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Assign all the \vec{Z}_i axes

- revolute joint
- prismatic joint

Along the i th joint axis \vec{Z}_i towards the direction to \vec{Z}_{i+1} preferably (otherwise, so as to cause the least possible change with regard to \vec{Z}_{i-1})

$i = 1$

Assign O_i , the origin of frame R_i

- \vec{Z}_i and \vec{Z}_{i+1} intersect: O_i located at the intersection of \vec{Z}_i and \vec{Z}_{i+1}
- \vec{Z}_i and \vec{Z}_{i+1} do not intersect: O_i located at the intersection of \vec{Z}_i with the common normal to axes \vec{Z}_i and \vec{Z}_{i+1}
- \vec{Z}_i and \vec{Z}_{i+1} coaxial: O_i anywhere along the axis (but at a known distance)

Assign \vec{X}_i axis

- \vec{Z}_i and \vec{Z}_{i+1} intersect: $\vec{X}_i = \vec{Z}_i \wedge \vec{Z}_{i+1}$. Choose direction freely (but, so as to cause the least possible change with regard to \vec{X}_{i-1})
- \vec{Z}_i and \vec{Z}_{i+1} do not intersect: Along the common normal to \vec{Z}_i and \vec{Z}_{i+1} (preferably pointing towards \vec{Z}_{i+1})
- \vec{Z}_i and \vec{Z}_{i+1} coaxial: Choose direction freely but observing $\vec{X}_i \perp \vec{Z}_i$ (try to cause the least possible change with regard to \vec{X}_{i-1})

Assign frame R_0

- If known, assign O_0 at the specified location away from O_1
- Otherwise, if not specified, assign origin O_0 to match O_1

assign frame R_0 to match R_1 when $q_1 = 0$

Assign end effector frame R_e

O_e located at the center of the end effector

\vec{Z}_e pointing in the direction of the object to be gripped

\vec{Y}_e perpendicular to \vec{Z}_e in the sliding plane of the gripper

$\vec{X}_e = \vec{Y}_e \wedge \vec{Z}_e$ so as to obtain a right-handed frame

Symbol	Name	Description
a_{i-1}	Link Length	$\vec{Z}_{i-1} \xrightarrow{\perp, \text{distance}} \vec{Z}_i$ @ \vec{X}_{i-1}
α_{i-1}	Twist Angle	$\vec{Z}_{i-1} \xrightarrow{\curvearrowright, \text{rotation}} \vec{Z}_i$ @ \vec{X}_{i-1}
d_i	Joint Offset	$\vec{X}_{i-1} \xrightarrow{\perp, \text{distance}} \vec{X}_i$ @ \vec{Z}_i
θ_i	Joint Angle	$\vec{X}_{i-1} \xrightarrow{\curvearrowright, \text{rotation}} \vec{X}_i$ @ \vec{Z}_i

Fill in the DHKK table

Check that you have only one q variable per row

	Joint	σ_i	a_{i-1}	α_{i-1}	d_i	θ_i
0T_1	1					
1T_2	2					
...	...					
${}^{n-1}T_n$	n					

${}^{i-1}T_i = \begin{bmatrix} C\theta_i & -S\theta_i & 0 & a_{i-1} \\ S\theta_i C\alpha_{i-1} & C\theta_i C\alpha_{i-1} & -S\alpha_{i-1} & -d_i S\alpha_{i-1} \\ S\theta_i S\alpha_{i-1} & C\theta_i S\alpha_{i-1} & C\alpha_{i-1} & d_i C\alpha_{i-1} \\ 0 & 0 & 0 & 1 \end{bmatrix}$