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1 algorithm

#include <algorithm> #include <numeric>

$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	Algo	Params	Funcion
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	sort, stable_sort	f, l	ordena el intervalo
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	nth_element	f, nth, l	void ordena el n-esimo, y
			particiona el resto
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	fill, fill_n	f, l / n, elem	void llena [f, l) o [f,
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$			f+n) con elem
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	lower_bound, upper_bound	f, l, elem	
$\begin{array}{cccccccccccccccccccccccccccccccccccc$			
$\begin{array}{cccccccccccccccccccccccccccccccccccc$			
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	binary_search		. ,
		, ,	
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	find, find_if, find_first_of	, ,	it encuentra i \in [f,l) tq. i=elem,
$\begin{array}{cccccccccccccccccccccccccccccccccccc$		/ pred / f2, l2	$\operatorname{pred}(i), i \in [f2, l2)$
replace, replace_if f, l, old cambia old / pred(i) por new / pred, new reverse f, l da vuelta partition, stable_partition f, l, pred pred(i) ad, !pred(i) atras min_element, max_element f, l, [comp] it min, max de [f,l] lexicographical_compare f1,l1,f2,l2 bool con [f1,l1];[f2,l2]	count, count_if	f, l, elem/pred	cuenta elem, pred(i)
		f, l, f2, l2	. , . , . ,
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	replace, replace_if	f, l, old	cambia old / pred(i) por new
$\begin{array}{llll} & \text{partition, stable_partition} & \text{f, l, pred} & \text{pred(i) ad, !pred(i) atras} \\ & \text{min_element, max_element} & \text{f, l, [comp]} & & it \text{min, max de [f,l]} \\ & \text{lexicographical_compare} & & \text{f1,l1,f2,l2} & & bool \text{ con [f1,l1]_i[f2,l2]} \\ \end{array}$			
$\begin{array}{ll} \text{min_element, max_element} & \text{f, l, [comp]} & it \text{ min, max de [f,l]} \\ \text{lexicographical_compare} & \text{f1,l1,f2,l2} & bool \text{ con [f1,l1]_i[f2,l2]} \\ \end{array}$,	
$lexicographical_compare \qquad f1,11,f2,12 \qquad bool \ con \ [f1,11]_i[f2,l2]$	partition, stable_partition		
	•		
	$lexicographical_compare$	f1,l1,f2,l2	
	$next/prev_permutation$	f,l	deja en [f,l) la perm sig, ant
set_intersection, f1, l1, f2, l2, res [res,) la op. de conj	,	f1, l1, f2, l2, res	$[res, \ldots)$ la op. de conj
set_difference, set_union,			
set_symmetric_difference,			
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$		f, l, e / e /	
make_heap hace un heap de [f,l)	_		
is_heap f,l $bool$ es $[f,l)$ un heap		/	
accumulate $f,l,i,[op]$ $T = \sum /oper de [f,l)$			
inner_product $f1, 11, f2, i$ $T = i + [f1, 11) \cdot [f2,)$	inner_product		
partial_sum			
-			Pos. del primer 1 desde la derecha
			Cant. de ceros desde la izquierda.
builtin_ctz unsigned int Cant. de ceros desde la derecha.		0	Cant. de ceros desde la derecha.
builtin_popcount unsigned int Cant. de 1's en x.			
builtin_parity unsigned int 1 si x es par, 0 si es impar.			
builtin_XXXXXXII unsigned ll = pero para long long's.	_builtin_XXXXXXII	unsigned ll	= pero para long long's.

2 Estructuras

2.1 RMQ (static) - MODIFICAR

Dado un arreglo y una operacion asociativa *idempotente*, get(i, j) opera sobre el rango [i, j). Restriccion: LVL \geq ceil(logn); Usar [] para llenar arreglo y luego build().

```
1 struct RMQ{
     #define LVL 10
     tipo vec[LVL] [1<<(LVL+1)];
     tipo &operator[](int p){return vec[0][p];}
     tipo get(int i, int j) {//intervalo [i,j)
       int p = 31-_builtin_clz(j-i);
6
       return min(vec[p][i],vec[p][j-(1<<p)]);
8
     void build(int n) {//O(nlogn)
9
       int mp = 31-__builtin_clz(n);
10
      forn(p, mp) forn(x, n-(1<<p))
11
         vec[p+1][x] = min(vec[p][x], vec[p][x+(1<<p)]);
12
13
   }};
```

2.2 Segment Tree

2.2.1 Segment Tree Recursivo

```
1 //inclusive segment tree [L,R]
2 int T[4 * N];
   void init(int node = 1,int l = 0,int r = n - 1){
     if(1 == r)T[node] = v[1];
     else{
5
       int mid = (1 + r) >> 1;
6
       init(2 * node,1,mid);
       init(2 * node + 1, mid + 1, r);
       T[node] = op(T[2 * node], T[2 * node + 1]);
9
10
11
   void update(int pos,int val,int node = 1,int l = 0,int r = n - 1){
     if(r < pos || 1 > pos)return;
     if(l == r)T[node] = val;
14
     else{
15
       int mid = (1 + r) >> 1;
16
       update(pos,val,2 * node,1,mid);
17
       update(pos, val, 2 * node + 1, mid + 1, r);
18
19
       T[node] = op(T[2 * node], T[2 * node + 1]);
```

```
solo sirve cuando la operacion que realizamos es conmutativa
20
                                                                                       por ejemplo la suma, pero no funciona con la asignacion
21
                                                                                  3
  int query(int x,int y,int node = 1,int l = 0,int r = n - 1){
                                                                                    */
                                                                                  4
^{22}
     if(r < x || 1 > y)return NEUTRO;
                                                                                    //adiciona value al rango [1, r)
23
     if(x <= 1 && r <= y)return T[node];</pre>
                                                                                    void modify(int 1, int r, int value) {// rango [1, r)
                                                                                      for (1 += n, r += n; 1 < r; 1 >>= 1, r >>= 1) {
     else{
25
       int mid = (1 + r) >> 1;
                                                                                         if (l&1) t[l++] += value;
26
       return op(query(x,y,2 * node,1,mid),query(x,y,2 * node + 1,mid + 1,r
                                                                                         if (r&1) t[--r] += value;
27
                                                                                      }
           ));
                                                                                  10
     }
                                                                                 11
28
  |}
                                                                                     //acceder a la posicion
29
                                                                                    int query(int p) {
    2.2.2 ST Iterativo - (Consulta en rango, modificacion a posicion)
                                                                                      int res = 0:
                                                                                 14
                                                                                      for (p += n; p > 0; p >>= 1) res += t[p];
1 //Segment tree iterative [1,r)
                                                                                       return res;
                                                                                  16
  int T[2 * N]:
                                                                                  17
   void init(){
                                                                                     //Si necesitamos actualizar todo lo podemos hacer en O(n)
     for(int i = n; i < 2 * n; i++)T[i] = val[i];
                                                                                     //Y luego acceder a las hojas en O(1)
    for(int i = n - 1; i \ge 1; i--)T[i] = op(T[i << 1], T[i << 1 | 1]);
5
                                                                                    void push() {
6
                                                                                      for (int i = 1; i < n; ++i) {
   int op(int a,int b){
                                                                                        t[i<<1] += t[i];
     //an asociative function
                                                                                        t[i<<1|1] += t[i];
     return a + b;
9
                                                                                        t[i] = 0;
                                                                                 24
10
                                                                                      }
                                                                                 25
   void update(int pos,int u){
                                                                                 26 }
     pos += n;
12
     for(pos >= 1; pos >= 1; pos >= 1)T[pos] = op(T[pos << 1],T[pos << 1
                                                                                                       2.2.4 Segment Tree con Punteros
13
         | 1]);
                                                                                                            2.2.5 Segment Tree 2D
14
15
                                                                                  1 typedef long long 11;
   int query(int 1,int r){
16
                                                                                    struct segmetree{
     1 += n, r += n;
17
                                                                                       int n;
     int ans = NEUTRO;
18
                                                                                       vector<ll>T;
     while(l < r){
                                                                                       segmetree(){n = 0;}
       if(1 \& 1)ans = op(ans,T[1++]);
20
                                                                                       segmetree(int _){
                                                                                  6
       if (r \& 1) ans = op(ans, T[--r]);
                                                                                         n = _{:}
       1 >>= 1,r >>= 1;
22
                                                                                         T.resize(2 * n + 1);
                                                                                  8
     }
23
                                                                                  9
     return ans;
                                                                                       void rupdate(int pos,int value){
                                                                                 10
25 }
                                                                                         pos += n;
                                                                                 11
    2.2.3 ST Iterativo - (Consulta a posicion, modificacion en rango)
                                                                                         T[pos] = value;
                                                                                 12
                                                                                         for(pos >>= 1; pos >= 1; pos >>= 1)
                                                                                 13
1 /*Segment Tree modificar un rango, acceder a una posicion
                                                                                           T[pos] = T[pos << 1] + T[pos << 1 | 1];
                                                                                 14
```

```
if(1 \& 1)ans += T[1++].query(b,t);
15
                                                                                   58
     void update(int pos,int value){
                                                                                             if (r \& 1) ans += T[--r].query(b,t);
                                                                                   59
16
       pos += n;
                                                                                             1 >>= 1, r >>= 1;
                                                                                   60
17
       T[pos] += value;
                                                                                   61
18
       for(pos >>= 1; pos >= 1; pos >>= 1)
                                                                                           return ans;
                                                                                   62
19
         T[pos] = T[pos << 1] + T[pos << 1 | 1];
20
                                                                                   63
     }
                                                                                   64 };
21
     int query(int 1,int r){
^{22}
                                                                                                         2.2.6 Segment Tree Lazy - Suma
       1 += n;r+= n;
23
       int ans = 0;
24
                                                                                                                Segment Tree Lazy - Pintar
       while(1 < r){
25
                                                                                                          2.2.8 Segment Tree Persistente
         if(1 \& 1)ans += T[1++];
26
         if (r \& 1) ans += T[--r]:
27
         1 >>= 1, r >>= 1;
                                                                                    int segcnt = 0;
28
       }
                                                                                      struct segment {
29
       return ans;
30
                                                                                           int 1, r, lid, rid, sum;
    }
31
                                                                                      } segs[2000000];
                                                                                      int build(int 1, int r) {
32
   struct st{
                                                                                           if (1 > r) return -1;
33
     int n;
                                                                                           int id = segcnt++;
34
     vector<segmetree>T;
                                                                                           segs[id].l = 1;
35
     st(){}
36
                                                                                           segs[id].r = r;
     st(int _){
                                                                                           if (1 == r) segs[id].lid = -1, segs[id].rid = -1;
37
       n = _{:}
                                                                                           else {
38
                                                                                   11
       for(int i = 0; i < 2 * n; i++){
                                                                                               int m = (1 + r) / 2:
39
         T.push_back(segmetree(n));
                                                                                               segs[id].lid = build(l , m);
40
                                                                                   13
       }
                                                                                               segs[id].rid = build(m + 1, r); }
41
                                                                                   14
     }
                                                                                           segs[id].sum = 0;
42
                                                                                   15
     void update(int x,int y,int val){
                                                                                           return id; }
43
       x += n:
                                                                                      int update(int idx, int v, int id) {
44
       T[x].update(y,val);
                                                                                           if (id == -1) return -1;
45
                                                                                   18
       segmetree ok;
                                                                                           if (idx < segs[id].1 || idx > segs[id].r) return id;
46
                                                                                   19
       for(x >>= 1: x >= 1: x >>= 1){
                                                                                           int nid = segcnt++;
47
                                                                                   20
         T[x].rupdate(y,T[x << 1].query(y,y + 1));
                                                                                           segs[nid].1 = segs[id].1;
48
                                                                                   21
         T[x].update(y,T[x << 1 | 1].query(y,y + 1));
                                                                                           segs[nid].r = segs[id].r;
49
                                                                                   22
       }
                                                                                           segs[nid].lid = update(idx, v, segs[id].lid);
50
                                                                                   23
     }
                                                                                           segs[nid].rid = update(idx, v, segs[id].rid);
51
                                                                                   24
     11 query(int 1,int b,int r,int t){
                                                                                           segs[nid].sum = segs[id].sum + v;
52
                                                                                   25
       1 += n;
                                                                                           return nid: }
53
                                                                                   26
       r += n;
                                                                                      int query(int id, int 1, int r) {
54
       r++,t++;
                                                                                           if (r < segs[id].1 || segs[id].r < 1) return 0;</pre>
55
                                                                                   28
       11 \text{ ans} = 0LL;
                                                                                           if (1 <= segs[id].l && segs[id].r <= r) return segs[id].sum;</pre>
56
                                                                                   29
       while(1 < r){
                                                                                           return query(segs[id].lid, 1, r) + query(segs[id].rid, 1, r); }
57
                                                                                   30
```

28

2.3 Fenwick Tree

2.3.1 Fenwick Tree 2D

```
11 T[1025][1025];
   int n;
   11 query(int x, int y)
5
6
     11 \text{ res} = 0:
7
     for(int i = x; i \ge 0; i = (i & (i+1)) - 1)
8
           for(int j = y; j >= 0; j = (j & (j+1)) - 1)
9
                res += T[i][j];
10
       return res;
11
12
13
   void update(int x, int y, int val)
14
15
     for(int i = x; i < n; i = (i | (i+1)))
16
           for(int j = y; j < n; j = (j | (j+1)))
17
                T[i][j] += val;
18
19 }
```

2.4 Union Find con rank

```
Complexity: O(N)
  index 0 to n - 1 warning
  Complexity O(N)
5
  #define MAX INSERTE_VALOR_AQUI
  int padre[MAX];
  int rango[MAX];
  void MakeSet(int n){
9
      for (int i = 0 ; i < n ; ++i) {
10
         padre[i] = i; rango[i] = 0; }
11
12
  int Find(int x) {
13
      if(x == padre[x])
14
         return x;
15
      return padre[x] = Find(padre[x]);
16
  }
17
  void UnionbyRank(int x , int y){
```

```
int xRoot = Find(x);
19
       int yRoot = Find(y);
20
      //el padre de ambas componentes sera el de mayor altura
21
      if(rango[xRoot] > rango[yRoot])//X tiene mas altura que Y
22
          padre[vRoot] = xRoot;
23
      }else{//Y} >= X
24
          padre[xRoot] = yRoot;
25
          if(rango[xRoot] == rango[yRoot])//si poseen la misma altura
26
              rango[yRoot]++;//incremento el rango de la nueva raiz
27
      }
28
29 }
                        2.5 BigInteger C++
1 // g++ -std=c++11 "bigint.cpp" -o run
  /***
   Contain a useful big int, overload all operators, including cin, cout,
   comparator, build via string (prefer this metod) or long long, for now
       this not have a
  to_string method
  Problem for practice: UVA 494
   */
8
   // base and base_digits must be consistent
   const int base = 1000000000;
   const int base_digits = 9;
12
   struct bigint {
       vector<int> a;
14
       int sign;
15
16
       bigint():
17
          sign(1) {
18
       }
19
20
       bigint(long long v) {
21
           *this = v;
22
       }
23
24
      bigint(const string &s) {
25
          read(s);
26
       }
27
```

```
void operator=(const bigint &v) {
                                                                                                        res.trim();
29
                                                                                    69
           sign = v.sign;
                                                                                                        return res;
                                                                                    70
30
           a = v.a;
                                                                                    71
31
       }
                                                                                                    return -(v - *this);
                                                                                    72
32
                                                                                               }
                                                                                    73
33
                                                                                               return *this + (-v);
       void operator=(long long v) {
34
                                                                                    74
                                                                                           }
           sign = 1;
35
                                                                                    75
           if (v < 0)
36
                                                                                    76
               sign = -1, v = -v;
                                                                                           void operator*=(int v) {
                                                                                    77
37
           for (; v > 0; v = v / base)
                                                                                               if (v < 0)
38
                                                                                    78
               a.push_back(v % base);
                                                                                                    sign = -sign, v = -v;
39
                                                                                    79
       }
                                                                                               for (int i = 0, carry = 0; i < (int) a.size() || carry; ++i) {
40
                                                                                    80
                                                                                                    if (i == (int) a.size())
41
                                                                                    81
       bigint operator+(const bigint &v) const {
                                                                                                        a.push_back(0);
                                                                                    82
42
           if (sign == v.sign) {
                                                                                                    long long cur = a[i] * (long long) v + carry;
43
                                                                                    83
               bigint res = v;
                                                                                                    carry = (int) (cur / base);
44
                                                                                                    a[i] = (int) (cur % base);
45
                                                                                                    //asm("divl %%ecx" : "=a"(carry), "=d"(a[i]) : "A"(cur), "c
               for (int i = 0, carry = 0; i < (int) max(a.size(), v.a.size
46
                                                                                    86
                    ()) || carry; ++i) {
                                                                                                        "(base)):
                    if (i == (int) res.a.size())
                                                                                               }
                                                                                    87
47
                        res.a.push_back(0);
                                                                                               trim();
                                                                                    88
48
                    res.a[i] += carry + (i < (int) a.size() ? a[i] : 0);
                                                                                           }
49
                                                                                    89
                    carry = res.a[i] >= base;
                                                                                    90
50
                                                                                           bigint operator*(int v) const {
                    if (carry)
                                                                                    91
51
                        res.a[i] -= base;
                                                                                               bigint res = *this;
                                                                                    92
52
               }
                                                                                               res *= v;
                                                                                    93
53
               return res;
                                                                                               return res;
                                                                                    94
54
                                                                                           }
                                                                                    95
55
           return *this - (-v);
                                                                                    96
56
       }
                                                                                           friend pair bigint, bigint bigint bigint &a1, const bigint &
                                                                                    97
57
                                                                                               b1) {
58
       bigint operator-(const bigint &v) const {
                                                                                               int norm = base / (b1.a.back() + 1);
                                                                                    98
59
           if (sign == v.sign) {
                                                                                               bigint a = a1.abs() * norm;
                                                                                    99
60
               if (abs() >= v.abs()) {
                                                                                               bigint b = b1.abs() * norm;
                                                                                   100
61
                    bigint res = *this;
                                                                                               bigint q, r;
                                                                                   101
62
                   for (int i = 0, carry = 0; i < (int) v.a.size() || carry</pre>
                                                                                               q.a.resize(a.a.size());
                                                                                   102
63
                                                                                   103
                        res.a[i] -= carry + (i < (int) v.a.size() ? v.a[i] :
                                                                                               for (int i = a.a.size() - 1; i >= 0; i--) {
                                                                                   104
64
                             0);
                                                                                                    r *= base;
                                                                                   105
                        carry = res.a[i] < 0;</pre>
                                                                                   106
                                                                                                    r += a.a[i];
65
                                                                                                    int s1 = r.a.size() <= b.a.size() ? 0 : r.a[b.a.size()];</pre>
                        if (carry)
                                                                                   107
66
                            res.a[i] += base;
                                                                                                    int s2 = r.a.size() \le b.a.size() - 1 ? 0 : r.a[b.a.size() -
67
                                                                                   108
                    }
                                                                                                         1];
68
```

```
int d = ((long long) base * s1 + s2) / b.a.back();
                                                                                                    for (int i = a.size() - 1; i >= 0; --i)
109
                                                                                       152
                                                                                                        m = (a[i] + m * (long long) base) % v;
                 r -= b * d:
                                                                                       153
110
                 while (r < 0)
                                                                                                    return m * sign;
                                                                                       154
111
                     r += b, --d;
                                                                                               }
                                                                                       155
112
                 q.a[i] = d;
                                                                                       156
113
                                                                                               void operator+=(const bigint &v) {
114
                                                                                       157
                                                                                                    *this = *this + v;
                                                                                       158
115
            q.sign = a1.sign * b1.sign;
                                                                                       159
116
            r.sign = a1.sign;
                                                                                               void operator-=(const bigint &v) {
117
                                                                                       160
            q.trim();
                                                                                                    *this = *this - v;
118
                                                                                       161
            r.trim();
119
                                                                                       162
            return make_pair(q, r / norm);
                                                                                               void operator*=(const bigint &v) {
120
                                                                                       163
                                                                                                    *this = *this * v;
        }
121
                                                                                       164
                                                                                               }
                                                                                       165
122
        bigint operator/(const bigint &v) const {
                                                                                               void operator/=(const bigint &v) {
123
                                                                                       166
            return divmod(*this, v).first;
                                                                                                    *this = *this / v;
124
                                                                                       167
                                                                                               }
        }
125
                                                                                       168
126
                                                                                       169
        bigint operator%(const bigint &v) const {
                                                                                               bool operator<(const bigint &v) const {</pre>
                                                                                       170
127
            return divmod(*this, v).second;
                                                                                                    if (sign != v.sign)
                                                                                       171
128
        }
                                                                                                        return sign < v.sign;</pre>
                                                                                       172
129
                                                                                                    if (a.size() != v.a.size())
130
        void operator/=(int v) {
                                                                                                        return a.size() * sign < v.a.size() * v.sign;</pre>
                                                                                       174
131
            if (v < 0)
                                                                                                    for (int i = a.size() - 1; i >= 0; i--)
                                                                                       175
132
                 sign = -sign, v = -v;
                                                                                                        if (a[i] != v.a[i])
                                                                                       176
133
            for (int i = (int) a.size() - 1, rem = 0; i >= 0; --i) {
                                                                                                             return a[i] * sign < v.a[i] * sign;</pre>
                                                                                       177
134
                 long long cur = a[i] + rem * (long long) base;
                                                                                                    return false;
                                                                                       178
135
                 a[i] = (int) (cur / v);
                                                                                               }
                                                                                       179
136
                 rem = (int) (cur % v);
                                                                                       180
137
            }
                                                                                               bool operator>(const bigint &v) const {
                                                                                       181
138
                                                                                                    return v < *this;
            trim();
                                                                                       182
139
        }
                                                                                       183
140
                                                                                               bool operator<=(const bigint &v) const {</pre>
                                                                                       184
141
        bigint operator/(int v) const {
                                                                                                    return !(v < *this);
                                                                                       185
142
            bigint res = *this;
                                                                                               }
                                                                                       186
143
            res /= v;
                                                                                               bool operator>=(const bigint &v) const {
                                                                                       187
144
                                                                                                    return !(*this < v);</pre>
            return res;
145
                                                                                       188
                                                                                               }
        }
                                                                                       189
146
                                                                                               bool operator==(const bigint &v) const {
                                                                                       190
147
                                                                                                    return !(*this < v) && !(v < *this);
        int operator%(int v) const {
                                                                                       191
148
            if (v < 0)
                                                                                       192
149
                 v = -v:
                                                                                               bool operator!=(const bigint &v) const {
                                                                                       193
150
                                                                                                    return *this < v || v < *this;
            int m = 0;
151
                                                                                       194
```

```
while (pos < (int) s.size() && (s[pos] == '-' || s[pos] == '+'))
        }
195
                                                                                      238
                                                                                                        {
196
        void trim() {
                                                                                                       if (s[pos] == '-')
197
                                                                                      239
             while (!a.empty() && !a.back())
                                                                                                           sign = -sign;
198
                                                                                      240
                 a.pop_back();
                                                                                                       ++pos;
199
                                                                                      241
            if (a.empty())
                                                                                      242
200
                 sign = 1;
                                                                                                  for (int i = s.size() - 1; i >= pos; i -= base_digits) {
                                                                                      243
201
        }
                                                                                                       int x = 0:
202
                                                                                      244
                                                                                                       for (int j = max(pos, i - base_digits + 1); j <= i; j++)
203
                                                                                      245
                                                                                                           x = x * 10 + s[j] - '0';
        bool isZero() const {
204
                                                                                      246
            return a.empty() || (a.size() == 1 && !a[0]);
                                                                                                       a.push_back(x);
205
                                                                                      247
                                                                                                  }
        }
206
                                                                                      248
                                                                                                  trim();
207
                                                                                      249
        bigint operator-() const {
                                                                                              }
                                                                                      250
208
            bigint res = *this;
                                                                                      251
209
            res.sign = -sign;
                                                                                              friend istream& operator>>(istream &stream, bigint &v) {
210
                                                                                      252
            return res;
                                                                                                  string s;
211
                                                                                      253
        }
                                                                                                  stream >> s;
212
                                                                                                  v.read(s):
                                                                                      255
213
        bigint abs() const {
                                                                                                  return stream;
214
            bigint res = *this;
                                                                                              }
                                                                                      257
215
            res.sign *= res.sign;
216
                                                                                      258
                                                                                              friend ostream& operator<<(ostream &stream, const bigint &v) {</pre>
            return res;
                                                                                      259
217
        }
                                                                                                  if (v.sign == -1)
                                                                                      260
218
                                                                                                       stream << '-';
                                                                                      261
219
                                                                                                  stream << (v.a.empty() ? 0 : v.a.back());
        long longValue() const {
                                                                                      262
220
                                                                                                  for (int i = (int) v.a.size() - 2; i >= 0; --i)
            long long res = 0;
                                                                                      263
221
            for (int i = a.size() - 1; i >= 0; i--)
                                                                                                       stream << setw(base_digits) << setfill('0') << v.a[i];</pre>
                                                                                      264
222
                 res = res * base + a[i];
                                                                                                  return stream;
                                                                                      265
223
            return res * sign;
                                                                                              }
                                                                                      266
224
        }
                                                                                      267
225
                                                                                              static vector<int> convert_base(const vector<int> &a, int old_digits
                                                                                      268
226
        friend bigint gcd(const bigint &a, const bigint &b) {
                                                                                                   . int new_digits) {
227
            return b.isZero() ? a : gcd(b, a % b);
                                                                                                  vector<long long> p(max(old_digits, new_digits) + 1);
                                                                                      269
228
        }
                                                                                                  p[0] = 1;
                                                                                      270
229
        friend bigint lcm(const bigint &a, const bigint &b) {
                                                                                                  for (int i = 1; i < (int) p.size(); i++)</pre>
                                                                                      271
230
            return a / gcd(a, b) * b;
                                                                                                       p[i] = p[i - 1] * 10;
231
                                                                                      272
        }
                                                                                                  vector<int> res:
                                                                                      273
232
                                                                                                  long long cur = 0;
                                                                                      274
233
        void read(const string &s) {
                                                                                                  int cur_digits = 0;
                                                                                      275
234
            sign = 1;
                                                                                                  for (int i = 0; i < (int) a.size(); i++) {
235
                                                                                      276
            a.clear();
                                                                                                       cur += a[i] * p[cur_digits];
236
                                                                                      277
            int pos = 0;
                                                                                                       cur_digits += old_digits;
237
                                                                                      278
```

```
while (cur_digits >= new_digits) {
279
                                                                                   322
                    res.push_back(int(cur % p[new_digits]));
                                                                                               for (int i = 0; i < (int) r.size(); i++)
                                                                                   323
280
                    cur /= p[new_digits];
                                                                                                   res[i + k] += r[i];
281
                                                                                   324
                    cur_digits -= new_digits;
                                                                                               for (int i = 0; i < (int) a1b1.size(); i++)</pre>
282
                                                                                   325
                }
                                                                                                   res[i] += a1b1[i];
283
                                                                                   326
                                                                                               for (int i = 0; i < (int) a2b2.size(); i++)</pre>
                                                                                   327
284
                                                                                                   res[i + n] += a2b2[i];
            res.push_back((int) cur);
                                                                                   328
285
            while (!res.empty() && !res.back())
                                                                                               return res;
286
                                                                                   329
                res.pop_back();
                                                                                           }
287
                                                                                   330
            return res;
288
                                                                                   331
       }
                                                                                           bigint operator*(const bigint &v) const {
289
                                                                                   332
                                                                                               vector<int> a6 = convert_base(this->a, base_digits, 6);
290
                                                                                   333
        typedef vector<long long> vll;
                                                                                               vector<int> b6 = convert_base(v.a, base_digits, 6);
291
                                                                                   334
                                                                                               vll a(a6.begin(), a6.end());
                                                                                   335
292
        static vll karatsubaMultiply(const vll &a, const vll &b) {
                                                                                               vll b(b6.begin(), b6.end());
                                                                                   336
293
            int n = a.size();
                                                                                               while (a.size() < b.size())</pre>
294
                                                                                   337
            vll res(n + n):
                                                                                                   a.push_back(0);
295
                                                                                   338
            if (n <= 32) {
                                                                                               while (b.size() < a.size())</pre>
296
                                                                                   339
                for (int i = 0; i < n; i++)
                                                                                                   b.push_back(0);
                                                                                   340
297
                    for (int j = 0; j < n; j++)
                                                                                               while (a.size() & (a.size() - 1))
                                                                                   341
298
                        res[i + j] += a[i] * b[j];
                                                                                                   a.push_back(0), b.push_back(0);
                                                                                   342
299
                                                                                               vll c = karatsubaMultiply(a, b);
                return res;
300
                                                                                   343
            }
                                                                                               bigint res;
                                                                                   344
301
                                                                                               res.sign = sign * v.sign;
                                                                                   345
302
            int k = n \gg 1;
                                                                                               for (int i = 0, carry = 0; i < (int) c.size(); i++) {
                                                                                   346
303
            vll a1(a.begin(), a.begin() + k);
                                                                                                   long long cur = c[i] + carry;
                                                                                   347
304
                                                                                                   res.a.push_back((int) (cur % 1000000));
            vll a2(a.begin() + k, a.end());
                                                                                   348
305
            vll b1(b.begin(), b.begin() + k);
                                                                                                   carry = (int) (cur / 1000000);
                                                                                   349
306
           vll b2(b.begin() + k, b.end());
                                                                                   350
307
                                                                                               res.a = convert_base(res.a, 6, base_digits);
                                                                                   351
308
            vll a1b1 = karatsubaMultiply(a1, b1);
                                                                                               res.trim();
                                                                                   352
309
            vll a2b2 = karatsubaMultiply(a2, b2);
                                                                                               return res;
                                                                                   353
310
                                                                                           }
                                                                                   354
311
            for (int i = 0; i < k; i++)
                                                                                   355
                                                                                      };
312
                a2[i] += a1[i];
                                                                                   356
313
            for (int i = 0; i < k; i++)
                                                                                      int main() {
                                                                                   357
314
                b2[i] += b1[i];
                                                                                           bigint a=0;
315
                                                                                   358
                                                                                           359
316
            vll r = karatsubaMultiply(a2, b2);
                                                                                           bigint b;
                                                                                   360
317
           for (int i = 0; i < (int) a1b1.size(); i++)</pre>
                                                                                           361
318
                r[i] = a1b1[i];
                                                                                           bigint n;
                                                                                   362
319
            for (int i = 0; i < (int) a2b2.size(); i++)</pre>
                                                                                           while(cin >> n) {
                                                                                   363
320
                r[i] = a2b2[i];
                                                                                               if(n==0){break;}
321
                                                                                  364
```

be used mapped type. Apparently,

any problems with them before),

order_of_key().

14

the tree supports the same operations as the set (at least I haven't

but also there are two new features - it is find_by_order() and

```
The first returns an iterator to the k-th largest element (counting
           a += n:
365
                                                                                        from zero), the second - the number of items
       }
366
                                                                                   in a set that are strictly smaller than our item. Example of use:
       cout<<a<<endl;
367
                                                                                   *
                                                                                17
368
                                                                                18 * */
                                 UnorderedSet
                                                                                                          2.8 Treap Modo Set
    //Compilar: g++ --std=c++11
                                                                                                            Treap Implicito(Rope)
   struct Hash{
 2
     size_t operator()(const ii &a)const{
                                                                                                            Treap - Toby and Bones
 3
                                                                                                    2.10
       size_t s=hash<int>()(a.fst);
 4
                                                                                                          Convex Hull Trick Estatico
       return hash<int>()(a.snd)+0x9e3779b9+(s<<6)+(s>>2);
 5
     }
 6
     size_t operator()(const vector<int> &v)const{
                                                                                 1 // g++ "convexhulltrick.cpp" -o run
 7
       size_t s=0;
                                                                                   /***
 8
                                                                                 2
       for(auto &e : v)
                                                                                           ====== <Convex hull trick normal version> =======
 9
         s = hash < int > ()(e) + 0x9e3779b9 + (s < 6) + (s > 2);
                                                                                   Contain a sample about convex hull trick optimization this recivie N
10
       return s;
                                                                                       pairs:
11
     }
                                                                                 5 a "value of length" and a cost, we need to minimize the value of
12
13
                                                                                       grouping
   unordered_set<ii, Hash> s;
                                                                                   this pairs taken the most large pair as the cost of the group
unordered_map<ii, int, Hash> m;//map<key, value, hasher>
                                                                                   Problem for practice: aquire
                            2.7 Ordered Set
                                                                                   */
                                                                                   #include <iostream>
                                                                                   #include <vector>
 1
    A brief explanation about use of a powerful library: orderd_set
                                                                                   #include <algorithm>
    Reference link: http://codeforces.com/blog/entry/11080
                                                                                   using namespace std;
    and a hash for the type pair
                                                                                   int pointer; //Keeps track of the best line from previous query
    */
                                                                                   vector<long long> M; //Holds the slopes of the lines in the envelope
 5
                                                                                   vector<long long> B; //Holds the y-intercepts of the lines in the
 6
   #include <ext/pb_ds/assoc_container.hpp>
                                                                                       envelope
    #include <ext/pb_ds/tree_policy.hpp>
                                                                                   //Returns true if either line 11 or line 13 is always better than line
    using namespace __gnu_pbds;
   typedef tree<int,null_type,less<int>,rb_tree_tag,
                                                                                   bool bad(int 11, int 12, int 13)
                                                                                   {
       tree_order_statistics_node_update> ordered_set;
                                                                                19
11
                                                                                20
   If we want to get map but not the set, as the second argument type must
                                                                                     intersection(11,12) has x-coordinate (b1-b2)/(m2-m1)
```

21

22

23

24

25

*/

eliminate division

intersection(11,13) has x-coordinate (b1-b3)/(m3-m1)

set the former greater than the latter, and cross-multiply to

return (B[13]-B[11])*(M[11]-M[12])<(B[12]-B[11])*(M[11]-M[13]);

```
27 }
                                                                                        for (i=0,N=0; i<M; i++)
   //Adds a new line (with lowest slope) to the structure
                                                                                        {
                                                                                  68
   void add(long long m,long long b)
                                                                                          /*
                                                                                  69
29
                                                                                          When we add a higher rectangle, any rectangles that are also
30
                                                                                   70
                                                                                          equally thin or thinner become irrelevant, as they are
     //First, let's add it to the end
                                                                                  71
31
     M.push_back(m);
                                                                                          completely contained within the higher one; remove as many
32
     B.push_back(b);
                                                                                          as necessary
                                                                                  73
33
     //If the penultimate is now made irrelevant between the
                                                                                          */
                                                                                  74
34
         antepenultimate
                                                                                          while (N>0&&rect[N-1].second<=a[i].second)</pre>
     //and the ultimate, remove it. Repeat as many times as necessary
                                                                                            N--;
                                                                                   76
35
     while (M.size()>=3\&\&bad(M.size()-3,M.size()-2,M.size()-1))
                                                                                          rect[N++]=a[i]; //add the new rectangle
                                                                                  77
36
37
                                                                                  78
       M.erase(M.end()-2):
                                                                                        long long cost;
38
                                                                                  79
       B.erase(B.end()-2):
                                                                                        add(rect[0].second,0);
39
     }
                                                                                        //initially, the best line could be any of the lines in the envelope,
40
                                                                                        //that is, any line with index 0 or greater, so set pointer=0
41
   //Returns the minimum y-coordinate of any intersection between a given
                                                                                        pointer=0:
       vertical
                                                                                        for (i=0; i<N; i++)
   //line and the lower envelope
                                                                                   85
   long long query(long long x)
                                                                                          cost=query(rect[i].first);
                                                                                   86
                                                                                          if (i<N)
                                                                                  87
45
     //If we removed what was the best line for the previous query, then
                                                                                            add(rect[i+1].second,cost);
46
                                                                                  88
                                                                                   89
     //newly inserted line is now the best for that query
                                                                                        printf("%lld\n",cost);
47
     if (pointer>=M.size())
                                                                                        return 0;
                                                                                  91
48
       pointer=M.size()-1;
                                                                                   92 }
49
     //Any better line must be to the right, since query values are
50
                                                                                                     2.12 Convex Hull Trick Dinamico
     //non-decreasing
51
     while (pointer<M.size()-1&&
52
       M[pointer+1]*x+B[pointer+1]<M[pointer]*x+B[pointer])</pre>
                                                                                   1 // g++ -std=c++11 "convexhulltrick_dynamic.cpp" -o run
53
       pointer++;
                                                                                   2 /***
54
     return M[pointer] *x+B[pointer];
                                                                                      ======== <Convex hull trick dynamic version version>
55
56
   int main()
                                                                                   4 warning with the use of this, this is a black box, try to use only in an
                                                                                           emergency.
58
     int M,N,i;
                                                                                     Problem for practice: aquire
59
     pair<int, int> a[50000];
60
                                                                                   6
     pair<int,int> rect[50000];
                                                                                      #include <bits/stdc++.h>
61
     scanf("%d",&M);
                                                                                      using namespace std;
62
     for (i=0; i<M; i++)</pre>
                                                                                      typedef long long 11;
63
       scanf("%du%d",&a[i].first,&a[i].second);
                                                                                      const ll is_query = -(1LL<<62);</pre>
64
     //Sort first by height and then by width (arbitrary labels)
                                                                                        struct Line {
65
                                                                                  11
     sort(a,a+M);
66
                                                                                       ll m, b;
                                                                                  12
```

```
mutable multiset<Line>::iterator it:
                                                                                    3 Sirve para encontrar el i-esimo numero de un conjunto de numeros que
13
     const Line *succ(multiset<Line>::iterator it) const;
                                                                                           vamos insertando en el arbol.
14
     bool operator<(const Line& rhs) const {</pre>
                                                                                    4 Sirve solo si nuestros numeros son del 0 al n-1 (pero podemos mapearlos
15
       if (rhs.b != is_query) return m < rhs.m;</pre>
                                                                                           antes de usarlos)
16
       const Line *s=succ(it);
                                                                                    5 La idea es esta:
17
       if(!s) return 0;
                                                                                      Funcionamiento:
18
       11 x = rhs.m;
                                                                                        - En el fondo sigue siendo un Segment-Tree (hacemos que 'n' sea 2^x)
19
                                                                                        - Cada nodo guarda cuantos numeros hay en el intervalo (entonces en
       return b - s \rightarrow b < (s \rightarrow m - m) * x;
20
                                                                                             tree[1] dice cuantos numeros tenemos en total)
^{21}
                                                                                        - Se sigue representando los hijos del nodo 'i' con '2 * i' (izq) y '2
22
   struct HullDynamic : public multiset<Line>{ // will maintain upper hull
                                                                                              * i + 1' (der):
       for maximum
                                                                                      Query:
                                                                                   10
     bool bad(iterator v) {
                                                                                        - si kth es mas grande que todos los que tenemos(tree[1]) o es
                                                                                   11
24
       iterator z = next(y);
                                                                                             negativo entonces -1
25
       if (y == begin()) {
                                                                                        - siempre nos mantenemos en el nodo de la izquierda y si es necario
26
                                                                                   12
         if (z == end()) return 0;
                                                                                             avanzamos al de la derecha
27
         return y->m == z->m && y->b <= z->b;
                                                                                                             'i <<= 1'
28
                                                                                   13
       }
                                                                                           - si kth es mas grande que el nodo de la izquierda(el actual) quiere
29
       iterator x = prev(y);
                                                                                                decir que podemos quitarle todos esos
30
                                                                                          numeros a nuestra busqueda 'kth - tree[i]' y buscar el nuevo kth en
       if (z == end()) return y \rightarrow m == x \rightarrow m \&\& y \rightarrow b <= x \rightarrow b;
                                                                                   15
31
       return (x-b - y-b)*(z-m - y-m) >= (y-b - z-b)*(y-m - x-m);
                                                                                               el arbol de la derecha
32
                                                                                             if (kth > tree [i]) kth -= tree [i++];
33
     iterator next(iterator y){return ++y;}
                                                                                          - Ojo en el 'i++' ahi es donde avanzamos al nodo de la derecha
                                                                                   17
34
     iterator prev(iterator y){return --y;}
                                                                                         - luego hace su formula rara que aun no entendi xD:
35
       void insert_line(ll m, ll b) {
                                                                                             'i - leaf + (kth > tree [i])';
                                                                                   19
36
       iterator y = insert((Line) { m, b });
                                                                                   20
37
       y->it=y;
                                                                                       const int MaxN = 1e6;
                                                                                   21
38
       if (bad(y)) { erase(y); return; }
                                                                                   22
39
       while (next(y) != end() && bad(next(y))) erase(next(y));
                                                                                       int a [MaxN], s [MaxN];
                                                                                   23
40
                                                                                      int leaf, tree [100 + MaxN << 2];</pre>
       while (y != begin() && bad(prev(y))) erase(prev(y));
41
     }
                                                                                   25
42
     11 \text{ eval}(11 \text{ x}) 
                                                                                       void bld (int n) { leaf = 1 << (32 - __builtin_clz (n)); }</pre>
43
                                                                                      void add (int x) { for (int i = leaf + x; i; i \gg 1) ++tree [i]; }//
       Line 1 = *lower_bound((Line) { x, is_query });
       return 1.m * x + 1.b;
                                                                                           Podemos insertar mas de una copia la vez tree [i] += xcopies;
45
    }
                                                                                   28 | void del (int x) { for (int i = leaf + x; i; i >>= 1) --tree [i]; }//
46
                                                                                           Podemos eliminar mas de una copia la vez tree [i] -= xcopies;
   const Line *Line::succ(multiset<Line>::iterator it) const{
                                                                                   29 // en "leaf + x" esta cuantas copias tenemos de "x"
                                                                                   30 //Cuidado con intentar hacer del con mas copias de las disponibles, el
49 | return (++it==h.end()? NULL : &*it);}
                                                                                           kth() no funcionaria
                             2.13 Misof Tree
                                                                                   _{31} long kth (int kth, int i = -1) {
                                                                                           if (kth > tree [1] || kth <= 0) return i;
                                                                                        for (i = 1; i < leaf; i <<= 1) if (kth > tree [i]) kth -= tree [i++];
2 http://codeforces.com/blog/entry/10493#comment-159335
                                                                                           return i - leaf + (kth > tree [i]);
                                                                                   34
```

```
35 }
```

2.14 SQRT Decomposition Basic

```
1 | const int maxn = 500010;
  int n;
2
   tipo v[maxn];//vector principal
   tipo lazy[maxn];
   pair<tipo, tipo> t[maxn];//para poder reordenar los elementos
   int SQRT;
   int N;//nro. de buckets
11
   //Recalcula y aplica el lazy al bucket con indice idx
   //guarda la informacion necesaria del bucket en otros vectores
   //podria ser la suma del bucket, o el min/max del bucket
   void recalc(int idx) {
     int a = idx * SQRT, b = min(n, (idx + 1) * SQRT);
     for (int i = a; i < b; i++) {
      v[i] += lazy[idx];
18
       t[i] = make_pair(v[i], i);
19
20
     lazv[idx] = 0:
21
     sort(t + a, t + b);
22
23
24
   //adiciona delta a todos los elementos
   //en el intervalo cerrado [a, b]
   void add(int a, int b, tipo delta) {
     int idx_a = a / SQRT, idx_b = b / SQRT;
28
     if (idx_a == idx_b) {
29
       for (int i = a; i <= b; i++)
30
         v[i] += delta;
31
       recalc(idx_a);
32
     } else {
33
       //head
34
       for (int i = a, \lim = \min(n, (idx_a + 1) * SQRT); i < \lim; i++)
35
         v[i] += delta:
36
       recalc(idx_a);//OJO puede ser necesario
37
38
       for (int i = idx_a + 1; i < idx_b; i++)
39
```

```
lazy[i] += delta;
40
       //tail
41
       for (int i = idx_b * SQRT; i \le b; i++)
42
         v[i] += delta;
43
       recalc(idx_b);//OJO puede ser necesario
44
45
   }
46
47
   //tambien podria ser en un rango como en el add
   tipo query(tipo val) {
     tipo ans = 0;
50
    //recorro todos los buckets
51
     for (int idx = 0: idx < N: idx++) {
52
       int a = idx * SQRT, b = min(n, (idx + 1) * SQRT);
      //... hacer algo ...
    }
55
     return ans;
56
57
   int main() {
     //leer n, q y los elementos de v
60
     SQRT = (int)sqrt(n) + 1;
61
     N = (n + SQRT - 1) / SQRT; //nro. de buckets
62
     //construir cada bucket
63
     for (int idx = 0; idx < N; idx++)
64
       recalc(idx);
65
66
     //resto del programa
67
     return 0;
69 }
    2.15 Nro. Elementos menores o iguales a x en O(loq(n))
1 //insersion y consulta de cuantos <= en log n
   struct legset {
     int maxl; vector<int> c;
     int pref(int n, int 1) { return (n>>(maxl-1))|(1<<1); }</pre>
4
     void ini(int ml) { maxl=ml: c=vector<int>(1<<(maxl+1)): }</pre>
     //inserta c copias de e, si c es negativo saca c copias
6
     void insert(int e, int q=1) { forn(l,maxl+1) c[pref(e,l)]+=q; }
     int leq(int e) {
8
       int r=0,a=1;
9
       forn(i,maxl) {
10
```

3 Algos

3.1 LIS en O(n log n) con Reconstruccion

```
//Para non-increasing, cambiar comparaciones y revisar busq binaria
  //Given an array, paint it in the least number of colors so that each
       color turns to a non-increasing subsequence.
  //Solution:Min number of colors=Length of the longest increasing
       subsequence
4
   // Las lineas marcadas con // Camino no son necesarias si no se desea
       reconstruir el camino.
  #define MAXN 1000000
   int v[MAXN]; // INPUT del algoritmo.
   int mv[MAXN];
   int mi[MAXN] ,p[MAXN]; // Camino
  int 1 [MAXN]; // Aca apareceria la maxima subsecuencia creciente(los
       indices)
   int lis(int n) {
     forn(i,n) mv[i] = INF;
12
     forn(i,n) mi[i] = -1; // Camino
13
     forn(i,n) p [i] = -1; // Camino
14
     mv[0] = -INF;
15
     int res = 0;
16
     forn(i,n) {
17
       // Con upper_bound es maxima subsecuencia no decreciente.
18
       // Con lower_bound es maxima subsecuencia creciente.
19
       int me = upper_bound(mv,mv+n,v[i]) - mv;
20
       p[i] = mi[me-1]; // Camino
^{21}
       mv[me] = v[i]:
22
       mi[me] = i: // Camino
23
       if (me > res) res = me;
24
25
     for(int a = mi[res], i = res - 1; a != -1; a = p[a], i--) // Camino
26
       1[i] = a; // Indices: poniendo 1[i] = v[a] quedan los valores.
27
```

```
return res;
29 }
                                3.2 Mo
1 // g++ -std=c++11 "mo.cpp" -o run
2
   Contain a sample about Mo algorithm
   Brief explanation when use Mo:
   Explain where and when we can use above algorithm
  As mentioned, this algorithm is offline, that means we cannot use it
       when we are forced to stick to given order of queries.
   That also means we cannot use this when there are update operations.
        Not just that, there is one important possible limitation:
  We should be able to write the functions add and remove. There will be
       many cases where add is trivial but remove is not.
11 One such example is where we want maximum in a range. As we add elements
       , we can keep track of maximum. But when we remove elements
12 it is not trivial. Anyways in that case we can use a set to add elements
       , remove elements and report minimum.
13 In that case the add and delete operations are O(log N) (Resulting in O(
       N * Sqrt(N) * log N) algorithm).
14
   Suggestion first use the add operation, then the erase operation
   Problem for practice: DQUERY spoj
   Input: N, then N elements of array M querys with a range L,R
18
   const int MAXV = 1e6 + 10;
   const int N = 30010;
   const int M = 200010;
   int cnt[MAXV];
   int v[N];
24
   struct query{
    int 1,r,pos;
     query(){}
27
   };
28
   int n;
   query qu[M];
  int ans[M];
31
32
```

```
int ret = 0:
   void add(int pos){
     pos = v[pos];
35
     cnt[pos]++;
36
     if(cnt[pos] == 1){
       ret++;
39
40
   void erase(int pos){
41
     pos = v[pos];
42
     cnt[pos]--;
43
     if(!cnt[pos])ret--;
45
   int main(){
     n = in():
47
     for(int i = 0; i < n; i++){
48
       v[i] = in();
49
     }
50
     int block = ceil(sqrt(n));
51
     int q = in();
52
     for(int i = 0; i < q; i++){
53
       qu[i].1 = in() - 1, qu[i].r = in() - 1, qu[i].pos = i;
54
55
     sort(qu,qu + q,[&](const query &a,const query &b){
56
       if(a.l / block != b.l / block)
57
         return a.1 / block < b.1 / block;
58
       return a.r < b.r;
59
     });
60
     int 1 = 0, r = 0;
61
     for(int i = 0; i < q; i++){
62
       int nl = qu[i].1,nr = qu[i].r;
63
       while(1 > n1){
64
          add(--1):
65
       }
66
       while(r <= nr){</pre>
67
          add(r++);
68
       }
69
       while(1 < n1){</pre>
70
          erase(1++);
71
72
       while(r > nr + 1){
73
          erase(--r);
74
75
```

4 Strings

4.1 Manacher

```
vector<int> manacher(const string &_s) {
     int n = _s.size();
    string s(2 * n + 3, '#');
    s[0] = \%, s[s.size() - 1] = \%';//no deben estar en la cadena
     for (int i = 0; i < n; i++)
       s[(i + 1) * 2] = _s[i];
7
     n = s.size();
8
     vector<int> P(n, 0);
     int C = 0, R = 0;
     for (int i = 1; i < n - 1; i++) {
       int j = C - (i - C);
       if (R > i)
13
        P[i] = min(R - i, P[i]);
       while (s[i + 1 + P[i]] == s[i - 1 - P[i]])
         P[i]++:
16
       if (i + P[i] > R) {
17
         C = i;
18
         R = i + P[i];
19
20
    }
21
     return P;
22
23
   bool is_pal(const vector<int> &mnch_vec, int i, int j) {//[i, j] - i<=j
    int len = i - i + 1;
    i = (i + 1) * 2; //idx to manacher vec idx
    j = (j + 1) * 2;
     int mid = (i + j) / 2;
28
     return mnch_vec[mid] >= len;
29
   }
30
   int main() {
31
     string s;
32
     cin >> s;
33
```

```
vector<int> mnch_vec= manacher(s);
if (is_pal(mnch_vec, 2, 7)) {
    //la subcadena desde la posicion 2 a la 7 es palindrome
}
return 0;
}
```

4.2 Trie - Punteros y bfs

4.3 Suffix Array O(n log n) con LCP (Kasai) O(n)

4.4 Minima rotacion lexicografica

```
1
   Rotacion Lexicografica minima MinRotLex(cadena,tamanio)
   para cambiar inicio de la cadena char s[300]; int h; s+h;
   retorna inicio de la rotacion minima :D
5
   int MinRotLex(const char *s, const int slen) {
      int i = 0, j = 1, k = 0, x, y, tmp;
7
      while(i < slen && j < slen && k < slen) {
8
         x = i + k;
9
         y = j + k;
10
         if(x >= slen) x -= slen;
11
         if(y >= slen) y -= slen;
12
         if(s[x] == s[y]) {
13
            k++:
14
         } else if(s[x] > s[y]) {
15
            i = j+1 > i+k+1 ? j+1 : i+k+1;
16
            k = 0;
17
            tmp = i, i = j, j = tmp;
18
         } else {
19
            j = i+1 > j+k+1 ? i+1 : j+k+1;
20
            k = 0;
21
         }
^{22}
23
      return i;
^{24}
25
   int main(){
26
     int n:
27
     scanf("%d",&n);getchar();
28
     while(n--){
29
       char str[1000009];
30
       gets(str);
31
```

```
printf("%d\n",MinRotLex(str,strlen(str))+1);
33
34 }
                              4.5 Matching
                                 4.5.1 KMP
string T;//cadena donde buscar(where)
string P;//cadena a buscar(what)
   int b[MAXLEN];//back table b[i] maximo borde de [0..i)
   void kmppre(){//by gabina with love
       int i =0, j=-1; b[0]=-1;
       while(i<sz(P)){</pre>
           while(j>=0 && P[i] != P[j]) j=b[j];
7
           i++, j++, b[i] = j;
       }
9
10
   void kmp(){
       int i=0, j=0;
12
       while(i<sz(T)){</pre>
13
           while(j>=0 && T[i]!=P[j]) j=b[j];
           i++, j++;
           if(j==sz(P)) printf("Puisufounduatuindexu%duinuT\n", i-j), j=b[j
16
       }
17
   }
18
19
   int main(){
       cout << "T=";
21
       cin >> T;
22
       cout << "P=";
23
       cin.ignore();
24
       cin >> P;
25
       kmppre();
26
       kmp();
27
       return 0;
28
29 }
                          4.5.2 Z - Por aprender
                      4.5.3 Matching con suffix array
1 | vector<int> FindOccurrences(const string& pattern, const string& text) {
```

vector<int> result;

21

```
int minIndex = 0,maxIndex = text.size();
                                                                                          if(pattern.size()){
3
                                                                                   22
     while(minIndex < maxIndex){</pre>
                                                                                             char letter = pattern.back();
4
                                                                                   23
       int mid = (minIndex + maxIndex) >> 1;
                                                                                             pattern.pop_back();
5
                                                                                   24
       if(cmp(pattern,sa[mid]) > 0)minIndex = mid + 1;
                                                                                             if(count[letter][bot + 1]){
6
                                                                                   25
       else maxIndex = mid;
                                                                                              top = fo[letter] + count[letter][top];
                                                                                   26
     }
                                                                                               bot = fo[letter] + count[letter][bot + 1] - 1;
8
                                                                                   27
     int start = minIndex;
                                                                                   28
     maxIndex = text.size();
                                                                                             else return 0;
10
                                                                                   29
     while(minIndex < maxIndex){</pre>
                                                                                          }
11
                                                                                   30
       int mid = (minIndex + maxIndex) >> 1;
                                                                                          else return bot - top + 1;
                                                                                   31
12
       if(cmp(pattern,sa[mid]) < 0)maxIndex = mid;</pre>
13
                                                                                   32
       else minIndex = mid + 1;
                                                                                        return 0;
14
                                                                                   33
                                                                                   34 }
     }
15
     int end = maxIndex;
16
                                                                                                        4.5.5 Matching con Aho-Corasick
     for(int i = start; i < end;i++){</pre>
17
       result.push_back(sa[i]);
18
    }
19
                                                                                   1
     return result;
                                                                                      struct trie{
21 }
                                                                                        map<char, trie> next;
                                                                                        trie* tran[256];//transiciones del automata
                         4.5.4 Matching con BWT
                                                                                        int idhoja, szhoja;//id de la hoja o 0 si no lo es
                                                                                        //link lleva al sufijo mas largo, nxthoja lleva al mas largo pero que
  map<char,int>fo;//first ocurrence
                                                                                             es hoja
   map<char,vector<int> >count;//count the i-th ocurrence of symbol
                                                                                        trie *padre, *link, *nxthoja;
                                                                                   7
   string first;//first colum of bwt
                                                                                         char pch;//caracter que conecta con padre
                                                                                   8
   string alpha = "ACGT$";//change this
                                                                                         trie(): tran(), idhoja(), padre(), link() {}
                                                                                   9
   void preprocess(const string& bwt) {//recieves a BWT
                                                                                        void insert(const string &s, int id=1, int p=0){//id>0!!!
                                                                                   10
     string ans = "";
                                                                                          if(p<sz(s)){</pre>
                                                                                   11
6
                                                                                            trie &ch=next[s[p]];
     first = bwt;
                                                                                   12
7
     sort(first.begin(),first.end());
                                                                                             tran[(int)s[p]]=&ch;
8
                                                                                   13
     for(int i = 0;first[i];i++){
                                                                                             ch.padre=this, ch.pch=s[p];
                                                                                   14
9
       if(!fo.count(first[i]))fo[first[i]] = i;
                                                                                             ch.insert(s, id, p+1);
                                                                                   15
10
                                                                                   16
11
     for(char u:alpha)count[u].push_back(0);
                                                                                          else idhoja=id, szhoja=sz(s);
                                                                                   17
12
     for(int i = 1; i <= bwt.size();i++){</pre>
13
                                                                                   18
       for(char u:alpha)
                                                                                        trie* get_link() {
                                                                                   19
14
         count[u].push_back(count[u].back() + (bwt[i - 1] == u));
                                                                                          if(!link){
                                                                                   20
15
     }
                                                                                             if(!padre) link=this;//es la raiz
                                                                                   21
16
                                                                                             else if(!padre->padre) link=padre;//hijo de la raiz
17
                                                                                   22
   //return the number of ocurrences of the pattern
                                                                                             else link=padre->get_link()->get_tran(pch);
                                                                                   23
   int bwtmatch(int bot,string &pattern){
                                                                                   24
19
     int top = 0;
                                                                                          return link; }
                                                                                   25
20
     while(top <= bot){</pre>
```

trie* get_tran(int c) {

21

22

np->step=p->step+1;

```
if(!tran[c]) tran[c] = !padre? this : this->get_link()->get_tran(c);
                                                                                          while(p&&!p->go[w])
27
                                                                                  23
       return tran[c]: }
                                                                                              p->go[w]=np,p=p->pre;
                                                                                  24
28
     trie *get_nxthoja(){
                                                                                          if(p==0)
                                                                                   25
29
       if(!nxthoja) nxthoja = get_link()->idhoja? link : link->nxthoja;
                                                                                              np->pre=root;
30
                                                                                   26
       return nxthoja; }
                                                                                          else {
                                                                                  27
31
                                                                                              State *q=p->go[w];
     void print(int p){
32
                                                                                   28
       if(idhoja) cout << "foundu" << idhoja << "LLat_positionu" << p-
                                                                                              if(p->step+1==q->step)
33
                                                                                   29
           szhoja << endl;
                                                                                                  np->pre=q;
                                                                                   30
       if(get_nxthoja()) get_nxthoja()->print(p); }
                                                                                              else {
34
                                                                                   31
     void matching(const string &s, int p=0){
                                                                                                  State *ng=cur++;
35
                                                                                   32
       print(p); if(p<sz(s)) get_tran(s[p])->matching(s, p+1); }
                                                                                                  nq->clear();
36
                                                                                   33
                                                                                                  memcpy(nq->go,q->go,sizeof(q->go));//nq->go = q->go; para
   }tri;
37
                                                                                   34
38
                                                                                                  nq->step=p->step+1;
                                                                                   35
39
   int main(){
                                                                                                  nq->pre=q->pre;
     tri=trie();//clear
                                                                                                  q->pre=nq;
     tri.insert("ho", 1);
                                                                                                  np->pre=nq;
42
     tri.insert("hoho", 2);
                                                                                                  while (p\&\&p->go[w]==q)
                                                                                                       p->go[w]=nq, p=p->pre;
                                                                                   40
                               Suffix Automaton
                                                                                              }
                                                                                   41
                                                                                          }
                                                                                   42
                                                                                          last=np;
    /*####################### Suffix Automata ################*/
                                                                                   43
   const int N = INSERTE_VALOR;//maxima longitud de la cadena
                                                                                   44
                                                                                       /*#################### Suffix Automata ###############/
   struct State { //0J0!!! tamanio del alfabeto, si MLE -> map
       State *pre, *go[26];//se puede usar un map<char, State*> go
                                                                                   46
                                                                                       /*################## Algunas aplicaciones ###############/
       int step:
5
                                                                                      //Obtiene el LCSubstring de 2 cadenas en O(|A| + |B|)
       void clear() {
6
                                                                                      string lcs(char A[N], char B[N]) {
           pre=0;
7
                                                                                          int n,m;
           step=0;
                                                                                   50
8
                                                                                          n = strlen(A); m = strlen(B);
           memset(go,0,sizeof(go));//go.clear();
9
                                                                                          //Construccion: O(|A|)
       }
10
                                                                                          //solo hacerlo una vez si A no cambia
   } *root,*last;
                                                                                          init():
   State statePool[N * 2],*cur;
                                                                                   54
                                                                                          for(int i=0; i<n; i++)</pre>
   void init() {
13
                                                                                              Insert(A[i]-'a'); //Fin construccion
                                                                                   56
       cur=statePool;
14
                                                                                          //LCS: 0(|B|)
       root=last=cur++;
15
                                                                                          int ans = 0, len = 0, bestpos = 0;
       root->clear();
16
                                                                                          State *p = root;
   | }
17
                                                                                          for(int i = 0; i < m; i++) {
   void Insert(int w) {
                                                                                   60
18
                                                                                              int x = B[i] - a;
       State *p=last;
                                                                                  61
19
                                                                                              if(p->go[x]) {
       State *np=cur++;
                                                                                   62
20
                                                                                                  len++;
       np->clear();
```

63

64

p = p - go[x];

```
} else {
65
                while (p \&\& !p->go[x]) p = p->pre;
66
                if(!p) p = root, len = 0;
67
                else len = p->step+1, p = p->go[x];
68
           }
69
            if (len > ans)
70
                ans = len, bestpos = i;
71
       }
72
       //return ans; //solo el tamanio del lcs
73
       return string(B + bestpos - ans + 1, B + bestpos + 1);
74
75
76
    /*Numero de subcadenas distintas + 1(subcadena vacia) en O(|A|)
    OJO: Por alguna razon Suffix Array es mas rapido
    Se reduce a contar el numero de paths que inician en q0 y terminan
79
    en cualquier nodo. dp[u] = # de paths que inician en u
    - Se debe construir el automata en el main(init y Insert's)
81
     Setear dp en -1
82
83
    number dp[N * 2];
84
   number num_dist_substr(State *u = root) {
85
        if (dp[u - statePool] != -1) return dp[u - statePool];
86
       number ans = 1;//el path vacio que representa este nodo
87
       for (int v = 0; v < 26; v++)//usar for (auto) para mapa
88
           if (u->go[v])
89
                ans += num_dist_substr(u->go[v]);
90
       return (dp[u - statePool] = ans);
91
92
93
    /*Suma la longitud de todos los substrings en O(|A|)
     Construir el automata(init y insert's)
95
    - Necesita el metodo num_dist_substr (el de arriba)
     setear dp's en -1
97
98
   number dp1[N * 2];
99
   number sum_length_dist_substr(State *u = root) {
100
       if (dp1[u - statePool] != -1) return dp1[u - statePool];
101
       number ans = 0;//el path vacio que representa este nodo
102
       for (int v = 0; v < 26; v++)//usar for (auto) para mapa
103
           if (u->go[v])
104
                ans += (num_dist_substr(u->go[v]) + sum_length_dist_substr(u
105
                    ->go[v]));
       return (dp1[u - statePool] = ans);
106
```

```
107 }
108
109
    Pregunta si p es subcadena de la cadena con la cual esta construida
110
    el automata.
111
    Complejidad: - Construir O(|Texto|) - solo una vez (init e insert's)
                  - Por Consulta O(|patron a buscar|)
113
114
    bool is_substring(char p[N]) {
        State *u = root;
116
        for (int i = 0; p[i]; i++) {
117
            if (!u->go.count(p[i]))//esta con map!!!
118
                 return false:
119
            u = u \rightarrow go[p[i]];//esta con map!!!
120
        }
121
        return true;
122
123 }
```

4.7 K-esima permutacion de una cadena

```
//Entrada: Una cadena cad(std::string), un long th
   //Salida : La th-esima permutacion lexicografica de cad
   string ipermutacion(string cad, long long int th){
     sort(cad.begin(), cad.end());
     string sol = "";
     int pos;
     for(int c = cad.size() - 1; c \ge 0; c - - ){
       pos = th / fact[c];
       th %= fact[c];
       sol += cad[pos];
       cad.erase(cad.begin() + pos);
11
    }
12
     return sol;
14 }
```

5 Geometria

- 5.1 Interseccion de circunferencias Sacar de Agustin
 - 5.2 Graham Scan
 - 5.3 Cortar Poligono

1 //cuts polygon Q along the line ab

```
//stores the left side (swap a, b for the right one) in P
void cutPolygon(pto a, pto b, vector<pto> Q, vector<pto> &P){
   P.clear();
   forn(i, sz(Q)){
        double left1=(b-a)^(Q[i]-a), left2=(b-a)^(Q[(i+1)%sz(Q)]-a);
        if(left1>=0) P.pb(Q[i]);
        if(left1*left2<0)
        P.pb(inter(line(Q[i], Q[(i+1)%sz(Q)]), line(a, b)));
   }
}</pre>
```

5.4 Interseccion de rectangulos

```
#define MAXC 2501
   struct Rect{
     int x1,y1, x2,y2;
     int color;
     int area:
     Rect(int _x1, int _y1, int _x2, int _y2){
       x1 = _x1;
       y1 = _{y1};
       x2 = _x2;
       y2 = _y2;
       getArea();
11
12
     int getArea(){
13
       if(x1>=x2 || y1>=y2)return area = 0;
14
       return area = (x2-x1)*(y2-y1);
15
     }
16
17
   Rect interseccion(Rect t, Rect r){
     int x1, y1, x2, y2;
19
     x1 = max(t.x1,r.x1);
20
     y1 = max(t.y1,r.y1);
     x2 = min(t.x2,r.x2);
22
     y2 = min(t.y2,r.y2);
     Rect res(x1,y1,x2,y2);
     return res;
26 }
```

5.5 Distancia punto-recta

```
double distance_point_to_line(const point &a, const point &b, const
point &pnt){
```

5.6 Distancia punto-segmento

```
struct point{
     double x,y;
  };
3
   inline double dist(const point &a, const point &b){
     return sqrt((a.x-b.x)*(a.x-b.x) + (a.y-b.y)*(a.y-b.y));
   inline double distsqr(const point &a, const point &b){
     return (a.x-b.x)*(a.x-b.x) + (a.y-b.y)*(a.y-b.y);
9
   double distance_point_to_segment(const point &a, const point &b, const
       point &pnt){
     double u = ((pnt.x - a.x)*(b.x - a.x) + (pnt.y - a.y)*(b.y - a.y)) /
11
         distsqr(a, b);
     point intersection;
12
     intersection.x = a.x + u*(b.x - a.x);
13
     intersection.y = a.y + u*(b.y - a.y);
14
15
     if (u < 0.0 | | u > 1.0)
16
       return min(dist(a, pnt), dist(b, pnt));
17
18
     return dist(pnt, intersection);
19
20 }
```

5.7 Parametrización de rectas - Sacar de codeforces

6 Math

6.1 Identidades

$$\sum_{i=0}^{n} {n \choose i} = 2^{n}$$

$$\sum_{i=0}^{n} i {n \choose i} = n * 2^{n-1}$$

$$\sum_{i=m}^{n} i = \frac{n(n+1)}{2} - \frac{m(m-1)}{2} = \frac{(n+1-m)(n+m)}{2}$$

$$\sum_{i=0}^{n} i = \sum_{i=1}^{n} i = \frac{n(n+1)}{2}$$

$$\sum_{i=0}^{n} i^2 = \frac{n(n+1)(2n+1)}{6} = \frac{n^3}{3} + \frac{n^2}{2} + \frac{n}{6}$$

$$\sum_{i=0}^{n} i(i-1) = \frac{8}{6} (\frac{n}{2})(\frac{n}{2}+1)(n+1) \text{ (doubles)} \rightarrow \text{Sino ver caso impar y par}$$

$$\sum_{i=0}^{n} i^3 = \left(\frac{n(n+1)}{2}\right)^2 = \frac{n^4}{4} + \frac{n^3}{2} + \frac{n^2}{4} = \left[\sum_{i=1}^{n} i\right]^2$$

$$\sum_{i=0}^{n} i^4 = \frac{n(n+1)(2n+1)(3n^2+3n-1)}{30} = \frac{n^5}{5} + \frac{n^4}{2} + \frac{n^3}{3} - \frac{n}{30}$$

$$\sum_{i=0}^{n} i^p = \frac{(n+1)^{p+1}}{p+1} + \sum_{k=1}^{p} \frac{B_k}{p-k+1} \binom{p}{k} (n+1)^{p-k+1}$$

$$r = e - v + k + 1$$

Teorema de Pick: (Area, puntos interiores y puntos en el borde) $A = I + \frac{B}{2} - 1$

6.2 Ec. Caracteristica

```
a_0T(n) + a_1T(n-1) + \ldots + a_kT(n-k) = 0
p(x) = a_0x^k + a_1x^{k-1} + \ldots + a_k
Sean r_1, r_2, \ldots, r_q las raíces distintas, de mult. m_1, m_2, \ldots, m_q
T(n) = \sum_{i=1}^q \sum_{j=0}^{m_i-1} c_{ij}n^jr_i^n
Las constantes c_{ij} se determinan por los casos base.
```

6.3 Identidades de agustin y mario

6.4 Combinatorio

```
forn(i, MAXN+1){//comb[i][k]=i tomados de a k
   comb[i][0]=comb[i][i]=1;
   forr(k, 1, i) comb[i][k]=(comb[i-1][k]+comb[i-1][k-1])%MOD;
}

ll lucas (ll n, ll k, int p){ //Calcula (n,k)%p teniendo comb[p][p]
        precalculado.

ll aux = 1;
   while (n + k) aux = (aux * comb[n%p][k%p]) %p, n/=p, k/=p;
   return aux;
}
```

6.5 Exp. de Numeros Mod.

```
1 | ll expmod (ll b, ll e, ll m){//0(log b)
2 | if(!e) return 1;
3 | ll q= expmod(b,e/2,m); q=(q*q)%m;
4 | return e%2? (b * q)%m : q;
5 |}
```

6.6 Exp. de Matrices y Fibonacci en log(n) - Sacar de Agustin

6.7 Gauss Jordan

```
_{1} | const int N = 300;
   typedef vector<double> col;
   typedef vector<double> row;
   typedef vector<row>Matrix;
   col solution;
   int main(){
     Matrix M;
     M.resize(300);
     solution.resize(300);
     for(int i = 0; i < 30; i++)M[i].resize(30);
     int n;
11
     cin >> n;
12
     for(int i = 0; i < n; i++)
13
       for(int j = 0; j \le n; j++)
14
          cin >> M[i][j];
15
     for(int j = 0; j < n - 1; j++){
17
       int l = j;
18
       for(int i = j + 1; i < n; i++){
19
         if(fabs(M[i][j]) > fabs(M[l][j]))l = i;
20
21
       for(int k = j; k \le n; k++){
          swap(M[j][k],M[l][k]);
23
24
       for(int i = j + 1; i < n; i++)
25
         for(int k = n; k \ge j; k--)
26
           M[i][k] -= M[j][k] * M[i][j] / M[j][j];
27
28
     double t = 0;
29
     for(int j = n - 1; j \ge 0; j--){
30
31
       for(int k = j + 1; k < n; k++)t += M[j][k] * solution[k];
32
       solution[i] = (M[i][n] - t) / M[i][i]:
33
34
     cout.precision(4);
35
     for(int i = 0; i < n;i++)cout<<fixed << solution[i] << "";</pre>
     return 0;
37
38 | }
```

6.8 Simplex

```
1 // Two-phase simplex algorithm for solving linear programs of the form
2
          maximize
                       c^T x
3
          subject to Ax <= b
                       x >= 0
   // INPUT: A -- an m x n matrix
             b -- an m-dimensional vector
            c -- an n-dimensional vector
             x -- a vector where the optimal solution will be stored
   // OUTPUT: value of the optimal solution (infinity if unbounded
              above, nan if infeasible)
13
   // To use this code, create an LPSolver object with A, b, and c as
   // arguments. Then, call Solve(x).
   #include <iostream>
   #include <iomanip>
   #include <vector>
   #include <cmath>
   #include <limits>
   using namespace std;
25
   typedef long double DOUBLE;
   typedef vector<DOUBLE> VD;
   typedef vector<VD> VVD;
   typedef vector<int> VI;
30
   const DOUBLE EPS = 1e-9;
31
32
   struct LPSolver {
33
     int m, n;
34
     VI B, N;
35
     VVD D:
36
37
     LPSolver(const VVD &A, const VD &b, const VD &c) :
38
       m(b.size()), n(c.size()), N(n + 1), B(m), D(m + 2, VD(n + 2)) {
39
       for (int i = 0; i < m; i++) for (int j = 0; j < n; j++) D[i][j] = A[
40
           i][i];
```

```
for (int i = 0; i < m; i++) { B[i] = n + i; D[i][n] = -1; D[i][n + i]
41
           1] = b[i]; }
       for (int j = 0; j < n; j++) { N[j] = j; D[m][j] = -c[j]; }
^{42}
       N[n] = -1; D[m + 1][n] = 1;
     }
44
45
     void Pivot(int r, int s) {
46
       double inv = 1.0 / D[r][s];
       for (int i = 0; i < m + 2; i++) if (i != r)
         for (int j = 0; j < n + 2; j++) if (j != s)
           D[i][j] -= D[r][j] * D[i][s] * inv;
       for (int j = 0; j < n + 2; j++) if (j != s) D[r][j] *= inv;
51
       for (int i = 0; i < m + 2; i++) if (i != r) D[i][s] *= -inv;
52
       D[r][s] = inv;
       swap(B[r], N[s]);
55
56
     bool Simplex(int phase) {
       int x = phase == 1 ? m + 1 : m;
58
       while (true) {
         int s = -1;
         for (int j = 0; j \le n; j++) {
           if (phase == 2 \&\& N[j] == -1) continue;
62
           if (s == -1 || D[x][i] < D[x][s] || D[x][i] == D[x][s] && N[i] <
63
                N[s]) s = j;
64
         if (D[x][s] > -EPS) return true;
         int r = -1;
         for (int i = 0; i < m; i++) {
67
           if (D[i][s] < EPS) continue;
           if (r == -1 || D[i][n + 1] / D[i][s] < D[r][n + 1] / D[r][s] ||
              (D[i][n + 1] / D[i][s]) == (D[r][n + 1] / D[r][s]) && B[i] < B
70
                  [r]) r = i:
71
         if (r == -1) return false:
         Pivot(r. s):
73
       }
74
     }
75
76
     DOUBLE Solve(VD &x) {
77
       int r = 0:
78
       for (int i = 1; i < m; i++) if (D[i][n + 1] < D[r][n + 1]) r = i;
79
       if (D[r][n + 1] < -EPS) {
80
```

```
Pivot(r, n);
                                                                                         for (size_t i = 0; i < x.size(); i++) cerr << "" << x[i];
81
          if (!Simplex(1) || D[m + 1][n + 1] < -EPS) return -numeric_limits</pre>
                                                                                   122
                                                                                         cerr << endl:
82
              DOUBLE>::infinity();//NO SOLUTION
                                                                                         return 0;
                                                                                   123
          for (int i = 0; i < m; i++) if (B[i] == -1) {
                                                                                   124 }
83
            int s = -1:
84
                                                                                                     6.9 Matrices y determinante O(n^3)
            for (int j = 0; j \le n; j++)
85
              if (s == -1 || D[i][j] < D[i][s] || D[i][j] == D[i][s] && N[j]
86
                   < N[s]) s = j;
                                                                                     1 | struct Mat {
            Pivot(i, s);
                                                                                           vector<vector<double> > vec;
87
                                                                                    2
          }
                                                                                           Mat(int n): vec(n, vector<double>(n) ) {}
88
        }
                                                                                           Mat(int n, int m): vec(n, vector<double>(m) ) {}
89
        if (!Simplex(2)) return numeric_limits<DOUBLE>::infinity();//
90
                                                                                           vector<double> &operator[](int f){return vec[f];}
                                                                                    5
            TNFTNTTY
                                                                                           const vector<double> &operator[](int f) const {return vec[f];}
        x = VD(n):
                                                                                           int size() const {return sz(vec);}
91
                                                                                    7
        for (int i = 0; i < m; i++) if (B[i] < n) x[B[i]] = D[i][n + 1];
                                                                                           Mat operator+(Mat &b) { ///this de n x m entonces b de n x m
        return D[m][n + 1];//solution find
93
                                                                                               Mat m(sz(b), sz(b[0]));
     }
                                                                                               forn(i,sz(vec)) forn(j,sz(vec[0])) m[i][j] = vec[i][j] + b[i][j
94
                                                                                    10
95
                                                                                                    ];
                                                                                               return m:
96
                                                                                    11
    int main() {
                                                                                           Mat operator*(const Mat &b) { ///this de n x m entonces b de m x t
                                                                                    12
                                                                                               int n = sz(vec), m = sz(vec[0]), t = sz(b[0]);
98
      const int m = 4;
99
                                                                                               Mat mat(n,t);
                                                                                    14
      const int n = 3;
                                                                                               forn(i,n) forn(j,t) forn(k,m) mat[i][j] += vec[i][k] * b[k][j];
100
                                                                                    15
      DOUBLE A[m][n] = {
101
                                                                                               return mat: }
                                                                                    16
       \{6, -1, 0\},\
                                                                                           double determinant(){//sacado de e maxx ru
102
                                                                                    17
       \{-1, -5, 0\},\
103
                                                                                               double det = 1:
                                                                                    18
       { 1, 5, 1 },
104
                                                                                               int n = sz(vec);
                                                                                    19
       \{-1, -5, -1\}
                                                                                               Mat m(*this);
105
                                                                                    20
                                                                                               forn(i, n){//para cada columna
106
                                                                                    21
      DOUBLE _b[m] = \{ 10, -4, 5, -5 \};
107
                                                                                                    int k = i;
                                                                                    22
      DOUBLE _c[n] = \{ 1, -1, 0 \};
108
                                                                                                    forr(j, i+1, n)//busco la fila con mayor val abs
                                                                                    23
109
                                                                                                        if(abs(m[i][i])>abs(m[k][i])) k = i;
                                                                                    24
      VVD A(m):
110
                                                                                                    if(abs(m[k][i])<1e-9) return 0;</pre>
                                                                                    25
      VD b( b, b + m):
                                                                                                    m[i].swap(m[k]);//la swapeo
111
                                                                                    26
      VD c(_c, _c + n);
                                                                                                    if(i!=k) det = -det;
112
                                                                                    27
      for (int i = 0; i < m; i++) A[i] = VD(_A[i], _A[i] + n);
113
                                                                                                    det *= m[i][i];
                                                                                    28
114
                                                                                                    forr(j, i+1, n) m[i][j] /= m[i][i];
                                                                                    29
      LPSolver solver(A. b. c):
115
                                                                                                    //hago 0 todas las otras filas
                                                                                    30
      VD x;
                                                                                                    forn(j, n) if (j!= i && abs(m[j][i])>1e-9)
116
                                                                                    31
      DOUBLE value = solver.Solve(x);
                                                                                                        forr(k, i+1, n) m[j][k]-=m[i][k]*m[j][i];
117
                                                                                    32
                                                                                               }
118
                                                                                    33
      cerr << "VALUE: " << value << endl; // VALUE: 1.29032
119
                                                                                               return det;
                                                                                    34
      cerr << "SOLUTION:"; // SOLUTION: 1.74194 0.451613 1</pre>
120
                                                                                    35
```

```
36 };
37
   int n;
38
   int main() {
   //DETERMINANTE:
   //https://uva.onlinejudge.org/index.php?option=com_onlinejudge&Itemid=8&
       page=show_problem&problem=625
     freopen("input.in", "r", stdin);
42
       ios::sync_with_stdio(0);
43
       while(cin >> n && n){
44
           Mat m(n);
45
           forn(i, n) forn(j, n) cin >> m[i][j];
46
           cout << (11)round(m.determinant()) << endl:</pre>
47
       }
48
       cout << "*" << endl:
49
     return 0;
50
51 }
```

6.10 Teorema Chino del Resto

$$y = \sum_{j=1}^{n} (x_j * (\prod_{i=1, i \neq j}^{n} m_i)_{m_j}^{-1} * \prod_{i=1, i \neq j}^{n} m_i)$$

6.11 Criba

```
#define MAXP 100000 //no necesariamente primo
   int criba[MAXP+1];
   void crearcriba(){
     int w[] = \{4,2,4,2,4,6,2,6\};
     for(int p=25;p<=MAXP;p+=10) criba[p]=5;</pre>
5
     for(int p=9;p<=MAXP;p+=6) criba[p]=3;</pre>
6
     for(int p=4;p<=MAXP;p+=2) criba[p]=2;</pre>
7
     for(int p=7,cur=0;p*p<=MAXP;p+=w[cur++&7]) if (!criba[p])</pre>
8
       for(int j=p*p;j<=MAXP;j+=(p<<1)) if(!criba[j]) criba[j]=p;</pre>
9
10
   vector<int> primos;
11
   void buscarprimos(){
12
     crearcriba():
13
     forr (i,2,MAXP+1) if (!criba[i]) primos.push_back(i);
14
15
   //^{\sim} Useful for bit trick: #define SET(i) ( criba[(i)>>5]|=1<<((i)&31) ),
        #define INDEX(i) ( (criba[i>>5]>>((i)&31))&1 ), unsigned int criba[
       MAXP/32+1];
```

```
17
18
   int main() {
19
     freopen("primos", "w", stdout);
20
     buscarprimos();
21
                       6.12 Funciones de primos
       Sea n = \prod p_i^{k_i}, fact(n) genera un map donde a cada p_i le asocia su k_i
   //factoriza bien numeros hasta MAXP^2
   map<11,11> fact(11 n){ //0 (cant primos)
     map<ll,ll> ret;
     forall(p, primos){
       while(!(n\price*p)){
         ret[*p]++;//divisor found
         n/=*p;
7
8
9
     if(n>1) ret[n]++;
     return ret:
12
    //factoriza bien numeros hasta MAXP
   map<11,11> fact2(11 n){ //0 (lg n)}
     map<ll,ll> ret;
15
     while (criba[n]){
16
       ret[criba[n]]++;
17
       n/=criba[n];
18
19
     if(n>1) ret[n]++;
20
     return ret;
21
22
   //Usar asi: divisores(fac, divs, fac.begin()); NO ESTA ORDENADO
   void divisores(const map<11,11> &f, vector<11> &divs, map<11,11>::
       iterator it, ll n=1){
       if(it==f.begin()) divs.clear();
       if(it==f.end()) { divs.pb(n); return; }
26
       ll p=it->fst, k=it->snd; ++it;
27
       forn(_, k+1) divisores(f, divs, it, n), n*=p;
28
29
   ll sumDiv (ll n){
     ll rta = 1;
31
     map<11,11> f=fact(n);
32
```

forall(it, f) {

33

```
11 \text{ pot} = 1, \text{ aux} = 0;
34
                                                                                       2
                                                                                          11 mulmod (11 a, 11 b, 11 c) { //returns (a*b)%c, and minimize overfloor
     forn(i, it->snd+1) aux += pot, pot *= it->fst;
35
                                                                                           11 x = 0, y = a\%c;
     rta*=aux;
36
     }
                                                                                            while (b > 0){
37
                                                                                            if (b \% 2 == 1) x = (x+y) \% c;
     return rta;
38
                                                                                              y = (y*2) \% c;
39
   ll eulerPhi (ll n){ // con criba: O(lg n)
                                                                                              b /= 2;
     11 \text{ rta} = n;
                                                                                           }
                                                                                       9
     map<ll,ll> f=fact(n);
                                                                                            return x % c;
42
                                                                                       10
     forall(it, f) rta -= rta / it->first;
                                                                                       11
     return rta;
44
                                                                                       12
                                                                                          ll expmod (ll b, ll e, ll m){\frac{1}{0}} \log b
45
                                                                                            if(!e) return 1:
   ll eulerPhi2 (ll n){ // 0 (sqrt n)
     11 r = n;
                                                                                            11 q = expmod(b, e/2, m); q = mulmod(q, q, m);
47
     forr (i,2,n+1){
                                                                                            return e%2? mulmod(b,q,m) : q;
                                                                                       16
       if ((11)i*i > n) break;
                                                                                       17
49
       if (n \% i == 0){
50
                                                                                       18
         while (n\%i == 0) n/=i;
                                                                                          bool es_primo_prob (ll n, int a)
51
         r = r/i: 
                                                                                      20
52
                                                                                            if (n == a) return true;
53
     if (n != 1) r= r/n;
                                                                                            ll s = 0, d = n-1;
54
                                                                                            while (d \% 2 == 0) s++, d/=2;
     return r;
55
56
                                                                                      24
                                                                                            11 x = expmod(a,d,n);
                                                                                      25
57
                                                                                            if ((x == 1) || (x+1 == n)) return true;
   int main() {
                                                                                      26
58
     buscarprimos();
                                                                                      27
59
     forr (x,1, 500000){
                                                                                            forn (i, s-1){
                                                                                      28
60
       cout << "x_{\sqcup}=_{\sqcup}" << x << endl;
                                                                                             x = mulmod(x, x, n);
61
       cout << "Numero_de_factores_primos:_" << numPrimeFactors(x) << endl;</pre>
                                                                                              if (x == 1) return false;
                                                                                      30
62
       cout << "Numero de distintos factores primos: " <<
                                                                                              if (x+1 == n) return true;
                                                                                      31
63
           numDiffPrimeFactors(x) << endl;</pre>
                                                                                      32
       cout << "Suma, de, factores, primos:,," << sumPrimeFactors(x) << endl;
                                                                                            return false;
                                                                                      33
64
       cout << "Numero de divisores:" << numDiv(x) << endl;</pre>
                                                                                      34
65
       cout << "Suma, de, divisores:" << sumDiv(x) << endl;</pre>
                                                                                      35
66
       cout << "Phi de Euler: " << eulerPhi(x) << endl;</pre>
                                                                                          bool rabin (ll n){ //devuelve true si n es primo
67
     }
                                                                                            if (n == 1) return false:
68
                                                                                            const int ar[] = \{2,3,5,7,11,13,17,19,23\};
     return 0;
69
                                                                                      38
70 | }
                                                                                            forn (j,9)
                                                                                      39
                                                                                              if (!es_primo_prob(n,ar[j]))
                                                                                      40
                                                                                                return false;
                                                                                      41
                     6.13 Phollard's Rho (rolando)
                                                                                            return true;
                                                                                      42
                                                                                      43
1 | 11 gcd(11 a, 11 b){return a?gcd(b %a, a):b;}
                                                                                      44
```

19

```
45 | 11 rho(11 n){
       if( (n \& 1) == 0 ) return 2;
46
       11 x = 2, y = 2, d = 1;
47
       ll c = rand() % n + 1;
48
       while(d == 1){
49
           x = (mulmod(x, x, n) + c)%n;
50
          y = (mulmod(y, y, n) + c)%n;
51
           y = (mulmod(y, y, n) + c)%n;
52
          if(x - y \ge 0) d = gcd(x - y, n);
53
           else d = gcd(y - x, n);
54
55
       return d==n? rho(n):d;
56
57
58
   map<ll,ll> prim;
   void factRho (ll n){ //O (lg n)^3. un solo numero
     if (n == 1) return;
61
     if (rabin(n)){
62
       prim[n]++;
63
       return;
64
     }
65
     11 factor = rho(n);
66
     factRho(factor);
67
     factRho(n/factor);
68
69 }
                               6.14 GCD
1 | tipo gcd(tipo a, tipo b){return a?gcd(b %a, a):b;}
                        6.15 Extended Euclid
  void extendedEuclid (ll a, ll b) \{ //a * x + b * y = d \}
     if (!b) { x = 1; y = 0; d = a; return;}
2
```

6.16 LCM

```
1 | tipo lcm(tipo a, tipo b){return a / gcd(a,b) * b;}
```

extendedEuclid (b, a%b);

11 y1 = x - (a/b) * y;

11 x1 = y;

x = x1; y = y1;

3

4

6

7

6.17 Inversos

```
1 #define MAXMOD 15485867
   11 inv[MAXMOD];//inv[i]*i=1 mod MOD
   void calc(int p){\frac{1}{0}}
     inv[1]=1;
     forr(i, 2, p) inv[i] = p-((p/i)*inv[p\%i])\%p;
6
   int inverso(int x){\frac{1}{0}(\log x)}
7
     return expmod(x, eulerphi(MOD)-2);//si mod no es primo(sacar a mano)
     return expmod(x, MOD-2);//si mod es primo
10 }
                              6.18 Simpson
double integral (double a, double b, int n=10000) \{/0(n), n=cantdiv\}
     double area=0, h=(b-a)/n, fa=f(a), fb;
     forn(i, n){
       fb=f(a+h*(i+1));
       area+=fa+ 4*f(a+h*(i+0.5)) +fb, fa=fb;
5
     }
6
     return area*h/6.;}
                              6.19 Fraction
tipo mcd(tipo a, tipo b){return a?mcd(b\(\mathbb{n}\)a, a):b;}
2 struct frac{
     tipo p,q;
     frac(tipo p=0, tipo q=1):p(p),q(q) {norm();}
     void norm(){
5
       tipo a = mcd(p,q);
6
       if(a) p/=a, q/=a;
7
       else q=1;
8
       if (q<0) q=-q, p=-p;}
9
     frac operator+(const frac& o){
10
       tipo a = mcd(q, o.q);
11
       return frac(p*(o.q/a)+o.p*(q/a), q*(o.q/a));}
12
     frac operator-(const frac& o){
13
       tipo a = mcd(q, o.q);
14
       return frac(p*(o.q/a)-o.p*(q/a), q*(o.q/a));}
15
     frac operator*(frac o){
16
       tipo a = mcd(q,o.p), b = mcd(o.q,p);
17
       return frac((p/b)*(o.p/a), (q/a)*(o.q/b));}
18
     frac operator/(frac o){
```

```
tipo a = mcd(q,o.q), b = mcd(o.p,p);
                                                                                      int n = sz(p.c) - 1;
20
       return frac((p/b)*(o.q/a),(q/a)*(o.p/b));}
                                                                                      vector<tipo> b(n);
                                                                                 37
^{21}
     bool operator<(const frac &o) const{return p*o.q < o.p*q;}</pre>
                                                                                      b[n-1] = p.c[n];
^{22}
                                                                                 38
     bool operator==(frac o){return p==o.p&kq==o.q;}
                                                                                      dforn(k,n-1) b[k] = p.c[k+1] + r*b[k+1];
23
                                                                                 39
24 };
                                                                                      tipo resto = p.c[0] + r*b[0];
                                                                                 40
                                                                                      polv result(b);
                                                                                 41
                             6.20 Polinomio
                                                                                      return make_pair(result,resto);
                                                                                 42
                                                                                 43
                                                                                    poly interpolate(const vector<tipo>& x,const vector<tipo>& y) {
           int m = sz(c), n = sz(o.c);
1
                                                                                        poly A; A.c.pb(1);
           vector<tipo> res(max(m,n));
2
                                                                                        forn(i,sz(x)) { poly aux; aux.c.pb(-x[i]), aux.c.pb(1), A = A * aux;
           forn(i, m) res[i] += c[i];
                                                                                 46
           forn(i, n) res[i] += o.c[i];
           return poly(res); }
                                                                                      poly S; S.c.pb(0);
                                                                                 47
5
       poly operator*(const tipo cons) const {
                                                                                      forn(i,sz(x)) { poly Li;
                                                                                        Li = ruffini(A,x[i]).fst;
       vector<tipo> res(sz(c));
7
                                                                                        Li = Li * (1.0 / Li.eval(x[i])); // here put a multiple of the
           forn(i, sz(c)) res[i]=c[i]*cons;
                                                                                 50
8
                                                                                            coefficients instead of 1.0 to avoid using double
           return poly(res); }
9
                                                                                        S = S + Li * y[i];
       polv operator*(const polv &o) const {
10
                                                                                      return S:
           int m = sz(c), n = sz(o.c);
                                                                                 52
11
                                                                                    }
           vector<tipo> res(m+n-1);
                                                                                 53
           forn(i, m) forn(j, n) res[i+j]+=c[i]*o.c[j];
                                                                                 54
13
                                                                                    int main(){
           return poly(res); }
14
                                                                                      return 0;
     tipo eval(tipo v) {
                                                                                 56
15
                                                                                 57 }
       tipo sum = 0:
16
       dforn(i, sz(c)) sum=sum*v + c[i];
17
                                                                                                             6.21 Ec. Lineales
       return sum: }
18
       //poly contains only a vector<int> c (the coeficients)
19
     //the following function generates the roots of the polynomial
                                                                                  bool resolver_ev(Mat a, Vec y, Vec &x, Mat &ev){
20
                                                                                      int n = a.size(), m = n?a[0].size():0, rw = min(n, m);
    //it can be easily modified to return float roots
21
                                                                                      vector<int> p; forn(i,m) p.push_back(i);
     set<tipo> roots(){
22
                                                                                 3
       set<tipo> roots;
                                                                                      forn(i, rw) {
                                                                                 4
23
       tipo a0 = abs(c[0]), an = abs(c[sz(c)-1]);
                                                                                        int uc=i, uf=i;
                                                                                 5
24
       vector<tipo> ps,qs;
                                                                                        forr(f, i, n) forr(c, i, m) if(fabs(a[f][c])>fabs(a[uf][uc])) {uf=f;
                                                                                  6
25
       forr(p,1,sqrt(a0)+1) if (a0\%p==0) ps.pb(p),ps.pb(a0/p);
                                                                                            uc=c:}
26
       forr(q,1,sqrt(an)+1) if (an\%q==0) qs.pb(q),qs.pb(an/q);
                                                                                        if (feq(a[uf][uc], 0)) { rw = i; break; }
27
                                                                                 7
       forall(pt,ps)
                                                                                        forn(j, n) swap(a[j][i], a[j][uc]);
                                                                                  8
28
                                                                                        swap(a[i], a[uf]); swap(y[i], y[uf]); swap(p[i], p[uc]);
         forall(gt,gs) if ( (*pt) % (*gt)==0 ) {
                                                                                 9
29
           tipo root = abs((*pt) / (*qt));
                                                                                        tipo inv = 1 / a[i][i]; //aca divide
                                                                                 10
30
           if (eval(root)==0) roots.insert(root);
                                                                                        forr(j, i+1, n) {
                                                                                 11
31
         }
                                                                                          tipo v = a[j][i] * inv;
                                                                                 12
32
                                                                                          forr(k, i, m) a[j][k]-=v * a[i][k];
       return roots; }
33
                                                                                 13
                                                                                          y[j] -= v*y[i];
34
                                                                                 14
pair<poly, tipo > ruffini(const poly p, tipo r) {
                                                                                 15
```

for (int i = 0; i < a.size(); i++) {

20

```
} // rw = rango(a), aca la matriz esta triangulada
                                                                                            for (int j = 0; j < b.size(); j++) {
                                                                                21
                                                                                                c[i+i] += a[i] * b[i];
     forr(i, rw, n) if (!feq(y[i],0)) return false; // checkeo de
                                                                                22
17
         compatibilidad
                                                                                            }
                                                                                23
     x = vector < tipo > (m, 0);
                                                                                       }
18
                                                                                24
     dforn(i, rw){
                                                                                        trim(c);
                                                                                25
19
       tipo s = v[i];
                                                                                        return c;
20
       forr(j, i+1, rw) s -= a[i][j]*x[p[j]];
                                                                                   }
                                                                                27
21
      x[p[i]] = s / a[i][i]; //aca divide
                                                                                    // a = a + b*(10^k)
22
     }
                                                                                    void addTo(vector<int>& a, const vector<int>& b, int k){
23
     ev = Mat(m-rw, Vec(m, 0)); // Esta parte va SOLO si se necesita el ev
                                                                                        if (a.size() < b.size() + k) a.resize(b.size() + k);</pre>
24
     forn(k, m-rw) {
                                                                                        for (int i = 0; i < b.size(); i++) a[i+k] += b[i];
25
                                                                                31
       ev[k][p[k+rw]] = 1;
26
                                                                                32
       dforn(i, rw){
                                                                                   void subFrom(vector<int>& a, const vector<int>& b){
27
         tipo s = -a[i][k+rw];
                                                                                        for (int i = 0; i < b.size(); i++) a[i] -= b[i];
28
        forr(j, i+1, rw) s -= a[i][j]*ev[k][p[j]];
                                                                                   }
                                                                                 35
29
         ev[k][p[i]] = s / a[i][i]; //aca divide
                                                                                    // a = a + b
30
       }
                                                                                   void addTo(vector<int>& a, const vector<int>& b){
31
                                                                                        addTo(a, b, 0);
     }
32
     return true;
33
                                                                                 39
34 }
                                                                                    vector<int> karatsuba(const vector<int>& a, const vector<int>& b)
                                                                                41
                            6.22 Karatsuba
                                                                                       int alen = a.size();
                                                                                       int blen = b.size();
                                                                                       if (alen == 0 || blen == 0) return vector<int>();
   // g++ -std=c++11 "karatsuba.cpp" -o hld
                                                                                       if (alen < blen) return karatsuba(b, a);
2
                                                                                        if (alen < 50) return multiply(a, b);
   /***
   47
                                                                                        int half = alen / 2;
   Complexity: O(N^1.7)
                                                                                 48
                                                                                        vector<int> a0(a.begin(), a.begin() + half);
   Call to karatsuba function paramter two vectors
                                                                                 49
                                                                                        vector<int> a1(a.begin() + half, a.end());
   * INPUT: two vectors A,B cointains the coeficients of the polynomail
                                                                                 50
                                                                                        vector<int> b0(b.begin(), b.begin() + min<int>(blen, half));
   * OUTPUT a vector coitains the coeficients of A * B
                                                                                51
                                                                                        vector<int> b1(b.begin() + min<int>(blen, half), b.end());
                                                                                 52
9
                                                                                 53
10
                                                                                        vector<int> z0 = karatsuba(a0, b0);
   int p,k;
11
                                                                                        vector<int> z2 = karatsuba(a1, b1);
   vector<int> b,r;
                                                                                        addTo(a0, a1);
13
                                                                                        addTo(b0, b1);
   void trim(vector<int>& a){
14
                                                                                        vector<int> z1 = karatsuba(a0, b0):
       while (a.size() > 0 \&\& a.back() == 0) a.pop_back();
15
                                                                                        subFrom(z1, z0);
                                                                                59
16
                                                                                        subFrom(z1, z2);
17
   vector<int> multiply(const vector<int>& a, const vector<int>& b){
                                                                                61
18
                                                                                        vector<int> res;
       vector<int> c(a.size() + b.size() + 1, 0);
                                                                                62
19
                                                                                        addTo(res, z0);
```

63

```
addTo(res, z1, half);
64
       addTo(res, z2, half + half);
                                                                                        35
65
66
                                                                                        36
       trim(res);
                                                                                                }
67
                                                                                        37
       return res;
68
                                                                                        38
69 }
                                                                                        39
                                                                                         40
                                   6.23 FFT
                                                                                        41
                                                                                                }
                                                                                         ^{42}
                                                                                            }
    #define lowbit(x) (((x) ^ (x-1)) & (x))
                                                                                         43
   typedef complex<long double> Complex;
                                                                                         44
   void FFT(vector<Complex> &A, int s){
                                                                                         46
       int n = A.size();
                                                                                         47
5
       int p = __builtin_ctz(n);
                                                                                         48
6
7
       vector<Complex> a = A;
                                                                                         50
8
                                                                                        51
9
       for(int i = 0; i < n; ++i){
                                                                                        52
10
            int rev = 0;
                                                                                         53
11
            for(int j = 0; j < p; ++j){
                                                                                        54
12
                rev <<= 1;
                                                                                        55
13
                rev |= ((i >> j) \& 1);
                                                                                         56
14
            }
                                                                                        57
15
            A[i] = a[rev];
                                                                                        58
16
       }
                                                                                        59
17
                                                                                         60
18
       Complex w,wn;
                                                                                        61
19
                                                                                         62
20
       for(int i = 1; i \le p; ++i){
21
            int M = (1 << i), K = (M >> 1);
22
            wn = Complex(cos(s*2.0*M_PI/(double)M), sin(s*2.0*M_PI/(double)M
23
                ));
^{24}
            for(int j = 0; j < n; j += M){
25
                w = Complex(1.0, 0.0);
26
                for(int 1 = j;1<K+j;++1){</pre>
27
                     Complex t = w;
28
                     t *= A[1 + K];
29
                     Complex u = A[1];
30
                     A[1] += t;
31
                     u -= t;
32
                     A[1 + K] = u;
33
```

```
w = wn;
34
               }
           }
       if(s==-1){
           for(int i = 0; i < n; ++i)
               A[i] /= (double)n;
   vector<Complex> FFT_Multiply(vector<Complex> &P, vector<Complex> &Q){
       int n = P.size()+Q.size();
       while(n!=lowbit(n)) n += lowbit(n);
       P.resize(n,0);
       Q.resize(n,0);
       FFT(P,1);
       FFT(Q,1);
       vector<Complex> R;
       for(int i=0;i<n;i++) R.push_back(P[i]*Q[i]);</pre>
       FFT(R,-1);
       return R;
   // Para multiplicacion de enteros grandes
   const long long B = 100000;
_{65} const int D = 5;
```

6.24 Tablas y cotas (Primos, Divisores, Factoriales, etc)

Factoriales

```
0! = 1
                  11! = 39.916.800
1! = 1
                  12! = 479.001.600 \ (\in int)
2! = 2
                  13! = 6.227.020.800
3! = 6
                  14! = 87.178.291.200
4! = 24
                  15! = 1.307.674.368.000
5! = 120
                  16! = 20.922.789.888.000
6! = 720
                  17! = 355.687.428.096.000
7! = 5.040
                  18! = 6.402.373.705.728.000
8! = 40.320
                  19! = 121.645.100.408.832.000
9! = 362.880
                  20! = 2.432.902.008.176.640.000 ( \in tint)
10! = 3.628.800 \mid 21! = 51.090.942.171.709.400.000
       max signed tint = 9.223.372.036.854.775.807
     max unsigned tint = 18.446.744.073.709.551.615
```

Primos

 $2\ 3\ 5\ 7\ 11\ 13\ 17\ 19\ 23\ 29\ 31\ 37\ 41\ 43\ 47\ 53\ 59\ 61\ 67\ 71\ 73\ 79\ 83\ 89\ 97\ 101\ 103\ 107\ 109$ $113\ 127\ 131\ 137\ 139\ 149\ 151\ 157\ 163\ 167\ 173\ 179\ 181\ 191\ 193\ 197\ 199\ 211\ 223\ 227$ 229 233 239 241 251 257 263 269 271 277 281 283 293 307 311 313 317 331 337 347 $349\ 353\ 359\ 367\ 373\ 379\ 383\ 389\ 397\ 401\ 409\ 419\ 421\ 431\ 433\ 439\ 443\ 449\ 457\ 461$ $463\ 467\ 479\ 487\ 491\ 499\ 503\ 509\ 521\ 523\ 541\ 547\ 557\ 563\ 569\ 571\ 577\ 587\ 593\ 599$ $601\ 607\ 613\ 617\ 619\ 631\ 641\ 643\ 647\ 653\ 659\ 661\ 673\ 677\ 683\ 691\ 701\ 709\ 719\ 727$ $733\ 739\ 743\ 751\ 757\ 761\ 769\ 773\ 787\ 797\ 809\ 811\ 821\ 823\ 827\ 829\ 839\ 853\ 857\ 859$ $863\ 877\ 881\ 883\ 887\ 907\ 911\ 919\ 929\ 937\ 941\ 947\ 953\ 967\ 971\ 977\ 983\ 991\ 997\ 1009$ 1013 1019 1021 1031 1033 1039 1049 1051 1061 1063 1069 1087 1091 1093 1097 1103 $1109\ 1117\ 1123\ 1129\ 1151\ 1153\ 1163\ 1171\ 1181\ 1187\ 1193\ 1201\ 1213\ 1217\ 1223\ 1229$ 1231 1237 1249 1259 1277 1279 1283 1289 1291 1297 1301 1303 1307 1319 1321 1327 1361 1367 1373 1381 1399 1409 1423 1427 1429 1433 1439 1447 1451 1453 1459 1471 1481 1483 1487 1489 1493 1499 1511 1523 1531 1543 1549 1553 1559 1567 1571 1579 $1583\ 1597\ 1601\ 1607\ 1609\ 1613\ 1619\ 1621\ 1627\ 1637\ 1657\ 1663\ 1667\ 1669\ 1693\ 1697$ 1699 1709 1721 1723 1733 1741 1747 1753 1759 1777 1783 1787 1789 1801 1811 1823 1831 1847 1861 1867 1871 1873 1877 1879 1889 1901 1907 1913 1931 1933 1949 1951 1973 1979 1987 1993 1997 1999 2003 2011 2017 2027 2029 2039 2053 2063 2069 2081

Primos cercanos a 10^n

9941 9949 9967 9973 10007 10009 10037 10039 10061 10067 10069 10079 99961 99971 99989 99991 100003 100019 100043 100049 100057 100069 999959 999961 999979 999983 1000003 1000033 1000037 1000039 9999943 9999971 99999991 10000019 10000079 10000103 10000121 99999941 99999959 99999971 99999989 100000007 100000037 100000039 100000049 999999893 99999929 99999937 1000000007 1000000009 1000000021 1000000033

Cantidad de primos menores que 10^n

```
Divisores

Cantidad de divisores (\sigma_0) para algunos\ n/\neg\exists n'< n, \sigma_0(n')\geqslant \sigma_0(n)

\sigma_0(60)=12; \sigma_0(120)=16; \sigma_0(180)=18; \sigma_0(240)=20; \sigma_0(360)=24

\sigma_0(720)=30; \sigma_0(840)=32; \sigma_0(1260)=36; \sigma_0(1680)=40; \sigma_0(10080)=72

\sigma_0(15120)=80; \sigma_0(50400)=108; \sigma_0(83160)=128; \sigma_0(110880)=144

\sigma_0(498960)=200; \sigma_0(554400)=216; \sigma_0(1081080)=256; \sigma_0(1441440)=288

Suma de divisores (\sigma_1) para algunos\ n/\neg\exists n'< n, \sigma_1(n')\geqslant \sigma_1(n)

\sigma_1(96)=252; \sigma_1(108)=280; \sigma_1(120)=360; \sigma_1(144)=403; \sigma_1(168)=480

\sigma_1(960)=3048; \sigma_1(1008)=3224; \sigma_1(1080)=3600; \sigma_1(1200)=3844

\sigma_1(4620)=16128; \sigma_1(4680)=16380; \sigma_1(5040)=19344; \sigma_1(5760)=19890

\sigma_1(8820)=31122; \sigma_1(9240)=34560; \sigma_1(10080)=39312; \sigma_1(10920)=40320

\sigma_1(32760)=131040; \sigma_1(35280)=137826; \sigma_1(36960)=145152; \sigma_1(37800)=148800

\sigma_1(60480)=243840; \sigma_1(64680)=246240; \sigma_1(65520)=270816; \sigma_1(70560)=280098
```

 $\sigma_1(95760) = 386880$; $\sigma_1(98280) = 403200$; $\sigma_1(100800) = 409448$

 $\sigma_1(491400) = 2083200 : \sigma_1(498960) = 2160576 : \sigma_1(514080) = 2177280$

 $\sigma_1(982800) = 4305280$; $\sigma_1(997920) = 4390848$; $\sigma_1(1048320) = 4464096$ $\sigma_1(4979520) = 22189440$; $\sigma_1(4989600) = 22686048$; $\sigma_1(5045040) = 23154768$

 $\sigma_1(9896040) = 44323200$; $\sigma_1(9959040) = 44553600$; $\sigma_1(9979200) = 45732192$

 $\pi(10^1) = 4 : \pi(10^2) = 25 : \pi(10^3) = 168 : \pi(10^4) = 1229 : \pi(10^5) = 9592$

 $\pi(10^6) = 78.498$; $\pi(10^7) = 664.579$; $\pi(10^8) = 5.761.455$; $\pi(10^9) = 50.847.534$

 $\pi(10^{10}) = 455.052.511$; $\pi(10^{11}) = 4.118.054.813$; $\pi(10^{12}) = 37.607.912.018$

7 Grafos

7.1 Bellman-Ford

```
int negative_cycle(vector<vector<int> > &G, vector<vector<int> > &cost)
       {
     //write your code here
2
     bool nc = false;
3
     int n = G.size();
4
     vector<int>dist(n,INT_MAX / 2);
5
     dist[0] = 0;
     for(int i = 0; i < n - 1; i++)
     for(int u = 0: u < n:u++)
       for(int j = 0; j < G[u].size();j++){</pre>
9
         int v = G[u][i]:
10
         int w = cost[u][i];
11
         dist[v] = min(dist[v], dist[u] + w);
12
13
```

```
for(int u = 0; u < n; u++){
14
     for(int j = 0; j < G[u].size();j++){</pre>
15
       int v = G[u][j];
16
       int w = cost[u][j];
17
       if(dist[v] > dist[u] + w)nc = true;
18
     }
19
     }
20
     return nc;
21
  |}
22
```

7.2 dijkstra grafos densos

7.3 2 SAT definitivamente no con Tarjan

```
// g++ -std=c++11 "twosat.cpp" -o run
   /***
       Complexity: O(N)
  Input: number of variables, then number of clause clauses in format (u
      or v)
  if u,v > 0 then is equivalent to u,v
  if u, v < 0 then is equivalent to u, v
  Output: UNSATISFIABLE can't find a solution
  SATISFIABLE if exist a solution then print the assignment of all
      variables (negative for xi = false)
10
  Examples:
11
  Input:
  3 3
13
  1 -3
14
  -1 2
15
   -2 -3
16
  Output
17
  SATISFIABLE
  1 2 -3
19
20
  Input
^{21}
  1 2
22
  1 1
23
  -1 -1
  Output
25
   UNSATISFIABLE
27
28 | #include <bits/stdc++.h>
```

```
using namespace std;
   vector<int>G[2][2000010],G2[2000010];
   int n, m;
   int scc[2000010];
   bool vis[2000010];
   vector<int>comp[2000010];
   int assign[2000010];
   int cc = 0;
   stack<int>st;
   vector<int>sta;
   void dfs(int u,int type){
    if(scc[u] != -1)return;
    scc[u] = cc:
    for(int v:G[type][u]){
       dfs(v,type);
    }
     if(!type)st.push(u);
45
46
   void topo(int u){
47
     if(vis[u])return;
     vis[u] = true;
49
     for(int v:G2[u])topo(v);
50
     sta.push_back(u);
51
52
   void buildGraphWitouthLoop(){
53
     for(int i = 0; i < 2 * n; i++){
       for(int j = 0; j < G[0][i].size(); j++){</pre>
55
         if(scc[i] != scc[G[0][i][j]])
56
           G2[scc[i]].push_back(scc[G[0][i][j]]);
       }
    }
59
60
  int main() {
       ios::sync_with_stdio(false);cin.tie(0);
       cin >> n >> m;
   for(int i = 0,u,v; i < m;i++){
       cin >> u >> v;
       int uu = (u > 0?(u - 1) * 2:(-u - 1) * 2 + 1):
       int vv = (v > 0?(v - 1) * 2:(-v - 1) * 2 + 1);
    // cout << uu << " " << (uu ^ 1) << "\n";
       G[0][uu ^ 1].push_back(vv);
       G[0][vv ^ 1].push_back(uu);
70
       G[1][vv].push_back(uu ^ 1);
71
```

```
G[1] [uu] .push_back(vv ^ 1);
72
73
      memset(scc,-1,sizeof scc);
74
      for(int i = 0; i < 2 * n; i++){
75
        if(scc[i] == -1)dfs(i,0);
76
      }
77
      memset(scc,-1,sizeof scc);
78
      while(!st.empty()){
79
        int u = st.top();st.pop();
80
        if(scc[u] == -1){
81
          dfs(u,1);
82
          cc++;
83
        }
84
      }
85
      bool unsat = false;
86
      for(int i = 0; i < 2 * n; i++){
87
        if(scc[i] == scc[i ^ 1])unsat = true;
88
        comp[scc[i]].push_back(i);
89
      }
90
      if(unsat){
91
        return cout << "UNSATISFIABLE",0;</pre>
92
      }
93
      cout << "SATISFIABLE\n";</pre>
94
      buildGraphWitouthLoop();
95
      for(int i = 0; i < 2 * n; i++){
96
        if(!vis[i])topo(i);
97
      }
98
      for(int u:sta){//inverse of topological sort
99
        for(int v:comp[u]){//transitivite Skew-Symmetry
100
          if(!assign[v]){
101
            assign[v] = 1;
102
            assign[v ^ 1] = -1;
103
          }
104
        }
105
106
      for(int i = 0, j = 1; i < 2 * n; i += 2, j++){
107
        cout << (j) * (assign[i]) << "";</pre>
108
      }
109
        return 0;
110
111 }
```

7.4 Prim

7.5 Articulataion Points (desgraciadamente tarjan)

```
1 // g++ -std=c++11 "articulationpointsandbridges.cpp" -o run
2
   /***
   ========== <Articulation points and bridges c++ version>
  Given a graph return a vector of paris with the bridges and a bool array
  true if the node is an articulation point
   * false otherwise
   Graph nodes: 0 to N - 1
   */
   using namespace std;
   vector<int>G[10010];
   int low[10010],num[10010],parent[10010],cc;
   //cc is my timer
int art[10010];//bool for detect art point, int for detect how many
       nodes are connected to my articulation point
int root,rC;
   int n;
15
   vector<pair<int,int> >bridges;
   void dfs(int u){
     low[u]=num[u]=cc++:
     for(int v:G[u]){
19
       if(num[v]==-1){
20
         parent[v]=u;
21
         if(u==root)rC++;
22
         dfs(v);
23
         if(low[v]>=num[u])art[u]++;//is a articulation point
24
         if(low[v]>num[u])bridges.push_back({u,v});//this is a bridge
25
         low[u]=min(low[u],low[v]);
26
27
       else if(v!=parent[u]){
28
           low[u]=min(low[u],num[v]);
29
30
     }
31
32
   void init(){
     bridges.clear();
34
    for(int i=0;i<n;i++){
35
       art[i]=low[i]=0;
36
```

if(low[next]>=dfn[cur]) cache_bc(cur,next);

}else low[cur] = min(low[cur],dfn[next]);

26

27

```
num[i]=parent[i]=-1;
37
                                                                                28
       G[i].clear();
                                                                                29
38
     }
39
                                                                                30
     cc=0;
                                                                                   void biconn_comp(){
40
                                                                                31
                                                                                       memset(dfn,-1,sizeof(dfn));
41
                                                                                32
   void callARTBRID(){
                                                                                       C.clear();
                                                                                33
     for(int i=0;i<n;i++){
                                                                                       DFS(0,0,0);
43
                                                                                34
       if(num[i]==-1){
                                                                                       int comp = C.size();
44
        root=i,rC=0;dfs(i);
                                                                                       printf("%d\n",comp);
45
         art[root]=(rC>1);
                                                                                       for(int i = 0; i < comp; ++i){
46
       }
                                                                                           sort(C[i].begin(),C[i].end());
47
                                                                                38
     }
                                                                                           C[i].erase(unique(C[i].begin(),C[i].end()),C[i].end());
48
                                                                                39
                                                                                           int m = C[i].size():
  | }
49
                                                                                40
                                                                                           for(int j = 0; j < m; ++j) printf("%d<sub>1</sub>",1 + C[i][j]);
                                                                                41
          componentes biconexas y puentes (block cut tree)
                                                                                           printf("\n");
                                                                                42
                                                                                       }
                                                                                43
                                                                                44 }
  |int V;
   vector<int> G[MAXN];
                                                                                                         LCA saltitos potencias de 2
   int dfn[MAXN],low[MAXN];
   vector< vector<int> > C;
                                                                                                  7.8 LCA sparse table query O(1)
   stack< pair<int, int> > stk;
                                                                                                                 7.9 HLD
   void cache_bc(int x, int y){
       vector<int> com;
7
                                                                                 1 // g++ -std=c++11 "hld.cpp" -o hld
       int tx,ty;
8
       do√
9
                                                                                2
           tx = stk.top().first, ty = stk.top().second;
                                                                                   /***
10
           stk.pop();
                                                                                    11
           com.push_back(tx), com.push_back(ty);
                                                                                   Complexity: O(N*log (N))
12
       }while(tx!=x || ty!=y);
                                                                                   Given a tree and asociative operation in the paths of this tree ask for
13
      C.push_back(com);
                                                                                       many querys, and updates
14
                                                                                   in nodes or edges
15
                                                                                   Input of this example:
16
   void DFS(int cur, int prev, int number){
                                                                                   N number of nodes, then N elements values in each node
17
       dfn[cur] = low[cur] = number;
                                                                                   then n - 1 conections
18
       for(int i = G[cur].size()-1;i>=0;--i){}
                                                                                   Q querys if T == 1 query on the path u,v
19
                                                                                   else update node U with value val.
           int next = G[cur][i];
20
           if(next==prev) continue;
                                                                                13
^{21}
           if(dfn[next]==-1){
                                                                                   Example problems: Spoj QTREE1 to QTREE6, toby and tree UVA
22
                                                                                14
               stk.push(make_pair(cur,next));
                                                                                   */
                                                                                15
23
               DFS(next,cur,number+1);
24
                                                                                16
               low[cur] = min(low[cur], low[next]);
                                                                                   #include <bits/stdc++.h>
25
```

using namespace std;

const int maxn = 1e5;

```
const int NEUTRO = 0; // a null value for my ST
   int vec[maxn];
21
   vector<int>G[maxn]; //the graph
   //int idx[maxn]; // case with value in the edge
   int op(int u,int v){// an operation for my path (using ST)
    //return __gcd(u,v);
25
     //return max(u,v);
     return u + v;
27
28
   int n;
   //ask to Branimir for information about this
   struct SegmentTree{
     int T[2*maxn];
32
     void init(){
33
       memset(T,0,sizeof T);
34
35
     void set(int pos,int val){
36
       pos += n;
37
       T[pos] = val:
38
       for(pos >>= 1; pos > 0; pos >>=1){
39
         T[pos] = op(T[pos << 1], T[(pos << 1)|1]);
40
       }
41
42
     int query(int 1,int r){
43
       1 += n;
44
       r += n;
45
       int ans = NEUTRO;
46
       while (1 < r)
47
         if (1 \& 1) ans = op(ans, T[1++]);
48
         if (r \& 1) ans = op(ans, T[--r]);
49
         1 >>= 1;
50
         r >>= 1;
51
       }
52
       return ans:
53
     }
54
55
   struct hld{
56
     int ncad: // store actual number of chain
57
     int root; // the root of a tree generally 0 or 1
58
     int pos; // pos of node in chain
59
60
     int sz[maxn]; // store the subsize of subtrees
61
     int depth[maxn]; //depth of the node, useful for LCA via HLD
62
```

```
int parent[maxn]; // useful for LCA
63
      int where[maxn]; // where chain is the node?
64
      //int edgepos[maxn]; // if the value is on the edge: stored in a node
65
      int chainIdx[maxn]; // position in the chain of the node
66
      int head[maxn]; // the head of the i-th chain
67
      //int val[maxn]; // if the value is on the edge
68
      SegmentTree tree; // this ST allow operations in the path
69
70
      void init(){//settings value, and process de HLD
71
        root = 0;
        ncad = 0;
73
        pos = 0;
74
        for(int i = 0: i \le n: i++){
75
          where[i] = head[i] = -1;
77
        depth[root] = 0;
        dfs(root , -1);
79
        descompose(root);
        tree.init():
        /* case with values in edges
        for(int i=0;i<n;i++){
          tree.set(i,val[i]);
       }
85
        */
86
     }
87
88
89
      ///init descomposition
90
      void dfs(int u,int pu){
91
        sz[u] = 1; //init the sz of this subtree
92
        parent[u] = pu; // assign the parent
93
        for(int i = 0; i < G[u].size(); i++){</pre>
94
          int v = G[u][i]:
95
          if ( v == pu )continue;
          //edgepos[idx[u][i]] = v;
97
          depth[v] = depth[u] + 1;
98
          dfs(v,u);
          sz[u] += sz[v]:
100
        }
101
102
      //descompose graph in HLD descomposition
103
      void descompose(int u){
104
        if( head[ncad] == -1)head[ncad] = u; // the head of ncad is u
105
```

```
where[u] = ncad; // assign where tu node
                                                                                                      ); value in edges
106
        //val[pos] = cost; cost another parameter in descompose for graphs
                                                                                                  return op(ans, tree.query( chainIdx[v], chainIdx[u] + 1) );
                                                                                      147
107
            with values in edges
                                                                                      148
        chainIdx[u] = pos++; //assing pos to this node
                                                                                                int hu = head[uChain];
                                                                                      149
108
        int maxi = -1, sc = -1; //finding a special child
                                                                                                ans = op( ans, tree.guery(chainIdx[hu], chainIdx[u] + 1) );
                                                                                      150
109
        for(int v:G[u]){
                                                                                                u = parent[hu];
110
                                                                                      151
          if (sz[v] > maxi && where[v] == -1){
                                                                                      152
111
            maxi = sz[v];
                                                                                           }
                                                                                      153
112
            sc = v;
                                                                                      154
113
                                                                                           int Q(int u,int v){
                                                                                      155
114
        }
                                                                                              int L = lca(u,v);
115
                                                                                      156
        if(sc != -1)descompose(sc);
                                                                                              return op( query(u,L) , query(v,L) );
116
                                                                                      157
        //light nodes here:
                                                                                           }
117
                                                                                      158
        for(int v:G[u]){
                                                                                         }HLD;
                                                                                      159
118
          if(where[v] == -1){}
                                                                                         int main(){
119
            ncad++:
                                                                                           //ios::sync_with_stdio(false);cin.tie(0);
120
                                                                                           while(cin >> n){
            descompose(v);
121
                                                                                      162
          }
                                                                                              for(int i = 0; i < n; i++)G[i].clear();
                                                                                      163
122
        }
                                                                                              for(int i = 0: i < n: i++){
123
      }
                                                                                                cin >> vec[i];
                                                                                      165
124
      ///end descomposition
                                                                                              }
                                                                                      166
125
                                                                                              for(int i = 1, u,v ; i < n; i++){
126
                                                                                      167
      int lca(int u,int v){
                                                                                                cin >> u >> v;
                                                                                      168
127
        while(where[u]!=where[v]){
                                                                                                G[u].push_back(v);
                                                                                      169
128
          if(depth[ head[ where[u] ] ] > depth[ head[ where[v] ] ])u =
                                                                                                G[v].push_back(u);
                                                                                      170
129
              parent[ head[ where[u] ] ];
                                                                                                /* case with value in edges
                                                                                      171
          else v = parent[ head[ where[v] ] ];
                                                                                                 G[u].push_back(make_pair(v,w));
                                                                                      172
130
                                                                                                idx[u].push_back(i-1);
                                                                                      173
131
        return depth[u] < depth[v] ? u:v;</pre>
                                                                                                G[v].push_back(make_pair(u,w));
                                                                                      174
132
      }
                                                                                                idx[v].push_back(i-1);
                                                                                      175
133
134
                                                                                      176
      void update(int u, int val){
                                                                                                 */
                                                                                      177
135
                                                                                              }
        tree.set(chainIdx[u],val);
                                                                                      178
136
      }
                                                                                              HLD.init():
                                                                                      179
137
                                                                                              for(int i = 0; i < n; i++){
                                                                                      180
138
      int query(int u,int v){
                                                                                                HLD.update(i, vec[i]);
                                                                                      181
139
                                                                                              }
        // if ( u == v) return NEUTRO; value in edges
                                                                                      182
140
        int vChain = where[v]:
                                                                                              int question;
                                                                                      183
141
        int ans = NEUTRO;
                                                                                              cin >> question;
                                                                                      184
142
                                                                                              for(int i = 0, t, u ,v; i < question; i++){
        while(true){
                                                                                      185
143
          int uChain = where[u];
                                                                                                cin >> t >> u >> v;
                                                                                      186
144
          if(uChain == vChain){
                                                                                                if(t == 1){}
                                                                                      187
145
            // return op(ans, tree.query( chainIdx[v] + 1, chainIdx[u] + 1)
                                                                                                  cout \ll HLD.Q(u,v) \ll "\n";
146
                                                                                     188
```

7.10 centroid descomposition

7.11 euler cycle

```
int n,m,ars[MAXE], eq;
   vector<int> G[MAXN];//fill G,n,m,ars,eq
   list<int> path;
   int used[MAXN];
   bool usede[MAXE];
   queue<list<int>::iterator> q;
   int get(int v){
     while(used[v]<sz(G[v]) && usede[ G[v][used[v]] ]) used[v]++;</pre>
     return used[v];
10
   void explore(int v, int r, list<int>::iterator it){
     int ar=G[v][get(v)]; int u=v^ars[ar];
12
     usede[ar]=true:
13
     list<int>::iterator it2=path.insert(it, u);
14
     if(u!=r) explore(u, r, it2);
15
     if(get(v)<sz(G[v])) q.push(it);</pre>
16
17
   void euler(){
18
     zero(used), zero(usede);
19
     path.clear();
20
     q=queue<list<int>::iterator>();
21
     path.push_back(0); q.push(path.begin());
^{22}
     while(sz(q)){
23
       list<int>::iterator it=q.front(); q.pop();
24
       if(used[*it] < sz(G[*it])) explore(*it, *it, it);</pre>
^{25}
26
     reverse(path.begin(), path.end());
27
28
   void addEdge(int u, int v){
29
     G[u].pb(eq), G[v].pb(eq);
30
     ars[eq++]=u^v;
31
32 | }
```

7.12 diámetro y centro de un árbol

```
====== <Diameter and center of a tree> ==========
   //Problem: Given a tree get the center (or centers)
4 /* the nodes in the tree that minimize the length of the longest path
       from it to any other node.
   * *Finding tree centers:
   * If diameter length is even, then we have one tree center. If odd,
        then we have 2 centers.
   * E.g. 1-2-3-4-5 -> center is 3
    * E.g. 1-2-3-4-5-6 \rightarrow center is 3, 4
    * On other side, we can get the worst nodes through the center nodes.
    * A worst node is one that is an end of a diameter, so it has the worst
         tree height
   Input:
11
   * No
   Output:
   * No
   dfs: calculate the diameter of the tree
   * maxi stores the diameter
   findingCenters() return the centers
   Nodes in graph 1 to N careful with this
   Complexity: O(N)
   */
20
21
22
   vector<int>G[5010];
   int maxi=-1,far;
   int n;
25
   int pre[5010];
   int Queue[5010];
28
   void dfs(int path,int u,int parent){
     pre[u]=parent;
30
     if(path>=maxi){
31
       maxi=path;
32
       far=u:
33
34
     for(int v:G[u]){
35
       if(parent!=v){
36
         dfs(path+1,v,u);//path + w if the graph as weighted
37
38
```

```
39
   }
40
   pair<int,int> findingCenters(){
41
     maxi=-1;
42
     dfs(0,1,-1);
43
     dfs(0,far,-1);
44
     int t=far,L=0;
45
     while(t!=-1){
46
       Queue[L]=t;
47
       t=pre[t];
48
       ++L;
49
     }
50
     int a=-1,b=-1;
     if(L&1){
52
       a=Queue[L/2];
53
     }
54
     else{
55
       a=min(Queue[L/2-1],Queue[L/2]),b=max(Queue[L/2-1],Queue[L/2]);
56
     }
57
     return {a,b};
58
59 }
```

7.13 algoritmo hungaro

7.14 union find dinámico

```
#include <bits/stdc++.h>
   using namespace std;
   \#define dprint(v) cerr << \#v"=" << v << endl //;)
   #define forr(i,a,b) for(int i=(a); i<(b); i++)</pre>
   #define forn(i,n) forr(i,0,n)
   #define dforn(i,n) for(int i=n-1; i>=0; i--)
   #define forall(it,v) for(auto it=v.begin();it!=v.end();++it)
   #define sz(c) ((int)c.size())
   #define zero(v) memset(v, 0, sizeof(v))
   #define pb push_back
   #define fst first
11
   #define snd second
   #define mkp make_pair
   typedef long long 11;
   typedef pair<int,int> ii;
15
16
  struct UnionFind {
17
       int n, comp;
18
```

```
vector<int> pre,si,c;
19
       UnionFind(int n=0):n(n), comp(n), pre(n), si(n, 1) {
20
           forn(i,n) pre[i] = i; }
21
       int find(int u){return u==pre[u]?u:find(pre[u]);}
22
       bool merge(int u, int v) {
23
           if((u=find(u))==(v=find(v))) return false;
24
           if(si[u]<si[v]) swap(u, v);</pre>
25
           si[u]+=si[v], pre[v]=u, comp--, c.pb(v);
           return true;
27
       }
28
       int snap(){return sz(c);}
29
       void rollback(int snap){
30
           while(sz(c)>snap){
31
                int v = c.back(); c.pop_back();
32
                si[pre[v]] -= si[v], pre[v] = v, comp++;
33
34
       }
35
   };
36
   enum {ADD,DEL,QUERY};
   struct Query {int type,u,v;};
   struct DynCon {
       vector<Query> q;
       UnionFind dsu;
41
       vector<int> match,res;
42
       map<ii,int> last;//se puede no usar cuando hay identificador para
43
           cada arista (mejora poco)
       DynCon(int n=0):dsu(n){}
44
       void add(int u, int v) {
45
           if(u>v) swap(u,v);
46
           q.pb((Query){ADD, u, v}), match.pb(-1);
47
           last[ii(u,v)] = sz(q)-1;
48
49
       void remove(int u, int v) {
50
           if(u>v) swap(u,v);
51
           q.pb((Query){DEL, u, v});
52
           int prev = last[ii(u,v)];
53
           match[prev] = sz(q)-1;
54
           match.pb(prev);
55
56
       void query() {//podria pasarle un puntero donde guardar la respuesta
57
           q.pb((Query){QUERY, -1, -1}), match.pb(-1);}
58
       void process() {
59
           forn(i,sz(q)) if (q[i].type == ADD && match[i] == -1) match[i] =
60
```

```
}
                sz(q);
                                                                                  99
           go(0,sz(q));
                                                                                              if(!k) continue;//k==0 WTF
                                                                                  100
61
                                                                                              dc.process();
                                                                                  101
62
       void go(int 1, int r) {
                                                                                              forn(i,sz(dc.res)) cout << dc.res[i] << endl;</pre>
63
                                                                                  102
           if(l+1==r){
                                                                                          }
                                                                                  103
64
               if (q[1].type == QUERY)//Aqui responder la query usando el
                                                                                          return 0;
                                                                                  104
65
                                                                                  105 }
                   res.pb(dsu.comp);//aqui query=cantidad de componentes
66
                                                                                  7.15 truquitos estúpidos por ejemplo second MST es con LCA
                        conexas
                                                                                                               7.16 erdos galloi
               return;
67
68
           int s=dsu.snap(), m = (l+r) / 2;
69
                                                                                   1 // g++ -std=c++11 "erdosgalloi.cpp" -o run
           forr(i,m,r) if(match[i]!=-1 && match[i]<1) dsu.merge(q[i].u, q[i</pre>
70
               ].v);
                                                                                         ======== <Erdosgalloi c++ version> =========
           go(1,m);
                                                                                   4 Given the grades of each node of a graph return if this form a valid
71
           dsu.rollback(s);
72
                                                                                          graph
           s = dsu.snap();
73
                                                                                   5 includes: algorithm, functional, numeric, forn
           forr(i,1,m) if(match[i]!=-1 && match[i]>=r) dsu.merge(q[i].u, q[
                                                                                     // Receives a sorted degree sequence (non ascending)
74
               il.v):
                                                                                     O(NlgN)
           go(m,r);
75
                                                                                   8
           dsu.rollback(s);
76
       }
77
                                                                                     bool isGraphicSequence(const vector<int> &seq) // O(n lg n)
   }dc;
78
                                                                                  11
79
                                                                                       vector<int> sum:
                                                                                  12
   // Problema ejemplo: http://codeforces.com/gym/100551/problem/A
                                                                                       int n = seq.size();
80
                                                                                  13
81
                                                                                  14
   int n,k;
                                                                                       if (n == 1 \&\& seq[0] != 0) return false;
82
                                                                                  15
83
                                                                                  16
   int main() {
                                                                                        sum.reserve(n + 1);
84
                                                                                  17
       //~ freopen("in", "r", stdin);
85
                                                                                        sum.push_back(0);
                                                                                  18
       freopen("connect.in", "r", stdin);
                                                                                       for (int i = 0; i < n; ++i) sum.push_back(sum[i] + seq[i]);</pre>
86
                                                                                  19
       freopen("connect.out", "w", stdout);
                                                                                        if ((sum[n] \& 1) == 1) return false;
87
                                                                                  20
       ios::sync_with_stdio(0);
88
                                                                                  21
       while(cin \gg n \gg k){
                                                                                       for (long long k = 1; k \le n - 1 & seq[k - 1] >= k; ++k) {
89
                                                                                  22
       dc=DynCon(n);
                                                                                          int j = distance(seq.begin(), upper_bound(seq.begin() + k, seq.end()
90
                                                                                  23
       forn(_,k) { string ord; cin >> ord;
91
                                                                                              , k,
         if (ord=="?") {
92
                                                                                                                                     greater<int>())) +
                                                                                  24
           dc.query();
                                                                                                  1;
93
                                                                                  25
         } else if (ord=="+") { int a,b; cin>>a>>b; a--;b--;
                                                                                         long long left = sum[k];
94
                                                                                  26
           dc.add(a,b);
                                                                                         long long right = k * (k - 1) + (j - k - 1) * k + (sum[n] - sum[j - k])
95
                                                                                  27
         } else if (ord=="-") { int a,b; cin>>a>>b; a--;b--;
96
                                                                                              1]);
           dc.remove(a,b);
97
                                                                                  28
         } else assert(false);
98
                                                                                          if (left > right) return false;
                                                                                  29
```

```
30 }
31 return true;
33 }
```

7.17 grafo funcional hallar k-esimo partiendo de un nodo

7.18 konig

- 7.19 min-vertex cover bipartitos
- 7.20 max-flow (min cost versión)

```
1 // g++ -std=c++11 "maxflowmincost.cpp" -o run
   /***
2
             ====== <Max flow-min cost c++ version> ==
   Given a grapth with edges with a capacity C and weight D
   * compute the max-flow min cost
   Edmond karps idea
   * Complexity O(v *E*log(v))
   Problem for practice: Dijkstra Dijkstra uva
   #define REP(i,j,k) for(int (i)=(j);(i)<(k);++(i))
   #define MP make_pair
12
   using namespace std;
13
14
   #define MAXN 500
15
   #define MAXM MAXN * 5
   typedef vector<int> VI;
   typedef long long 11;
   const int INF = 1E9; // $infinity$: be careful to make this big enough
       111
  int S; // source
   int T; // sink
   int FN; // number of nodes
  int FM; // number of edges (initialize this to 0)
   // ra[a]: edges connected to a (NO MATTER WHICH WAY!!!); clear this in
       the beginning
  VI ra[MAXN];
  int kend[MAXM], cap[MAXM], cost[MAXM]; // size: TWICE the number of
       edges
27
  // Adds an edge from a to b with capacity c and cost d and returns the
```

```
number of the new edge
29
   int addedge(int a, int b, int c, int d) {
     int i = 2*FM;
     kend[i] = b;
32
     cap[i] = c;
33
     cost[i] = d;
34
     ra[a].push_back(i);
     kend[i+1] = a;
     cap[i+1] = 0;
     cost[i+1] = -d;
38
     ra[b].push_back(i+1);
39
     FM++:
40
     return i;
42
   int n:
   int dst[MAXM], pre[MAXM], pret[MAXM];
   //finding the shortest path via fanding duan, also it works with bellman
         ford
   //or dijkstra (careful of negative cycles)
   bool spfa(){
     REP(i,0,FN) dst[i] = INF;
     dst[S] = 0;
49
     queue<int> que; que.push(S);
50
     while(!que.empty()){
51
       int x = que.front(); que.pop();
       for (int t : ra[x]){
         int y = kend[t], nw = dst[x] + cost[t];
         if(cap[t] > 0 && nw<dst[y]){</pre>
55
           dst[y] = nw; pre[y] = x; pret[y] = t; que.push(y);
56
         }
57
58
59
     return dst[T]!=INF;
60
61
    // returns the maximum flow and the minimum cost for this flow
   pair<11,11> solve(){
     11 \text{ totw} = 0, \text{ totf} = 0;
64
     while(spfa()){
65
       int minflow = INF;
       for (int x = T; x!=S; x = pre[x]){
67
         minflow = min(minflow, cap[pret[x]]);
68
69
```

int edge = 0;

```
for (int x = T; x!=S; x = pre[x]){
70
         cap[pret[x]] -= minflow;
71
         cap[pret[x]^1] += minflow;
72
73
       totf += minflow;
74
       totw += minflow*dst[T];
75
76
     return make_pair(totf, totw);
77
78
    void init(){
79
     FN=4*n+15;//make this big n=number of nodes of the graph
80
     FM=0;
81
     S=0.T=n+1:
82
     for(int i=0;i<FN;i++)ra[i].clear();//clear the graph be careful</pre>
84 }
```

7.21 max-flow corto con matriz

```
1 // g++ "maxflowMVEK.cpp" -o run
   /***
2
    ========== <Max Flow with matriz Edmonds karp c++ version>
       _____
   //Given a graph with capacitys find the max-flow
   Nodes indexed 1 to N
   * Complexity O(N *E)
   Problem for practice: UVA 820
   #define N 500
   int cap[N][N], pre[N], n;
   int s://source
   int t://destination
   bool bfs() {
14
       queue<int>q;
15
       q.push(s);
16
       memset(pre,-1,sizeof pre);
17
       pre[s]=s;
18
       while(!q.empty()){
19
           int u=q.front();q.pop();
20
           if(u==t)return true;
21
           for(int i=1;i \le n;i++){//nodes 1 to n
22
               if(pre[i] == -1&&cap[u][i])pre[i] = u,q.push(i);
23
           }
24
```

```
}
25
       return false;
26
   }
27
28
   int maxFlow() {
29
       int mf=0,f,v;//max flow, flow for a path, the vertex
       while(bfs()){//while encountered a path source to destination
31
           v=t;//min
32
           f=INT_MAX;//make this big enough
33
           while(pre[v]!=v){f=min(f,cap[pre[v]][v]),v=pre[v];}//finding the
34
                min capacity
           v=t;mf+=f;
35
           while(pre[v]!=v){cap[pre[v]][v]-=f,cap[v][pre[v]]+=f,v=pre[v];}
36
               //update the flow
       }
37
       return mf;
38
   }
39
   void init(){
     memset(cap,0,sizeof cap);
41
     //cap[u][v]+=capacidad,cap[v][u]+=capacidad
42
43 }
                      7.22 max-flow sin matriz
1 // g++ -std=c++11 "maxflowNMEK.cpp" -o run
  /***
   ========== <Max Flow with-out matriz Edmonds karp c++ version>
   //Given a graph with capacitys find the max-flow
   Nodes indexed 1 to N
  * Complexity O(N *E)
  Problem for practice: UVA 820
   * Input N number of nodes,
   * M edges conections
   st compute the flow with source 1 and sink N
11
12
   using namespace std;
13
   const int N = 110;
15 const int M = 10010 * 2;
   vector<int>G[N];
int kend[M], cap[M], cost[M];
```

```
int s.t:
19
   void add(int u,int v,int c){
     int forward = edge * 2, backward = edge * 2 + 1;
21
     kend[forward] = v;
^{22}
     cap[forward] = c;
23
     G[u].push_back(forward);
24
     kend[backward] = u;
     cap[backward] = 0;
26
     G[v].push_back(backward);
     edge++;
28
29
   int vis[M],pre[M],pret[M];
   bool bfs(){
     for(int i = 0: i \le 100:i++)vis[i] = false:
     vis[s] = true;
     queue<int>q;
34
     q.push(s);
35
     while(!q.empty()){
36
       int u = q.front();q.pop();
37
       for(int edge:G[u]){
38
         int v = kend[edge];
39
         if(cap[edge] > 0 && !vis[v]){
40
           vis[v] = true;
41
           pre[v] = u;
42
           pret[v] = edge;//the edge store the information
43
           q.push(v);
44
         }
45
       }
46
47
     return vis[t];
48
49
   int max flow(){
     int totf = OLL:
51
     while(bfs()){
52
       int minflow = INT_MAX;
53
       for(int x = t; x != s; x = pre[x]){
54
         minflow = min(minflow,cap[pret[x]]);
55
       }
56
       for(int x = t; x != s; x = pre[x]){
57
         cap[pret[x]] -= minflow;
58
         cap[pret[x] ^ 1] += minflow;
59
       }
60
       totf += minflow;
61
```

```
62
     return totf;
63
   }
64
   int main(){
65
     int n,m;
66
     scanf("%d_{\sqcup}%d",&n,&m);
     for(int i = 0,u,v,ca; i < m;i++){
       scanf("%du%du,&u,&v,&ca);
       add(u,v,ca);
    }
     s = 1, t = n;
72
     printf("%lld\n",max_flow());
73
74 }
```

7.23 Dinic

```
2 const int MAX = 300;
3 // Corte minimo: vertices con dist[v]>=0 (del lado de src) VS. dist[v
       l==-1 (del lado del dst)
4 // Para el caso de la red de Bipartite Matching (Sean V1 y V2 los
       conjuntos mas proximos a src y dst respectivamente):
5 // Reconstruir matching: para todo v1 en V1 ver las aristas a vertices
       de V2 con it->f>0, es arista del Matching
6 // Min Vertex Cover: vertices de V1 con dist[v]==-1 + vertices de V2 con
        dist[v]>0
7 // Max Independent Set: tomar los vertices NO tomados por el Min Vertex
s // Max Clique: construir la red de G complemento (debe ser bipartito!) y
        encontrar un Max Independet Set
9 // Min Edge Cover: tomar las aristas del matching + para todo vertices
       no cubierto hasta el momento, tomar cualquier arista de el
10 int nodes, src, dst;
  int dist[MAX], q[MAX], work[MAX];
  struct Edge {
       int to, rev;
13
       ll f, cap;
14
       Edge(int to, int rev, 11 f, 11 cap): to(to), rev(rev), f(f), cap(
15
           cap) {}
<sub>16</sub> };
  vector<Edge> G[MAX];
void addEdge(int s, int t, ll cap){
       G[s].pb(Edge(t, sz(G[t]), 0, cap)), G[t].pb(Edge(s, sz(G[s])-1, 0,
```

```
0));}
   bool dinic_bfs(){
       fill(dist, dist+nodes, -1), dist[src]=0;
21
       int qt=0; q[qt++]=src;
22
       for(int qh=0; qh<qt; qh++){</pre>
23
            int u =q[qh];
24
           forall(e, G[u]){
25
                int v=e->to;
26
                if(dist[v]<0 && e->f < e->cap)
27
                    dist[v]=dist[u]+1, q[qt++]=v;
28
           }
29
       }
30
       return dist[dst]>=0;
31
32
   ll dinic_dfs(int u, ll f){
33
       if(u==dst) return f;
34
       for(int &i=work[u]; i<sz(G[u]); i++){</pre>
35
           Edge &e = G[u][i];
36
           if(e.cap<=e.f) continue;</pre>
37
           int v=e.to;
38
           if(dist[v]==dist[u]+1){
39
                    11 df=dinic_dfs(v, min(f, e.cap-e.f));
40
                    if(df>0){
41
                             e.f+=df, G[v][e.rev].f-= df;
42
                             return df; }
43
44
       }
45
       return 0;
46
47
   ll maxFlow(int _src, int _dst){
48
       src=_src, dst=_dst;
49
       11 result=0;
50
       while(dinic bfs()){
51
           fill(work, work+nodes, 0);
52
            while(ll delta=dinic_dfs(src,INF))
53
                result+=delta;
54
       }
55
       // todos los nodos con dist[v]!=-1 vs los que tienen dist[v]==-1
56
            forman el min-cut
       return result; }
57
```

7.24 máximo emparejamiento bipartito

```
1 // g++ -std=c "bipartitematching.cpp" -o run
2 /***
   ========= <MCBM max cardinality bipartite matching c++ version>
   Return the bipartite matching of a Graph
   * Format of nodes: 1 to N
   */
 6
7
   const int N = 100010;
   vector<int>G[N];
   bool v[N];//for the greedy speed up
   int match[N];
12 bool vis[N]:
   int n,m;
   //calling aumenting path
   bool aug(int u){
       if(vis[u])return false;
       vis[u]=true;
       for(int i=0;i<(int)G[u].size();++i){</pre>
18
       int r=G[u][i];
           if(match[r]==-1||aug(match[r])){
20
               match[r]=u;match[u]=r;return true;
21
           }
22
       }
23
       return 0;
24
25
   int mc;
   //findging all augmenting path's
   int solve(){
      bool check=true;
      while(check){
30
           check=false;
31
           memset(vis,0,sizeof vis);
32
           for(int i=1:i<=n:++i){
33
         if(!v[i]&&match[i]==-1){
34
           bool op=aug(i);
35
           check | = op;
36
           mc+=op;
37
38
39
40
       return mc;
41
42 }
```

14 | */

```
void init(){
     memset(v,0,sizeof v);
44
     memset(vis,false,sizeof vis);
45
46
     memset(match,-1,sizeof match);
47
       for(int i=0;i<=n;i++)G[i].clear();</pre>
48
49
    void greedySpeedUp(){
     //greedy optimization, match with the first not matched
51
     for(int i=1;i<=n;++i){</pre>
52
             for(int j=0;j<(int)G[i].size();++j){</pre>
53
                 if(match[G[i][j]]==-1){
54
             match[G[i][j]]=i,match[i]=G[i][j],mc++,v[i]=true;break;
          }
58
59 }
```

- 7.25 max-independent set en bipartitos
- 7.26 min-path cover (ver tópicos raros de halim)
 - 7.27 min-cost arborescence
- 7.28 lema de diapositivas de nico de grafos funcionales
 - 7.29 minimax y maximini con kruskal y dijkstra

```
1 // g++ -std=c++11 "maximini.cpp" -o run
2
      ======== <maximini c++ version> ==============
  Given a weighted graph return the maximini (the maximun of the minimum)
  or the minimax (the minimum of the maximum) in the path a,b
5
6
  Minimax as definded as: finding the minimum of maximum edge weight among
        all posible paths
_{8} \mid * between two verrtices a to b, the cost for a path from a to b is
      determined by maximum edge
9 * weight along this path. Among all these possible paths from a to b,
      pick the one with the minimum
   * ax-edge-weight
   * Complexity O(E*log(E) + V + E)
13 Problem for practice: UVA 534,544
```

```
int n;
   pair<int,pair<int,int> >Edges[20000];
   map<string,int>mp;
   int parent[210];
   pair<int,int>child[210];
   bool vis[210];
   vector<pair<int,int> >G[210];
   int find(int u){return u==parent[u]?u:parent[u]=find(parent[u]);}
   void Union(int u,int v){
     int pu=find(u),pv=find(v);
26
     if(pu!=pv){
27
       parent[pv]=pu;
28
     }
29
30
   int mst(int a,int b){
     sort(Edges,Edges+t);
32
     reverse(Edges, Edges+t); //don't reverse for the minimax
     for(int i=0;i<=200;i++)parent[i] = i;
34
     int w,u,v, maximini = 1e8, minimax = 0;
     for(int i=0;i<t;i++){</pre>
36
       tie(w,u,v) = make_tuple(Edges[i].first, Edges[i].second.first, Edges
37
            [i].second.second);
       if(find(u) != find(v)){
38
         Union(u,v);
39
         G[u].push_back({v,w});
         G[v].push_back({u,w});
41
       }
42
43
     queue<int>q;
     q.push(a);
45
     vis[a]=true;
46
     while(!q.empty()){
47
       int u = q.front();q.pop();
48
       //if(u==1)break;
49
       for(pair<int,double>node: G[u]){
50
         if(!vis[node.first]){
51
           vis[node.first] = true;
52
           q.push(node.first);
53
           //maximini=max(maximini,node.second);
54
           child[node.first].first = u;
55
```

```
child[node.first].second = node.second;
56
57
       }
58
59
     for(int t = b;t != -1;t = child[t].first){
60
       //cout<<t<" "<<child[t].second<<"\n";
61
       //minimax=max(minimax,child[t].second);
62
       maximini = min(maximini,child[t].second);
63
     }
64
     return maximini;
65
  |}
66
```

8 Teoria de juegos

8.1 Teorema fundamental de los juegos optimos

8.2 Como calcular grundy

```
int grundyNumber(position pos) {
   moves[] = possible positions to which I can move from pos
   set s;
   for (all x in moves) insert into s grundyNumber(x);
   //return the smallest non-negative integer not in the set s;
   int ret=0;
   while (s.contains(ret)) ret++;
   return ret;
}
```

9 Probabilidad

9.1 Formulas clave

10 Otros/utilitarios

10.1 josephus

```
int survivor(int n, int m){
  int s = 0;
  for (int i=1;i<=n;++i) s = (s+m)%i;
  return (s+1);
}</pre>
```

10.2 josephus k = 2

```
//////JAVA
       /**
2
3
      * Oparam n the number of people standing in the circle
      * Oreturn the safe position who will survive the execution
5
      * f(N) = 2L + 1 where N = 2^M + L and 0 \le L \le 2^M
      */
7
     public int getSafePosition(int n) {
       // find value of L for the equation
       int valueOfL = n - Integer.highestOneBit(n);
       int safePosition = 2 * valueOfL + 1;
11
       return safePosition;
12
13
```

10.3 poker

10.4 iterar subconjuntos

```
for(int sbm=bm; sbm; sbm=(sbm-1)&bm)
```

10.5 como reconstruir una DP (normal)

```
1    /*
2    You just need to revisit your steps in the DP. In case of 0-1 knapsack,
    lets say the original DP function was solve, and the function
    reconstruct will give you the actual solution (I'm writing the code
    in C++):
3    */
```

getrlimit(RLIMIT_STACK, &rl);

```
4 | int solve(int pos, int capacity){
                                                                                  4 | rl.rlim_cur=1024L*1024L*256L;//256mb
                                                                                 5 setrlimit(RLIMIT_STACK, &rl);
       if(pos == no_of_objects) return 0;
5
       if(memo[pos][capacity] != -1) return memo[pos][capacity];
6
                                                                                                   10.7 comparar doubles for noobs
       int r1 = solve(pos + 1, capacity); //dont take
       int r2 = 0;
                                                                                  const double EPS = 1e-9;
       if(weight[pos] <= capacity){</pre>
9
                                                                                  _2 | x == y <=> fabs(x-y) < EPS
           r2 = solve(pos + 1, capacity - weight[pos]) + profit[pos]; //
10
                                                                                  _3 | x > y <=> x > y + EPS
                                                                                  _4 | x >= y <=> x > y - EPS
       }
11
       return memo[pos][capacity] = max(r1, r2);
                                                                                                                  infix to postfix
                                                                                                           10.8
12
13
   void reconstruct(int pos, int capacity){
                                                                                  1 //infix to postfix with shunting yard, Halim interpretation
       if(pos == no_of_objects) return; //you have completed reconstruction
                                                                                   //plus eval function given a postfix return the result of the operation
15
       int r1 = memo[pos + 1][capacity]; //dont take
                                                                                    //format: string like (xox (xox)) o=operation x=value
16
       int r2 = 0:
                                                                                    string s;
17
       if(weight[pos] <= capacity)r2 = memo[pos + 1][capacity - weight[pos</pre>
                                                                                    bool isOperator(string u){
18
           ]] + profit[pos]; //take
                                                                                      return u=="+"||u=="-"||u=="*"||u=="/";
       if(r1 > r2) {reconstruct(pos + 1, capacity);}
19
                                                                                 7
       else{
                                                                                    bool precede(string u){
20
           cout << "Take_object_" << pos << endl;</pre>
                                                                                      if(u=="*"||u=="/")return true:
21
           reconstruct(pos + 1, capacity - weight[pos]) + profit[pos];
22
                                                                                      return false;
                                                                                 10
       }
23
                                                                                 11
                                                                                    void solve(){
24
   After executing reconstruct, it will print all those objects that give
                                                                                      getline(cin,s);
                                                                                 13
       you the optimal solution. As you can see, at most no_of_objects
                                                                                      stack<string>st;
                                                                                 14
       calls will be made in the reconstruct function.
                                                                                 15
                                                                                      vector<string>v;
26 Similarly, you can reconstruct the solution of any DP greedily.
                                                                                      stringstream ss;
                                                                                 16
                                                                                      ss<<s;
                                                                                 17
                          10.6 muajaja con j
                                                                                      while(ss>>s){
                                                                                 18
                                                                                        if(isOperator(s)){
                                                                                 19
  #include <signal.h>
                                                                                          while(!st.empty()&&isOperator(st.top())&&precede(st.top())>=
                                                                                 20
  void divzero(int p){
                                                                                              precede(s)){
     while(true);}
                                                                                            v.push_back(st.top());st.pop();
                                                                                 21
  void segm(int p){
                                                                                 22
     exit(0);}
                                                                                          st.push(s);
                                                                                 23
   //in main
                                                                                 24
  signal(SIGFPE, divzero);
                                                                                        else{
                                                                                 25
8 signal(SIGSEGV, segm);
                                                                                           if(s=="("){
                                                                                 26
                              Expandir pila
                                                                                             st.push(s);
                                                                                 27
                                                                                          }
                                                                                 28
#include <sys/resource.h>
                                                                                          else{
                                                                                 29
                                                                                            if(s==")"){
2 | rlimit rl;
                                                                                 30
```

31

while(!st.empty()&&st.top()!="("){

```
v.push_back(st.top());st.pop();
32
33
             if(!st.empty()&&st.top()=="(")st.pop();
34
35
           else {
36
              v.push_back(s);
37
38
39
40
41
     while(!st.empty()){
42
       v.push_back(st.top());st.pop();
43
     }
     stack<double>stans;
     double x;
46
     for(string eva:v){
47
       if(!isOperator(eva)){
48
         stringstream nu;
49
         nu<<eva:
50
         nu>>x;
51
         stans.push(x);
52
       }
53
       else{
54
         double a=stans.top();stans.pop();
55
         double b=stans.top();stans.pop();
56
         if(eva=="*")b*=a;
57
         if(eva=="/")b/=a;
58
         if(eva=="+")b+=a;
59
         if(eva=="-")b-=a;
60
         stans.push(b);
61
       }
62
     }
63
     cout<<fixed<<stans.top()<<"\n";</pre>
64
65
                         10.9
                                 numeros romanos
   #include <bits/stdc++.h>
```

```
#include <bits/stdc++.h>
using namespace std;
map<int,string>cvt;

string aromano(int n){
    cvt[1000] = "M";cvt[900] = "CM",cvt[500] = "D", cvt[400] = "CD";
```

```
cvt[100] = "C";cvt[90] = "XC"; cvt[50] = "L";
     cvt[40] = "XL";cvt[10] = "X";cvt[9] = "IX";cvt[5] = "V"; cvt[4] = "IV"
8
     cvt[1] = "I";
9
     string ans = "";
10
     for(map<int,string>::reverse_iterator it = cvt.rbegin();it != cvt.rend
11
         ();it++)
       while(n >= it->first){
12
         ans += it->second;
         n -= it->first;
       }
15
     return ans;
16
17
   map<string,int>crn;
   int anumero(string R){
     map<char, int> crn;
     crn['I'] = 1; crn['V'] = 5; crn['X'] = 10; crn['L'] = 50;
     crn['C'] = 100; crn['D'] = 500; crn['M'] = 1000;
     int value = 0:
23
     for (int i = 0; R[i]; i++)
       if (i + 1 < R.size() && crn[R[i]] < crn[R[i+1]]) {</pre>
         value += crn[R[i+1]] - crn[R[i]];
26
         i++;
27
       }
28
       else value += crn[R[i]];
29
     return value;
31 }
```

10.10 get k-th permutacion

```
vector<int>v;
  //finding the number of permutation 0....n-1
   int main()
   {
4
       string s;
5
       while(getline(cin,s)){
6
           stringstream ss;
7
           ss<<s:
8
           int pos=0,u;
9
           v.clear();
10
           while(ss>>u){
11
               v.push_back(u-1);
12
           }
13
```

```
vector<int>le(v.size(),0);
14
            for(int i=0;i<v.size();i++){</pre>
15
                 for(int j=i+1; j<v.size(); j++){</pre>
16
                     if(v[i]>v[j])le[i]++;
17
                 }
18
19
            long long ans=OLL,fact=OLL,por=1LL;
20
            for(int i=le.size()-1;i>=0;i--){
21
                 if(fact!=OLL)por*=fact;
^{22}
                 fact++;
23
                 ans=ans+por*le[i];
24
25
            cout << ans +1 << "\n";
26
        }
27
        return 0;
28
29 }
```

10.11 sliding window

10.12 permutaciones de un dado

```
// izquierda, derecha, arriba, al frente, abajo, atras
2
   int p[][6] = {
3
       \{0,1,2,3,4,5\},
4
       \{0,1,3,4,5,2\},\
5
       \{0,1,4,5,2,3\},\
6
       \{0,1,5,2,3,4\},
7
       \{1,0,2,5,4,3\},
8
       {1,0,3,2,5,4},
9
       \{1,0,4,3,2,5\},\
10
       {1,0,5,4,3,2},
11
       \{2,4,5,1,3,0\},\
12
       \{2,4,1,3,0,5\},\
13
       \{2,4,3,0,5,1\},
14
       \{2,4,0,5,1,3\},
15
       {3,5,2,1,4,0},
16
       {3,5,1,4,0,2},
17
       {3,5,4,0,2,1},
18
       {3,5,0,2,1,4},
19
       {4,2,5,0,3,1},
20
       {4,2,0,3,1,5},
21
       {4,2,3,1,5,0},
22
       {4,2,1,5,0,3},
23
```

```
{5,3,2,0,4,1},
24
      {5,3,0,4,1,2},
25
      {5,3,4,1,2,0},
26
      {5,3,1,2,0,4}
27
28 };
                      10.13 ternary search
                    10.14 liebre y el tortugo
                     10.15 como usar printf
                           10.16 java
                          10.17 python
                         10.18 template
                         10.19 file setup
1 //tambien se pueden usar comas: {a, x, m, l}
touch {a..l}.in; tee {a..l}.cpp < template.cpp
```