

Title Of The Paper

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1 Abstract

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2 Introduction

Free surface flows occur in many important and different applications such as; tsunamis, storm surges, tidal bores and riverine flooding. As these surfaces vary

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4 more rapidly the assumption of hydrostatic pressure in a fluid column breaks
 5 down and vertical acceleration inside the fluid becomes important. Therefore it
 6 is no longer fully justified to use the shallow water wave equations in this flow
 7 regime because they enforce a hydrostatic pressure distribution. At the other
 8 end numerical methods for the Euler equations are not yet computationally
 9 efficient enough to deal with these problems over large domains to high accuracy.
 10 Thus a family of equations has been developed to approximate this regime where
 11 fluid is still shallow () but now we also allow different nonlinearity parameters
 12 (), called the Boussinesq type models.

13 **3 One Dimensional Serre Equations**

14 The Serre equations are derived as an approximation to the full Euler equations
 15 by depth integration as in []. They can also be seen as an asymptotic expansion
 16 to the Euler equations as well []. The former is more consistent with the
 17 perspective from which numerical methods will be developed while the latter
 18 indicates the appropriate regions in which to use these equations as a model for
 19 fluid flow. Restricting to the two dimensional problem, the Euler equations are.

20 **3.1 Conservative Form**

21 **3.2 Bounding Wave Speeds**

22 **4 Hybrid Finite Difference, Finite Volume Method** 23 **Solver**

24 **4.1 First Order**

25 **4.2 Second Order**

26 **4.3 Third Order**

27 **5 Numerical Experiments**

28 **5.1 Soliton**

29 **5.2 Experimental Data**

30 **5.3 Dam Break**

31 [1]

32 **References**

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