

# EDEXCEL

Stewart house 32 Russell Square London WC1B 5DN

June 2004

Advanced Subsidiary/Advanced Level

General Certificate of Education

Subject: 6690 Decision Maths

Paper: D2

Question Number	Scheme	Marks																																																																																											
1) (a)	A game in which the gain to one player is equal to the loss of the other	B2, 1, 0 (2)																																																																																											
(b)	If there is a <u>stable solution(s)</u> $a_{ij}$ in a game, the <u>location</u> of this stable solution is called the saddle point. It is the point(s) where row maximin = column minimax	B2, 1, 0 (2) <u>4</u>																																																																																											
2)	<p>Subtract all terms from some <math>n \geq 35</math>, e.g. 35</p> <table><tr><td>4</td><td>11</td><td>3</td><td>0</td></tr><tr><td>19</td><td>25</td><td>16</td><td>13</td></tr><tr><td>16</td><td>21</td><td>15</td><td>14</td></tr><tr><td>17</td><td>20</td><td>14</td><td>12</td></tr></table> <p>Reducing rows then columns</p> <table><tr><td>2</td><td>4</td><td>2</td><td>0</td></tr><tr><td>4</td><td>5</td><td>2</td><td>0</td></tr><tr><td>0</td><td>0</td><td>0</td><td>0</td></tr><tr><td>3</td><td>1</td><td>1</td><td>0</td></tr></table> <p>— minimum uncovered 1</p> <table><tr><td>1</td><td>3</td><td>1</td><td>0</td></tr><tr><td>3</td><td>4</td><td>1</td><td>0</td></tr><tr><td>0</td><td>0</td><td>0</td><td>1</td></tr><tr><td>2</td><td>0</td><td>0</td><td>0</td></tr></table> <p>— minimum uncovered 1</p> <table><tr><td>0</td><td>2</td><td>0</td><td>0</td></tr><tr><td>2</td><td>3</td><td>0</td><td>0</td></tr><tr><td>0</td><td>0</td><td>0</td><td>2</td></tr><tr><td>2</td><td>0</td><td>0</td><td>1</td></tr></table> <p>e.g. matching</p> <table><tr><td>D</td><td>-</td><td>A</td><td>A</td><td>m</td><td>s</td></tr><tr><td>H</td><td>-</td><td>s</td><td>or</td><td>s</td><td>or</td><td>s</td><td>or</td><td>m</td></tr><tr><td>k</td><td>-</td><td>m</td><td>L</td><td>A</td><td>A</td></tr><tr><td>T</td><td>-</td><td>L</td><td>m</td><td>L</td><td>L</td></tr></table> <p>Total 88 points</p>	4	11	3	0	19	25	16	13	16	21	15	14	17	20	14	12	2	4	2	0	4	5	2	0	0	0	0	0	3	1	1	0	1	3	1	0	3	4	1	0	0	0	0	1	2	0	0	0	0	2	0	0	2	3	0	0	0	0	0	2	2	0	0	1	D	-	A	A	m	s	H	-	s	or	s	or	s	or	m	k	-	m	L	A	A	T	-	L	m	L	L	<p>m1 A1✓ (2)</p> <p>B1</p> <p>m1 A1✓ (3)</p> <p>m1 A1✓</p> <p>A1✓</p> <p>A1 (4) <u>9</u></p>
4	11	3	0																																																																																										
19	25	16	13																																																																																										
16	21	15	14																																																																																										
17	20	14	12																																																																																										
2	4	2	0																																																																																										
4	5	2	0																																																																																										
0	0	0	0																																																																																										
3	1	1	0																																																																																										
1	3	1	0																																																																																										
3	4	1	0																																																																																										
0	0	0	1																																																																																										
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Question Number	Scheme	Marks
3) (a)(i)	Minimum connector using eg Prim: AC, CB, CD, CE length = $98 + 74 + 82 + 103 = 357$ {1,3,2,4,5} So upper bound = $2 \times 357 = 714$	MI AI MI AI ✓ (4)
(ii)	A <u>(98)</u> C <u>(74)</u> B <u>(131)</u> D <u>(134)</u> E <u>(115)</u> A length = $98 + 74 + 131 + 134 + 115 = 552$	MI AI AI (3)
(b)	Residual minimum connector is AC, CB, CD length 254 Lower bound = $254 + 103 + 115 = 472$	MI AI MI AI ✓ (4)
(c)	$472 \leq \text{solution} \leq 552$	BI ✓ (1) <u>12</u>

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4) (a)	<p>row min</p> $\begin{pmatrix} -4 & -1 & 3 \\ 2 & 1 & -2 \end{pmatrix}$ <p>col max</p> <p><math>-4</math> <math>-2 \leftarrow \max</math></p> <p><math>2</math> <math>1</math> <math>3</math></p> <p><math>\uparrow</math> min</p> <p><math>-2 \neq 1 \therefore</math> not stable</p>	<p><math>m_1 A_1</math></p> <p><math>A_1</math></p> <p>(3)</p>
(b)	<p>Let Emma play <math>R_1</math> with probability <math>p</math></p> <p>If Freddie plays <math>C_1</math> Emmas winnings are <math>-4p + 2(1-p) = 2-6p</math></p> <p><math>C_2</math> " " " " " <math>-p + 1(1-p) = 1-2p</math></p> <p><math>C_3</math> " " " " " <math>3p - 2(1-p) = -2+5p</math></p> <p>need intersection of <math>2-6p</math> and <math>-2+5p</math></p> $2-6p = -2+5p$ $4 = 11p$ $p = \frac{4}{11}$ <p>So Emma should play <math>R_1</math> with probability <math>\frac{4}{11}</math></p> <p><math>R_2</math> " " " " " <math>\frac{7}{11}</math></p> <p>The value of the game is <math>-\frac{2}{11}</math> to Emma.</p>	<p><math>m_1 A_1</math></p> <p><math>A_1</math></p> <p>(3)</p>
(c)	<p>value to Freddie <math>\frac{2}{11}</math>, matrix <math>\begin{pmatrix} 4 &amp; -2 \\ 1 &amp; -1 \\ -3 &amp; 2 \end{pmatrix}</math></p>	<p><math>m_1 A_1</math></p> <p><math>A_1</math></p> <p>(3)</p>

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5) (a)	Idea of many supply and demand points and many units to be moved. Costs are variable and dependent upon the supply and demand points, need to minimize costs. <u>Practical</u> Costs proportional to number of units.	B2, 1, 0 (2)																
(b)	Supply = 120 Demand = 110 so not balanced	B1 (1)																
(c)	Adds 0, 0, 0, 10 to column f <table> <tr> <td></td> <td>d</td> <td>e</td> <td>f</td> </tr> <tr> <td>A</td> <td>45</td> <td></td> <td></td> </tr> <tr> <td>B</td> <td>5</td> <td>30</td> <td></td> </tr> <tr> <td>C</td> <td></td> <td>30</td> <td>10</td> </tr> </table> <p>Cost 545</p>		d	e	f	A	45			B	5	30		C		30	10	m1, A1 m1, A1 B1✓(5)
	d	e	f															
A	45																	
B	5	30																
C		30	10															
(d)	$R_1 = 0$ $R_2 = -1$ $R_3 = -3$ $k_1 = 5$ $k_2 = 7$ $k_3 = 3$ $Ae = 3 - 0 - 7 = -4$ ← $Af = 0 - 0 - 3 = -3$ $Bf = 0 + 1 - 3 = -2$ $Cd = 2 + 3 - 5 = 0$	m1 A1 m1 A1✓ A1✓ (5)																
(e)	$Ae^+ \rightarrow Be^- \rightarrow Bd^+ \rightarrow Ad^-$ send 30 <table> <tr> <td></td> <td>d</td> <td>e</td> <td>f</td> </tr> <tr> <td>A</td> <td>15</td> <td>30</td> <td></td> </tr> <tr> <td>B</td> <td>35</td> <td></td> <td></td> </tr> <tr> <td>C</td> <td></td> <td>30</td> <td>10</td> </tr> </table> <p>Cost 425</p>		d	e	f	A	15	30		B	35			C		30	10	<div> <div></div> <div> m1 A1✓ Dm1 A1✓ A1 (5) </div> </div>
	d	e	f															
A	15	30																
B	35																	
C		30	10															
		18																

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6) (a)	Stage - number of weeks to finish state - show being attended Action - Next journey to undertake eg	B1 B1 B1 (3)																																																					
(b)	<table><tr><th>Stage</th><th>State</th><th>Action</th><th>Value</th></tr><tr><td rowspan="3">1</td><td>F</td><td>F-Home</td><td><math>500 - 80 = 420 *</math></td></tr><tr><td>G</td><td>G-Home</td><td><math>700 - 90 = 610 *</math></td></tr><tr><td>H</td><td>H-Home</td><td><math>600 - 70 = 530 *</math></td></tr><tr><td rowspan="6">2</td><td rowspan="3">D</td><td>DF</td><td><math>1500 - 200 + 420 = 1720</math></td></tr><tr><td>DG</td><td><math>1500 - 160 + 610 = 1950 *</math></td></tr><tr><td>DH</td><td><math>1500 - 120 + 530 = 1910</math></td></tr><tr><td rowspan="3">E</td><td>EF</td><td><math>1300 - 170 + 420 = 1550</math></td></tr><tr><td>EG</td><td><math>1300 - 100 + 610 = 1810 *</math></td></tr><tr><td>EH</td><td><math>1300 - 110 + 530 = 1720</math></td></tr><tr><td rowspan="6">3</td><td rowspan="2">A</td><td>AD</td><td><math>900 - 180 + 1950 = 2670 *</math></td></tr><tr><td>AE</td><td><math>900 - 150 + 1810 = 2560</math></td></tr><tr><td rowspan="2">B</td><td>BD</td><td><math>800 - 140 + 1950 = 2610 *</math></td></tr><tr><td>BE</td><td><math>800 - 120 + 1810 = 2490</math></td></tr><tr><td rowspan="2">C</td><td>CD</td><td><math>1000 - 200 + 1950 = 2750 *</math></td></tr><tr><td>CE</td><td><math>1000 - 210 + 1810 = 2600</math></td></tr><tr><td rowspan="3">4</td><td rowspan="3">Home</td><td>Home-A</td><td><math>-70 + 2670 = 2600 *</math></td></tr><tr><td>Home-B</td><td><math>-80 + 2610 = 2530</math></td></tr><tr><td>Home-C</td><td><math>-150 + 2750 = 2600 *</math></td></tr></table>	Stage	State	Action	Value	1	F	F-Home	$500 - 80 = 420 *$	G	G-Home	$700 - 90 = 610 *$	H	H-Home	$600 - 70 = 530 *$	2	D	DF	$1500 - 200 + 420 = 1720$	DG	$1500 - 160 + 610 = 1950 *$	DH	$1500 - 120 + 530 = 1910$	E	EF	$1300 - 170 + 420 = 1550$	EG	$1300 - 100 + 610 = 1810 *$	EH	$1300 - 110 + 530 = 1720$	3	A	AD	$900 - 180 + 1950 = 2670 *$	AE	$900 - 150 + 1810 = 2560$	B	BD	$800 - 140 + 1950 = 2610 *$	BE	$800 - 120 + 1810 = 2490$	C	CD	$1000 - 200 + 1950 = 2750 *$	CE	$1000 - 210 + 1810 = 2600$	4	Home	Home-A	$-70 + 2670 = 2600 *$	Home-B	$-80 + 2610 = 2530$	Home-C	$-150 + 2750 = 2600 *$	M1 A1 (2)  M1 A1✓ A1✓ A1 (4)  M1 A1✓ A1✓ A1 (4)  M1 A1 (2)
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(c)	Home < $\begin{matrix} A \\ c \end{matrix}$ > D-G Total profit £ 2600	B2✓/1/0  B1✓ (3)  118																																																					