Curriculum Vitae: Luc Rey-Bellet

Contact Information

arXiv:2407.11901

Educational History:

- Ph.D. in Mathematics (1998): Department of Mathematics, University of Geneva, Geneva, Switzerland. Advisor: *Prof. Jean-Pierre Eckmann*
- Dipl. Phys. ETHZ (1994): , Department of Physics, Swiss Federal Institute of Technology (ETHZ), Zurich, Switzerland. Advisor: *Prof. Jürg Fröhlich*

Professional appointments:

- Research Fellow: Rutgers University 1998-1999
- Whyburn Instructor: University of Virginia 1999-2002
- Assistant Professor: University of Massachusetts 2002-2008
- Associate Professor: University of Massachusetts 2008-2013
- Visiting Professor: University of Crete 2011 (Spring semester)
- Professor: University of Massachusetts since 2013

Selected recent service

- Editorial board of Journal of Statistical Physics 2013–2018
- Organizer of the Oberwolfach seminar on Markov processes, 2011
- Organizer of the Conference in honor of J.P. Eckmann 75th birthday, 2022
- Organizer of ICERM Workshop on Optimal Transport and Machine Learning, 2023

Grant funding

- FNRS Bourse de jeune chercheur 1999 (SFr 45k)
- NSF Grant 2003 (3 year, PI, \$101K)
- NSF Grant 2006 (3 year, PI, \$106K)
- NSF Grant 2011 (3 Year, PI, \$99K)
- NSF Grant 2015 (3 year, PI (with 1 Co-PI) \$280K)
- DOE Grant 2016 (3 year, co-PI (with 4 PI) \$900K)
- AFOSR Grant 2019 (3 year, co-PI (with 2 PIs) \$900 K)
- NSF Grant 2020 (3 year, PI (with 1 Co-PI) \$ 370K)
- AFOSR Grant 2021 (4 year (with 2 PIs) \$1.950M)
- NSF Grant 2023 (3 year, PI (with 1 Co-PI) \$300K)

Graduate students and postdoctoral advising:

- Dimitrios Tsagkarogiannis (Graduation 2006, University of L'Aquila)
- Michael Diehl (Graduation 2008, Endicott College)
- Sasanka Are (Graduation 2009, Cerner Corporation)
- Sung-Ha Hwang (Graduation 2011, KAIST, Korea)
- Yannis Pantazis (Postdoctoral fellow, 2012-2013, and 2014-2015, Forth Crete)
- Kostis Gourgoulias (Graduation 2017, JP Morgan)
- Georgios Arampatzis (Postdoctoral fellow, 2014-2015, University of Crete)
- Jinchao Feng (Graduation 2019, John Hopkins University)
- Jie Wang (Graduation 2019, Discover)
- Jeremiah Birrell (Postdoctoral fellow, 2017-2022, Texas State University)
- Pangiota Birmpa (Postdoctoral fellow, 2018-2022, Heriott-Watt University)
- Hyemin Gu (Graduate Student since 2021)
- Benjamin Zhang (Postdoctoral fellow, 2022-2024, UNC Chapel Hill)
- Ziyu Chen (Postdoctoral fellow, 2022-2025, UNC Chapel Hill)
- Thejani Gamage (Postdoctoral fellow, 2024-)

Publications

Hyemin Gu, Markos A. Katsoulakis, Luc Rey-Bellet, and Benjamin J. Zhang. Combining Wasserstein-1 and Wasserstein-2 proximals: robust manifold learning via well-posed generative flows. Submitted.
 arXiv:2407.11901

Jeremiah Birrell, Markos A. Katsoulakis, Luc Rey-Bellet, Benjamin Zhang, and Wei Zhu. Nonlinear denoising score matching for enhanced learning of structured distributions.

Submitted.

arXiv:2405.15625

Ziyu Chen, Hyemin Gu, Markos A. Katsoulakis, Luc Rey-Bellet, and Wei Zhu.

Learning heavy-tailed distributions with Wasserstein-proximal-regularized - divergences. Submitted.

arXiv:2405.13962

Ziyu Chen, Markos A. Katsoulakis, Luc Rey-Bellet, and Wei Zhu.

Statistical Guarantees of Group-Invariant GANs. Submitted.

arXiv:2305.13517

Ziyu Chen, Markos A. Katsoulakis, Luc Rey-Bellet, and Wei Zhu.

Sample Complexity of Probability Divergences under Group Symmetry.

Proceedings of 40th International Conference on Machine Learning, PMLR 202 (2023) pp. 4713-4734.

Online Version Reprint in PDF (including supplementary materials)

Hyemin Gu, Panagiota Birmpa, Yannis Pantazis, Luc Rey-Bellet, and Markos A. Katsoulakis. Lipschitz-regularized gradient flows and generative particle algorithms for high-dimensional scarce data.

To appear in Siam Journal on Mathematics of Data Science (2024). arXiv:2210.17230

Jeremiah Birrell, Paul Dupuis, Markos Katsoulakis, Yannis Pantazis, and Luc Rey-Bellet. Function-space regularized Rényi divergences.

Proceedings of The Eleventh International Conference on Learning Representations (ICLR 2023).

Poster and Slides Open review Reprint in PDF

Jeremiah Birrell, Markos Katsoulakis, Luc Rey-Bellet, and Wei Zu.

Structure-preserving GANs.

Proceedings of the 39th International Conference on Machine Learning, PMLR 162 (2022), pp.1982-2020.

Online Version Reprint in PDF (including supplementary materials)

Panagiota Birmpa, Jinchao Feng, Markos Katsoulakis, and Luc Rey-Bellet.

Model Uncertainty and Correctability for Directed Graphical Models.

SIAM/ASA Journal on Uncertainty Quantification 10 (2022), no.4, pp 1461–1512.

DOI:10.1137/21M1434453 Reprint in PDF

Jeremiah Birrell, Paul Dupuis, Markos Katsoulakis, Yannis Pantazis, and Luc Rey-Bellet. (f,Γ) -Divergences: Interpolating between f-Divergences and Integral Probability Metrics. Journal of Machine Learning Research 23 (2022), paper 39, pp.1-70. Online Version Reprint in PDF

Jeremiah Birrell, Paul Dupuis, Markos A. Katsoulakis, Luc Rey-Bellet, and Jie Wang. A variational formula for Rényi divergences.

SIAM Journal on Mathematics of Data Science 3 (2021), no. 4, pp. 1093-1116 DOI: 10.1137/20M1368926 Reprint in PDF

Jeremiah Birrell, Paul Dupuis, Markos A. Katsoulakis, Luc Rey-Bellet, and Jie Wang. Distributional robustness and uncertainty quantification for rare events. Preprint.

arXiv:1911.09580 Preprint in PDF

Sung-Ha Hwang and Luc Rey-Bellet.

Positive feedback in coordination games: stochastic evolutionary dynamics and the logit choice rule.

Games and Economic Behavior 126 (2021), pp. 355-373

DOI: 10.1016/j.geb.2021.01.003 Reprint in PDF Supplementary Materials

Jeremiah Birrell, Markos Katsoulakis, and Luc Rev-Bellet.

Quantification of model uncertainty on path-space via goal-oriented relative entropy.

ESAIM: Mathematical Modeling and Numerical Analysis 55 (2021), no.1, pp. 131-169.

DOI: 10.1051/m2an/2020070 Reprint in PDF

Jeremiah Birrell and Luc Rey-Bellet.

 ${\bf Concentration\ inequalities\ and\ performance\ guarantees\ for\ hypocoercive\ MCMC\ samplers.}$

Preprint. arXiv:1907.11973 Preprint in PDF

Paul Dupuis, Markos Katoulakis, Yannis Pantazis, and Luc Rey-Bellet.

Sensitivity analysis for rare events based on Rényi divergence.

The Annals of Applied Probability, 30 (2020), no.4, pp. 1507-1533.

DOI:10.1214/19-AAP1468 Reprint in PDF

Jeremiah Birrell and Luc Rey-Bellet.

Uncertainty quantification for Markov processes via variational principles and functional

inequalities.

SIAM/ASA Journal on Uncertainty Quantification, 8 (2020), no. 2, pp. 539–572.

DOI: 10.1137/19M1237429 Reprint in PDF

Konstantinos Gourgoulias, Markos Katsoulakis, Luc Rey-Bellet, and Jie Wang.

How biased is your model? Concentration inequalities, information and model bias. IEEE Transactions on Information Theory 66 (2020), no.5, pp. 3079–3097.

DOI: 10.1109/TIT.2020.2977067 Reprint in PDF

Sung-Ha Hwang and Luc Rey-Bellet.

Simple characterizations of potential games and zero-sum equivalent games. Journal of Economic Theory and Econometrics, 31 (2020), pp. 1–13.

Online version Reprint in PDF

Sung-Ha Hwang and Luc Rey-Bellet.

Strategic decompositions of normal form games: potential games and zero-sum games.

Games and Economic Behavior 122, (2020), pp. 370–390.

DOI: 10.1016/j.geb.2020.05.003 Reprint in PDF file Supplementary Materials

Mark Demers, Luc Rey-Bellet, and Hongkun Zhang.

Fluctuations of the entropy production for the Lorentz gas under small external forces.

Communications in Mathematical Physics 363 (2018), no. 2, pp. 699–740.

DOI: 10.1007/s00220-018-3228-3 MR3851827 Reprint in PDF

Noé Cuneo, Jean-Pierre Eckmann, Martin Hairer, and Luc Rey-Bellet.

Non-equilibrium steady states for networks of oscillators.

Electronic Journal of Probability 23 (2018), paper no. 55, 28 pp.

DOI: 10.1214/18-EJP177 MR3814249 Reprint in PDF

Markos Katsoulakis, Luc Rey-Bellet, and Jie Wang.

Scalable information inequalities for uncertainty quantification.

Journal of Computational Physics 336 (2017), pp. 513–545.

DOI: 10.1016/j.jcp.2017.02.020 Reprint in PDF

Konstantinos Gourgoulias, Markos Katsoulakis, and Luc Rey-Bellet.

Information criteria for quantifying loss of reversibility in parallelized KMC.

Journal of Computational Physics 328 (2017), pp. 438–454.

DOI: 10.1016/j.jcp.2016.10.031 MR3571894 Reprint in PDF

Eric Hall, Markos Katsoulakis, and Luc Rey-Bellet.

Uncertainty quantification for generalized Langevin dynamics.

Journal of Chemical Physics 145 (2016), 224108.

DOI: 10.1063/1.4971433 Reprint in PDF

Konstantinos Spiliopoulos and Luc Rey-Bellet.

Improving the convergence of reversible samplers.

Journal of Statistical Physics 164 (2016), no.3, 472–494.

DOI: 10.1007/s10955-016-1565-1 MR3519206 Reprint in PDF

Georgios Arampatzis, Markos Katsoulakis, and Luc Rey-Bellet.

Efficient estimators for likelihood ratio sensitivity indices of complex stochastic dynamics.

Journal of Chemical Physics 144 (2016), 104107.

DOI: 10.1063/1.4943388 Reprint in PDF

Konstantinos Gourgoulias, Markos Katsoulakis, and Luc Rey-Bellet.

Information metrics for long-time errors in splitting schemes for stochastic dynamics and parallel kinetic Monte Carlo.

SIAM Journal on Scientific Computing 38 (2016), no. 6, pp. A3808–A3832.

DOI: 10.1137/15M1047271 MR3582415 Reprint in PDF

Konstantinos Spiliopoulos and Luc Rey-Bellet.

Variance reduction for irreversible Langevin samplers and diffusion on graphs.

Electronic Communications in Probability 20 (2015), no. 15, 16pp.

DOI: 10.1214/ECP.v20-3855 MR3314650 Reprint in PDF

Konstantinos Spiliopoulos and Luc Rey-Bellet.

Irreversible Langevin samplers and variance reduction: a large deviation approach.

Nonlinearity 28 (2015), no.7, pp. 2081–2103.

DOI: 10.1088/0951-7715/28/7/2081 MR3366637 Reprint in PDF

Markos Katsoulakis, Yannis Pantazis, and Luc Rey-Bellet.

Measuring the irreversibility of numerical schemes for reversible stochastic differential equations.

ESAIM: Mathematical Modelling and Numerical Analysis 48 (2014), no.5, pp. 1351–1379.

DOI: 10.1051/m2an/2013142 MR3264357 Reprint in PDF.

M. Katsoulakis, P. Plecháč, Luc Rey-Bellet, and D. Tsagkarogiannis.

Coarse-graining schemes for stochastic lattice systems with short and long-range interactions.

Mathematics of Computation 83 (2014), no.288, pp. 1757–1793.

DOI: 10.1090/S0025-5718-2014-02806-8 MR3194129 Reprint in PDF

Sung-Ha Hwang, Luc Rey-Bellet, and Markos Katsoulakis.

Deterministic equations for stochastic spatial evolutionary games.

Theoretical Economics 8 (2013), no.3, pp. 829–874.

DOI: 10.3982/TE829 MR3106962 Reprint in PDF

Andrea Nahmod, Hiro Oh, Luc Rey-Bellet, and Gigliola Staffilani.

Invariant weighted Wiener measures and almost sure global well-posedness for the periodic derivative NLS.

Journal of the European Mathematical Society 14 (2012), no.4, pp. 1275–1330.

DOI: 10.4171/JEMS/333 MR2928851 Reprint in PDF

Sung-Ha Hwang and Luc Rey-Bellet.

Decompositions of two player games: potential, zero-sum, and stable games.

Unpublished (2011).

arXiv:1106.3552.

Andrea Nahmod, Luc Rey-Bellet, Scott Sheffield, and Gigliola Staffilani.

Absolute continuity of Brownian bridges under certain gauge transformations.

Mathematical Research Letters 18 (2011), no.5, pp. 875–887.

DOI: 10.4310/MRL.2011.v18.n5.a6 MR2875861 Reprint in PDF

Yoshiko Ogata and Luc Rey-Bellet.

Ruelle-Lanford functions and large deviations for asymptotically decoupled quantum spin systems.

Reviews in Mathematical Physics 23 (2011), no.2, pp. 211–232.

DOI: 10.1142/S0129055X11004291 MR2786227 Reprint in PDF

Vojkan Jaksic, Claude-Alain Pillet, and Luc Rey-Bellet.

Entropic fluctuations in statistical mechanics I. Classical dynamical systems.

Nonlinearity 24 (2011), no.3, pp. 699–763.

DOI: 10.1088/0951-7715/24/3/003 MR2765481 Reprint in PDF

Wojciech De Roeck, Christian Maes, Karel Netočný, and Luc Rev-Bellet.

A note on the non-commutative Laplace-Varadhan integral lemma,

Reviews in Mathematical Physics 22 (2010), no.7, pp. 839–858.

DOI: 10.1142/S0129055X10004089 MR2673696 Reprint in PDF

Sasanka Are, Markos Katsoulakis, Petr Plecháč, and Luc Rey-Bellet.

Multi-body interactions in coarse-graining schemes of extended systems.

SIAM Journal on Scientific Computing 31 (2008/2009), no.2, pp. 987–1015.

DOI: 10.1137/080713276 MR2466145 Reprint in PDF

Markos Katsoulakis, Petr Plecháč, and Luc Rey-Bellet.

Numerical and statistical methods for the coarse-graining of many-particle stochastic systems.

Journal of Scientific Computing 37 (2008), no.1, pp. 43–71.

DOI: 10.1007/s10915-008-9216-6 MR2442973 Reprint in PDF

Lai-Sang Young and Luc Rey-Bellet.

Large deviations in nonuniformly hyperbolic dynamical systems. Ergodic Theory and Dynamical Systems 28 (2008), no.2, pp. 587-612.

DOI:10.1017/S0143385707000478 MR2408394 Reprint in PDF

Markos Katsoulakis, Petr Plecháč, Luc Rey-Bellet, and Dimitrios Tsagkarogiannis.

Mathematical strategies in the coarse-graining of extensive systems: error quantification and adaptivity.

Journal of Non Newtonian Fluid Mechanics 152 (2008), pp. 101–112.

DOI: 10.1016/j.jnnfm.2007.05.005 Reprint in PDF

Markos Katsoulakis, Petr Plecháč, Luc Rey-Bellet, and Dimitrios Tsagkarogiannis.

Coarse-graining schemes and a posteriori error estimates for stochastic lattice systems.

ESAIM: Mathematical Modelling and Numerical Analysis 41 (2007), no.3, pp. 627–660.

DOI: 10.1051/m2an:2007032 MR2355714 Reprint in PDF

Federico Bonetto and Luc Rey-Bellet.

Fourier Law.

In: Encyclopedia of Mathematical Physics. J.-P. Francoise, G. L. Naber, S.T. Tsou (Eds.), Elsevier 2006, pp. 374–379.

Reprint in PDF

Luc Rey-Bellet.

Open Classical Systems.

In: Quantum Open Systems II. The Markovian approach. Stéphane Attal, Alain Joye, Claude-Alain Pillet (Eds.), Lecture Notes in Mathematics 1881, Berlin: Springer, 2006, pp. 41–78.

DOI: 10.1007/3-540-33966-3_2 MR2248987 Reprint in PDF

Luc Rey-Bellet.

Ergodic Properties of Markov Processes.

In: Quantum Open Systems II. The Markovian approach. Stéphane Attal, Alain Joye, Claude-Alain Pillet (Eds.), Lecture Notes in Mathematics 1881, Berlin: Springer, 2006, pp. 1–39.

DOI:10.1007/3-540-33966-3 1 MR2248986 Reprint in PDF

Luc Rey-Bellet.

Nonequilibrium statistical mechanics of open classical systems.

In: XIVth International Conference on Mathematical Physics, Lisbon, Portugal, 28 July – 2 August 2003, World Scientific 2006, pp. 447–454

DOI: 10.1142/9789812704016_0043 MR2227858 PDF file

Marco Lenci and Luc Rev-Bellet.

Large deviations in quantum lattice systems: one phase region.

Journal of Statistical Physics 119 (2005), no. 3-4, pp. 715–746. DOI: 10.1007/s10955-005-3015-3 MR2151220 Reprint in PDF

Lawrence E. Thomas and Luc Rey-Bellet.

Low regularity solutions to a gently stochastic nonlinear wave equation in nonequilibrium statistical mechanics.

Stochastic Processes and their Applications 115 (2005), no.6, pp. 1041–1059. (2005).

DOI: 10.1016/j.spa.2005.02.003 MR2138813 Reprint in PDF

Luc Rey-Bellet.

Statistical mechanics of anharmonic lattices.

In: Advances in Differential Equations and Mathematical Physics, AMS Contemporary Mathematics Series 327 (2003), pp. 283–298.

DOI: MR1991548 Reprint in PDF

Lawrence E. Thomas and Luc Rey-Bellet.

Fluctuations of the entropy production in anharmonic chains,

Annales Henri Poincaré 3 (2002), no.3, pp. 483–502.

DOI: 10.1007/s00023-002-8625-6 MR1915300 Reprint in PDF

Lawrence E. Thomas and Luc Rey-Bellet.

Exponential convergence to non-equilibrium stationary states in classical statistical mechanics.

Communications in Mathematical Physics 225 (2002), no.1, pp. 305–329.

DOI: 10.1007/s002200100583 MR1889227 Reprint in PDF

Jürg Fröhlich, Luc Rey-Bellet, and Daniel Ueltschi.

Quantum lattice systems at intermediate temperature,

Communications in Mathematical Physics 224 (2001), no. 1, pp. 33–63.

DOI: 10.1007/s002200100530 MR1869003 Reprint in PDF

Federico Bonetto, Joel Lebowitz, and Luc Rey-Bellet.

Fourier Law: A challenge to theorists.

In: Mathematical Physics 2000, A. Fokas, A. Grigoryan, T. Kibble, and B. Zegarlinski (Eds.)

Imperial College Press, London 2000, pp. 128–150.

DOI:10.1142/9781848160224 0008 MR1773043 Reprint in PDF

Lawrence E. Thomas and Luc Rey-Bellet.

Asymptotic behavior of thermal non-equilibrium steady states for a driven chain of anharmonic oscillators.

Communications in Mathematical Physics 215 (2000), no.1, pp. 1–24.

DOI: 10.1007/s002200000285 MR1799873 Reprint in PDF

Jean-Pierre Eckmann, Claude-Alain Pillet, and Luc Rey-Bellet.

Entropy production in non-linear, thermally driven Hamiltonian systems.

Journal of Statistical Physics 95 (1999), no. 1-2, pp. 305–331.

DOI:10.1023/A:1004537730090 MR1705589 Reprint in PDF

Jean-Pierre Eckmann, Claude-Alain Pillet, and Luc Rey-Bellet.

Non-equilibrium statistical mechanics of anharmonic chains coupled to two heat baths at different temperatures.

Communications in Mathematical Physics 201 (1999), no. 3, pp. 657–697.

DOI: 10.1007/s002200050572 MR1685893 Reprint in PDF

Jürg Fröhlich and Luc Rey-Bellet.

Low-temperature phase diagrams of quantum lattice systems. III. Examples.

Helvetica Physica Acta 69 (1996), 5-6, pp. 821–849.

DOI: 10.5169/seals-116980 MR1428029 Reprint in PDF

Nilanjana Datta, Roberto Fernandez, Jürg Fröhlich, and Luc Rey-Bellet.

Low-temperature phase diagrams of quantum lattice systems. II. Convergent perturbation expansions and stability in systems with infinite degeneracy.

Helvetica Physica Acta 69 (1996), 5-6, pp. 752–820.

DOI: 10.5169/seals-116979 MR1428028 Reprint in PDF

Publications

Nilanjana Datta, Roberto Fernandez, Jürg Fröhlich, and Luc Rey-Bellet, Low-temperature phase diagrams of quantum lattice systems. II. Convergent perturbation expansions and stability in systems with infinite degeneracy, Helvetica Physica Acta 69 (1996), 5-6, pp. 752–820.

Jürg Fröhlich and Luc Rey-Bellet, Low-temperature phase diagrams of quantum lattice systems. III. Examples, Helvetica Physica Acta 69 (1996), 5-6, pp. 821–849.

Jean-Pierre Eckmann, Claude-Alain Pillet, and Luc Rey-Bellet, Non-equilibrium statistical mechanics of anharmonic chains coupled to two heat baths at different temperatures, Communications in Mathematical Physics 201 (1999), no. 3, pp. 657–697.

Jean-Pierre Eckmann, Claude-Alain Pillet, and Luc Rey-Bellet, Entropy production in non-linear, thermally driven Hamiltonian systems, Journal of Statistical Physics 95 (1999), no. 1-2, pp. 305–331.

Lawrence E. Thomas and Luc Rey-Bellet, Asymptotic behavior of thermal non-equilibrium steady states for a driven chain of anharmonic oscillators, Communications in Mathematical Physics 215 (2000), no.1, pp. 1–24.

Federico Bonetto, Joel Lebowitz, and Luc Rey-Bellet, Fourier Law: A challenge to theorists, In: Mathematical Physics 2000, A. Fokas, A. Grigoryan, T. Kibble, and B. Zegarlinski (Eds.) Imperial College Press, London 2000, pp. 128–150.

Jürg Fröhlich, Luc Rey-Bellet, and Daniel Ueltschi, Quantum lattice systems at intermediate temperature, Communications in Mathematical Physics 224 (2001), no. 1, pp. 33–63.

Lawrence E. Thomas and Luc Rey-Bellet, Exponential convergence to non-equilibrium stationary states in classical statistical mechanics, Communications in Mathematical Physics 225 (2002), no.1, pp. 305–329.

Lawrence E. Thomas and Luc Rey-Bellet, Fluctuations of the entropy production in anharmonic chains, Annales Henri Poincaré 3 (2002), no.3, pp. 483–502.

Luc Rey-Bellet Statistical mechanics of anharmonic lattices, In: Advances in Differential Equations and Mathematical Physics, AMS Contemporary Mathematics Series 327 (2003), pp. 283–298.

Lawrence E. Thomas and Luc Rey-Bellet, Low regularity solutions to a gently stochastic nonlinear wave equation in nonequilibrium statistical mechanics,

Stochastic Processes and their Applications 115 (2005), no.6, pp. 1041–1059. (2005).

Marco Lenci and Luc Rey-Bellet, Large deviations in quantum lattice systems: one phase region, Journal of Statistical Physics 119 (2005), no. 3-4, pp. 715–746.

Luc Rey-Bellet, Nonequilibrium statistical mechanics of open classical systems, In: XIVth International Conference on Mathematical Physics, Lisbon, Portugal, 28 July – 2 August 2003, World Scientific 2006, pp. 447–454

Luc Rey-Bellet Ergodic Properties of Markov Processes, In: Quantum Open Systems II. The Markovian approach. Stéphane Attal, Alain Joye, Claude-Alain Pillet (Eds.), Lecture Notes in Mathematics 1881, Berlin: Ser, 2006, pp. 1–39.

Luc Rey-Bellet, Open Classical Systems, In: Quantum Open Systems II. The Markovian approach. Stéphane Attal, Alain Joye, Claude-Alain Pillet (Eds.), Lecture Notes in Mathematics 1881, Berlin: Springer, 2006, pp. 41–78.

Federico Bonetto and Luc Rey-Bellet, Fourier Law, In: Encyclopedia of Mathematical Physics. J.-P. Francoise, G. L. Naber, S.T. Tsou (Eds.), Elsevier 2006, pp. 374–379.

Markos Katsoulakis, Petr Plechač, Luc Rey-Bellet, and Dimitrios Tsagkarogiannis, Coarse-graining schemes and a posteriori error estimates for stochastic lattice systems, ESAIM: Mathematical Modelling and Numerical Analysis 41 (2007), no.3, pp. 627–660.

Markos Katsoulakis, Petr Plechač, Luc Rey-Bellet, and Dimitrios Tsagkarogiannis, Mathematical strategies in the coarse-graining of extensive systems: error quantification and adaptivity, Journal of Non Newtonian Fluid Mechanics 152 (2008), pp. 101–112.

Lai-Sang Young and Luc Rey-Bellet, Large deviations in nonuniformly hyperbolic dynamical systems, Ergodic Theory and Dynamical Systems 28 (2008), no.2, pp. 587-612.

Markos Katsoulakis, Petr Plechac, and Luc Rey-Bellet, Numerical and statistical methods for the coarse-graining of many-particle stochastic systems, Journal of Scientific Computing 37 (2008), no.1, pp. 43–71.

Sasanka Are, Markos Katsoulakis, Petr Plechač, and Luc Rey-Bellet, Multi-body interactions in coarse-graining schemes of extended systems, SIAM Journal on Scientific Computing 31 (2008/2009), no.2, pp. 987–1015.

Wojciech De Roeck, Christian Maes, Karel Netočný, and Luc Rey-Bellet, A note on the non-commutative Laplace-Varadhan integral lemma, Reviews in Mathematical Physics 22 (2010), no.7, pp. 839–858.

Vojkan Jaksic, Claude-Alain Pillet, and Luc Rey-Bellet, Entropic fluctuations in statistical mechanics I. Classical dynamical systems, Nonlinearity 24 (2011), no.3, pp. 699–763.

Yoshiko Ogata and Luc Rey-Bellet, Ruelle-Lanford functions and large deviations for asymptotically decoupled quantum spin systems, Reviews in Mathematical Physics 23 (2011), no.2, pp. 211–232.

Andrea Nahmod, Luc Rey-Bellet, Scott Sheffield, and Gigliola Staffilani, Absolute continuity of Brownian bridges under certain gauge transformations, Mathematical Research Letters 18 (2011), no.5, pp. 875–887.

Sung-Ha Hwang and Luc Rey-Bellet, Decompositions of two player games: potential, zero-sum, and stable games, Unpublished (2011).

Andrea Nahmod, Hiro Oh, Luc Rey-Bellet, and Gigliola Staffilani, Invariant weighted Wiener measures and almost sure global well-posedness for the periodic derivative NLS, Journal of the European Mathematical Society 14 (2012), no.4, pp. 1275–1330.

Sung-Ha Hwang, Luc Rey-Bellet, and Markos Katsoulakis, Deterministic equations for stochastic spatial evolutionary games, Theoretical Economics 8 (2013), no.3, pp. 829–874.

M. Katsoulakis, P. Plechač, Luc Rey-Bellet, and D. Tsagkarogiannis, Coarse-graining schemes for stochastic lattice systems with short and long-range interactions, Mathematics of Computation 83 (2014), no.288, pp. 1757–1793.

Markos Katsoulakis, Yannis Pantazis, and Luc Rey-Bellet, Measuring the irreversibility of numerical schemes for reversible stochastic differential equations, ESAIM: Mathematical Modelling and Numerical Analysis 48 (2014), no.5, pp. 1351–1379.

Konstantinos Spiliopoulos and Luc Rey-Bellet, Irreversible Langevin samplers and variance reduction: a large deviation approach, Nonlinearity 28 (2015), no.7, pp. 2081–2103.

Konstantinos Spiliopoulos and Luc Rey-Bellet, Variance reduction for irreversible Langevin samplers and diffusion on graphs, Electronic Communications in Probability 20 (2015), no. 15, 16pp.

Konstantinos Gourgoulias, Markos Katsoulakis, and Luc Rey-Bellet, Information metrics for long-time errors in splitting schemes for stochastic dynamics and parallel kinetic Monte Carlo, SIAM Journal on Scientific Computing 38 (2016), no. 6, pp. A3808–A3832.

Georgios Arampatzis, Markos Katsoulakis, and Luc Rey-Bellet, Efficient estimators for likelihood ratio sensitivity indices of complex stochastic dynamics, Journal of Chemical Physics 144 (2016), 104107.

Konstantinos Spiliopoulos and Luc Rey-Bellet, Improving the convergence of reversible samplers, Journal of Statistical Physics 164 (2016), no.3, 472–494.

Eric Hall, Markos Katsoulakis, and Luc Rey-Bellet, Uncertainty quantification for generalized Langevin dynamics, Journal of Chemical Physics 145 (2016), 224108.

Konstantinos Gourgoulias, Markos Katsoulakis, and Luc Rey-Bellet, Information criteria for quantifying loss of reversibility in parallelized KMC, Journal of Computational Physics 328 (2017), pp. 438–454.

Markos Katsoulakis, Luc Rey-Bellet, and Jie Wang, Scalable information inequalities for uncertainty quantification, Journal of Computational Physics 336 (2017), pp. 513–545.

Noé Cuneo, Jean-Pierre Eckmann, Martin Hairer, and Luc Rey-Bellet, Non-equilibrium steady states for networks of oscillators, Electronic Journal of Probability 23 (2018), paper no. 55, 28 pp.

Mark Demers, Luc Rey-Bellet, and Hongkun Zhang, Fluctuations of the entropy production for the Lorentz gas under small external forces, Communications in Mathematical Physics 363 (2018), no. 2, pp. 699–740.

Sung-Ha Hwang and Luc Rey-Bellet, Strategic decompositions of normal form games: potential games and zero-sum games, Games and Economic Behavior 122, (2020), pp. 370–390.

Sung-Ha Hwang and Luc Rey-Bellet, Simple characterizations of potential games and zero-sum equivalent games, Journal of Economic Theory and Econometrics, 31 (2020), pp. 1–13.

Konstantinos Gourgoulias, Markos Katsoulakis, Luc Rey-Bellet, and Jie Wang, How biased is your model? Concentration inequalities, information and model bias, IEEE Transactions on Information Theory 66 (2020), no.5, pp. 3079–3097.

Jeremiah Birrell and Luc Rey-Bellet, Uncertainty quantification for Markov processes via variational principles and functional inequalities, SIAM/ASA Journal on Uncertainty Quantification, 8 (2020), no. 2, pp. 539–572.

Paul Dupuis, Markos Katoulakis, Yannis Pantazis, and Luc Rey-Bellet, Sensitivity analysis for rare events based on Rényi divergence, The Annals of Applied Probability, 30 (2020), no.4, pp. 1507-1533.

Jeremiah Birrell and Luc Rey-Bellet Concentration inequalities and performance guarantees for hypocoercive MCMC samplers, Preprint.

Jeremiah Birrell, Markos Katsoulakis, and Luc Rey-Bellet, Quantification of model uncertainty on path-space via goal-oriented relative entropy, ESAIM: Mathematical Modeling and Numerical Analysis 55 (2021), no.1, pp. 131-169.

Sung-Ha Hwang and Luc Rey-Bellet, Positive feedback in coordination games: stochastic evolutionary dynamics and the logit choice rule, Games and Economic Behavior 126 (2021), pp. 355-373.

Jeremiah Birrell, Paul Dupuis, Markos A. Katsoulakis, Luc Rey-Bellet, and Jie Wang, Distributional robustness and uncertainty quantification for rare events, Preprint.

Jeremiah Birrell, Paul Dupuis, Markos A. Katsoulakis, Luc Rey-Bellet, and Jie Wang, A variational formula for Rényi divergences, SIAM Journal on Mathematics of Data Science 3 (2021), no. 4, pp. 1093-1116

Jeremiah Birrell, Paul Dupuis, Markos Katsoulakis, Yannis Pantazis, and Luc Rey-Bellet, (f,Γ) -Divergences: Interpolating between f-Divergences and Integral Probability Metrics, Journal of Machine Learning Research 23 (2022), paper 39, pp.1—70.

Panagiota Birmpa, Jinchao Feng, Markos Katsoulakis and Luc Rey-Bellet, Model Uncertainty and Correctability for Directed Graphical Models, SIAM/ASA Journal on Uncertainty Quantification 10 (2022), no.4, pp 1461–1512.

Jeremiah Birrell, Markos Katsoulakis, Luc Rey-Bellet, Wei Zu Structure-preserving GANs, Proceedings of the 39th International Conference on Machine Learning, PMLR 162 (2022) pp.1982-2020.

Jeremiah Birrell, Paul Dupuis, Markos Katsoulakis, Yannis Pantazis, Luc Rey-Bellet Function-space regularized Rényi divergences. Proceedings of The Eleventh International Conference on Learning Representations (ICLR 2023).

Hyemin Gu, Panagiota Birmpa, Yannis Pantazis, Luc Rey-Bellet, and Markos A. Katsoulakis, Lipschitz-regularized gradient flows and generative particle algorithms for high-dimensional scarce data, Submitted.

Ziyu Chen, Markos A. Katsoulakis, Luc Rey-Bellet, and Wei Zhu, Sample Complexity of Probability Divergences under Group Symmetry,
Submitted

Ziyu Chen, Markos A. Katsoulakis, Luc Rey-Bellet, and Wei Zhu, *Statistical Guarantees of Group-Invariant GANs*, Submitted.

Invited talks

- Journées semi-classiques 1998, Grenoble, February 1998
- Statphys 20, Paris, July 1998
- 80th Statistical mechanics conference, Rutgers University, December 1998
- Non equilibrium statistical mechanics, Schrodinger Institute, February 1999
- The 2002 UAB International conference mathematical physics, March 2002
- Workshop on Fokker-Planck equations, Rennes, France, February 2003
- ODYN-II, Probability and statistical mechanics, CIRM, Marseilles, March 2003
- 89th Statistical mechanics conference, Rutgers university, May 2003
- Summer school on open quantum systems, Grenoble, July 2003
- International congress of mathematical physics, ICMP 2003, Lisbon, August 2003
- Young researcher symposium, Lisbon, July 2003
- Workshop on dynamics and statistical mechanics, CRM, Montreal, August 2004
- SIAM conference on applications of dynamical systems, Snowbird, May 2005
- International congress on the applications of mathematics, Santiago, March 2006
- Workshop on statistical mechanics, CPT-CNRS, Marseilles, July 2006
- 96th Statistical mechanics Conference, Rutgers University, December 2006
- Workshop on nonequilibrium statistical mechanics, Vienna, June 2008
- Workshop on stochastic dynamical systems, Bielefeld, November 2008
- Arizona school of analysis with applications I, University of Arizona, March 2009
- NORDITA Stockholm, Multiscale modeling and simulation in science, November 2009
- SAMSI, Theory and qualitative behavior of stochastic dynamics, February 2010
- Indam meeting, Corinaldo, Hyperbolic dynamical systems in the sciences, June 2010
- SIAM conference on nonlinear waves and coherent stuctures, August 2010
- Oberwolfach seminar on ergodic theory of Markov processes, October 2010
- 105th Statistical mechanics Conference, Rutgers University, May 2011
- FRG workshop on quantum spin systems, Harvard University, May 2011
- Workshop on Coarse-graining of many-body systems. Heraklion, June 2011
- ENUMATH conference. September 2011
- Three hours course on statistical mechanics), Ecole des Ponts, September 2011
- SIAM conference on material sciences, Philadelphia, June 2013
- SPA conference (Stochastic processes and applications), Boulder, August 2013
- AMS sectional meeting, Session on dynamical systems. Saint Louis, October 2013
- Randomness and Long-Time Dynamics, Radcliffe Institute, November 2014
- CIRM Workshop on Averaging and Homogenization, Marseille, May 2015
- CRiSM Workshop on Non-Reversible Markov Chains, Warwick, September 2015
- Meeting of the Canadian Mathematical Society, Montreal, December 2015
- 114th Statistical Mechanics Conference, Rutgers, December 2015
- Computational Statistics and Molecular Simulation (COSMOS), Paris, February 2016
- Numerical Aspects of Nonequilibrium Dynamics, Paris, April 2017
- BIRS-CMO Workshop, Oaxaca, November 2018

- Worskshop on Entropic Fluctuation Relations, Montreal, October 2018
- Ki-Net: Dimension reduction in physical and data sciences. Duke. April 2019
- Bernoulli Center, EPFL, May 2019
- Quantissima III, Venice, August 2019.
- Non Reversible Markovian Monte-Carlo Methods, Lorentz Center, August 2021
- Meetings on Foundations of Data Science, Tufts University, March 2022
- AFOSR PI Meeting, Arlington, VA, August 2022
- Conference in Honor of J.P. Eckmann 75th birthday, Geneva, Switzerland, June 2022
- ICML 2022, Baltimore, Poster presentation, July 2022
- Neurips 2022, New orleans, Poster presentation, December 2022
- ICLR 2023, Kigali, Rwanda, Poster presentation, April 2023
- AFOSR PI Meeting, Arlington, VA, August 2023
- AFOSR PI Meeting, Arlington, VA, August 2024
- ICERM Meeting. Providence, RI, September 2024
- JMM Meeting. Seattle, WA, January 2025
- IPAM Workshop. Los Angeles, CA, July 2025

Seminar talks

- Mathematical physics seminar, ETH, Zürich January 1998
- Mathematical physics seminar, CPT-CNRS, Marseille, January 1998
- Mathematical physics seminar, Institut Fourier Grenoble, February 1998
- Mathematical physics seminar, University Paris-XI Orsay, April 1998
- Mathematical physics seminar, University of Virginia, November 1998
- Colloquium, University of Ottawa, January 1999
- Statistical mechanics seminar, Princeton University, February 1999
- Mathematical physics seminar, University of Geneva, July 1999
- Dynamical systems seminar, SUNY at Stony Brook, November 1999
- Mathematical physics seminar, University of Geneva, July 2000
- Mathematical physics seminar, ETH, Zürich, August 2000
- Colloquium, University of Arizona, October 2000
- Statistical mechanics seminar, Princeton University, February 2001
- Applied mathematics seminar, University of Toronto, March 2001
- Theoretical physics seminar, University of Geneva, May 2001
- Mathematical physics seminar, ETH Zürich, June 2001
- Analysis seminar, University of Helsinki, August 2001
- Mathematical physics seminar, University of Texas at Austin, January 2002
- Colloquium, University of Massachusetts, Amherst, January 2002
- Colloquium, University of Maryland, College Park, January 2002
- Colloquium, University of Rochester, February 2002
- Colloquium, University of Notre Dame, February 2002
- Statistical mechanics seminar, Institute of Advanced Study, February 2002

- Nonlinear analysis seminar, Stevens Institute of Technology, May 2002
- Mathematical physics seminar, Rutgers University, October 2002
- Stochastic processes seminar, Brown University, November 2002
- Mathematical physics seminar, University of Virginia, January 2003
- Condensed matter seminar, University of Massachusetts, April 2003
- Probability seminar, EPFL, Lausanne, June 2003
- Mathematical physics seminar, University of Geneva, June 2003
- Applied mathematics seminar, Duke University, March 2004
- Mathematical physics seminar, University of Geneva, January 2005
- Analysis and mumerics seminar, Munich University, January 2005
- Mathematical physics seminar, Munich University, January 2005
- Dynamical systems seminar, Boston University, April 2005
- Nonlinear systems seminar, Stevens Institute of Technology, April 2005
- Mathematical physics seminar, Rutgers University, September 2005
- Mathematical physics seminar, University of Virginia, November 2006
- Mathematical physics seminar, Rutgers University, November 2006
- Applied mathematics seminar, Dartmouth College, April 2007
- Mathematical physics seminar, University of Arizona, October 2007
- Analysis seminar, University of Toronto, October 2007
- Applied mathematics seminar, Brown University, November 2007
- Colloquium, University of Connecticut, February 2009
- Probability seminar, University of Wisconsin, March 2009
- Theoretical physics Seminar, University of Geneva, April 2009
- Mathematical physics Seminar, University of Rome, April 2009
- Mathematical physics Seminar, University of Bologna, April 2009
- Mathematical physics Seminar, University of Grenoble, May 2009
- Applied mathematics Seminar, University of Crete, May 2009
- Mathematical physics seminar, Rutgers University, November 2009
- Operator algebra, University of Tokyo, January 2010
- Joint PDE seminar Boston University Brown University, November 2010
- Applied Mathematics Seminar, University of Crete, March 2011
- Probability Seminar, Warwick University, March 2011
- Probability Seminar, Boston University, September 2012
- Probability Seminar, University of Delaware, October 2013
- Probability Seminar, Concordia University, May 2015
- Probability Seminar, Brown University, November 2016
- Mathematical physics seminar, Rutgers University, December 2017
- Dynamical systems seminar, Courant Institute, NYU January 2018
- Applied PDE seminar, Imperial College, November 2020
- Probability seminar KTH, November 2020
- Probability and Statistics Seminar, Boston University, November 2024

Teaching Experience

University of Massachusetts Amherst (since 2002)

Fall 2002: "Math 131 Calculus I

Spring 2003: Math 132 Calculus II

Spring 2003: Math 421 Complex variables

Fall 2003: " Math 597/697 Introduction to stochastic processes

Spring 2004: Math 131 Calculus I

Fall 2004: " Math 645 Differential equations and dynamical systems

Spring 2005: Math 646 Ergodic theory

Spring 2005: Math 131 Calculus I

Fall 2005: "Math 645 Differential equations and dynamical systems

Fall 2005: "Stat 515 Introduction to Statistics I

Spring 2006: Math597/697 Introduction to stochastic processes

Fall 2006: "Math 623 Real analysis I

Fall 2006: "Math 131H Honor calculus I

Spring 2007: Math 624 Real analysis II

Fall 2007: "Math 697U Introduction to stochastic processes

Fall 2007: "Math 331 Differential equations

Spring 2008: Math 331 Differential equations

Fall 2008: "Math 331 Differential equations

Fall 2008: "Math 645 Differential equations and dynamical systems

Fall 2009: "Math 697EG Evolutionary game theory

Spring 2010: Math 697U Introduction to stochastic processes

Spring 2010: Math 331 Differential equations

Fall 2010: Math 623 Real analysis I

Fall 2010: Math 131H Honor calculus I

Fall 2011: Math 623 Real analysis I

Spring 2012: Math 624 Real analysis II

Spring 2012: Math 456 Mathematical Modeling

Spring 2013: Math 456 Mathematical Modeling

Spring 2013: Math797fn Functional Analysis

Fall 2013: Math 623 Real Analysis I

Spring 2014: Math 624 Real Analysis II

Spring 2014: Math 331 Differential equations

Fall 2014: "Math697U Introduction to stochastic processes

Spring 2015: Math 456 Mathematical Modeling

Spring 2015: Math 797MR Information Theory

Fall 2015: Math 797AB Agent-based modeling

Spring 2016: Math 456 Mathematical Modeling

Spring 2016: Math 523H Real analysis

Fall 2016: Math 797SM Statistical mechanics

Spring 2017: Math 331 Differential equations

Spring 2017: Math 523H Real analysis

Fall 2017: Stat 605 Probability Theory

Fall 2017: Math 331 Differential equations

Spring 2018: Math697U Stochastic Processes

Spring 2019: Math 456 Mathematical Modeling

% % % % %%\begin{tabular}{lll} %{ Courses:} & Fall 2002& Math 131 Calculus I \ % & Spring 2003 & Math 132 Calculus II \ % & Spring 2003& Math 421 Complex variables \ % & Fall 2003& Math 597/697 Introduction to stochastic processes\ % & Spring 2004& Math 131 Calculus I \ % & Fall 2004& Math 645 Differential equations and dynamical systems \ % & Spring 2005& Math 646 Ergodic theory \ % & Spring 2005& Math 131 Calculus I \ % & Fall 2005& Math 645 Differential equations and dynamical systems\ % & Fall 2005& Stat 515 Introduction to Statistics I \ % & Spring 2006& Math597/697 Introduction to stochastic processes\ % & Fall 2006& Math 623 Real analysis I \ % & Fall 2006& Math 131H Honor calculus I \ % & Spring 2007& Math 624 Real analysis II \ % & Fall 2007& Math 697U Introduction to stochastic processes \ % & Fall 2007& Math 331 Differential equations \ % & Spring 2008& Math 331 Differential equations \ % & Fall 2008& Math 645 Differential equations and dynamical systems\ % & Fall 2009 & Math 697EG Evolutionary game theory \ % & Spring 2010 & Math 697U Introduction to stochastic processes % \end{tabular} % %%\begin{tabular}{1} % & Spring 2010 & Math 697U Introduction to stochastic processes % \end{tabular} % % Spring 2010 & Math 697U Introduction to stochastic processes % \end{tabular} % % Spring 2010 & Math 697U Introduction to stochastic processes % \end{tabular} % % Spring 2010 & Math 697U Introduction to stochastic processes % \end{tabular} % % Spring 2010 & Math 697U Introduction to stochastic processes % \end{tabular} % % Spring 2010 & Math 697U Introduction to stochastic processes % \end{tabular} % % Spring 2010 & Math 697U Introduction to stochastic processes % \end{tabular} % % Spring 2010 & Math 697U Introduction to stochastic processes % \end{tabular} % Spring 2010 & Math 697U Introduction to stochastic processes % \end{tabular} % Spring 2010 & Math 697U Introduction to stochastic processes % \end{tabular} % Spring 2010 & Math 697U Introduction to stochastic processes % \end{tabular} % Spring 2010 & Math

2010 & Math 331 Differential equations \ % & Fall 2010 & Math 623 Real analysis I \ % & Fall 2010 & Math 131H Honor calculus I \ % & Fall 2011 & Math 623 Real analysis I \ % & Spring 2012 & Math 624 Real analysis II \ % & Spring 2012 & Math 456 Mathematical Modeling \ % & Spring 2013 & Math 797fn Functional Analysis \ % & Fall 2013& Math 623 Real Analysis I \ % & Spring 2014& Math 624 Real Analysis II \ % & Spring 2014& Math 623 Real Analysis I \ % & Fall 2014& Math 697U Introduction to stochastic processes \ % & Spring 2015 & Math 456 Mathematical Modeling \ % & Spring 2015 & Math 797MR Information Theory \ % & Fall 2015 & Math 797AB Agent-based modeling \ % & Spring 2016 & Math 456 Mathematical Modeling \ % & Spring 2016 & Math 523H Real analysis \ % & Fall 2016 & Math 797SM Statistical mechanics \ % & Spring 2017 & Math 331 Differential equations \ % & Fall 2017 & Math 331 Differential equations \ % & Fall 2017 & Math 331 Differential equations \ % & Fall 2017 & Math 331 Differential equations \ % & Spring 2018 & Math697U Stochastic Processes \ % & Spring 2019 & Math 456 Mathematical Modeling % \end{tabular}

{ University of Virginia} 1999-2002

Fall 1999: "APMA 310 Probability

Spring 2000: APMA 206, Differential equations (2 sections)

Fall 2000: "APMA 310 Probability

Fall 2000: "Math 531 Introduction to real analysis I

Spring 2001: Math 532 Introduction to real analysis II

Fall 2001: "Math 131 Calculus I (2 sections)

Spring 2002: Math 845 Ergodic Theory

% %%\begin{tabular}{lll} %{ Courses:} & Fall 1999& APMA 310 Probability \ % & Spring 2000& APMA 206, Differential equations (2 sections) \ % & Fall 2000& APMA 310 Probability \ % & Fall 2000& Math 531 Introduction to real analysis I \ % & Spring 2001& Math 532 Introduction to real analysis II \ % & Fall 2001& Math 131 Calculus I (2 sections) \ % & Spring 2002& Math 845 Ergodic Theory %\end{tabular}

% %KK %% Research Fellow 1998–1999}, Center for Mathematical Sciences Research, %Department of Mathematics, Rutgers University, New Brunswick NJ 08854.

{ University of Geneva}, 1994-1998 (Teaching assistant)

1994-1995: Mathematics II for computer scientists

1994-1995: Function of several complex variables

1995-1996: Analysis I

1995-1996: Dynamical systems and ergodic theory

1996-1997: Mathematics for engineers

1996-1997: Numerical methods for PDE

1997-1998: Analysis II

%~%~%~%~% begin{tabular}{lll} %{ Courses:} & 1994-1995& Mathematics II for computer scientists \ % & 1994-1995& Function of several complex variables \ % & 1995-1996& Analysis I \ % & 1995-1996& Dynamical systems and ergodic theory \ % & 1996-1997& Mathematics for engineers \ % & 1996-1997& Numerical methods for PDE \ % & 1997-1998& Analysis II %\end{tabular}