

Question Number	Scheme	Marks
1.	<p>(a) Stratified</p> <p>(b) Label De-luxe rooms 1 – 20</p> <p>Using <i>random numbers</i> in range 1 – 20 select 2 <i>rooms</i></p> <p>Repeat for Premier using 1 – 40 and select 4 rooms</p> <p>Repeat for Standard using 1 – 100 and select 10 rooms</p>	<p>B1 (1)</p> <p>B1</p> <p>B1 B1</p> <p>B1 (4)</p> <p>(5 marks)</p>
2.	<p>(a) $H_0: \mu_A = \mu_B$ $H_1: \mu_A \neq \mu_B$</p> <p>standard error = $\sqrt{\frac{9.1^2}{100} + \frac{8.4^2}{120}} = 1.19$ (awrt)</p> <p>$\alpha = 0.01 \Rightarrow$ CR: $z < -2.5758$ or $z > 2.5758$</p> <p>$z = \frac{70.6 - 67.2}{1.19} = 2.86$ (awrt)</p> <p>Since 2.86 is in the critical range, H_0 is rejected. There is evidence of a difference in mean playing time.</p> <p>(b) Central Limit Theorem applies to enable normal distribution to be used.</p>	<p>B1 B1</p> <p>M1 A1</p> <p>B1 need both</p> <p>M1 A1</p> <p>A1ft (8)</p> <p>B1 (1)</p> <p>(9 marks)</p>
3.	<p>(a) $\bar{M} \sim N(80, \frac{2.6^2}{10})$ or $N(80, 0.676)$</p> <p>(b) $P(\bar{M} < 78.5) = P(z < \frac{78.5 - 80}{2.6/\sqrt{10}})$</p> <p>$= P(z < -1.82)$</p> <p>$= 0.0344$</p> <p>(c) Let W = weight of all 10 people</p> <p>$W = M_1 + \dots + M_6 + F_1 + \dots + F_4$</p> <p>$E(W) = (6 \times 80) + (4 \times 59) = 716$</p> <p>$\text{Var}(W) = (6 \times 2.6^2) + (4 \times 1.9^2) = 55$</p> <p>$P(W > 730) = P(z > \frac{730 - 716}{\sqrt{55}})$</p> <p>$= P(z > 1.89)$</p> <p>$= 0.0294$</p>	<p>B1 B1 (2)</p> <p>M1</p> <p>A1</p> <p>A1 (3)</p> <p>B1</p> <p>B1</p> <p>M1 A1</p> <p>A1 (5)</p> <p>(10 marks)</p>

awrt = “anything which rounds to...”

Question Number	Scheme											Marks	
4.	(a)		A	B	C	D	E	F	G	H	I	J	M1
		Performance	10	5	8	3	9	6	1	4	7	2	
		Dedication	7	6	3	5	9	10	4	2	8	1	
		$\Sigma d^2 = 70$											
		$r_s = 1 - \frac{6 \times 70}{10 \times 99} = 0.576$											M1 A1 (5)
	(b)	$H_0: \rho = 0; H_1: \rho \neq 0$											B1 B1
		$n = 10 \Rightarrow$ critical value = 0.5636											B1
		0.576 is in the critical region											M1
		Evidence of correlation between performance and dedication.											A1ft (5)
	(c)	Likely to be an element of judgement in grading.											B1 (1)
	Dedication unlikely to be normally distributed.											(11 marks)	
5.		Expected Frequency	Male:	50.98		27.85		39.17					M1 A1 A1
			Female:	57.02		31.15		48.83					
		H_0 : no association between gender and facility											B1
		H_1 : Association between gender and facility											B1
		$\Sigma \frac{(O - E)^2}{E} = \frac{(50.98 - 40)^2}{50.98} + \frac{(57.02 - 68)^2}{57.02} + \dots + \frac{(43.83 - 31)^2}{43.83}$											M1 A1
		$= 12.7$											A1
		$\alpha = 0.05, \nu = 2 \Rightarrow$ CR: $\chi^2 > \underline{5.991}$											<u>B1</u> <u>B1</u>
		Evidence of association between gender and facility											A1ft (11)
													(11 marks)

ft = follow through mark

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6.	<p>(a) $R = 43.76$; $S = 54.68$; $T = 43.76$ using tables (OR $R = 43.75$; $S = 54.69$; $T = 43.75$ using calculator)</p> <p>(b) H_0: Binomial model with $n = 8$, $p = 0.5$ is suitable H_1: Binomial model with $n = 8$, $p = 0.5$ is not suitable Amalgamation of data $\sum \frac{(O - E)^2}{E} = 5.69$ (awrt) $\alpha = 0.05$, $\nu = 6 \Rightarrow \text{CR: } \chi^2 > \underline{12.592}$ Since 5.69 is not in the critical region there is no evidence to reject H_0. The binomial model with $n = 8$ and $p = 0.5$ is a suitable model.</p> <p>(c) Apart from the expected values and $\sum \frac{(O - E)^2}{E}$ being different, the degrees of freedom would have been reduced by 1 ($\nu = 5$).</p>	<p>M1 A1; B1 B1 (4)</p> <p>B1 (both)</p> <p>M1</p> <p>M1 A1</p> <p><u>B1 B1</u></p> <p>A1ft (7)</p> <p>B1 (1)</p> <p>(12 marks)</p>
7.	<p>(a) Cooling by subtracting 500 for each observation gives Mean = $500 + \frac{22}{10} = 502.2$ Variance = $\frac{1}{9} \left\{ 288 - \frac{22^2}{10} \right\} = 26.622$</p> <p>(b) Limits are $502.2 \pm 1.6449 \times 5.0$ (493.98, 510.42) [accept (494, 510)]</p> <p>(c) 95 % confidence limits are $502.2 \pm 1.96 \times \frac{5.0}{\sqrt{10}}$ (499, 505)</p> <p>(d) $H_0: \mu = 500$ $H_1: \mu > 500$ $\alpha = 0.05 \Rightarrow \text{CR: } z > 2.3263$ $z = \frac{503.9 - 500}{5.0 / \sqrt{15}} = 1.47$ 1.47 is not in the critical region \Rightarrow no evidence to reject H_0; no evidence to suggest mean is greater than 500g</p>	<p>M1 A1</p> <p>M1 A1 A1 (5)</p> <p>M1</p> <p>A1 (2)</p> <p>M1 A1ft B1 (for 1.96)</p> <p>A1 A1 (5)</p> <p>B1 (both)</p> <p>B1</p> <p>M1 A1</p> <p>A1 ft (5)</p> <p>(17 marks)</p>