The Kinetic Theory of Gases

Supplementary Questions

Study Guide 24

Part 1

1. 
$$T_1 = 273 \, \text{K}$$
;  $P_1 = 1.01 \times 10^5 \, \text{Pa}$ ;  $V_1 = 3.0 \times 10^{-5} \, \text{M}^3$   
 $T_2 = 313 \, \text{K}$ ;  $P_2 = 4.0 \times 10^5 \, \text{Pa}$ ;  $V_2 = ?$ 

$$\frac{P_1V_1}{T_1} = \frac{P_2V_2}{T_2} \implies V_2 = \frac{P_1}{P_2} \cdot \frac{T_2}{T_1} \cdot V_1$$

$$V_2 = \frac{1.01 \times 10^5}{4.0 \times 10^5} \times \frac{313}{273} \times 3.0 \times 10^5$$

$$V_2 = 8.68 \times 10^6 \,\mathrm{m}^3$$

2. 
$$P_1 = 128 \times 10^3 Pa$$
;  $V_1 = 1.51 (= 0.0015 m^3)$ 

$$P_2 = ?$$
 ;  $V_2 = 1.31 = 0.0013 \text{ m}^3$ 

$$P_1V_1 = P_2V_2$$

$$P_2 = P_1 \cdot \frac{V_1}{V_2}$$

$$= 128 \times 10^{3} \times \frac{1.5}{1.3}$$

i) 
$$V_1 = 4.5 \times 10^{-3} \text{ m}^3$$
;  $P_1 = 3.0 \times 10^6 \text{ Pa}$ ;  $T_1 = 287 \text{ k}$ 

$$V_2 = ?$$

$$i \quad P_2 = 1.01 \times 10^5 \text{ Pa}$$

$$i \quad T_2 = 273 \text{ k}$$

$$\frac{P_1 V_1}{T_1} = \frac{P_2 V_2}{T_2} \implies V_2 = \frac{P_1}{P_2} \cdot \frac{T_2}{T_1} \cdot V_1$$

$$V_2 = \frac{3.0 \times 10^6}{1.01 \times 10^5} \times \frac{273}{287} \times 4.5 \times 10^{-3}$$

$$V_2 = 1.27 \times 10^{-1} \,\mathrm{m}^3$$

ii) 
$$M = \rho V_2$$
  
= 1.4 x 1.27 x10

$$= 0.178 \text{ kg}$$

4. 
$$T_1 = 303K$$
;  $P_1 = P$ ;  $V_1 = V$ 

$$T_2 = ?$$
;  $P_2 = P$ ;  $V_2 = 2V$ 

$$\frac{P_1 V_1}{T_1} = \frac{P_2 V_2}{T_2} \implies T_2 = \frac{P_2}{P_1} \frac{V_2}{V_1} \cdot T_1$$

$$T_2 = \frac{P}{P} \times \frac{2V}{V} \times 303$$

$$= 2 \times 303$$

$$T_2 = 606 \, \text{K} = 333^{\circ} \text{C}$$

$$\frac{P_1}{T_1} = \frac{P_2}{T_2} \Rightarrow T_2 = \frac{P_2}{P_1} T_1$$

$$T_2 = \frac{2.75 \times 10^5}{1.75 \times 10^5} \times 292$$

$$\frac{T_2}{2} = 459 \, \text{K}$$

6. 
$$V_1 = 250 \text{ cm}^3$$
;  $T_1 = 340 \text{ K}$ ;  $P_1 = 1.04 \times 10^5 \text{ Pa}$ 

$$V_2 = ?$$

$$\frac{P_1 V_1}{T_1} = \frac{P_2 V_2}{T_2} \implies V_2 = \frac{P_1}{P_2} \cdot \frac{T_2}{T_1} \cdot V_1$$

$$V_2 = \frac{1.64 \times 10^5}{1.01 \times 10^5} \times \frac{273}{340} \times 250$$

$$V_2 = 207 \text{ cm}^3$$

$$T_2 = 278 \, \text{K}$$
 ;  $P_2 = 0.75 \, \text{Atm}$ .

$$\frac{P_1 V_1}{T_1} = \frac{P_2 V_2}{T_2} \Rightarrow \frac{V_2}{V_1} = \frac{P_1}{P_2} \cdot \frac{T_2}{T_1}$$
at 2.5km

Vol. at 2.5km

$$\frac{V_2}{V_1} = \frac{1.0}{0.75} \times \frac{278}{290}$$

8. i) 
$$V_1 = 0.050 \text{ n}^3$$
;  $P_1 = 2.5 \times 10^6 \text{ Pa}$ 

$$V_2 = ?$$
;  $P_2 = 1.01 \times 10^5 \text{ Pa}$ 

$$P_1V_1 = P_2V_2$$

$$V_2 = \frac{P_1}{P_2} \cdot V_1 = \frac{2.5 \times 10^6}{1.01 \times 10^5} \times 0.050$$

$$V_2 = 1.24 \text{ m}^3$$

1.19 m³ of air is released from the cylinder.

9. 
$$P_1 = 1.01 \times 10^5 + 4.2 \times 10^5$$
;  $V_1 = 2.5 \times 10^{-2} \text{ m}^3$ ;  $T_1 = 296 \text{ K}$   
=  $5.21 \times 10^5 \text{ Pa}$ 

$$V_2 = ?$$
 ;  $P_2 = 1.01 \times 10^5 P_a$  ;  $T_2 = 273 k$ 

$$\frac{P_1V_1}{T_1} = \frac{P_2V_2}{T_2} \implies V_2 = \frac{P_1}{P_2} \cdot \frac{T_2}{T_1} \cdot V_1$$

$$\frac{1}{1.01 \times 10^{5}} \times \frac{273}{296} \times 2.5 \times 10^{-2}$$

$$V_2 = 0.1189 \, \text{m}^3$$
 at STP.

$$M = \rho V_2 = 1.34 \times 0.1189$$
  
= 0.159 kg

i) 
$$T_1 = 291 \, \text{K}$$
 ;  $P_1 = 1.01 \times 10^5 \, \text{Pa}$ 

$$T_2 = ?$$

$$P_2 = 1.01 \times 10^5 + 2.00 \times 10^4$$

$$= 1.21 \times 10^5 Pa$$

$$\frac{P_1}{T_1} = \frac{P_2}{T_2} \Rightarrow T_2 = \frac{P_2}{P_1} T_1$$

$$T_2 = \frac{1.21 \times 10^5}{1.01 \times 10^5} \times 291$$

$$= 349 K$$

$$F = A \times \Delta P = 3.14 \times 10^{-4} \times 2 \times 10^{4} = 6.28 \, \text{N}$$
  
 $F = ma \implies \alpha = \frac{F}{m} = \frac{6.28}{0.025} = \frac{251.2 \, \text{m/s}^2}{251.2 \, \text{m/s}^2}$ 

11.\* 
$$P_1 = 190 \times 10^3 + 102 \times 10^3$$
;  $T_1 = 281 \text{K}$   
= 292 × 10<sup>3</sup> Pa

$$P_2 = ?$$
 ;  $T_2 = 302 K$ 

$$\frac{P_1}{T_1} = \frac{P_2}{T_2} \implies P_2 = \frac{T_2}{T_1} \cdot P_1$$

$$\frac{P_2}{2} = \frac{302}{281} \times 292 \times 10^3$$

$$313.8 \times 10^{3} - 102 \times 10^{3}$$
  
=  $212 \times 10^{3} Pa$   
=  $212 \times Pa$  (=  $30.74 \cdot Psi$ )

12. Volume remains constant.

$$P_2 = ?$$

$$P_2 = ?$$
  $j T_2 = 473 K$ 

$$\frac{P_1}{T_1} = \frac{P_2}{T_2} \implies P_2 = \frac{T_2}{T_1} \cdot P_1$$

$$P_2 = \frac{473}{288} \times 1.01 \times 10^5$$

$$\Delta P = 1.6588 \times 10^{5}$$

$$-1.01 \times 10^{5}$$

$$= 6.488 \times 10^{4} Pa$$

$$A = 0.3^2 = 0.09 \, \text{m}^2$$

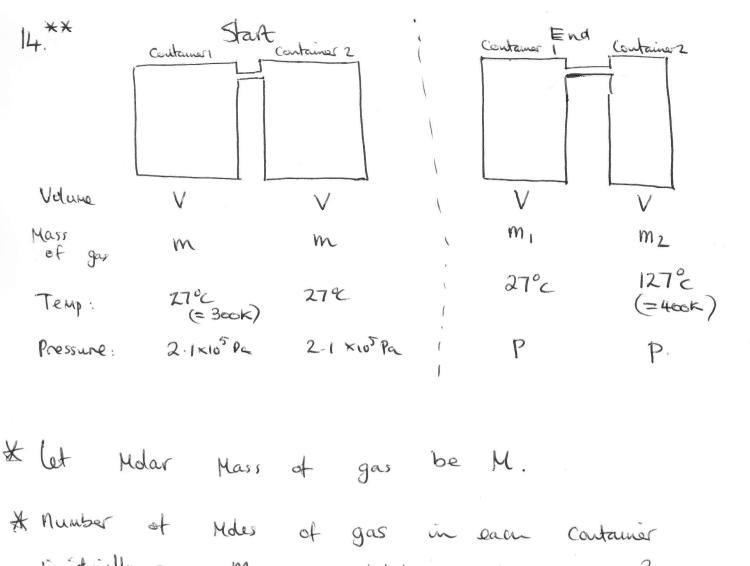
$$P_{i} = P_{i} V_{i} = V_{i} T_{i} = T_{i}$$

$$P_2 = ?$$
 ;  $V_2 = 2V$  ;  $T_2 = 3T$ 

$$\frac{P_1 V_1}{T_1} = \frac{P_2 V_2}{T_2} \Longrightarrow P_2 = \frac{T_2}{T_1} \cdot \frac{V_1}{V_2} \cdot P_1$$

$$P_2 = \frac{3T}{T} \times \frac{V}{2V} \times P$$

$$\frac{p_2}{2} = \frac{3p}{2}$$



A number of Mdes of gas in each container thirtially is 
$$\frac{m}{M}$$
  $\Longrightarrow$  total no. I Holes  $=\frac{2m}{M}$   $\Longrightarrow$   $\frac{m_1+m_2=2m}{M}$   $\Longrightarrow$   $=\frac{2m}{M}$   $\Longrightarrow$ 

\* Finally: 
$$pV = \frac{m_1}{M} R \times 300$$
 (container 1)

\* Finally: 
$$PV = \frac{m_2}{M} R \times 400$$
.

$$\frac{M_1}{M} R \times 300 = \frac{M_2}{M} R \times 400$$

$$\frac{3M_1 = 4M_2}{2M} = M_1 + M_2 = M_1 + \frac{3}{4}M_1 = 1.75M_1$$

$$\frac{1.2.1 \times 10^{5} \times 2V}{M} = \frac{1.75 \text{ M/s}}{1.75 \text{ M/s}} \times R \times 300$$

and 
$$pV = \frac{m_1}{M} \times R \times 300$$

$$\frac{2.1\times10^{5}\times2V}{PV} = 1.75$$

$$P = \frac{2.1 \times 10^5 \times 2}{1.75} = \frac{2.4 \times 10^5 \text{ Pa}}{1.75}$$

## Part 2 - Ideal Gases

$$n = \frac{PV}{RT}$$

$$= \frac{200 \times 10^{3} \times 0.2}{8.31 \times 290}$$

$$= \frac{3}{200 \times 10 \times 0.2}$$

$$= \frac{3}{1.38 \times 10^{-23} \times 290}$$

$$N = 1.00 \times 10^{25}$$

$$= \frac{105 \times 10^{3} \times 0.002}{1.38 \times 10^{-23} \times 290}$$

$$N = \frac{pV}{K_BT}$$

$$= \frac{120 \times 10^{3} \times 0.002}{1.38 \times 10^{-27} \times 290}$$

$$JN = 5.997 \times 10^{22} - 5.25 \times 10^{22}$$
  
=  $7.47 \times 10^{21}$  Moleaules

$$= \frac{8.6 \times 10^{4} \times 3.2 \times 10^{-2}}{8.31 \times (273 + 27)}$$

$$n = 1.10$$
 moles

$$N = \underbrace{pV}_{K_BT}$$

$$= 8.6 \times 10^{4} \times 3.2 \times 10^{2}$$

$$1.38 \times 10^{-23} \times 300$$

$$N = 6.65 \times 10^{23} \text{ Helecules}$$

$$\frac{6.65 \times 10^{23}}{3.2 \times 10^{-2}} = 2.08 \times 10^{25} \text{ Holeanles } / \text{M}^3$$

$$\frac{P_1V_1}{T_1} = \frac{P_2V_2}{T_2}$$

$$\frac{T_2}{P_1} = \frac{P_2}{V_1} \frac{V_2}{V_1} T_1$$

$$= 2 \times 2 \times (273 + 30)$$

$$= 1212 K$$

$$= 939 °C$$

$$\Rightarrow$$
  $n = \frac{PV}{RT}$ 

$$= \frac{2.00 \times 10^{5} \times 1.50 \times 10^{3}}{8.31 \times 303}$$

$$2 \times 119145.489 = 2.38 \times 10^{5} g$$

$$= 2.38 \times 10^{2} \text{ kg}$$

$$\frac{N}{V} = \frac{P}{K_BT}$$

M

No. of Molecules

per M3

$$\frac{N}{V} = \frac{1.01 \times 10^{5}}{1.38 \times 10^{-23} \times 273}$$

$$\frac{P_1V_1}{T_1} = \frac{P_2V_2}{T_2}$$

$$V_2 = \frac{P_1}{P_2} \cdot \frac{T_2}{T_1} \cdot V_1$$

$$V_1 = 25 \, dm^3 = 25 \times (dm)^3$$
  
=  $25 \times (10^1 \, m)^3$   
=  $25 \times 10^{-3} \, m^3$ 

$$V_2 = \frac{1 \times 10^6}{5 \times 10^5} \times \frac{600}{300} \times 25 \times 10^{-3}$$

$$V_2 = 0.1 \, \text{M}^3$$

7. 
$$V = 100 l = 0.1 \text{ m}^3$$

$$T = \frac{PV}{\Pi R}$$

$$= \frac{1.01 \times 10^5 \times 0.1}{3 \times 8.31}$$

$$= 405 \, \mathrm{K}$$

8. 
$$PV = nRT \implies V = \frac{nRT}{P}$$

$$\rho = \frac{m}{V} = \frac{mP}{nRT}$$

$$\frac{1 \times 8.31 \times 273}{1 \times 8.31 \times 273}$$

$$\rho = 1.29 \text{ kg/m}^3$$

9. 
$$N = \frac{N}{N_A} = \frac{6.02 \times 10^{22}}{6.02 \times 10^{23}}$$

ii) 
$$M = n M^4$$
 mdar mass
$$= 0.1 \times 3.55 \times 10^{-2}$$

$$= 3.55 \times 10^{-3} \text{ kg}$$

$$V = \frac{nRT}{P}$$

$$1.V = 2.095... \times 10^{-3}$$

$$= 2.10 \times 10^{-3} \text{ m}^3$$

$$N_L = \frac{N}{V} = \frac{P}{\kappa_B T}$$

$$N_{L} = \frac{1.01 \times 10^{5}}{1.38 \times 10^{-23} \times 273}$$

$$L^{3} = 3.73 \times 10^{-26} \, \text{m}^{3}$$

$$L = 3.34 \times 10^{-9} \, \text{m}$$

(iii)

Volume of Koleenle = 
$$\frac{4}{3}\pi r^3$$

$$= \frac{4}{3} \pi \times (1.25 \times 10^{-10})^{3}$$

$$= 8.18 \times 10^{-30} \text{ m}^{3}$$

11.\* X->Y is an Isothernal expansion

as Pressure halves but volume doubles,

hence PV = constant.

Y-> Z " an iso anone themal increase, as V remains constant.

Hence,  $\frac{P_1}{T_1} = \frac{P_2}{T_2}$ 

 $T_2 = \frac{P_2}{P_1} \cdot T_1$ 

 $= \frac{0.75 \times 10^5}{0.5 \times 10^5} \times 300$ 

 $T_2 = 450 \,\mathrm{K}$ 

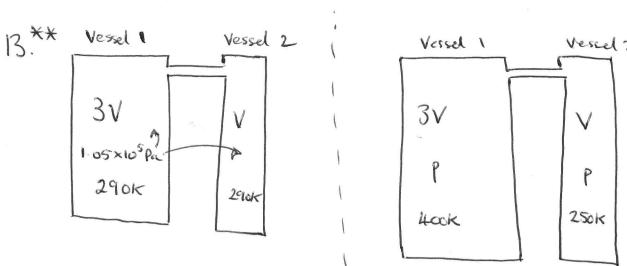
He: n<sub>He</sub> = 
$$\frac{4}{4}$$
 = 1 mole

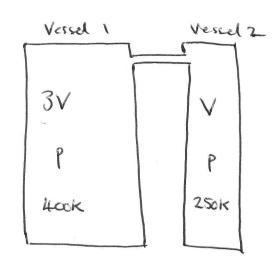
$$n = n_{H_2} + n_{He}$$

$$= 2 \text{ mdes}$$

$$P = \frac{\Lambda RT}{V}$$

$$= 2 \times 8.31 \times 320$$





X let M be the Molar Mass of gas.

M, = mas, of gas in Vessel 1 after heating M2 = mass " " " " 2 after cooling

 $M = M_1 + M_2$   $\Longrightarrow$   $N = \frac{M}{M}$ 

\* after : Vessel 1 Vessel 2  $3pV = \frac{m_1}{M} R \times 400$ ;  $pV = \frac{m_2}{M} R \times 250$ 

 $\frac{400 \, \text{M}_1}{3} = 250 \, \text{M}_2 \implies 8 \, \text{M}_1 = 15 \, \text{H}_2$ 

$$8m = 8m_1 + 8m_2$$

$$= 15m_2 + 8m_2$$

$$= 23m_2$$

$$M = \frac{23m_2}{8}$$

\* before: both vessels: 
$$p \times 4V = \frac{M}{M}RT$$
1.05×10<sup>5</sup>Pa 290K

$$= 290 \times \frac{23m_2}{8M} R$$

$$PV = \frac{M_2}{M} R \times 250$$
 and  $4.2 \times 10^5 V = 290 \times \frac{23 M_2}{8 M} R$ 

$$\frac{P}{4.2\times10^5} = \frac{250}{290\times23/8} \Rightarrow P = 1.26\times10^5 \text{ Pa}$$

1. 
$$E = \frac{3}{2} k_B T$$

$$E = 2.07 \times 10^{22} \text{ J}$$

2. 
$$E = \frac{3}{2} k_B T$$

$$= 2 \times 6.21 \times 10^{-21}$$

$$3 \times 1.38 \times 10^{-23}$$

3. 
$$E = \frac{3}{2} k_B T$$

$$E = \frac{3}{2} \times 1.38 \times 10^{-23} \times 288$$

All three goises with have the Same kinetie energy if we assure trey behave as idéal gases.

$$N = \frac{PV}{RT}$$

$$= \frac{200 \times 10^{3} \times 8 \times 10^{-4}}{8.31 \times 300}$$

$$M = nM = 0.0641797 \times 4\times10^{-3}$$

ii) 
$$E = \frac{3}{2} k_B T$$

iii) 
$$E_{\text{Hol}} = N \times \frac{3}{2} k_{\text{B}}T = \frac{3}{2} N k_{\text{B}}T$$

5. 
$$E = \frac{3}{2} K_B T = energy of one Holeaule.$$

$$\frac{1}{16} = \frac{1}{16} = \frac{1}{16}$$

$$= \frac{3}{2}RT$$

$$= 1.5 \times 8.31 \times 273$$

$$E = \frac{3}{2} k_B T = \frac{1}{2} M \langle v^2 \rangle$$

$$T = \frac{M \langle v^2 \rangle}{3k_B}$$

If 
$$V \Rightarrow 2V$$
, hen  $\langle V^2 \rangle \Rightarrow 4\langle V^2 \rangle$ 

$$T' = 4 \times \frac{M \langle v^2 \rangle}{3k_B}$$

4.

7. 
$$E = \frac{1}{2}M\langle v^2 \rangle = \frac{3}{2}k_BT$$

$$\sqrt{\langle v^2 \rangle} = \sqrt{\frac{3k_BT}{m}}$$

$$= \int \frac{3 \times 1.38 \times 10^{-23} \times (273 - 12)}{5.3 \times 10^{-26}}$$

$$\sqrt{\langle V^2 \rangle} = 452 \text{ M/s}$$

8. 
$$E = \frac{1}{2}M\langle v^2 \rangle = \frac{3}{2}K_BT$$

$$= 6134.8$$

$$\frac{1}{2}M_{x}\langle V_{x}^{2}\rangle = \frac{3}{2}k_{B}T = \frac{1}{2}M_{y}\langle V_{y}^{2}\rangle$$

$$\therefore M_X \langle V_X^2 \rangle = M_Y \langle V_Y^2 \rangle$$

$$\frac{111}{111} \frac{1}{111} \frac{1}{111} = \frac{1}{111} \frac{1}{111}$$

$$\frac{\langle V_x^2 \rangle}{\langle V_y^2 \rangle} = \sqrt{\frac{M_Y}{M_X}}.$$

$$\sqrt{\frac{\langle V_x^2 \rangle}{\langle V_y^2 \rangle}} = \frac{1}{2}$$

if 
$$p \rightarrow 2p$$
, hen  $T \rightarrow 2T$ 

$$\frac{1}{2}MV^2 = \frac{3}{2}k_BT$$

When heated: 
$$\frac{1}{2}M(v')^2 = \frac{3}{2}k_B(2T)$$

$$= 2 \times \frac{3}{2} k_{B}T$$

$$\frac{1}{2} MV^{2}$$

$$\frac{1}{2}M(v')^{2} = 2x \frac{1}{2}Mv^{2}$$

$$= \frac{500\times10^3\times5\times10^{-3}}{1\times8.31}$$

$$= \frac{5.05 \times 10^{-3} \, \text{M}^3}{}$$

$$T = \frac{pV}{NR} = \frac{200 \times 10^3 \times 5.05 \times 10^{-3}}{1 \times 8.31}$$