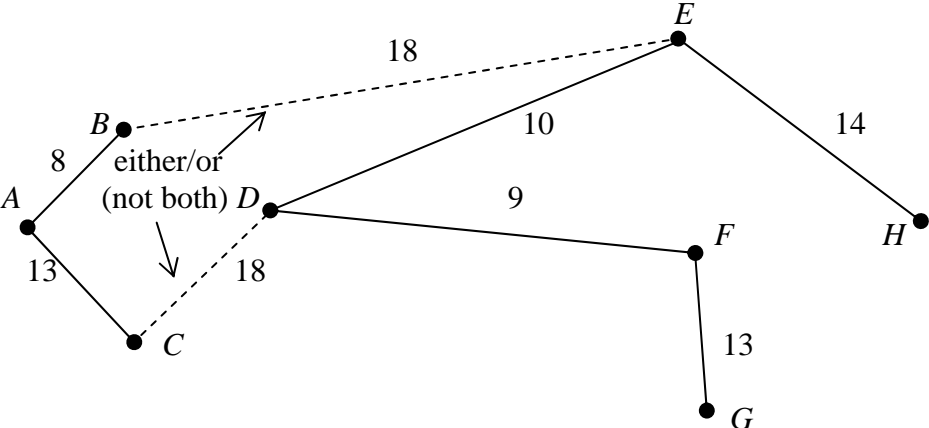


EDEXCEL DECISION MATHEMATICS D2 (6690) – JUNE 2003 PROVISIONAL MARK SCHEME

Question Number	Scheme	Marks																								
1.	<p>(a)</p> <table> <tr> <td></td><td>A(I)</td><td>A(II)</td></tr> <tr> <td>B(I)</td><td>3</td><td>-4</td></tr> <tr> <td>B(II)</td><td>-2</td><td>1</td></tr> <tr> <td>B(III)</td><td>-5</td><td>4</td></tr> </table> <p>(b) e.g. Let <math>v</math> = value of the game, <math>p</math> = pay-off, <math>q_i = P(B \text{ plays } i)</math>, <math>i = 1, 2, 3</math></p> <table> <tr> <td></td><td>A(I)</td><td>A(II)</td></tr> <tr> <td>B(I)</td><td>9</td><td>2</td></tr> <tr> <td>B(II)</td><td>4</td><td>7</td></tr> <tr> <td>B(III)</td><td>1</td><td>10</td></tr> </table> <p>Matrix becomes</p> <p>maximise <math>p = v</math></p> <p>subject to <math>v - 9q_1 - 4q_2 - q_3 + r = 0</math></p> <p><math>v - 2q_1 - 7q_2 - 10q_3 + s = 0</math></p> <p><math>q_1 + q_2 + q_3 + t = 0</math></p>		A(I)	A(II)	B(I)	3	-4	B(II)	-2	1	B(III)	-5	4		A(I)	A(II)	B(I)	9	2	B(II)	4	7	B(III)	1	10	<p>B2, 1, 0 (2)</p> <p>B1</p> <p>M1</p> <p>A2 ft, 1 ft, 0</p> <p>(4)</p> <p><b>(6 marks)</b></p>
	A(I)	A(II)																								
B(I)	3	-4																								
B(II)	-2	1																								
B(III)	-5	4																								
	A(I)	A(II)																								
B(I)	9	2																								
B(II)	4	7																								
B(III)	1	10																								

(ft = follow through mark)

Question Number	Scheme	Marks
2.	(a) In the <i>practical</i> TSP each vertex must be visited <i>at least once</i>	B1
	In the <i>classical</i> TSP each vertex must be visited <i>exactly once</i>	B1 (2)
	(b) $AB, DF, DE, (\text{reject } EF), \left\{ \begin{matrix} FG \\ AC \end{matrix} \right\} EH \left\{ \begin{matrix} DC \\ \text{or} \\ BE \end{matrix} \right\}$	M1 A1
		B1 (3)
	(c) Initial upper bound = $2 \times 85 = 170$ km	M1 A1 (2)
	(d) e.g. when $CD$ is part of the tree Use $GH$ (saving 26) and $BD$ (saving 19) giving new upper bound of 125 km Tour $A B D E H G F D C A$ (or e.g. when $BE$ is part of the tree, use $CG$ (saving 40) giving new upper bound of 130 km; Tour $A B E H E D F G C A$ )	M1 A1 A1 (3)
		<b>(10 marks)</b>

EDEXCEL DECISION MATHEMATICS D2 (6690) – JUNE 2003 PROVISIONAL MARK SCHEME

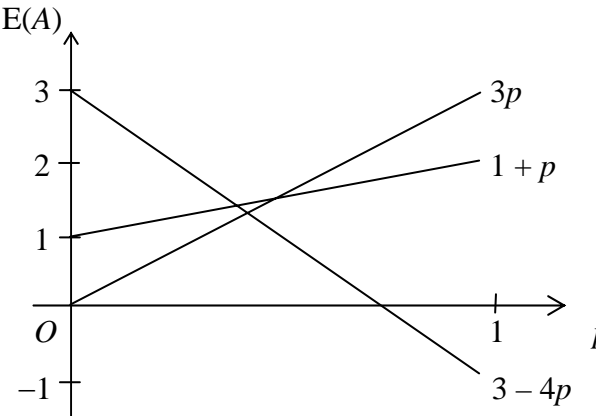
Question Number	Scheme	Marks																																																																												
3. (a)(i)	<p><b>Either rows then columns giving</b></p> <table><tr><td></td><td>I</td><td>II</td><td>III</td><td>IV</td><td></td><td>I</td><td>II</td><td>III</td><td>IV</td></tr><tr><td><math>C</math></td><td>0</td><td>22</td><td>16</td><td>4</td><td rowspan="4">then</td><td><math>C</math></td><td>0</td><td>4</td><td>0</td><td>4</td></tr><tr><td><math>J</math></td><td>1</td><td>20</td><td>24</td><td>0</td><td><math>J</math></td><td>1</td><td>2</td><td>8</td><td>0</td></tr><tr><td><math>N</math></td><td>1</td><td>18</td><td>18</td><td>0</td><td><math>N</math></td><td>1</td><td>0</td><td>2</td><td>0</td></tr><tr><td><math>S</math></td><td>1</td><td>23</td><td>26</td><td>0</td><td><math>S</math></td><td>1</td><td>5</td><td>10</td><td>0</td></tr></table> <p>3 lines only needed <math>\Rightarrow</math> least element 1 so</p> <table><tr><td></td><td>I</td><td>II</td><td>III</td><td>IV</td></tr><tr><td><math>C</math></td><td>0</td><td>4</td><td>0</td><td>5</td></tr><tr><td><math>J</math></td><td>0</td><td>1</td><td>7</td><td>0</td></tr><tr><td><math>N</math></td><td>1</td><td>0</td><td>2</td><td>1</td></tr><tr><td><math>S</math></td><td>0</td><td>4</td><td>9</td><td>0</td></tr></table>		I	II	III	IV		I	II	III	IV	$C$	0	22	16	4	then	$C$	0	4	0	4	$J$	1	20	24	0	$J$	1	2	8	0	$N$	1	18	18	0	$N$	1	0	2	0	$S$	1	23	26	0	$S$	1	5	10	0		I	II	III	IV	$C$	0	4	0	5	$J$	0	1	7	0	$N$	1	0	2	1	$S$	0	4	9	0	M1, A1, A1 (3)  <
	I	II	III	IV		I	II	III	IV																																																																					
$C$	0	22	16	4	then	$C$	0	4	0	4																																																																				
$J$	1	20	24	0		$J$	1	2	8	0																																																																				
$N$	1	18	18	0		$N$	1	0	2	0																																																																				
$S$	1	23	26	0		$S$	1	5	10	0																																																																				
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$J$	0	1	7	0																																																																										
$N$	1	0	2	1																																																																										
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(continued page 4)

**EDEXCEL DECISION MATHEMATICS D2 (6690) – JUNE 2003 PROVISIONAL MARK SCHEME**

Question Number	Scheme					Marks																									
3. (b)	<div>Subtracting all entries from some <math>n \geq 36</math> (stated)</div> <div><div>e.g. subtractions from 36</div><table><tr><td></td><td>I</td><td>II</td><td>III</td><td>IV</td></tr><tr><td><math>C</math></td><td>24</td><td>2</td><td>8</td><td>20</td></tr><tr><td><math>J</math></td><td>23</td><td>4</td><td>0</td><td>24</td></tr><tr><td><math>N</math></td><td>21</td><td>4</td><td>4</td><td>22</td></tr><tr><td><math>S</math></td><td>25</td><td>3</td><td>0</td><td>26</td></tr></table></div>						I	II	III	IV	$C$	24	2	8	20	$J$	23	4	0	24	$N$	21	4	4	22	$S$	25	3	0	26	M1
							I	II	III	IV																					
						$C$	24	2	8	20																					
						$J$	23	4	0	24																					
						$N$	21	4	4	22																					
	$S$	25	3	0	26																										
A2, 1, 0 (3)																															
(13 marks)																															

EDEXCEL DECISION MATHEMATICS D2 (6690) – JUNE 2003 PROVISIONAL MARK SCHEME

Question Number	Scheme	Marks
4.	(a) Player A: row minimums are $-1, 0, -3$ so maximin choice is play II	M1 A1
	Player B: column maximums are $2, 3, 3$ so minimax choice is play I	M1 A1 (4)
	(b) Since A's maximin ( $0$ ) $\neq$ B's minimax ( $2$ ) there is no stable solution	B1 (1)
	(c) For player A row II dominates row III, so A will <i>now</i> play III	B2, 1, 0 (2)
	(d) Let A play I with probability $p$ and II with probability $(1 - p)$	
	If B plays I, A's expected winnings are $2p + (1 - p) = 1 + p$	
	If B plays II, A's expected winnings are $-p + 3(1 - p) = 3 - 4p$	M1, A2, 1, 0
	If B plays III, A's expected winnings are $3p$	(3)
	 <p> <math>3 - 4p = 3p \Rightarrow p = \frac{3}{7}</math>  A should play I with probability <math>\frac{3}{7}</math>  A should play II with probability <math>\frac{4}{7}</math>  and never play III  The value of the game is <math>\frac{9}{7}</math> to A </p>	M1
		A1
		A1
		A1 (4)
		(14 marks)

(ft = follow through mark)

EDEXCEL DECISION MATHEMATICS D2 (6690) – JUNE 2003 PROVISIONAL MARK SCHEME

Question Number	Scheme		Marks																																																
5.	(a)	<table><tr><td></td><td>D</td><td>E</td><td>F</td></tr><tr><td>A</td><td>6</td><td></td><td></td></tr><tr><td>B</td><td>0</td><td>5</td><td></td></tr><tr><td>C</td><td></td><td>4</td><td>4</td></tr></table> <i>or</i> <table><tr><td></td><td>D</td><td>E</td><td>F</td></tr><tr><td>A</td><td>6</td><td>0</td><td></td></tr><tr><td>B</td><td></td><td>5</td><td></td></tr><tr><td>C</td><td></td><td>4</td><td>4</td></tr></table> <p>cost £470</p>		D	E	F	A	6			B	0	5		C		4	4		D	E	F	A	6	0		B		5		C		4	4	M1 A1  A1 (3)																
		D	E	F																																															
	A	6																																																	
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		D	E	F																																															
	A	6	0																																																
	B		5																																																
	C		4	4																																															
	(b)	$S_A = 0, S_B = 0, S_C = -10$ $D_D = 20, D_E = 30, D_F = 40$ $I_{AE} = 40 - 30 = 10$ $I_{AF} = 10 - 40 = -30$ $I_{BF} = 40 - 40 = 0$ $I_{CD} = 10 - 10 = 0$  Choose <i>AF</i> as entering route  $AF(+) \rightarrow CF(-) \rightarrow CE(+) \rightarrow BE(-)$ $\rightarrow BD(+) \rightarrow AD(-)$  Exiting route <i>CF</i> $\theta = 4$ <table><tr><td></td><td>D</td><td>E</td><td>F</td></tr><tr><td>A</td><td>2</td><td></td><td>4</td></tr><tr><td>B</td><td>4</td><td>1</td><td></td></tr><tr><td>C</td><td></td><td>8</td><td></td></tr></table> $S_A = 0, S_B = 0, S_C = -10$ $D_D = 20, D_E = 30, D_F = 40$ $I_{AE} = 10, I_{BF} = 30,$ $I_{CD} = 0, I_{CF} = 30$		D	E	F	A	2		4	B	4	1		C		8		$S_A = 0, S_B = -10, S_C = -20$ $D_D = 20, D_E = 40, D_F = 50$ $I_{AF} = 10 - 50 = -40$ $I_{BD} = 20 - 10 = 10$ $I_{BF} = 40 - 40 = 0$ $I_{CD} = 10 - 0 = 10$  $AF(+) \rightarrow CF(-) \rightarrow CE(+) \rightarrow AE(-)$  Exiting route <i>AE</i> $\theta = 0$ <table><tr><td></td><td>D</td><td>E</td><td>F</td></tr><tr><td>A</td><td>6</td><td></td><td>0</td></tr><tr><td>B</td><td></td><td>5</td><td></td></tr><tr><td>C</td><td></td><td>4</td><td>4</td></tr></table> $S_A = 0, S_B = 10, S_C = 20$ $D_D = 20, D_E = 0, D_F = 10$ $I_{AE} = 40, I_{BD} = -10,$ $I_{BF} = 20, I_{CD} = -30$  $CD(+) \rightarrow AD(-) \rightarrow AF(+) \rightarrow CF(-)$ $\theta = 4$ <table><tr><td></td><td>D</td><td>E</td><td>F</td></tr><tr><td>A</td><td>2</td><td></td><td>4</td></tr><tr><td>B</td><td></td><td>5</td><td></td></tr><tr><td>C</td><td>4</td><td>4</td><td></td></tr></table> $S_A = 0, S_B = 0, S_C = -10$ $D_D = 20, D_E = 30, D_F = 10$ $I_{AE} = 40, I_{BD} = 0, I_{BF} = 30, I_{CF} = 30$		D	E	F	A	6		0	B		5		C		4	4		D	E	F	A	2		4	B		5		C	4	4	
	D	E	F																																																
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C	4	4																																																	
$\therefore$ optimal, cost £350		$\therefore$ optimal, cost £350	(14 marks)																																																

## EDEXCEL DECISION MATHEMATICS D2 (6690) – JUNE 2003 PROVISIONAL MARK SCHEME

Question Number	Scheme						Marks																																																				
6.	(a)	Total cost = $2 \times 40 + 350 + 200 = \text{£}630$						M1 A1 (2)																																																			
	(b)	<table><tr><td>Stage</td><td>Demand</td><td>State</td><td>Action</td><td>Desti- nation</td><td>Value</td></tr><tr><td rowspan="6">(2)</td><td rowspan="6">(5)</td><td>(1)</td><td>(4)</td><td>(0)</td><td><math>(590 + 200 = 790)</math></td></tr><tr><td rowspan="2">(2)</td><td>(3)</td><td>(0)</td><td><math>280 + 200 = 480</math></td></tr><tr><td>(4)</td><td>(1)</td><td><math>630 + 240 = 870</math></td></tr><tr><td rowspan="3">(3)</td><td>(2)</td><td>0</td><td><math>320 + 200 = 520</math></td></tr><tr><td>3</td><td>1</td><td><math>320 + 240 = 560</math></td></tr><tr><td>4</td><td>2</td><td><math>670 + 80 = 750</math></td></tr><tr><td rowspan="3">3</td><td rowspan="3">3</td><td>0</td><td>4</td><td>1</td><td><math>550 + 790 = 1340</math></td></tr><tr><td rowspan="2">1</td><td>3</td><td>1</td><td><math>240 + 790 = 1030</math></td></tr><tr><td>4</td><td>2</td><td><math>590 + 480 = 1070</math></td></tr><tr><td rowspan="2">4</td><td rowspan="2">3</td><td>0</td><td>3</td><td>0</td><td><math>200 + 1340 = 1540</math></td></tr><tr><td>4</td><td>1</td><td><math>550 + 1030 = 1580</math></td></tr></table>						Stage	Demand	State	Action	Desti- nation	Value	(2)	(5)	(1)	(4)	(0)	$(590 + 200 = 790)$	(2)	(3)	(0)	$280 + 200 = 480$	(4)	(1)	$630 + 240 = 870$	(3)	(2)	0	$320 + 200 = 520$	3	1	$320 + 240 = 560$	4	2	$670 + 80 = 750$	3	3	0	4	1	$550 + 790 = 1340$	1	3	1	$240 + 790 = 1030$	4	2	$590 + 480 = 1070$	4	3	0	3	0	$200 + 1340 = 1540$	4	1	$550 + 1030 = 1580$	M1 A1 M1 A1 ft  M1 A1 ft (6)
		Stage	Demand	State	Action	Desti- nation	Value																																																				
		(2)	(5)	(1)	(4)	(0)	$(590 + 200 = 790)$																																																				
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<table><tr><td>Month</td><td>August</td><td>September</td><td>October</td><td>November</td></tr><tr><td>Make</td><td>3</td><td>4</td><td>4</td><td>2</td></tr></table>						Month	August	September	October	November	Make	3	4	4	2	M1 A1																																											
Month	August	September	October	November																																																							
Make	3	4	4	2																																																							
cost = £1540						A1 ft (3)																																																					
Profit per cycle = $13 \times 1400$ Cost of Kim's time = £2000 																																																											

(ft = follow through mark)