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§ Overview of High-Frequency Electronic Circuits

1.1 Transceiver Architecture (transceiver \Rightarrow transmitter + receiver)

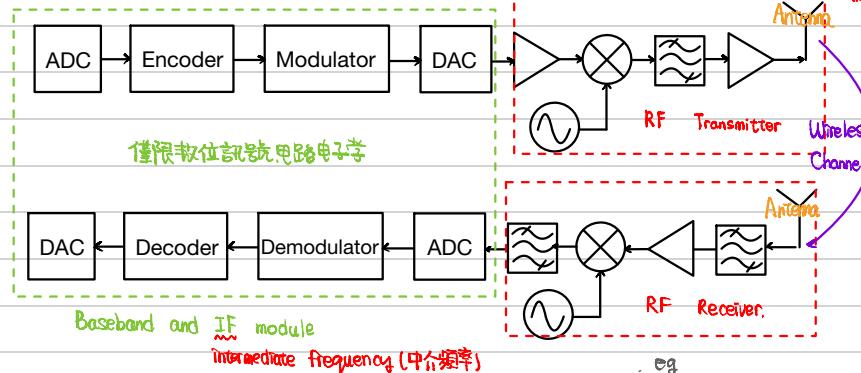
• Typical Microwave Communication System.

Definition of Radio frequency $\Rightarrow A \cos(\omega t + \phi)$. 其中 $3k = f \leq 300$ GHz.

$$\omega = 2\pi f$$

$$10^3 \leq \lambda \leq 10^6 \text{ m.}$$

Block Diagram.



*補充.

VHF: 3~30K.

LF: 30K~300K.

MF: 300K~3M.

HF: 3M~30M.

VHF: 30M~300M

JHF: 300M~3G.

SHF: 3G~30G.

EHF: 30G~300G.

微波
波長
 $\lambda = 10^{-3} \text{ m.}$

毫米波
目前通訊頻帶

4G, LTE.

1.71GHz~2.71GHz.
(bandwidth=700MHz~960MHz)

WiFi, BlueTooth.

2.4G, 5.8G.

GPS, 1.575GHz.

Satellite 11.7GHz.

$$\text{Parity Bit} = \begin{cases} P_1 = \text{mod}(B_1, B_2) \\ P_2 = \text{mod}(B_2, B_3) \\ P_3 = \text{mod}(B_1, B_3) \end{cases}$$

e.g.

B_1	B_2	B_3	原資訊
0	0	0	
0	0	1	
0	1	0	
0	1	1	
1	0	0	
1	0	1	
1	1	0	
1	1	1	

▼ " " " Free Space

○ " " " 錯誤

TX Baseband Modulation Idea

- transforming baseband signal to intermediate frequency (several KHz → hundreds MHz)

- Modulation process:

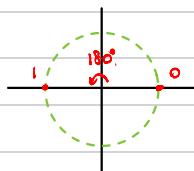
$$U_c(t) = A \cos(\omega_c t + \phi) \Rightarrow \begin{cases} \text{basic Method:} \\ \text{Amplitude Shift Keying.} \\ \text{Phase Shift Keying.} \\ \text{Frequency Shift Keying.} \end{cases} \xrightarrow{\text{Quadrature Amplitude Modulation.}}$$

Phase Shift Keying (PSK)

BPSK.

Digital	Modulated Carrier
0	$A \cos(\omega t + 0^\circ)$
1	$A \cos(\omega t + 180^\circ)$

constellation chart



△ 8-PSK.

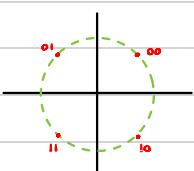
000	$A \cos(\omega t + \phi_0)$
001	$A \cos(\omega t + \phi_1)$
010	$A \cos(\omega t + \phi_2)$
011	$A \cos(\omega t + \phi_3)$
100	$A \cos(\omega t + \phi_4)$
101	$A \cos(\omega t + \phi_5)$
110	$A \cos(\omega t + \phi_6)$
111	$A \cos(\omega t + \phi_7)$

⇒ 角度 $(\phi_i - \phi_0) = \frac{360}{8} = 45^\circ$
可利用 phasor transform 轉成
 $A < \phi_i$

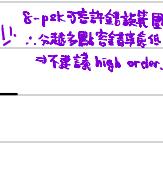
QPSK

Digital	Modulated Carrier
00	$A \cos(\omega t + 45^\circ)$
01	$A \cos(\omega t + 135^\circ)$
10	$A \cos(\omega t - 45^\circ)$
11	$A \cos(\omega t - 135^\circ)$

constellation chart

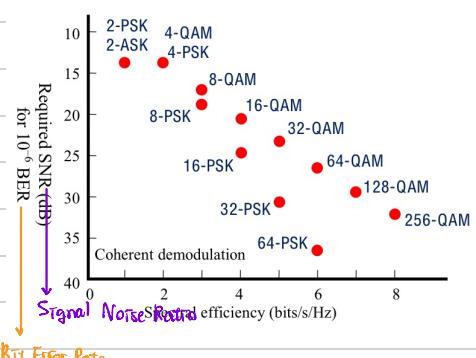
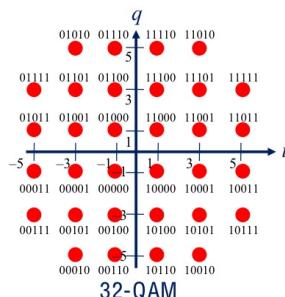
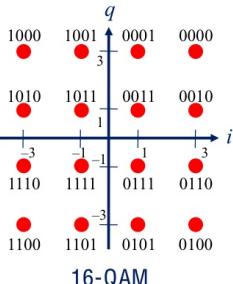


constellation chart



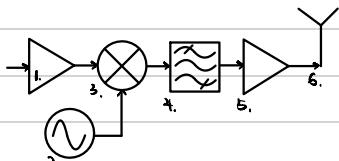
• Amplitude Shift Keying ⇒ usually don't use this method

• Quadrature amplitude modulation ⇒ using Amplitude . Phase



∴ 可得知傳率 bit ↑ 其訊號功率 > 噪音功率 其 BER
才會得到 10^{-6} 之錯誤率

• TX RF Band.



1. IF Amplifier: Enhance Signal Level. with modulator produce insertion loss

2. Oscillator: Generate precise controlled carrier frequency "f_{lo}".
产生任意频率，生成精确的正弦波

3. Mixer: Up-converting intermediate signal to RF.

Output of idealized mixer
frequency convergent oscillator 的频率 原中介频率放大器

$$V_{RF}(t) = K V_{LO}(t) V_{IF}(t) = K \cos(\omega_L f_{LO} t) \cos(\omega_R f_{RF} t)$$

输出信号 = $\frac{K}{2} [\cos(2\pi(f_{LO}-f_{RF})t) + \cos(2\pi(f_{LO}+f_{RF})t)]$

4. RF Filter: frequency conversion result from nonlinearity of transistor or diode.

↓ Select the wave only $f_{LO} + f_{RF} = f_{RF}$. generate wide variety of harmonic wave

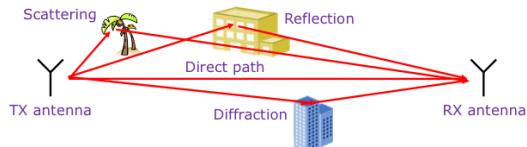
5. Power Amplifier: Increasing output power of transmitter.

6. TX Antenna: Converting modulated carrier signal from transmitter to propagating EM plane wave.

↓ PA 传递 $V(x,t), I(x,t)$ 给 Antenna 生成 Electromagnetic Wave. (传播至 channel) $E(t,r) = \frac{E_0}{r} \cos(\omega t - kr - \phi)$
signal fading propagates

• Channel.

• Wireless Propagation (considering free space)



令 $f = 2.4 \text{ GHz}$, $\lambda = 12.5 \text{ cm}$.

by considering size of Object

1. $O \gg \lambda$ ($O \geq 10\lambda$): reflection \Rightarrow 反射, size of object

2. $\frac{\lambda}{10} < O < 10\lambda$: scattering \Rightarrow 散射,

3. $\lambda \gg O$, ($O < \frac{\lambda}{10}$): diffraction \Rightarrow 網射,

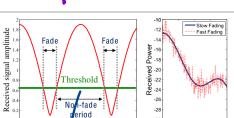
* most important issues of wireless propagation.

1. Multipath effects: fading, intersymbol interference, path loss.

2. Fading: amplitude of received signal fluctuates severely.

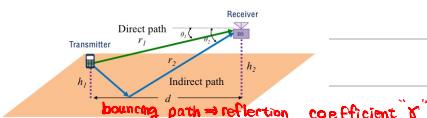
衰弱 (Amplitude)

Ex.



低於 threshold 造成無法辨認 noise - signal.

example of fading.



$$\Rightarrow \text{direct path} \Rightarrow r_1 = \sqrt{d^2 + (h_a - h_b)^2} = d + \frac{(h_a - h_b)^2}{2d} \text{ 为实数 (虚元)}$$

$$\text{indirect path due reflection} \Rightarrow r_2 = \sqrt{d^2 + (h_a + h_b)^2} = d + \frac{(h_a + h_b)^2}{2d}$$

$$\text{assuming reflection coefficient } R = |R|e^{j\phi}$$

\Rightarrow received field, in phasor domain. ($E = E_0 \frac{e^{j\omega t}}{r} \cos(\omega t - kr + \phi)$)

$$\vec{E} = \frac{E_0}{r_1} e^{-jk r_1} + \frac{E_0}{r_2} e^{-jk r_2} \quad \therefore E_r = \frac{E_0 e^{-jk r_1}}{r_1} + \frac{E_0 R e^{-jk r_2}}{r_2}$$

濘数, $k = \frac{2\pi}{\lambda}$ (+公尺有多少个波长).

$$\text{或 } \frac{2\pi}{\lambda} \quad (+一圈有多少个波长)$$

Ex. $r_1 = 100 \lambda, r_2 = 100 \lambda, \phi = 0^\circ$ $\Rightarrow E_r = E_0 \frac{e^{-jk r_1}}{r_1} + E_0 R e^{-jk r_2} = E_0 \frac{e^{-jk r_1}}{r_1}$

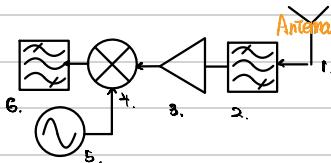
Assuming $r_1 \approx r_2 \Rightarrow$ 其长度约於波长相似, 但不可直接化成二倍

$$E_r = \frac{E_0 e^{-jk r_1}}{r_1} + \frac{E_0 R e^{-jk r_2}}{r_2} = \frac{E_0 e^{-jk r_1}}{r_1} (1 + R e^{-jk(r_2 - r_1)})$$

$$\text{将繁杂项化简, } R = \frac{E_0}{r_1} (1 + |R| e^{j(k \frac{2h_a h_b}{d} - \phi)}) = \frac{E_0 e^{-jk r_1}}{r_1} (1 + |R| (\cos(\frac{k 2h_a h_b}{d} - \phi) - j \sin(\frac{k 2h_a h_b}{d} - \phi)))$$

$$\therefore \text{in time domain, } E_r(t) = \operatorname{Re}\{\vec{E}_r\} = \frac{E_0}{r_1} \cos(\omega t - kr_1)(1 + |R| (\cos(\frac{k 2h_a h_b}{d} - \phi))) + \frac{E_0}{r_1} \sin(\omega t - kr_1)(|R| \sin(\frac{k 2h_a h_b}{d} - \phi))$$

• RX RF Band.



1. RX Antenna: Receives EM Wave with multipath propagation, on very broad frequency range.
本身具有些許濾波功能(低頻雜訊濾除)

2. Bandpass Filter: Reject interfering signals at undesired frequencies.

→ Antenna 會把部份諧波接收(但實際不需要), 要 BPF 濾除。
可以減少高功率的干擾訊號被敏感的放大器, 超載的機率。

3. Low - Noise Amplifier: Magnifying signal received, which is weak, noisy, only for receiver.

4.5. Mixer and Oscillator: Local Carrier to down-convert the RF signal back to IF
that processed by baseband module

→ RF, LO 的頻率很相似 $\Rightarrow f_{RF} + f_{LO} = 2f_{RF}$, $f_{RF} - f_{LO} \Rightarrow$ baseband.

通常會串接多級來有更好的特性。

若沒有使用 LNA, 則 mixer 的 noise, loss 特性會占接收端累的一大部份

6. Filter: Remove any undesired harmonic, spurious products result from mixing process.

▲ Conclusion.

• RF front ends required low loss, low cost, light weight, high performance, power efficient

⇒ can be integrated in IC except Antenna.

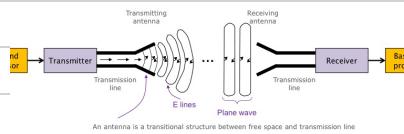
• RX Baseband

Demodulator: Retrieving message from IF signal

Decoder: retrieve original message from channel bits received.

1.2 How does an Antenna Work

• Basic Structure of Antenna.



Receiving: input power comes from transmitter.

⇒ impedance matching, return loss, operational bandwidth.

Radiating: input power toward desired direction

⇒ patterns, directivity, beamwidth, radiation efficiency.

scenarios don't produce radiation.

⇒ Gauss's Law, charge not moving
Produce Static E-field.

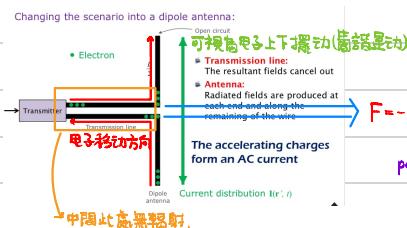
⇒ Biot-Savart Law, charges moved constant velocity
Produce Static Magnetic field.

produce radiation.

Time-Varying current.

Acceleration and deceleration of charge

• Antenna Workflow.



$$\therefore m \cdot \frac{d^2x}{dt^2} + kx = 0, \text{ let } x = e^{j\omega t}$$

$$\Rightarrow m \lambda^2 e^{j\omega t} + k e^{j\omega t} = 0.$$

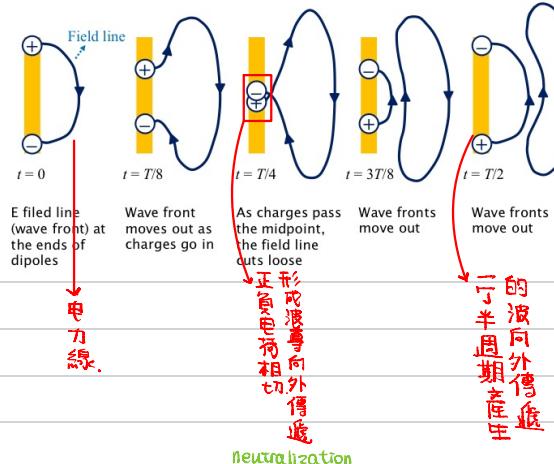
position of electron (current) $\lambda = \pm j \sqrt{\frac{k}{m}}$

$$\therefore x = c_1 \cos \left[\frac{\sqrt{k}}{\sqrt{m}} t \right] + c_2 \sin \left[\frac{\sqrt{k}}{\sqrt{m}} t \right]$$

$$= A \cos \left(\frac{\sqrt{k}}{\sqrt{m}} t + \phi \right)$$

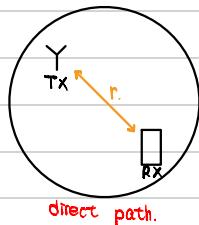
→ 形成一類似 sinusoid 波。

A closer look to the radiation mechanism:



1.3 Link Budget.

• Friis Transmission Formula.



Transmitting Antenna

Transmitting Power: P_t

Antenna Gain: G_t

Receiving Antenna.

Receiving Power: P_r

Antenna Gain: G_r

Free Space

Distance: r

Frequency: f_0

common sense.

def. Friis Formula

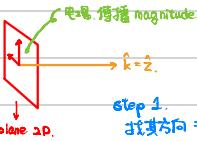
$$\frac{P_r}{P_t} = G_t G_r \left(\frac{\lambda_0}{4\pi r} \right)^2$$

$$\lambda_0 = \frac{C}{f_0} \Rightarrow f_0 = 1 \text{ GHz}, \lambda_0 = 30 \text{ cm}.$$

$$\therefore 2.4 \text{ GHz}, \lambda_0 = \frac{30}{2.4} = 12.5 \text{ cm}.$$

修正
修正

if polarizations mismatch.
电场方向.



$$P_r = P_t G_t G_r \left(\frac{\lambda_0}{4\pi r} \right)^2 |E|^2 |E_r|^2$$

電場强度 magnitude.

$\hat{k} = \hat{z}$.

ex. Transmitt.

$$\vec{E} = (E_0 \hat{x} + E_0 \hat{y} \cos 90^\circ) e^{j k z}$$

Step 1:

$$\text{电场方向} \Rightarrow \vec{E} = \langle E_0, E_0 \cos 90^\circ \rangle$$

Step 2:

$$\text{normalize } \langle 1, j \rangle = \left\langle \frac{1}{\sqrt{2}}, \frac{j}{\sqrt{2}} \right\rangle$$

Step 3:

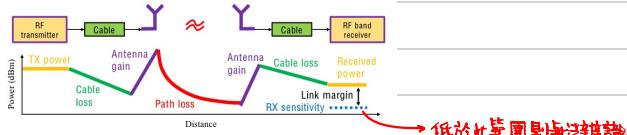
$$\text{非 polarization loss factor: } |E| \cdot |E_r| = |j| = 1.$$

Receive

$$\vec{E} = \langle E_0 \cos 90^\circ, -E_0 \cos 180^\circ \rangle e^{-jkz}$$

$$\vec{E} = \langle E_0, -E_0 \rangle$$

• Objective of Link Budget Calculation



→ by Friis Equation, $P_r = P_t G_t G_r \left(\frac{\lambda_0}{4\pi r} \right)^2$.

we can have more precise estimation of path loss = $\left(\frac{\lambda_0}{4\pi r} \right)^2$.

by breakpoint model:

1. for distance $r \leq r_{\text{break}}$

$$\text{path loss} = \left(\frac{\lambda_0}{4\pi r} \right)^2$$

2. for distance $r > r_{\text{break}}$

$$\text{path loss} = \left(\frac{\lambda_0}{4\pi r_{\text{break}}} \right)^2 \left(\frac{r_{\text{break}}}{r} \right)^n$$

Environment	Path loss exponent n
Free space	2
Urban	2.7–3.5
Shadowed urban	3–5
In-building LOS	1.6–1.8
In-building shadowed	4–6
Factory shadowed	2–3
Retail store	2.2
Office-soft partitions	2.4

Problem 1

Consider an outdoor small cell with $f_c = 2.5$ GHz, cells of radius 10 m, and gains of transmitting and receiving antennas $G_t = 1$ dBi and $G_r = 1$ dBi.

- Using the free-space model, what is the path loss?
- Based on (1), what transmit power is required at the base station in order for all terminals within the cell to receive a minimum power of $0.1 \mu\text{W}$?
- How does the transmit power change if the system frequency is 5 GHz?
- How does the transmit power change if the transmitting distance is 40 m?
- Propose methods to lower the transmit power yet maintaining the transmitting distance.

$$f_c = 2.5 \text{ GHz} \quad \lambda_0 = 12 \text{ cm}$$

$$1. \text{ path loss} = \left(\frac{\lambda_0}{4\pi r} \right)^2 = \left(\frac{12 \times 10^{-3}}{4\pi \cdot 10} \right)^2$$

$$3. f_c = 5 \text{ GHz}, \quad \lambda = 6 \text{ cm}, \quad \therefore \text{Path Loss} = -6 \text{ dB}.$$

$$\text{Tx } 10 \log \Rightarrow P_L = 10 \log \left(\frac{\lambda_0}{4\pi r} \right)^2 = 10 \log \left(\frac{12 \times 10^{-3}}{\pi} \right)^2 = -60.4 \text{ dB}.$$

$$-40 = 10 \log P_t + 1 + -60.4 - 6 \Rightarrow \log P_t = 2.44 \quad P_t = 275.4 \text{ mW}.$$

$$2. P_r = P_t G_t G_r \left(\frac{\lambda_0}{4\pi r} \right)^2$$

$$4. R = 40 \text{ m}, \quad \therefore \text{Path Loss} = -12.04 \text{ dB}.$$

$$10 \log P_r = 10 \log P_t + 1 + -60.4$$

$$-40 = 10 \log P_t + 1 + -60.4 - 12.04 \Rightarrow \log P_t = 3.44 = 275.4 \text{ mW}.$$

$$-40 = 10 \log P_t - 58.4 \Rightarrow \log P_t = 1.84, \quad \therefore P_t = 69 \text{ mW}.$$

Problem 2

An engineer is designing a communication link at 3 GHz. The transmitting and receiving antennas are arranged face-to-face along the z axis. The separation between the two antennas is 1 km. The transmitter uses an antenna with gain of 10 dB, transmitting power of 25 watts. The gain of the receiving antenna is 8 dB. Consider each condition and find the receiving power.

- The transmitting antenna transmits a time-domain E-field of $e(t, z) = E_0 \cos(\omega t - \beta z) \hat{x} - E_0 \cos(\omega t - \beta z) \hat{y}$, whereas the receiving antenna uses a time-domain E-field of $e(t, z) = E_0 \cos(\omega t + \beta z) \hat{x} - E_0 \cos(\omega t + \beta z) \hat{y}$.
- The transmitting antenna transmits a time-domain E-field of $e(t, z) = E_0 \cos(\omega t - \beta z) \hat{x} + E_0 \cos(\omega t - \beta z) \hat{y}$, whereas the receiving antenna uses a time-domain E-field of $e(t, z) = E_0 \cos(\omega t + \beta z) \hat{x} - E_0 \cos(\omega t + \beta z) \hat{y}$.
- The transmitting antenna transmits a time-domain E-field of $e(t, z) = E_0 \cos(\omega t - \beta z) \hat{x} + E_0 \cos(\omega t - \beta z) \hat{y}$, whereas the receiving antenna uses a time-domain E-field of $e(t, z) = E_0 \cos(\omega t + \beta z) \hat{x} - E_0 \cos(\omega t + \beta z) \hat{y} + 90^\circ \hat{z}$.
- Based on (3), consider a doubled separation and do the problem one more time.
- Propose methods to minimize the effect of polarization loss.

$$f_c = 3 \text{ GHz}, \quad \lambda = 10 \text{ cm}.$$

$$P_L = 20 \log \frac{0.1}{4\pi \cdot 1000} = -101.98 \text{ dB}.$$

$$10 \log P_r = 10 \log 25 \times 10^3 + 10 + 8 - 101.98 - \text{polarization}.$$

$$3. \text{ polarization} = < E_0 < \beta z, E_0 < \beta z >, < E_0 < \beta z, E_0 < \beta z + 90^\circ >.$$

$$\Rightarrow < 1, 1 >, < 1, -1 >$$

$$\Rightarrow < 1, 1 >, < -1, -1 >$$

$$(1, j) = 1 - 2j - 1$$

$$= < \frac{-1}{\sqrt{2}}, \frac{1}{\sqrt{2}} >, < \frac{1}{\sqrt{2}}, \frac{-1}{\sqrt{2}} >$$

$$E_T = | < \frac{1}{\sqrt{2}}, \frac{1}{\sqrt{2}} >, < \frac{-1}{\sqrt{2}}, \frac{-1}{\sqrt{2}} > | = | \frac{-1 - j}{2} | = | \frac{-j}{2} | = \frac{1}{2}, \quad 10 \log E_T = -3 \text{ dB}.$$

$$E_T = | < \frac{-1}{\sqrt{2}}, \frac{1}{\sqrt{2}} >, < \frac{1}{\sqrt{2}}, \frac{-1}{\sqrt{2}} > | = 1, \quad 10 \log E_T = 0$$

$$10 \log P_r = 30 + 10 \log 25 + 10 + 8 - 101.98 - 3, \quad \log P_r = -4.3 \text{ dBm}, \quad P_r = 0.05 \mu\text{W}.$$

$$10 \log P_r = 30 + 10 \log 25 + 10 + 8 - 101.98$$

$$\log P_r = -4, \quad \therefore P_r = 0.1 \mu\text{W}, \quad 4. R = 2 \text{ km}, \quad \text{path loss} = 6 \text{ dB}.$$

$$2. \text{ polarization} = < E_0 < -\beta z, E_0 < \beta z >, < E_0 < \beta z, -E_0 < \beta z >.$$

$$10 \log P_r = 30 + 10 \log 25 + 10 + 8 - 101.98 - 6, \quad \log P_r = -4.9 \text{ dBm}, \quad P_r = 0.025 \mu\text{W}$$

$$\Rightarrow < 1, 1 >, < -1, 1 >$$

$$E_T = | < \frac{1}{\sqrt{2}}, \frac{1}{\sqrt{2}} >, < \frac{-1}{\sqrt{2}}, \frac{1}{\sqrt{2}} > | = 0,$$

$$\therefore P_r = 0 \text{ W}.$$

Problem 3

In this problem, you will analyze the path loss in a UWB communication system (3.1–10.6 GHz) by considering different environments and carrier frequencies. The breakpoint model is used to differentiate the path loss behavior before and after a breakpoint distance d_{break} . There are two carrier frequencies used in this system: $f_1 = 4.0 \text{ GHz}$ and $f_2 = 8.0 \text{ GHz}$. The environments considered are urban, with a path loss exponent of 2.7, and indoor line-of-sight, with a path loss exponent of 1.7. The breakpoint distance (d_{break}) for the two environments is 4 m.

- Find the path loss at 10 m at the two frequencies in the environment of urban.
- Find the path loss at 10 m at the two frequencies in the environment of indoor line-of-sight.
- Find the path loss at 10 m at the two frequencies if the environment is free space.
- How does the path loss exponent affect the path loss?
- What role does the breakpoint distance play?

$$f_{c1} = 4 \text{ GHz}, \lambda_1 = 7.5 \text{ cm}$$

$$f_{c2} = 8 \text{ GHz}, \lambda_2 = 3.75 \text{ cm}$$

$$1. PL_{U1} = \left(\frac{\lambda_0}{4\pi d_{break}} \right)^2 \left(\frac{d_{break}}{d} \right)^{2.7} = \left(\frac{7.5 \times 10^{-2}}{4\pi \times 4} \right)^2 \left(\frac{4}{10} \right)^{2.7} = 1.88 \times 10^{-7}$$

$$3. PL_1 = 3.56 \times 10^{-7}$$

$$PL_{U2} = 8.91 \times 10^{-8}$$

$$PL_{I1} = 4.69 \times 10^{-8}$$

$$2. PL_{I1} = \left(\frac{\lambda_0}{4\pi d_{break}} \right)^2 \left(\frac{d_{break}}{d} \right)^{1.7} = 4.68 \times 10^{-7}$$

$$PL_{I2} = 1.17 \times 10^{-8}$$