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1 algorithm

#include <algorithm> #include <numeric>

| Algo | Params | Funcion |
|--|-------------------------------|--|
| sort, stable_sort | f, l | ordena el intervalo |
| nth_element | f, nth, l | void ordena el n-esimo, y particiona el resto |
| fill, fill_n | f, l / n, elem | void llena [f, l) o [f, f+n) con elem |
| lower_bound, upper_bound | f, l, elem | it al primer / ultimo donde se puede insertar elem para que quede ordenada |
| binary_search | f, l, elem | bool esta elem en [f, l) |
| copy | f, l, resul | hace resul+i=f+i $\forall i$ |
| find, find_if, find_first_of | f, l, elem / pred / f2, l2 | it encuentra i $\in [f, l)$ tq. i=elem, pred(i), i $\in [f2, l2)$ |
| count, count_if | f, l, elem/pred | cuenta elem, pred(i) |
| search | f, l, f2, l2 | busca [f2, l2) $\in [f, l)$ |
| replace, replace_if | f, l, old / pred, new | cambia old / pred(i) por new |
| reverse | f, l | da vuelta |
| partition, stable_partition | f, l, pred | pred(i) ad, !pred(i) atras |
| min_element, max_element | f, l, [comp] | it min, max de [f, l) |
| lexicographical_compare | f1, l1, f2, l2 | bool con [f1, l1) i [f2, l2) |
| next/prev_permutation | f, l | deja en [f, l) la perm sig, ant |
| set_intersection, set_difference, set_union, set_symmetric_difference, | f1, l1, f2, l2, res | [res, ...) la op. de conj |
| push_heap, pop_heap, make_heap | f, l, e / e / | mete/saca e en heap [f, l), hace un heap de [f, l) |
| is_heap | f, l | bool es [f, l) un heap |
| accumulate | f, l, i, [op] | $T = \sum / \text{oper de } [f, l)$ |
| inner_product | f1, l1, f2, i | $T = i + [f1, l1) \cdot [f2, \dots)$ |
| partial_sum | f, l, r, [op] | $r+i = \sum / \text{oper de } [f, f+i) \forall i \in [f, l)$ |
| __builtin_ffs | unsigned int | Pos. del primer 1 desde la derecha |
| __builtin_clz | unsigned int | Cant. de ceros desde la izquierda. |
| __builtin_ctz | unsigned int | Cant. de ceros desde la derecha. |
| __builtin_popcount | unsigned int | Cant. de 1's en x. |
| __builtin_parity | unsigned int | 1 si x es par, 0 si es impar. |
| __builtin_XXXXXXll | unsigned ll | = pero para long long's. |

2 Estructuras

2.1 RMQ (static) - MODIFICAR

Dado un arreglo y una operacion asociativa *idempotente*, get(i, j) opera sobre el rango [i, j). Restriccion: $LVL \geq \text{ceil}(\log n)$; Usar [] para llenar arreglo y luego build().

```

1 struct RMQ{
2     #define LVL 10
3     tipo vec[LVL] [1<<(LVL+1)];
4     tipo &operator[] (int p){return vec[0] [p];}
5     tipo get(int i, int j) {//intervalo [i,j)
6         int p = 31-__builtin_clz(j-i);
7         return min(vec[p] [i], vec[p] [j-(1<<p)]);
8     }
9     void build(int n) {//O(nlogn)
10        int mp = 31-__builtin_clz(n);
11        forn(p, mp) forn(x, n-(1<<p))
12            vec[p+1] [x] = min(vec[p] [x], vec[p] [x+(1<<p)]);
13    }
};

```

2.2 Segment Tree

2.2.1 Segment Tree Recursivo

2.2.2 ST Iterativo - (Consulta en rango, modificacion a posicion)

2.2.3 ST Iterativo - (Consulta a posicion, modificacion en rango)

```

1 /*Segment Tree modificar un rango, acceder a una posicion
2     solo sirve cuando la operacion que realizamos es conmutativa
3     por ejemplo la suma, pero no funciona con la asignacion
4 */
5 //adiciona value al rango [l, r)
6 void modify(int l, int r, int value) {// rango [l, r)
7     for (l += n, r += n; l < r; l >>= 1, r >>= 1) {
8         if (l&1) t[l++] += value;
9         if (r&1) t[--r] += value;
10    }
11 }
12 //acceder a la posicion
13 int query(int p) {
14     int res = 0;
15     for (p += n; p > 0; p >>= 1) res += t[p];

```

```

16     return res;
17 }
18 //Si necesitamos actualizar todo lo podemos hacer en O(n)
19 //Y luego acceder a las hojas en O(1)
20 void push() {
21     for (int i = 1; i < n; ++i) {
22         t[i<<1] += t[i];
23         t[i<<1|1] += t[i];
24         t[i] = 0;
25     }
26 }

```

2.2.4 Segment Tree con Punteros

2.2.5 Segment Tree 2D

2.2.6 Segment Tree Lazy - Suma

2.2.7 Segment Tree Lazy - Pintar

2.2.8 Segment Tree Persistente

2.3 Fenwick Tree

2.3.1 Fenwick Tree 2D

```

1 ll T[1025][1025];
2 int n;
3
4 ll query(int x, int y)
5 {
6     ll res = 0;
7     for(int i = x; i >= 0; i = (i & (i+1)) - 1)
8         for(int j = y; j >= 0; j = (j & (j+1)) - 1)
9             res += T[i][j];
10     return res;
11 }
12
13 void update(int x, int y, int val)
14 {
15     for(int i = x; i < n; i = (i | (i+1)))
16         for(int j = y; j < n; j = (j | (j+1)))
17             T[i][j] += val;
18 }
19

```

2.4 Union Find con rank

```

1  /*===== <Union find rangos> =====
2  Complexity: O(N)
3  index 0 to n - 1 warning
4  Complexity O(N)
5  */
6  #define MAX INSERTE_VALOR_AQUI
7  int padre[MAX];
8  int rango[MAX];
9  void MakeSet(int n){
10     for (int i = 0 ; i < n ; ++i) {
11         padre[i] = i; rango[i] = 0; }
12 }
13 int Find(int x) {
14     if(x == padre[x])
15         return x;
16     return padre[x] = Find(padre[x]);
17 }
18 void UnionbyRank(int x , int y){
19     int xRoot = Find(x);
20     int yRoot = Find(y);
21     //el padre de ambas componentes sera el de mayor altura
22     if(rango[xRoot] > rango[yRoot])//X tiene mas altura que Y
23         padre[yRoot] = xRoot;
24     }else{//Y >= X
25         padre[xRoot] = yRoot;
26         if(rango[xRoot] == rango[yRoot])//si poseen la misma altura
27             rango[yRoot]++;//incremento el rango de la nueva raiz
28     }
29 }

```

2.5 BigInteger C++

```

1  // g++ -std=c++11 "bigint.cpp" -o run
2  /**
3  ===== <Big Int c++ version> =====
4  Contain a useful big int, overload all operators, including cin, cout,
5  comparator, build via string (prefer this metod) or long long, for now
6  this not have a
7  to_string method
8  Problem for practice: UVA 494
9  */

```

```

9 // base and base_digits must be consistent
10 const int base = 1000000000;
11 const int base_digits = 9;
12
13 struct bigint {
14     vector<int> a;
15     int sign;
16
17     bigint() :
18         sign(1) {
19     }
20
21     bigint(long long v) {
22         *this = v;
23     }
24
25     bigint(const string &s) {
26         read(s);
27     }
28
29     void operator=(const bigint &v) {
30         sign = v.sign;
31         a = v.a;
32     }
33
34     void operator=(long long v) {
35         sign = 1;
36         if (v < 0)
37             sign = -1, v = -v;
38         for (; v > 0; v = v / base)
39             a.push_back(v % base);
40     }
41
42     bigint operator+(const bigint &v) const {
43         if (sign == v.sign) {
44             bigint res = v;
45
46             for (int i = 0, carry = 0; i < (int) max(a.size(), v.a.size()) || carry; ++i) {
47                 if (i == (int) res.a.size())
48                     res.a.push_back(0);
49                 res.a[i] += carry + (i < (int) a.size() ? a[i] : 0);
50                 carry = res.a[i] >= base;

```

```

51         if (carry)
52             res.a[i] -= base;
53     }
54     return res;
55 }
56 return *this - (-v);
57 }
58
59 bigint operator-(const bigint &v) const {
60     if (sign == v.sign) {
61         if (abs() >= v.abs()) {
62             bigint res = *this;
63             for (int i = 0, carry = 0; i < (int) v.a.size() || carry; ++i) {
64                 res.a[i] -= carry + (i < (int) v.a.size() ? v.a[i] : 0);
65                 carry = res.a[i] < 0;
66                 if (carry)
67                     res.a[i] += base;
68             }
69             res.trim();
70             return res;
71         }
72         return -(v - *this);
73     }
74     return *this + (-v);
75 }
76
77 void operator*=(int v) {
78     if (v < 0)
79         sign = -sign, v = -v;
80     for (int i = 0, carry = 0; i < (int) a.size() || carry; ++i) {
81         if (i == (int) a.size())
82             a.push_back(0);
83         long long cur = a[i] * (long long) v + carry;
84         carry = (int) (cur / base);
85         a[i] = (int) (cur % base);
86         //asm("divl %%ecx" : "=a"(carry), "=d"(a[i]) : "A"(cur), "c"(base));
87     }
88     trim();
89 }
90

```

```

91     bigint operator*(int v) const {
92         bigint res = *this;
93         res *= v;
94         return res;
95     }
96
97     friend pair<bigint, bigint> divmod(const bigint &a1, const bigint &
98         b1) {
99         int norm = base / (b1.a.back() + 1);
100        bigint a = a1.abs() * norm;
101        bigint b = b1.abs() * norm;
102        bigint q, r;
103        q.a.resize(a.a.size());
104
105        for (int i = a.a.size() - 1; i >= 0; i--) {
106            r *= base;
107            r += a.a[i];
108            int s1 = r.a.size() <= b.a.size() ? 0 : r.a[b.a.size()];
109            int s2 = r.a.size() <= b.a.size() - 1 ? 0 : r.a[b.a.size() -
110                1];
111            int d = ((long long) base * s1 + s2) / b.a.back();
112            r -= b * d;
113            while (r < 0)
114                r += b, --d;
115            q.a[i] = d;
116        }
117
118        q.sign = a1.sign * b1.sign;
119        r.sign = a1.sign;
120        q.trim();
121        r.trim();
122        return make_pair(q, r / norm);
123    }
124
125    bigint operator/(const bigint &v) const {
126        return divmod(*this, v).first;
127    }
128
129    bigint operator%(const bigint &v) const {
130        return divmod(*this, v).second;
131    }
132
133    void operator/=(int v) {

```

```

132        if (v < 0)
133            sign = -sign, v = -v;
134        for (int i = (int) a.size() - 1, rem = 0; i >= 0; --i) {
135            long long cur = a[i] + rem * (long long) base;
136            a[i] = (int) (cur / v);
137            rem = (int) (cur % v);
138        }
139        trim();
140    }
141
142    bigint operator/(int v) const {
143        bigint res = *this;
144        res /= v;
145        return res;
146    }
147
148    int operator%(int v) const {
149        if (v < 0)
150            v = -v;
151        int m = 0;
152        for (int i = a.size() - 1; i >= 0; --i)
153            m = (a[i] + m * (long long) base) % v;
154        return m * sign;
155    }
156
157    void operator+=(const bigint &v) {
158        *this = *this + v;
159    }
160    void operator-=(const bigint &v) {
161        *this = *this - v;
162    }
163    void operator*=(const bigint &v) {
164        *this = *this * v;
165    }
166    void operator/=(const bigint &v) {
167        *this = *this / v;
168    }
169
170    bool operator<(const bigint &v) const {
171        if (sign != v.sign)
172            return sign < v.sign;
173        if (a.size() != v.a.size())
174            return a.size() * sign < v.a.size() * v.sign;

```

```

175     for (int i = a.size() - 1; i >= 0; i--)
176         if (a[i] != v.a[i])
177             return a[i] * sign < v.a[i] * sign;
178     return false;
179 }
180
181 bool operator>(const bigint &v) const {
182     return v < *this;
183 }
184 bool operator<=(const bigint &v) const {
185     return !(v < *this);
186 }
187 bool operator>=(const bigint &v) const {
188     return !(*this < v);
189 }
190 bool operator==(const bigint &v) const {
191     return !(*this < v) && !(v < *this);
192 }
193 bool operator!=(const bigint &v) const {
194     return *this < v || v < *this;
195 }
196
197 void trim() {
198     while (!a.empty() && !a.back())
199         a.pop_back();
200     if (a.empty())
201         sign = 1;
202 }
203
204 bool isZero() const {
205     return a.empty() || (a.size() == 1 && !a[0]);
206 }
207
208 bigint operator-() const {
209     bigint res = *this;
210     res.sign = -sign;
211     return res;
212 }
213
214 bigint abs() const {
215     bigint res = *this;
216     res.sign *= res.sign;
217     return res;

```

```

218 }
219
220 long long longValue() const {
221     long long res = 0;
222     for (int i = a.size() - 1; i >= 0; i--)
223         res = res * base + a[i];
224     return res * sign;
225 }
226
227 friend bigint gcd(const bigint &a, const bigint &b) {
228     return b.isZero() ? a : gcd(b, a % b);
229 }
230 friend bigint lcm(const bigint &a, const bigint &b) {
231     return a / gcd(a, b) * b;
232 }
233
234 void read(const string &s) {
235     sign = 1;
236     a.clear();
237     int pos = 0;
238     while (pos < (int) s.size() && (s[pos] == '-' || s[pos] == '+'))
239     {
240         if (s[pos] == '-')
241             sign = -sign;
242         ++pos;
243     }
244     for (int i = s.size() - 1; i >= pos; i -= base_digits) {
245         int x = 0;
246         for (int j = max(pos, i - base_digits + 1); j <= i; j++)
247             x = x * 10 + s[j] - '0';
248         a.push_back(x);
249     }
250     trim();
251 }
252
253 friend istream& operator>>(istream &stream, bigint &v) {
254     string s;
255     stream >> s;
256     v.read(s);
257     return stream;
258 }
259
260 friend ostream& operator<<(ostream &stream, const bigint &v) {

```

```

260     if (v.sign == -1)
261         stream << '-';
262     stream << (v.a.empty() ? 0 : v.a.back());
263     for (int i = (int) v.a.size() - 2; i >= 0; --i)
264         stream << setw(base_digits) << setfill('0') << v.a[i];
265     return stream;
266 }
267
268 static vector<int> convert_base(const vector<int> &a, int old_digits
    , int new_digits) {
269     vector<long long> p(max(old_digits, new_digits) + 1);
270     p[0] = 1;
271     for (int i = 1; i < (int) p.size(); i++)
272         p[i] = p[i - 1] * 10;
273     vector<int> res;
274     long long cur = 0;
275     int cur_digits = 0;
276     for (int i = 0; i < (int) a.size(); i++) {
277         cur += a[i] * p[cur_digits];
278         cur_digits += old_digits;
279         while (cur_digits >= new_digits) {
280             res.push_back(int(cur % p[new_digits]));
281             cur /= p[new_digits];
282             cur_digits -= new_digits;
283         }
284     }
285     res.push_back((int) cur);
286     while (!res.empty() && !res.back())
287         res.pop_back();
288     return res;
289 }
290
291 typedef vector<long long> vll;
292
293 static vll karatsubaMultiply(const vll &a, const vll &b) {
294     int n = a.size();
295     vll res(n + n);
296     if (n <= 32) {
297         for (int i = 0; i < n; i++)
298             for (int j = 0; j < n; j++)
299                 res[i + j] += a[i] * b[j];
300     }
301     return res;

```

```

302
303     int k = n >> 1;
304     vll a1(a.begin(), a.begin() + k);
305     vll a2(a.begin() + k, a.end());
306     vll b1(b.begin(), b.begin() + k);
307     vll b2(b.begin() + k, b.end());
308
309     vll a1b1 = karatsubaMultiply(a1, b1);
310     vll a2b2 = karatsubaMultiply(a2, b2);
311
312     for (int i = 0; i < k; i++)
313         a2[i] += a1[i];
314     for (int i = 0; i < k; i++)
315         b2[i] += b1[i];
316
317     vll r = karatsubaMultiply(a2, b2);
318     for (int i = 0; i < (int) a1b1.size(); i++)
319         r[i] -= a1b1[i];
320     for (int i = 0; i < (int) a2b2.size(); i++)
321         r[i] -= a2b2[i];
322
323     for (int i = 0; i < (int) r.size(); i++)
324         res[i + k] += r[i];
325     for (int i = 0; i < (int) a1b1.size(); i++)
326         res[i] += a1b1[i];
327     for (int i = 0; i < (int) a2b2.size(); i++)
328         res[i + n] += a2b2[i];
329     return res;
330 }
331
332 bigint operator*(const bigint &v) const {
333     vector<int> a6 = convert_base(this->a, base_digits, 6);
334     vector<int> b6 = convert_base(v.a, base_digits, 6);
335     vll a(a6.begin(), a6.end());
336     vll b(b6.begin(), b6.end());
337     while (a.size() < b.size())
338         a.push_back(0);
339     while (b.size() < a.size())
340         b.push_back(0);
341     while (a.size() & (a.size() - 1))
342         a.push_back(0), b.push_back(0);
343     vll c = karatsubaMultiply(a, b);
344     bigint res;

```



```
res.sign = sign * v.sign;
for (int i = 0, carry = 0; i < (int) c.size(); i++) {
    long long cur = c[i] + carry;
    res.a.push_back((int) (cur % 1000000));
    carry = (int) (cur / 1000000);
}
res.a = convert_base(res.a, 6, base_digits);
res.trim();
return res;
}
};

int main() {
    bigint a=0;
    //("999999999999999999999999999999999999999999999999");
    bigint b;
    //("199999999999999999999999999999999999999999999998");
    bigint n;
    while(cin >> n) {
        if(n==0){break;}
        a += n;
    }
    cout<<a<<endl;
```

2.6 UnorderedSet

```
1 //Compiler: g++ --std=c++11
2 struct Hash{
3     size_t operator()(const ii &a) const{
4         size_t s=hash<int>()(a.fst);
5         return hash<int>()(a.snd)+0x9e3779b9+(s<<6)+(s>>2);
6     }
7     size_t operator()(const vector<int> &v) const{
8         size_t s=0;
9         for(auto &e : v)
10             s ^= hash<int>()(e)+0x9e3779b9+(s<<6)+(s>>2);
11         return s;
12     }
13 };
14 unordered_set<ii, Hash> s;
15 unordered_map<ii, int, Hash> m; //map<key, value, hasher>
```

2.7 Ordered Set

```

1  /*
2   A brief explanation about use of a powerful library: orderd_set
3   Reference link: http://codeforces.com/blog/entry/11080
4   and a hash for the type pair
5   */
6
7  #include <ext/pb_ds/assoc_container.hpp>
8  #include <ext/pb_ds/tree_policy.hpp>
9  using namespace __gnu_pbds;
10 typedef tree<int,null_type,less<int>,rb_tree_tag,
    tree_order_statistics_node_update> ordered_set;
11 /*
12 If we want to get map but not the set, as the second argument type must
    be used mapped type. Apparently,
13 the tree supports the same operations as the set (at least I haven't
    any problems with them before),
14 but also there are two new features - it is find_by_order() and
    order_of_key().
15 The first returns an iterator to the k-th largest element (counting
    from zero), the second - the number of items
16 in a set that are strictly smaller than our item. Example of use:
17 *
18 * */

```

2.8 Treap Modo Set

2.9 Treap Implicito(Rope)

2.10 Treap - Toby and Bones

2.11 Convex Hull Trick Estatico

```

1 // g++ "convexhulltrick.cpp" -o run
2 /**
3 ===== <Convex hull trick normal version> =====
4 Contain a sample about convex hull trick optimization this recieve N
   pairs:
5 a "value of length" and a cost, we need to minimize the value of
   grouping
6 this pairs taken the most large pair as the cost of the group
7
8 Problem for practice: aquire

```

```

9  */
10 #include <iostream>
11 #include <vector>
12 #include <algorithm>
13 using namespace std;
14 int pointer; //Keeps track of the best line from previous query
15 vector<long long> M; //Holds the slopes of the lines in the envelope
16 vector<long long> B; //Holds the y-intercepts of the lines in the
    envelope
17 //Returns true if either line l1 or line l3 is always better than line
    l2
18 bool bad(int l1,int l2,int l3)
19 {
20     /*
21     intersection(l1,l2) has x-coordinate (b1-b2)/(m2-m1)
22     intersection(l1,l3) has x-coordinate (b1-b3)/(m3-m1)
23     set the former greater than the latter, and cross-multiply to
24     eliminate division
25     */
26     return (B[l3]-B[l1])*(M[l1]-M[l2])<(B[l2]-B[l1])*(M[l1]-M[l3]);
27 }
28 //Adds a new line (with lowest slope) to the structure
29 void add(long long m,long long b)
30 {
31     //First, let's add it to the end
32     M.push_back(m);
33     B.push_back(b);
34     //If the penultimate is now made irrelevant between the
        antepenultimate
35     //and the ultimate, remove it. Repeat as many times as necessary
36     while (M.size()>=3&&bad(M.size()-3,M.size()-2,M.size()-1))
37     {
38         M.erase(M.end()-2);
39         B.erase(B.end()-2);
40     }
41 }
42 //Returns the minimum y-coordinate of any intersection between a given
    vertical
43 //line and the lower envelope
44 long long query(long long x)
45 {
46     //If we removed what was the best line for the previous query, then
        the

```

```

47     //newly inserted line is now the best for that query
48     if (pointer>=M.size())
49         pointer=M.size()-1;
50     //Any better line must be to the right, since query values are
        //non-decreasing
51     while (pointer<M.size()-1&&
52         M[pointer+1]*x+B[pointer+1]<M[pointer]*x+B[pointer])
53         pointer++;
54     return M[pointer]*x+B[pointer];
55 }
56
57 int main()
58 {
59     int M,N,i;
60     pair<int,int> a[50000];
61     pair<int,int> rect[50000];
62     scanf("%d",&M);
63     for (i=0; i<M; i++)
64         scanf("%d%d",&a[i].first,&a[i].second);
65     //Sort first by height and then by width (arbitrary labels)
66     sort(a,a+M);
67     for (i=0,N=0; i<M; i++)
68     {
69         /*
70         When we add a higher rectangle, any rectangles that are also
71         equally thin or thinner become irrelevant, as they are
72         completely contained within the higher one; remove as many
73         as necessary
74         */
75         while (N>0&&rect[N-1].second<=a[i].second)
76             N--;
77         rect[N++]=a[i]; //add the new rectangle
78     }
79     long long cost;
80     add(rect[0].second,0);
81     //initially, the best line could be any of the lines in the envelope,
82     //that is, any line with index 0 or greater, so set pointer=0
83     pointer=0;
84     for (i=0; i<N; i++)
85     {
86         cost=query(rect[i].first);
87         if (i<N)
88             add(rect[i+1].second,cost);
89     }

```

```

90 printf("%lld\n", cost);
91 return 0;
92 }

```

2.12 Convex Hull Trick Dinamico

```

1 // g++ -std=c++11 "convexhulltrick_dynamic.cpp" -o run
2 /**
3 ===== <Convex hull trick dynamic version version>
4 =====
5 warning with the use of this, this is a black box, try to use only in an
6 emergency.
7 Problem for practice: aquire
8 */
9 #include <bits/stdc++.h>
10 using namespace std;
11 typedef long long ll;
12 const ll is_query = -(1LL<<62);
13 struct Line {
14     ll m, b;
15     mutable multiset<Line>::iterator it;
16     const Line *succ(multiset<Line>::iterator it) const;
17     bool operator<(const Line& rhs) const {
18         if (rhs.b != is_query) return m < rhs.m;
19         const Line *s=succ(it);
20         if(!s) return 0;
21         ll x = rhs.m;
22         return b - s->b < (s->m - m) * x;
23     }
24 };
25 struct HullDynamic : public multiset<Line>{ // will maintain upper hull
26     for maximum
27     bool bad(iterator y) {
28         iterator z = next(y);
29         if (y == begin()) {
30             if (z == end()) return 0;
31             return y->m == z->m && y->b <= z->b;
32         }
33         iterator x = prev(y);
34         if (z == end()) return y->m == x->m && y->b <= x->b;
35         return (x->b - y->b)*(z->m - y->m) >= (y->b - z->b)*(y->m - x->m);
36     }
37     iterator next(iterator y){return ++y;}

```

```

35 iterator prev(iterator y){return --y;}
36 void insert_line(ll m, ll b) {
37     iterator y = insert((Line) { m, b });
38     y->it=y;
39     if (bad(y)) { erase(y); return; }
40     while (next(y) != end() && bad(next(y))) erase(next(y));
41     while (y != begin() && bad(prev(y))) erase(prev(y));
42 }
43 ll eval(ll x) {
44     Line l = *lower_bound((Line) { x, is_query });
45     return l.m * x + l.b;
46 }
47 }h;
48 const Line *Line::succ(multiset<Line>::iterator it) const{
49     return (++it==h.end())? NULL : &*it;}

```

2.13 Misof Tree

```

1 /*
2 http://codeforces.com/blog/entry/10493#comment-159335
3 Sirve para encontrar el i-esimo numero de un conjunto de numeros que
4 vamos insertando en el arbol.
5 Sirve solo si nuestros numeros son del 0 al n-1 (pero podemos mapearlos
6 antes de usarlos)
7 La idea es esta:
8 Funcionamiento:
9 - En el fondo sigue siendo un Segment-Tree (hacemos que 'n' sea 2^x)
10 - Cada nodo guarda cuantos numeros hay en el intervalo (entonces en
11 tree[1] dice cuantos numeros tenemos en total)
12 - Se sigue representando los hijos del nodo 'i' con '2 * i' (izq) y '2
13 * i + 1' (der);
14 Query:
15 - si kth es mas grande que todos los que tenemos(tree[1]) o es
16 negativo entonces -1
17 - siempre nos mantenemos en el nodo de la izquierda y si es necesario
18 avanzamos al de la derecha
19 'i <= 1'
20 - si kth es mas grande que el nodo de la izquierda(el actual) quiere
21 decir que podemos quitarle todos esos
22 numeros a nuestra busqueda 'kth - tree[i]' y buscar el nuevo kth en
23 el arbol de la derecha
24 if (kth > tree [i]) kth -= tree [i++];
25 - Ojo en el 'i++' ahi es donde avanzamos al nodo de la derecha

```

```

18 - luego hace su formula rara que aun no entendi xD:
19 'i - leaf + (kth > tree [i])';
20 */
21 const int MaxN = 1e6;
22
23 int a [MaxN], s [MaxN];
24 int leaf, tree [100 + MaxN << 2];
25
26 void bld (int n) { leaf = 1 << (32 - __builtin_clz (n)); }
27 void add (int x) { for (int i = leaf + x; i; i >>= 1) ++tree [i]; }//
    Podemos insertar mas de una copia la vez tree [i] += xcopies;
28 void del (int x) { for (int i = leaf + x; i; i >>= 1) --tree [i]; }//
    Podemos eliminar mas de una copia la vez tree [i] -= xcopies;
29 // en "leaf + x" esta cuantas copias tenemos de "x"
30 //Cuidado con intentar hacer del con mas copias de las disponibles, el
    kth() no funcionaria
31 long kth (int kth, int i = -1) {
32     if (kth > tree [1] || kth <= 0) return i;
33     for (i = 1; i < leaf; i <= 1) if (kth > tree [i]) kth -= tree [i++];
34     return i - leaf + (kth > tree [i]);
35 }

```

2.14 SQRT Decomposition Basic

```

1 const int maxn = 500010;
2 int n;
3
4 tipo v[maxn]; //vector principal
5
6 tipo lazy[maxn];
7 pair<tipo, tipo> t[maxn]; //para poder reordenar los elementos
8
9 int SQRT;
10 int N; //nro. de buckets
11
12 //Recalcula y aplica el lazy al bucket con indice idx
13 //guarda la informacion necesaria del bucket en otros vectores
14 //podria ser la suma del bucket, o el min/max del bucket
15 void recalc(int idx) {
16     int a = idx * SQRT, b = min(n, (idx + 1) * SQRT);
17     for (int i = a; i < b; i++) {
18         v[i] += lazy[idx];
19         t[i] = make_pair(v[i], i);

```

```

20     }
21     lazy[idx] = 0;
22     sort(t + a, t + b);
23 }
24
25 //adiciona delta a todos los elementos
26 //en el intervalo cerrado [a, b]
27 void add(int a, int b, tipo delta) {
28     int idx_a = a / SQRT, idx_b = b / SQRT;
29     if (idx_a == idx_b) {
30         for (int i = a; i <= b; i++)
31             v[i] += delta;
32         recalc(idx_a);
33     } else {
34         //head
35         for (int i = a, lim = min(n, (idx_a + 1) * SQRT); i < lim; i++)
36             v[i] += delta;
37         recalc(idx_a); //OJO puede ser necesario
38         //body
39         for (int i = idx_a + 1; i < idx_b; i++)
40             lazy[i] += delta;
41         //tail
42         for (int i = idx_b * SQRT; i <= b; i++)
43             v[i] += delta;
44         recalc(idx_b); //OJO puede ser necesario
45     }
46 }
47
48 //tambien podria ser en un rango como en el add
49 tipo query(tipo val) {
50     tipo ans = 0;
51     //recorro todos los buckets
52     for (int idx = 0; idx < N; idx++) {
53         int a = idx * SQRT, b = min(n, (idx + 1) * SQRT);
54         //... hacer algo ...
55     }
56     return ans;
57 }
58 int main() {
59     //leer n, q y los elementos de v
60
61     SQRT = (int)sqrt(n) + 1;
62     N = (n + SQRT - 1) / SQRT; //nro. de buckets

```

```

63 //construir cada bucket
64 for (int idx = 0; idx < N; idx++)
65     recalc(idx);
66
67 //resto del programa
68 return 0;
69 }

```

2.15 Nro. Elementos menores o iguales a x en $O(\log(n))$

```

1 //insercion y consulta de cuantos <= en log n
2 struct leqset {
3     int maxl; vector<int> c;
4     int pref(int n, int l) { return (n>>(maxl-l))|(1<<l); }
5     void ini(int ml) { maxl=ml; c=vector<int>(1<<(maxl+1)); }
6     //inserta c copias de e, si c es negativo saca c copias
7     void insert(int e, int q=1) { for(l,maxl+1) c[pref(e,l)]+=q; }
8     int leq(int e) {
9         int r=0,a=1;
10        for(i,maxl) {
11            a<=&1; int b=(e>>maxl-i-1)&1;
12            if (b) r+=c[a]; a|=b;
13        } return r + c[a]; //sin el c[a] da los estrictamente menores
14    }
15    int size() { return c[1]; }
16    int count(int e) { return c[e|(1<<maxl)]; }
17 };

```

3 Algos

3.1 LIS en $O(n \log n)$ con Reconstruccion

```

1 //Para non-increasing, cambiar comparaciones y revisar busq binaria
2 //Given an array, paint it in the least number of colors so that each
   color turns to a non-increasing subsequence.
3 //Solution:Min number of colors=Length of the longest increasing
   subsequence
4
5 // Las lineas marcadas con // Camino no son necesarias si no se desea
   reconstruir el camino.
6 #define MAXN 1000000
7 int v[MAXN]; // INPUT del algoritmo.
8 int mv[MAXN];

```

```

9 int mi[MAXN], p[MAXN]; // Camino
10 int l[MAXN]; // Aca apareceria la maxima subsecuencia creciente(los
   indices)
11 int lis(int n) {
12     for(i,n) mv[i] = INF;
13     for(i,n) mi[i] = -1; // Camino
14     for(i,n) p[i] = -1; // Camino
15     mv[0] = -INF;
16     int res = 0;
17     for(i,n) {
18         // Con upper_bound es maxima subsecuencia no decreciente.
19         // Con lower_bound es maxima subsecuencia creciente.
20         int me = upper_bound(mv,mv+n,v[i]) - mv;
21         p[i] = mi[me-1]; // Camino
22         mv[me] = v[i];
23         mi[me] = i; // Camino
24         if (me > res) res = me;
25     }
26     for(int a = mi[res], i = res - 1; a != -1; a = p[a], i--) // Camino
27         l[i] = a; // Indices: poniendo l[i] = v[a] quedan los valores.
28     return res;
29 }

```

3.2 Mo

```

1 // g++ -std=c++11 "mo.cpp" -o run
2 /**
3 ===== <Mo> =====
4 Contain a sample about Mo algorithm
5 Brief explanation when use Mo:
6 Explain where and when we can use above algorithm
7
8 As mentioned, this algorithm is offline, that means we cannot use it
   when we are forced to stick to given order of queries.
9 That also means we cannot use this when there are update operations.
   Not just that, there is one important possible limitation:
10 We should be able to write the functions add and remove. There will be
   many cases where add is trivial but remove is not.
11 One such example is where we want maximum in a range. As we add elements
   , we can keep track of maximum. But when we remove elements
12 it is not trivial. Anyways in that case we can use a set to add elements
   , remove elements and report minimum.

```

13 In that case the add and delete operations are $O(\log N)$ (Resulting in $O(N * \sqrt{N} * \log N)$ algorithm).

14
15 Suggestion first use the add operation, then the erase operation
16 Problem for practice: DQUERY spoj

17 Input: N, then N elements of array M querys with a range L,R

18 */

19 const int MAXV = 1e6 + 10;

20 const int N = 30010;

21 const int M = 200010;

22 int cnt[MAXV];

23 int v[N];

24

25 struct query{

26 int l,r,pos;

27 query(){}

28 };

29 int n;

30 query qu[M];

31 int ans[M];

32

33 int ret = 0;

34 void add(int pos){

35 pos = v[pos];

36 cnt[pos]++;

37 if(cnt[pos] == 1){

38 ret++;

39 }

40 }

41 void erase(int pos){

42 pos = v[pos];

43 cnt[pos]--;

44 if(!cnt[pos])ret--;

45 }

46 int main(){

47 n = in();

48 for(int i = 0; i < n;i++){

49 v[i] = in();

50 }

51 int block = ceil(sqrt(n));

52 int q = in();

53 for(int i = 0; i < q;i++){

54 qu[i].l = in() - 1,qu[i].r = in() - 1,qu[i].pos = i;

55 }

56 sort(qu,qu + q,[&](const query &a,const query &b){

57 if(a.l / block != b.l / block)

58 return a.l / block < b.l / block;

59 return a.r < b.r;

60 });

61 int l = 0, r = 0;

62 for(int i = 0; i < q;i++){

63 int nl = qu[i].l,nr = qu[i].r;

64 while(l > nl){

65 add(--l);

66 }

67 while(r <= nr){

68 add(r++);

69 }

70 while(l < nl){

71 erase(l++);

72 }

73 while(r > nr + 1){

74 erase(--r);

75 }

76

77 ans[qu[i].pos] = ret;

78 }

79 for(int i = 0; i < q;i++)printf("%d\n",ans[i]);

80 }

4 Strings

4.1 Manacher

1 vector<int> manacher(const string &s) {

2 int n = s.size();

3 string s(2 * n + 3, '#');

4 s[0] = '%', s[s.size() - 1] = '\$';//no deben estar en la cadena

5 for (int i = 0; i < n; i++)

6 s[(i + 1) * 2] = s[i];

7

8 n = s.size();

9 vector<int> P(n, 0);

10 int C = 0, R = 0;

11 for (int i = 1; i < n - 1; i++) {

12 int j = C - (i - C);

```

13     if (R > i)
14         P[i] = min(R - i, P[j]);
15     while (s[i + 1 + P[i]] == s[i - 1 - P[i]])
16         P[i]++;
17     if (i + P[i] > R) {
18         C = i;
19         R = i + P[i];
20     }
21 }
22 return P;
23 }
24 bool is_pal(const vector<int> &mnch_vec, int i, int j) {//[i, j] - i<=j
25     int len = j - i + 1;
26     i = (i + 1) * 2; //idx to manacher vec idx
27     j = (j + 1) * 2;
28     int mid = (i + j) / 2;
29     return mnch_vec[mid] >= len;
30 }
31 int main() {
32     string s;
33     cin >> s;
34     vector<int> mnch_vec = manacher(s);
35     if (is_pal(mnch_vec, 2, 7)) {
36         //la subcadena desde la posicion 2 a la 7 es palindrome
37     }
38     return 0;
39 }

```

4.2 Trie - Punteros y bfs

4.3 Suffix Array $O(n \log n)$ con LCP (Kasai) $O(n)$

4.4 Minima rotacion lexicografica

```

1  /*
2  Rotacion Lexicografica minima MinRotLex(cadena,tamano)
3  para cambiar inicio de la cadena char s[300]; int h; s+h;
4  retorna inicio de la rotacion minima :D
5  */
6  int MinRotLex(const char *s, const int slen) {
7      int i = 0, j = 1, k = 0, x, y, tmp;
8      while(i < slen && j < slen && k < slen) {
9          x = i + k;
10         y = j + k;

```

```

11         if(x >= slen) x -= slen;
12         if(y >= slen) y -= slen;
13         if(s[x] == s[y]) {
14             k++;
15         } else if(s[x] > s[y]) {
16             i = j+1 > i+k+1 ? j+1 : i+k+1;
17             k = 0;
18             tmp = i, i = j, j = tmp;
19         } else {
20             j = i+1 > j+k+1 ? i+1 : j+k+1;
21             k = 0;
22         }
23     }
24     return i;
25 }
26 int main(){
27     int n;
28     scanf("%d",&n);getchar();
29     while(n--){
30         char str[1000009];
31         gets(str);
32         printf("%d\n",MinRotLex(str,strlen(str))+1);
33     }
34 }

```

4.5 Matching

4.5.1 KMP

```

1  string T; //cadena donde buscar(what)
2  string P; //cadena a buscar(what)
3  int b[MAXLEN]; //back table b[i] maximo borde de [0..i)
4  void kmppre(){ //by gabina with love
5      int i = 0, j = -1; b[0] = -1;
6      while(i < sz(P)){
7          while(j >= 0 && P[i] != P[j]) j = b[j];
8          i++, j++, b[i] = j;
9      }
10 }
11 void kmp(){
12     int i = 0, j = 0;
13     while(i < sz(T)){
14         while(j >= 0 && T[i] != P[j]) j = b[j];
15         i++, j++;

```

```

16         if(j==sz(P)) printf("P_is_found_at_index_%d_in_T\n", i-j), j=b[j
17         ];
18     }
19 }
20 int main(){
21     cout << "T=";
22     cin >> T;
23     cout << "P=";
24     cin.ignore();
25     cin >> P;
26     kmppre();
27     kmp();
28     return 0;
29 }

```

4.5.2 Z - Por aprender

4.5.3 Matching con suffix array

```

1 vector<int> FindOccurrences(const string& pattern, const string& text) {
2     vector<int> result;
3     int minIndex = 0,maxIndex = text.size();
4     while(minIndex < maxIndex){
5         int mid = (minIndex + maxIndex) >> 1;
6         if(cmp(pattern,sa[mid]) > 0)minIndex = mid + 1;
7         else maxIndex = mid;
8     }
9     int start = minIndex;
10    maxIndex = text.size();
11    while(minIndex < maxIndex){
12        int mid = (minIndex + maxIndex) >> 1;
13        if(cmp(pattern,sa[mid]) < 0)maxIndex = mid;
14        else minIndex = mid + 1;
15    }
16    int end = maxIndex;
17    for(int i = start; i < end;i++){
18        result.push_back(sa[i]);
19    }
20    return result;
21 }

```

4.5.4 Matching con BWT

```

1 map<char,int>fo;//first ocurrence

```

```

2 map<char,vector<int> >count;//count the i-th ocurrence of symbol
3 string first;//first colum of bwt
4 string alpha = "ACGT$";//change this
5 void preprocess(const string& bwt) { //recieves a BWT
6     string ans = "";
7     first = bwt;
8     sort(first.begin(),first.end());
9     for(int i = 0;first[i];i++){
10         if(!fo.count(first[i]))fo[first[i]] = i;
11     }
12     for(char u:alpha)count[u].push_back(0);
13     for(int i = 1; i <= bwt.size();i++){
14         for(char u:alpha)
15             count[u].push_back(count[u].back() + (bwt[i - 1] == u));
16     }
17 }
18 //return the number of ocurrences of the pattern
19 int bwtmatch(int bot,string &pattern){
20     int top = 0;
21     while(top <= bot){
22         if(pattern.size()){
23             char letter = pattern.back();
24             pattern.pop_back();
25             if(count[letter][bot + 1]){
26                 top = fo[letter] + count[letter][top];
27                 bot = fo[letter] + count[letter][bot + 1] - 1;
28             }
29             else return 0;
30         }
31         else return bot - top + 1;
32     }
33     return 0;
34 }

```

4.5.5 Matching con Aho-Corasick

```

1 struct trie{
2     map<char, trie> next;
3     trie* tran[256];//transiciones del automata
4     int idhoja, szhoja;//id de la hoja o 0 si no lo es
5     //link lleva al sufijo mas largo, nxthoja lleva al mas largo pero que
6     //es hoja

```



```

7  trie *padre, *link, *nxthoja;
8  char pch; //caracter que conecta con padre
9  trie(): tran(), idhoja(), padre(), link() {}
10 void insert(const string &s, int id=1, int p=0){ //id>0!!!
11     if(p<sz(s)){
12         trie &ch=next[s[p]];
13         tran[(int)s[p]]=&ch;
14         ch.padre=this, ch.pch=s[p];
15         ch.insert(s, id, p+1);
16     }
17     else idhoja=id, szhoja=sz(s);
18 }
19 trie* get_link() {
20     if(!link){
21         if(!padre) link=this; //es la raiz
22         else if(!padre->padre) link=padre; //hijo de la raiz
23         else link=padre->get_link()->get_tran(pch);
24     }
25     return link; }
26 trie* get_tran(int c) {
27     if(!tran[c]) tran[c] = !padre? this : this->get_link()->get_tran(c);
28     return tran[c]; }
29 trie *get_nxthoja(){
30     if(!nxthoja) nxthoja = get_link()->idhoja? link : link->nxthoja;
31     return nxthoja; }
32 void print(int p){
33     if(idhoja) cout << "found_" << idhoja << "_at_position_" << p-
34         szhoja << endl;
35     if(get_nxthoja()) get_nxthoja()->print(p); }
36 void matching(const string &s, int p=0){
37     print(p); if(p<sz(s)) get_tran(s[p])->matching(s, p+1); }
38 }tri;
39
40 int main(){
41     tri=trie(); //clear
42     tri.insert("ho", 1);
43     tri.insert("hoho", 2);

```

4.6 Suffix Automaton

```

1  /***** Suffix Automata *****/
2  const int N = INSERTE_VALOR; //maxima longitud de la cadena

```

```

3  struct State { //OJO!!! tamaño del alfabeto, si MLE -> map
4      State *pre,*go[26]; //se puede usar un map<char, State*> go
5      int step;
6      void clear() {
7          pre=0;
8          step=0;
9          memset(go,0,sizeof(go)); //go.clear();
10     }
11 } *root,*last;
12 State statePool[N * 2],*cur;
13 void init() {
14     cur=statePool;
15     root=last=cur++;
16     root->clear();
17 }
18 void Insert(int w) {
19     State *p=last;
20     State *np=cur++;
21     np->clear();
22     np->step=p->step+1;
23     while(p&&!p->go[w])
24         p->go[w]=np, p=p->pre;
25     if(p==0)
26         np->pre=root;
27     else {
28         State *q=p->go[w];
29         if(p->step+1==q->step)
30             np->pre=q;
31         else {
32             State *nq=cur++;
33             nq->clear();
34             memcpy(nq->go,q->go,sizeof(q->go)); //nq->go = q->go; para
35                 mapa
36             nq->step=p->step+1;
37             nq->pre=q->pre;
38             q->pre=nq;
39             np->pre=nq;
40             while(p&&p->go[w]==q)
41                 p->go[w]=nq, p=p->pre;
42         }
43     }
44     last=np;

```

```

45 /***** Suffix Automata *****/
46
47 /***** Algunas aplicaciones *****/
48 //Obtiene el LCS substring de 2 cadenas en O(|A| + |B|)
49 string lcs(char A[N], char B[N]) {
50     int n,m;
51     n = strlen(A); m = strlen(B);
52     //Construccion: O(|A|)
53     //solo hacerlo una vez si A no cambia
54     init();
55     for(int i=0; i<n; i++)
56         Insert(A[i]-'a'); //Fin construccion
57     //LCS: O(|B|)
58     int ans = 0, len = 0, bestpos = 0;
59     State *p = root;
60     for(int i = 0; i < m; i++) {
61         int x = B[i]-'a';
62         if(p->go[x]) {
63             len++;
64             p = p->go[x];
65         } else {
66             while (p && !p->go[x]) p = p->pre;
67             if(!p) p = root, len = 0;
68             else len = p->step+1, p = p->go[x];
69         }
70         if (len > ans)
71             ans = len, bestpos = i;
72     }
73     //return ans; //solo el tamaño del lcs
74     return string(B + bestpos - ans + 1, B + bestpos + 1);
75 }
76
77 /*Numero de subcadenas distintas + 1(subcadena vacia) en O(|A|)
78 OJO: Por alguna razon Suffix Array es mas rapido
79 Se reduce a contar el numero de paths que inician en q0 y terminan
80 en cualquier nodo. dp[u] = # de paths que inician en u
81 - Se debe construir el automata en el main(init y Insert's)
82 - Setear dp en -1
83 */
84 number dp[N * 2];
85 number num_dist_substr(State *u = root) {
86     if (dp[u - statePool] != -1) return dp[u - statePool];
87     number ans = 1; //el path vacio que representa este nodo

```

```

88     for (int v = 0; v < 26; v++) //usar for (auto) para mapa
89         if (u->go[v])
90             ans += num_dist_substr(u->go[v]);
91     return (dp[u - statePool] = ans);
92 }
93
94 /*Suma la longitud de todos los substrings en O(|A|)
95 - Construir el automata(init y insert's)
96 - Necesita el metodo num_dist_substr (el de arriba)
97 - setear dp's en -1
98 */
99 number dp1[N * 2];
100 number sum_length_dist_substr(State *u = root) {
101     if (dp1[u - statePool] != -1) return dp1[u - statePool];
102     number ans = 0; //el path vacio que representa este nodo
103     for (int v = 0; v < 26; v++) //usar for (auto) para mapa
104         if (u->go[v])
105             ans += (num_dist_substr(u->go[v]) + sum_length_dist_substr(u->go[v]));
106     return (dp1[u - statePool] = ans);
107 }
108
109 /*
110 Pregunta si p es subcadena de la cadena con la cual esta construida
111 el automata.
112 Complejidad: - Construir O(|Texto|) - solo una vez (init e insert's)
113               - Por Consulta O(|patron a buscar|)
114 */
115 bool is_substring(char p[N]) {
116     State *u = root;
117     for (int i = 0; p[i]; i++) {
118         if (!u->go.count(p[i])) //esta con map!!!
119             return false;
120         u = u->go[p[i]]; //esta con map!!!
121     }
122     return true;
123 }

```

4.7 K-esima permutacion de una cadena

```

1 //Entrada: Una cadena cad(std::string), un long th
2 //Salida : La th-esima permutacion lexicografica de cad
3 string ipermutacion(string cad, long long int th){

```

```

4  sort(cad.begin(), cad.end());
5  string sol = "";
6  int pos;
7  for(int c = cad.size() - 1; c >= 0; c--){
8      pos = th / fact[c];
9      th %= fact[c];
10     sol += cad[pos];
11     cad.erase(cad.begin() + pos);
12 }
13 return sol;
14 }

```

5 Geometria

5.1 Interseccion de circunferencias - Sacar de Agustin

5.2 Graham Scan

5.3 Cortar Poligono

```

1  //cuts polygon Q along the line ab
2  //stores the left side (swap a, b for the right one) in P
3  void cutPolygon(pto a, pto b, vector<pto> Q, vector<pto> &P){
4      P.clear();
5      forn(i, sz(Q)){
6          double left1=(b-a)^(Q[i]-a), left2=(b-a)^(Q[(i+1)%sz(Q)]-a);
7          if(left1>=0) P.pb(Q[i]);
8          if(left1*left2<0)
9              P.pb(inter(line(Q[i], Q[(i+1)%sz(Q)]), line(a, b)));
10     }
11 }

```

5.4 Interseccion de rectangulos

```

1  #define MAXC 2501
2  struct Rect{
3      int x1,y1, x2,y2;
4      int color;
5      int area;
6      Rect(int _x1, int _y1, int _x2, int _y2){
7          x1 = _x1;
8          y1 = _y1;
9          x2 = _x2;
10         y2 = _y2;

```

```

11     getArea();
12 }
13 int getArea(){
14     if(x1>=x2 || y1>=y2)return area = 0;
15     return area = (x2-x1)*(y2-y1);
16 }
17 };
18 Rect interseccion(Rect t, Rect r){
19     int x1,y1,x2,y2;
20     x1 = max(t.x1,r.x1);
21     y1 = max(t.y1,r.y1);
22     x2 = min(t.x2,r.x2);
23     y2 = min(t.y2,r.y2);
24     Rect res(x1,y1,x2,y2);
25     return res;
26 }

```

5.5 Distancia punto-recta

```

1  double distance_point_to_line(const point &a, const point &b, const
2      point &pnt){
3      double u = ((pnt.x - a.x)*(b.x - a.x) + (pnt.y - a.y)*(b.y - a.y)) /
4          distsq(a, b);
5      point intersection;
6      intersection.x = a.x + u*(b.x - a.x);
7      intersection.y = a.y + u*(b.y - a.y);
8      return dist(pnt, intersection);
9  }

```

5.6 Distancia punto-segmento

```

1  struct point{
2      double x,y;
3  };
4  inline double dist(const point &a, const point &b){
5      return sqrt((a.x-b.x)*(a.x-b.x) + (a.y-b.y)*(a.y-b.y));
6  }
7  inline double distsq(const point &a, const point &b){
8      return (a.x-b.x)*(a.x-b.x) + (a.y-b.y)*(a.y-b.y);
9  }
10 double distance_point_to_segment(const point &a, const point &b, const
11     point &pnt){
12     double u = ((pnt.x - a.x)*(b.x - a.x) + (pnt.y - a.y)*(b.y - a.y)) /
13         distsq(a, b);

```

```

12 point intersection;
13 intersection.x = a.x + u*(b.x - a.x);
14 intersection.y = a.y + u*(b.y - a.y);
15
16 if (u < 0.0 || u > 1.0)
17     return min(dist(a, pnt), dist(b, pnt));
18
19 return dist(pnt, intersection);
20 }

```

5.7 Parametrizacion de rectas - Sacar de codeforces

6 Math

6.1 Identidades

$$\sum_{i=0}^n \binom{n}{i} = 2^n$$

$$\sum_{i=0}^n i \binom{n}{i} = n * 2^{n-1}$$

$$\sum_{i=m}^n i = \frac{n(n+1)}{2} - \frac{m(m-1)}{2} = \frac{(n+1-m)(n+m)}{2}$$

$$\sum_{i=0}^n i = \sum_{i=1}^n i = \frac{n(n+1)}{2}$$

$$\sum_{i=0}^n i^2 = \frac{n(n+1)(2n+1)}{6} = \frac{n^3}{3} + \frac{n^2}{2} + \frac{n}{6}$$

$$\sum_{i=0}^n i(i-1) = \frac{8}{6} \left(\frac{n}{2} + 1\right)(n+1) \text{ (doubles)} \rightarrow \text{Sino ver caso impar y par}$$

$$\sum_{i=0}^n i^3 = \left(\frac{n(n+1)}{2}\right)^2 = \frac{n^4}{4} + \frac{n^3}{2} + \frac{n^2}{4} = \left[\sum_{i=1}^n i\right]^2$$

$$\sum_{i=0}^n i^4 = \frac{n(n+1)(2n+1)(3n^2+3n-1)}{30} = \frac{n^5}{5} + \frac{n^4}{2} + \frac{n^3}{3} - \frac{n}{30}$$

$$\sum_{i=0}^n i^p = \frac{(n+1)^{p+1}}{p+1} + \sum_{k=1}^p \frac{B_k}{p-k+1} \binom{p}{k} (n+1)^{p-k+1}$$

$$r = e - v + k + 1$$

Teorema de Pick: (Area, puntos interiores y puntos en el borde)

$$A = I + \frac{B}{2} - 1$$

6.2 Ec. Caracteristica

$$a_0 T(n) + a_1 T(n-1) + \dots + a_k T(n-k) = 0$$

$$p(x) = a_0 x^k + a_1 x^{k-1} + \dots + a_k$$

Sean r_1, r_2, \dots, r_q las raíces distintas, de mult. m_1, m_2, \dots, m_q

$$T(n) = \sum_{i=1}^q \sum_{j=0}^{m_i-1} c_{ij} n^j r_i^n$$

Las constantes c_{ij} se determinan por los casos base.

6.3 Identidades de agustin y mario

6.4 Combinatorio

```

1 | forn(i, MAXN+1){ //comb[i][k]=i tomados de a k

```

```

2   comb[i][0]=comb[i][i]=1;
3   forr(k, 1, i) comb[i][k]=(comb[i-1][k]+comb[i-1][k-1])%MOD;
4 }
5 ll lucas (ll n, ll k, int p){ //Calcula (n,k)%p teniendo comb[p][p]
6     precalculado.
7     ll aux = 1;
8     while (n + k) aux = (aux * comb[n%p][k%p]) %p, n/=p, k/=p;
9     return aux;
10 }

```

6.5 Exp. de Numeros Mod.

```

1 ll expmod (ll b, ll e, ll m){ //O(log b)
2     if(!e) return 1;
3     ll q= expmod(b,e/2,m); q=(q*q)%m;
4     return e%2? (b * q)%m : q;
5 }

```

6.6 Exp. de Matrices y Fibonacci en log(n) - Sacar de Agustin

6.7 Gauss Jordan

```

1 const int N = 300;
2 typedef vector<double> col;
3 typedef vector<double> row;
4 typedef vector<row> Matrix;
5 col solution;
6 int main(){
7     Matrix M;
8     M.resize(300);
9     solution.resize(300);
10    for(int i = 0; i < 30;i++)M[i].resize(30);
11    int n;
12    cin >> n;
13    for(int i = 0; i < n;i++)
14        for(int j = 0; j <= n;j++)
15            cin >> M[i][j];
16
17    for(int j = 0; j < n - 1;j++){
18        int l=j;
19        for(int i = j + 1; i < n;i++){
20            if(fabs(M[i][j]) > fabs(M[l][j]))l = i;
21        }
22        for(int k = j; k <= n;k++){

```

```

23     swap(M[j][k], M[l][k]);
24 }
25 for(int i = j + 1; i < n; i++)
26     for(int k = n; k >= j; k--)
27         M[i][k] -= M[j][k] * M[i][j] / M[j][j];
28 }
29 double t = 0;
30 for(int j = n - 1; j >= 0; j--){
31     t = 0.0;
32     for(int k = j + 1; k < n; k++) t += M[j][k] * solution[k];
33     solution[j] = (M[j][n] - t) / M[j][j];
34 }
35 cout.precision(4);
36 for(int i = 0; i < n; i++) cout << fixed << solution[i] << " ";
37 return 0;
38 }

```

6.8 Simplex

```

1 // Two-phase simplex algorithm for solving linear programs of the form
2 //
3 //     maximize    c^T x
4 //     subject to  Ax <= b
5 //                x >= 0
6 //
7 // INPUT: A -- an m x n matrix
8 //         b -- an m-dimensional vector
9 //         c -- an n-dimensional vector
10 //         x -- a vector where the optimal solution will be stored
11 //
12 // OUTPUT: value of the optimal solution (infinity if unbounded
13 //         above, nan if infeasible)
14 //
15 // To use this code, create an LPSolver object with A, b, and c as
16 // arguments. Then, call Solve(x).
17
18 #include <iostream>
19 #include <iomanip>
20 #include <vector>
21 #include <cmath>
22 #include <limits>
23
24 using namespace std;

```

```

25
26 typedef long double DOUBLE;
27 typedef vector<DOUBLE> VD;
28 typedef vector<VD> VVD;
29 typedef vector<int> VI;
30
31 const DOUBLE EPS = 1e-9;
32
33 struct LPSolver {
34     int m, n;
35     VI B, N;
36     VVD D;
37
38     LPSolver(const VVD &A, const VD &b, const VD &c) :
39         m(b.size()), n(c.size()), N(n + 1), B(m), D(m + 2, VD(n + 2)) {
40         for (int i = 0; i < m; i++) for (int j = 0; j < n; j++) D[i][j] = A[
41             i][j];
42         for (int i = 0; i < m; i++) { B[i] = n + i; D[i][n] = -1; D[i][n +
43             1] = b[i]; }
44         for (int j = 0; j < n; j++) { N[j] = j; D[m][j] = -c[j]; }
45         N[n] = -1; D[m + 1][n] = 1;
46     }
47
48     void Pivot(int r, int s) {
49         double inv = 1.0 / D[r][s];
50         for (int i = 0; i < m + 2; i++) if (i != r)
51             for (int j = 0; j < n + 2; j++) if (j != s)
52                 D[i][j] -= D[r][j] * D[i][s] * inv;
53         for (int j = 0; j < n + 2; j++) if (j != s) D[r][j] *= inv;
54         for (int i = 0; i < m + 2; i++) if (i != r) D[i][s] *= -inv;
55         D[r][s] = inv;
56         swap(B[r], N[s]);
57     }
58
59     bool Simplex(int phase) {
60         int x = phase == 1 ? m + 1 : m;
61         while (true) {
62             int s = -1;
63             for (int j = 0; j <= n; j++) {
64                 if (phase == 2 && N[j] == -1) continue;
65                 if (s == -1 || D[x][j] < D[x][s] || D[x][j] == D[x][s] && N[j] <
66                     N[s]) s = j;
67             }
68         }
69     }
70 }

```

```

65     if (D[x][s] > -EPS) return true;
66     int r = -1;
67     for (int i = 0; i < m; i++) {
68         if (D[i][s] < EPS) continue;
69         if (r == -1 || D[i][n + 1] / D[i][s] < D[r][n + 1] / D[r][s] ||
70             (D[i][n + 1] / D[i][s]) == (D[r][n + 1] / D[r][s]) && B[i] < B
             [r]) r = i;
71     }
72     if (r == -1) return false;
73     Pivot(r, s);
74 }
75 }
76
77 DOUBLE Solve(VD &x) {
78     int r = 0;
79     for (int i = 1; i < m; i++) if (D[i][n + 1] < D[r][n + 1]) r = i;
80     if (D[r][n + 1] < -EPS) {
81         Pivot(r, n);
82         if (!Simplex(1) || D[m + 1][n + 1] < -EPS) return -numeric_limits<
            DOUBLE>::infinity(); //NO SOLUTION
83         for (int i = 0; i < m; i++) if (B[i] == -1) {
84             int s = -1;
85             for (int j = 0; j <= n; j++)
86                 if (s == -1 || D[i][j] < D[i][s] || D[i][j] == D[i][s] && N[j]
                    < N[s]) s = j;
87             Pivot(i, s);
88         }
89     }
90     if (!Simplex(2)) return numeric_limits<DOUBLE>::infinity(); //
        INFINITY
91     x = VD(n);
92     for (int i = 0; i < m; i++) if (B[i] < n) x[B[i]] = D[i][n + 1];
93     return D[m][n + 1]; //solution find
94 }
95 };
96
97 int main() {
98
99     const int m = 4;
100     const int n = 3;
101     DOUBLE _A[m][n] = {
102         { 6, -1, 0 },
103         { -1, -5, 0 },

```

```

104         { 1, 5, 1 },
105         { -1, -5, -1 }
106     };
107     DOUBLE _b[m] = { 10, -4, 5, -5 };
108     DOUBLE _c[n] = { 1, -1, 0 };
109
110     VVD A(m);
111     VD b(_b, _b + m);
112     VD c(_c, _c + n);
113     for (int i = 0; i < m; i++) A[i] = VD(_A[i], _A[i] + n);
114
115     LPSolver solver(A, b, c);
116     VD x;
117     DOUBLE value = solver.Solve(x);
118
119     cerr << "VALUE:" << value << endl; // VALUE: 1.29032
120     cerr << "SOLUTION:"; // SOLUTION: 1.74194 0.451613 1
121     for (size_t i = 0; i < x.size(); i++) cerr << " " << x[i];
122     cerr << endl;
123     return 0;
124 }

```

6.9 Matrices y determinante $O(n^3)$

```

1 struct Mat {
2     vector<vector<double>> > vec;
3     Mat(int n): vec(n, vector<double>(n) ) {}
4     Mat(int n, int m): vec(n, vector<double>(m) ) {}
5     vector<double> &operator[](int f){return vec[f];}
6     const vector<double> &operator[](int f) const {return vec[f];}
7     int size() const {return sz(vec);}
8     Mat operator+(Mat &b) { //this de n x m entonces b de n x m
9         Mat m(sz(b),sz(b[0]));
10        forn(i,sz(vec)) forn(j,sz(vec[0])) m[i][j] = vec[i][j] + b[i][j]
        ];
11        return m;    }
12    Mat operator*(const Mat &b) { //this de n x m entonces b de m x t
13        int n = sz(vec), m = sz(vec[0]), t = sz(b[0]);
14        Mat mat(n,t);
15        forn(i,n) forn(j,t) forn(k,m) mat[i][j] += vec[i][k] * b[k][j];
16        return mat;    }
17    double determinant(){//sacado de e maxx ru
18        double det = 1;

```

```

19     int n = sz(vec);
20     Mat m(*this);
21     forn(i, n){//para cada columna
22         int k = i;
23         forr(j, i+1, n)//busco la fila con mayor val abs
24             if(abs(m[j][i])>abs(m[k][i])) k = j;
25         if(abs(m[k][i])<1e-9) return 0;
26         m[i].swap(m[k]); //la swapeo
27         if(i!=k) det = -det;
28         det *= m[i][i];
29         forr(j, i+1, n) m[i][j] /= m[i][i];
30         //hago 0 todas las otras filas
31         forn(j, n) if (j!= i && abs(m[j][i])>1e-9)
32             forr(k, i+1, n) m[j][k]-=m[i][k]*m[j][i];
33     }
34     return det;
35 }
36 };
37
38 int n;
39 int main() {
40     //DETERMINANTE:
41     //https://uva.onlinejudge.org/index.php?option=com_onlinejudge&Itemid=8&
42     //page=show_problem&problem=625
43     freopen("input.in", "r", stdin);
44     ios::sync_with_stdio(0);
45     while(cin >> n && n){
46         Mat m(n);
47         forn(i, n) forn(j, n) cin >> m[i][j];
48         cout << (ll)round(m.determinant()) << endl;
49     }
50     cout << "*" << endl;
51     return 0;
52 }

```

6.10 Teorema Chino del Resto

$$y = \sum_{j=1}^n (x_j * (\prod_{i=1, i \neq j}^n m_i)^{-1} * \prod_{i=1, i \neq j}^n m_i)$$

6.11 Criba

```

1 #define MAXP 100000 //no necesariamente primo

```

```

2 int criba[MAXP+1];
3 void crearcriba(){
4     int w[] = {4,2,4,2,4,6,2,6};
5     for(int p=25;p<=MAXP;p+=10) criba[p]=5;
6     for(int p=9;p<=MAXP;p+=6) criba[p]=3;
7     for(int p=4;p<=MAXP;p+=2) criba[p]=2;
8     for(int p=7,cur=0;p*p<=MAXP;p+=w[cur++&7]) if (!criba[p])
9         for(int j=p*p;j<=MAXP;j+=(p<<1)) if(!criba[j]) criba[j]=p;
10 }
11 vector<int> primos;
12 void buscarprimos(){
13     crearcriba();
14     forr (i,2,MAXP+1) if (!criba[i]) primos.push_back(i);
15 }
16 //~ Useful for bit trick: #define SET(i) ( criba[(i)>>5]|=1<<((i)&31) ),
17 //~ #define INDEX(i) ( (criba[i]>>5)>>((i)&31)&1 ), unsigned int criba[
18 //~ MAXP/32+1];
19
20 int main() {
21     freopen("primos", "w", stdout);
22     buscarprimos();
23 }

```

6.12 Funciones de primos

Sea $n = \prod p_i^{k_i}$, fact(n) genera un map donde a cada p_i le asocia su k_i

```

1 //factoriza bien numeros hasta MAXP^2
2 map<ll,ll> fact(ll n){ //0 (cant primos)
3     map<ll,ll> ret;
4     forall(p, primos){
5         while(!(n%p)){
6             ret[*p]++; //divisor found
7             n/=p;
8         }
9     }
10    if(n>1) ret[n]++;
11    return ret;
12 }
13 //factoriza bien numeros hasta MAXP
14 map<ll,ll> fact2(ll n){ //0 (lg n)
15     map<ll,ll> ret;
16     while (criba[n]){
17         ret[criba[n]]++;
18     }
19 }

```

```

18     n/=criba[n];
19 }
20 if(n>1) ret[n]++;
21 return ret;
22 }
23 //Usar asi: divisores(fac, divs, fac.begin()); NO ESTA ORDENADO
24 void divisores(const map<ll,ll> &f, vector<ll> &divs, map<ll,ll>::
    iterator it, ll n=1){
25     if(it==f.begin()) divs.clear();
26     if(it==f.end()) { divs.pb(n); return; }
27     ll p=it->fst, k=it->snd; ++it;
28     forn(_, k+1) divisores(f, divs, it, n), n*=p;
29 }
30 ll sumDiv (ll n){
31     ll rta = 1;
32     map<ll,ll> f=fact(n);
33     forall(it, f) {
34         ll pot = 1, aux = 0;
35         forn(i, it->snd+1) aux += pot, pot *= it->fst;
36         rta*=aux;
37     }
38     return rta;
39 }
40 ll eulerPhi (ll n){ // con criba: O(lg n)
41     ll rta = n;
42     map<ll,ll> f=fact(n);
43     forall(it, f) rta -= rta / it->first;
44     return rta;
45 }
46 ll eulerPhi2 (ll n){ // O (sqrt n)
47     ll r = n;
48     forr (i,2,n+1){
49         if ((ll)i*i > n) break;
50         if (n % i == 0){
51             while (n%i == 0) n/=i;
52             r -= r/i; }
53     }
54     if (n != 1) r-= r/n;
55     return r;
56 }
57
58 int main() {
59     buscarprimos();

```

```

60     forr (x,1, 500000){
61         cout << "x_=" << x << endl;
62         cout << "Numero_de_factores_primos:" << numPrimeFactors(x) << endl;
63         cout << "Numero_de_distintos_factores_primos:" <<
            numDiffPrimeFactors(x) << endl;
64         cout << "Suma_de_factores_primos:" << sumPrimeFactors(x) << endl;
65         cout << "Numero_de_divisores:" << numDiv(x) << endl;
66         cout << "Suma_de_divisores:" << sumDiv(x) << endl;
67         cout << "Phi_de_Euler:" << eulerPhi(x) << endl;
68     }
69     return 0;
70 }

```

6.13 Phollard's Rho (rolando)

```

1 ll gcd(ll a, ll b){return a?gcd(b %a, a):b;}
2
3 ll mulmod (ll a, ll b, ll c) { //returns (a*b)%c, and minimize overflow
4     ll x = 0, y = a%c;
5     while (b > 0){
6         if (b % 2 == 1) x = (x+y) % c;
7         y = (y*2) % c;
8         b /= 2;
9     }
10    return x % c;
11 }
12
13 ll expmod (ll b, ll e, ll m){//O(log b)
14     if(!e) return 1;
15     ll q= expmod(b,e/2,m); q=mulmod(q,q,m);
16     return e%2? mulmod(b,q,m) : q;
17 }
18
19 bool es_primo_prob (ll n, int a)
20 {
21     if (n == a) return true;
22     ll s = 0,d = n-1;
23     while (d % 2 == 0) s++,d/=2;
24
25     ll x = expmod(a,d,n);
26     if ((x == 1) || (x+1 == n)) return true;
27

```



```

28  forn (i, s-1){
29      x = mulmod(x, x, n);
30      if (x == 1) return false;
31      if (x+1 == n) return true;
32  }
33  return false;
34 }
35
36 bool rabin (ll n){ //devuelve true si n es primo
37     if (n == 1) return false;
38     const int ar[] = {2,3,5,7,11,13,17,19,23};
39     forn (j,9)
40         if (!es_primo_prob(n,ar[j]))
41             return false;
42     return true;
43 }
44
45 ll rho(ll n){
46     if( (n & 1) == 0 ) return 2;
47     ll x = 2 , y = 2 , d = 1;
48     ll c = rand() % n + 1;
49     while( d == 1 ){
50         x = (mulmod( x , x , n ) + c)%n;
51         y = (mulmod( y , y , n ) + c)%n;
52         y = (mulmod( y , y , n ) + c)%n;
53         if( x - y >= 0 ) d = gcd( x - y , n );
54         else d = gcd( y - x , n );
55     }
56     return d==n? rho(n):d;
57 }
58
59 map<ll,ll> prim;
60 void factRho (ll n){ //0 (lg n)^3. un solo numero
61     if (n == 1) return;
62     if (rabin(n)){
63         prim[n]++;
64         return;
65     }
66     ll factor = rho(n);
67     factRho(factor);
68     factRho(n/factor);
69 }

```

6.14 GCD

```

1 | tipo gcd(tipo a, tipo b){return a?gcd(b %a, a):b;}

```

6.15 Extended Euclid

```

1 | void extendedEuclid (ll a, ll b){ //a * x + b * y = d
2 |     if (!b) { x = 1; y = 0; d = a; return;}
3 |     extendedEuclid (b, a%b);
4 |     ll x1 = y;
5 |     ll y1 = x - (a/b) * y;
6 |     x = x1; y = y1;
7 | }

```

6.16 LCM

```

1 | tipo lcm(tipo a, tipo b){return a / gcd(a,b) * b;}

```

6.17 Inversos

```

1 | #define MAXMOD 15485867
2 | ll inv[MAXMOD]; //inv[i]*i=1 mod MOD
3 | void calc(int p){ //0(p)
4 |     inv[1]=1;
5 |     forr(i, 2, p) inv[i]= p-((p/i)*inv[p%i])%p;
6 | }
7 | int inverso(int x){ //0(log x)
8 |     return expmod(x, eulerphi(MOD)-2); //si mod no es primo(sacar a mano)
9 |     return expmod(x, MOD-2); //si mod es primo
10 | }

```

6.18 Simpson

```

1 | double integral(double a, double b, int n=10000) { //0(n), n=cantdiv
2 |     double area=0, h=(b-a)/n, fa=f(a), fb;
3 |     forn(i, n){
4 |         fb=f(a+h*(i+1));
5 |         area+=fa+ 4*f(a+h*(i+0.5)) +fb, fa=fb;
6 |     }
7 |     return area*h/6.;}

```

6.19 Fraction

```

1 | tipo mcd(tipo a, tipo b){return a?mcd(b%a, a):b;}
2 | struct frac{

```

```

3  tipo p,q;
4  frac(tipo p=0, tipo q=1):p(p),q(q) {norm();}
5  void norm(){
6      tipo a = mcd(p,q);
7      if(a) p/=a, q/=a;
8      else q=1;
9      if (q<0) q=-q, p=-p;}
10 frac operator+(const frac& o){
11     tipo a = mcd(q,o.q);
12     return frac(p*(o.q/a)+o.p*(q/a), q*(o.q/a));}
13 frac operator-(const frac& o){
14     tipo a = mcd(q,o.q);
15     return frac(p*(o.q/a)-o.p*(q/a), q*(o.q/a));}
16 frac operator*(frac o){
17     tipo a = mcd(q,o.p), b = mcd(o.q,p);
18     return frac((p/b)*(o.p/a), (q/a)*(o.q/b));}
19 frac operator/(frac o){
20     tipo a = mcd(q,o.q), b = mcd(o.p,p);
21     return frac((p/b)*(o.q/a), (q/a)*(o.p/b));}
22 bool operator<(const frac &o) const{return p*o.q < o.p*q;}
23 bool operator==(frac o){return p==o.p&&q==o.q;}
24 };

```

6.20 Polinomio

```

1      int m = sz(c), n = sz(o.c);
2      vector<tipo> res(max(m,n));
3      forn(i, m) res[i] += c[i];
4      forn(i, n) res[i] += o.c[i];
5      return poly(res);    }
6 poly operator*(const tipo cons) const {
7     vector<tipo> res(sz(c));
8     forn(i, sz(c)) res[i]=c[i]*cons;
9     return poly(res);    }
10 poly operator*(const poly &o) const {
11     int m = sz(c), n = sz(o.c);
12     vector<tipo> res(m+n-1);
13     forn(i, m) forn(j, n) res[i+j]+=c[i]*o.c[j];
14     return poly(res);    }
15 tipo eval(tipo v) {
16     tipo sum = 0;
17     dforn(i, sz(c)) sum=sum*v + c[i];
18     return sum; }

```

```

19 //poly contains only a vector<int> c (the coefficients)
20 //the following function generates the roots of the polynomial
21 //it can be easily modified to return float roots
22 set<tipo> roots(){
23     set<tipo> roots;
24     tipo a0 = abs(c[0]), an = abs(c[sz(c)-1]);
25     vector<tipo> ps,qs;
26     forr(p,1,sqrt(a0)+1) if (a0%p==0) ps.pb(p),ps.pb(a0/p);
27     forr(q,1,sqrt(an)+1) if (an%q==0) qs.pb(q),qs.pb(an/q);
28     forall(pt,ps)
29         forall(qt,qs) if ( (*pt) % (*qt)==0 ) {
30             tipo root = abs((*pt) / (*qt));
31             if (eval(root)==0) roots.insert(root);
32         }
33     return roots; }
34 };
35 pair<poly,tipo> ruffini(const poly p, tipo r) {
36     int n = sz(p.c) - 1 ;
37     vector<tipo> b(n);
38     b[n-1] = p.c[n];
39     dforn(k,n-1) b[k] = p.c[k+1] + r*b[k+1];
40     tipo resto = p.c[0] + r*b[0];
41     poly result(b);
42     return make_pair(result,resto);
43 }
44 poly interpolate(const vector<tipo>& x,const vector<tipo>& y) {
45     poly A; A.c.pb(1);
46     forn(i,sz(x)) { poly aux; aux.c.pb(-x[i]), aux.c.pb(1), A = A * aux;
47     }
48     poly S; S.c.pb(0);
49     forn(i,sz(x)) { poly Li;
50         Li = ruffini(A,x[i]).fst;
51         Li = Li * (1.0 / Li.eval(x[i])); // here put a multiple of the
52         coefficients instead of 1.0 to avoid using double
53         S = S + Li * y[i]; }
54     return S;
55 }
56 int main(){
57     return 0;
58 }

```

6.21 Ec. Lineales

```

1 bool resolver_ev(Mat a, Vec y, Vec &x, Mat &ev){
2   int n = a.size(), m = n?a[0].size():0, rw = min(n, m);
3   vector<int> p; forn(i,m) p.push_back(i);
4   forn(i, rw) {
5     int uc=i, uf=i;
6     forr(f, i, n) forr(c, i, m) if(fabs(a[f][c])>fabs(a[uf][uc])) {uf=f;
7       uc=c;}
8     if (freq(a[uf][uc], 0)) { rw = i; break; }
9     forn(j, n) swap(a[j][i], a[j][uc]);
10    swap(a[i], a[uf]); swap(y[i], y[uf]); swap(p[i], p[uc]);
11    tipo inv = 1 / a[i][i]; //aca divide
12    forr(j, i+1, n) {
13      tipo v = a[j][i] * inv;
14      forr(k, i, m) a[j][k]-=v * a[i][k];
15      y[j] -= v*y[i];
16    }
17    // rw = rango(a), aca la matriz esta triangulada
18    forr(i, rw, n) if (!freq(y[i],0)) return false; // chequeo de
19    compatibilidad
20    x = vector<tipo>(m, 0);
21    dforn(i, rw){
22      tipo s = y[i];
23      forr(j, i+1, rw) s -= a[i][j]*x[p[j]];
24      x[p[i]] = s / a[i][i]; //aca divide
25    }
26    ev = Mat(m-rw, Vec(m, 0)); // Esta parte va SOLO si se necesita el ev
27    forn(k, m-rw) {
28      ev[k][p[k+rw]] = 1;
29      dforn(i, rw){
30        tipo s = -a[i][k+rw];
31        forr(j, i+1, rw) s -= a[i][j]*ev[k][p[j]];
32        ev[k][p[i]] = s / a[i][i]; //aca divide
33      }
34    }
35    return true;
36  }

```

6.22 Karatsuba

```

1 // g++ -std=c++11 "karatsuba.cpp" -o hld
2
3 /**
4 ===== <karatsuba> =====

```

```

5 Complexity:  $O(N^{1.7})$ 
6 Call to karatsuba function paramter two vectors
7 * INPUT: two vectors A,B contains the coeficients of the polynomail
8 * OUTPUT a vector coitains the coeficients of  $A * B$ 
9 */
10
11 int p,k;
12 vector<int> b,r;
13
14 void trim(vector<int>& a){
15   while (a.size() > 0 && a.back() == 0) a.pop_back();
16 }
17
18 vector<int> multiply(const vector<int>& a, const vector<int>& b){
19   vector<int> c(a.size() + b.size() + 1, 0);
20   for (int i = 0; i < a.size(); i++) {
21     for (int j = 0; j < b.size(); j++) {
22       c[i+j] += a[i] * b[j];
23     }
24   }
25   trim(c);
26   return c;
27 }
28 // a = a + b*(10^k)
29 void addTo(vector<int>& a, const vector<int>& b, int k){
30   if (a.size() < b.size() + k) a.resize(b.size() + k);
31   for (int i = 0; i < b.size(); i++) a[i+k] += b[i];
32 }
33 void subFrom(vector<int>& a, const vector<int>& b){
34   for (int i = 0; i < b.size(); i++) a[i] -= b[i];
35 }
36 // a = a + b
37 void addTo(vector<int>& a, const vector<int>& b){
38   addTo(a, b, 0);
39 }
40 vector<int> karatsuba(const vector<int>& a, const vector<int>& b)
41 {
42   int alen = a.size();
43   int blen = b.size();
44   if (alen == 0 || blen == 0) return vector<int>();
45   if (alen < blen) return karatsuba(b, a);
46   if (alen < 50) return multiply(a, b);
47

```

```

48     int half = alen / 2;
49     vector<int> a0(a.begin(), a.begin() + half);
50     vector<int> a1(a.begin() + half, a.end());
51     vector<int> b0(b.begin(), b.begin() + min<int>(blen, half));
52     vector<int> b1(b.begin() + min<int>(blen, half), b.end());
53
54     vector<int> z0 = karatsuba(a0, b0);
55     vector<int> z2 = karatsuba(a1, b1);
56     addTo(a0, a1);
57     addTo(b0, b1);
58     vector<int> z1 = karatsuba(a0, b0);
59     subFrom(z1, z0);
60     subFrom(z1, z2);
61
62     vector<int> res;
63     addTo(res, z0);
64     addTo(res, z1, half);
65     addTo(res, z2, half + half);
66
67     trim(res);
68     return res;
69 }

```

6.23 FFT

```

1  #define lowbit(x) (((x) ^ (x-1)) & (x))
2  typedef complex<long double> Complex;
3
4  void FFT(vector<Complex> &A, int s){
5      int n = A.size();
6      int p = __builtin_ctz(n);
7
8      vector<Complex> a = A;
9
10     for(int i = 0; i<n; ++i){
11         int rev = 0;
12         for(int j = 0; j<p; ++j){
13             rev <<= 1;
14             rev |= ((i >> j) & 1);
15         }
16         A[i] = a[rev];
17     }
18 }

```

```

19     Complex w, wn;
20
21     for(int i = 1; i<=p; ++i){
22         int M = (1<<i), K = (M>>1);
23         wn = Complex(cos(s*2.0*M_PI/(double)M), sin(s*2.0*M_PI/(double)M));
24
25         for(int j = 0; j<n; j += M){
26             w = Complex(1.0, 0.0);
27             for(int l = j; l<K+j; ++l){
28                 Complex t = w;
29                 t *= A[l + K];
30                 Complex u = A[l];
31                 A[l] += t;
32                 u -= t;
33                 A[l + K] = u;
34                 w *= wn;
35             }
36         }
37     }
38
39     if(s==1){
40         for(int i = 0; i<n; ++i)
41             A[i] /= (double)n;
42     }
43 }
44
45 vector<Complex> FFT_Multiply(vector<Complex> &P, vector<Complex> &Q){
46     int n = P.size()+Q.size();
47     while(n!=lowbit(n)) n += lowbit(n);
48
49     P.resize(n,0);
50     Q.resize(n,0);
51
52     FFT(P,1);
53     FFT(Q,1);
54
55     vector<Complex> R;
56     for(int i=0; i<n; i++) R.push_back(P[i]*Q[i]);
57
58     FFT(R,-1);
59
60     return R;

```

```

61 }
62
63 // Para multiplicacion de enteros grandes
64 const long long B = 100000;
65 const int D = 5;

```

6.24 Tablas y cotas (Primos, Divisores, Factoriales, etc)

| | Factoriales |
|--|---|
| 0! = 1 | 11! = 39.916.800 |
| 1! = 1 | 12! = 479.001.600 ($\in \text{int}$) |
| 2! = 2 | 13! = 6.227.020.800 |
| 3! = 6 | 14! = 87.178.291.200 |
| 4! = 24 | 15! = 1.307.674.368.000 |
| 5! = 120 | 16! = 20.922.789.888.000 |
| 6! = 720 | 17! = 355.687.428.096.000 |
| 7! = 5.040 | 18! = 6.402.373.705.728.000 |
| 8! = 40.320 | 19! = 121.645.100.408.832.000 |
| 9! = 362.880 | 20! = 2.432.902.008.176.640.000 ($\in \text{tint}$) |
| 10! = 3.628.800 | 21! = 51.090.942.171.709.400.000 |
| max signed tint = 9.223.372.036.854.775.807 | |
| max unsigned tint = 18.446.744.073.709.551.615 | |

Primos

2 3 5 7 11 13 17 19 23 29 31 37 41 43 47 53 59 61 67 71 73 79 83 89 97 101 103 107 109
 113 127 131 137 139 149 151 157 163 167 173 179 181 191 193 197 199 211 223 227
 229 233 239 241 251 257 263 269 271 277 281 283 293 307 311 313 317 331 337 347
 349 353 359 367 373 379 383 389 397 401 409 419 421 431 433 439 443 449 457 461
 463 467 479 487 491 499 503 509 521 523 541 547 557 563 569 571 577 587 593 599
 601 607 613 617 619 631 641 643 647 653 659 661 673 677 683 691 701 709 719 727
 733 739 743 751 757 761 769 773 787 797 809 811 821 823 827 829 839 853 857 859
 863 877 881 883 887 907 911 919 929 937 941 947 953 967 971 977 983 991 997 1009
 1013 1019 1021 1031 1033 1039 1049 1051 1061 1063 1069 1087 1091 1093 1097 1103
 1109 1117 1123 1129 1151 1153 1163 1171 1181 1187 1193 1201 1213 1217 1223 1229
 1231 1237 1249 1259 1277 1279 1283 1289 1291 1297 1301 1303 1307 1319 1321 1327
 1361 1367 1373 1381 1399 1409 1423 1427 1429 1433 1439 1447 1451 1453 1459 1471
 1481 1483 1487 1489 1493 1499 1511 1523 1531 1543 1549 1553 1559 1567 1571 1579
 1583 1597 1601 1607 1609 1613 1619 1621 1627 1637 1657 1663 1667 1669 1693 1697
 1699 1709 1721 1723 1733 1741 1747 1753 1759 1777 1783 1787 1789 1801 1811 1823
 1831 1847 1861 1867 1871 1873 1877 1879 1889 1901 1907 1913 1931 1933 1949 1951
 1973 1979 1987 1993 1997 1999 2003 2011 2017 2027 2029 2039 2053 2063 2069 2081

Primos cercanos a 10^n

9941 9949 9967 9973 10007 10009 10037 10039 10061 10067 10069 10079

99961 99971 99989 99991 100003 100019 100043 100049 100057 100069
 999959 999961 999979 999983 1000003 1000033 1000037 1000039
 9999943 9999971 9999973 9999991 10000019 10000079 10000103 10000121
 99999941 99999959 99999971 99999989 100000007 100000037 100000039 100000049
 999999893 999999929 999999937 1000000007 1000000009 1000000021 1000000033

Cantidad de primos menores que 10^n

$\pi(10^1) = 4$; $\pi(10^2) = 25$; $\pi(10^3) = 168$; $\pi(10^4) = 1229$; $\pi(10^5) = 9592$
 $\pi(10^6) = 78.498$; $\pi(10^7) = 664.579$; $\pi(10^8) = 5.761.455$; $\pi(10^9) = 50.847.534$
 $\pi(10^{10}) = 455.052.511$; $\pi(10^{11}) = 4.118.054.813$; $\pi(10^{12}) = 37.607.912.018$

Divisores

Cantidad de divisores (σ_0) para *algunos* $n/\neg\exists n' < n, \sigma_0(n') \geq \sigma_0(n)$
 $\sigma_0(60) = 12$; $\sigma_0(120) = 16$; $\sigma_0(180) = 18$; $\sigma_0(240) = 20$; $\sigma_0(360) = 24$
 $\sigma_0(720) = 30$; $\sigma_0(840) = 32$; $\sigma_0(1260) = 36$; $\sigma_0(1680) = 40$; $\sigma_0(10080) = 72$
 $\sigma_0(15120) = 80$; $\sigma_0(50400) = 108$; $\sigma_0(83160) = 128$; $\sigma_0(110880) = 144$
 $\sigma_0(498960) = 200$; $\sigma_0(554400) = 216$; $\sigma_0(1081080) = 256$; $\sigma_0(1441440) = 288$
 $\sigma_0(4324320) = 384$; $\sigma_0(8648640) = 448$

Suma de divisores (σ_1) para *algunos* $n/\neg\exists n' < n, \sigma_1(n') \geq \sigma_1(n)$
 $\sigma_1(96) = 252$; $\sigma_1(108) = 280$; $\sigma_1(120) = 360$; $\sigma_1(144) = 403$; $\sigma_1(168) = 480$
 $\sigma_1(960) = 3048$; $\sigma_1(1008) = 3224$; $\sigma_1(1080) = 3600$; $\sigma_1(1200) = 3844$
 $\sigma_1(4620) = 16128$; $\sigma_1(4680) = 16380$; $\sigma_1(5040) = 19344$; $\sigma_1(5760) = 19890$
 $\sigma_1(8820) = 31122$; $\sigma_1(9240) = 34560$; $\sigma_1(10080) = 39312$; $\sigma_1(10920) = 40320$
 $\sigma_1(32760) = 131040$; $\sigma_1(35280) = 137826$; $\sigma_1(36960) = 145152$; $\sigma_1(37800) = 148800$
 $\sigma_1(60480) = 243840$; $\sigma_1(64680) = 246240$; $\sigma_1(65520) = 270816$; $\sigma_1(70560) = 280098$
 $\sigma_1(95760) = 386880$; $\sigma_1(98280) = 403200$; $\sigma_1(100800) = 409448$
 $\sigma_1(491400) = 2083200$; $\sigma_1(498960) = 2160576$; $\sigma_1(514080) = 2177280$
 $\sigma_1(982800) = 4305280$; $\sigma_1(997920) = 4390848$; $\sigma_1(1048320) = 4464096$
 $\sigma_1(4979520) = 22189440$; $\sigma_1(4989600) = 22686048$; $\sigma_1(5045040) = 23154768$
 $\sigma_1(9896040) = 44323200$; $\sigma_1(9959040) = 44553600$; $\sigma_1(9979200) = 45732192$

7 Grafos

7.1 Bellman-Ford

```

1 int negative_cycle(vector<vector<int> > &G, vector<vector<int> > &cost)
2 {
3     //write your code here
4     bool nc = false;
5     int n = G.size();
6     vector<int> dist(n, INT_MAX / 2);
7     dist[0] = 0;

```

```

7   for(int i = 0; i < n - 1; i++){
8   for(int u = 0; u < n;u++){
9       for(int j = 0; j < G[u].size();j++){
10          int v = G[u][j];
11          int w = cost[u][j];
12          dist[v] = min(dist[v], dist[u] + w);
13      }
14      for(int u = 0; u < n;u++){
15      for(int j = 0; j < G[u].size();j++){
16          int v = G[u][j];
17          int w = cost[u][j];
18          if(dist[v] > dist[u] + w)nc = true;
19      }
20      }
21      return nc;
22  }

```

7.2 dijkstra grafos densos

7.3 2 SAT definitivamente no con Tarjan

```

1 // g++ -std=c++11 "twosat.cpp" -o run
2 /**
3 ===== <Two Sat> =====
4 Complexity: O(N)
5 Input: number of variables, then number of clause clauses in format (u
6       or v)
7 if u,v > 0 then is equivalent to u,v
8 if u,v < 0 then is equivalent to u , v
9 Output: UNSATISFIABLE can't find a solution
10 SATISFIABLE if exist a solution then print the assignment of all
11       variables (negative for xi = false)
12
13 Examples:
14 Input:
15 3 3
16 1 -3
17 -1 2
18 -2 -3
19 Output
20 SATISFIABLE
21 1 2 -3
22 *
23 Input

```

```

22 1 2
23 1 1
24 -1 -1
25 Output
26 UNSATISFIABLE
27 */
28 #include <bits/stdc++.h>
29 using namespace std;
30 vector<int>G[2][2000010],G2[2000010];
31 int n, m;
32 int scc[2000010];
33 bool vis[2000010];
34 vector<int>comp[2000010];
35 int assign[2000010];
36 int cc = 0;
37 stack<int>st;
38 vector<int>sta;
39 void dfs(int u,int type){
40     if(scc[u] != -1)return;
41     scc[u] = cc;
42     for(int v:G[type][u]){
43         dfs(v,type);
44     }
45     if(!type)st.push(u);
46 }
47 void topo(int u){
48     if(vis[u])return;
49     vis[u] = true;
50     for(int v:G2[u])topo(v);
51     sta.push_back(u);
52 }
53 void buildGraphWitouthLoop(){
54     for(int i = 0;i < 2 * n;i++){
55         for(int j = 0;j < G[0][i].size();j++){
56             if(scc[i] != scc[G[0][i][j]])
57                 G2[scc[i]].push_back(scc[G[0][i][j]]);
58         }
59     }
60 }
61 int main() {
62     ios::sync_with_stdio(false);cin.tie(0);
63     cin >> n >> m;
64     for(int i = 0,u,v; i < m;i++){

```

```

65     cin >> u >> v;
66     int uu = (u > 0?(u - 1) * 2:(-u - 1) * 2 + 1);
67     int vv = (v > 0?(v - 1) * 2:(-v - 1) * 2 + 1);
68     // cout << uu << " " << (uu ^ 1) << "\n";
69     G[0][uu ^ 1].push_back(vv);
70     G[0][vv ^ 1].push_back(uu);
71     G[1][vv].push_back(uu ^ 1);
72     G[1][uu].push_back(vv ^ 1);
73 }
74 memset(scc,-1,sizeof scc);
75 for(int i = 0; i < 2 * n;i++){
76     if(scc[i] == -1)dfs(i,0);
77 }
78 memset(scc,-1,sizeof scc);
79 while(!st.empty()){
80     int u = st.top();st.pop();
81     if(scc[u] == -1){
82         dfs(u,1);
83         cc++;
84     }
85 }
86 bool unsat = false;
87 for(int i = 0; i < 2 * n;i++){
88     if(scc[i] == scc[i ^ 1])unsat = true;
89     comp[scc[i]].push_back(i);
90 }
91 if(unsat){
92     return cout << "UNSATISFIABLE",0;
93 }
94 cout << "SATISFIABLE\n";
95 buildGraphWithouthLoop();
96 for(int i = 0; i < 2 * n;i++){
97     if(!vis[i])topo(i);
98 }
99 for(int u:sta){//inverse of topological sort
100     for(int v:comp[u]){//transitive Skew-Symmetry
101         if(!assign[v]){
102             assign[v] = 1;
103             assign[v ^ 1] = -1;
104         }
105     }
106 }
107 for(int i = 0,j = 1; i < 2 * n; i += 2,j++){

```

```

108     cout << (j) * (assign[i]) << "\n";
109 }
110     return 0;
111 }

```

7.4 Prim

7.5 Articulation Points (desgraciadamente tarjan)

```

1 // g++ -std=c++11 "articulationpointsandbridges.cpp" -o run
2 /**
3 ===== <Articulation points and bridges c++ version>
4 =====
5 Given a graph return a vector of pairs with the bridges and a bool array
6 art[]
7 true if the node is an articulation point
8 * false otherwise
9 Graph nodes: 0 to N - 1
10 */
11 using namespace std;
12 vector<int>G[10010];
13 int low[10010],num[10010],parent[10010],cc;
14 //cc is my timer
15 int art[10010];//bool for detect art point, int for detect how many
16 nodes are connected to my articulation point
17 int root,rC;
18 int n;
19 vector<pair<int,int> >bridges;
20 void dfs(int u){
21     low[u]=num[u]=cc++;
22     for(int v:G[u]){
23         if(num[v]==-1){
24             parent[v]=u;
25             if(u==root)rC++;
26             dfs(v);
27             if(low[v]>=num[u])art[u]++;//is a articulation point
28             if(low[v]>num[u])bridges.push_back({u,v});//this is a bridge
29             low[u]=min(low[u],low[v]);
30         }
31         else if(v!=parent[u]){
32             low[u]=min(low[u],num[v]);
33         }
34     }
35 }

```

```

33 void init(){
34     bridges.clear();
35     for(int i=0;i<n;i++){
36         art[i]=low[i]=0;
37         num[i]=parent[i]=-1;
38         G[i].clear();
39     }
40     cc=0;
41 }
42 void callARTBRID(){
43     for(int i=0;i<n;i++){
44         if(num[i]==-1){
45             root=i,rC=0;dfs(i);
46             art[root]=(rC>1);
47         }
48     }
49 }

```

7.6 componentes biconexas y puentes (block cut tree)

7.7 LCA saltitos potencias de 2

7.8 LCA sparse table query O(1)

7.9 HLD

```

1 // g++ -std=c++11 "hld.cpp" -o hld
2
3 /**
4 ===== <HLD> =====
5 Complexity: O(N*log(N))
6 Given a tree and asociative operation in the paths of this tree ask for
7 many queries, and updates
8 in nodes or edges
9 Input of this example:
10 N number of nodes, then N elements values in each node
11 then n - 1 conexions
12 Q queries if T == 1 query on the path u,v
13 else update node U with value val.
14
15 Example problems: Spoj QTREE1 to QTREE6, toby and tree UVA
16 */
17 #include <bits/stdc++.h>

```

```

18 using namespace std;
19 const int maxn = 1e5;
20 const int NEUTRO = 0; // a null value for my ST
21 int vec[maxn];
22 vector<int>G[maxn]; //the graph
23 //int idx[maxn]; // case with value in the edge
24 int op(int u,int v){// an operation for my path (using ST)
25     //return __gcd(u,v);
26     //return max(u,v);
27     return u + v;
28 }
29 int n;
30 //ask to Branimir for information about this
31 struct SegmentTree{
32     int T[2*maxn];
33     void init(){
34         memset(T,0,sizeof T);
35     }
36     void set(int pos,int val){
37         pos += n;
38         T[pos] = val;
39         for(pos >>= 1; pos > 0; pos >>=1){
40             T[pos] = op( T[pos << 1] , T[(pos << 1)|1] );
41         }
42     }
43     int query(int l,int r){
44         l += n;
45         r += n;
46         int ans = NEUTRO;
47         while( l < r){
48             if ( l & 1 ) ans = op(ans, T[l++] );
49             if ( r & 1 ) ans = op( ans, T[--r] );
50             l >>= 1;
51             r >>= 1;
52         }
53         return ans;
54     }
55 };
56 struct hld{
57     int ncad; // store actual number of chain
58     int root; // the root of a tree generally 0 or 1
59     int pos; // pos of node in chain
60 }

```



```

61 int sz[maxn]; // store the subsize of subtrees
62 int depth[maxn]; //depth of the node, useful for LCA via HLD
63 int parent[maxn]; // useful for LCA
64 int where[maxn]; // where chain is the node?
65 //int edgepos[maxn]; // if the value is on the edge: stored in a node
66 int chainIdx[maxn]; // position in the chain of the node
67 int head[maxn]; // the head of the i-th chain
68 //int val[maxn]; // if the value is on the edge
69 SegmentTree tree; // this ST allow operations in the path
70
71 void init(){//settings value, and process de HLD
72     root = 0;
73     ncad = 0;
74     pos = 0;
75     for(int i = 0; i <=n; i++){
76         where[i] = head[i] = -1;
77     }
78     depth[root] = 0;
79     dfs(root , -1);
80     descompose(root);
81     tree.init();
82     /* case with values in edges
83     for(int i=0;i<n;i++){
84         tree.set(i,val[i]);
85     }
86     */
87 }
88
89
90 ///init descomposition
91 void dfs(int u,int pu){
92     sz[u] = 1; //init the sz of this subtree
93     parent[u] = pu; // assign the parent
94     for(int i = 0; i < G[u].size(); i++){
95         int v = G[u][i];
96         if ( v == pu )continue;
97         //edgepos[idx[u][i]] = v;
98         depth[v] = depth[u] + 1;
99         dfs(v,u);
100         sz[u] += sz[v];
101     }
102 }
103 //descompose graph in HLD descomposition

```

```

104 void descompose(int u){
105     if( head[ncad] == -1)head[ncad] = u; // the head of ncad is u
106     where[u] = ncad; // assign where tu node
107     //val[pos] = cost; cost another parameter in descompose for graphs
        with values in edges
108     chainIdx[u] = pos++; //assing pos to this node
109     int maxi = -1, sc = -1; //finding a special child
110     for(int v:G[u]){
111         if( sz[v] > maxi && where[v] == -1){
112             maxi = sz[v];
113             sc = v;
114         }
115     }
116     if(sc != -1)descompose(sc);
117     //light nodes here:
118     for(int v:G[u]){
119         if(where[v] == -1){
120             ncad++;
121             descompose(v);
122         }
123     }
124 }
125 ///end descomposition
126
127 int lca(int u,int v){
128     while(where[u]!=where[v]){
129         if(depth[ head[ where[u] ] ] > depth[ head[ where[v] ] ] )u =
            parent[ head[ where[u] ] ];
130         else v = parent[ head[ where[v] ] ];
131     }
132     return depth[u] < depth[v] ? u:v;
133 }
134
135 void update(int u, int val){
136     tree.set(chainIdx[u],val);
137 }
138
139 int query(int u,int v){
140     // if ( u == v) return NEUTRO; value in edges
141     int vChain = where[v];
142     int ans = NEUTRO;
143     while(true){
144         int uChain = where[u];

```

```

145     if(uChain == vChain){
146         // return op(ans, tree.query( chainIdx[v] + 1, chainIdx[u] + 1)
147         ); value in edges
148         return op(ans, tree.query( chainIdx[v], chainIdx[u] + 1 ));
149     }
150     int hu = head[uChain];
151     ans = op( ans, tree.query(chainIdx[hu], chainIdx[u] + 1 ));
152     u = parent[hu];
153 }
154
155 int Q(int u,int v){
156     int L = lca(u,v);
157     return op( query(u,L) , query(v,L) );
158 }
159 }HLD;
160 int main(){
161     //ios::sync_with_stdio(false);cin.tie(0);
162     while(cin >> n){
163         for(int i = 0; i < n; i++)G[i].clear();
164         for(int i = 0; i < n; i++){
165             cin >> vec[i];
166         }
167         for(int i = 1, u,v ; i < n; i++){
168             cin >> u >> v;
169             G[u].push_back(v);
170             G[v].push_back(u);
171             /* case with value in edges
172             G[u].push_back(make_pair(v,w));
173             idx[u].push_back(i-1);
174             G[v].push_back(make_pair(u,w));
175             idx[v].push_back(i-1);
176
177             */
178         }
179         HLD.init();
180         for(int i = 0; i < n; i++){
181             HLD.update(i, vec[i]);
182         }
183         int question;
184         cin >> question;
185         for(int i = 0, t, u ,v; i < question; i++){
186             cin >> t >> u >> v;

```

```

187         if( t == 1){
188             cout << HLD.Q(u,v) << "\n";
189         }
190         else HLD.update(u,v);
191     }
192 }
193 }

```

7.10 centroid decomposition

7.11 euler cycle

```

1 int n,m,ars[MAXE], eq;
2 vector<int> G[MAXN]; //fill G,n,m,ars,eq
3 list<int> path;
4 int used[MAXN];
5 bool usede[MAXE];
6 queue<list<int>::iterator> q;
7 int get(int v){
8     while(used[v]<sz(G[v]) && usede[ G[v][used[v]] ]) used[v]++;
9     return used[v];
10 }
11 void explore(int v, int r, list<int>::iterator it){
12     int ar=G[v][get(v)]; int u=v^ars[ar];
13     usede[ar]=true;
14     list<int>::iterator it2=path.insert(it, u);
15     if(u!=r) explore(u, r, it2);
16     if(get(v)<sz(G[v])) q.push(it);
17 }
18 void euler(){
19     zero(used), zero(usede);
20     path.clear();
21     q=queue<list<int>::iterator>();
22     path.push_back(0); q.push(path.begin());
23     while(sz(q)){
24         list<int>::iterator it=q.front(); q.pop();
25         if(used[*it]<sz(G[*it])) explore(*it, *it, it);
26     }
27     reverse(path.begin(), path.end());
28 }
29 void addEdge(int u, int v){
30     G[u].pb(eq), G[v].pb(eq);
31     ars[eq++]=u^v;
32 }

```

7.12 diámetro y centro de un árbol

```

1  /**
2  ===== <Diameter and center of a tree> =====
3  //Problem: Given a tree get the center (or centers)
4  /* the nodes in the tree that minimize the length of the longest path
   from it to any other node.
5  * *Finding tree centers:
6  * If diameter length is even, then we have one tree center. If odd,
   then we have 2 centers.
7  * E.g. 1-2-3-4-5 -> center is 3
8  * E.g. 1-2-3-4-5-6 -> center is 3, 4
9  * On other side, we can get the worst nodes through the center nodes.
10 * A worst node is one that is an end of a diameter, so it has the worst
   tree height
11 Input:
12 * No
13 Output:
14 * No
15 dfs: calculate the diameter of the tree
16 * maxi stores the diameter
17 findingCenters() return the centers
18 Nodes in graph 1 to N careful with this
19 Complexity: O(N)
20 */
21
22 vector<int>G[5010];
23 int maxi=-1,far;
24 int n;
25 int pre[5010];
26 int Queue[5010];
27
28 void dfs(int path,int u,int parent){
29     pre[u]=parent;
30     if(path>=maxi){
31         maxi=path;
32         far=u;
33     }
34     for(int v:G[u]){
35         if(parent!=v){
36             dfs(path+1,v,u); //path + w if the graph as weighted
37         }
38     }

```

```

39     }
40 }
41 pair<int,int> findingCenters(){
42     maxi=-1;
43     dfs(0,1,-1);
44     dfs(0,far,-1);
45     int t=far,L=0;
46     while(t!=-1){
47         Queue[L]=t;
48         t=pre[t];
49         ++L;
50     }
51     int a=-1,b=-1;
52     if(L&1){
53         a=Queue[L/2];
54     }
55     else{
56         a=min(Queue[L/2-1],Queue[L/2]),b=max(Queue[L/2-1],Queue[L/2]);
57     }
58     return {a,b};
59 }

```

7.13 algoritmo hungaro

7.14 union find dinámico

```

1  #include <bits/stdc++.h>
2  using namespace std;
3  #define dprint(v) cerr << #v "=" << v << endl //;)
4  #define forr(i,a,b) for(int i=(a); i<(b); i++)
5  #define forn(i,n) forr(i,0,n)
6  #define dform(i,n) for(int i=n-1; i>=0; i--)
7  #define forall(it,v) for(auto it=v.begin();it!=v.end();++it)
8  #define sz(c) ((int)c.size())
9  #define zero(v) memset(v, 0, sizeof(v))
10 #define pb push_back
11 #define fst first
12 #define snd second
13 #define mkp make_pair
14 typedef long long ll;
15 typedef pair<int,int> ii;
16
17 struct UnionFind {
18     int n, comp;

```

```

19  vector<int> pre,si,c;
20  UnionFind(int n=0):n(n), comp(n), pre(n), si(n, 1) {
21      forn(i,n) pre[i] = i; }
22  int find(int u){return u==pre[u]?u:find(pre[u]);}
23  bool merge(int u, int v) {
24      if((u=find(u))==v) return false;
25      if(si[u]<si[v]) swap(u, v);
26      si[u]+=si[v], pre[v]=u, comp--, c.pb(v);
27      return true;
28  }
29  int snap(){return sz(c);}
30  void rollback(int snap){
31      while(sz(c)>snap){
32          int v = c.back(); c.pop_back();
33          si[pre[v]] -= si[v], pre[v] = v, comp++;
34      }
35  }
36 };
37 enum {ADD,DEL,QUERY};
38 struct Query {int type,u,v;};
39 struct DynCon {
40     vector<Query> q;
41     UnionFind dsu;
42     vector<int> match,res;
43     map<ii,int> last; //se puede no usar cuando hay identificador para
                        //cada arista (mejora poco)
44     DynCon(int n=0):dsu(n){}
45     void add(int u, int v) {
46         if(u>v) swap(u,v);
47         q.pb((Query){ADD, u, v}), match.pb(-1);
48         last[ii(u,v)] = sz(q)-1;
49     }
50     void remove(int u, int v) {
51         if(u>v) swap(u,v);
52         q.pb((Query){DEL, u, v});
53         int prev = last[ii(u,v)];
54         match[prev] = sz(q)-1;
55         match.pb(prev);
56     }
57     void query() { //podria pasarle un puntero donde guardar la respuesta
58         q.pb((Query){QUERY, -1, -1}), match.pb(-1);}
59     void process() {
60         forn(i,sz(q)) if (q[i].type == ADD && match[i] == -1) match[i] =

```

```

        sz(q);
61         go(0,sz(q));
62     }
63     void go(int l, int r) {
64         if(l+1==r){
65             if (q[l].type == QUERY) //Aqui responder la query usando el
                dsu!
66             res.pb(dsu.comp); //aqui query=cantidad de componentes
                conexas
67             return;
68         }
69         int s=dsu.snap(), m = (l+r) / 2;
70         forr(i,m,r) if(match[i]!=-1 && match[i]<l) dsu.merge(q[i].u, q[i]
                ].v);
71         go(l,m);
72         dsu.rollback(s);
73         s = dsu.snap();
74         forr(i,l,m) if(match[i]!=-1 && match[i]>=r) dsu.merge(q[i].u, q[
                i].v);
75         go(m,r);
76         dsu.rollback(s);
77     }
78 }dc;
79
80 // Problema ejemplo: http://codeforces.com/gym/100551/problem/A
81
82 int n,k;
83
84 int main() {
85     //~ freopen("in", "r", stdin);
86     freopen("connect.in", "r", stdin);
87     freopen("connect.out", "w", stdout);
88     ios::sync_with_stdio(0);
89     while(cin >> n >> k){
90         dc=DynCon(n);
91         forn(_,k) { string ord; cin >> ord;
92             if (ord=="?") {
93                 dc.query();
94             } else if (ord=="+") { int a,b; cin>>a>>b; a--;b--;
95                 dc.add(a,b);
96             } else if (ord=="-") { int a,b; cin>>a>>b; a--;b--;
97                 dc.remove(a,b);
98             } else assert(false);

```

```

99     }
100     if(!k) continue;//k==0 WTF
101     dc.process();
102     forn(i,sz(dc.res)) cout << dc.res[i] << endl;
103 }
104 return 0;
105 }

```

7.15 truquitos estúpidos por ejemplo second MST es con LCA

7.16 erdos galloi

```

1 // g++ -std=c++11 "erdosgalloi.cpp" -o run
2 /**
3 ===== <Erdosgalloi c++ version> =====
4 Given the grades of each node of a graph return if this form a valid
5 graph
6 includes: algorithm, functional, numeric, forn
7 // Receives a sorted degree sequence (non ascending)
8 O(NlgN)
9 */
10 bool isGraphicSequence(const vector<int> &seq) // O(n lg n)
11 {
12     vector<int> sum;
13     int n = seq.size();
14
15     if (n == 1 && seq[0] != 0) return false;
16
17     sum.reserve(n + 1);
18     sum.push_back(0);
19     for (int i = 0; i < n; ++i) sum.push_back(sum[i] + seq[i]);
20     if ((sum[n] & 1) == 1) return false;
21
22     for (long long k = 1; k <= n - 1 && seq[k - 1] >= k; ++k) {
23         int j = distance(seq.begin(), upper_bound(seq.begin() + k, seq.end()
24             , k,
25                 greater<int>())) +
26             1;
27         long long left = sum[k];
28         long long right = k * (k - 1) + (j - k - 1) * k + (sum[n] - sum[j -
29             1]);
30
31         if (left > right) return false;

```

```

30     }
31
32     return true;
33 }

```

7.17 grafo funcional hallar k-esimo partiendo de un nodo

7.18 konig

7.19 min-vertex cover bipartitos

7.20 max-flow (min cost versión)

```

1 // g++ -std=c++11 "maxflowmincost.cpp" -o run
2 /**
3 ===== <Max flow-min cost c++ version> =====
4 Given a graph with edges with a capacity C and weight D
5 * compute the max-flow min cost
6 Edmond karps idea
7 * Complexity O(v *E*log(v))
8 Problem for practice: Dijkstra Dijkstra uva
9 */
10 #define REP(i,j,k) for(int (i)=(j);(i)<(k);++(i))
11 #define MP make_pair
12
13 using namespace std;
14
15 #define MAXN 500
16 #define MAXM MAXN * 5
17 typedef vector<int> VI;
18 typedef long long ll;
19 const int INF = 1E9; // $infinity$: be careful to make this big enough
20
21 int S; // source
22 int T; // sink
23 int FN; // number of nodes
24 int FM; // number of edges (initialize this to 0)
25 // ra[a]: edges connected to a (NO MATTER WHICH WAY!!!); clear this in
26 // the beginning
27 VI ra[MAXN];
28 int kend[MAXM], cap[MAXM], cost[MAXM]; // size: TWICE the number of
29 // edges
30
31 // Adds an edge from a to b with capacity c and cost d and returns the

```

```

    number of the new edge
29
30 int addedge(int a, int b, int c, int d) {
31     int i = 2*FM;
32     kend[i] = b;
33     cap[i] = c;
34     cost[i] = d;
35     ra[a].push_back(i);
36     kend[i+1] = a;
37     cap[i+1] = 0;
38     cost[i+1] = -d;
39     ra[b].push_back(i+1);
40     FM++;
41     return i;
42 }
43 int n;
44 int dst[MAXM], pre[MAXM], pret[MAXM];
45 //finding the shortest path via fanning duan, also it works with bellman
    ford
46 //or dijkstra (careful of negative cycles)
47 bool spfa(){
48     REP(i,0,FN) dst[i] = INF;
49     dst[S] = 0;
50     queue<int> que; que.push(S);
51     while(!que.empty()){
52         int x = que.front(); que.pop();
53         for (int t : ra[x]){
54             int y = kend[t], nw = dst[x] + cost[t];
55             if(cap[t] > 0 && nw<dst[y]){
56                 dst[y] = nw; pre[y] = x; pret[y] = t; que.push(y);
57             }
58         }
59     }
60     return dst[T] != INF;
61 }
62 // returns the maximum flow and the minimum cost for this flow
63 pair<ll,ll> solve(){
64     ll totw = 0, totf = 0;
65     while(spfa()){
66         int minflow = INF;
67         for (int x = T; x!=S; x = pre[x]){
68             minflow = min(minflow, cap[pret[x]]);
69         }

```

```

70         for (int x = T; x!=S; x = pre[x]){
71             cap[pret[x]] -= minflow;
72             cap[pret[x]^1] += minflow;
73         }
74         totf += minflow;
75         totw += minflow*dst[T];
76     }
77     return make_pair(totf, totw);
78 }
79 void init(){
80     FN=4*n+15; //make this big n=number of nodes of the graph
81     FM=0;
82     S=0,T=n+1;
83     for(int i=0;i<FN;i++)ra[i].clear();//clear the graph be careful
84 }

```

7.21 max-flow corto con matriz

```

1 // g++ "maxflowMVEK.cpp" -o run
2 /**
3 ===== <Max Flow with matriz Edmonds karp c++ version>
4 =====
5 //Given a graph with capacitys find the max-flow
6
7 Nodes indexed 1 to N
8 * Complexity O(N *E)
9 Problem for practice: UVA 820
10 */
11 #define N 500
12 int cap[N][N], pre[N], n;
13 int s;//source
14 int t;//destination
15 bool bfs() {
16     queue<int>q;
17     q.push(s);
18     memset(pre,-1,sizeof pre);
19     pre[s]=s;
20     while(!q.empty()){
21         int u=q.front();q.pop();
22         if(u==t)return true;
23         for(int i=1;i<=n;i++){//nodes 1 to n
24             if(pre[i]==-1&&cap[u][i])pre[i]=u,q.push(i);
25         }
26     }

```

```

25     }
26     return false;
27 }
28
29 int maxFlow() {
30     int mf=0,f,v;//max flow, flow for a path, the vertex
31     while(bfs()){while encountered a path source to destination
32         v=t;//min
33         f=INT_MAX;//make this big enough
34         while(pre[v]!=v){f=min(f,cap[pre[v]][v]),v=pre[v];};//finding the
            min capacity
35         v=t;mf+=f;
36         while(pre[v]!=v){cap[pre[v]][v]-=f,cap[v][pre[v]]+=f,v=pre[v];}
            //update the flow
37     }
38     return mf;
39 }
40 void init(){
41     memset(cap,0,sizeof cap);
42     //cap[u][v]+=capacidad, cap[v][u]+=capacidad
43 }

```

7.22 max-flow sin matriz

```

1 // g++ -std=c++11 "maxflowNMEK.cpp" -o run
2 /**
3 ===== <Max Flow with-out matriz Edmonds karp c++ version>
4 =====
5 //Given a graph with capacitys find the max-flow
6
7 Nodes indexed 1 to N
8 * Complexity O(N *E)
9 Problem for practice: UVA 820
10 * Input N number of nodes,
11 * M edges conexions
12 * compute the flow with source 1 and sink N
13 */
14 using namespace std;
15 const int N = 110;
16 const int M = 10010 * 2;
17 vector<int>G[N];
18 int kend[M], cap[M], cost[M];
19 int edge = 0;

```

```

19 int s,t;
20 void add(int u,int v,int c){
21     int forward = edge * 2, backward = edge * 2 + 1;
22     kend[forward] = v;
23     cap[forward] = c;
24     G[u].push_back(forward);
25     kend[backward] = u;
26     cap[backward] = 0;
27     G[v].push_back(backward);
28     edge++;
29 }
30 int vis[M],pre[M],pret[M];
31 bool bfs(){
32     for(int i = 0; i <= 100;i++)vis[i] = false;
33     vis[s] = true;
34     queue<int>q;
35     q.push(s);
36     while(!q.empty()){
37         int u = q.front();q.pop();
38         for(int edge:G[u]){
39             int v = kend[edge];
40             if(cap[edge] > 0 && !vis[v]){
41                 vis[v] = true;
42                 pre[v] = u;
43                 pret[v] = edge;//the edge store the information
44                 q.push(v);
45             }
46         }
47     }
48     return vis[t];
49 }
50 int max_flow(){
51     int totf = 0LL;
52     while(bfs()){
53         int minflow = INT_MAX;
54         for(int x = t; x != s; x = pre[x]){
55             minflow = min(minflow,cap[pret[x]]);
56         }
57         for(int x = t; x != s; x = pre[x]){
58             cap[pret[x]] -= minflow;
59             cap[pret[x] ^ 1] += minflow;
60         }
61         totf += minflow;

```

```

62 }
63 return totf;
64 }
65 int main(){
66     int n,m;
67     scanf("%d%d",&n,&m);
68     for(int i = 0,u,v,ca; i < m;i++){
69         scanf("%d%d%d",&u,&v,&ca);
70         add(u,v,ca);
71     }
72     s = 1, t = n;
73     printf("%lld\n",max_flow());
74 }

```

7.23 Dinic

```

1
2 const int MAX = 300;
3 // Corte minimo: vertices con dist[v]>=0 (del lado de src) VS. dist[v]
// ==-1 (del lado del dst)
4 // Para el caso de la red de Bipartite Matching (Sean V1 y V2 los
// conjuntos mas proximos a src y dst respectivamente):
5 // Reconstruir matching: para todo v1 en V1 ver las aristas a vertices
// de V2 con it->f>0, es arista del Matching
6 // Min Vertex Cover: vertices de V1 con dist[v]==-1 + vertices de V2 con
// dist[v]>0
7 // Max Independent Set: tomar los vertices NO tomados por el Min Vertex
// Cover
8 // Max Clique: construir la red de G complemento (debe ser bipartito!) y
// encontrar un Max Independet Set
9 // Min Edge Cover: tomar las aristas del matching + para todo vertices
// no cubierto hasta el momento, tomar cualquier arista de el
10 int nodes, src, dst;
11 int dist[MAX], q[MAX], work[MAX];
12 struct Edge {
13     int to, rev;
14     ll f, cap;
15     Edge(int to, int rev, ll f, ll cap) : to(to), rev(rev), f(f), cap(
// cap) {}
16 };
17 vector<Edge> G[MAX];
18 void addEdge(int s, int t, ll cap){
19     G[s].pb(Edge(t, sz(G[t]), 0, cap)), G[t].pb(Edge(s, sz(G[s])-1, 0,

```

```

0));}
20 bool dinic_bfs(){
21     fill(dist, dist+nodes, -1), dist[src]=0;
22     int qt=0; q[qt++]=src;
23     for(int qh=0; qh<qt; qh++){
24         int u =q[qh];
25         forall(e, G[u]){
26             int v=e->to;
27             if(dist[v]<0 && e->f < e->cap)
28                 dist[v]=dist[u]+1, q[qt++]=v;
29         }
30     }
31     return dist[dst]>=0;
32 }
33 ll dinic_dfs(int u, ll f){
34     if(u==dst) return f;
35     for(int &i=work[u]; i<sz(G[u]); i++){
36         Edge &e = G[u][i];
37         if(e.cap<=e.f) continue;
38         int v=e.to;
39         if(dist[v]==dist[u]+1){
40             ll df=dinic_dfs(v, min(f, e.cap-e.f));
41             if(df>0){
42                 e.f+=df, G[v][e.rev].f-= df;
43                 return df; }
44         }
45     }
46     return 0;
47 }
48 ll maxFlow(int _src, int _dst){
49     src=_src, dst=_dst;
50     ll result=0;
51     while(dinic_bfs()){
52         fill(work, work+nodes, 0);
53         while(ll delta=dinic_dfs(src,INF))
54             result+=delta;
55     }
56     // todos los nodos con dist[v]!=-1 vs los que tienen dist[v]==-1
// forman el min-cut
57     return result; }

```

7.24 máximo emparejamiento bipartito


```

1 // g++ -std=c "bipartitematching.cpp" -o run
2 /**
3 ===== <MCBM max cardinality bipartite matching c++ version>
4 =====
5 Return the bipartite matching of a Graph
6 * Format of nodes: 1 to N
7 */
8 const int N = 100010;
9 vector<int>G[N];
10 bool v[N]; //for the greedy speed up
11 int match[N];
12 bool vis[N];
13 int n,m;
14 //calling augmenting path
15 bool aug(int u){
16     if(vis[u])return false;
17     vis[u]=true;
18     for(int i=0;i<(int)G[u].size();++i){
19         int r=G[u][i];
20         if(match[r]==-1||aug(match[r])){
21             match[r]=u;match[u]=r;return true;
22         }
23     }
24     return 0;
25 }
26 int mc;
27 //finding all augmenting path's
28 int solve(){
29     bool check=true;
30     while(check){
31         check=false;
32         memset(vis,0,sizeof vis);
33         for(int i=1;i<=n;++i){
34             if(!v[i]&&match[i]==-1){
35                 bool op=aug(i);
36                 check|=op;
37                 mc+=op;
38             }
39         }
40     }
41     return mc;
42 }

```

```

43 void init(){
44     memset(v,0,sizeof v);
45     memset(vis,false,sizeof vis);
46     mc=0;
47     memset(match,-1,sizeof match);
48     for(int i=0;i<=n;i++)G[i].clear();
49 }
50 void greedySpeedUp(){
51     //greedy optimization, match with the first not matched
52     for(int i=1;i<=n;++i){
53         for(int j=0;j<(int)G[i].size();++j){
54             if(match[G[i][j]]==-1){
55                 match[G[i][j]]=i,match[i]=G[i][j],mc++,v[i]=true;break;
56             }
57         }
58     }
59 }

```

7.25 max-independent set en bipartitos

7.26 min-path cover (ver tópicos raros de halim)

7.27 min-cost arborescence

7.28 lema de diapositivas de nico de grafos funcionales

7.29 minimax y maximini con kruskal y dijkstra

```

1 // g++ -std=c++11 "maximini.cpp" -o run
2 /**
3 ===== <maximini c++ version> =====
4 Given a weighted graph return the maximini (the maximum of the minimum)
5 or the minimax (the minimum of the maximum) in the path a,b
6 *
7 Minimax as defined as: finding the minimum of maximum edge weight among
8 all possible paths
9 * between two vertices a to b, the cost for a path from a to b is
10 determined by maximum edge
11 * weight along this path. Among all these possible paths from a to b,
12 pick the one with the minimum
13 * ax-edge-weight
14 * Complexity  $O(E \cdot \log(E) + V + E)$ 
15 *
16 Problem for practice: UVA 534,544

```

```

14 */
15 int n;
16 pair<int,pair<int,int> >Edges[20000];
17 int t;
18 map<string,int>mp;
19 int parent[210];
20 pair<int,int>child[210];
21 bool vis[210];
22 vector<pair<int,int> >G[210];
23
24 int find(int u){return u==parent[u]?u:parent[u]=find(parent[u]);}
25 void Union(int u,int v){
26     int pu=find(u),pv=find(v);
27     if(pu!=pv){
28         parent[pv]=pu;
29     }
30 }
31 int mst(int a,int b){
32     sort(Edges,Edges+t);
33     reverse(Edges,Edges+t);//don't reverse for the minimax
34     for(int i=0;i<=200;i++)parent[i] = i;
35     int w,u,v, maximini = 1e8, minimax = 0;
36     for(int i=0;i<t;i++){
37         tie(w,u,v) = make_tuple(Edges[i].first, Edges[i].second.first, Edges
38             [i].second.second);
39         if(find(u) != find(v)){
40             Union(u,v);
41             G[u].push_back({v,w});
42             G[v].push_back({u,w});
43         }
44     }
45     queue<int>q;
46     q.push(a);
47     vis[a]=true;
48     while(!q.empty()){
49         int u = q.front();q.pop();
50         //if(u==1)break;
51         for(pair<int,double>node: G[u]){
52             if(!vis[node.first]){
53                 vis[node.first] = true;
54                 q.push(node.first);
55                 //maximini=max(maximini,node.second);
56                 child[node.first].first = u;

```

```

56         child[node.first].second = node.second;
57     }
58 }
59 }
60 for(int t = b;t != -1;t = child[t].first){
61     //cout<<t<<" "<<child[t].second<<"\n";
62     //minimax=max(minimax,child[t].second);
63     maximini = min(maximini,child[t].second);
64 }
65 return maximini;
66 }

```

8 Teoria de juegos

8.1 Teorema fundamental de los juegos optimos

```

1 boolean isWinning(position pos) {
2     moves[] = possible positions to which I can move from the position
3     pos;
4     for (all x in moves)
5         if (!isWinning(x)) return true;
6
7     return false;
8 }

```

8.2 Como calcular grundy

```

1 int grundyNumber(position pos) {
2     moves[] = possible positions to which I can move from pos
3     set s;
4     for (all x in moves) insert into s grundyNumber(x);
5     //return the smallest non-negative integer not in the set s;
6     int ret=0;
7     while (s.contains(ret)) ret++;
8     return ret;
9 }

```

9 Probabilidad

9.1 Formulas clave

10 Otros/utilitarios

10.1 josephus

```

1 int survivor(int n, int m){
2     int s = 0;
3     for (int i=1;i<=n;++i) s = (s+m)%i;
4     return (s+1);
5 }

```

10.2 josephus k = 2

```

1 ///////////////JAVA
2 /**
3  *
4  * @param n the number of people standing in the circle
5  * @return the safe position who will survive the execution
6  *   f(N) = 2L + 1 where N = 2^M + L and 0 <= L < 2^M
7  */
8 public int getSafePosition(int n) {
9     // find value of L for the equation
10    int valueOfL = n - Integer.highestOneBit(n);
11    int safePosition = 2 * valueOfL + 1;
12    return safePosition;
13 }

```

10.3 poker

10.4 iterar subconjuntos

```

1 for(int sbm=bm; sbm; sbm=(sbm-1)&bm)

```

10.5 como reconstruir una DP (normal)

```

1 /*
2 You just need to revisit your steps in the DP. In case of 0-1 knapsack,
3 lets say the original DP function was solve, and the function
4 reconstruct will give you the actual solution (I'm writing the code
5 in C++):
6 */

```

```

4 int solve(int pos, int capacity){
5     if(pos == no_of_objects) return 0;
6     if(memo[pos][capacity] != -1) return memo[pos][capacity];
7     int r1 = solve(pos + 1, capacity); //dont take
8     int r2 = 0;
9     if(weight[pos] <= capacity){
10        r2 = solve(pos + 1, capacity - weight[pos]) + profit[pos]; //
11        take
12    }
13    return memo[pos][capacity] = max(r1, r2);
14 }
15 void reconstruct(int pos, int capacity){
16     if(pos == no_of_objects) return; //you have completed reconstruction
17     int r1 = memo[pos + 1][capacity]; //dont take
18     int r2 = 0;
19     if(weight[pos] <= capacity)r2 = memo[pos + 1][capacity - weight[pos]
20     ] + profit[pos]; //take
21     if(r1 > r2) {reconstruct(pos + 1, capacity);}
22     else{
23         cout << "Take_object_" << pos << endl;
24         reconstruct(pos + 1, capacity - weight[pos]) + profit[pos];
25     }
26 }
27 After executing reconstruct, it will print all those objects that give
28 you the optimal solution. As you can see, at most no_of_objects
29 calls will be made in the reconstruct function.
30 Similarly, you can reconstruct the solution of any DP greedily.

```

10.6 muajaja con j

```

1 #include <signal.h>
2 void divzero(int p){
3     while(true);}
4 void segm(int p){
5     exit(0);}
6 //in main
7 signal(SIGFPE, divzero);
8 signal(SIGSEGV, segm);

```

Expandir pila

```

1 #include <sys/resource.h>
2 rlimit rl;
3 getrlimit(RLIMIT_STACK, &rl);

```

```

4 | rl.rlim_cur=1024L*1024L*256L;//256mb
5 | setrlimit(RLIMIT_STACK, &rl);

```

10.7 comparar doubles for noobs

```

1 | const double EPS = 1e-9;
2 | x == y <=> fabs(x-y) < EPS
3 | x > y <=> x > y + EPS
4 | x >= y <=> x > y - EPS

```

10.8 infix to postfix

```

1 | //infix to postfix with shunting yard, Halim interpretation
2 | //plus eval function given a postfix return the result of the operation
3 | //format: string like ( x o x ( x o x ) ) o=operation x=value
4 | string s;
5 | bool isOperator(string u){
6 |     return u=="+" || u=="-" || u=="*" || u=="/";
7 | }
8 | bool precede(string u){
9 |     if(u=="*" || u=="/")return true;
10 |    return false;
11 | }
12 | void solve(){
13 |     getline(cin,s);
14 |     stack<string>st;
15 |     vector<string>v;
16 |     stringstream ss;
17 |     ss<<s;
18 |     while(ss>>s){
19 |         if(isOperator(s)){
20 |             while(!st.empty()&&isOperator(st.top())&&precede(st.top())>=
21 |                 precede(s)){
22 |                 v.push_back(st.top());st.pop();
23 |             }
24 |             st.push(s);
25 |         }
26 |         else{
27 |             if(s=="("){
28 |                 st.push(s);
29 |             }
30 |             else{
31 |                 if(s=="){
32 |                     while(!st.empty()&&st.top()!="("){

```

```

32 |                     v.push_back(st.top());st.pop();
33 |                 }
34 |                 if(!st.empty()&&st.top()=="(")st.pop();
35 |             }
36 |         }
37 |         else {
38 |             v.push_back(s);
39 |         }
40 |     }
41 | }
42 | while(!st.empty()){
43 |     v.push_back(st.top());st.pop();
44 | }
45 | stack<double>stans;
46 | double x;
47 | for(string eva:v){
48 |     if(!isOperator(eva)){
49 |         stringstream nu;
50 |         nu<<eva;
51 |         nu>>x;
52 |         stans.push(x);
53 |     }
54 |     else{
55 |         double a=stans.top();stans.pop();
56 |         double b=stans.top();stans.pop();
57 |         if(eva=="*")b*=a;
58 |         if(eva=="/")b/=a;
59 |         if(eva=="+")b+=a;
60 |         if(eva=="-")b-=a;
61 |         stans.push(b);
62 |     }
63 | }
64 | cout<<fixed<<stans.top()<<"\n";
65 | }

```

10.9 numeros romanos

```

1 | #include <bits/stdc++.h>
2 | using namespace std;
3 | map<int,string>cvt;
4 |
5 | string aromano(int n){
6 |     cvt[1000] = "M";cvt[900] = "CM",cvt[500] = "D", cvt[400] = "CD";

```

```

7   cvt[100] = "C";cvt[90] = "XC"; cvt[50] = "L";
8   cvt[40] = "XL";cvt[10] = "X";cvt[9] = "IX";cvt[5] = "V"; cvt[4] = "IV"
9   ;
10  cvt[1] = "I";
11  string ans = "";
12  for(map<int,string>::reverse_iterator it = cvt.rbegin();it != cvt.rend
13    ());it++){
14    while(n >= it->first){
15      ans += it->second;
16      n -= it->first;
17    }
18    return ans;
19  }
20  map<string,int>crn;
21  int anumero(string R){
22    map<char, int> crn;
23    crn['I'] = 1;   crn['V'] = 5;   crn['X'] = 10;   crn['L'] = 50;
24    crn['C'] = 100; crn['D'] = 500; crn['M'] = 1000;
25    int value = 0;
26    for (int i = 0; R[i]; i++)
27      if (i + 1 < R.size() && crn[R[i]] < crn[R[i+1]]) {
28        value += crn[R[i+1]] - crn[R[i]];
29        i++;
30      }
31      else value += crn[R[i]];
32    return value;
33  }

```

10.10 get k-th permutacion

```

1  vector<int>v;
2  //finding the number of permutation 0.....n-1
3  int main()
4  {
5    string s;
6    while(getline(cin,s)){
7      stringstream ss;
8      ss<<s;
9      int pos=0,u;
10     v.clear();
11     while(ss>>u){
12       v.push_back(u-1);
13     }

```

```

14     vector<int>le(v.size(),0);
15     for(int i=0;i<v.size();i++){
16       for(int j=i+1;j<v.size();j++){
17         if(v[i]>v[j])le[i]++;
18       }
19     }
20     long long ans=0LL,fact=0LL,pow=1LL;
21     for(int i=le.size()-1;i>=0;i--){
22       if(fact!=0LL)pow*=fact;
23       fact++;
24       ans=ans+pow*le[i];
25     }
26     cout<<ans+1<<"\n";
27   }
28   return 0;
29 }

```

10.11 sliding window

10.12 permutaciones de un dado

```

1  // izquierda, derecha, arriba, al frente, abajo, atras
2
3  int p[][6] = {
4    {0,1,2,3,4,5},
5    {0,1,3,4,5,2},
6    {0,1,4,5,2,3},
7    {0,1,5,2,3,4},
8    {1,0,2,5,4,3},
9    {1,0,3,2,5,4},
10   {1,0,4,3,2,5},
11   {1,0,5,4,3,2},
12   {2,4,5,1,3,0},
13   {2,4,1,3,0,5},
14   {2,4,3,0,5,1},
15   {2,4,0,5,1,3},
16   {3,5,2,1,4,0},
17   {3,5,1,4,0,2},
18   {3,5,4,0,2,1},
19   {3,5,0,2,1,4},
20   {4,2,5,0,3,1},
21   {4,2,0,3,1,5},
22   {4,2,3,1,5,0},
23   {4,2,1,5,0,3},

```

```
24 | {5,3,2,0,4,1},  
25 | {5,3,0,4,1,2},  
26 | {5,3,4,1,2,0},  
27 | {5,3,1,2,0,4}  
28 | };
```

10.13 ternary search

10.14 liebre y el tortugo

10.15 como usar printf

10.16 java

10.17 python

10.18 template

10.19 file setup

```
1 | //tambien se pueden usar comas: {a, x, m, l}  
2 | touch {a..l}.in; tee {a..l}.cpp < template.cpp
```