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1 algorithm

#include <algorithm> #include <numeric>

Algo	Params	Funcion
sort, stable_sort	f, 1	ordena el intervalo
nth_element	f, nth, l	void ordena el n-esimo, y
		particiona el resto
fill, fill_n	f, l / n, elem	void llena [f, l) o [f,
		f+n) con elem
lower_bound, upper_bound	f, l, elem	it al primer / ultimo donde se
		puede insertar elem para que
		quede ordenada
binary_search	f, l, elem	bool esta elem en [f, l)
copy	f, l, resul	hace $resul+i=f+i \ \forall i$
find, find_if, find_first_of	f, l, elem	it encuentra i \in [f,l) tq. i=elem,
	/ pred / f2, l2	$\operatorname{pred}(i), i \in [f2, l2)$
count, count_if	f, l, elem/pred	cuenta elem, pred(i)
search	f, l, f2, l2	busca $[f2,l2) \in [f,l)$
replace, replace_if	f, l, old	cambia old / pred(i) por new
	/ pred, new	
reverse	f, 1	da vuelta
partition, stable_partition	f, l, pred	pred(i) ad, !pred(i) atras
min_element, max_element	f, l, [comp]	$it \min, \max de [f,l]$
lexicographical_compare	f1,l1,f2,l2	bool con [f1,l1];[f2,l2]
next/prev_permutation	f,l	deja en [f,l) la perm sig, ant
set_intersection,	f1, l1, f2, l2, res	$[res, \ldots)$ la op. de conj
set_difference, set_union,		
set_symmetric_difference,		
push_heap, pop_heap,	f, l, e / e /	mete/saca e en heap [f,l),
make_heap		hace un heap de [f,l)
is_heap	f,l	bool es [f,l) un heap
accumulate	f,l,i,[op]	$T = \sum /\text{oper de [f,l)}$
inner_product	f1, l1, f2, i	$T = i + [f1, 11) \cdot [f2, \dots)$
partial_sum	f, l, r, [op]	$r+i = \sum /oper de [f,f+i] \forall i \in [f,l)$
builtin_ffs	unsigned int	Pos. del primer 1 desde la derecha
builtin_clz	unsigned int	Cant. de ceros desde la izquierda.
_builtin_ctz	unsigned int	Cant. de ceros desde la derecha.
_builtin_popcount	unsigned int	Cant. de 1's en x.
_builtin_parity	unsigned int	1 si x es par, 0 si es impar.
_builtin_XXXXXXII	unsigned ll	= pero para long long's.

2 Estructuras

2.1 RMQ (static)

Dado un arreglo y una operacion asociativa *idempotente*, get(i, j) opera sobre el rango [i, j). Restriccion: LVL \geq ceil(logn); Usar [] para llenar arreglo y luego build().

```
1 struct RMQ{
     #define LVL 10
     tipo vec[LVL] [1<<(LVL+1)];</pre>
     tipo &operator[](int p){return vec[0][p];}
     tipo get(int i, int j) {//intervalo [i,j)
       int p = 31-_builtin_clz(j-i);
6
       return min(vec[p][i],vec[p][j-(1<<p)]);
8
     void build(int n) {//O(nlogn)
9
       int mp = 31-__builtin_clz(n);
10
       forn(p, mp) forn(x, n-(1<<p))
11
         vec[p+1][x] = min(vec[p][x], vec[p][x+(1<<p)]);
12
   }};
13
```

2.2 Segment Tree

2.2.1 Segment Tree Recursivo

```
1 //inclusive segment tree [L,R]
2 int T[4 * N];
   void init(int node = 1,int l = 0,int r = n - 1){
     if(1 == r)T[node] = v[1];
     else{
5
       int mid = (1 + r) >> 1;
6
       init(2 * node,1,mid);
       init(2 * node + 1, mid + 1, r);
       T[node] = op(T[2 * node], T[2 * node + 1]);
9
10
11
   void update(int pos,int val,int node = 1,int l = 0,int r = n - 1){
     if(r < pos || 1 > pos)return;
     if(l == r)T[node] = val;
14
     else{
15
       int mid = (1 + r) >> 1;
16
       update(pos,val,2 * node,1,mid);
17
       update(pos, val, 2 * node + 1, mid + 1, r);
18
19
       T[node] = op(T[2 * node], T[2 * node + 1]);
```

```
20
                                                                                    3
^{21}
   int query(int x,int y,int node = 1,int l = 0,int r = n - 1){
                                                                                      */
                                                                                    4
^{22}
     if(r < x || 1 > y)return NEUTRO;
23
     if(x <= 1 && r <= y)return T[node];</pre>
     else{
25
       int mid = (1 + r) >> 1;
26
       return op(query(x,y,2 * node,1,mid),query(x,y,2 * node + 1,mid + 1,r
27
                                                                                        }
           ));
                                                                                   10
     }
                                                                                   11
28
29
    2.2.2 ST Iterativo - (Consulta en rango, modificacion a posicion)
                                                                                        int res = 0:
                                                                                   14
  //Segment tree iterative [1,r)
                                                                                        return res;
                                                                                   16
  int T[2 * N];
                                                                                   17
   void init(){
     for(int i = n; i < 2 * n; i++)T[i] = val[i];
    for(int i = n - 1; i \ge 1; i--)T[i] = op(T[i << 1], T[i << 1 | 1]);
5
                                                                                      void push() {
6
   int op(int a,int b){
     //an asociative function
     return a + b;
9
                                                                                          t[i] = 0;
                                                                                   24
10
                                                                                        }
                                                                                   25
   void update(int pos,int u){
                                                                                   26 }
     pos += n;
12
     for(pos >= 1; pos >= 1; pos >= 1)T[pos] = op(T[pos << 1],T[pos << 1
13
         | 1]);
14
15
   int query(int 1,int r){
16
     1 += n, r += n;
17
     int ans = NEUTRO;
18
     while(l < r){
                                                                                      tipo v[maxn];
       if(1 \& 1)ans = op(ans,T[1++]);
20
       if (r \& 1) ans = op(ans, T[--r]);
       1 >>= 1,r >>= 1;
22
     }
23
                                                                                   10
     return ans;
                                                                                   11
25 }
    2.2.3 ST Iterativo - (Consulta a posicion, modificacion en rango)
                                                                                   13
                                                                                        int 1, r;
                                                                                   14
1 /*Segment Tree modificar un rango, acceder a una posicion
                                                                                         tipo value;
                                                                                   15
```

```
solo sirve cuando la operacion que realizamos es conmutativa
     por ejemplo la suma, pero no funciona con la asignacion
   //adiciona value al rango [1, r)
   void modify(int 1, int r, int value) {// rango [1, r)
    for (1 += n, r += n; 1 < r; 1 >>= 1, r >>= 1) {
       if (l&1) t[l++] += value;
       if (r&1) t[--r] += value;
   //acceder a la posicion
   int query(int p) {
    for (p += n; p > 0; p >>= 1) res += t[p];
   //Si necesitamos actualizar todo lo podemos hacer en O(n)
   //Y luego acceder a las hojas en O(1)
    for (int i = 1; i < n; ++i) {
     t[i << 1] += t[i];
      t[i<<1|1] += t[i];
                    2.2.4 Segment Tree con Punteros
1 /*La creacion y las queries son [0, n)
   [cerrado, abierto)
   Por alguna razon el destructor hace que se borre todo
   inmediatamente despues de que termina el constructor*/
   const int maxn = 1000000;
   const tipo NEUTRO = PONGA_AQUI_EL_NEUTRO;
   tipo oper(tipo a, tipo b) {
     return min(a, b);
12 | struct segment_tree {
     segment_tree *L, *R;
```

```
segment_tree(): L(nullptr), R(nullptr), value(NEUTRO) {}
                                                                                           for(pos >>= 1; pos >= 1; pos >>= 1)
16
                                                                                    13
                                                                                             T[pos] = T[pos << 1] + T[pos << 1 | 1];
     segment_tree(int _1, int _r) : l(_1), r(_r) {
                                                                                    14
17
       if (1 + 1 == r) {
                                                                                         }
                                                                                    15
18
         value = v[1];
                                                                                         void update(int pos,int value){
19
                                                                                    16
       } else {
                                                                                           pos += n;
                                                                                    17
20
         int mid = (1 + r) >> 1;
                                                                                           T[pos] += value;
21
                                                                                    18
         L = new segment_tree(1, mid);
                                                                                           for(pos >>= 1; pos >= 1; pos >>= 1)
22
                                                                                    19
         R = new segment_tree(mid, r);
                                                                                             T[pos] = T[pos << 1] + T[pos << 1 | 1];
23
                                                                                    20
         value = oper(L->value, R->value);
                                                                                         }
24
                                                                                    21
                                                                                         int query(int 1,int r){
       }
                                                                                    22
25
     }
                                                                                           1 += n; r+= n;
                                                                                    23
26
     //~segment_tree() {delete L; delete R;}//NO PONER!!! ERROR!!!
                                                                                           int ans = 0;
27
                                                                                    24
     void update(int pos, int val) {
                                                                                           while(1 < r){
28
                                                                                    25
                                                                                             if(1 & 1)ans += T[1++];
       if (r \le pos || 1 > pos) return;
29
       if (1 + 1 == r) {
                                                                                             if(r \& 1)ans += T[--r];
30
         v[pos] = value = val;
                                                                                             1 >>= 1, r >>= 1;
31
       } else {
                                                                                           }
32
                                                                                    29
         L->update(pos, val);
                                                                                           return ans;
33
                                                                                    30
         R->update(pos, val);
                                                                                         }
                                                                                    31
34
         value = oper(L->value, R->value);
                                                                                       };
                                                                                    32
35
       }
                                                                                       struct st{
36
                                                                                         int n;
37
     tipo query(int a, int b) {
                                                                                         vector<segmetree>T;
38
                                                                                    35
       if (a <= 1 && r <= b) return value;
                                                                                         st(){}
                                                                                    36
39
       if (1 \ge b \mid | r \le a) return NEUTRO;
                                                                                         st(int _){
                                                                                    37
40
       return oper(L->query(a, b), R->query(a, b));
                                                                                           n = _{:}
                                                                                    38
41
     }
                                                                                           for(int i = 0; i < 2 * n; i++){
^{42}
                                                                                    39
43 | } tree;
                                                                                             T.push_back(segmetree(n));
                                                                                    40
                                                                                           }
                                                                                    41
                           2.2.5 Segment Tree 2D
                                                                                         }
                                                                                    42
                                                                                         void update(int x,int y,int val){
                                                                                    43
                                                                                           x += n:
   typedef long long 11;
                                                                                    44
                                                                                           T[x].update(y,val);
   struct segmetree{
                                                                                    45
                                                                                           segmetree ok;
                                                                                    46
     int n;
3
                                                                                           for(x >>= 1; x >= 1; x >>= 1){
                                                                                    47
     vector<ll>T;
4
                                                                                             T[x].rupdate(y,T[x << 1].query(y,y + 1));
     segmetree(){n = 0;}
5
                                                                                             T[x].update(y,T[x << 1 | 1].query(y,y + 1));
     segmetree(int _){
                                                                                    49
6
                                                                                           }
       n = _{;}
                                                                                    50
       T.resize(2 * n + 1);
                                                                                    51
8
                                                                                         11 query(int 1,int b,int r,int t){
                                                                                    52
9
                                                                                           1 += n:
     void rupdate(int pos,int value){
                                                                                    53
10
                                                                                           r += n;
       pos += n;
                                                                                    54
11
       T[pos] = value;
                                                                                           r++,t++;
                                                                                    55
12
```

```
ll ans = OLL:
                                                                                        shift(id, l, r);
56
       while(1 < r){
                                                                                        int mid = (1+r)/2;
57
         if(l & 1)ans += T[l++].query(b,t);
                                                                                        increase(x, y, v, id * 2, 1, mid);
58
                                                                                        increase(x, y, v, id*2+1, mid, r);
         if(r & 1)ans += T[--r].query(b,t);
                                                                                   34
59
         1 >>= 1, r >>= 1;
                                                                                        s[id] = s[id * 2] + s[id * 2 + 1];
60
       }
61
                                                                                   36
                                                                                      //(We should call increase(l r x))
       return ans;
62
                                                                                      int sum(int x,int y,int id = 1,int l = 0,int r = n){
    }
63
64 };
                                                                                       if(x \ge r \text{ or } 1 \ge y) \text{ return } 0;
                                                                                       if(x \le 1 \&\& r \le y) return s[id];
                     2.2.6 Segment Tree Lazy - Suma
                                                                                       shift(id, l, r);
                                                                                       int mid = (1+r)/2;
                                                                                        return sum(x, y, id * 2, 1, mid) +
1 //Todo es [1, r)
   void build(int id = 1,int l = 0,int r = n){
                                                                                                sum(x, y, id * 2 + 1, mid, r);
                                                                                   44
                                                                                   45 }
     if(r - 1 < 2) \{ // 1 + 1 == r \}
       s[id] = a[1];
4
                                                                                                        2.2.7 Segment Tree Lazy - Pintar
       return ;
5
6
     int mid = (1+r)/2;
                                                                                    void shift(int id){
     build(id * 2, 1, mid);
                                                                                        if(lazv[id])
     build(id * 2 + 1, mid, r);
                                                                                          lazy[2 * is] = lazy[2 * id + 1] = lazy[id];
     s[id] = s[id * 2] + s[id * 2 + 1];
                                                                                        lazy[id] = 0;
                                                                                      }
                                                                                    5
11
   //agui poner los arrays lazy and id
                                                                                      //color > 1, por que se usa el 0 para decir que no hay lazy
   void upd(int id,int 1,int r,int x){// increase all members in this
                                                                                      void upd(int x,int y,int color, int id = 0,int 1 = 0,int r = n)\{//
       interval by x
                                                                                          painting the interval [x,y) whith color "color"
     lazy[id] += x;
                                                                                        if(x \ge r \text{ or } 1 \ge y) \text{ return };
     s[id] += (r - 1) * x;
                                                                                        if(x \le 1 \&\& r \le y){
15
                                                                                          lazy[id] = color;
                                                                                   10
16
   //A function to pass the update information to its children :
                                                                                          return ;
17
                                                                                   11
   void shift(int id,int l,int r){//pass update information to the children
                                                                                        }
                                                                                   12
     int mid = (1+r)/2;
                                                                                   13
                                                                                        int mid = (1+r)/2;
19
     upd(id * 2, 1, mid, lazy[id]);
                                                                                        shift(id);
                                                                                   14
20
     upd(id * 2 + 1, mid, r, lazy[id]);
                                                                                        upd(x, y, color, 2 * id, 1, mid);
                                                                                   15
21
     lazv[id] = 0;// passing is done
                                                                                        upd(x, y, color, 2*id+1, mid, r);
22
                                                                                   16
                                                                                      }
                                                                                   17
23
    //A function to perform increase gueries :
                                                                                   18
24
   void increase(int x,int y,int v,int id = 1,int l = 0,int r = n){
                                                                                      set <int> se:
     if(x \ge r \text{ or } 1 \ge y) \text{ return };
                                                                                      void cnt(int id = 1,int l = 0,int r = n){
26
     if(x \le 1 \&\& r \le y){
                                                                                        if(lazy[id]){
                                                                                   21
27
       upd(id, 1, r, v);
                                                                                          se.insert(lazy[id]);
                                                                                   22
28
                                                                                          return : // there is no need to see the children, because all the
       return ;
                                                                                   23
29
     }
                                                                                               interval is from the same color
30
```

```
3 | void init(int n) {
24
     if(r - 1 < 2) return ;
                                                                                      tree = vector<tipo>(n, 0);
25
     int mid = (1+r)/2;
                                                                                      maxn = n;
26
     cnt(2 * id, 1, mid);
                                                                                    }
                                                                                  6
27
     cnt(2*id+1, mid, r);
                                                                                    void add(int i, tipo k) { //i valid [1, n)
28
                                                                                      for(; i < maxn; i += i&-i ) tree[i] += k;</pre>
29
                                                                                    }
                                                                                  9
                      2.2.8 Segment Tree Persistente
                                                                                 10
                                                                                    tipo get(int i){//returns sum [1, i]
int segcnt = 0;
                                                                                     tipo s = 0;
  struct segment {
2
                                                                                     for(; i > 0; i-=i&-i) s+=tree[i];
       int 1, r, lid, rid, sum;
                                                                                      return s;
   } segs[2000000];
                                                                                 15 }
   int build(int 1, int r) {
       if (1 > r) return -1;
                                                                                                            2.3.1 Fenwick Tree 2D
       int id = segcnt++;
7
       segs[id].l = 1;
8
       segs[id].r = r;
                                                                                    11 T[1025] [1025];
9
       if (1 == r) segs[id].lid = -1, segs[id].rid = -1;
                                                                                    int n;
10
       else {
11
                                                                                    11 query(int x, int y)
           int m = (1 + r) / 2;
12
           segs[id].lid = build(l , m);
                                                                                  6
13
           segs[id].rid = build(m + 1, r); }
                                                                                      11 \text{ res} = 0;
                                                                                  7
14
       segs[id].sum = 0;
                                                                                      for(int i = x; i \ge 0; i = (i & (i+1)) - 1)
15
       return id; }
                                                                                            for(int j = y; j \ge 0; j = (j & (j+1)) - 1)
16
                                                                                 9
   int update(int idx, int v, int id) {
                                                                                                 res += T[i][i];
                                                                                 10
17
       if (id == -1) return -1;
                                                                                        return res;
                                                                                 11
18
       if (idx < segs[id].l || idx > segs[id].r) return id;
                                                                                    }
                                                                                 12
19
       int nid = segcnt++;
                                                                                 13
20
       segs[nid].l = segs[id].l;
                                                                                    void update(int x, int y, int val)
21
       segs[nid].r = segs[id].r;
22
                                                                                 15
                                                                                      for(int i = x; i < n; i = (i | (i+1)))
       segs[nid].lid = update(idx, v, segs[id].lid);
                                                                                 16
23
                                                                                            for(int j = y; j < n; j = (j | (j+1)))
       segs[nid].rid = update(idx, v, segs[id].rid);
                                                                                 17
24
       segs[nid].sum = segs[id].sum + v;
                                                                                                 T[i][j] += val;
                                                                                 18
25
       return nid: }
                                                                                 19 }
26
   int query(int id, int 1, int r) {
27
                                                                                                        2.4 Union Find con rank
       if (r < segs[id].1 || segs[id].r < 1) return 0;</pre>
28
       if (1 <= segs[id].l && segs[id].r <= r) return segs[id].sum;</pre>
29
                                                                                  1 /*======== <Union find rangos> ==========
       return query(segs[id].lid, 1, r) + query(segs[id].rid, 1, r); }
30
                                                                                  2 Complexity: O(N)
                           2.3 Fenwick Tree
                                                                                  3 index 0 to n - 1 warning
                                                                                    Complexity O(N)
                                                                                    */
vector<tipo> tree;
                                                                                  5
2 | int maxn;
                                                                                    #define MAX INSERTE_VALOR_AQUI
```

```
7 int padre[MAX];
   int rango[MAX];
   void MakeSet(int n){
       for (int i = 0; i < n; ++i) {
           padre[i] = i; rango[i] = 0; }
11
12
   int Find(int x) {
13
       if(x == padre[x])
14
           return x;
15
       return padre[x] = Find(padre[x]);
16
17
   void UnionbyRank(int x , int y){
18
       int xRoot = Find(x):
19
       int yRoot = Find(y);
20
       //el padre de ambas componentes sera el de mayor altura
21
       if(rango[xRoot] > rango[yRoot])//X tiene mas altura que Y
22
           padre[yRoot] = xRoot;
23
       }else{//Y} >= X
24
           padre[xRoot] = yRoot;
25
           if(rango[xRoot] == rango[yRoot])//si poseen la misma altura
26
               rango[yRoot]++;//incremento el rango de la nueva raiz
27
       }
28
29 }
```

2.5 BigInteger C++

```
1 // g++ -std=c++11 "bigint.cpp" -o run
  /***
2
   Contain a useful big int, overload all operators, including cin, cout,
  comparator, build via string (prefer this metod) or long long, for now
      this not have a
  to_string method
  Problem for practice: UVA 494
  */
8
  // base and base_digits must be consistent
  const int base = 1000000000;
  const int base_digits = 9;
11
12
  struct bigint {
13
      vector<int> a;
14
      int sign;
15
16
```

```
bigint():
17
           sign(1) {
18
       }
19
20
       bigint(long long v) {
21
            *this = v;
22
       }
23
24
       bigint(const string &s) {
25
           read(s);
26
       }
27
28
       void operator=(const bigint &v) {
29
           sign = v.sign;
30
           a = v.a;
31
       }
32
33
       void operator=(long long v) {
34
           sign = 1;
35
           if (v < 0)
                sign = -1, v = -v;
37
           for (; v > 0; v = v / base)
                a.push_back(v % base);
39
       }
40
41
       bigint operator+(const bigint &v) const {
42
           if (sign == v.sign) {
43
                bigint res = v;
44
45
                for (int i = 0, carry = 0; i < (int) max(a.size(), v.a.size
46
                    ()) || carry; ++i) {
                    if (i == (int) res.a.size())
47
                        res.a.push_back(0);
48
                    res.a[i] += carry + (i < (int) a.size() ? a[i] : 0);
49
                    carry = res.a[i] >= base;
50
                    if (carry)
51
                        res.a[i] -= base;
52
                }
53
54
                return res;
55
           return *this - (-v);
56
57
58
```

```
bigint operator-(const bigint &v) const {
                                                                                                int norm = base / (b1.a.back() + 1);
59
                                                                                    98
           if (sign == v.sign) {
                                                                                                bigint a = a1.abs() * norm;
                                                                                    99
60
                if (abs() >= v.abs()) {
                                                                                                bigint b = b1.abs() * norm;
                                                                                    100
61
                    bigint res = *this;
                                                                                                bigint q, r;
                                                                                    101
62
                    for (int i = 0, carry = 0; i < (int) v.a.size() || carry</pre>
                                                                                                q.a.resize(a.a.size());
                                                                                    102
63
                        ; ++i) {
                                                                                    103
                                                                                                for (int i = a.a.size() - 1; i >= 0; i--) {
                        res.a[i] -= carry + (i < (int) v.a.size() ? v.a[i] :
                                                                                    104
64
                                                                                                    r *= base:
                                                                                    105
                        carry = res.a[i] < 0;</pre>
                                                                                                    r += a.a[i]:
                                                                                    106
65
                        if (carry)
                                                                                                    int s1 = r.a.size() \le b.a.size() ? 0 : r.a[b.a.size()];
                                                                                    107
66
                            res.a[i] += base;
                                                                                                    int s2 = r.a.size() \le b.a.size() - 1 ? 0 : r.a[b.a.size() -
67
                                                                                    108
68
                    res.trim():
                                                                                                    int d = ((long long) base * s1 + s2) / b.a.back();
69
                                                                                    109
                    return res:
                                                                                                    r -= b * d:
                                                                                    110
70
                }
                                                                                                    while (r < 0)
                                                                                    111
71
                return -(v - *this);
                                                                                                        r += b, --d;
                                                                                    112
72
           }
                                                                                                    q.a[i] = d;
73
                                                                                    113
           return *this + (-v);
                                                                                                }
                                                                                    114
74
       }
                                                                                    115
75
                                                                                                q.sign = a1.sign * b1.sign;
                                                                                    116
76
       void operator*=(int v) {
                                                                                                r.sign = a1.sign;
                                                                                    117
77
           if (v < 0)
                                                                                                q.trim();
                                                                                    118
78
                sign = -sign, v = -v;
                                                                                                r.trim();
                                                                                    119
79
           for (int i = 0, carry = 0; i < (int) a.size() || carry; ++i) {
                                                                                                return make_pair(q, r / norm);
                                                                                    120
80
                if (i == (int) a.size())
                                                                                            }
                                                                                    121
81
                    a.push_back(0);
                                                                                    122
82
               long long cur = a[i] * (long long) v + carry;
                                                                                    123
                                                                                            bigint operator/(const bigint &v) const {
83
                carry = (int) (cur / base);
                                                                                                return divmod(*this, v).first;
                                                                                    124
84
                a[i] = (int) (cur % base);
                                                                                            }
                                                                                    125
85
                //asm("divl %%ecx" : "=a"(carry), "=d"(a[i]) : "A"(cur), "c
                                                                                    126
86
                    "(base)):
                                                                                            bigint operator%(const bigint &v) const {
                                                                                    127
           }
                                                                                                return divmod(*this, v).second;
                                                                                    128
87
                                                                                            }
           trim();
88
                                                                                    129
       }
                                                                                    130
89
                                                                                            void operator/=(int v) {
                                                                                    131
90
       bigint operator*(int v) const {
                                                                                                if (v < 0)
                                                                                    132
91
           bigint res = *this;
                                                                                                    sign = -sign, v = -v;
                                                                                    133
92
                                                                                                for (int i = (int) \ a.size() - 1, rem = 0; i \ge 0; --i) {
           res *= v;
93
                                                                                    134
                                                                                                    long long cur = a[i] + rem * (long long) base;
           return res;
                                                                                    135
94
                                                                                                    a[i] = (int) (cur / v);
       }
                                                                                    136
95
                                                                                                    rem = (int) (cur % v);
                                                                                    137
96
       friend pair bigint, bigint divmod(const bigint &a1, const bigint &
                                                                                    138
97
           b1) {
                                                                                                trim();
                                                                                   139
```

```
}
                                                                                                }
140
                                                                                        183
                                                                                                bool operator<=(const bigint &v) const {</pre>
                                                                                       184
141
        bigint operator/(int v) const {
                                                                                                    return !(v < *this);</pre>
                                                                                       185
142
            bigint res = *this;
143
                                                                                        186
            res /= v;
                                                                                                bool operator>=(const bigint &v) const {
                                                                                       187
144
            return res;
                                                                                                    return !(*this < v);
145
                                                                                       188
                                                                                                }
        }
146
                                                                                       189
                                                                                                bool operator==(const bigint &v) const {
                                                                                       190
147
                                                                                                    return !(*this < v) && !(v < *this);
        int operator%(int v) const {
148
                                                                                       191
            if (v < 0)
                                                                                                }
                                                                                        192
149
                                                                                                bool operator!=(const bigint &v) const {
                 v = -v:
150
                                                                                       193
                                                                                                    return *this < v || v < *this;
            int m = 0:
151
                                                                                       194
            for (int i = a.size() - 1; i >= 0; --i)
                                                                                                }
152
                                                                                       195
                 m = (a[i] + m * (long long) base) % v;
                                                                                        196
153
            return m * sign;
                                                                                                void trim() {
                                                                                       197
154
        }
                                                                                                    while (!a.empty() && !a.back())
155
                                                                                                         a.pop_back();
156
                                                                                       199
                                                                                                    if (a.empty())
        void operator+=(const bigint &v) {
157
             *this = *this + v;
                                                                                                         sign = 1;
                                                                                       201
158
        }
                                                                                                }
                                                                                        202
159
        void operator-=(const bigint &v) {
                                                                                       203
160
            *this = *this - v;
                                                                                                bool isZero() const {
161
                                                                                       204
                                                                                                    return a.empty() || (a.size() == 1 && !a[0]);
        }
                                                                                       205
162
        void operator*=(const bigint &v) {
                                                                                                }
                                                                                       206
163
            *this = *this * v;
                                                                                       207
164
        }
                                                                                                bigint operator-() const {
                                                                                       208
165
        void operator/=(const bigint &v) {
                                                                                                    bigint res = *this;
                                                                                       209
166
             *this = *this / v;
                                                                                                    res.sign = -sign;
                                                                                       210
167
        }
                                                                                                    return res;
                                                                                       211
168
                                                                                                }
                                                                                       212
169
        bool operator<(const bigint &v) const {</pre>
                                                                                       213
170
            if (sign != v.sign)
                                                                                                bigint abs() const {
                                                                                       214
171
                 return sign < v.sign;</pre>
                                                                                                    bigint res = *this;
172
                                                                                       215
            if (a.size() != v.a.size())
                                                                                                    res.sign *= res.sign;
                                                                                       216
173
                return a.size() * sign < v.a.size() * v.sign;</pre>
                                                                                                    return res;
                                                                                       217
174
            for (int i = a.size() - 1; i >= 0; i--)
                                                                                                }
                                                                                       218
175
                 if (a[i] != v.a[i])
                                                                                       219
176
                     return a[i] * sign < v.a[i] * sign;</pre>
                                                                                                long longValue() const {
                                                                                       220
177
            return false;
                                                                                                    long long res = 0;
                                                                                       221
178
        }
                                                                                                    for (int i = a.size() - 1; i >= 0; i--)
                                                                                       222
179
                                                                                                         res = res * base + a[i];
                                                                                       223
180
        bool operator>(const bigint &v) const {
                                                                                                    return res * sign;
181
                                                                                       ^{224}
                                                                                                }
            return v < *this;
182
                                                                                       ^{225}
```

```
static vector<int> convert_base(const vector<int> &a, int old_digits
226
                                                                                     268
        friend bigint gcd(const bigint &a, const bigint &b) {
                                                                                                  , int new_digits) {
227
            return b.isZero() ? a : gcd(b, a % b);
                                                                                                  vector<long long> p(max(old_digits, new_digits) + 1);
228
                                                                                      269
        }
                                                                                                  p[0] = 1;
229
                                                                                      270
        friend bigint lcm(const bigint &a, const bigint &b) {
                                                                                                  for (int i = 1; i < (int) p.size(); i++)
                                                                                     271
230
            return a / gcd(a, b) * b;
                                                                                                      p[i] = p[i - 1] * 10;
                                                                                      272
231
        }
                                                                                                  vector<int> res;
232
                                                                                      273
                                                                                                  long long cur = 0;
233
                                                                                      274
        void read(const string &s) {
                                                                                                  int cur_digits = 0;
234
                                                                                      275
                                                                                                  for (int i = 0; i < (int) a.size(); i++) {
            sign = 1;
235
                                                                                                      cur += a[i] * p[cur_digits];
            a.clear();
236
                                                                                     277
            int pos = 0;
                                                                                                      cur_digits += old_digits;
237
                                                                                     278
            while (pos < (int) s.size() && (s[pos] == '-' || s[pos] == '+'))
                                                                                                      while (cur_digits >= new_digits) {
                                                                                     279
238
                 {
                                                                                                           res.push_back(int(cur % p[new_digits]));
                if (s[pos] == '-')
                                                                                                           cur /= p[new_digits];
                                                                                      281
239
                                                                                                           cur_digits -= new_digits;
                     sign = -sign;
240
                                                                                                      }
241
                ++pos;
                                                                                      283
                                                                                                  }
242
                                                                                      284
            for (int i = s.size() - 1; i >= pos; i -= base_digits) {
                                                                                                  res.push_back((int) cur);
                                                                                      285
243
                int x = 0;
                                                                                                  while (!res.empty() && !res.back())
                                                                                      286
244
                for (int j = max(pos, i - base_digits + 1); j <= i; j++)
                                                                                                      res.pop_back();
                                                                                      287
245
                     x = x * 10 + s[i] - '0';
                                                                                                  return res;
246
                                                                                      288
                                                                                              }
                a.push_back(x);
                                                                                     289
247
                                                                                      290
248
            trim();
                                                                                              typedef vector<long long> vll;
                                                                                     291
249
        }
                                                                                      292
250
                                                                                              static vll karatsubaMultiply(const vll &a, const vll &b) {
                                                                                     293
251
        friend istream& operator>>(istream &stream, bigint &v) {
                                                                                                  int n = a.size();
                                                                                      294
252
                                                                                                  vll res(n + n);
            string s;
                                                                                     295
253
            stream >> s;
                                                                                                  if (n <= 32) {
                                                                                      296
254
            v.read(s);
                                                                                                      for (int i = 0; i < n; i++)
255
                                                                                     297
                                                                                                           for (int j = 0; j < n; j++)
            return stream;
256
                                                                                      298
        }
                                                                                                               res[i + j] += a[i] * b[j];
                                                                                     299
257
                                                                                                      return res:
                                                                                      300
258
        friend ostream& operator<<(ostream &stream, const bigint &v) {</pre>
                                                                                                  }
                                                                                     301
259
            if (v.sign == -1)
                                                                                      302
260
                stream << '-';
                                                                                                  int k = n \gg 1;
261
                                                                                      303
            stream << (v.a.empty() ? 0 : v.a.back());
                                                                                                  vll a1(a.begin(), a.begin() + k);
                                                                                      304
262
            for (int i = (int) \ v.a.size() - 2; i >= 0; --i)
                                                                                                  vll a2(a.begin() + k, a.end());
                                                                                      305
263
                 stream << setw(base_digits) << setfill('0') << v.a[i];</pre>
                                                                                                  vll b1(b.begin(), b.begin() + k);
                                                                                      306
264
                                                                                                  vll b2(b.begin() + k, b.end());
            return stream;
265
                                                                                     307
        }
266
                                                                                      308
                                                                                                  vll a1b1 = karatsubaMultiply(a1, b1);
267
                                                                                     309
```

```
vll a2b2 = karatsubaMultiply(a2, b2);
310
311
            for (int i = 0; i < k; i++)
312
                 a2[i] += a1[i];
313
            for (int i = 0; i < k; i++)
314
                 b2[i] += b1[i];
315
316
            vll r = karatsubaMultiply(a2, b2);
317
            for (int i = 0; i < (int) a1b1.size(); i++)</pre>
318
                 r[i] = a1b1[i];
319
            for (int i = 0; i < (int) a2b2.size(); i++)</pre>
320
                 r[i] = a2b2[i];
321
322
            for (int i = 0; i < (int) r.size(); i++)
323
                 res[i + k] += r[i];
324
            for (int i = 0; i < (int) a1b1.size(); i++)</pre>
325
                 res[i] += a1b1[i];
326
            for (int i = 0; i < (int) a2b2.size(); i++)</pre>
327
                 res[i + n] += a2b2[i]:
328
            return res;
329
        }
330
331
        bigint operator*(const bigint &v) const {
332
            vector<int> a6 = convert_base(this->a, base_digits, 6);
333
            vector<int> b6 = convert_base(v.a, base_digits, 6);
334
            vll a(a6.begin(), a6.end());
335
            vll b(b6.begin(), b6.end());
336
            while (a.size() < b.size())</pre>
337
                 a.push_back(0);
338
            while (b.size() < a.size())</pre>
339
                 b.push_back(0);
340
            while (a.size() & (a.size() - 1))
341
                 a.push_back(0), b.push_back(0);
342
            vll c = karatsubaMultiply(a, b);
343
            bigint res;
344
            res.sign = sign * v.sign;
345
            for (int i = 0, carry = 0; i < (int) c.size(); i++) {
346
                 long long cur = c[i] + carry;
347
                res.a.push_back((int) (cur % 1000000));
348
                 carry = (int) (cur / 1000000);
349
350
            res.a = convert_base(res.a, 6, base_digits);
351
            res.trim();
352
```

```
353
          return res;
354
   };
355
356
   int main() {
357
       bigint a=0;
358
       359
       bigint b;
       bigint n;
       while(cin >> n) {
363
          if(n==0){break;}
364
          a += n:
365
       }
366
       cout<<a<<endl;</pre>
367
368 | }
                               UnorderedSet
                         2.6
 1 //Compilar: g++ --std=c++11
   struct Hash{
     size_t operator()(const ii &a)const{
       size_t s=hash<int>()(a.fst);
 4
      return hash<int>()(a.snd)+0x9e3779b9+(s<<6)+(s>>2);
 5
    }
 6
    size_t operator()(const vector<int> &v)const{
      size_t s=0;
8
      for(auto &e : v)
9
        s = hash < int > ()(e) + 0x9e3779b9 + (s < < 6) + (s > > 2);
      return s;
11
    }
12
   };
13
   unordered_set<ii, Hash> s;
unordered_map<ii, int, Hash> m;//map<key, value, hasher>
                               Ordered Set
1 /*
   A brief explanation about use of a powerful library: orderd_set
    Reference link: http://codeforces.com/blog/entry/11080
    and a hash for the type pair
4
5
   #include <ext/pb_ds/assoc_container.hpp>
  #include <ext/pb_ds/tree_policy.hpp>
```

```
8 using namespace __gnu_pbds;
9 /*typedef tree<int,null_type,less<int>,rb_tree_tag,
       tree_order_statistics_node_update> ordered_set;
10 If we want to get map but not the set, as the second argument type must
       be used mapped type. Apparently, the tree supports the same
       operations as the set (at least I haven't any problems with them
       before), but also there are two new features - it is find_by_order
       () and order_of_key().
11 The first returns an iterator to the k-th largest element (counting from
        zero), the second - the number of items
   in a set that are strictly smaller than our item. Example of use:*/
   template <typename T>
   using ordered_set = tree<T, null_type, less<T>, rb_tree_tag,
       tree_order_statistics_node_update>;
   int main(){
     ordered_set<int> s;
16
     s.insert(1);
17
     s.insert(3);
18
     cout << *s.find_by_order(0) << endl; // print the 0-th smallest number</pre>
19
          in s(0-based)
     cout << s.order_of_key(2) << endl; // the number of elements in the s</pre>
20
         less than 2
     //find_by_order(i) devuelve iterador al i-esimo elemento
21
     //order_of_key(k): devuelve la pos del lower bound de k
22
     //Ej: 12, 100, 505, 1000, 10000.
23
    //order_of_key(10) == 0, order_of_key(100) == 1,
    //order_of_key(707) == 3, order_of_key(9999999) == 5
25
     return 0;
26
27 }
```

Treap Modo Set

```
struct treap {
     typedef struct _node {
2
       int x, y, cnt;
3
       _node *1, *r;
       _{\text{node}}(\text{int }_{x}): x(_{x}), y((\text{rand}() << 16) ^ rand()), cnt(1), l(nullptr)
5
            ), r(nullptr) {}
       ~_node() {delete 1; delete r;}
       void recalc() {
          cnt = 1:
8
          if (1) cnt += 1->cnt;
9
          if (r) cnt += r->cnt;
10
```

```
}
11
     } *node;
12
     treap(): root(nullptr) {}
13
     ~treap() {delete root;}
14
     node root;
15
     /*Divide el arbol que tiene como raiz a "t", guarda en
16
       L todos los nodos con key menor o igual a "x"
17
       R todos los nodos con key mayor estricto a x
18
       t es destruido/modificado
19
      */
20
     void split(node t, int x, node &L, node &R) {
21
       if (t == nullptr) {L = R = nullptr; return;}
22
       if (t->x <= x) {
23
         split(t->r, x, t->r, R);
24
         L = t:
25
       } else {
         split(t->1, x, L, t->1);
         R = t;
       }
29
       t->recalc();
30
     }
31
     /*Une los dos nodos L y R en un solo arbol y los devuelve.
       L y R son modificados
33
      */
34
     node merge(node L, node R) {
35
       if (L == nullptr) return R;
36
       if (R == nullptr) return L;
37
       if (L->y > R->y) {
        L->r = merge(L->r, R);
         L->recalc();
         return L;
41
       } else {
         R->1 = merge(L, R->1);
         R->recalc():
         return R:
       }
46
47
     /*Inserta un solo nodo con key igual a "x"*/
     void insert(int x) {
49
       //verificar que no se inserten elementos repetidos
       //pueden ocasionar que ya no cumplan la propiedad de BST
       //pueden haber keys iguales a izquierda y derecha
52
       node L, R;
53
```

```
split(root, x, L, R);
                                                                                             /*Numero de elementos con keys menores a "x"*/
54
                                                                                       97
       root = merge(merge(L, new _node(x)), R);
                                                                                             int less(int x) {
                                                                                       98
55
                                                                                               node cur = root;
                                                                                       99
56
     /*Borra todos los nodos con key igual a "x"
                                                                                               int ans = 0;
57
                                                                                       100
       No pasa nada si no hay nodos con key igual a "x"*/
                                                                                               while (cur != nullptr) {
                                                                                       101
58
     void erase(int x) {
                                                                                                 if (cur->x >= x) {
59
                                                                                       102
       node L, m, R;
                                                                                                   cur = cur->l;
                                                                                       103
60
       split(root, x, L, R);
                                                                                                 } else {
61
                                                                                       104
       split(L, x - 1, L, m);
                                                                                                   ans += cnt(cur->1) + 1;
62
                                                                                       105
       root = merge(L, R);
                                                                                                   cur = cur -> r;
63
                                                                                                 }
64
                                                                                       107
     int count(int x) {
                                                                                               }
65
                                                                                       108
       node L. m. R:
                                                                                               return ans;
                                                                                       109
       split(root, x, L, R);
                                                                                      110
67
       split(L, x - 1, L, m);
                                                                                            int cnt(node t) const {
                                                                                      111
68
       int ans = cnt(m);
                                                                                               return t ? t->cnt : 0;
69
       root = merge(merge(L, m), R);
                                                                                            }
70
                                                                                      113
                                                                                            int size() const {
       return ans;
71
                                                                                               return cnt(root):
                                                                                      115
72
     /*Borra un nodo con key igual a "x"
                                                                                       116
73
       No sucede nada si no hay nodo con ese key*/
                                                                                           /*//from e-maxx.ru son mas rapidos(no x mucho) pero menos entendibles
74
                                                                                           //solo borra un elemento
     void erase_one(int x) {
75
                                                                                            void erase(node &t, int x) {
       node L, m, R;
76
                                                                                              if (t\rightarrow x == x)
       split(root, x, L, R);
77
       split(L, x - 1, L, m);
                                                                                               t = merge(t->1, t->r);
                                                                                      121
78
       if (m)
                                                                                               else
                                                                                      122
79
         m = merge(m->1, m->r);
                                                                                                 erase(x < t->x?t->1:t->r, x);
                                                                                       123
80
       root = merge(merge(L, m), R);
                                                                                              if (t)
                                                                                       124
81
                                                                                                 t->recalc();
                                                                                      125
82
     /*k-esimo indexado desde 0
                                                                                            }
                                                                                      126
83
         devuelve INT_MAX si no hay k-esimo*/
                                                                                             void erase_one(int x) {erase(root, x);}
                                                                                      127
84
     int kthElement(int k) {
                                                                                             void insert(node &t, node it) {
                                                                                       128
85
                                                                                              if (t == nullptr)
       node cur = root:
                                                                                      129
86
       while (cur != nullptr) {
                                                                                               t = it:
                                                                                       130
87
          int sizeLeft = cnt(cur->1);
                                                                                               else if (it->y > t->y)
                                                                                      131
88
          if (sizeLeft == k)
                                                                                                 split(t, it\rightarrow x, it\rightarrow l, it\rightarrow r), t = it;
                                                                                       132
89
           return cur->x;
                                                                                      133
90
          cur = sizeLeft > k ? cur->l : cur->r:
                                                                                                 insert(it\rightarrow x < t\rightarrow x? t\rightarrow 1: t\rightarrow r, it);
                                                                                       134
91
          if (sizeLeft < k)</pre>
                                                                                               t->recalc();
                                                                                      135
92
            k = (sizeLeft + 1);
                                                                                      136
93
                                                                                            void insert(int x) {insert(root, new _node(x));}*/
       }
                                                                                      137
94
       return INT_MAX;
                                                                                       138 };
95
96
```

2.9 Treap Implicito(Rope)

```
1 struct rope {
     typedef struct _node {
2
       int value, y, cnt;
       _node *1, *r;
       _node(int _value) : value(_value), y((rand() << 16) ^ rand()), cnt</pre>
           (1), l(nullptr), r(nullptr) {}
       ~_node() {delete 1; delete r;}
       void recalc() {
         cnt = 1;
         if (1) cnt += 1->cnt;
         if (r) cnt += r->cnt;
       }
11
     } *node;
12
     rope(): root(nullptr) {}
13
     ~rope() {delete root;}
14
     node root;
15
     /*Divide el arbol que tiene como raiz a "t", guarda en
      L los primeros "x" elementos del array
      R el primer elemento de R es el elemento en posicion x(indexado desde
18
           0) del array
      t es destruido/modificado
19
      L = [0, x)
20
      R = [x, n) */
21
     void split(node t, int x, node &L, node &R) {
22
       if (t == nullptr) {L = R = nullptr; return;}
23
       int curIndex = cnt(t->1) + 1;
24
       if (curIndex <= x) {</pre>
25
         split(t->r, x - curIndex, t->r, R);
26
         L = t;
27
       } else {
28
         split(t->1, x, L, t->1);
29
         R = t;
30
       }
31
       t->recalc();
32
33
     /* Une los dos nodos L y R en un solo arbol y los devuelve.
34
        L y R son modificados */
35
     node merge(node L, node R) {
36
       if (L == nullptr) return R;
37
       if (R == nullptr) return L;
38
       if (L->y > R->y) {
39
```

```
L->r = merge(L->r, R);
40
         L->recalc();
41
         return L;
42
       } else {
         R->1 = merge(L, R->1);
44
         R->recalc();
         return R;
46
47
     }
48
     /*Inserta "value" en la posicion "pos"(indexado desde 0) recorre todos
          los elementos a la derecha desde la posicion pos*/
     void insert(int pos, int value) {
50
       node L, R;
       split(root, pos, L, R);//en R esta pos
       root = merge(merge(L, new _node(value)), R);
53
     /*Borra el elemento en posicion pos*/
55
     void erase(int pos) {
       node L, m, R;
57
       split(root, pos, L, R);
       split(R, 1, m, R);
59
       root = merge(L, R);
60
61
     int cnt(node t) const {
62
       return t ? t->cnt : 0;
63
    }
64
     int size() const {
65
       return cnt(root);
66
    }
67
68
69 int main() {srand(time(nullptr));return 0;}
                    2.10 Treap - Toby and Stones
const int PAINT = 0, FLIP = 1, REVERSE = 2;
  struct rope {
     typedef struct _node {
       int value, y, cnt;
4
       int negros;
5
       bool rev;
6
       bool lazy_flip;
7
       int lazy_pintar;
8
       _node *1, *r;
```

```
_node(int _value) : value(_value), y((rand() << 16) ^ rand()), cnt</pre>
                                                                                          }
10
                                                                                   51
           (1), l(nullptr), r(nullptr) {
                                                                                          string to_string() {
                                                                                   52
         negros = _value;
                                                                                   53
                                                                                             stringstream ss;
11
         rev = false;
                                                                                             ss << "value=" << value << ",_negros=" << negros << ",_cnt="<< cnt
12
                                                                                   54
                                                                                                  << "("<<rev<< "," << lazy_pintar<<","<< lazy_flip << ")";</pre>
         lazy_flip = false;
13
         lazy_pintar = -1;
                                                                                            return ss.str();
14
                                                                                   55
                                                                                          }
15
                                                                                   56
                                                                                        } *node;
        ~_node() {delete l; delete r;}
                                                                                   57
16
       void recalc() {
                                                                                         rope(): root(nullptr) {}
17
                                                                                         ~rope() {delete root;}
         cnt = 1;
18
                                                                                        node root;
         negros = value;
19
                                                                                   60
                                                                                        void push(node &t) {
         if (1) cnt += 1->cnt, negros += 1->negros;
20
                                                                                   61
                                                                                          if (t == nullptr) return;
         if (r) cnt += r->cnt, negros += r->negros;
21
                                                                                   62
       }
                                                                                          bool op1 = ((t->lazy_pintar) != -1);
                                                                                   63
22
       void push_lazy(int type, int param = -1) {
                                                                                          bool op2 = ((t->rev) || (t->lazy_flip));
23
                                                                                   64
         if (type == PAINT) {
                                                                                          //solo puede pasar uno de los 2 casos, o ninguno esta activado o
24
                                                                                   65
           rev = false;
                                                                                               solo uno de los dos
25
                                                                                          assert((!op1 and !op2) or (op1 xor op2));
           lazy_flip = false;
26
           lazy_pintar = param;
                                                                                          if (op1) {
                                                                                   67
27
           negros = param * cnt;
                                                                                            t->value = t->lazy_pintar;
28
                                                                                            if (t->1) t->1->push_lazy(PAINT, t->lazy_pintar);
                                                                                   69
29
         if (type == FLIP) {
                                                                                             if (t->r) t->r->push_lazy(PAINT, t->lazy_pintar);
30
                                                                                   70
                                                                                             t->lazy_pintar = -1;
           if (lazy_pintar != -1) {
31
                                                                                   71
             assert(rev == false && lazy_flip == false);
                                                                                   72
32
             lazy_pintar = (1 - lazy_pintar);
                                                                                           if (op2) {//no importa el orden en que se aplique estos 2
                                                                                   73
33
             negros = lazy_pintar * cnt;
                                                                                             //reverse
                                                                                   74
34
                                                                                            if (t->rev) {
           } else {
                                                                                   75
35
                                                                                               swap(t->1, t->r);
             lazy_flip ^= true;
                                                                                   76
36
                                                                                               t->rev = false;
             negros = cnt - negros;
37
                                                                                   77
           }
                                                                                               if (t->1) t->1->push_lazy(REVERSE);
38
                                                                                   78
         }
                                                                                               if (t->r) t->r->push_lazy(REVERSE);
                                                                                   79
39
         if (type == REVERSE) {
40
                                                                                   80
           if (lazy_pintar == -1) {
                                                                                             //invertir colores
                                                                                   81
41
             rev ^= true;
                                                                                             if (t->lazy_flip) {
                                                                                   82
42
           }
                                                                                               t->value = 1 - (t->value);
                                                                                   83
43
         }
                                                                                               t->lazy_flip = false;
                                                                                   84
44
       }
                                                                                               if (t->1) t->1->push_lazy(FLIP);
45
                                                                                   85
       void verify() {
                                                                                               if (t->r) t->r->push_lazy(FLIP);
                                                                                   86
46
         bool op1 = (lazy_pintar != -1);
                                                                                            }
47
                                                                                   87
                                                                                          }
         bool op2 = (rev || lazy_flip);
                                                                                   88
48
         //solo puede pasar uno de los 2 casos, o ninguno esta activado o
                                                                                   89
49
             solo uno de los dos
                                                                                        void split(node t, int x, node &L, node &R) {
                                                                                   90
         assert((!op1 and !op2) or (op1 xor op2));
                                                                                          push(t);
50
                                                                                   91
```

```
if (t == nullptr) {L = R = nullptr; return;}
92
        int curIndex = cnt(t->1) + 1;
93
        if (curIndex <= x) {</pre>
94
          split(t->r, x - curIndex, t->r, R);
95
          L = t;
96
        } else {
97
          split(t->1, x, L, t->1);
98
          R = t;
99
        }
100
        t->recalc();
101
102
      node merge(node L, node R) {
103
        push(L); push(R);
104
        if (L == nullptr) return R;
105
        if (R == nullptr) return L;
106
        if (L->y > R->y) {
107
          L->r = merge(L->r, R);
108
          L->recalc();
109
          return L:
110
        } else {
111
          R->1 = merge(L, R->1);
112
          R->recalc();
113
          return R;
114
        }
115
      }
116
      void insert(int pos, int value) {
117
        node L, R;
118
        split(root, pos, L, R);//en R esta pos
119
        root = merge(merge(L, new _node(value)), R);
120
      }
121
      int cnt(node t) {
122
        return t ? t->cnt : 0;
123
124
      int size() {
125
        return cnt(root);
126
127
      void reverse(int i, int j) {
128
        node L. m. R:
129
        split(root, i, L, R);
130
        split(R, j - i + 1, m, R);
131
        m->push_lazy(REVERSE);
132
        root = merge(merge(L, m), R);
133
134
```

```
void flip(int i, int j) {
135
        node L, m, R;
136
        split(root, i, L, R);
137
        split(R, j - i + 1, m, R);
138
        m->push_lazy(FLIP);
139
        root = merge(merge(L, m), R);
140
141
      void pintar(int i, int j, int color) {
142
        node L, m, R;
143
        split(root, i, L, R);
144
        split(R, j - i + 1, m, R);
145
        m->push_lazy(PAINT, color);
146
        root = merge(merge(L, m), R);
147
     }
148
     void query(int i, int j) {
149
       node L, m, R;
        split(root, i, L, R);
151
        split(R, j - i + 1, m, R);
        int negros = m->negros;
        int blancos = m->cnt - negros;
        printf("%d\\n", negros, blancos);
        root = merge(merge(L, m), R);
156
157
     void print(node &t, string spacio, char lado = ''') {
158
        if (t == nullptr) return;
159
        cout << spacio << lado <<"_->_" << (t->to_string()) << endl;
160
        print(t->1, spacio + "\t", 'L');
161
        print(t->r, spacio + "\t", 'R');
162
163
164
     void print() {
        print(root, "");
165
     }
166
167 };
```

2.11 Convex Hull Trick Estatico

```
// g++ "convexhulltrick.cpp" -o run
/***

Contain a sample about convex hull trick optimization this recivie N
pairs:
a "value of length" and a cost, we need to minimize the value of
grouping
```

```
6 this pairs taken the most large pair as the cost of the group
   Problem for practice: aquire
9
   #include <iostream>
   #include <vector>
   #include <algorithm>
   using namespace std;
   int pointer; //Keeps track of the best line from previous query
   vector<long long> M; //Holds the slopes of the lines in the envelope
   vector<long long> B; //Holds the y-intercepts of the lines in the
       envelope
   //Returns true if either line 11 or line 13 is always better than line
   bool bad(int 11, int 12, int 13)
19
20
     intersection(11,12) has x-coordinate (b1-b2)/(m2-m1)
21
     intersection(11.13) has x-coordinate (b1-b3)/(m3-m1)
22
     set the former greater than the latter, and cross-multiply to
23
     eliminate division
24
     */
25
     return (B[13]-B[11])*(M[11]-M[12])<(B[12]-B[11])*(M[11]-M[13]);
26
27
    //Adds a new line (with lowest slope) to the structure
28
   void add(long long m,long long b)
29
30
     //First, let's add it to the end
31
     M.push_back(m);
32
     B.push_back(b);
33
     //If the penultimate is now made irrelevant between the
34
         antepenultimate
     //and the ultimate, remove it. Repeat as many times as necessary
35
     while (M.size() \ge 3\&\&bad(M.size() - 3, M.size() - 2, M.size() - 1))
36
37
       M.erase(M.end()-2);
38
       B.erase(B.end()-2);
39
     }
40
41
   //Returns the minimum y-coordinate of any intersection between a given
   //line and the lower envelope
44 long long query(long long x)
```

```
45 {
     //If we removed what was the best line for the previous query, then
46
     //newly inserted line is now the best for that query
47
     if (pointer>=M.size())
48
       pointer=M.size()-1;
49
     //Any better line must be to the right, since query values are
50
     //non-decreasing
51
     while (pointer<M.size()-1&&
52
       M[pointer+1] *x+B[pointer+1] < M[pointer] *x+B[pointer])</pre>
53
       pointer++;
54
     return M[pointer] *x+B[pointer];
55
56
   int main()
57
   {
58
     int M,N,i;
59
     pair<int, int> a[50000];
60
     pair<int,int> rect[50000];
     scanf("%d",&M);
62
     for (i=0; i<M; i++)
63
       scanf("%du%d",&a[i].first,&a[i].second);
64
     //Sort first by height and then by width (arbitrary labels)
65
     sort(a,a+M);
66
     for (i=0,N=0; i<M; i++)</pre>
67
68
       /*
69
       When we add a higher rectangle, any rectangles that are also
70
       equally thin or thinner become irrelevant, as they are
71
       completely contained within the higher one; remove as many
72
       as necessary
73
74
       while (N>0&&rect[N-1].second<=a[i].second)
75
76
       rect[N++]=a[i]; //add the new rectangle
77
78
     long long cost;
79
     add(rect[0].second,0);
80
     //initially, the best line could be any of the lines in the envelope,
81
     //that is, any line with index 0 or greater, so set pointer=0
82
     pointer=0;
     for (i=0; i<N; i++)
84
85
       cost=query(rect[i].first);
86
```

2.12 Convex Hull Trick Dinamico

```
// g++ -std=c++11 "convexhulltrick_dynamic.cpp" -o run
2
           ======= <Convex hull trick dynamic version version>
  warning with the use of this, this is a black box, try to use only in an
         emergency.
   Problem for practice: aquire
6
   #include <bits/stdc++.h>
   using namespace std;
   typedef long long 11;
   const ll is_query = -(1LL<<62);</pre>
     struct Line {
     ll m, b;
12
     mutable multiset<Line>::iterator it:
13
     const Line *succ(multiset<Line>::iterator it) const;
14
     bool operator<(const Line& rhs) const {
15
       if (rhs.b != is_query) return m < rhs.m;</pre>
16
       const Line *s=succ(it);
17
       if(!s) return 0;
18
       11 x = rhs.m;
19
       return b - s->b < (s->m - m) * x;
20
21
^{22}
   struct HullDynamic : public multiset<Line>{ // will maintain upper hull
        for maximum
     bool bad(iterator y) {
24
       iterator z = next(y);
^{25}
       if (y == begin()) {
26
          if (z == end()) return 0;
27
         return y->m == z->m && y->b <= z->b;
28
29
       iterator x = prev(y);
30
       if (z == end()) return y \rightarrow m == x \rightarrow m \&\& y \rightarrow b <= x \rightarrow b;
31
```

```
return (x-b - y-b)*(z-m - y-m) >= (y-b - z-b)*(y-m - x-m);
32
33
     iterator next(iterator y){return ++y;}
34
     iterator prev(iterator y){return --y;}
35
       void insert_line(ll m, ll b) {
36
      iterator y = insert((Line) { m, b });
       y->it=y;
       if (bad(y)) { erase(y); return; }
       while (next(y) != end() && bad(next(y))) erase(next(y));
       while (y != begin() && bad(prev(y))) erase(prev(y));
42
     ll eval(ll x) {
43
       Line 1 = *lower_bound((Line) { x, is_query });
      return 1.m * x + 1.b;
    }
46
   }h:
47
   const Line *Line::succ(multiset<Line>::iterator it) const{
49 | return (++it==h.end()? NULL : &*it);}
                            2.13 Misof Tree
```

```
http://codeforces.com/blog/entry/10493#comment-159335
  Sirve para encontrar el i-esimo numero de un conjunto de numeros que
       vamos insertando en el arbol.
4 Sirve solo si nuestros numeros son del 0 al n-1 (pero podemos mapearlos
       antes de usarlos)
5 La idea es esta:
  Funcionamiento:
    - En el fondo sigue siendo un Segment-Tree (hacemos que 'n' sea 2^x)
    - Cada nodo guarda cuantos numeros hay en el intervalo (entonces en
         tree[1] dice cuantos numeros tenemos en total)
    - Se sigue representando los hijos del nodo 'i' con '2 * i' (izq) y '2
          * i + 1' (der);
   Query:
10
11
    - si kth es mas grande que todos los que tenemos(tree[1]) o es
         negativo entonces -1
    - siempre nos mantenemos en el nodo de la izquierda y si es necario
         avanzamos al de la derecha
                        'i <<= 1'
13
       - si kth es mas grande que el nodo de la izquierda(el actual) quiere
14
            decir que podemos quitarle todos esos
```

```
numeros a nuestra busqueda 'kth - tree[i]' y buscar el nuevo kth en
15
           el arbol de la derecha
         if (kth > tree [i]) kth -= tree [i++];
16
       - Ojo en el 'i++' ahi es donde avanzamos al nodo de la derecha
17
     - luego hace su formula rara que aun no entendi xD:
18
         'i - leaf + (kth > tree [i])';
19
20
   const int MaxN = 1e6;
21
^{22}
   int a [MaxN], s [MaxN];
   int leaf, tree [100 + MaxN << 2];
   void bld (int n) { leaf = 1 << (32 - __builtin_clz (n)); }</pre>
   void add (int x) { for (int i = leaf + x; i; i >>= 1) ++tree [i]; }//
       Podemos insertar mas de una copia la vez tree [i] += xcopies;
   void del (int x) { for (int i = leaf + x; i; i >>= 1) --tree [i]; }//
       Podemos eliminar mas de una copia la vez tree [i] -= xcopies;
   // en "leaf + x" esta cuantas copias tenemos de "x"
   //Cuidado con intentar hacer del con mas copias de las disponibles, el
       kth() no funcionaria
   long kth (int kth, int i = -1) {
       if (kth > tree [1] || kth <= 0) return i;</pre>
32
     for (i = 1; i < leaf; i <<= 1) if (kth > tree [i]) kth -= tree [i++];
       return i - leaf + (kth > tree [i]);
34
35 }
```

2.14 SQRT Decomposition Basic

```
const int maxn = 500010;
int n;

tipo v[maxn];//vector principal

tipo lazy[maxn];
pair<tipo, tipo> t[maxn];//para poder reordenar los elementos

int SQRT;
int N;//nro. de buckets

//Recalcula y aplica el lazy al bucket con indice idx
//guarda la informacion necesaria del bucket en otros vectores
//podria ser la suma del bucket, o el min/max del bucket
void recalc(int idx) {
```

```
int a = idx * SQRT, b = min(n, (idx + 1) * SQRT);
     for (int i = a; i < b; i++) {
17
       v[i] += lazy[idx];
18
       t[i] = make_pair(v[i], i);
19
     }
20
     lazv[idx] = 0;
21
     sort(t + a, t + b);
22
23
24
   //adiciona delta a todos los elementos
   //en el intervalo cerrado [a, b]
   void add(int a, int b, tipo delta) {
     int idx_a = a / SQRT, idx_b = b / SQRT;
     if (idx_a == idx_b) {
29
    for (int i = a; i <= b; i++)
30
         v[i] += delta;
31
      recalc(idx_a);
    } else {
       //head
34
       for (int i = a, lim = min(n, (idx_a + 1) * SQRT); i < lim; i++)
         v[i] += delta;
36
       recalc(idx_a);//OJO puede ser necesario
37
       //body
38
       for (int i = idx_a + 1; i < idx_b; i++)
         lazv[i] += delta;
40
       //tail
       for (int i = idx_b * SQRT; i \le b; i++)
42
         v[i] += delta;
43
       recalc(idx_b);//OJO puede ser necesario
44
45
   }
46
47
   //tambien podria ser en un rango como en el add
   tipo query(tipo val) {
     tipo ans = 0;
50
     //recorro todos los buckets
51
     for (int idx = 0; idx < N; idx++) {
       int a = idx * SQRT, b = min(n, (idx + 1) * SQRT);
      //... hacer algo ...
54
55
     return ans;
56
57
58 | int main() {
```

```
//leer n, q y los elementos de v
59
60
     SQRT = (int)sqrt(n) + 1;
61
     N = (n + SQRT - 1) / SQRT; //nro. de buckets
62
     //construir cada bucket
63
     for (int idx = 0; idx < N; idx++)
64
       recalc(idx);
65
66
     //resto del programa
     return 0;
68
  |}
69
    2.15 Nro. Elementos menores o iguales a x en O(loq(n))
```

```
//insersion y consulta de cuantos <= en log n
   struct leqset {
2
     int maxl; vector<int> c;
     int pref(int n, int l) { return (n>>(maxl-l))|(1<<l); }</pre>
     void ini(int ml) { maxl=ml; c=vector<int>(1<<(maxl+1)); }</pre>
     //inserta c copias de e, si c es negativo saca c copias
     void insert(int e, int q=1) { forn(1,maxl+1) c[pref(e,1)]+=q; }
     int leq(int e) {
       int r=0,a=1;
9
       forn(i,maxl) {
10
         a<<=1; int b=(e>>maxl-i-1)&1;
11
         if (b) r+=c[a]: a|=b:
12
       } return r + c[a]; //sin el c[a] da los estrictamente menores
13
14
     int size() { return c[1]; }
     int count(int e) { return c[e|(1<<maxl)]; }</pre>
17 | };
```

3 Algos

3.1 LIS en O(n log n) con Reconstruccion

```
//Para non-increasing, cambiar comparaciones y revisar busq binaria
//Given an array, paint it in the least number of colors so that each color turns to a non-increasing subsequence.
//Solution:Min number of colors=Length of the longest increasing subsequence
// Las lineas marcadas con // Camino no son necesarias si no se desea reconstruir el camino.
```

```
6 #define MAXN 1000000
7 int v[MAXN]; // INPUT del algoritmo.
  int mv[MAXN];
   int mi[MAXN] ,p[MAXN]; // Camino
   int 1 [MAXN]; // Aca apareceria la maxima subsecuencia creciente(los
       indices)
int lis(int n) {
    forn(i,n) mv[i] = INF;
     forn(i,n) mi[i] = -1; // Camino
     forn(i,n) p [i] = -1; // Camino
     mv[0] = -INF;
15
     int res = 0;
16
     forn(i,n) {
17
       // Con upper_bound es maxima subsecuencia no decreciente.
       // Con lower_bound es maxima subsecuencia creciente.
19
       int me = upper_bound(mv,mv+n,v[i]) - mv;
       p[i] = mi[me-1]; // Camino
21
       mv[me] = v[i];
       mi[me] = i: // Camino
       if (me > res) res = me;
    }
25
     for(int a = mi[res], i = res - 1;a != -1; a = p[a], i--) // Camino
26
       1[i] = a; // Indices: poniendo 1[i] = v[a] quedan los valores.
27
     return res;
28
29 }
```

3.2 Mo

```
// g++ -std=c++11 "mo.cpp" -o run
/***

Contain a sample about Mo algorithm
Brief explanation when use Mo:
Explain where and when we can use above algorithm

As mentioned, this algorithm is offline, that means we cannot use it when we are forced to stick to given order of queries.

That also means we cannot use this when there are update operations.
Not just that, there is one important possible limitation:

We should be able to write the functions add and remove. There will be many cases where add is trivial but remove is not.

One such example is where we want maximum in a range. As we add elements , we can keep track of maximum. But when we remove elements
```

 $_{11} | x = 1;$

```
12 it is not trivial. Anyways in that case we can use a set to add elements
        , remove elements and report minimum.
  In that case the add and delete operations are O(log N) (Resulting in O(
       N * Sqrt(N) * log N) algorithm).
14
   Suggestion first use the add operation, then the erase operation
   Problem for practice: DQUERY spoj
   Input: N, then N elements of array M querys with a range L,R
18
   const int MAXV = 1e6 + 10;
   const int N = 30010;
   const int M = 200010;
   int cnt[MAXV]:
   int v[N];
24
   struct query{
     int 1,r,pos;
26
     query(){}
27
28
   int n;
   query qu[M];
   int ans[M];
31
32
   int ret = 0;
   void add(int pos){
34
     pos = v[pos];
35
     cnt[pos]++;
36
     if(cnt[pos] == 1){
37
       ret++;
38
     }
39
40
   void erase(int pos){
41
     pos = v[pos];
42
     cnt[pos]--;
43
     if(!cnt[pos])ret--;
44
45
   int main(){
46
     n = in():
47
     for(int i = 0; i < n; i++){}
48
       v[i] = in();
49
50
     int block = ceil(sqrt(n));
51
     int q = in();
52
```

```
for(int i = 0; i < q; i++){
53
       qu[i].1 = in() - 1, qu[i].r = in() - 1, qu[i].pos = i;
54
55
     sort(qu,qu + q,[&](const query &a,const query &b){
56
       if(a.l / block != b.l / block)
57
         return a.1 / block < b.1 / block;
58
       return a.r < b.r;
59
     });
60
     int 1 = 0, r = 0;
61
     for(int i = 0; i < q; i++){
       int nl = qu[i].1,nr = qu[i].r;
63
       while(l > nl){
64
         add(--1):
65
       }
66
       while(r <= nr){</pre>
         add(r++);
       }
69
       while(1 < n1){</pre>
         erase(1++):
71
72
       while(r > nr + 1){
73
         erase(--r);
74
       }
75
76
       ans[qu[i].pos] = ret;
77
78
     for(int i = 0; i < q; i++)printf("%d\n",ans[i]);
80 }
                     3.3 Ternary Search - Reales
    f[x] increases and then decreases, and we want the maximum value of f[x].
1 //yeputons ~ 300 iteraciones es mas que suficiente
   double l = a, r = b;
   for(int i=0; i<200; i++) {
     double 11 = (1*2+r)/3;
     double 12 = (1+2*r)/3;
     if(f(11) > f(12))
       r = 12;
     else
       1 = 11:
9
   }
10
```

Si f(x) es facil derivar se deriva f(x) - > f'(x) luego se iguala f'(x) = 0 y se despeja x, estamos consiguiendo el punto donde la pendiente es zero (si es de varias variables se deriva parcialmente).

Si no se puede despejar x de f'(x) y estamos seguros que tiene forma de parabola, se puede *aplicar binary search*, buscamos el punto donde la pendiente cambie de signo(osea sea igual a 0)

3.4 Ternary Search - Enteros

f[x] increases and then decreases, and we want the maximum value of f[x].

```
//f[x] increases and then decreases, and we want the maximum value of f[
    x].
int lo = -1, hi = n;
while (hi - lo > 1){
    int mid = (hi + lo)>>1;
    if (f(mid) > f(mid + 1))
        hi = mid;
else
    lo = mid;
}
//lo + 1 is the answer
```

4 Strings

4.1 Manacher

```
vector<int> manacher(const string &_s) {
     int n = _s.size();
2
     string s(2 * n + 3, '#');
     s[0] = \%, s[s.size() - 1] = \%, s[s.size() - 1] = \%
     for (int i = 0; i < n; i++)
      s[(i + 1) * 2] = _s[i];
6
7
     n = s.size();
8
     vector<int> P(n, 0);
9
     int C = 0, R = 0:
10
    for (int i = 1; i < n - 1; i++) {
11
       int j = C - (i - C);
12
       if (R > i)
13
        P[i] = min(R - i, P[i]);
14
       while (s[i + 1 + P[i]] == s[i - 1 - P[i]])
15
```

```
P[i]++:
       if (i + P[i] > R) {
17
18
         C = i;
         R = i + P[i];
19
20
21
     return P;
22
23
   bool is_pal(const vector<int> &mnch_vec, int i, int j) {//[i, j] - i<=j
     int len = i - i + 1;
     i = (i + 1) * 2; //idx to manacher vec idx
     j = (j + 1) * 2;
     int mid = (i + i) / 2:
28
     return mnch vec[mid] >= len:
29
30
   int main() {
     string s;
     cin >> s;
     vector<int> mnch_vec= manacher(s);
     if (is_pal(mnch_vec, 2, 7)) {
       //la subcadena desde la posicion 2 a la 7 es palindrome
    }
37
     return 0;
39 }
                                  Trie(estatico)
int trie[10000000] [26];
   int sig;
   int root = 0;
   void reset() {
       sig = -1;
       addNode();//Root
6
   | }
7
   void addNode() {
       sig++;
       memset(trie[sig], -1, sizeof(trie[sig]));
10
   }
11
```

void insert(const string &s) {

if (trie[cur][c] == -1) {

for (int i = 0; i < sz(s); i++) {

int cur = root:

int c = s[i] - 'a';

13

14

15

16

```
addNode():
                                                                                                 for(int i = 0; i < N; i = nxt[i]){
17
                                                                                     35
           trie[cur][c] = sig;
                                                                                                     for(int j = i;j<nxt[i];++j){</pre>
                                                                                     36
18
       }
                                                                                                         int s = sa[j]-H;
19
                                                                                     37
       cur = trie[cur][c];
                                                                                                         if(s>=0){
20
                                                                                     38
       }
                                                                                                              int head = rk[s];
21
                                                                                     39
22 }
                                                                                                              rk[s] = head+cont[head];
                                                                                     40
                                                                                                              ++cont[head];
                                                                                     41
              Suffix Array O(n log n) con LCP (Kasai) O(n)
                                                                                                              b2h[rk[s]] = true;
                                                                                     42
                                                                                                         }
                                                                                     43
   #define MAX_LEN 100000
                                                                                                     for(int j = i;j<nxt[i];++j){</pre>
   #define ALPH_SIZE 123
                                                                                     45
                                                                                                         int s = sa[j]-H;
   typedef char tipo;
                                                                                     46
                                                                                                         if(s>=0 && b2h[rk[s]]){
   tipo s[MAX_LEN+1];
                                                                                     47
                                                                                                              for(int k = rk[s]+1;!bh[k] && b2h[k];++k)
   int N,sa[MAX_LEN],rk[MAX_LEN];
                                                                                                                  b2h[k] = false;
   int cont[MAX_LEN],nxt[MAX_LEN];
                                                                                                         }
   bool bh[MAX_LEN+1],b2h[MAX_LEN+1];
                                                                                     50
                                                                                                     }
                                                                                     51
                                                                                                 }
    void build_suffix_array(){
                                                                                     52
       N = strlen(s); //size for ints
                                                                                                 for(int i = 0:i < N:++i){
                                                                                     53
10
                                                                                                     sa[rk[i]] = i;
       memset(cont,0,sizeof(cont));
11
                                                                                                     bh[i] |= b2h[i];
       for(int i = 0; i < N; ++i) ++cont[s[i]];
                                                                                     55
12
                                                                                                 }
       for(int i = 1;i<ALPH_SIZE;++i) cont[i] += cont[i-1];</pre>
                                                                                     56
13
                                                                                             }
       for(int i = 0; i < N; ++i)sa[--cont[s[i]]] = i;
                                                                                     57
14
       for(int i = 0:i < N:++i){
                                                                                     58
15
                                                                                        vector<int> kasai(){
           bh[i] = (i==0 || s[sa[i]] != s[sa[i-1]]);
16
                                                                                             int n = N, k = 0;
           b2h[i] = false;
                                                                                     60
17
                                                                                             vector<int> lcp(n,0);
       }
                                                                                     61
18
                                                                                             vector<int> rank(n,0);
       for(int H = 1; H < N; H <<= 1){
                                                                                     62
19
                                                                                             for(int i=0; i<n; i++) rank[sa[i]]=i;</pre>
            int buckets = 0;
                                                                                     63
20
                                                                                             for(int i=0; i<n; i++, k?k--:0){
                                                                                     64
           for(int i = 0, j; i < N; i = j){
21
                                                                                                 if(rank[i]==n-1) {k=0; continue;}
                j = i+1;
                                                                                     65
22
                                                                                                 int j=sa[rank[i]+1];
                while(j<N && !bh[j]) ++j;
                                                                                     66
23
                                                                                                 while(i+k<n && j+k<n && s[i+k]==s[j+k]) k++;
                nxt[i] = j;
                                                                                     67
^{24}
                                                                                                 lcp[rank[i]]=k;
                                                                                     68
                ++buckets;
25
                                                                                            }
           }
                                                                                     69
26
                                                                                            return lcp;
                                                                                     70
           if(buckets==N) break;
27
                                                                                     71 }
           for(int i = 0; i < N; i = nxt[i]){
28
                cont[i] = 0:
29
                                                                                                        4.4 Minima rotacion lexicografica
                for(int j = i; j<nxt[i];++j)</pre>
30
                    rk[sa[j]] = i;
31
32
            ++cont[rk[N-H]];
                                                                                      2 Rotacion Lexicografica minima MinRotLex(cadena,tamanio)
33
            b2h[rk[N-H]] = true;
                                                                                      para cambiar inicio de la cadena char s[300]; int h; s+h;
34
```

```
4 | retorna inicio de la rotacion minima :D
5
   int MinRotLex(const char *s, const int slen) {
6
      int i = 0, j = 1, k = 0, x, y, tmp;
      while(i < slen && j < slen && k < slen) {</pre>
         x = i + k;
         y = j + k;
         if(x >= slen) x -= slen;
         if(y >= slen) y -= slen;
12
         if(s[x] == s[y]) {
13
            k++;
14
         else if(s[x] > s[y]) {
15
            i = j+1 > i+k+1 ? j+1 : i+k+1;
16
            k = 0:
17
            tmp = i, i = j, j = tmp;
18
         } else {
19
            j = i+1 > j+k+1 ? i+1 : j+k+1;
20
            k = 0;
21
         }
22
      }
23
      return i;
24
25
   int main(){
26
     int n;
27
     scanf("%d",&n);getchar();
28
     while(n--){
29
       char str[1000009];
30
       gets(str);
31
       printf("%d\n",MinRotLex(str,strlen(str))+1);
32
33
34 }
                              4.5 Matching
                                 4.5.1 KMP
```

```
string T;//cadena donde buscar(where)
  string P;//cadena a buscar(what)
  int b[MAXLEN];//back table b[i] maximo borde de [0..i)
  void kmppre(){//by gabina with love
      int i =0, j=-1; b[0]=-1;
5
      while(i<sz(P)){</pre>
6
          while(j>=0 && P[i] != P[j]) j=b[j];
7
          i++, j++, b[i] = j;
8
```

```
}
9
10
11
   void kmp(){
       int i=0, j=0;
       while(i<sz(T)){</pre>
13
            while(j>=0 && T[i]!=P[j]) j=b[j];
            i++, j++;
15
            if(j==sz(P)) printf("Puisufounduatuindexu%duinuT\n", i-j), j=b[j
16
       }
17
   }
18
19
   int main(){
       cout << "T=";
21
       cin >> T;
       cout << "P=";
       cin.ignore();
       cin >> P;
       kmppre();
       kmp();
       return 0;
29 }
```

4.5.2 Z - Por aprender

4.5.3 Matching con hash

```
typedef unsigned long long ull;
  const int p = 500009;
   int x;
   long long pw[500010];
   long long h[500010];
   long long poly(const string &t,int le,int ri){
    long long h = OLL;
     string s = "";
    for(int i = le; i < ri;i++)s += t[i];
     for(int i = s.size() - 1; i >= 0; i--){}
      h = ((h \% p) * (x \% p) + s[i]) \% p;
11
12
     return h;
13
14
   bool equal(const string &s,const string &t,int ini){
    for(int i = 0; i < t.size();i++){
16
       if(s[i + ini] != t[i])return false;
17
```

```
18
                                                                                    8
     return true;
                                                                                        int start = minIndex;
19
   }
                                                                                        maxIndex = text.size();
20
   int main() {
                                                                                        while(minIndex < maxIndex){</pre>
                                                                                   11
21
       x = (rand() \% (p - 1)) + 1;
                                                                                           int mid = (minIndex + maxIndex) >> 1;
                                                                                   12
22
                                                                                          if(cmp(pattern,sa[mid]) < 0)maxIndex = mid;</pre>
     pw[0] = 1;
23
       for(int i = 1; i \le 5e5 + 5; i++){
                                                                                           else minIndex = mid + 1;
                                                                                   14
       pw[i] = (pw[i - 1] * x % p) % p;
                                                                                        }
                                                                                   15
25
                                                                                        int end = maxIndex;
                                                                                   16
26
                                                                                        for(int i = start; i < end;i++){</pre>
     string pattern, text;
27
     cin >> pattern >> text;
                                                                                           result.push_back(sa[i]);
28
                                                                                   18
     long long y = 1LL;
29
                                                                                   19
     h[text.size() - pattern.size()] = poly(text, text.size() - pattern.
                                                                                        return result;
                                                                                   20
         size(), text.size()):
                                                                                   21 }
     for(int i = 0; i < pattern.size(); i++){</pre>
                                                                                                             4.5.5 Matching con BWT
       y = (y \% p * x \% p) \% p;
32
33
     for(int i = text.size() - pattern.size() - 1; i>= 0; i--){
                                                                                    1 | map<char,int>fo;//first ocurrence
34
       long long cal = (text[i] - (y * text[i + pattern.size()]) % p + p )
                                                                                    map<char,vector<int> >count;//count the i-th ocurrence of symbol
35
           % p;
                                                                                      string first;//first colum of bwt
       if(cal < 0) cal += p;
                                                                                      string alpha = "ACGT$";//change this
36
       h[i] = ((x * h[i + 1]) \% p + cal) \% p;
                                                                                       void preprocess(const string& bwt) {//recieves a BWT
37
     }
                                                                                         string ans = "";
38
     vector<int>res;
                                                                                        first = bwt:
39
                                                                                    7
     int pHash = poly(pattern,0,pattern.size());
                                                                                        sort(first.begin(),first.end());
40
     for(int i = 0; i <= text.size() - pattern.size(); i++){</pre>
                                                                                        for(int i = 0;first[i];i++){
41
       if(pHash != h[i])continue;
                                                                                           if(!fo.count(first[i]))fo[first[i]] = i;
42
                                                                                   10
       if(equal(text,pattern,i))res.push_back(i);
43
                                                                                   11
                                                                                        for(char u:alpha)count[u].push_back(0);
                                                                                   12
44
     for(auto u:res)cout << u << "";</pre>
                                                                                        for(int i = 1; i <= bwt.size();i++){</pre>
45
                                                                                   13
     cout << "\n";
46
                                                                                           for(char u:alpha)
                                                                                   14
       return 0;
                                                                                             count[u].push_back(count[u].back() + (bwt[i - 1] == u));
47
                                                                                   15
48 }
                                                                                        }
                                                                                   16
                                                                                       }
                                                                                   17
                      4.5.4 Matching con suffix array
                                                                                       //return the number of ocurrences of the pattern
                                                                                       int bwtmatch(int bot,string &pattern){
   vector<int> FindOccurrences(const string& pattern, const string& text) {
                                                                                        int top = 0;
                                                                                   20
     vector<int> result:
                                                                                         while(top <= bot){</pre>
                                                                                   21
2
     int minIndex = 0,maxIndex = text.size();
                                                                                           if(pattern.size()){
                                                                                   22
     while(minIndex < maxIndex){</pre>
                                                                                             char letter = pattern.back();
                                                                                   23
       int mid = (minIndex + maxIndex) >> 1;
                                                                                             pattern.pop_back();
5
                                                                                   24
       if(cmp(pattern,sa[mid]) > 0)minIndex = mid + 1;
                                                                                             if(count[letter][bot + 1]){
                                                                                   25
6
       else maxIndex = mid;
                                                                                               top = fo[letter] + count[letter][top];
7
                                                                                   26
```

```
bot = fo[letter] + count[letter][bot + 1] - 1;
                                                                                     void print(int p){
27
                                                                                32
                                                                                       if(idhoja) cout << "found" << idhoja << "___at_position_" << p-
                                                                                33
28
         else return 0;
                                                                                           szhoja << endl;
29
                                                                                       if(get_nxthoja()) get_nxthoja()->print(p); }
30
                                                                                34
                                                                                     void matching(const string &s, int p=0){
       else return bot - top + 1;
                                                                                35
31
                                                                                       print(p); if(p<sz(s)) get_tran(s[p])->matching(s, p+1); }
32
     return 0;
                                                                                   }tri;
                                                                                37
33
34 }
                                                                                38
                    4.5.6 Matching con Aho-Corasick
                                                                                   int main(){
                                                                                     tri=trie();//clear
                                                                                41
                                                                                     tri.insert("ho", 1);
                                                                                42
                                                                                     tri.insert("hoho", 2);
   struct trie{
                                                                                43
2
     map<char, trie> next;
                                                                                                               Suffix Automaton
     trie* tran[256];//transiciones del automata
     int idhoja, szhoja;//id de la hoja o 0 si no lo es
     //link lleva al sufijo mas largo, nxthoja lleva al mas largo pero que
                                                                                 6
                                                                                   const int N = INSERTE_VALOR; //maxima longitud de la cadena
         es hoja
     trie *padre, *link, *nxthoja;
                                                                                   struct State { //OJO!!! tamanio del alfabeto, si MLE -> map
     char pch;//caracter que conecta con padre
                                                                                       State *pre, *go[26];//se puede usar un map<char, State*> go
     trie(): tran(), idhoja(), padre(), link() {}
                                                                                       int step;
                                                                                5
     void insert(const string &s, int id=1, int p=0){//id>0!!!
                                                                                       void clear() {
10
       if(p \le z(s)){
                                                                                           pre=0;
11
                                                                                7
         trie &ch=next[s[p]];
                                                                                           step=0:
                                                                                8
12
         tran[(int)s[p]]=&ch;
                                                                                           memset(go,0,sizeof(go));//go.clear();
13
         ch.padre=this, ch.pch=s[p];
                                                                                       }
                                                                                10
14
         ch.insert(s, id, p+1);
                                                                                   } *root,*last;
15
                                                                                   State statePool[N * 2],*cur;
16
                                                                                   void init() {
       else idhoja=id, szhoja=sz(s);
17
                                                                                       cur=statePool;
18
                                                                                14
     trie* get_link() {
                                                                                       root=last=cur++;
                                                                                15
19
       if(!link){
                                                                                       root->clear();
                                                                                16
20
         if(!padre) link=this;//es la raiz
                                                                                   | }
                                                                                17
^{21}
                                                                                   void Insert(int w) {
         else if(!padre->padre) link=padre;//hijo de la raiz
                                                                                18
^{22}
         else link=padre->get_link()->get_tran(pch);
                                                                                       State *p=last;
23
                                                                                19
       }
                                                                                       State *np=cur++;
                                                                                20
24
       return link; }
                                                                                       np->clear();
                                                                                21
^{25}
                                                                                       np->step=p->step+1;
     trie* get_tran(int c) {
                                                                                22
26
       if(!tran[c]) tran[c] = !padre? this : this->get_link()->get_tran(c);
                                                                                       while(p&&!p->go[w])
                                                                                23
27
                                                                                           p->go[w]=np,p=p->pre;
       return tran[c]; }
                                                                                24
28
     trie *get_nxthoja(){
                                                                                       if(p==0)
                                                                                25
29
       if(!nxthoja) nxthoja = get_link()->idhoja? link : link->nxthoja;
                                                                                26
                                                                                           np->pre=root;
30
       return nxthoja; }
                                                                                       else {
                                                                                27
31
```

```
State *q=p->go[w];
                                                                                              if (len > ans)
28
                                                                                  70
                                                                                                  ans = len, bestpos = i;
           if(p->step+1==q->step)
                                                                                  71
29
               np->pre=q;
                                                                                  72
30
           else {
                                                                                          //return ans; //solo el tamanio del lcs
                                                                                  73
31
                                                                                          return string(B + bestpos - ans + 1, B + bestpos + 1);
               State *ng=cur++;
                                                                                  74
32
               nq->clear();
                                                                                      }
33
                                                                                   75
               memcpy(nq->go,q->go,sizeof(q->go));//nq->go = q->go; para
34
                                                                                   76
                                                                                      /*Numero de subcadenas distintas + 1(subcadena vacia) en O(|A|)
               nq->step=p->step+1;
                                                                                      OJO: Por alguna razon Suffix Array es mas rapido
35
                                                                                      Se reduce a contar el numero de paths que inician en gO y terminan
               nq->pre=q->pre;
36
                                                                                      en cualquier nodo. dp[u] = # de paths que inician en u
               q->pre=nq;
37
                                                                                      - Se debe construir el automata en el main(init y Insert's)
               np->pre=nq;
38
               while (p\&\&p->go[w]==q)
                                                                                      - Setear dp en -1
39
                   p->go[w]=nq, p=p->pre;
                                                                                      */
                                                                                   83
40
           }
                                                                                      number dp[N * 2];
41
       }
                                                                                      number num_dist_substr(State *u = root) {
42
                                                                                          if (dp[u - statePool] != -1) return dp[u - statePool];
       last=np;
43
                                                                                          number ans = 1;//el path vacio que representa este nodo
44
                                                                                          for (int v = 0; v < 26; v++)//usar for (auto) para mapa
    /*####################### Suffix Automata ################/
                                                                                  88
45
                                                                                              if (u->go[v])
46
                                                                                                  ans += num_dist_substr(u->go[v]);
    /*################## Algunas aplicaciones ################/
                                                                                  90
47
                                                                                          return (dp[u - statePool] = ans);
   //Obtiene el LCSubstring de 2 cadenas en O(|A| + |B|)
                                                                                  91
   string lcs(char A[N], char B[N]) {
                                                                                      }
                                                                                  92
49
       int n,m;
                                                                                   93
50
       n = strlen(A); m = strlen(B);
                                                                                      /*Suma la longitud de todos los substrings en O(|A|)
51
       //Construccion: O(|A|)
                                                                                      - Construir el automata(init y insert's)
52
       //solo hacerlo una vez si A no cambia
                                                                                      - Necesita el metodo num_dist_substr (el de arriba)
53
       init();
                                                                                      - setear dp's en -1
54
       for(int i=0; i<n; i++)</pre>
                                                                                      */
                                                                                   98
55
                                                                                     number dp1[N * 2];
           Insert(A[i]-'a'); //Fin construccion
56
       //LCS: 0(|B|)
                                                                                     number sum_length_dist_substr(State *u = root) {
57
                                                                                          if (dp1[u - statePool] != -1) return dp1[u - statePool];
       int ans = 0, len = 0, bestpos = 0;
                                                                                  101
58
       State *p = root;
                                                                                          number ans = 0;//el path vacio que representa este nodo
                                                                                  102
59
                                                                                          for (int v = 0; v < 26; v++)//usar for (auto) para mapa
       for(int i = 0; i < m; i++) {
                                                                                  103
60
           int x = B[i] - a;
                                                                                              if (u->go[v])
                                                                                  104
61
           if(p->go[x]) {
                                                                                                  ans += (num_dist_substr(u->go[v]) + sum_length_dist_substr(u
                                                                                  105
62
                                                                                                       ->go[v]));
               len++;
63
                                                                                          return (dp1[u - statePool] = ans);
               p = p - go[x];
                                                                                  106
64
           } else {
                                                                                      }
                                                                                  107
65
               while (p \&\& !p->go[x]) p = p->pre;
                                                                                  108
66
               if(!p) p = root, len = 0;
                                                                                  109
67
               else len = p->step+1, p = p->go[x];
                                                                                      Pregunta si p es subcadena de la cadena con la cual esta construida
68
           }
                                                                                  el automata.
69
```

10

```
Complejidad: - Construir O(|Texto|) - solo una vez (init e insert's)
                 - Por Consulta O(|patron a buscar|)
113
114
    bool is_substring(char p[N]) {
115
        State *u = root;
116
        for (int i = 0; p[i]; i++) {
117
            if (!u->go.count(p[i]))//esta con map!!!
118
                return false;
119
            u = u->go[p[i]];//esta con map!!!
120
        }
121
        return true;
122
123 | }
```

K-esima permutacion de una cadena

```
//Entrada: Una cadena cad(std::string), un long th
   //Salida : La th-esima permutacion lexicografica de cad
   string ipermutacion(string cad, long long int th){
     sort(cad.begin(), cad.end());
     string sol = "";
5
     int pos;
6
     for(int c = cad.size() - 1; c \ge 0; c - - ){
       pos = th / fact[c];
       th %= fact[c]:
9
       sol += cad[pos];
       cad.erase(cad.begin() + pos);
11
12
     return sol;
13
14 }
```

Geometria

5.1 Cortar Poligono

```
1 //cuts polygon Q along the line ab
  //stores the left side (swap a, b for the right one) in P
  void cutPolygon(pto a, pto b, vector<pto> Q, vector<pto> &P){
    P.clear():
    forn(i, sz(Q)){
      double left1=(b-a)^(Q[i]-a), left2=(b-a)^(Q[(i+1)\%sz(Q)]-a);
      if(left1>=0) P.pb(Q[i]);
      if(left1*left2<0)
        P.pb(inter(line(Q[i], Q[(i+1)\%sz(Q)]), line(a, b)));
9
```

```
11 }
```

Interseccion de rectangulos

```
1 #define MAXC 2501
   struct Rect{
     int x1, y1, x2, y2;
     int color;
     int area:
     Rect(int _x1, int _y1, int _x2, int _y2){
      x1 = x1;
       y1 = _y1;
       x2 = _x2;
       y2 = _y2;
       getArea();
11
12
     int getArea(){
13
       if(x1>=x2 \mid \mid y1>=y2)return area = 0;
       return area = (x2-x1)*(y2-y1);
15
16
17
   Rect interseccion(Rect t, Rect r){
     int x1, y1, x2, y2;
    x1 = max(t.x1,r.x1);
    y1 = max(t.y1,r.y1);
    x2 = min(t.x2,r.x2);
    y2 = min(t.y2,r.y2);
    Rect res(x1,y1,x2,y2);
     return res;
25
26 }
```

5.3 Otra representación de rectas y segmentos

```
y = mx + b
```

La fraccion debe estar normalizada todo el tiempo. O podria causar errores.

```
bool between(fraction a, fraction b, fraction c) {
    return a <= c && c <= b;
  }
3
  struct segment {
    fraction pendiente, ordenada;
6
    fraction A, B;
    segment(fraction p, fraction ord, fraction a, fraction b) {
```

```
pendiente = p;
8
       ordenada = ord;
9
       A = a;
10
       B = b;
11
12
     bool read() {//retorna true si no se vertical
13
       fraction a, b, c, d;//(a,b) (c,d)
14
       a.read();
15
       b.read();
16
       c.read();
17
       d.read();
18
       if (a == c) {//vertical
19
         A = \min(b, d):
         B = max(b, d);
21
         ordenada = a;
22
         return false;
23
       }
24
       A = min(a, c);
25
       B = max(a, c):
26
       pendiente = (d - b) / (c - a);
27
       ordenada = b - (pendiente * a);
28
       return true;
29
30
     bool same_line(const segment &other) const {
31
       return (pendiente == other.pendiente) && (ordenada == other.ordenada
32
           );
     }
33
     bool intersect(const segment &other) const {
34
       if (!same_line(other)) return false;
35
       return between(A, B, other.A) || between(A, B, other.B);
36
     }
37
     void merge(const segment &other) const {
38
       A = \min(A, \text{ other. } A);
39
       B = min(B, other.B):
40
41
     bool operator < (const segment &other) const {</pre>
42
       if (A == other.A)
43
         return B < other.B:
44
       return A < other.A;
45
46
     string to_string() {
47
       stringstream ss;
48
       ss << "(" << A.to_string() << ", " << B.to_string() << ")";
49
```

```
return ss.str();
50
51
   };
52
   int main() {
     int n; cin >> n;
    vector<segment> verticales;
     vector<segment> normal;
    forn (i, n) {
       segment x;
       if (x.read()) {
         normal.pb(x);
      } else {
         verticales.pb(x);
       }
    }
64
    return 0;
66 }
```

5.4 Distancia punto-recta

```
double distance_point_to_line(const point &a, const point &b, const
    point &pnt) {
    double u = ((pnt.x - a.x)*(b.x - a.x) + (pnt.y - a.y)*(b.y - a.y)) /
        distsqr(a, b);
    point intersection;
    intersection.x = a.x + u*(b.x - a.x);
    intersection.y = a.y + u*(b.y - a.y);
    return dist(pnt, intersection);
}
```

5.5 Distancia punto-segmento

```
struct point{
   double x,y;
};
inline double dist(const point &a, const point &b){
   return sqrt((a.x-b.x)*(a.x-b.x) + (a.y-b.y)*(a.y-b.y));
}
inline double distsqr(const point &a, const point &b){
   return (a.x-b.x)*(a.x-b.x) + (a.y-b.y)*(a.y-b.y);
}
double distance_point_to_segment(const point &a, const point &b, const point &pnt){
```

 $_{1}$ const int N = 300;

```
double u = ((pnt.x - a.x)*(b.x - a.x) + (pnt.y - a.y)*(b.y - a.y)) /
11
         distsqr(a, b);
     point intersection;
12
     intersection.x = a.x + u*(b.x - a.x);
13
     intersection.y = a.y + u*(b.y - a.y);
14
15
     if (u < 0.0 \mid | u > 1.0)
16
       return min(dist(a, pnt), dist(b, pnt));
17
18
     return dist(pnt, intersection);
19
  |}
20
```

6 Math

6.1 Identidades

$$\sum_{i=0}^{n} \binom{n}{i} = 2^{n}$$

$$\sum_{i=0}^{n} i \binom{n}{i} = n * 2^{n-1}$$

$$\sum_{i=m}^{n} i = \frac{n(n+1)}{2} - \frac{m(m-1)}{2} = \frac{(n+1-m)(n+m)}{2}$$

$$\sum_{i=0}^{n} i = \sum_{i=1}^{n} i = \frac{n(n+1)}{2}$$

$$\sum_{i=0}^{n} i^{2} = \frac{n(n+1)(2n+1)}{6} = \frac{n^{3}}{3} + \frac{n^{2}}{2} + \frac{n}{6}$$

$$\sum_{i=0}^{n} i(i-1) = \frac{8}{6} (\frac{n}{2})(\frac{n}{2} + 1)(n+1) \text{ (doubles)} \rightarrow \text{Sino ver caso impar y par}$$

$$\sum_{i=0}^{n} i^{3} = \left(\frac{n(n+1)}{2}\right)^{2} = \frac{n^{4}}{4} + \frac{n^{3}}{2} + \frac{n^{2}}{4} = \left[\sum_{i=1}^{n} i\right]^{2}$$

$$\sum_{i=0}^{n} i^{4} = \frac{n(n+1)(2n+1)(3n^{2}+3n-1)}{30} = \frac{n^{5}}{5} + \frac{n^{4}}{2} + \frac{n^{3}}{3} - \frac{n}{30}$$

$$\sum_{i=0}^{n} i^{p} = \frac{(n+1)^{p+1}}{p+1} + \sum_{k=1}^{p} \frac{B_{k}}{p-k+1} \binom{p}{k} (n+1)^{p-k+1}$$

$$r = e - v + k + 1$$

Teorema de Pick: (Area, puntos interiores y puntos en el borde) $A = I + \frac{B}{2} - 1$

6.2 Ec. Caracteristica

$$\begin{aligned} a_0T(n) + a_1T(n-1) + \ldots + a_kT(n-k) &= 0 \\ p(x) &= a_0x^k + a_1x^{k-1} + \ldots + a_k \\ \text{Sean } r_1, r_2, \ldots, r_q \text{ las raı́ces distints, de mult. } m_1, m_2, \ldots, m_q \\ T(n) &= \sum_{i=1}^q \sum_{j=0}^{m_i-1} c_{ij} n^j r_i^n \end{aligned}$$

6.3 Identidades de agustin y mario

Las constantes c_{ij} se determinan por los casos base.

6.4 Combinatorio

```
forn(i, MAXN+1){//comb[i][k]=i tomados de a k
     comb[i][0]=comb[i][i]=1;
     forr(k, 1, i) comb[i][k]=(comb[i-1][k]+comb[i-1][k-1])%MOD;
3
4
  ll lucas (ll n, ll k, int p){ //Calcula (n,k)%p teniendo comb[p][p]
       precalculado.
    11 \text{ aux} = 1;
     while (n + k) aux = (aux * comb[n\%p][k\%p]) \%p, n/=p, k/=p;
     return aux;
9 }
                    6.5 Exp. de Numeros Mod.
1 | 11 expmod (11 b, 11 e, 11 m)\{\frac{1}{0}
     if(!e) return 1;
    11 q= expmod(b,e/2,m); q=(q*q)\%m;
    return e%2? (b * q)%m : q;
5 }
            6.6 Matrices de 2x2 y Fibonacci en log(n)
   tipo mod;
  struct M22 {
                       //|a b|
     tipo a, b, c, d; //|c d|
    M22 operator * (const M22 &p) const {
       return (M22){(a*p.a+b*p.c) % mod, (a*p.b+b*p.d) % mod, (c*p.a+d*p.c)
            % mod, (c*p.b+d*p.d) % mod};
6
   };
7
   M22 operator ^ (const M22 &p, tipo n) {
    if(!n) return (M22){1, 0, 0, 1};//matriz identidad
    M22 q = p (n/2); q = q * q;
     return (n \% 2)? p * q : q;
11
12
   //devuelve el n-esimo fibonacci (index 0)
   //f0 = fibo(0), f1 = fibo(1):
   tipo fibo(tipo n, tipo f0, tipo f1) {
    M22 \text{ mat}=(M22)\{0, 1, 1, 1\}^n;
     return (mat.a*f0 + mat.b*f1) % mod;
17
18 | }
                           6.7 Gauss Jordan
```

```
typedef vector<double> col;
   typedef vector<double> row;
   typedef vector<row>Matrix;
   col solution;
   int main(){
     Matrix M;
     M.resize(300);
8
     solution.resize(300);
9
     for(int i = 0; i < 30; i++)M[i].resize(30);
10
     int n;
11
     cin >> n;
12
     for(int i = 0; i < n; i++)
13
       for(int j = 0; j \le n; j++)
         cin >> M[i][j];
15
16
     for(int j = 0; j < n - 1; j++){
17
       int 1 = j;
18
       for(int i = j + 1; i < n; i++){
19
         if(fabs(M[i][j]) > fabs(M[l][j]))l = i;
20
21
       for(int k = j; k \le n; k++){
22
         swap(M[j][k],M[l][k]);
23
24
       for(int i = j + 1; i < n; i++)
25
         for(int k = n; k \ge j; k--)
26
           M[i][k] -= M[j][k] * M[i][j] / M[j][j];
27
     }
28
     double t = 0;
29
     for(int j = n - 1; j \ge 0; j--){
30
       t = 0.0:
31
       for(int k = j + 1; k < n; k++)t += M[j][k] * solution[k];
32
       solution[j] = (M[j][n] - t) / M[j][j];
33
     }
34
     cout.precision(4);
35
     for(int i = 0; i < n;i++)cout<<fixed << solution[i] << "";</pre>
     return 0;
37
38 }
```

6.8 Tridiangonal

```
4
     b :subdiagonal
     a :diagonal
     c :super diagonal
   //the answer is in D
   #define MAXN 5000
   long double A[MAXN], B[MAXN], C[MAXN], D[MAXN], X[MAXN];
   void solve(int n) {
       C[0] /= B[0]; D[0] /= B[0];
       for(int i = 1; i < n - 1; i++) C[i] /= B[i] - A[i] *C[i-1];
       for(int i = 1; i < n; i++)D[i] = (D[i] - A[i] * D[i-1]) / (B[i] - A[i]
           ] * C[i-1]):
      X[n-1] = D[n-1];
       for (int i = n-2; i \ge 0; i--) X[i] = D[i] - C[i] * X[i+1];
17
18 }
                              6.9 Simplex
1 // Two-phase simplex algorithm for solving linear programs of the form
2 //
3 //
          maximize
                       c^T x
4 //
          subject to Ax <= b
   //
                       x >= 0
   //
   // INPUT: A -- an m x n matrix
             b -- an m-dimensional vector
   //
             c -- an n-dimensional vector
  //
             x -- a vector where the optimal solution will be stored
10
   //
11
   // OUTPUT: value of the optimal solution (infinity if unbounded
   //
              above, nan if infeasible)
13
14
   // To use this code, create an LPSolver object with A, b, and c as
   // arguments. Then, call Solve(x).
17
   #include <iostream>
   #include <iomanip>
   #include <vector>
   #include <cmath>
   #include <limits>
23
using namespace std;
```

```
if (D[x][s] > -EPS) return true:
25
   typedef long double DOUBLE;
                                                                                            int r = -1;
                                                                                  66
   typedef vector<DOUBLE> VD;
                                                                                            for (int i = 0; i < m; i++) {
                                                                                  67
   typedef vector<VD> VVD;
                                                                                              if (D[i][s] < EPS) continue;
                                                                                              if (r == -1 || D[i][n + 1] / D[i][s] < D[r][n + 1] / D[r][s] ||
   typedef vector<int> VI;
                                                                                                (D[i][n + 1] / D[i][s]) == (D[r][n + 1] / D[r][s]) && B[i] < B
   const DOUBLE EPS = 1e-9;
                                                                                                     [r]) r = i;
                                                                                           }
                                                                                  71
   struct LPSolver {
                                                                                            if (r == -1) return false;
33
                                                                                           Pivot(r, s);
     int m, n;
     VI B, N;
35
                                                                                  74
     VVD D;
                                                                                       }
36
                                                                                  75
37
                                                                                  76
     LPSolver(const VVD &A, const VD &b, const VD &c):
                                                                                       DOUBLE Solve(VD &x) {
38
       m(b.size()), n(c.size()), N(n + 1), B(m), D(m + 2, VD(n + 2)) {
                                                                                          int r = 0:
                                                                                  78
39
       for (int i = 0; i < m; i++) for (int j = 0; j < n; j++) D[i][j] = A[
                                                                                          for (int i = 1; i < m; i++) if (D[i][n + 1] < D[r][n + 1]) r = i;
40
                                                                                          if (D[r][n + 1] < -EPS) {
           i][i];
       for (int i = 0; i < m; i++) { B[i] = n + i; D[i][n] = -1; D[i][n + i]
                                                                                           Pivot(r, n);
41
           1] = b[i]: 
                                                                                           if (!Simplex(1) | D[m + 1][n + 1] < -EPS) return -numeric limits<
                                                                                  82
       for (int j = 0; j < n; j++) { N[j] = j; D[m][j] = -c[j]; }
                                                                                                DOUBLE>::infinity();//NO SOLUTION
42
       N[n] = -1; D[m + 1][n] = 1;
                                                                                            for (int i = 0; i < m; i++) if (B[i] == -1) {
43
     }
                                                                                              int s = -1;
44
                                                                                              for (int j = 0; j \le n; j++)
45
     void Pivot(int r, int s) {
                                                                                                if (s == -1 \mid | D[i][j] < D[i][s] \mid | D[i][j] == D[i][s] && N[j]
46
       double inv = 1.0 / D[r][s];
                                                                                                     < N[s]) s = j;
47
       for (int i = 0; i < m + 2; i++) if (i != r)
                                                                                              Pivot(i, s);
                                                                                  87
48
                                                                                           }
         for (int j = 0; j < n + 2; j++) if (j != s)
                                                                                  88
49
           D[i][j] -= D[r][j] * D[i][s] * inv;
                                                                                          }
50
       for (int j = 0; j < n + 2; j++) if (j != s) D[r][j] *= inv;
                                                                                          if (!Simplex(2)) return numeric_limits<DOUBLE>::infinity();//
                                                                                  90
51
       for (int i = 0; i < m + 2; i++) if (i != r) D[i][s] *= -inv;
                                                                                              TNFTNTTY
52
       D[r][s] = inv;
                                                                                          x = VD(n);
                                                                                  91
53
       swap(B[r], N[s]);
                                                                                         for (int i = 0; i < m; i++) if (B[i] < n) x[B[i]] = D[i][n + 1];
54
                                                                                          return D[m][n + 1]://solution find
     }
55
                                                                                  94
56
     bool Simplex(int phase) {
                                                                                     };
                                                                                  95
57
       int x = phase == 1 ? m + 1 : m;
58
       while (true) {
                                                                                     int main() {
59
         int s = -1:
60
         for (int j = 0; j \le n; j++) {
                                                                                       const int m = 4;
61
           if (phase == 2 && N[j] == -1) continue;
                                                                                       const int n = 3;
                                                                                  100
           if (s == -1 \mid | D[x][j] < D[x][s] \mid | D[x][j] == D[x][s] && N[j] <
                                                                                       DOUBLE A[m][n] = {
                                                                                  101
63
                N[s]) s = j;
                                                                                         \{6, -1, 0\},\
                                                                                  102
                                                                                         \{-1, -5, 0\},\
         }
                                                                                 103
64
```

Mat mat(n,t);

return mat:

double det = 1;

double determinant(){//sacado de e maxx ru

forn(i,n) forn(j,t) forn(k,m) mat[i][j] += vec[i][k] * b[k][j];

14

15

16

17

18

```
int n = sz(vec):
        { 1, 5, 1 },
                                                                                      19
104
        \{-1, -5, -1\}
                                                                                                  Mat m(*this);
                                                                                      20
105
                                                                                                  forn(i, n){//para cada columna
106
                                                                                      21
      DOUBLE _b[m] = \{ 10, -4, 5, -5 \};
                                                                                                       int k = i;
107
                                                                                      22
      DOUBLE _{c}[n] = \{ 1, -1, 0 \};
                                                                                                       forr(j, i+1, n)//busco la fila con mayor val abs
108
                                                                                      23
                                                                                                           if(abs(m[j][i])>abs(m[k][i])) k = j;
                                                                                      24
109
      VVD A(m);
                                                                                                       if(abs(m[k][i])<1e-9) return 0;
110
                                                                                      25
      VD b(_b, _b + m);
                                                                                                       m[i].swap(m[k]);//la swapeo
111
                                                                                      26
      VD c(_c, _c + n);
                                                                                                       if(i!=k) det = -det;
112
                                                                                      27
      for (int i = 0; i < m; i++) A[i] = VD(_A[i], _A[i] + n);
                                                                                                       det *= m[i][i];
113
                                                                                                       forr(j, i+1, n) m[i][j] /= m[i][i];
114
                                                                                      29
      LPSolver solver(A, b, c);
                                                                                                       //hago 0 todas las otras filas
115
                                                                                      30
      VD x:
                                                                                                       forn(j, n) if (j!= i && abs(m[j][i])>1e-9)
                                                                                      31
116
      DOUBLE value = solver.Solve(x):
                                                                                                           forr(k, i+1, n) m[j][k]-=m[i][k]*m[j][i];
117
                                                                                      32
                                                                                                  }
                                                                                      33
118
      cerr << "VALUE: | " << value << endl; // VALUE: 1.29032
                                                                                                  return det;
119
      cerr << "SOLUTION:"; // SOLUTION: 1.74194 0.451613 1
                                                                                              }
120
                                                                                      35
      for (size_t i = 0; i < x.size(); i++) cerr << "" << x[i];
                                                                                          };
121
                                                                                      36
      cerr << endl:
122
                                                                                      37
      return 0;
123
                                                                                          int n;
124 }
                                                                                          int main() {
                                                                                          //DETERMINANTE:
                  6.10 Matrices y determinante O(n^3)
                                                                                          //https://uva.onlinejudge.org/index.php?option=com_onlinejudge&Itemid=8&
                                                                                              page=show_problem&problem=625
                                                                                            freopen("input.in", "r", stdin);
 1 | struct Mat {
                                                                                      42
                                                                                              ios::sync_with_stdio(0);
        vector<vector<double> > vec:
                                                                                      43
 2
                                                                                              while(cin >> n && n){
        Mat(int n): vec(n, vector<double>(n) ) {}
                                                                                      44
 3
                                                                                                  Mat m(n);
        Mat(int n, int m): vec(n, vector<double>(m) ) {}
                                                                                      45
 4
                                                                                                  forn(i, n) forn(j, n) cin >> m[i][j];
        vector<double> &operator[](int f){return vec[f];}
                                                                                      46
 5
                                                                                                  cout << (11)round(m.determinant()) << endl;</pre>
        const vector<double> &operator[](int f) const {return vec[f];}
                                                                                      47
 6
        int size() const {return sz(vec);}
                                                                                      48
 7
                                                                                              cout << "*" << endl;
        Mat operator+(Mat &b) { ///this de n x m entonces b de n x m
                                                                                      49
 8
                                                                                            return 0:
            Mat m(sz(b), sz(b[0]));
 9
                                                                                      51 }
            forn(i,sz(vec)) forn(j,sz(vec[0])) m[i][j] = vec[i][j] + b[i][j
10
                 ];
                                                                                                           6.11 Teorema Chino del Resto
            return m;
11
        Mat operator*(const Mat &b) { ///this de n x m entonces b de m x t
                                                                                                            y = \sum_{j=1}^{n} (x_j * (\prod_{i=1, i \neq j}^{n} m_i)_{m_j}^{-1} * \prod_{i=1, i \neq j}^{n} m_i)
12
            int n = sz(vec), m = sz(vec[0]), t = sz(b[0]);
13
```

6.12 Criba

1 #define MAXP 100000 //no necesariamente primo

17

```
1 int criba[MAXP+1];
                                                                                            n/=criba[n];
                                                                                     18
   void crearcriba(){
                                                                                         }
                                                                                    19
     int w[] = \{4,2,4,2,4,6,2,6\};
                                                                                          if(n>1) ret[n]++;
                                                                                    20
     for(int p=25;p<=MAXP;p+=10) criba[p]=5;</pre>
                                                                                          return ret;
                                                                                    21
     for(int p=9;p<=MAXP;p+=6) criba[p]=3;</pre>
                                                                                    22
     for(int p=4;p<=MAXP;p+=2) criba[p]=2;</pre>
                                                                                        //Usar asi: divisores(fac, divs, fac.begin()); NO ESTA ORDENADO
     for(int p=7,cur=0;p*p<=MAXP;p+=w[cur++&7]) if (!criba[p])
                                                                                        void divisores(const map<11,11> &f, vector<11> &divs, map<11,11>::
       for(int j=p*p;j<=MAXP;j+=(p<<1)) if(!criba[j]) criba[j]=p;</pre>
                                                                                            iterator it, ll n=1){
9
                                                                                            if(it==f.begin()) divs.clear();
10
                                                                                            if(it==f.end()) { divs.pb(n); return; }
   vector<int> primos;
   void buscarprimos(){
                                                                                            ll p=it->fst, k=it->snd; ++it;
12
                                                                                    27
                                                                                            forn(_, k+1) divisores(f, divs, it, n), n*=p;
     crearcriba();
13
                                                                                    28
     forr (i,2,MAXP+1) if (!criba[i]) primos.push_back(i);
                                                                                        }
                                                                                    29
                                                                                        ll sumDiv (ll n){
15
   //^{\sim} Useful for bit trick: #define SET(i) ( criba[(i)>>5]|=1<<((i)&31) ),
                                                                                         ll rta = 1;
                                                                                    31
        #define INDEX(i) ( (criba[i>>5]>>((i)&31))&1 ), unsigned int criba[
                                                                                          map<11,11> f=fact(n);
       MAXP/32+1];
                                                                                          forall(it, f) {
                                                                                    33
                                                                                          11 \text{ pot} = 1, \text{ aux} = 0;
17
                                                                                          forn(i, it->snd+1) aux += pot, pot *= it->fst;
                                                                                    35
18
   int main() {
                                                                                          rta*=aux;
19
     freopen("primos", "w", stdout);
                                                                                          }
20
                                                                                    37
     buscarprimos();
                                                                                          return rta;
21
                                                                                    38
                                                                                    39
                       6.13 Funciones de primos
                                                                                        ll eulerPhi (ll n){ // con criba: O(lg n)
                                                                                     40
                                                                                          11 \text{ rta} = n;
                                                                                    41
       Sea n = \prod p_i^{k_i}, fact(n) genera un map donde a cada p_i le asocia su k_i
                                                                                          map<11,11> f=fact(n);
                                                                                    42
                                                                                          forall(it, f) rta -= rta / it->first;
   //factoriza bien numeros hasta MAXP^2
                                                                                    43
   map<ll,ll> fact(ll n){ //0 (cant primos)
                                                                                     44
                                                                                          return rta;
     map<ll,ll> ret;
                                                                                     45
                                                                                        11 eulerPhi2 (11 n){ // 0 (sqrt n)
     forall(p, primos){
4
                                                                                          11 r = n;
       while(!(n%*p)){
                                                                                    47
5
                                                                                          forr (i,2,n+1){
         ret[*p]++;//divisor found
6
                                                                                            if ((11)i*i > n) break;
         n/=*p;
7
                                                                                            if (n \% i == 0){
       }
8
                                                                                              while (n\%i == 0) n/=i;
9
                                                                                              r = r/i; 
     if(n>1) ret[n]++;
                                                                                    52
10
                                                                                         }
     return ret;
11
                                                                                          if (n != 1) r= r/n:
12
                                                                                          return r;
    //factoriza bien numeros hasta MAXP
                                                                                    55
   map<11,11> fact2(11 n){ //0 (lg n)
                                                                                     56
14
     map<ll,ll> ret;
15
                                                                                        int main() {
     while (criba[n]){
16
                                                                                          buscarprimos();
       ret[criba[n]]++;
```

```
forr (x,1, 500000){
60
       cout << "x_1 = 1" << x << endl;
61
       cout << "Numero_de_factores_primos:_" << numPrimeFactors(x) << endl;</pre>
62
       cout << "Numero_de_distintos_factores_primos:_" <<
63
            numDiffPrimeFactors(x) << endl;</pre>
       cout << "Suma_de_factores_primos:_" << sumPrimeFactors(x) << endl;
64
       cout << "Numero de divisores:" << numDiv(x) << endl;</pre>
65
       cout << "Suma de divisores:" << sumDiv(x) << endl;</pre>
       cout << "Phi_de_Euler:_" << eulerPhi(x) << endl;</pre>
68
     return 0;
69
70 |}
```

6.14 Phollard's Rho (rolando)

```
1 | 11 gcd(11 a, 11 b){return a?gcd(b %a, a):b;}
2
  | 11 mulmod (11 a, 11 b, 11 c) { //returns (a*b)%c, and minimize overfloor
     11 x = 0, y = a\%c;
     while (b > 0)
       if (b \% 2 == 1) x = (x+y) \% c;
       y = (y*2) \% c;
       b /= 2:
8
9
     return x % c;
10
11
12
   ll expmod (ll b, ll e, ll m){\frac{1}{0}} \log b
13
     if(!e) return 1;
14
     11 q= expmod(b,e/2,m); q=mulmod(q,q,m);
15
     return e%2? mulmod(b,q,m) : q;
16
17
18
   bool es_primo_prob (ll n, int a)
19
20
     if (n == a) return true;
^{21}
     ll s = 0.d = n-1:
22
     while (d \% 2 == 0) s++, d/=2:
23
24
     11 x = expmod(a,d,n);
25
     if ((x == 1) \mid | (x+1 == n)) return true;
26
27
```

```
forn (i. s-1){
       x = mulmod(x, x, n);
29
       if (x == 1) return false;
       if (x+1 == n) return true;
31
    }
32
     return false;
33
34
35
   bool rabin (ll n){ //devuelve true si n es primo
     if (n == 1) return false;
     const int ar[] = \{2,3,5,7,11,13,17,19,23\};
    forn (j,9)
       if (!es_primo_prob(n,ar[j]))
        return false:
41
     return true;
42
   }
43
   ll rho(ll n){
       if((n & 1) == 0) return 2:
       11 x = 2 , y = 2 , d = 1;
       ll c = rand() % n + 1;
       while(d == 1){
           x = (mulmod(x, x, n) + c)%n;
           y = (mulmod(y, y, n) + c)%n;
           y = (mulmod( y , y , n ) + c)%n;
          if(x - y \ge 0) d = gcd(x - y, n);
           else d = gcd(v - x, n);
54
55
       return d==n? rho(n):d;
56
57
58
   map<11,11> prim;
   void factRho (ll n){ //O (lg n)^3. un solo numero
    if (n == 1) return:
    if (rabin(n)){
       prim[n]++;
       return;
65
    11 factor = rho(n);
    factRho(factor);
    factRho(n/factor);
69 }
```

return L;

30

6.15 GCD

```
tipo gcd(tipo a, tipo b){return a?gcd(b %a, a):b;}
                        6.16 Extended Euclid
  number ext_gcd(number a, number b, number &x, number &y){
     if(b == 0) {
       x = 1; y = 0; return a;
4
     number g = ext_gcd(b,a % b,y,x);
     y = a / b * x;
     return g;
8
   pair<number, number> solve(number a, number b, number c, number n,
       number m, number g, number tk) {
     pair<number, number> ans(LLONG_MAX, LLONG_MAX);
     for (number k = tk - 3; k < tk + 3; k++) {
11
       number x = (n * c) / g + (b * k) / g;
12
       number y = (m * c) / g - (a * k) / g;
13
       if (x >= 1 \&\& y >= 1)
14
         ans = min(ans, mp(x, y));
15
     }
16
     return ans;
17
18
   int main() {
19
     //Encuentra a v b de a*x + b*x = c
20
     //tal que a > 0 && b > 0 y minimiza (a, b)
21
     number a, b, c;
22
     scanf("%lld, %lld, %lld", &a, &b, &c);
     number n, m;
24
     number g = ext_gcd(a, b, n, m);
25
     number L = (g - n * c) / b, R = (m * c - g) / a;
     auto ans =min(solve(a, b, c, n, m, g, L), solve(a, b, c, n, m, g, R));
     printf("%lld\\n", ans.first, ans.second);
     return 0:
29
30 }
                               6.17 LCM
tipo lcm(tipo a, tipo b){return a / gcd(a,b) * b;}
```

6.18 Inversos

```
1 #define MAXMOD 15485867
1 ll inv[MAXMOD];//inv[i]*i=1 mod MOD
  void calc(int p){\frac{1}{0}}
    inv[1]=1;
    forr(i, 2, p) inv[i] = p-((p/i)*inv[p\%i])\%p;
6
   int inverso(int x){\frac{1}{0(\log x)}}
     return expmod(x, eulerphi(MOD)-2);//si mod no es primo(sacar a mano)
     return expmod(x, MOD-2);//si mod es primo
10 }
                             6.19 Simpson
double integral(double a, double b, int n=10000) {//O(n), n=cantdiv
     double area=0, h=(b-a)/n, fa=f(a), fb;
    forn(i, n){
    fb=f(a+h*(i+1));
       area+=fa+ 4*f(a+h*(i+0.5)) +fb, fa=fb;
5
6
    return area*h/6.;}
   //////////////OTRA IMPLEMENTACION////////
   double a[12]:
   int n;
   //la funcion puede ser un polinomio
   double f(double x){
    double ans = 0:
    for(int i = 0; i <= n; i++)
       ans += (a[i] * pow(x,i));
     return ans*ans*PI;
16
17
   double S(double a, double b, double c, double h){
     return (h / 3.0) * (f(a) + 4.0 * f(c) + f(b));
19
20
   double SIMP(double a, double b, double E ){
21
     double h = (b-a)/2.0,
22
            c = (b+a)/2.0;
23
     double a1 = a, b1 = c,
24
            a2 = c, b2 = b:
25
     double c1 = (b1+a1)/2.0,
26
            c2 = (b2+a2)/2.0:
27
     double L = (S(a1,b1, c1,h) + S(a2,b2,c2,h)) / 2.0;
28
     if(0.1*abs(L-S(a,b,c,h)) < E)
29
```

```
else
                                                                                            vector<tipo> res(m+n-1);
31
                                                                                 12
                                                                                            forn(i, m) forn(j, n) res[i+j]+=c[i]*o.c[j];
       return SIMP(a1,b1, E/2.0) + SIMP(a2,b2, E/2.0);
32
                                                                                 13
33 }
                                                                                            return poly(res); }
                                                                                 14
                                                                                       tipo eval(tipo v) {
                                                                                 15
                              6.20 Fraction
                                                                                        tipo sum = 0;
                                                                                 16
                                                                                        dforn(i, sz(c)) sum=sum*v + c[i];
                                                                                 17
   tipo mcd(tipo a, tipo b){return a?mcd(b%a, a):b;}
                                                                                        return sum; }
                                                                                 18
   struct frac{
                                                                                        //poly contains only a vector<int> c (the coeficients)
     tipo p,q;
3
                                                                                      //the following function generates the roots of the polynomial
     frac(tipo p=0, tipo q=1):p(p),q(q) {norm();}
4
                                                                                     //it can be easily modified to return float roots
     void norm(){
5
                                                                                      set<tipo> roots(){
                                                                                 22
       tipo a = mcd(p,q);
6
                                                                                        set<tipo> roots;
                                                                                 23
       if(a) p/=a, q/=a;
                                                                                        tipo a0 = abs(c[0]), an = abs(c[sz(c)-1]);
                                                                                 24
       else q=1;
8
                                                                                        vector<tipo> ps,qs;
                                                                                 25
       if (q<0) q=-q, p=-p;}
9
                                                                                        forr(p,1,sqrt(a0)+1) if (a0\%p==0) ps.pb(p),ps.pb(a0/p);
                                                                                 26
     frac operator+(const frac& o){
10
                                                                                        forr(q,1,sqrt(an)+1) if (an/q==0) qs.pb(q),qs.pb(an/q);
                                                                                 27
       tipo a = mcd(q, o.q);
11
                                                                                        forall(pt,ps)
                                                                                 28
       return frac(p*(o.q/a)+o.p*(q/a), q*(o.q/a));}
12
                                                                                          forall(qt,qs) if ( (*pt) % (*qt)==0 ) {
     frac operator-(const frac& o){
13
                                                                                            tipo root = abs((*pt) / (*qt));
                                                                                 30
       tipo a = mcd(q, o.q);
14
                                                                                            if (eval(root)==0) roots.insert(root);
                                                                                 31
       return frac(p*(o.q/a)-o.p*(q/a), q*(o.q/a));}
15
                                                                                 32
     frac operator*(frac o){
16
                                                                                        return roots; }
                                                                                 33
       tipo a = mcd(q, o.p), b = mcd(o.q, p);
17
                                                                                    };
                                                                                 34
       return frac((p/b)*(o.p/a), (q/a)*(o.q/b));}
18
                                                                                    pair<poly,tipo> ruffini(const poly p, tipo r) {
     frac operator/(frac o){
19
                                                                                      int n = sz(p.c) - 1;
                                                                                 36
       tipo a = mcd(q,o.q), b = mcd(o.p,p);
20
                                                                                      vector<tipo> b(n);
                                                                                 37
       return frac((p/b)*(o.q/a),(q/a)*(o.p/b));}
^{21}
                                                                                      b[n-1] = p.c[n];
                                                                                 38
     bool operator<(const frac &o) const{return p*o.g < o.p*g;}</pre>
22
                                                                                      dforn(k,n-1) b[k] = p.c[k+1] + r*b[k+1];
                                                                                 39
     bool operator==(frac o){return p==o.p&kq==o.q;}
23
                                                                                      tipo resto = p.c[0] + r*b[0];
                                                                                 40
24 };
                                                                                      poly result(b);
                                                                                 41
                                                                                      return make_pair(result,resto);
                             6.21 Polinomio
                                                                                 42
                                                                                 43
                                                                                    poly interpolate(const vector<tipo>& x,const vector<tipo>& y) {
           int m = sz(c), n = sz(o.c);
                                                                                 44
1
           vector<tipo> res(max(m,n));
                                                                                        poly A; A.c.pb(1);
2
                                                                                        forn(i,sz(x)) { poly aux; aux.c.pb(-x[i]), aux.c.pb(1), A = A * aux;
           forn(i, m) res[i] += c[i];
                                                                                 46
3
           forn(i, n) res[i] += o.c[i];
                                                                                      poly S; S.c.pb(0);
           return poly(res); }
                                                                                 47
5
                                                                                      forn(i,sz(x)) { poly Li;
       poly operator*(const tipo cons) const {
6
                                                                                        Li = ruffini(A,x[i]).fst;
       vector<tipo> res(sz(c));
7
                                                                                        Li = Li * (1.0 / Li.eval(x[i])); // here put a multiple of the
           forn(i, sz(c)) res[i]=c[i]*cons;
8
                                                                                            coefficients instead of 1.0 to avoid using double
           return poly(res); }
9
                                                                                        S = S + Li * y[i]; }
       poly operator*(const poly &o) const {
                                                                                 51
10
                                                                                      return S;
           int m = sz(c), n = sz(o.c);
                                                                                 52
11
```

return true;

```
34 }
54
   int main(){
55
     return 0;
56
  |}
57
                                                                                   2
                            6.22 Ec. Lineales
  |bool resolver_ev(Mat a, Vec y, Vec &x, Mat &ev){
                                                                                      Complexity: O(N^1.7)
     int n = a.size(), m = n?a[0].size():0, rw = min(n, m);
2
     vector<int> p; forn(i,m) p.push_back(i);
     forn(i, rw) {
       int uc=i, uf=i;
                                                                                      */
                                                                                   9
5
       forr(f, i, n) forr(c, i, m) if(fabs(a[f][c])>fabs(a[uf][uc])) {uf=f;
                                                                                   10
           uc=c;}
                                                                                      int p,k;
       if (feg(a[uf][uc], 0)) { rw = i; break; }
                                                                                      vector<int> b,r;
7
       forn(j, n) swap(a[j][i], a[j][uc]);
8
       swap(a[i], a[uf]); swap(y[i], y[uf]); swap(p[i], p[uc]);
                                                                                      void trim(vector<int>& a){
9
       tipo inv = 1 / a[i][i]; //aca divide
                                                                                   15
       forr(j, i+1, n) {
                                                                                      }
                                                                                   16
         tipo v = a[j][i] * inv;
                                                                                   17
12
         forr(k, i, m) a[j][k]-=v * a[i][k];
13
         y[j] = v*y[i];
14
                                                                                   19
15
                                                                                   20
     } // rw = rango(a), aca la matriz esta triangulada
                                                                                   21
16
     forr(i, rw, n) if (!feg(y[i],0)) return false; // checkeo de
                                                                                                   c[i+j] += a[i] * b[j];
                                                                                   22
17
         compatibilidad
                                                                                              }
                                                                                   23
     x = vector < tipo > (m, 0);
                                                                                   24
18
     dforn(i, rw){
                                                                                          trim(c);
                                                                                   25
19
       tipo s = v[i];
                                                                                          return c;
                                                                                   26
20
       forr(j, i+1, rw) s -= a[i][j]*x[p[j]];
                                                                                      }
                                                                                   27
21
       x[p[i]] = s / a[i][i]; //aca divide
                                                                                      // a = a + b*(10^k)
22
23
     ev = Mat(m-rw, Vec(m, 0)); // Esta parte va SOLO si se necesita el ev
                                                                                   30
24
     forn(k, m-rw) {
                                                                                   31
25
       ev[k][p[k+rw]] = 1;
                                                                                      }
                                                                                   32
26
       dforn(i, rw){
                                                                                   33
27
         tipo s = -a[i][k+rw];
                                                                                   34
28
         forr(j, i+1, rw) s -= a[i][j]*ev[k][p[j]];
                                                                                      }
                                                                                   35
29
         ev[k][p[i]] = s / a[i][i]; //aca divide
                                                                                      // a = a + b
30
       }
31
     }
32
```

6.23 Karatsuba

```
1 // g++ -std=c++11 "karatsuba.cpp" -o hld
   ========= <karatsuba> =============
   Call to karatsuba function paramter two vectors
   * INPUT: two vectors A,B cointains the coeficients of the polynomail
   * OUTPUT a vector coitains the coeficients of A * B
       while (a.size() > 0 \&\& a.back() == 0) a.pop_back();
   vector<int> multiply(const vector<int>& a, const vector<int>& b){
       vector<int> c(a.size() + b.size() + 1, 0);
       for (int i = 0: i < a.size(): i++) {
           for (int j = 0; j < b.size(); j++) {
   void addTo(vector<int>& a, const vector<int>& b, int k){
       if (a.size() < b.size() + k) a.resize(b.size() + k);</pre>
       for (int i = 0; i < b.size(); i++) a[i+k] += b[i];
   void subFrom(vector<int>& a, const vector<int>& b){
       for (int i = 0; i < b.size(); i++) a[i] -= b[i];
   void addTo(vector<int>& a, const vector<int>& b){
       addTo(a, b, 0);
38
39 }
```

 $for(int i = 0; i < n; ++i){$

10

```
vector<int> karatsuba(const vector<int>& a, const vector<int>& b)
                                                                                                int rev = 0:
                                                                                    11
   {
                                                                                                for(int j = 0; j < p; ++j){
41
                                                                                    12
       int alen = a.size();
                                                                                                    rev <<= 1;
                                                                                    13
42
       int blen = b.size();
                                                                                                    rev |= ((i >> j) & 1);
                                                                                    14
43
       if (alen == 0 || blen == 0) return vector<int>();
                                                                                                }
                                                                                     15
44
       if (alen < blen) return karatsuba(b, a);</pre>
                                                                                                A[i] = a[rev];
45
                                                                                     16
       if (alen < 50) return multiply(a, b);</pre>
                                                                                            }
                                                                                     17
46
                                                                                     18
47
       int half = alen / 2;
                                                                                            Complex w,wn;
48
                                                                                    19
       vector<int> a0(a.begin(), a.begin() + half);
49
                                                                                    20
       vector<int> a1(a.begin() + half, a.end());
                                                                                            for(int i = 1; i \le p; ++i){
                                                                                    21
50
                                                                                                int M = (1 << i), K = (M >> 1);
       vector<int> b0(b.begin(), b.begin() + min<int>(blen, half));
                                                                                    22
51
       vector<int> b1(b.begin() + min<int>(blen, half), b.end());
                                                                                                wn = Complex(cos(s*2.0*M_PI/(double)M), sin(s*2.0*M_PI/(double)M
                                                                                    23
52
                                                                                                     ));
53
       vector<int> z0 = karatsuba(a0, b0);
                                                                                    24
54
       vector<int> z2 = karatsuba(a1, b1);
                                                                                                for(int j = 0; j < n; j += M){
                                                                                    25
55
       addTo(a0, a1);
                                                                                                     w = Complex(1.0, 0.0);
56
                                                                                    26
       addTo(b0, b1);
                                                                                                    for(int l = j; 1 < K + j; ++1){
57
                                                                                                         Complex t = w;
       vector<int> z1 = karatsuba(a0, b0):
                                                                                    28
58
       subFrom(z1, z0);
                                                                                                         t *= A[1 + K];
59
       subFrom(z1, z2);
                                                                                                         Complex u = A[1];
60
                                                                                                         A[1] += t;
61
       vector<int> res;
                                                                                                         u -= t;
                                                                                    32
62
       addTo(res, z0);
                                                                                                         A[1 + K] = u;
63
       addTo(res, z1, half);
                                                                                                         w = wn;
                                                                                    34
64
       addTo(res, z2, half + half);
                                                                                                    }
                                                                                    35
65
                                                                                                }
                                                                                    36
66
       trim(res);
                                                                                            }
67
                                                                                    37
       return res;
                                                                                    38
68
69 }
                                                                                            if(s==-1){
                                                                                                for(int i = 0; i < n; ++i)
                                                                                    40
                                 6.24 FFT
                                                                                                     A[i] /= (double)n;
                                                                                    41
                                                                                            }
                                                                                     42
                                                                                        }
   #define lowbit(x) (((x) ^ (x-1)) & (x))
                                                                                     43
   typedef complex<long double> Complex;
                                                                                        vector<Complex> FFT_Multiply(vector<Complex> &P, vector<Complex> &Q){
                                                                                            int n = P.size()+Q.size();
                                                                                     46
   void FFT(vector<Complex> &A, int s){
                                                                                            while(n!=lowbit(n)) n += lowbit(n):
       int n = A.size():
                                                                                    47
5
       int p = __builtin_ctz(n);
6
                                                                                            P.resize(n,0);
                                                                                    49
7
                                                                                            Q.resize(n,0);
       vector<Complex> a = A;
                                                                                    50
8
                                                                                    51
9
```

FFT(P,1);

52

```
FFT(Q,1);
53
54
       vector<Complex> R;
55
       for(int i=0;i<n;i++) R.push_back(P[i]*Q[i]);</pre>
56
57
       FFT(R,-1);
58
59
       return R;
60
61
62
    // Para multiplicacion de enteros grandes
   const long long B = 100000;
   const int D = 5:
```

6.25 Tablas y cotas (Primos, Divisores, Factoriales, etc)

```
Factoriales
0! = 1
                  11! = 39.916.800
1! = 1
                  12! = 479.001.600 \ (\in int)
2! = 2
                  13! = 6.227.020.800
3! = 6
                  14! = 87.178.291.200
4! = 24
                  15! = 1.307.674.368.000
5! = 120
                  16! = 20.922.789.888.000
6! = 720
                  17! = 355.687.428.096.000
7! = 5.040
                  18! = 6.402.373.705.728.000
8! = 40.320
                  19! = 121.645.100.408.832.000
9! = 362.880
                  20! = 2.432.902.008.176.640.000 ( \in tint)
10! = 3.628.800 \mid 21! = 51.090.942.171.709.400.000
       max signed tint = 9.223.372.036.854.775.807
     max unsigned tint = 18.446.744.073.709.551.615
```

Primos

 $\begin{array}{c} 2\ 3\ 5\ 7\ 11\ 13\ 17\ 19\ 23\ 29\ 31\ 37\ 41\ 43\ 47\ 53\ 59\ 61\ 67\ 71\ 73\ 79\ 83\ 89\ 97\ 101\ 103\ 107\ 109\\ 113\ 127\ 131\ 137\ 139\ 149\ 151\ 157\ 163\ 167\ 173\ 179\ 181\ 191\ 193\ 197\ 199\ 211\ 223\ 227\\ 229\ 233\ 239\ 241\ 251\ 257\ 263\ 269\ 271\ 277\ 281\ 283\ 293\ 307\ 311\ 313\ 317\ 331\ 337\ 347\\ 349\ 353\ 359\ 367\ 373\ 379\ 383\ 389\ 397\ 401\ 409\ 419\ 421\ 431\ 433\ 439\ 443\ 449\ 457\ 461\\ 463\ 467\ 479\ 487\ 491\ 499\ 503\ 509\ 521\ 523\ 541\ 547\ 557\ 563\ 569\ 571\ 577\ 587\ 593\ 599\\ 601\ 607\ 613\ 617\ 619\ 631\ 641\ 643\ 647\ 653\ 659\ 661\ 673\ 677\ 683\ 691\ 701\ 709\ 719\ 727\\ 733\ 739\ 743\ 751\ 757\ 761\ 769\ 773\ 787\ 797\ 809\ 811\ 821\ 823\ 827\ 829\ 839\ 853\ 857\ 859\\ 863\ 877\ 881\ 883\ 887\ 907\ 911\ 919\ 929\ 937\ 941\ 947\ 953\ 967\ 971\ 977\ 983\ 991\ 997\ 1009\\ 1013\ 1019\ 1021\ 1031\ 1033\ 1039\ 1049\ 1051\ 1061\ 1063\ 1069\ 1087\ 1091\ 1093\ 1097\ 1103\\ 1109\ 1117\ 1123\ 1129\ 1151\ 1153\ 1163\ 1171\ 1181\ 1187\ 1193\ 1201\ 1213\ 1217\ 1223\ 1229\\ 1231\ 1237\ 1249\ 1259\ 1277\ 1279\ 1283\ 1289\ 1291\ 1297\ 1301\ 1303\ 1307\ 1319\ 1321\ 1327\\ 1361\ 1367\ 1373\ 1381\ 1399\ 1409\ 1423\ 1427\ 1429\ 1433\ 1439\ 1447\ 1451\ 1451\ 1453\ 1459\ 1471\\ \end{array}$

 $1481\ 1483\ 1487\ 1489\ 1493\ 1499\ 1511\ 1523\ 1531\ 1543\ 1549\ 1553\ 1559\ 1567\ 1571\ 1579$ $1583\ 1597\ 1601\ 1607\ 1609\ 1613\ 1619\ 1621\ 1627\ 1637\ 1657\ 1663\ 1667\ 1669\ 1693\ 1697$ $1699\ 1709\ 1721\ 1723\ 1733\ 1741\ 1747\ 1753\ 1759\ 1777\ 1783\ 1787\ 1789\ 1801\ 1811\ 1823$ $1847\ 1861\ 1867\ 1871\ 1873\ 1877\ 1879\ 1889\ 1901\ 1907\ 1913\ 1931\ 1933\ 1949\ 1951$ $1973\ 1979\ 1987\ 1993\ 1997\ 1999\ 2003\ 2011\ 2017\ 2027\ 2029\ 2039\ 2053\ 2063\ 2069\ 2081$

Primos cercanos a 10^n

 $\begin{array}{c} 9941\ 9949\ 9967\ 9973\ 10007\ 10009\ 10037\ 10039\ 10061\ 10067\ 10069\ 10079\\ 99961\ 99971\ 99989\ 99991\ 100003\ 100019\ 1000033\ 1000037\ 1000039\\ 9999943\ 9999971\ 99999991\ 10000019\ 10000079\ 10000103\ 10000121\\ 99999941\ 99999959\ 99999971\ 99999989\ 100000007\ 100000037\ 100000039\ 100000049\\ 99999893\ 99999929\ 99999937\ 1000000007\ 1000000009\ 1000000021\ 1000000033\\ \end{array}$

Cantidad de primos menores que 10^n

```
\pi(10^1) = 4; \pi(10^2) = 25; \pi(10^3) = 168; \pi(10^4) = 1229; \pi(10^5) = 9592

\pi(10^6) = 78.498; \pi(10^7) = 664.579; \pi(10^8) = 5.761.455; \pi(10^9) = 50.847.534

\pi(10^{10}) = 455.052,511; \pi(10^{11}) = 4.118.054.813; \pi(10^{12}) = 37.607.912.018
```

Divisores

```
Cantidad de divisores (\sigma_0) para algunos n/\neg \exists n' < n, \sigma_0(n') \geqslant \sigma_0(n)
       \sigma_0(60) = 12; \sigma_0(120) = 16; \sigma_0(180) = 18; \sigma_0(240) = 20; \sigma_0(360) = 24
    \sigma_0(720) = 30; \sigma_0(840) = 32; \sigma_0(1260) = 36; \sigma_0(1680) = 40; \sigma_0(10080) = 72
        \sigma_0(15120) = 80; \sigma_0(50400) = 108; \sigma_0(83160) = 128; \sigma_0(110880) = 144
    \sigma_0(498960) = 200; \sigma_0(554400) = 216; \sigma_0(1081080) = 256; \sigma_0(1441440) = 288
                            \sigma_0(4324320) = 384 : \sigma_0(8648640) = 448
             Suma de divisores (\sigma_1) para algunos n/\neg \exists n' < n, \sigma_1(n') \ge \sigma_1(n)
    \sigma_1(96) = 252; \sigma_1(108) = 280; \sigma_1(120) = 360; \sigma_1(144) = 403; \sigma_1(168) = 480
        \sigma_1(960) = 3048; \sigma_1(1008) = 3224; \sigma_1(1080) = 3600; \sigma_1(1200) = 3844
     \sigma_1(4620) = 16128; \sigma_1(4680) = 16380; \sigma_1(5040) = 19344; \sigma_1(5760) = 19890
   \sigma_1(8820) = 31122; \sigma_1(9240) = 34560; \sigma_1(10080) = 39312; \sigma_1(10920) = 40320
\sigma_1(32760) = 131040; \sigma_1(35280) = 137826; \sigma_1(36960) = 145152; \sigma_1(37800) = 148800
\sigma_1(60480) = 243840; \sigma_1(64680) = 246240; \sigma_1(65520) = 270816; \sigma_1(70560) = 280098
            \sigma_1(95760) = 386880; \sigma_1(98280) = 403200; \sigma_1(100800) = 409448
        \sigma_1(491400) = 2083200; \sigma_1(498960) = 2160576; \sigma_1(514080) = 2177280
        \sigma_1(982800) = 4305280; \sigma_1(997920) = 4390848; \sigma_1(1048320) = 4464096
    \sigma_1(4979520) = 22189440; \sigma_1(4989600) = 22686048; \sigma_1(5045040) = 23154768
    \sigma_1(9896040) = 44323200; \sigma_1(9959040) = 44553600; \sigma_1(9979200) = 45732192
```

7 Grafos

7.1 Bellman-Ford

```
int negative_cycle(vector<vector<int> > &G, vector<vector<int> > &cost)
       {
     //write your code here
2
     bool nc = false;
3
     int n = G.size();
     vector<int>dist(n,INT_MAX / 2);
     dist[0] = 0;
     for(int i = 0; i < n - 1; i++)
     for(int u = 0; u < n; u++)
       for(int j = 0; j < G[u].size();j++){</pre>
9
         int v = G[u][j];
10
         int w = cost[u][j];
11
         dist[v] = min(dist[v], dist[u] + w);
12
       }
13
     for(int u = 0; u < n; u++){
14
     for(int j = 0; j < G[u].size();j++){</pre>
15
       int v = G[u][j];
16
       int w = cost[u][i];
       if(dist[v] > dist[u] + w)nc = true;
18
     }
19
     }
20
     return nc;
21
22 | }
```

7.2 dijkstra grafos densos

7.3 2 SAT definitivamente no con Tarjan

```
// g++ -std=c++11 "twosat.cpp" -o run
/***

Complexity: O(N)

Input: number of variables, then number of clause clauses in format (u or v)

if u,v > 0 then is equivalent to u,v

if u,v < 0 then is equivalent to u , v

Output: UNSATISFIABLE can't find a solution

SATISFIABLE if exist a solution then print the assignment of all variables (negative for xi = false)</pre>
```

```
11 Examples:
   Input:
   3 3
   1 -3
   -1 2
   -2 -3
   Output
   SATISFIABLE
   1 2 -3
   *
   Input
   1 2
  1 1
   -1 -1
   Output
   UNSATISFIABLE
   #include <bits/stdc++.h>
   using namespace std;
   vector<int>G[2][2000010],G2[2000010];
   int n, m;
   int scc[2000010];
   bool vis[2000010];
   vector<int>comp[2000010];
   int assign[2000010];
   int cc = 0;
   stack<int>st;
   vector<int>sta;
   void dfs(int u,int type){
    if(scc[u] != -1)return;
     scc[u] = cc;
41
    for(int v:G[type][u]){
       dfs(v,type);
43
     }
44
     if(!type)st.push(u);
45
46
   void topo(int u){
47
     if(vis[u])return:
     vis[u] = true;
     for(int v:G2[u])topo(v);
     sta.push_back(u);
51
52
  void buildGraphWitouthLoop(){
```

```
for(int i = 0; i < 2 * n; i++){
                                                                                         if(!vis[i])topo(i);
54
                                                                                  97
       for(int j = 0; j < G[0][i].size(); j++){</pre>
                                                                                  98
55
         if(scc[i] != scc[G[0][i][j]])
                                                                                       for(int u:sta){//inverse of topological sort
56
                                                                                  99
           G2[scc[i]].push_back(scc[G[0][i][j]]);
                                                                                         for(int v:comp[u]){//transitivite Skew-Symmetry
57
                                                                                  100
       }
                                                                                            if(!assign[v]){
                                                                                  101
58
                                                                                              assign[v] = 1;
59
                                                                                  102
                                                                                              assign[v ^ 1] = -1;
60
                                                                                  103
   int main() {
61
                                                                                  104
       ios::sync_with_stdio(false);cin.tie(0);
                                                                                         }
62
                                                                                  105
       cin >> n >> m;
63
                                                                                  106
       for(int i = 0, u, v; i < m; i++){
                                                                                       for(int i = 0, j = 1; i < 2 * n; i += 2, j++){
                                                                                  107
64
                                                                                         cout << (j) * (assign[i]) << "";
       cin >> u >> v;
65
                                                                                  108
       int uu = (u > 0?(u - 1) * 2:(-u - 1) * 2 + 1):
                                                                                       }
                                                                                  109
       int vv = (v > 0?(v - 1) * 2:(-v - 1) * 2 + 1);
                                                                                         return 0;
                                                                                  110
     // cout << uu << " " << (uu ^ 1) << "\n";
                                                                                 111 }
68
       G[0][uu ^ 1].push_back(vv);
69
                                                                                         7.4 Articulataion Points (desgraciadamente tarjan)
       G[0][vv ^ 1].push_back(uu);
70
       G[1][vv].push_back(uu ^ 1);
71
       G[1] [uu] .push_back(vv ^ 1);
                                                                                   1 // g++ -std=c++11 "articulationpointsandbridges.cpp" -o run
72
73
     memset(scc,-1,sizeof scc);
                                                                                     ========= <Articulation points and bridges c++ version>
74
     for(int i = 0; i < 2 * n; i++){
75
                                                                                         _____
       if(scc[i] == -1)dfs(i,0);
                                                                                   4 Given a graph return a vector of paris with the bridges and a bool array
76
77
     memset(scc,-1,sizeof scc);
                                                                                   true if the node is an articulation point
78
     while(!st.empty()){
                                                                                     * false otherwise
79
       int u = st.top();st.pop();
                                                                                     Graph nodes: 0 to N - 1
80
       if(scc[u] == -1){
                                                                                     */
81
         dfs(u,1);
                                                                                     using namespace std;
82
         cc++;
                                                                                     vector<int>G[10010];
83
       }
                                                                                     int low[10010],num[10010],parent[10010],cc;
84
85
                                                                                     //cc is my timer
     bool unsat = false:
                                                                                     int art[10010];//bool for detect art point, int for detect how many
86
     for(int i = 0; i < 2 * n; i++){
                                                                                         nodes are connected to my articulation point
87
       if(scc[i] == scc[i ^ 1])unsat = true;
                                                                                  int root,rC;
88
       comp[scc[i]].push_back(i);
                                                                                     int n;
89
                                                                                  15
     }
90
                                                                                     vector<pair<int,int> >bridges;
     if(unsat){
                                                                                     void dfs(int u){
91
       return cout << "UNSATISFIABLE",0;</pre>
                                                                                       low[u]=num[u]=cc++;
92
                                                                                      for(int v:G[u]){
93
     cout << "SATISFIABLE\n";</pre>
                                                                                         if(num[v]==-1){
94
                                                                                  20
     buildGraphWitouthLoop();
                                                                                           parent[v]=u;
95
                                                                                  21
     for(int i = 0; i < 2 * n; i++){
96
                                                                                           if(u==root)rC++;
                                                                                  22
```

```
dfs(v):
23
          if(low[v]>=num[u])art[u]++;//is a articulation point
^{24}
          if(low[v]>num[u])bridges.push_back({u,v});//this is a bridge
25
          low[u] =min(low[u],low[v]);
26
       }
27
       else if(v!=parent[u]){
28
           low[u]=min(low[u],num[v]);
29
30
     }
31
32
   void init(){
33
     bridges.clear();
34
     for(int i=0;i<n;i++){</pre>
35
       art[i]=low[i]=0;
36
       num[i]=parent[i]=-1;
37
       G[i].clear();
38
     }
39
     cc=0;
40
41
    void callARTBRID(){
     for(int i=0;i<n;i++){
43
       if(num[i]==-1){
44
         root=i,rC=0;dfs(i);
45
          art[root]=(rC>1);
46
       }
47
48
49
```

7.5 componentes biconexas y puentes (block cut tree)

```
|int V:
1
   vector<int> G[MAXN];
   int dfn[MAXN],low[MAXN];
   vector< vector<int> > C;
  stack< pair<int, int> > stk;
   void cache_bc(int x, int y){
6
       vector<int> com;
       int tx,ty;
8
       do{
9
           tx = stk.top().first, ty = stk.top().second;
10
           stk.pop();
11
           com.push_back(tx), com.push_back(ty);
12
       }while(tx!=x || ty!=y);
13
```

```
C.push_back(com);
14
   }
15
16
   void DFS(int cur, int prev, int number){
       dfn[cur] = low[cur] = number;
18
       for(int i = G[cur].size()-1;i>=0;--i){}
19
           int next = G[cur][i];
20
           if(next==prev) continue;
21
           if(dfn[next]==-1){
22
                stk.push(make_pair(cur,next));
                DFS(next,cur,number+1);
24
                low[cur] = min(low[cur], low[next]);
25
                if(low[next]>=dfn[cur]) cache_bc(cur,next);
26
           }else low[cur] = min(low[cur],dfn[next]);
27
       }
28
29
30
   void biconn_comp(){
       memset(dfn,-1,sizeof(dfn));
32
       C.clear();
       DFS(0,0,0);
34
       int comp = C.size();
       printf("%d\n",comp);
36
       for(int i = 0; i < comp; ++i){
37
           sort(C[i].begin(),C[i].end());
38
           C[i].erase(unique(C[i].begin(),C[i].end()),C[i].end());
39
           int m = C[i].size();
40
           for(int j = 0; j < m; ++j) printf("%du", 1 + C[i][j]);</pre>
41
           printf("\n");
42
       }
43
44 }
```

7.6 LCA saltitos potencias de 2

```
const int MAXN = 100000;
const int MAXLOG = 23;

//Preprocess:
int par[MAXN] [MAXLOG]; // initially all -1
int h[MAXN];
void dfs(int v,int p = -1){
  par[v][0] = p;
  if(p + 1)
  h[v] = h[p] + 1;
```

```
for(int i = 1;i < MAXLOG;i ++)</pre>
10
       if(par[v][i-1] + 1)
11
         par[v][i] = par[par[v][i-1]][i-1];
12
     for(auto u : adj[v]) if(p - u)
13
       dfs(u,v);
14
15
    //Query:
16
   int LCA(int v,int u){
     if(h[v] < h[u])
18
       swap(v,u);
19
     for(int i = MAXLOG - 1; i \ge 0; i --)
20
       if(par[v][i] + 1 \text{ and } h[par[v][i]] >= h[u])
21
         v = par[v][i];
22
     // now h[v] = h[u]
     if(v == u)
       return v;
25
     for(int i = MAXLOG - 1; i \ge 0; i --)
26
       if(par[v][i] - par[u][i])
27
         v = par[v][i], u = par[u][i];
28
     return par[v][0];
29
30 }
```

7.7 LCA sparse table query O(1)

```
/*Three) Sparse table O(NlogN),O(1)
2 Let's introduce you an order of tree vertices, haas and I named it Euler
        order. It is like DFS order, but every time we enter a vertex, we
      write it's number down (even when we come from a child to this node
      in DFS).*/
  Code for calculate this :
   vector<int> euler;
  void dfs(int v,int p = -1){
5
    euler.push_back(v);
6
    for(auto u : adj[v]) if(p - u)
      dfs(u,v), euler.push_back(v);
8
9
10
  If we have a vector <pair <int,int> > instead of this and push {h[v], v}
      in the vector, and the first time \{h[v], v\} is appeared is s[v] and
      s[v] < s[u] then LCA(v, u) = (mini = s[v]s[u]euler[i])
12 For this propose we can use RMQ problem, and the best algorithm for that
       , is to use Sparse table.*/
```

7.8 HLD

```
1 // g++ -std=c++11 "hld.cpp" -o hld
2
   /***
3
   Complexity: O(N*log (N))
  Given a tree and asociative operation in the paths of this tree ask for
       many querys, and updates
7 in nodes or edges
  Input of this example:
   N number of nodes, then N elements values in each node
  then n - 1 conections
  Q querys if T == 1 query on the path u,v
  else update node U with value val.
   Example problems: Spoj QTREE1 to QTREE6, toby and tree UVA
14
   */
15
   #include <bits/stdc++.h>
   using namespace std;
   const int maxn = 1e5;
   const int NEUTRO = 0; // a null value for my ST
   int vec[maxn]:
   vector<int>G[maxn]; //the graph
   //int idx[maxn]; // case with value in the edge
   int op(int u,int v){// an operation for my path (using ST)
    //return __gcd(u,v);
25
    //return max(u,v);
26
    return u + v;
27
28
29
   //ask to Branimir for information about this
   struct SegmentTree{
     int T[2*maxn];
32
     void init(){
33
       memset(T,0,sizeof T);
34
35
     void set(int pos,int val){
36
      pos += n;
37
      T[pos] = val;
38
       for(pos >>= 1; pos > 0; pos >>=1){
39
        T[pos] = op(T[pos << 1], T[(pos << 1)|1]);
40
```

```
}
                                                                                              tree.set(i,val[i]);
41
                                                                                    84
     }
                                                                                    85
42
     int query(int 1,int r){
                                                                                            */
43
                                                                                    86
       1 += n;
                                                                                         }
44
                                                                                    87
       r += n;
45
                                                                                    88
       int ans = NEUTRO;
46
                                                                                    89
       while (1 < r)
                                                                                         ///init descomposition
47
                                                                                    90
         if (1 \& 1) ans = op(ans, T[1++]);
                                                                                         void dfs(int u,int pu){
48
                                                                                    91
         if (r \& 1) ans = op( ans, T[--r] );
                                                                                            sz[u] = 1; //init the sz of this subtree
49
                                                                                    92
                                                                                            parent[u] = pu; // assign the parent
         1 >>= 1;
50
                                                                                           for(int i = 0; i < G[u].size(); i++){</pre>
         r >>= 1;
51
                                                                                    94
                                                                                              int v = G[u][i];
       }
52
                                                                                    95
                                                                                              if ( v == pu )continue;
       return ans;
53
                                                                                    96
                                                                                              //edgepos[idx[u][i]] = v;
54
                                                                                              depth[v] = depth[u] + 1;
55
   struct hld{
                                                                                              dfs(v,u);
     int ncad; // store actual number of chain
                                                                                              sz[u] += sz[v];
57
                                                                                    100
     int root; // the root of a tree generally 0 or 1
                                                                                           }
58
                                                                                    101
     int pos; // pos of node in chain
                                                                                         }
                                                                                    102
59
                                                                                          //descompose graph in HLD descomposition
                                                                                    103
60
     int sz[maxn]; // store the subsize of subtrees
                                                                                          void descompose(int u){
                                                                                   104
61
                                                                                           if( head[ncad] == -1)head[ncad] = u; // the head of ncad is u
     int depth[maxn]; //depth of the node, useful for LCA via HLD
62
                                                                                    105
     int parent[maxn]; // useful for LCA
                                                                                            where[u] = ncad; // assign where tu node
                                                                                    106
63
     int where[maxn]; // where chain is the node?
                                                                                            //val[pos] = cost; cost another parameter in descompose for graphs
                                                                                    107
64
     //int edgepos[maxn]; // if the value is on the edge: stored in a node
                                                                                                with values in edges
65
     int chainIdx[maxn]; // position in the chain of the node
                                                                                           chainIdx[u] = pos++; //assing pos to this node
                                                                                    108
66
                                                                                           int maxi = -1, sc = -1; //finding a special child
     int head[maxn]; // the head of the i-th chain
                                                                                   109
67
     //int val[maxn]; // if the value is on the edge
                                                                                            for(int v:G[u]){
                                                                                   110
68
                                                                                             if( sz[v] > maxi && where[v] == -1){
     SegmentTree tree; // this ST allow operations in the path
                                                                                   111
69
                                                                                   112
                                                                                                maxi = sz[v]:
70
     void init(){//settings value, and process de HLD
                                                                                                sc = v;
                                                                                   113
71
                                                                                             }
       root = 0;
                                                                                   114
72
                                                                                           }
       ncad = 0:
                                                                                   115
73
       pos = 0:
                                                                                            if(sc != -1)descompose(sc);
                                                                                   116
74
       for(int i = 0; i \le n; i++){
                                                                                           //light nodes here:
                                                                                   117
75
         where [i] = head[i] = -1;
                                                                                            for(int v:G[u]){
                                                                                   118
76
       }
                                                                                              if(where[v] == -1){
77
                                                                                   119
       depth[root] = 0:
                                                                                                ncad++:
                                                                                   120
78
       dfs(root , -1);
                                                                                                descompose(v);
                                                                                   121
79
       descompose(root);
                                                                                   122
80
       tree.init();
                                                                                           }
                                                                                   123
81
       /* case with values in edges
                                                                                   124
82
       for(int i=0;i<n;i++){</pre>
                                                                                         ///end descomposition
83
```

```
126
      int lca(int u,int v){
127
        while(where[u]!=where[v]){
128
          if(depth[ head[ where[u] ] ] > depth[ head[ where[v] ] ])u =
129
              parent[ head[ where[u] ] ];
          else v = parent[ head[ where[v] ] ];
130
131
        return depth[u] < depth[v] ? u:v;</pre>
132
133
134
      void update(int u, int val){
135
        tree.set(chainIdx[u],val);
136
      }
137
138
      int query(int u,int v){
139
        // if ( u == v) return NEUTRO; value in edges
140
        int vChain = where[v];
141
        int ans = NEUTRO;
142
        while(true){
143
          int uChain = where[u];
144
          if(uChain == vChain){
145
            // return op(ans, tree.query( chainIdx[v] + 1, chainIdx[u] + 1)
146
                 ); value in edges
            return op(ans, tree.query( chainIdx[v], chainIdx[u] + 1) );
147
148
          int hu = head[uChain];
149
          ans = op( ans, tree.query(chainIdx[hu], chainIdx[u] + 1) );
150
          u = parent[hu];
151
        }
152
      }
153
154
      int Q(int u,int v){
155
        int L = lca(u,v):
156
        return op( query(u,L) , query(v,L) );
157
      }
158
    }HLD;
159
    int main(){
160
      //ios::sync_with_stdio(false);cin.tie(0);
161
      while(cin >> n){
162
        for(int i = 0; i < n; i++)G[i].clear();
163
        for(int i = 0; i < n; i++){
164
          cin >> vec[i];
165
        }
166
```

```
for(int i = 1, u,v ; i < n; i++){
167
          cin >> u >> v;
168
          G[u].push_back(v);
169
          G[v].push_back(u);
170
          /* case with value in edges
171
           G[u].push_back(make_pair(v,w));
172
          idx[u].push_back(i-1);
173
          G[v].push_back(make_pair(u,w));
174
          idx[v].push_back(i-1);
175
176
177
        }
178
        HLD.init();
179
        for(int i = 0; i < n; i++){
          HLD.update(i, vec[i]);
181
        }
182
        int question;
183
        cin >> question;
        for(int i = 0, t, u ,v; i < question; i++){
185
          cin >> t >> u >> v;
          if(t == 1){
187
            cout << HLD.Q(u,v) << "\n";
188
          }
189
          else HLD.update(u,v);
190
191
192
193 }
```

7.9 centroid descomposition

```
const int MAXN = 100010;
vector<int> g[MAXN];
int ID[MAXN];
int cnt[MAXN];
int contar(int u, int parent) {
  if (ID[u] != -1) return cnt[u] = 0;
  cnt[u] = 1;
  for (int v: g[u])
   if (v != parent)
      cnt[u] += contar(v, u);
  return cnt[u];
}
```

```
int get_centroid(int u, int parent, int size) {
     for (int v: g[u])
15
       if (v != parent)
16
         if (cnt[v] > (size / 2))
17
           return get_centroid(v, u, size);
18
     return u;
19
20
   void dfs(int u, int id) {
     contar(u, -1);
^{22}
     int centroid = get_centroid(u, -1, cnt[u]);
23
     ID[centroid] = id;
24
     for (int v: g[centroid])
25
       if (ID[v] == -1)
         dfs(v, id + 1);
27
28
29
   int main() {
30
     memset(ID, -1, sizeof(ID));//No olvidar esta linea
31
     //el arbol es conexo
32
     //iniciar con "dfs(nodoqueexiste, 0)"
33
     dfs(0, 0);
34
     /*
35
       Esta implementacin halla el centroide y elimina el centroide
36
       y halla el centroide de los subarboles(recursivamente)
37
       Complejidad: O(N Log(N))
38
       Si solo se quiere el centroide del arbol
39
       solo llamar a la funcion "get_centroid" una sola vez
40
       "get_centroid(nodoqueexiste, -1, contar(u, -1))"
41
       No olvidar el "contar(u, -1)" para preprocesar tama os
42
43
44
     return 0;
45
46 }
```

7.10 euler cycle

```
int n,m,ars[MAXE], eq;
vector<int> G[MAXN];//fill G,n,m,ars,eq
list<int> path;
int used[MAXN];
bool usede[MAXE];
queue<list<int>::iterator> q;
int get(int v){
```

```
while(used[v]<sz(G[v]) && usede[ G[v][used[v]] ]) used[v]++;</pre>
     return used[v];
9
10
   void explore(int v, int r, list<int>::iterator it){
     int ar=G[v][get(v)]; int u=v^ars[ar];
12
     usede[ar]=true;
13
     list<int>::iterator it2=path.insert(it, u);
14
     if(u!=r) explore(u, r, it2);
     if(get(v)<sz(G[v])) q.push(it);</pre>
   }
17
   void euler(){
18
     zero(used), zero(usede);
     path.clear();
20
     q=queue<list<int>::iterator>();
21
     path.push_back(0); q.push(path.begin());
22
     while(sz(q)){
23
       list<int>::iterator it=q.front(); q.pop();
       if(used[*it]<sz(G[*it])) explore(*it, *it, it);</pre>
25
26
     reverse(path.begin(), path.end());
27
28
   void addEdge(int u, int v){
     G[u].pb(eq), G[v].pb(eq);
30
     ars[eq++]=u^v;
31
32 }
```

7.11 diámetro y centro de un árbol

```
a=min(Queue[L/2-1],Queue[L/2]),b=max(Queue[L/2-1],Queue[L/2]);
  Output:
13
                                                                                        }
                                                                                   57
14
   dfs: calculate the diameter of the tree
                                                                                        return {a,b};
                                                                                   58
   * maxi stores the diameter
                                                                                   59 }
   findingCenters() return the centers
                                                                                                                   algoritmo hungaro
   Nodes in graph 1 to N careful with this
   Complexity: O(N)
                                                                                                          7.13 union find dinámico
19
   */
20
                                                                                    #include <bits/stdc++.h>
21
                                                                                      using namespace std;
22
   vector<int>G[5010];
                                                                                      #define dprint(v) cerr << #v"=" << v << endl //;)
   int maxi=-1,far;
                                                                                      #define forr(i,a,b) for(int i=(a); i<(b); i++)</pre>
   int n:
                                                                                      #define forn(i,n) forr(i,0,n)
25
   int pre[5010];
                                                                                      #define dforn(i,n) for(int i=n-1; i>=0; i--)
   int Queue[5010];
                                                                                      #define forall(it,v) for(auto it=v.begin();it!=v.end();++it)
                                                                                      #define sz(c) ((int)c.size())
28
   void dfs(int path,int u,int parent){
29
                                                                                      #define zero(v) memset(v, 0, sizeof(v))
     pre[u]=parent;
30
                                                                                      #define pb push_back
     if(path>=maxi){
                                                                                      #define fst first
31
       maxi=path;
                                                                                      #define snd second
32
       far=u;
                                                                                      #define mkp make_pair
33
     }
                                                                                      typedef long long 11;
34
     for(int v:G[u]){
                                                                                      typedef pair<int,int> ii;
35
       if(parent!=v){
36
                                                                                   16
         dfs(path+1,v,u);//path + w if the graph as weighted
                                                                                      struct UnionFind {
37
                                                                                   17
                                                                                          int n, comp;
38
                                                                                   18
     }
                                                                                          vector<int> pre,si,c;
39
                                                                                   19
                                                                                          UnionFind(int n=0):n(n), comp(n), pre(n), si(n, 1) {
40
                                                                                   20
   pair<int,int> findingCenters(){
                                                                                              forn(i,n) pre[i] = i; }
41
                                                                                   21
     maxi=-1;
                                                                                          int find(int u){return u==pre[u]?u:find(pre[u]);}
42
                                                                                   22
     dfs(0,1,-1);
                                                                                          bool merge(int u, int v) {
43
                                                                                   23
     dfs(0,far,-1);
                                                                                              if((u=find(u))==(v=find(v))) return false;
44
                                                                                   24
     int t=far.L=0:
                                                                                              if(si[u]<si[v]) swap(u, v);</pre>
45
                                                                                   25
     while(t!=-1){
                                                                                              si[u]+=si[v], pre[v]=u, comp--, c.pb(v);
46
                                                                                   26
       Queue[L]=t;
47
                                                                                              return true;
                                                                                   27
       t=pre[t];
48
                                                                                   28
       ++L;
                                                                                          int snap(){return sz(c);}
49
                                                                                   29
     }
                                                                                          void rollback(int snap){
50
                                                                                   30
     int a=-1,b=-1;
                                                                                              while(sz(c)>snap){
51
                                                                                   31
     if(L&1){
                                                                                                   int v = c.back(); c.pop_back();
52
                                                                                   32
       a=Queue[L/2];
                                                                                                   si[pre[v]] -= si[v], pre[v] = v, comp++;
53
                                                                                   33
     }
                                                                                              }
54
                                                                                   34
     else{
55
                                                                                          }
                                                                                   35
```

```
36 };
   enum {ADD,DEL,QUERY};
   struct Query {int type,u,v;};
   struct DynCon {
       vector<Query> q;
40
       UnionFind dsu;
41
       vector<int> match,res;
42
       map<ii,int> last;//se puede no usar cuando hay identificador para
43
           cada arista (mejora poco)
       DynCon(int n=0):dsu(n){}
44
       void add(int u, int v) {
45
           if(u>v) swap(u,v);
46
           q.pb((Query){ADD, u, v}), match.pb(-1);
47
           last[ii(u,v)] = sz(q)-1;
48
       }
49
       void remove(int u, int v) {
50
           if(u>v) swap(u,v);
51
           q.pb((Query){DEL, u, v});
52
           int prev = last[ii(u,v)];
53
           match[prev] = sz(q)-1;
54
           match.pb(prev);
55
       }
56
       void query() {//podria pasarle un puntero donde guardar la respuesta
57
           q.pb((Query){QUERY, -1, -1}), match.pb(-1);}
58
       void process() {
59
           forn(i,sz(q)) if (q[i].type == ADD && match[i] == -1) match[i] =
60
                sz(q);
           go(0,sz(q));
61
       }
62
       void go(int 1, int r) {
63
           if(l+1==r){
64
               if (q[1].type == QUERY)//Aqui responder la query usando el
65
                    res.pb(dsu.comp);//aqui query=cantidad de componentes
66
                        conexas
               return;
67
68
           int s=dsu.snap(), m = (l+r) / 2;
69
           forr(i,m,r) if(match[i]!=-1 && match[i]<1) dsu.merge(q[i].u, q[i</pre>
70
               ].v);
           go(1,m);
71
           dsu.rollback(s);
72
           s = dsu.snap();
73
```

```
forr(i,1,m) if(match[i]!=-1 && match[i]>=r) dsu.merge(q[i].u, q[
74
                i].v);
            go(m,r);
75
            dsu.rollback(s);
76
       }
   }dc;
78
    // Problema ejemplo: http://codeforces.com/gym/100551/problem/A
81
   int n,k;
83
   int main() {
        //~ freopen("in", "r", stdin);
85
       freopen("connect.in", "r", stdin);
86
       freopen("connect.out", "w", stdout);
87
        ios::sync_with_stdio(0);
        while(cin >> n >> k){
        dc=DynCon(n);
        forn(_,k) { string ord; cin >> ord;
91
          if (ord=="?") {
            dc.query();
93
         } else if (ord=="+") { int a,b; cin>>a>>b; a--;b--;
            dc.add(a,b);
95
         } else if (ord=="-") { int a,b; cin>>a>>b; a--;b--;
96
            dc.remove(a,b);
97
         } else assert(false);
       }
99
            if(!k) continue;//k==0 WTF
100
            dc.process();
101
            forn(i,sz(dc.res)) cout << dc.res[i] << endl;</pre>
102
        }
103
        return 0;
104
105 }
```

7.14 truquitos estúpidos por ejemplo second MST es con LCA 7.15 erdos galloi

```
// g++ -std=c++11 "erdosgalloi.cpp" -o run
/***

Given the grades of each node of a graph return if this form a valid graph
includes: algorithm, functional, numeric, forn
```

```
6 // Receives a sorted degree sequence (non ascending)
   O(NlgN)
9
   bool isGraphicSequence(const vector<int> &seq) // O(n lg n)
11
     vector<int> sum;
12
     int n = seq.size();
13
14
     if (n == 1 \&\& seq[0] != 0) return false;
15
     sum.reserve(n + 1);
17
     sum.push_back(0);
18
     for (int i = 0; i < n; ++i) sum.push_back(sum[i] + seq[i]);
19
     if ((sum[n] \& 1) == 1) return false;
20
21
     for (long long k = 1; k \le n - 1 \&\& seq[k - 1] >= k; ++k) {
22
       int j = distance(seq.begin(), upper_bound(seq.begin() + k, seq.end()
23
           , k,
                                                    greater<int>())) +
24
                1;
25
       long long left = sum[k];
26
       long long right = k * (k - 1) + (j - k - 1) * k + (sum[n] - sum[j - k])
27
           1]);
28
       if (left > right) return false;
29
30
31
     return true;
32
33
```

7.16 grafo funcional hallar k-esimo partiendo de un nodo

7.17 konig

- 7.18 min-vertex cover bipartitos
- 7.19 max-flow (min cost versión)

```
// g++ -std=c++11 "maxflowmincost.cpp" -o run
/***

Given a grapth with edges with a capacity C and weight D

* compute the max-flow min cost
```

```
6 Edmond karps idea
  * Complexity O(v *E*log(v))
  Problem for practice: Dijkstra Dijkstra uva
9
   #define REP(i,j,k) for(int (i)=(j);(i)<(k);++(i))
   #define MP make_pair
   using namespace std;
   #define MAXN 500
   #define MAXM MAXN * 5
   typedef vector<int> VI;
   typedef long long 11;
   const int INF = 1E9; // $infinity$: be careful to make this big enough
       111
   int S; // source
  int T; // sink
  int FN; // number of nodes
  int FM; // number of edges (initialize this to 0)
24 // ra[a]: edges connected to a (NO MATTER WHICH WAY!!!); clear this in
       the beginning
25 VI ra[MAXN];
   int kend[MAXM], cap[MAXM], cost[MAXM]; // size: TWICE the number of
       edges
27
   // Adds an edge from a to b with capacity c and cost d and returns the
       number of the new edge
29
   int addedge(int a, int b, int c, int d) {
     int i = 2*FM:
31
     kend[i] = b;
     cap[i] = c;
     cost[i] = d:
34
     ra[a].push_back(i);
35
    kend[i+1] = a;
36
     cap[i+1] = 0;
     cost[i+1] = -d;
     ra[b].push_back(i+1);
     FM++;
40
     return i;
41
42
   int n;
int dst[MAXM], pre[MAXM], pret[MAXM];
```

```
45 //finding the shortest path via fanding duan, also it works with bellman
   //or dijkstra (careful of negative cycles)
   bool spfa(){
     REP(i,0,FN) dst[i] = INF;
48
     dst[S] = 0;
49
     queue<int> que; que.push(S);
50
     while(!que.empty()){
51
       int x = que.front(); que.pop();
52
       for (int t : ra[x]){
53
         int y = kend[t], nw = dst[x] + cost[t];
54
         if(cap[t] > 0 && nw<dst[y]){
55
            dst[y] = nw; pre[y] = x; pret[y] = t; que.push(y);
         }
57
       }
58
     }
59
     return dst[T]!=INF;
60
61
    // returns the maximum flow and the minimum cost for this flow
    pair<ll,ll> solve(){
     11 \text{ totw} = 0, \text{ totf} = 0;
64
     while(spfa()){
65
       int minflow = INF;
66
       for (int x = T; x!=S; x = pre[x]){
67
         minflow = min(minflow, cap[pret[x]]);
68
       }
69
       for (int x = T; x!=S; x = pre[x]){
70
         cap[pret[x]] -= minflow;
71
         cap[pret[x]^1] += minflow;
72
       }
73
       totf += minflow;
74
       totw += minflow*dst[T];
75
76
     return make_pair(totf, totw);
77
78
    void init(){
79
     FN=4*n+15;//make this big n=number of nodes of the graph
80
     FM=0:
81
     S=0,T=n+1;
82
     for(int i=0;i<FN;i++)ra[i].clear();//clear the graph be careful</pre>
83
84 }
```

7.20 max-flow corto con matriz

```
1 // g++ "maxflowMVEK.cpp" -o run
2 /***
   =========== <Max Flow with matriz Edmonds karp c++ version>
3
   //Given a graph with capacitys find the max-flow
5
   Nodes indexed 1 to N
   * Complexity O(N *E)
   Problem for practice: UVA 820
   */
9
   #define N 500
   int cap[N][N], pre[N], n;
  int s://source
   int t://destination
  bool bfs() {
       queue<int>q;
       q.push(s);
16
       memset(pre,-1,sizeof pre);
       pre[s]=s;
18
       while(!q.empty()){
           int u=q.front();q.pop();
20
           if(u==t)return true;
21
           for(int i=1; i \le n; i++){//nodes 1 to n
22
                if(pre[i] == -1 & cap[u][i])pre[i] = u,q.push(i);
23
           }
24
       }
25
       return false;
26
   }
27
28
   int maxFlow() {
       int mf=0,f,v;//max flow, flow for a path, the vertex
30
       while(bfs()){//while encountered a path source to destination
31
           v=t://min
32
           f=INT_MAX;//make this big enough
33
           while(pre[v]!=v){f=min(f,cap[pre[v]][v]),v=pre[v];}//finding the
34
                 min capacity
           v=t;mf+=f;
35
           while(pre[v]!=v){cap[pre[v]][v]-=f,cap[v][pre[v]]+=f,v=pre[v];}
36
               //update the flow
       }
37
       return mf;
38
39
40 | void init(){
```

```
memset(cap,0,sizeof cap);
                                                                                          int u = q.front();q.pop();
     //cap[u][v]+=capacidad,cap[v][u]+=capacidad
                                                                                          for(int edge:G[u]){
42
                                                                                  38
43 }
                                                                                            int v = kend[edge];
                                                                                  39
                                                                                            if(cap[edge] > 0 && !vis[v]){
                                                                                   40
                       7.21 max-flow sin matriz
                                                                                              vis[v] = true;
                                                                                  41
                                                                                              pre[v] = u;
                                                                                              pret[v] = edge;//the edge store the information
1 // g++ -std=c++11 "maxflowNMEK.cpp" -o run
                                                                                   43
   /***
                                                                                              q.push(v);
2
    ============= <Max Flow with-out matriz Edmonds karp c++ version>
                                                                                   45
   //Given a graph with capacitys find the max-flow
                                                                                   47
                                                                                        return vis[t];
                                                                                   48
   Nodes indexed 1 to N
                                                                                   49
                                                                                      int max flow(){
   * Complexity O(N *E)
                                                                                        int totf = OLL;
   Problem for practice: UVA 820
                                                                                        while(bfs()){
   * Input N number of nodes,
                                                                                          int minflow = INT_MAX;
   * M edges conections
                                                                                          for(int x = t; x != s; x = pre[x]){
   * compute the flow with source 1 and sink N
                                                                                            minflow = min(minflow,cap[pret[x]]);
                                                                                  55
   using namespace std;
                                                                                          for(int x = t; x != s; x = pre[x]){
   const int N = 110;
                                                                                            cap[pret[x]] -= minflow;
   const int M = 10010 * 2;
                                                                                            cap[pret[x] ^ 1] += minflow;
   vector<int>G[N];
                                                                                  59
   int kend[M], cap[M], cost[M];
                                                                                  60
                                                                                          totf += minflow;
   int edge = 0;
                                                                                  61
                                                                                  62
   int s,t;
19
                                                                                        return totf;
   void add(int u,int v,int c){
                                                                                  63
     int forward = edge * 2, backward = edge * 2 + 1;
                                                                                  64
21
     kend[forward] = v;
                                                                                      int main(){
                                                                                  65
22
                                                                                        int n,m;
     cap[forward] = c;
23
                                                                                        \operatorname{scanf}("%d_1%d",\&n,\&m);
     G[u].push_back(forward);
                                                                                  67
24
                                                                                        for(int i = 0,u,v,ca; i < m;i++){
     kend[backward] = u;
25
                                                                                          scanf("%du%du,&u,&v,&ca);
     cap[backward] = 0;
                                                                                  69
26
                                                                                          add(u,v,ca);
     G[v].push_back(backward);
                                                                                  70
27
                                                                                       }
                                                                                  71
     edge++;
28
                                                                                        s = 1, t = n;
29
                                                                                        printf("%lld\n",max_flow());
   int vis[M],pre[M],pret[M];
                                                                                  74 }
   bool bfs(){
31
     for(int i = 0; i <= 100;i++)vis[i] = false;
32
                                                                                                                   7.22 Dinic
     vis[s] = true;
33
     queue<int>q;
34
     q.push(s);
35
                                                                                   1
     while(!q.empty()){
                                                                                   2 const int MAX = 300;
```

```
3 // Corte minimo: vertices con dist[v]>=0 (del lado de src) VS. dist[v
       l==-1 (del lado del dst)
4 // Para el caso de la red de Bipartite Matching (Sean V1 y V2 los
       conjuntos mas proximos a src y dst respectivamente):
5 // Reconstruir matching: para todo v1 en V1 ver las aristas a vertices
       de V2 con it->f>0, es arista del Matching
6 // Min Vertex Cover: vertices de V1 con dist[v] ==-1 + vertices de V2 con
        dist[v]>0
7 // Max Independent Set: tomar los vertices NO tomados por el Min Vertex
       Cover
s // Max Clique: construir la red de G complemento (debe ser bipartito!) y
        encontrar un Max Independet Set
9 // Min Edge Cover: tomar las aristas del matching + para todo vertices
       no cubierto hasta el momento, tomar cualquier arista de el
  int nodes, src, dst;
   int dist[MAX], q[MAX], work[MAX];
  struct Edge {
       int to, rev;
13
       ll f. cap:
14
       Edge(int to, int rev, ll f, ll cap) : to(to), rev(rev), f(f), cap(
15
16
   vector<Edge> G[MAX];
   void addEdge(int s, int t, ll cap){
       G[s].pb(Edge(t, sz(G[t]), 0, cap)), G[t].pb(Edge(s, sz(G[s])-1, 0,
19
           0));}
   bool dinic_bfs(){
20
       fill(dist, dist+nodes, -1), dist[src]=0;
21
       int qt=0; q[qt++]=src;
22
       for(int qh=0; qh<qt; qh++){</pre>
23
           int u = q[qh];
24
           forall(e, G[u]){
25
               int v=e->to:
26
               if(dist[v]<0 && e->f < e->cap)
27
                   dist[v]=dist[u]+1, q[qt++]=v;
28
           }
29
       }
30
       return dist[dst]>=0;
31
32
   ll dinic_dfs(int u, ll f){
33
       if(u==dst) return f;
34
       for(int &i=work[u]; i<sz(G[u]); i++){</pre>
35
           Edge &e = G[u][i];
36
```

```
if(e.cap<=e.f) continue;</pre>
37
           int v=e.to;
38
           if(dist[v]==dist[u]+1){
39
                    11 df=dinic_dfs(v, min(f, e.cap-e.f));
40
                    if(df>0){
41
                            e.f+=df, G[v][e.rev].f-= df;
42
                            return df; }
43
           }
44
45
       return 0;
   }
47
   11 maxFlow(int _src, int _dst){
       src=_src, dst=_dst;
49
       11 result=0;
       while(dinic_bfs()){
           fill(work, work+nodes, 0);
           while(ll delta=dinic_dfs(src,INF))
               result+=delta;
       // todos los nodos con dist[v]!=-1 vs los que tienen dist[v]==-1
           forman el min-cut
       return result; }
57
```

7.23 máximo emparejamiento bipartito

```
1 // g++ -std=c "bipartitematching.cpp" -o run
2
  /***
   ========= <MCBM max cardinality bipartite matching c++ version>
4 Return the bipartite matching of a Graph
  * Format of nodes: 1 to N
   */
6
   const int N = 100010;
  vector<int>G[N];
  bool v[N];//for the greedy speed up
  int match[N];
12 bool vis[N]:
  int n,m;
14 //calling aumenting path
bool aug(int u){
       if(vis[u])return false;
16
       vis[u]=true;
17
```

```
for(int i=0;i<(int)G[u].size();++i){</pre>
18
       int r=G[u][i];
19
            if(match[r]==-1||aug(match[r])){
20
                match[r]=u;match[u]=r;return true;
21
            }
22
       }
23
       return 0;
24
25
   int mc;
26
    //findging all augmenting path's
   int solve(){
28
      bool check=true;
29
      while(check){
30
            check=false:
31
            memset(vis,0,sizeof vis);
32
            for(int i=1;i<=n;++i){
33
          if(!v[i]&&match[i]==-1){
34
            bool op=aug(i);
35
            check | = op;
36
            mc+=op;
37
38
39
40
       return mc;
41
42
    void init(){
43
     memset(v,0,sizeof v);
44
     memset(vis,false,sizeof vis);
45
46
     memset(match,-1,sizeof match);
47
       for(int i=0;i<=n;i++)G[i].clear();</pre>
48
49
   void greedySpeedUp(){
50
     //greedy optimization, match with the first not matched
51
     for(int i=1;i<=n;++i){</pre>
52
             for(int j=0;j<(int)G[i].size();++j){</pre>
53
                 if(match[G[i][j]]==-1){
54
             match[G[i][j]]=i,match[i]=G[i][j],mc++,v[i]=true;break;
55
          }
56
57
58
59
```

- 7.24 max-independent set en bipartitos
- 7.25 min-path cover (ver tópicos raros de halim)
 - 7.26 min-cost arborescence
- 7.27 lema de diapositivas de nico de grafos funcionales
 - 7.28 minimax y maximini con kruskal y dijkstra

```
1 // g++ -std=c++11 "maximini.cpp" -o run
2
            ====== <maximini c++ version> ============
   Given a weighted graph return the maximini (the maximun of the minimum)
   or the minimax (the minimum of the maximum) in the path a,b
6
  Minimax as definded as: finding the minimum of maximum edge weight among
        all posible paths
_{8} \mid * between two verrtices a to b, the cost for a path from a to b is
       determined by maximum edge
9 * weight along this path. Among all these possible paths from a to b,
       pick the one with the minimum
   * ax-edge-weight
   * Complexity O(E*log(E) + V + E)
   Problem for practice: UVA 534,544
14
   int n;
   pair<int,pair<int,int> >Edges[20000];
   map<string,int>mp;
   int parent[210];
   pair<int,int>child[210];
   bool vis[210];
   vector<pair<int,int> >G[210];
23
   int find(int u){return u==parent[u]?u:parent[u]=find(parent[u]);}
   void Union(int u,int v){
     int pu=find(u),pv=find(v);
26
     if(pu!=pv){
27
       parent[pv]=pu;
28
29
30
31 | int mst(int a,int b){
```

```
sort(Edges,Edges+t);
32
     reverse(Edges, Edges+t);//don't reverse for the minimax
33
     for(int i=0;i<=200;i++)parent[i] = i;</pre>
34
     int w,u,v, maximini = 1e8, minimax = 0;
35
     for(int i=0;i<t;i++){</pre>
36
       tie(w,u,v) = make_tuple(Edges[i].first, Edges[i].second.first, Edges
37
            [i].second.second);
       if(find(u) != find(v)){
38
         Union(u,v);
39
         G[u].push_back(\{v,w\});
40
         G[v].push_back(\{u,w\});
41
42
     }
43
     queue<int>q;
     q.push(a);
45
     vis[a]=true;
46
     while(!q.empty()){
47
       int u = q.front();q.pop();
48
       //if(u==1)break:
49
       for(pair<int,double>node: G[u]){
50
         if(!vis[node.first]){
51
            vis[node.first] = true:
52
           q.push(node.first);
53
            //maximini=max(maximini,node.second);
54
            child[node.first].first = u;
55
            child[node.first].second = node.second;
56
         }
57
       }
58
59
     for(int t = b;t != -1;t = child[t].first){
60
       //cout<<t<" "<<child[t].second<<"\n";
61
       //minimax=max(minimax,child[t].second);
62
       maximini = min(maximini.child[t].second):
63
     }
64
     return maximini:
65
66 | }
```

8 Teoria de juegos

8.1 Teorema fundamental de los juegos optimos

```
| boolean isWinning(position pos) {
    moves[] = possible positions to which I can move from the position
```

2

```
pos;
for (all x in moves)
if (!isWinning(x)) return true;

return false;
}
```

8.2 Como calcular grundy

```
int grundyNumber(position pos) {
   moves[] = possible positions to which I can move from pos
   set s;

for (all x in moves) insert into s grundyNumber(x);

//return the smallest non-negative integer not in the set s;
int ret=0;
while (s.contains(ret)) ret++;
return ret;
}
```

9 Algunas formulas de probabilidad

Importante

Verificar la independencia de eventos.

9.1 Regla general de la probabilidad

$$P(E) = \frac{Nro.casos favorables}{Nro.casos posibles}$$

9.2 Teorema de bayes (Probabilidad condicional)

$$P(A/B) = \frac{P(A \cap B)}{P(B)}$$

9.3 Regla de la suma

Se suman 2 probabilidades cuando los eventos no pueden ocurrir al mismo tiempo "Pasa el evento X o pasa el evento Y"

$$P(A) \cup P(B) = P(A) + P(B)$$

Regla de la suma con eventos compatibles e incompatibles (que pueden pasar al mismo tiempo o no)

$$P(A \cup B) = P(A) + P(B) - P(A \cap B)$$

9.4 Regla de la multiplicacion

La misma idea de arriba, "Pasa el evento X y pasa el evento Y"

$$P(A \cap B) = P(A) * P(B)$$

9.5 Esperanza matematica

$$E[X] = \sum_{i=0}^{n} X * P(X)$$

En el caso continuo reemplazar sumatoria por integral

9.6 Ley de la esperanza total

Esto se usa cuando quieres calcular el valor en el que pasa el evento X ej. calcular el dia esperado en el que muere el i-esimo pez

$$E(X) = E(E(X|Y))$$

9.7 Esperanza de variables independientes

$$E(X * Y) = E(X) * E(Y)$$

9.8 Varianza

$$\sigma^2 = E(X^2) - (E(X))^2$$

9.9 Distribucion Binomial

$$f(x) = \binom{n}{x} p^x (1-p)^{n-x}$$

Ejemplo. Supongamos que se lanza un dado (con 6 caras) 51 veces y queremos conocer la probabilidad de que el número 3 salga 20 veces.

$$f(X=20) = {51 \choose 20} \frac{1}{6}^{20} * (1 - \frac{1}{6})^{51-20}$$
 Esperanza:
$$E(x) = n * p$$
 Varianza:
$$V(x) = np * (1-p)$$

10 Otros/utilitarios

10.1 josephus

```
return (s+1);
4
5 }
                         10.2 josephus k=2
   ///////JAVA
       /**
2
      * Oparam n the number of people standing in the circle
      * Oreturn the safe position who will survive the execution
      * f(N) = 2L + 1 where N = 2^M + L and 0 \le L \le 2^M
6
     public int getSafePosition(int n) {
      // find value of L for the equation
       int valueOfL = n - Integer.highestOneBit(n);
       int safePosition = 2 * valueOfL + 1;
11
       return safePosition;
12
13
                              10.3 poker
```

int survivor(int n, int m){

for (int i=1; i <=n; ++i) s = (s+m)%i;

int s = 0;

10.4 iterar subconjuntos

```
for(int sbm=bm; sbm; sbm=(sbm-1)&bm)
             10.5 como reconstruir una DP (normal)
1 /*
  You just need to revisit your steps in the DP. In case of 0-1 knapsack,
       lets say the original DP function was solve, and the function
       reconstruct will give you the actual solution (I'm writing the code
       in C++):
3
   int solve(int pos, int capacity){
       if(pos == no_of_objects) return 0;
5
       if(memo[pos][capacity] != -1) return memo[pos][capacity];
6
       int r1 = solve(pos + 1, capacity); //dont take
       int r2 = 0;
8
       if(weight[pos] <= capacity){</pre>
9
           r2 = solve(pos + 1, capacity - weight[pos]) + profit[pos]; //
10
               take
       }
11
       return memo[pos][capacity] = max(r1, r2);
12
13
   void reconstruct(int pos, int capacity){
14
       if(pos == no_of_objects) return; //you have completed reconstruction
15
       int r1 = memo[pos + 1] [capacity]; //dont take
16
       int r2 = 0;
17
       if(weight[pos] <= capacity)r2 = memo[pos + 1][capacity - weight[pos</pre>
18
           ]] + profit[pos]; //take
       if(r1 > r2) {reconstruct(pos + 1, capacity);}
19
       else{
20
           cout << "Take_object_" << pos << endl;</pre>
21
           reconstruct(pos + 1, capacity - weight[pos]) + profit[pos];
22
                                                                                 10
       }
23
                                                                                 11
24
                                                                                 12
  After executing reconstruct, it will print all those objects that give
                                                                                 13
       you the optimal solution. As you can see, at most no_of_objects
                                                                                 14
       calls will be made in the reconstruct function.
                                                                                 15
26 Similarly, you can reconstruct the solution of any DP greedily.
                                                                                 16
                          10.6 muajaja con j
                                                                                 17
                                                                                 18
  #include <signal.h>
                                                                                 19
  void divzero(int p){
                                                                                 20
     while(true);}
  void segm(int p){
                                                                                 21
```

```
exit(0):}
 //in main
  signal(SIGFPE, divzero);
8 signal(SIGSEGV, segm);
                            Expandir pila
#include <sys/resource.h>
2 rlimit rl:
  getrlimit(RLIMIT_STACK, &rl);
 rl.rlim_cur=1024L*1024L*256L;//256mb
5 setrlimit(RLIMIT_STACK, &rl);
                10.7 comparar doubles for noobs
const double EPS = 1e-9;
_2 | x == y <=> fabs(x-y) < EPS
_3 | x > y <=> x > y + EPS
_4 | x >= y <=> x > y - EPS
                               infix to postfix
                        10.8
1 //infix to postfix with shunting yard, Halim interpretation
  //plus eval function given a postfix return the result of the operation
  //format: string like (xox (xox)) o=operation x=value
  string s:
  bool isOperator(string u){
    return u=="+"||u=="-"||u=="*"||u=="/";
7
  bool precede(string u){
    if(u=="*"||u=="/")return true;
    return false;
  void solve(){
    getline(cin,s);
    stack<string>st;
    vector<string>v;
    stringstream ss;
    ss<<s:
    while(ss>>s){
      if(isOperator(s)){
        while(!st.empty()&&isOperator(st.top())&&precede(st.top())>=
            precede(s)){
          v.push_back(st.top());st.pop();
```

```
}
                                                                                  65 }
22
         st.push(s);
23
                                                                                                           10.9
                                                                                                                   numeros romanos
^{24}
       else{
25
                                                                                   #include <bits/stdc++.h>
          if(s=="("){
26
                                                                                      using namespace std;
            st.push(s);
27
                                                                                     map<int,string>cvt;
28
         else{
29
                                                                                      string aromano(int n){
           if(s==")"){
30
                                                                                        cvt[1000] = "M";cvt[900] = "CM",cvt[500] = "D", cvt[400] = "CD";
             while(!st.empty()&&st.top()!="("){
31
                                                                                        cvt[100] = "C";cvt[90] = "XC"; cvt[50] = "L";
               v.push_back(st.top());st.pop();
32
                                                                                        cvt[40] = "XL";cvt[10] = "X";cvt[9] = "IX";cvt[5] = "V"; cvt[4] = "IV"
33
             if(!st.empty()&&st.top()=="(")st.pop();
34
                                                                                        cvt[1] = "I";
                                                                                   9
           }
35
                                                                                        string ans = "";
                                                                                  10
           else {
36
                                                                                        for(map<int,string>::reverse_iterator it = cvt.rbegin();it != cvt.rend
                                                                                  11
             v.push_back(s);
37
                                                                                            ():it++)
           }
38
                                                                                          while(n >= it->first){
                                                                                  12
         }
39
                                                                                            ans += it->second:
                                                                                  13
       }
40
                                                                                            n -= it->first;
                                                                                  14
41
                                                                                  15
     while(!st.empty()){
42
                                                                                        return ans:
                                                                                   16
       v.push_back(st.top());st.pop();
43
                                                                                  17
     }
44
                                                                                      map<string,int>crn;
                                                                                   18
     stack<double>stans;
45
                                                                                      int anumero(string R){
     double x;
46
                                                                                        map<char, int> crn;
                                                                                  20
     for(string eva:v){
47
                                                                                        crn['I'] = 1; crn['V'] = 5; crn['X'] = 10; crn['L'] = 50;
                                                                                  21
       if(!isOperator(eva)){
48
                                                                                        crn['C'] = 100; crn['D'] = 500; crn['M'] = 1000;
         stringstream nu;
49
                                                                                        int value = 0;
                                                                                  23
         nu<<eva;
50
                                                                                       for (int i = 0; R[i]; i++)
                                                                                  24
         nu>>x;
51
                                                                                         if (i + 1 < R.size() && crn[R[i]] < crn[R[i+1]]) {</pre>
         stans.push(x);
52
                                                                                            value += crn[R[i+1]] - crn[R[i]];
                                                                                  26
       }
53
                                                                                            i++;
       else{
54
                                                                                  28
         double a=stans.top();stans.pop();
55
                                                                                          else value += crn[R[i]];
         double b=stans.top();stans.pop();
56
                                                                                        return value:
         if(eva=="*")b*=a;
57
                                                                                  31 }
         if(eva=="/")b/=a;
58
         if(eva=="+")b+=a:
                                                                                                        10.10 get k-th permutacion
59
         if(eva=="-")b-=a;
60
         stans.push(b);
                                                                                   vector<int>v;
61
       }
                                                                                   //finding the number of permutation 0....n-1
62
                                                                                   3 | int main()
63
     cout<<fixed<<stans.top()<<"\n";</pre>
                                                                                   4 {
64
```

```
string s;
 5
        while(getline(cin,s)){
 6
            stringstream ss;
            ss<<s;
 8
            int pos=0,u;
 9
            v.clear();
10
            while(ss>>u){
11
                v.push_back(u-1);
^{12}
            }
13
            vector<int>le(v.size(),0);
14
            for(int i=0;i<v.size();i++){</pre>
15
                for(int j=i+1; j<v.size(); j++){</pre>
16
                     if(v[i]>v[j])le[i]++;
17
                }
18
            }
19
            long long ans=OLL,fact=OLL,por=1LL;
20
            for(int i=le.size()-1;i>=0;i--){
21
                if(fact!=OLL)por*=fact;
22
                fact++:
23
                ans=ans+por*le[i];
24
            }
25
            cout << ans+1 << "\n";
26
       }
27
        return 0;
28
29 }
```

10.11 sliding window

10.12 permutaciones de un dado

```
// izquierda, derecha, arriba, al frente, abajo, atras
2
   int p[][6] = {
3
       \{0,1,2,3,4,5\},
4
        \{0,1,3,4,5,2\},
5
        \{0,1,4,5,2,3\},\
6
        \{0,1,5,2,3,4\},
7
        \{1,0,2,5,4,3\},
8
        \{1,0,3,2,5,4\},
9
        \{1,0,4,3,2,5\},\
10
        \{1,0,5,4,3,2\},\
11
        \{2,4,5,1,3,0\},\
12
        \{2,4,1,3,0,5\},\
13
        \{2,4,3,0,5,1\},
14
```

```
\{2,4,0,5,1,3\},
15
       {3,5,2,1,4,0},
16
       {3,5,1,4,0,2},
17
       {3,5,4,0,2,1},
       {3,5,0,2,1,4},
19
       {4,2,5,0,3,1},
       {4,2,0,3,1,5},
       {4,2,3,1,5,0},
       {4,2,1,5,0,3},
       \{5,3,2,0,4,1\},
       \{5,3,0,4,1,2\},
25
       \{5,3,4,1,2,0\},\
26
       {5,3,1,2,0,4}
27
28 };
                      10.13 liebre y el tortugo
1 | ii floydCycleFinding(int x0) { // function int f(int x) is defined
    // 1st part: finding k*mu, hare's speed is 2x tortoise's
     int tortoise = f(x0), hare = f(f(x0)); // f(x0) is the node next to
     while (tortoise != hare) { tortoise = f(tortoise); hare = f(f(hare));
4
     // 2nd part: finding mu, hare and tortoise move at the same speed
5
     int mu = 0; hare = x0;
6
     while (tortoise != hare) { tortoise = f(tortoise); hare = f(hare); mu
         ++: }
     // 3rd part: finding lambda, hare moves, tortoise stays
     int lambda = 1; hare = f(tortoise);
9
     while (tortoise != hare) { hare = f(hare); lambda++; }
10
     return ii(mu, lambda);
11
12 }
                       10.14 como usar printf
                               10.15 java
                             10.16 python
                            10.17 template
#include <bits/stdc++.h>
using namespace std;
3
```

```
4 /* no sirve en todos los jueces probar primero
  int in() {
      int num, c;
6
       while((c = getchar_unlocked()) < '-');</pre>
      num = c - '0';
       while((c = getchar_unlocked()) >= '0') {
           num = (num << 3) + (num << 1) + (c-'0');
10
11
       return num;
12
13
14
  int in(){int r=0,c;for(c=getchar();c<=32;c=getchar());if(c=='-') return</pre>
       -in();for(;c>32;r=(r<<1)+(r<<3)+c-'0',c=getchar());return r;}
16
  #define DBG(x) cout << #x << ": " << x << "\n";
  #define eb emplace_back
  #define pb push_back
  #define mp make_pair
  #define mt make_tuple
  int main(){
    return 0;
23
24 }
                            10.18 file setup
1 //tambien se pueden usar comas: {a, x, m, l}
```

```
//tambien se pueden usar comas: {a, x, m, 1}
touch {a..l}.in; tee {a..l}.cpp < template.cpp
```