Math 331.2: Homework 11 (Section 6.3, 6.4, 6.5)

For the following function find the inverse Laplace transform.

1.
$$\frac{5e^{-4s}}{s^2+4}$$

$$2. \ \frac{1 - e^{-s} - e^{-2s} - e^{-3s} - e^{-4s}}{s}$$

3.
$$\frac{2e^{-4s}s}{s^2+4s+9}$$

$$4. \ \frac{1 - 3e^{-4s}}{s^2 - 6s + 18}$$

For the following problems, using Laplace transform, solve the initial value problem and make a graph of the solutions.

5.
$$y' + 3y = h(t)$$
, $y(0) = -1$, where $h(t) = \begin{cases} 2 & 0 \le t < 4 \\ 5 & t \ge 4 \end{cases}$

6.
$$y' - 5y = 2\delta(t - 2) - 2\delta(t - 4)$$
, $y(0) = 0$

7.
$$y' + 4y = 3u_4(t)\cos(3(t-4)), \ y(0) = 0$$

8.
$$y'' + 2y = 2u_5 + u_7(t)$$
, $y(0) = 0$, $y'(0) = -2$

9.
$$y'' + 3y' + \frac{5}{2}y = 3\delta(t-2), \ y(0) = 1, \ y'(0) = -3$$

10.
$$y'' + 7y' + 6y = g(t)$$
, $y(0) = 0$, $y'(0) = 1$, where $g(t) = \begin{cases} 3 & 0 \le t < 2 \\ -2 & t \ge 2 \end{cases}$

11.
$$y'' + 2y' + 3y = \delta(t - 4) + 2u_3(t), y(0) = 0, y'(0) = 0$$

12.
$$y'' + y = u_3(t)e^{-2(t-3)}$$
, $y(0) = 0$, $y'(0) = 0$