

Curriculum Vitae: Luc Rey-Bellet

Contact Information

[arXiv:2407.11901](https://arxiv.org/abs/2407.11901)

Educational History:

- **Ph.D. in Mathematics (1998):** Department of Mathematics, University of Geneva, Geneva, Switzerland. Advisor: *Prof. Jean-Pierre Eckmann*
- **Dipl. Phys. ETHZ (1994):** , Department of Physics, Swiss Federal Institute of Technology (ETHZ), Zurich, Switzerland. Advisor: *Prof. Jürg Fröhlich*

Professional appointments:

- **Research Fellow:** Rutgers University 1998-1999
- **Whyburn Instructor:** University of Virginia 1999-2002
- **Assistant Professor:** University of Massachusetts 2002-2008
- **Associate Professor:** University of Massachusetts 2008-2013
- **Visiting Professor:** University of Crete 2011 (Spring semester)
- **Professor:** University of Massachusetts since 2013

Selected recent service

- Editorial board of Journal of Statistical Physics 2013–2018
- Organizer of the Oberwolfach seminar on Markov processes, 2011
- Organizer of the Conference in honor of J.P. Eckmann 75th birthday, 2022
- Organizer of ICERM Workshop on Optimal Transport and Machine Learning, 2023

Grant funding

- FNRS Bourse de jeune chercheur 1999 (SFr 45k)
- NSF Grant 2003 (3 year, PI, \$101K)
- NSF Grant 2006 (3 year, PI, \$106K)
- NSF Grant 2011 (3 Year, PI, \$99K)
- NSF Grant 2015 (3 year, PI (with 1 Co-PI) \$280K)
- DOE Grant 2016 (3 year, co-PI (with 4 PI) \$900K)
- AFOSR Grant 2019 (3 year, co-PI (with 2 PIs) \$900 K)
- NSF Grant 2020 (3 year, PI (with 1 Co-PI) \$ 370K)
- AFOSR Grant 2021 (4 year (with 2 PIs) \$1.950M)
- NSF Grant 2023 (3 year, PI (with 1 Co-PI) \$300K)

Graduate students and postdoctoral advising:

- Dimitrios Tsagkarogiannis (Graduation 2006, University of L'Aquila)
- Michael Diehl (Graduation 2008, Endicott College)
- Sasanka Are (Graduation 2009, Cerner Corporation)
- Sung-Ha Hwang (Graduation 2011, KAIST, Korea)
- Yannis Pantazis (Postdoctoral fellow, 2012-2013, and 2014-2015, Forth Crete)
- Kostis Gourgoulas (Graduation 2017, JP Morgan)
- Georgios Arampatzis (Postdoctoral fellow, 2014-2015, University of Crete)
- Jinchao Feng (Graduation 2019, John Hopkins University)
- Jie Wang (Graduation 2019, Discover)
- Jeremiah Birrell (Postdoctoral fellow, 2017-2022, Texas State University)
- Pangioti Birmpa (Postdoctoral fellow, 2018-2022, Heriott-Watt University)
- Hyemin Gu (Graduate Student since 2021)
- Benjamin Zhang (Postdoctoral fellow, 2022-2024, UNC Chapel Hill)
- Ziyu Chen (Postdoctoral fellow, 2022-2025, UNC Chapel Hill)
- Thejani Gamage (Postdoctoral fellow, 2024-)

Publications

- Hyemin Gu, Markos A. Katsoulakis, Luc Rey-Bellet, and Benjamin J. Zhang. **Combining Wasserstein-1 and Wasserstein-2 proximals: robust manifold learning via well-posed generative flows.** Submitted.
arXiv:2407.11901

Jeremiah Birrell, Markos A. Katsoulakis, Luc Rey-Bellet, Benjamin Zhang, and Wei Zhu.
Nonlinear denoising score matching for enhanced learning of structured distributions.

Submitted.
arXiv:2405.15625

Ziyu Chen, Hyemin Gu, Markos A. Katsoulakis, Luc Rey-Bellet, and Wei Zhu.
Learning heavy-tailed distributions with Wasserstein-proximal-regularized - divergences. Submitted.
arXiv:2405.13962

Ziyu Chen, Markos A. Katsoulakis, Luc Rey-Bellet, and Wei Zhu.
Statistical Guarantees of Group-Invariant GANs. Submitted.
arXiv:2305.13517

Ziyu Chen, Markos A. Katsoulakis, Luc Rey-Bellet, and Wei Zhu.
Sample Complexity of Probability Divergences under Group Symmetry.
Proceedings of 40th International Conference on Machine Learning, PMLR 202 (2023)
pp. 4713-4734.
Online Version Reprint in PDF (including supplementary materials)

Hyemin Gu, Panagioti Birmpa, Yannis Pantazis, Luc Rey-Bellet, and Markos A. Katsoulakis.
Lipschitz-regularized gradient flows and generative particle algorithms for high-dimensional scarce data.
To appear in Siam Journal on Mathematics of Data Science (2024).
arXiv:2210.17230

Jeremiah Birrell, Paul Dupuis, Markos Katsoulakis, Yannis Pantazis, and Luc Rey-Bellet.
Function-space regularized Rényi divergences.
Proceedings of The Eleventh International Conference on Learning Representations (ICLR 2023).
Poster and Slides Open review Reprint in PDF

Jeremiah Birrell, Markos Katsoulakis, Luc Rey-Bellet, and Wei Zu.
Structure-preserving GANs.
Proceedings of the 39th International Conference on Machine Learning, PMLR 162 (2022),
pp.1982-2020.
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Panagioti Birmpa, Jinchao Feng, Markos Katsoulakis, and Luc Rey-Bellet.
Model Uncertainty and Correctability for Directed Graphical Models.
SIAM/ASA Journal on Uncertainty Quantification 10 (2022), no.4, pp 1461–1512.

DOI:10.1137/21M1434453 Reprint in PDF

Jeremiah Birrell, Paul Dupuis, Markos Katsoulakis, Yannis Pantazis, and Luc Rey-Bellet.
(f,Γ)-Divergences: Interpolating between f-Divergences and Integral Probability Metrics.
Journal of Machine Learning Research 23 (2022), paper 39, pp.1–70.
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Jeremiah Birrell, Paul Dupuis, Markos A. Katsoulakis, Luc Rey-Bellet, and Jie Wang.
A variational formula for Rényi divergences.
SIAM Journal on Mathematics of Data Science 3 (2021), no. 4, pp. 1093-1116
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Jeremiah Birrell, Paul Dupuis, Markos A. Katsoulakis, Luc Rey-Bellet, and Jie Wang.
Distributional robustness and uncertainty quantification for rare events.
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Sung-Ha Hwang and Luc Rey-Bellet.
Positive feedback in coordination games: stochastic evolutionary dynamics and the logit choice rule.
Games and Economic Behavior 126 (2021), pp. 355-373
DOI: 10.1016/j.geb.2021.01.003 Reprint in PDF Supplementary Materials

Jeremiah Birrell, Markos Katsoulakis, and Luc Rey-Bellet.
Quantification of model uncertainty on path-space via goal-oriented relative entropy.
ESAIM: Mathematical Modeling and Numerical Analysis 55 (2021), no.1, pp. 131-169.
DOI: 10.1051/m2an/2020070 Reprint in PDF

Jeremiah Birrell and Luc Rey-Bellet.
Concentration inequalities and performance guarantees for hypocoercive MCMC samplers.
Preprint. arXiv:1907.11973 Preprint in PDF

Paul Dupuis, Markos Katsoulakis, Yannis Pantazis, and Luc Rey-Bellet.
Sensitivity analysis for rare events based on Rényi divergence.
The Annals of Applied Probability, 30 (2020), no.4, pp. 1507-1533.
DOI:10.1214/19-AAP1468 Reprint in PDF

Jeremiah Birrell and Luc Rey-Bellet.
Uncertainty quantification for Markov processes via variational principles and functional

inequalities.

SIAM/ASA Journal on Uncertainty Quantification, 8 (2020), no. 2, pp. 539–572.

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Konstantinos Gourgoulas, Markos Katsoulakis, Luc Rey-Bellet, and Jie Wang.

How biased is your model? Concentration inequalities, information and model bias. IEEE Transactions on Information Theory 66 (2020), no.5, pp. 3079–3097.

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Sung-Ha Hwang and Luc Rey-Bellet.

Simple characterizations of potential games and zero-sum equivalent games. Journal of Economic Theory and Econometrics, 31 (2020), pp. 1–13.

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Strategic decompositions of normal form games: potential games and zero-sum games.

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Mark Demers, Luc Rey-Bellet, and Hongkun Zhang.

Fluctuations of the entropy production for the Lorentz gas under small external forces.

Communications in Mathematical Physics 363 (2018), no. 2, pp. 699–740.

DOI: 10.1007/s00220-018-3228-3 MR3851827 Reprint in PDF

Noé Cuneo, Jean-Pierre Eckmann, Martin Hairer, and Luc Rey-Bellet.

Non-equilibrium steady states for networks of oscillators.

Electronic Journal of Probability 23 (2018), paper no. 55, 28 pp.

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Markos Katsoulakis, Luc Rey-Bellet, and Jie Wang.

Scalable information inequalities for uncertainty quantification.

Journal of Computational Physics 336 (2017), pp. 513–545.

DOI: 10.1016/j.jcp.2017.02.020 Reprint in PDF

Konstantinos Gourgoulas, Markos Katsoulakis, and Luc Rey-Bellet.

Information criteria for quantifying loss of reversibility in parallelized KMC.

Journal of Computational Physics 328 (2017), pp. 438–454.

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- Eric Hall, Markos Katsoulakis, and Luc Rey-Bellet.
 Uncertainty quantification for generalized Langevin dynamics.
 Journal of Chemical Physics 145 (2016), 224108.
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- Konstantinos Spiliopoulos and Luc Rey-Bellet.
 Improving the convergence of reversible samplers.
 Journal of Statistical Physics 164 (2016), no.3, 472–494.
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- Georgios Arampatzis, Markos Katsoulakis, and Luc Rey-Bellet.
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- Konstantinos Gourgoulis, Markos Katsoulakis, and Luc Rey-Bellet.
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 SIAM Journal on Scientific Computing 38 (2016), no. 6, pp. A3808–A3832.
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- Konstantinos Spiliopoulos and Luc Rey-Bellet.
 Variance reduction for irreversible Langevin samplers and diffusion on graphs.
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- Konstantinos Spiliopoulos and Luc Rey-Bellet.
 Irreversible Langevin samplers and variance reduction: a large deviation approach.
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- Markos Katsoulakis, Yannis Pantazis, and Luc Rey-Bellet.
 Measuring the irreversibility of numerical schemes for reversible stochastic differential equations.
 ESAIM: Mathematical Modelling and Numerical Analysis 48 (2014), no.5, pp. 1351–1379.
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- M. Katsoulakis, P. Plecháč, Luc Rey-Bellet, and D. Tsagkarogiannis.
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 Mathematics of Computation 83 (2014), no.288, pp. 1757–1793.
 DOI: 10.1090/S0025-5718-2014-02806-8 MR3194129 Reprint in PDF
- Sung-Ha Hwang, Luc Rey-Bellet, and Markos Katsoulakis.
 Deterministic equations for stochastic spatial evolutionary games.
 Theoretical Economics 8 (2013), no.3, pp. 829–874.
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- Andrea Nahmod, Hiro Oh, Luc Rey-Bellet, and Gigliola Staffilani.
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Journal of the European Mathematical Society 14 (2012), no.4, pp. 1275–1330.
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- Sung-Ha Hwang and Luc Rey-Bellet.
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arXiv:1106.3552 .
- Andrea Nahmod, Luc Rey-Bellet, Scott Sheffield, and Gigliola Staffilani.
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- Yoshiko Ogata and Luc Rey-Bellet.
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- Vojkan Jaksic, Claude-Alain Pillet, and Luc Rey-Bellet.
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- Sasanka Are, Markos Katsoulakis, Petr Plecháč, and Luc Rey-Bellet.
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- Markos Katsoulakis, Petr Plecháč, and Luc Rey-Bellet.
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Fourier Law.

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Luc Rey-Bellet.

Open Classical Systems.

In: *Quantum Open Systems II. The Markovian approach*. Stéphane Attal, Alain Joye, Claude-Alain Pillet (Eds.), *Lecture Notes in Mathematics* 1881, Berlin: Springer, 2006, pp. 41–78.

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Luc Rey-Bellet.

Ergodic Properties of Markov Processes.

In: *Quantum Open Systems II. The Markovian approach*. Stéphane Attal, Alain Joye, Claude-Alain Pillet (Eds.), *Lecture Notes in Mathematics* 1881, Berlin: Springer, 2006, pp. 1–39.

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Luc Rey-Bellet.

Nonequilibrium statistical mechanics of open classical systems.

In: *XIVth International Conference on Mathematical Physics*, Lisbon, Portugal, 28 July – 2 August 2003, World Scientific 2006, pp. 447–454

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Marco Lenci and Luc Rey-Bellet.

Large deviations in quantum lattice systems: one phase region.

Journal of Statistical Physics 119 (2005), no. 3-4, pp. 715–746.
DOI: 10.1007/s10955-005-3015-3 MR2151220 Reprint in PDF

Lawrence E. Thomas and Luc Rey-Bellet.

Low regularity solutions to a gently stochastic nonlinear wave equation in nonequilibrium statistical mechanics.

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Luc Rey-Bellet.

Statistical mechanics of anharmonic lattices.

In: Advances in Differential Equations and Mathematical Physics, AMS Contemporary Mathematics Series 327 (2003), pp. 283–298.

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Lawrence E. Thomas and Luc Rey-Bellet.

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Lawrence E. Thomas and Luc Rey-Bellet.

Exponential convergence to non-equilibrium stationary states in classical statistical mechanics.

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Jürg Fröhlich, Luc Rey-Bellet, and Daniel Ueltschi.

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Federico Bonetto, Joel Lebowitz, and Luc Rey-Bellet.

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- Sung-Ha Hwang and Luc Rey-Bellet, Simple characterizations of potential games and zero-sum equivalent games, *Journal of Economic Theory and Econometrics*, 31 (2020), pp. 1–13.
- Konstantinos Gourgoulas, Markos Katsoulakis, Luc Rey-Bellet, and Jie Wang, How biased is your model? Concentration inequalities, information and model bias, *IEEE Transactions on Information Theory* 66 (2020), no.5, pp. 3079–3097.
- Jeremiah Birrell and Luc Rey-Bellet, Uncertainty quantification for Markov processes via variational principles and functional inequalities, *SIAM/ASA Journal on Uncertainty Quantification*, 8 (2020), no. 2, pp. 539–572.

Paul Dupuis, Markos Katsoulakis, Yannis Pantazis, and Luc Rey-Bellet, Sensitivity analysis for rare events based on Rényi divergence, *The Annals of Applied Probability*, 30 (2020), no.4, pp. 1507-1533.

Jeremiah Birrell and Luc Rey-Bellet Concentration inequalities and performance guarantees for hypocoercive MCMC samplers, Preprint.

Jeremiah Birrell, Markos Katsoulakis, and Luc Rey-Bellet, Quantification of model uncertainty on path-space via goal-oriented relative entropy, *ESAIM: Mathematical Modeling and Numerical Analysis* 55 (2021), no.1, pp. 131-169.

Sung-Ha Hwang and Luc Rey-Bellet, Positive feedback in coordination games: stochastic evolutionary dynamics and the logit choice rule, *Games and Economic Behavior* 126 (2021), pp. 355-373.

Jeremiah Birrell, Paul Dupuis, Markos A. Katsoulakis, Luc Rey-Bellet, and Jie Wang, Distributional robustness and uncertainty quantification for rare events, Preprint.

Jeremiah Birrell, Paul Dupuis, Markos A. Katsoulakis, Luc Rey-Bellet, and Jie Wang, A variational formula for Rényi divergences, *SIAM Journal on Mathematics of Data Science* 3 (2021), no. 4, pp. 1093-1116

Jeremiah Birrell, Paul Dupuis, Markos Katsoulakis, Yannis Pantazis, and Luc Rey-Bellet, (f, Γ) -Divergences: Interpolating between f -Divergences and Integral Probability Metrics, *Journal of Machine Learning Research* 23 (2022), paper 39, pp.1–70.

Panagiota Birmpa, Jinchao Feng, Markos Katsoulakis and Luc Rey-Bellet, Model Uncertainty and Correctability for Directed Graphical Models, *SIAM/ASA Journal on Uncertainty Quantification* 10 (2022), no.4, pp 1461–1512.

Jeremiah Birrell, Markos Katsoulakis, Luc Rey-Bellet, Wei Zu Structure-preserving GANs, *Proceedings of the 39th International Conference on Machine Learning*, PMLR 162 (2022) pp.1982-2020.

Jeremiah Birrell, Paul Dupuis, Markos Katsoulakis, Yannis Pantazis, Luc Rey-Bellet Function-space regularized Rényi divergences. *Proceedings of The Eleventh International Conference on Learning Representations (ICLR 2023)*.

Hyemin Gu, Panagiota Birmpa, Yannis Pantazis, Luc Rey-Bellet, and Markos A. Katsoulakis, *Lipschitz-regularized gradient flows and generative particle algorithms for high-dimensional scarce data*, Submitted.

Ziyu Chen, Markos A. Katsoulakis, Luc Rey-Bellet, and Wei Zhu, *Sample Complexity of Probability Divergences under Group Symmetry*, Submitted

Ziyu Chen, Markos A. Katsoulakis, Luc Rey-Bellet, and Wei Zhu, *Statistical Guarantees of Group-Invariant GANs*, Submitted.

Invited talks

- Journées semi-classiques 1998, Grenoble, February 1998
- Statphys 20, Paris, July 1998
- 80th Statistical mechanics conference, Rutgers University, December 1998
- Non equilibrium statistical mechanics, Schrodinger Institute, February 1999
- The 2002 UAB International conference mathematical physics, March 2002
- Workshop on Fokker-Planck equations, Rennes, France, February 2003
- ODYN-II, Probability and statistical mechanics, CIRM, Marseilles, March 2003
- 89th Statistical mechanics conference, Rutgers university, May 2003
- Summer school on open quantum systems, Grenoble, July 2003
- International congress of mathematical physics, ICMP 2003, Lisbon, August 2003
- Young researcher symposium, Lisbon, July 2003
- Workshop on dynamics and statistical mechanics, CRM, Montreal, August 2004
- SIAM conference on applications of dynamical systems, Snowbird, May 2005
- International congress on the applications of mathematics, Santiago, March 2006
- Workshop on statistical mechanics, CPT-CNRS, Marseilles, July 2006
- 96th Statistical mechanics Conference, Rutgers University, December 2006
- Workshop on nonequilibrium statistical mechanics, Vienna, June 2008
- Workshop on stochastic dynamical systems, Bielefeld, November 2008
- Arizona school of analysis with applications I, University of Arizona, March 2009
- NORDITA Stockholm, Multiscale modeling and simulation in science, November 2009
- SAMSI, Theory and qualitative behavior of stochastic dynamics, February 2010
- Indam meeting, Corinaldo, Hyperbolic dynamical systems in the sciences, June 2010
- SIAM conference on nonlinear waves and coherent structures, August 2010
- Oberwolfach seminar on ergodic theory of Markov processes, October 2010
- 105th Statistical mechanics Conference, Rutgers University, May 2011
- FRG workshop on quantum spin systems, Harvard University, May 2011
- Workshop on Coarse-graining of many-body systems. Heraklion, June 2011
- ENUMATH conference. September 2011
- Three hours course on statistical mechanics), Ecole des Ponts, September 2011
- SIAM conference on material sciences, Philadelphia, June 2013
- SPA conference (Stochastic processes and applications), Boulder, August 2013
- AMS sectional meeting, Session on dynamical systems. Saint Louis, October 2013
- Randomness and Long-Time Dynamics, Radcliffe Institute, November 2014
- CIRM Workshop on Averaging and Homogenization, Marseille, May 2015
- CRiSM Workshop on Non-Reversible Markov Chains, Warwick, September 2015
- Meeting of the Canadian Mathematical Society, Montreal, December 2015
- 114th Statistical Mechanics Conference, Rutgers, December 2015
- Computational Statistics and Molecular Simulation (COSMOS), Paris, February 2016
- Numerical Aspects of Nonequilibrium Dynamics, Paris, April 2017
- BIRS-CMO Workshop, Oaxaca, November 2018

- Workshop on Entropic Fluctuation Relations, Montreal, October 2018
- Ki-Net: Dimension reduction in physical and data sciences. Duke. April 2019
- Bernoulli Center, EPFL, May 2019
- Quantissima III, Venice, August 2019.
- Non Reversible Markovian Monte-Carlo Methods, Lorentz Center, August 2021
- Meetings on Foundations of Data Science, Tufts University, March 2022
- AFOSR PI Meeting, Arlington, VA, August 2022
- Conference in Honor of J.P. Eckmann 75th birthday, Geneva, Switzerland, June 2022
- ICML 2022, Baltimore, Poster presentation, July 2022
- Neurips 2022, New orleans, Poster presentation, December 2022
- ICLR 2023, Kigali, Rwanda, Poster presentation, April 2023
- AFOSR PI Meeting, Arlington, VA, August 2023
- AFOSR PI Meeting, Arlington, VA, August 2024
- ICERM Meeting. Providence, RI, September 2024
- JMM Meeting. Seattle, WA, January 2025
- IPAM Workshop. Los Angeles, CA, July 2025

Seminar talks

- Mathematical physics seminar, ETH, Zürich January 1998
- Mathematical physics seminar, CPT-CNRS, Marseille, January 1998
- Mathematical physics seminar, Institut Fourier Grenoble, February 1998
- Mathematical physics seminar, University Paris-XI Orsay, April 1998
- Mathematical physics seminar, University of Virginia, November 1998
- Colloquium, University of Ottawa, January 1999
- Statistical mechanics seminar, Princeton University, February 1999
- Mathematical physics seminar, University of Geneva, July 1999
- Dynamical systems seminar, SUNY at Stony Brook, November 1999
- Mathematical physics seminar, University of Geneva, July 2000
- Mathematical physics seminar, ETH, Zürich, August 2000
- Colloquium, University of Arizona, October 2000
- Statistical mechanics seminar, Princeton University, February 2001
- Applied mathematics seminar, University of Toronto, March 2001
- Theoretical physics seminar, University of Geneva, May 2001
- Mathematical physics seminar, ETH Zürich, June 2001
- Analysis seminar, University of Helsinki, August 2001
- Mathematical physics seminar, University of Texas at Austin, January 2002
- Colloquium, University of Massachusetts, Amherst, January 2002
- Colloquium, University of Maryland, College Park, January 2002
- Colloquium, University of Rochester, February 2002
- Colloquium, University of Notre Dame, February 2002
- Statistical mechanics seminar, Institute of Advanced Study, February 2002

- Nonlinear analysis seminar, Stevens Institute of Technology, May 2002
- Mathematical physics seminar, Rutgers University, October 2002
- Stochastic processes seminar, Brown University, November 2002
- Mathematical physics seminar, University of Virginia, January 2003
- Condensed matter seminar, University of Massachusetts, April 2003
- Probability seminar, EPFL, Lausanne, June 2003
- Mathematical physics seminar, University of Geneva, June 2003
- Applied mathematics seminar, Duke University, March 2004
- Mathematical physics seminar, University of Geneva, January 2005
- Analysis and numerics seminar, Munich University, January 2005
- Mathematical physics seminar, Munich University, January 2005
- Dynamical systems seminar, Boston University, April 2005
- Nonlinear systems seminar, Stevens Institute of Technology, April 2005
- Mathematical physics seminar, Rutgers University, September 2005
- Mathematical physics seminar, University of Virginia, November 2006
- Mathematical physics seminar, Rutgers University, November 2006
- Applied mathematics seminar, Dartmouth College, April 2007
- Mathematical physics seminar, University of Arizona, October 2007
- Analysis seminar, University of Toronto, October 2007
- Applied mathematics seminar, Brown University, November 2007
- Colloquium, University of Connecticut, February 2009
- Probability seminar, University of Wisconsin, March 2009
- Theoretical physics Seminar, University of Geneva, April 2009
- Mathematical physics Seminar, University of Rome, April 2009
- Mathematical physics Seminar, University of Bologna, April 2009
- Mathematical physics Seminar, University of Grenoble, May 2009
- Applied mathematics Seminar, University of Crete, May 2009
- Mathematical physics seminar, Rutgers University, November 2009
- Operator algebra, University of Tokyo, January 2010
- Joint PDE seminar Boston University – Brown University, November 2010
- Applied Mathematics Seminar, University of Crete, March 2011
- Probability Seminar, Warwick University, March 2011
- Probability Seminar, Boston University, September 2012
- Probability Seminar, University of Delaware, October 2013
- Probability Seminar, Concordia University, May 2015
- Probability Seminar, Brown University, November 2016
- Mathematical physics seminar, Rutgers University, December 2017
- Dynamical systems seminar, Courant Institute, NYU January 2018
- Applied PDE seminar, Imperial College, November 2020
- Probability seminar KTH, November 2020
- Probability and Statistics Seminar, Boston University, November 2024

Teaching Experience

University of Massachusetts Amherst (since 2002)

Fall 2002: „ Math 131 Calculus I

Spring 2003: Math 132 Calculus II

Spring 2003: Math 421 Complex variables

Fall 2003: „ Math 597/697 Introduction to stochastic processes

Spring 2004: Math 131 Calculus I

Fall 2004: „ Math 645 Differential equations and dynamical systems

Spring 2005: Math 646 Ergodic theory

Spring 2005: Math 131 Calculus I

Fall 2005: „ Math 645 Differential equations and dynamical systems

Fall 2005: „ Stat 515 Introduction to Statistics I

Spring 2006: Math 597/697 Introduction to stochastic processes

Fall 2006: „ Math 623 Real analysis I

Fall 2006: „ Math 131H Honor calculus I

Spring 2007: Math 624 Real analysis II

Fall 2007: „ Math 697U Introduction to stochastic processes

Fall 2007: „ Math 331 Differential equations

Spring 2008: Math 331 Differential equations

Fall 2008: „ Math 331 Differential equations

Fall 2008: „ Math 645 Differential equations and dynamical systems

Fall 2009: „ Math 697EG Evolutionary game theory

Spring 2010: Math 697U Introduction to stochastic processes

Spring 2010: Math 331 Differential equations

Fall 2010: Math 623 Real analysis I

Fall 2010: Math 131H Honor calculus I

Fall 2011: Math 623 Real analysis I

Spring 2012: Math 624 Real analysis II

Spring 2012: Math 456 Mathematical Modeling
 Spring 2013: Math 456 Mathematical Modeling
 Spring 2013: Math797fn Functional Analysis
 Fall 2013: Math 623 Real Analysis I
 Spring 2014: Math 624 Real Analysis II
 Spring 2014: Math 331 Differential equations
 Fall 2014: „, Math697U Introduction to stochastic processes
 Spring 2015: Math 456 Mathematical Modeling
 Spring 2015: Math 797MR Information Theory
 Fall 2015: Math 797AB Agent-based modeling
 Spring 2016: Math 456 Mathematical Modeling
 Spring 2016: Math 523H Real analysis
 Fall 2016: Math 797SM Statistical mechanics
 Spring 2017: Math 331 Differential equations
 Spring 2017: Math 523H Real analysis
 Fall 2017: Stat 605 Probability Theory
 Fall 2017: Math 331 Differential equations
 Spring 2018: Math697U Stochastic Processes
 Spring 2019: Math 456 Mathematical Modeling

% % % % % %\begin{tabular}{lll} % { Courses:} & Fall 2002& Math 131 Calculus I \ %
 & Spring 2003 & Math 132 Calculus II \ % & Spring 2003& Math 421 Complex variables \ %
 & Fall 2003& Math 597/697 Introduction to stochastic processes \ % & Spring 2004& Math
 131 Calculus I \ % & Fall 2004& Math 645 Differential equations and dynamical systems \ %
 & Spring 2005& Math 646 Ergodic theory \ % & Spring 2005& Math 131 Calculus I \ %
 & Fall 2005& Math 645 Differential equations and dynamical systems \ % & Fall 2005& Stat
 515 Introduction to Statistics I \ % & Spring 2006& Math597/697 Introduction to stochastic
 processes \ % & Fall 2006& Math 623 Real analysis I \ % & Fall 2006& Math 131H Honor
 calculus I \ % & Spring 2007& Math 624 Real analysis II \ % & Fall 2007& Math 697U
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 & Spring 2008& Math 331 Differential equations \ % & Fall 2008 & Math 331 Differential
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 2009 & Math 697EG Evolutionary game theory \ % & Spring 2010 & Math 697U Introduction
 to stochastic processes % \end{tabular} % %\begin{tabular}{lll} % {
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2010 & Math 331 Differential equations \ % & Fall 2010 & Math 623 Real analysis I \ % & Fall 2010 & Math 131H Honor calculus I \ % & Fall 2011 & Math 623 Real analysis I \ % & Spring 2012 & Math 624 Real analysis II \ % & Spring 2012 & Math 456 Mathematical Modeling \ % & Spring 2013 & Math 456 Mathematical Modeling \ % & Spring 2013 & Math 797fn Functional Analysis \ % & Fall 2013 & Math 623 Real Analysis I \ % & Spring 2014 & Math 624 Real Analysis II \ % & Spring 2014 & Math 331 Differential equations \ % & Fall 2014 & Math 697U Introduction to stochastic processes \ % & Spring 2015 & Math 456 Mathematical Modeling \ % & Spring 2015 & Math 797MR Information Theory \ % & Fall 2015 & Math 797AB Agent-based modeling \ % & Spring 2016 & Math 456 Mathematical Modeling \ % & Spring 2016 & Math 523H Real analysis \ % & Fall 2016 & Math 797SM Statistical mechanics \ % & Spring 2017 & Math 331 Differential equations \ % & Spring 2017 & Math 523H Real analysis \ % & Fall 2017 & Stat 605 Probability Theory \ % & Fall 2017 & Math 331 Differential equations \ % & Spring 2018 & Math 697U Stochastic Processes \ % & Spring 2019 & Math 456 Mathematical Modeling % \end{tabular}

{ University of Virginia} 1999-2002

Fall 1999: \ , APMA 310 Probability

Spring 2000: APMA 206, Differential equations (2 sections)

Fall 2000: \ , APMA 310 Probability

Fall 2000: \ , Math 531 Introduction to real analysis I

Spring 2001: Math 532 Introduction to real analysis II

Fall 2001: \ , Math 131 Calculus I (2 sections)

Spring 2002: Math 845 Ergodic Theory

% % %%\begin{tabular}{lll} % { Courses:} & Fall 1999& APMA 310 Probability \ % & Spring 2000& APMA 206, Differential equations (2 sections) \ % & Fall 2000& APMA 310 Probability \ % & Fall 2000& Math 531 Introduction to real analysis I \ % & Spring 2001& Math 532 Introduction to real analysis II \ % & Fall 2001& Math 131 Calculus I (2 sections) \ % & Spring 2002& Math 845 Ergodic Theory % \end{tabular}

% %KK %%{ Research Fellow 1998–1999}, Center for Mathematical Sciences Research, %Department of Mathematics, Rutgers University, New Brunswick NJ 08854.

{ University of Geneva}, 1994-1998 (Teaching assistant)

1994-1995: Mathematics II for computer scientists

1994-1995: Function of several complex variables

1995-1996: Analysis I

1995-1996: Dynamical systems and ergodic theory

1996-1997: Mathematics for engineers

1996-1997: Numerical methods for PDE

1997-1998: Analysis II

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scientists \ % & 1994-1995& Function of several complex variables \ % & 1995-1996& Analysis  
I \ % & 1995-1996& Dynamical systems and ergodic theory \ % & 1996-1997& Mathematics  
for engineers \ % & 1996-1997& Numerical methods for PDE \ % & 1997-1998& Analysis II  
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