	(5)	
				(5 m	narks)	
2.	(a)	<u> </u>	3, 4, 5 Δ	B1		
		Al $ Sl $	$R(\uparrow) T \sin \theta = mg$	M1		
		T m_2	$T = \frac{5mg}{4}$	A1	(3)	
	(b)	,	s $\theta = \frac{mv^2}{3l}$	M1 A2		
		$\frac{8}{5}$ ×	$\frac{5mg}{4} = \frac{mv^2}{3l}$	M1		
		v =	$\sqrt{6gl}$	A1	(5)	
	(c)	Could not assume tension	s same	B1	(1)	
				(9 m	narks)	
3.	(a)	Cylinder	half-sphere toy			
		$\pi r^2 h ho$	$\frac{2}{3}\pi r^36\rho \qquad \pi r^2h\rho + \frac{2}{3}\pi r^36\rho$	M1 A1		
		$\frac{h}{2} + r$	$\frac{5r}{8}$ d	B1 B1		
		$\pi^2 h \rho(\frac{h}{2} + r) +$	$4\pi r^3 \rho \frac{5r}{8} = (\pi r^2 h \rho + 4\pi r^3 \rho)d$	M1 A1		
			$\Rightarrow d = \frac{h^2 + 2rh + 5r^2}{2(h+4r)} \tag{*}$	A1	(7)	
	(<i>b</i>)	$d=r, \implies h^2+2r$	$rh + 5r^2 = 2r(h + 4r)$	M1, M1		
			$h = \sqrt{3}r$	A1	(3)	
				(10 m	narks)	

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4.	(a)	$\frac{2\pi}{\omega} = \pi \Rightarrow = 2$	В1		
		$2.4^2 = 4 (a^2 - 0.5^2)$	M1 A1ft	M1 A1ft	
		a = 1.3 m	A1 ((4)	
	(<i>b</i>)	$v_{\text{max}} = a\omega = 2.6 \text{ m s}^{-1}$	B1 ((1)	
(c)		$\arctan = a \omega^2 = 5.2 \text{ m s}^{-2}$	B1ft ((1)	
	(<i>d</i>)	$0.5 = 1.3 \sin 2t$	M1		
		$t = \frac{1}{2} \sin^{-1} \left(\frac{0.5}{1.3} \right)$	M1 A1		
		Total time = $4t = 0.79 (2 \text{ dp})$	M1 A1 ((5)	
			(11 marks)		
5.	(a)	$800 \frac{dv}{dt} = \frac{48000}{(t+2)^2}$	M1		
		$v = 60 \int \frac{\mathrm{d}t}{(t+2)^2} = \frac{-60}{(t+2)} (+c)$	M1 A1		
		$t = 0, v = 0 \Rightarrow c = 30$	M1 A1		
		$v = 30 - \frac{60}{(t+2)} \Rightarrow v \rightarrow 30 \text{ as } t \rightarrow \infty$	A1 ((6)	
	(<i>b</i>)	$s = \int v dt = 30t - 60 \ln(t+2) \ (+c)$	M1 A1		
		substitute in $t = 0$ and $t = 6$	M1		
		$s = 180 - 60 \ln 8,60 \ln 2$	A1, A1		
		≈ 96.8 m	A1 ((6)	
			(12 marks))	

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6.	(a)	$\frac{1}{2} \times \frac{58.8}{4} x^2 = 0.5 \times 9.8 (x+4)$	M1 A1 A1		
		$3x^2 - 2x - 8 = 0$		M1 A1	
		(3x+4)(x-2)=0, x=2			
		Distance fallen = 6 m	M1 A1	(7)	
	(b)	$\frac{1}{2} \times 0.5v^2 = \frac{1}{2} \times \frac{58.8}{4} \times 3^2 - 0.5 \times 9.8 \times 3$	M1 A1 A1		
		$v = 14.3 \text{ m s}^{-1}$	M1 A1	(5)	
			(12 marks)		
7.	(a)	$\frac{1}{2}mu^2 - \frac{1}{2}mv^2 = mga (1 + \cos 60^\circ)$	M1 A1		
		$v^2 = u^2 - 3ga$	A1	(3)	
	(b)	$R + mg\cos 60^\circ = \frac{mv^2}{a}$			
		$R = \frac{m}{a} \left(6ga - 3ga \right) - \frac{mg}{2}$			
		$=\frac{5mg}{2}$	A1	(3)	
	(c)	$R = 0$ at $B \Rightarrow \frac{mg}{2} = \frac{mv^2}{a} \Rightarrow v^2 = \frac{1}{2}ag$			
		$\Rightarrow u^2 = \frac{7ga}{2} \implies u = \sqrt{\frac{7ga}{2}}$	M1 A1	(3)	
	(<i>d</i>)	$(\rightarrow) B \text{ to } C: v \cos 60^{\circ} \times t = a\sqrt{3}$	M1 A1		
		$t = \frac{2a\sqrt{3}}{a}$			
		C $\frac{v}{a^{\frac{\sqrt{3}}{2}} + a^{\frac{\sqrt{3}}{2}}}$ $a^{\frac{\sqrt{3}}{2}}$ $a^{\frac{\sqrt{3}}{2}}$ $a^{\frac{\sqrt{3}}{2}}$ $a^{\frac{\sqrt{3}}{2}}$ $a^{\frac{\sqrt{3}}{2}}$ $a^{\frac{\sqrt{3}}{2}}$ $a^{\frac{\sqrt{3}}{2}}$ $a^{\frac{\sqrt{3}}{2}}$	M1 A1		
		$\Rightarrow t = \frac{2v\sin 60^{\circ}}{g} = \frac{v\sqrt{3}}{g}$			
		$\therefore \frac{2a\sqrt{3}}{v} = \frac{v\sqrt{3}}{g} \Rightarrow v^2 = 2ga$	M1 A1		
		$\Rightarrow u^2 = 5ga$			
		$\Rightarrow u = \sqrt{5ga}$	A1	(7)	
			(16 ma	rks)	