

**EDEXCEL FOUNDATION**  
Stewart House 32 Russell Square London WC1B 5DN

**January 2004**

**Advanced Subsidiary / Advanced Level  
General Certificate of Education**

**SUBJECT: STATISTICS 6684**

**PAPER NO: S2**

Question number	Scheme	Marks
<b>1.</b>		
<b>(a)</b>	List of patients registered with the practice. Require 'list' or 'register' or database or similar	<b>B1</b>
<b>(b)</b>	The patient(s)	<b>B1</b>
<b>(c)</b>	Adv: Quicker, cheaper, easier, used when testing results in destruction of item, quality of info about each sampling unit is often better. Any one Disadv: Uncertainty due to natural variation, uncertainty due to bias, possible bias as sampling frame incomplete, bias due to subjective choice of sample, bias due to non-response. Any one	<b>B1</b> <b>B1</b>
<b>(d)</b>	Non-response due to patients registered with the practice but who have left the area	<b>B1</b>
		<b>(Total 5 Marks)</b>
<b>2(a)</b>	$P(R \geq 4) = 1 - P(R \leq 3) = 0.6533$ Require 1 minus and correct inequality	<b>M1A1</b>
<b>(b)</b>	$P(S \leq 1) = P(S = 0) + P(S = 1), = e^{-2.71} + 2.71e^{-2.71}, = 0.2469$ awrt 0.247	<b>M1,A1,A1</b>
<b>(c)</b>	$P(T \leq 18) = P(Z \leq \frac{18-25}{5}), = P(Z \leq -1.4) = 0.0808$ 4 dp, cc no marks	<b>M1,A1</b>
		<b>(Total 7 Marks)</b>
<b>3(a)</b>	$p = \frac{1}{2}$	<b>B1</b>
<b>(b)</b>	Binomial distribution is symmetrical	<b>B1</b>
<b>(c)</b>	Since $n$ is large and $p \approx 0.5$ then use normal approximation, $np = 96$ and $npq = 49.92$ $P(90 \leq X < 105) \approx P(89.5 \leq Y \leq 104.5)$ where $Y \sim N(96, 49.92)$ $\pm 0.5$ cc on both $\approx P\left(\frac{89.5-96}{\sqrt{49.92}} \leq Z \leq \frac{104.5-96}{\sqrt{49.92}}\right)$ Standardisation of both $\approx P(-0.92 \leq Z \leq 1.20)$ awrt -0.92 & 1.20 $\approx 0.7055-0.7070$ 4dp in range	<b>M1</b> <b>A1A1</b> <b>M1,</b> <b>M1</b> <b>A1</b> <b>A1</b>
		<b>(Total 9 Marks)</b>

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<b>4</b>		
<b>(a)</b>	$n$ large, $p$ small	<b>B1,B1</b> (2)
<b>(b)</b>	Let $X$ represent the number of people catching the virus, $X \sim B\left(12, \frac{1}{150}\right)$ $P(X = 2) = C_2^{12} \left(\frac{1}{150}\right)^2 \left(\frac{149}{150}\right)^{10} = 0.0027$ Use of Bin including $C_2^{12}$ , 0.0027(4) only	Implied <b>B1</b> <b>M1A1,A1</b> (4)
<b>(c)</b>	$X \sim \text{Po}(np) = \text{Po}(8)$ $P(X < 7) = P(X \leq 6) = 0.3134$	Poisson, 8 <b>B1,B1</b> $X \leq 6$ for method, 0.3134 <b>M1A1</b> (4)
		<b>(Total 10 Marks)</b>
<b>5(a)</b>	Vehicles pass at random / one at a time / independently / at a constant rate	Any 2&context <b>B1B1dep</b> (2)
<b>(b)</b>	$X$ is the number of vehicles passing in a 10 minute interval, $X \sim \text{Po}\left(\frac{51}{60} \times 10\right) = \text{Po}(8.5)$ $P(X=6) = \frac{8.5^6 e^{-8.5}}{6!} = 0.1066$ (or $0.2562 - 0.1496 = 0.1066$ ) Clear attempt using 6, 4dp	Implied <b>Po(8.5) B1</b> <b>M1A1</b> (3)
<b>(c)</b>	$P(X \geq 9) = 1 - P(X \leq 8) = 0.4769$	Require 1 minus and correct inequality <b>M1A1</b> (2)
<b>(d)</b>	$H_0 : \lambda = 8.5, H_1 : \lambda < 8.5$ $P(X \leq 4   \lambda = 8.5) = 0.0744, > 0.05$ ( Or $P(X \leq 3   \lambda = 8.5) = 0.0301, < 0.05$ so CR $X \leq 3$ correct CR Insufficient evidence to reject $H_0$ , so no evidence to suggest number of vehicles has decreased.	One tailed test only for alt hyp <b>B1f,B1f</b> $X \leq 4$ for method, 0.0744 <b>M1,A1</b> <b>M1,A1</b> 'Accept' <b>M1</b> Context <b>A1f</b> (6)
		<b>(Total 13 Marks)</b>

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<b>6</b>		
<b>(a)</b>	Let $X$ represent the number of plant pots with defects, $X \sim B(25, 0.20)$ $P(X \leq 1) = 0.0274, P(X \geq 10) = 0.0173$ Critical region is $X \leq 1, X \geq 10$	Implied <b>B1</b> Clear attempt at both tails required, 4dp <b>M1A1A1</b> <b>A1</b> <b>(5)</b>
<b>(b)</b>	Significance level = $0.0274 + 0.0173 = 0.0447$	Accept % 4dp <b>B1</b> cao <b>(1)</b>
<b>(c)</b>	$H_0 : \lambda = 10, H_1 : \lambda > 10$ (or $H_0 : \lambda = 60, H_1 : \lambda > 60$ ) Let $Y$ represent the number sold in 6 weeks, under $H_0, Y \sim \text{Po}(60)$ $P(Y \geq 74) \approx P(W > 73.5)$ where $W \sim N(60, 60)$ $\approx P(Z \geq \frac{73.5 - 60}{\sqrt{60}}) = P(Z > 1.74) = 0.0407 - 0.0409 < 0.05$ Evidence that rate of sales per week has increased.	$\pm 0.5$ for cc, 73.5 <b>M1A1</b> Standardise using $60\sqrt{60}$ <b>M1, A1</b> <b>A1f</b> <b>(7)</b> <b>(Total 13 Marks)</b>

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7		
(a)	$\int_0^4 kx(5-x)dx = 1$ $k \left[ \frac{5x^2}{2} - \frac{x^3}{3} \right]_0^4 = 1$ <p>Sub in limits and solve to give **** <math>k = \frac{3}{56}</math> ****</p>	<p>Limits required <b>M1</b></p> <p><math>\left[ \frac{5x^2}{2} - \frac{x^3}{3} \right]</math> <b>A1</b></p> <p>Correct solution <b>A1</b></p> <p style="text-align: right;"><b>(3)</b></p>
(b)	$F(x) = \int_0^{x_0} f(x)dx = \int_0^{x_0} \frac{3}{56}x(5-x)dx = \frac{3}{56} \left[ \frac{5x^2}{2} - \frac{x^3}{3} \right]_0^{x_0}$ $= \frac{x_0^2}{112}(15-2x_0)$ <p style="text-align: center;">0 <math>x &lt; 0</math></p> <p style="text-align: center;"><math>F(x) = \frac{x^2}{112}(15-2x)</math> <math>0 \leq x \leq 4</math></p> <p style="text-align: center;">1 <math>x &gt; 4</math></p>	<p>Variable upper limit required <b>M1</b></p> <p><b>A1</b></p> <p>Ends, middle. <b>B1, B1f</b></p> <p style="text-align: right;"><b>(4)</b></p>
(c)	$E(x) = \int_0^4 \frac{3}{56}x^2(5-x)dx = \frac{3}{56} \left[ \frac{5x^3}{3} - \frac{x^4}{4} \right]_0^4 = 2.29$ $\int xf(x)dx, \left[ \frac{5x^3}{3} - \frac{x^4}{4} \right], 3sf \left( 2\frac{2}{7} \right)$	<p><b>M1A1A1</b></p> <p style="text-align: right;"><b>(3)</b></p>
(d)	$f'(x) = \frac{3}{56}(5-2x) = 0 \Rightarrow \text{Mode} = 2.5$	<p>Attempt <math>f'(x)</math>, <math>(5-2x) = 0</math>, 2.5 <b>M1A1A1</b></p> <p>(Or Sketch <b>M1</b>, <math>x=0 \&amp; 5</math> <b>A1</b>, Mode=2.5 <b>A1</b>)</p> <p style="text-align: right;"><b>(3)</b></p>
(e)	$F(2.3) = 0.491$ , $F(2.5) = 0.558$ $F(m) = 0.5 \Rightarrow m$ lies between 2.3 and 2.5	<p>Their <math>F</math>, awrt 0.491 &amp; 0.558 or 0.984 &amp; -6.5 <b>M1, A1</b></p> <p>cso <b>A1</b></p> <p style="text-align: right;"><b>(3)</b></p>
(f)	<p>Mean (2.29) &lt; Median (2.3-2.5) &lt; Mode (2.5)</p> <p>Negative skew</p>	<p><b>B1</b></p> <p><b>B1 dep</b></p> <p style="text-align: right;"><b>(2)</b></p> <p style="text-align: right;"><b>(Total 18 Marks)</b></p>