A1 (5%) Submission due on 18 September 2020 (Friday)

Given
$$\mathbf{X}\mathbf{w} = \mathbf{y}$$
 where $\mathbf{X} = \begin{bmatrix} 1 & 2 \\ 3 & 4 \\ 5 & 6 \\ 7 & 8 \\ 9 & 10 \end{bmatrix}$ and $\mathbf{y} = \begin{bmatrix} 0 \\ 0 \\ 1 \\ 0 \\ 0 \end{bmatrix}$ constitute an example problem. Write a Python routine to find

the least squares solution for \mathbf{w} given arbitrary $\mathbf{X} \in \mathcal{R}^{5 \times 2}$ and $\mathbf{y} \in \mathcal{R}^{5 \times 1}$. Submit your Python code as a function with routine ("def Al_MatricNumber(X, y)") that takes in \mathbf{X} and \mathbf{y} as inputs and generate $(\mathbf{X}^T\mathbf{X})^{-1}$ and \mathbf{w} as outputs in a single file with filename "Al_StudentMatriculationNumber.py". Your Python routine should return the matrix $(\mathbf{X}^T\mathbf{X})^{-1}$ (as numpy array) first and then the least squares solution vector \mathbf{w} (as numpy array). Hint: you will need "import numpy as np" and its matrix manipulation functions.

Please use the python template provided to you. Remember to rename both "A1_StudentMatriculationNumber.py" and "A1_MatricNumber" using your student matriculation number. For example, if your matriculation ID is A1234567R, then you should submit "A1_A1234567R.py" that contains the function "A1_A1234567R". Please do NOT zip/compress your file. Because of the large class size, **points will be deducted if instructions are not followed**. The way we would run your code might be something like this:

```
>> import A1_A1234567R as grading
>> InvXTX, w = grading.A1_A1234567R(X,y)
Marks allocation: InvXTX (2.5%), w (2.5%)
```

Submission folder: LumiNUS >> files >> A1

(The submission folder in LumiNUS will be closed on 18 September at 2359 hour)