

# EDEXCEL

Stewart house 32 Russell Square London WC1B 5DN

June 2004

Advanced Subsidiary/Advanced Level

General Certificate of Education

Subject: 6679 Mechanics

Paper: M3

Question number	Scheme	Marks
1.	$1000 \text{ r.p.m.} = \frac{1000 \times 2\pi}{60} \text{ rad/s}$ $v = 0.035 \times \frac{1000 \times 2\pi}{60} = 3.67 \text{ ms}^{-1} \text{ (3 SF)}$ <p><i>M1 their r x their ω</i></p>	<p>B1</p> <p>M1 A1 (3)</p>
2.	<p>Extn at bottom = <math>\frac{a}{\cos \alpha} - a = \frac{2a}{3}</math> (0.67a or better)</p> <p>Energy: <math>mg \tan \alpha = \frac{2\lambda \left(\frac{2a}{3}\right)^2}{2a}</math></p> <p><math>3mg = \lambda</math></p> <p><i>Second M0 if treated as equilibrium.</i> <i>Third M1 for solving for λ.</i></p>	<p>M1 A1</p> <p>dep. <math>\rightarrow</math> M1 A1 A1 f.t. M1 A1 (7)</p>
3.(a)	<p><math>mg \sin 30^\circ - mx^2 = ma</math></p> <p><math>\frac{g}{2} - x^2 = v \frac{dv}{dx}</math> or <math>\frac{d(\frac{1}{2}v^2)}{dx}</math></p> <p><math>\frac{gx}{2} - \frac{x^3}{3} (+C) = \frac{v^2}{2}</math></p> <p><math>x = 2: g - \frac{g}{3} = \frac{v^2}{2}</math></p> <p><math>v = 3.8 \text{ ms}^{-1} \text{ (3.78)}</math></p> <p><i>Third M1 for attempting to integrate</i></p>	<p>M1 A1</p> <p>dep. <math>\rightarrow</math> M1</p> <p>M1A1</p> <p>dep. <math>\rightarrow</math> M1</p> <p>A1 (7)</p>
(b)	<p><math>v = 0: \frac{gx}{2} - \frac{x^3}{3} = 0</math></p> <p><math>x^2 = \frac{3g}{2} \Rightarrow x = 3.8, (3.83), \sqrt{\frac{3g}{2}}</math></p> <p><i>Must have integrated for first M1</i></p>	<p><math>\rightarrow</math> M1</p> <p>dep. <math>\rightarrow</math> M1 A1 c.s.o. (3)</p> <p>(10)</p>

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4.(a)	$(\uparrow), R=mg$ $m \frac{4a}{3} \omega^2$ <i>seen and used.</i> $m \frac{4a}{3} \omega^2 \leq \frac{3}{5} mg$ $\Rightarrow \omega^2 \leq \frac{9g}{20a}$	B1 <del>B1</del> M1 A1 c.s.o. (4)
(b)	$T = \frac{2mg}{a} \frac{a}{3} = \frac{2mg}{3}$ $(\rightarrow), \frac{3}{5} mg + \frac{2mg}{3} \geq m \frac{4a}{3} \omega_{\max}^2$ $\frac{19g}{20a} = \omega_{\max}^2$ $(\rightarrow), -\frac{3}{5} mg + \frac{2mg}{3} \leq m \frac{4a}{3} \omega_{\min}^2$ $\frac{g}{20a} = \omega_{\min}^2$	B1 M1 A1 f.t. A1 M1 A1 f.t. A1 (7)
<i>If only one answer, must be clear whether max or min for final A1</i>		<div style="border: 1px solid black; border-radius: 50%; width: 30px; height: 30px; display: flex; align-items: center; justify-content: center;">11</div>

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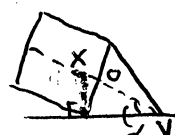
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5. (a)	<p> cylinder (<del>36</del><math>\pi r^3</math>) cone (<math>12\pi r^3</math>) toy (<del>48</del><math>\pi r^3</math>) </p> <p> mass ratio      3                  1                  4 </p> <p> dist. from O    <math>2r</math>                  <math>(-) r</math>                  <math>\bar{x}</math> </p> <p> <math>(3 \times 2r) - r = 4\bar{x}</math> </p> <p> <math>\frac{5r}{4} = \bar{x}</math> </p> <p> M1 for clear attempt at <math>\Sigma mx = \bar{x} \Sigma m</math> - correct no. of terms.  If distances not measured from O, B1B1M1A1 available. </p>	<p>B1</p> <p>B1</p> <p>M1 A1</p> <p>A1                  (5)</p>
(b)	 <p>AG vertical, seen or implied</p> <p> <math>\tan \theta = \frac{3r}{4r - \bar{x}}</math> </p> <p> <math>\theta = 47.5^\circ</math> (1 d.p.) </p> <p>Second M1 for use of tan</p>	<p>M1</p> <p>M1 A1</p> <p>A1                  (4)</p>
(c)	 <p> sim <math>\Delta</math>'s : <math>\frac{OX}{3r} = \frac{3r}{4r} (= \tan \alpha)</math> </p> <p> <math>\Rightarrow OX = \frac{9r}{4}</math> </p> <p> <math>\bar{x} &lt; OX</math> </p> <p> <math>\Rightarrow</math> won't topple </p> <p>Note that second M1 is independent, for the general idea.</p>	<p>M1</p> <p>A1 (This is <math>\sqrt{\quad}</math> on alternatives)</p> <p>M1</p> <p>A1 c.s.o.                  (4)</p> <p>(13)</p>

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	<i>All M marks require correct number of terms with appropriate terms resolved.</i>	
6.(a)	$B \text{ to } C : \frac{1}{2}mv^2 - \frac{1}{2}m20^2 = mg.50(1 - \sin 30^\circ)$ $v = 30\text{ms}^{-1}(29.8)$	M1 A1 A1 (3)
(b)	(↑) at C, $R - mg = m\frac{890}{50}$ $R = 1900 \text{ N } (1930\text{N})$	M1 A1 ft A1 (3)
(c)	$C \text{ to } D : \frac{1}{2}m890 - \frac{1}{2}mw^2 = mg.50(1 - \cos 30^\circ)$ $w = 28\text{ms}^{-1}(27.5)$	M1 A1 ft A1 (3)
(d)	Before: $R = mg \cos \theta$ After: $R = mg \cos \theta + m\frac{20^2}{50}$ Change = $70 \cdot \frac{20^2}{50} = 560 \text{ N}$	B1 M1 A1 A1 c.s.o (4)
(e)	lower speed at C $\Rightarrow R$ reduced	M1 A1 (2) <b>(15)</b>

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7.(a)	$(-)\frac{21.6x}{2} = 0.3\ddot{x}$ $-36x = \ddot{x}$ $\text{S.H.M., period} = \frac{2\pi}{\sqrt{36}} = \frac{\pi}{3}$	<p>M1 A1</p> <p>M1</p> <p>A1 c.s.o. (4)</p>
(b)	At A: $v = a\omega = 1.5 \times 6 = 9 \text{ ms}^{-1}$	M1 A1 (2)
(c)	$x = a\cos\omega t$ $0.75 = 1.5\cos 6t$ $\frac{\pi}{3} = 6t \Rightarrow t = \frac{\pi}{18} \text{ (no decimals)}$	<p><i>general.</i></p> <p>M1</p> <p>dep M1 A1 (3)</p>
(d)	$(-)\frac{21.6x}{2} = 0.5\ddot{x}$ $-21.6x = \ddot{x} \Rightarrow \text{S.H.M., } \omega = \sqrt{21.6}$ <p>At collision: CLM: <math>0.3 \times 9 = 0.5v \Rightarrow v = 5.4</math></p> $a \times \sqrt{21.6} = 5.4$ $a = 1.16 \text{ m (3SF)}$	<p>M1 A1</p> <p>A1</p> <p>M1 A1 f.t</p> <p>M1</p> <p>A1 (7)</p> <p>(16)</p>

HJJ. 26.5.04