

Newton's Laws of Motion, Momentum and Impulse

Supplementary Questions

Part 1

$$\begin{aligned} 1. \quad p &= mv \\ &= 6.6 \times 10^{-26} \times 2.0 \times 10^7 \\ &= 1.32 \times 10^{-18} \text{ kg m/s} \end{aligned}$$

$$\begin{aligned} 2. \quad p &= mv \\ &= 9.11 \times 10^{-31} \times 7.5 \times 10^6 \\ &= 6.83 \times 10^{-24} \text{ kg m/s} \end{aligned}$$

$$3. \quad F = \frac{\Delta p}{\Delta t} ; \quad \Delta p = m(v-u)$$

$$\Delta p = 1400 \times (0 - 20) = (-) 28,000 \text{ kg m/s}$$

$$\therefore \Delta t = \frac{\Delta p}{F} = \frac{28,000}{480 \times 10^3} = \underline{\underline{0.0583 \text{ seconds}}}$$

$$4. \quad F = \frac{\Delta p}{\Delta t} ; \quad \Delta p = m(v-u)$$

$$\begin{aligned} \Delta p &= 3.4 \times 10^{-6} \times (0 - 0.1) \\ &= (-) 3.4 \times 10^{-7} \text{ kg m/s} \end{aligned}$$

$$F = \frac{\Delta p}{\Delta t} = \frac{3.4 \times 10^{-7}}{2.2 \times 10^{-3}}$$

$$\therefore F = \underline{\underline{1.55 \times 10^{-4} \text{ N}}}$$

$$5. \quad F = \frac{\Delta p}{\Delta t} ; \quad \Delta p = m(v-u)$$

$$\begin{aligned} \Delta p &= 50 \times 10^{-3} \times (40 - 0) \\ &= 2 \text{ kg m/s} \end{aligned}$$

$$F = \frac{\Delta p}{\Delta t} = \frac{2}{3 \times 10^{-3}}$$

$$\therefore F = \underline{\underline{667 \text{ N}}}$$

$$6. \quad F = \frac{\Delta p}{\Delta t} = \frac{m \Delta v}{\Delta t}$$

$$F = \frac{m}{\Delta t} \cdot \Delta v$$
$$= 900 \times 40 \times 10^3$$

$$\therefore F = 3.6 \times 10^7 \text{ N}$$

$$7. \text{ i) } \Delta p = m(v-u)$$

$$\Delta p \text{ per second} = 75 \times 550$$

$$= \underline{\underline{41250 \text{ kg m/s}^2}}$$

$$\text{ii) } F = \Delta p / \Delta t$$

$$= \underline{\underline{41250 \text{ N}}}$$

$$\text{iii) } 4 \times 41250 = \underline{\underline{1.65 \times 10^5 \text{ N}}}$$

$$8. i) \Delta p = p_2 - p_1$$

$$= 30 \times 10^3 - 60 \times 10^3$$

$$= \underline{\underline{-30 \times 10^3 \text{ kg m/s}}}$$

$$ii) \Delta p = p_2 - p_1$$

$$= 45 \times 10^3 - 15 \times 10^3$$

$$= \underline{\underline{30 \times 10^3 \text{ kg m/s}}}$$

$$iii) p = 60 \times 10^3 \text{ kg m/s}$$

$$m = 20 \times 10^3 \text{ kg}$$

$$p = mv \Rightarrow v = \frac{p}{m} = \frac{60 \times 10^3}{20 \times 10^3}$$

$$\therefore \underline{\underline{v = 3 \text{ m/s}}}$$

$$iv) p = 45 \times 10^3 \text{ kg m/s}$$

$$m = 30 \times 10^3 \text{ kg}$$

$$p = mv \Rightarrow v = \frac{p}{m} = \frac{45 \times 10^3}{30 \times 10^3}$$

$$\therefore \underline{\underline{v = 1.5 \text{ m/s}}}$$

$$v) \Delta t = 1.00 - 0.64 = 0.36 \text{ seconds.}$$

$$F = \frac{\Delta p}{\Delta t} = \frac{30 \times 10^3}{0.36} = \underline{\underline{8.33 \times 10^4 \text{ N}}}$$

$$\begin{aligned}
 9.^* \text{ i)} \quad \Delta p &= m(v-u) \\
 &= 4.8 \times 10^{-26} \times (500 - (-500)) \\
 &= 4.8 \times 10^{-23} \text{ kg m/s}
 \end{aligned}$$

$$\text{ii)} \quad F = \frac{\Delta p}{\Delta t} = 4.8 \times 10^{-23} \text{ N} \quad \text{for each molecule.}$$

$$\begin{aligned}
 \# \text{ of molecules} &= \frac{0.1}{4.8 \times 10^{-23}} \\
 &= \underline{\underline{2.08 \times 10^{21}}}
 \end{aligned}$$

$$\begin{aligned}
 \text{iii)} \quad A &= 1 \mu\text{m}^2 \\
 &= 1 \times 10^{-6} \text{ m}^2
 \end{aligned}$$

$$P = \frac{F}{A} = \frac{0.1}{1 \times 10^{-6}}$$

$$\underline{\underline{P = 1.00 \times 10^5 \text{ Pa}}}$$

Part 2

$$1. \Delta p = m(v-u) ; F = \frac{\Delta p}{\Delta t}$$

$$\therefore m(v-u) = F \cdot \Delta t$$

$$\therefore \text{Since } u=0,$$

$$V = \frac{F \cdot \Delta t}{m}$$

$$= \frac{75 \times 7.5 \times 10^{-3}}{0.23}$$

$$= \underline{\underline{2.45 \text{ m/s}}}$$

$$\begin{aligned} 2. \text{ i) } \Delta p &= F \cdot \Delta t \\ &= 75 \times 0.03 \\ &= \underline{\underline{2.25 \text{ kg m/s}}} \end{aligned}$$

$$\text{ii) } \Delta p = m(v-u) ; u=0$$

$$V = \frac{\Delta p}{m} = \frac{2.25}{0.025} = \underline{\underline{90 \text{ m/s}}}$$

$$3. \quad F = \frac{\Delta p}{\Delta t}$$

$$= \frac{0.028 \times (10 - 0)}{0.035}$$

$$\underline{\underline{F = 8N}}$$

$$4. \quad F = \frac{\Delta p}{\Delta t} = \frac{m}{\Delta t} \cdot \Delta v$$

$$F = \frac{300 \times 18 \times 10^{-3}}{60} \times 550$$

$$\underline{\underline{\therefore F = 49.5N}}$$

$$5. \quad F = \frac{\Delta p}{\Delta t}$$

$$\therefore F = \frac{60 \times 10^{-3} \times (52 - 0)}{0.065}$$

$$\underline{\underline{\therefore F = 48N}}$$

$$\begin{aligned}
 6. \text{ i) } \Delta p &= m(v-u) \\
 &= 60 \times 10^{-3} \times (25 - (-20)) \\
 &= \underline{\underline{2.7 \text{ kg m/s}}}
 \end{aligned}$$

$$\text{ii) } \underline{\underline{2.7 \text{ kg m/s}}}$$

$$\text{iii) } F = \frac{\Delta p}{\Delta t} = \frac{2.7}{0.09}$$

$$\therefore \underline{\underline{F = 30 \text{ N}}}$$