

Question Number	Scheme	Marks
1.	<p>Total in School = $(15 \times 30) + 150 = 600$</p> <p>random sample of $\frac{30}{600} \times 40$ (Use of $\frac{40}{\text{their } 600}$)</p> <p>= <u>2</u> from each of the 15 classes</p> <p>random sample of $\frac{150}{600} \times 40$ Either</p> <p>= <u>10</u> from sixth form;</p> <p>Label the boys in each class from 1 – 15 and the girls from 1 – 15. use random numbers to select 1 girl and 1 boy</p> <p>Label the boys in the sixth form from 1 – 75 and the girls from 1 – 75. use random numbers to select <u>5</u> different boys and 5 different girls.</p>	<p>B1</p> <p>M1</p> <p>A1</p> <p>A1</p> <p>B1</p> <p>B1</p> <p>B1</p> <p>(7)</p>

Question Number	Scheme	Marks
2. (a)	$E(R) = 20 + 10 = 30$	B1 (1)
(b)	$\text{Var}(R) = 4 + 0.84, = 4.84$	M1, A1 (2)
(c)	$R \sim N(30, 4.84)$ $P(28.9 < R < 32.64) = P(R < 32.64) - P(R < 28.9)$ $= P\left(Z < \frac{32.64 - 30}{2.2}\right) - P\left(Z < \frac{28.9 - 30}{2.2}\right)$ $= P(Z < 1.2) - P(Z < -0.5)$ $= 0.8849 - (1 - 0.6915)$ $= 0.8849 - 0.3085 = 0.5764$	(Use of normal with their (a),(b)) B1ft M1 Stand their σ and μ A1, A1 M1 Correct area A1 (accept AWRT 0.576) (6)

3. (a)	$\hat{\mu} = \frac{82 + 98 + 140 + 110 + 90 + 125 + 150 + 130 + 70 + 110}{10}$ $= 110.5$ $\hat{\sigma}^2 = \frac{1}{9}(128153 - 10 \times 110.5^2)$ $= 672.28$	M1 A1 B1 M1 A1 (AWRT 672)	(5)
(b)	<p>95% confidence limits are</p> $110.5 \pm 1.96 \times \frac{25}{\sqrt{10}}$ <p>95% conf. lim. = AWRT(95, 126)</p>	<p>(condone use of 5 instead of 25) (for 1.96)</p> M1 B1 A1√ A1 A1	(5)
(c)	<p>Number of intervals = $\frac{95}{100} \times 15$</p> $= 14.25$	<p>(Allow 14 or 14.3 if method is clear)</p> M1 A1	(2)
12			

4.	<p>H_0 : No association between gender and acceptance H_1 : gender and acceptance are associated</p> <table><tr><td></td><td>Accept</td><td>Not accept</td><td>Total</td></tr><tr><td>Males</td><td>170 (180)</td><td>110 (100)</td><td>280</td></tr><tr><td>Females</td><td>280 (270)</td><td>140 (150)</td><td>420</td></tr><tr><td>Totals</td><td>450</td><td>250</td><td>700</td></tr></table> <p>Expected Values</p> <table><tr><td>O</td><td>E</td><td>$\frac{(O - E)^2}{E}$</td></tr><tr><td>170</td><td>180</td><td>0.5556</td></tr><tr><td>110</td><td>100</td><td>1.0000</td></tr><tr><td>280</td><td>270</td><td>0.3704</td></tr><tr><td>140</td><td>150</td><td>0.6667</td></tr></table> <p>$\sum \frac{(O - E)^2}{E} = 2.59$ (Yates' 2.34) (Condone use of Yates')</p> <p>$\nu = 1; (5\%) = 3.841$</p> <p>$3.841 > 2.59$. There is insufficient evidence to reject H_0 There is no association between a persons gender and their acceptance (of the offer of a flu jab.)</p>		Accept	Not accept	Total	Males	170 (180)	110 (100)	280	Females	280 (270)	140 (150)	420	Totals	450	250	700	O	E	$\frac{(O - E)^2}{E}$	170	180	0.5556	110	100	1.0000	280	270	0.3704	140	150	0.6667	<p>B1</p> <p>M1 A1</p> <p>M1 A1</p> <p>B1; B1</p> <p>M1 A1✓</p> <p>(9)</p> <p>9</p>
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5. (a)	μ_b = mean mark of boys, μ_g = mean mark of girls. $H_0 : \mu_b = \mu_g$ $H_1 : \mu_b \neq \mu_g$ $z = \frac{53 - 50}{\sqrt{\frac{144}{80} + \frac{144}{80}}}$ $= 1.58$ <p>Critical region $z \geq 1.96$ $1.58 < 1.96$ insufficient evidence to reject H_0. No diff. between mean scores of boys and girls.</p>	both	B1 M1 A1 A1 B1 M1 A1	(7)
(b)	$H_0 : \mu_b = \mu_g$ $H_1 : \mu_b < \mu_g$ $z = \frac{62 - 59}{\sqrt{\frac{36}{80} + \frac{36}{80}}}$ $= 3.16$ <p>Critical region $z \geq 1.6449$ (accept 1.645) $3.16 > 1.6449$ sufficient evidence to reject H_0. the mean mark for boys is less than the mean mark of the girls.</p>		B1 M1 A1 B1 A1	(5)
(c)	Girls have improved more than boys or girls performed better than boys after 1 year		B1	(1)
13				

6. (a)	$r = 27.07,$ $s = 18.04,$ $t = 0.11$ using tables or 0.12 using totals	M1 A1 B1 B1 ft (4)
(b)	<p> H_0 : A Poisson model $Po(2)$ is a suitable model. H_1 : A Poisson model $Po(2)$ is not a suitable model. </p> <p>Amalgamate data</p> $\sum \frac{(O - E)^2}{E} = 3.28 \text{ (awrt)}$ <p>$\nu = 6 - 1 = 5$</p> $\chi^2_5(5\%) = 11.070$ <p>(follow through their degrees of freedom)</p> <p>$3.25 < 11.070$ There is insufficient evidence to reject H_0, <u>$Po(2)$ is a suitable model.</u></p>	both B1 M1 M1 A1 B1 B1ft A1ft (7)
(c)	<p>The expected values, and hence $\sum \frac{(O - E)^2}{E}$ would be different, and the degrees of freedom would be 1 less.</p>	B1 B1 (2)
		13

7. (a)	The variables cannot be assumed to be normally distributed						B1	(1)																																			
(b)	<table><tr><td></td><td>20-29</td><td>30-39</td><td>40-49</td><td>50-59</td><td>60-69</td><td>70+</td></tr><tr><td>Rank x</td><td>5</td><td>6</td><td>4</td><td>3</td><td>1</td><td>2</td></tr><tr><td>Rank y</td><td>6</td><td>5</td><td>4</td><td>1</td><td>3</td><td>2</td></tr><tr><td>d</td><td>1</td><td>1</td><td>0</td><td>2</td><td>2</td><td>0</td></tr><tr><td>d^2</td><td>1</td><td>1</td><td>0</td><td>4</td><td>4</td><td>0</td></tr></table>		20-29	30-39	40-49	50-59	60-69	70+	Rank x	5	6	4	3	1	2	Rank y	6	5	4	1	3	2	d	1	1	0	2	2	0	d^2	1	1	0	4	4	0						M1 A1	
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d	1	1	0	2	2	0																																					
d^2	1	1	0	4	4	0																																					
	$\sum d^2 = 10$					(follow through their rankings)	dM1 (depends on ranking attempt)	A1 ft																																			
	$r_s = 1 - \frac{6\sum d^2}{n(n^2 - 1)} = 1 - \frac{60}{210} = 0.714$					$\left(\frac{5}{7} \text{ or awrt } 0.714\right)$	M1 A1	(6)																																			
(c)	$H_0 : \rho = 0$ $H_1 : \rho \neq 0 \text{ (or } \rho > 0)$ $n = 6 \Rightarrow 5\% \text{ critical value} = 0.8857 \text{ (or } 0.8286)$ $0.714 < 0.8857$ No evidence to reject H_0 ; No evidence of correlation between deaths from pneumoconiosis and lung cancer.						B1 B1 B1✓ M1 A1	(5)																																			
							12																																				