

## Search Landscapes

The set of possible genotypes is the GA's search space,  $S$

Given genotypes of length  $L$  from alphabet of size  $A$ :

- The space has  $L$  dimensions which each have  $A$  possible values
- Therefore there are  $A^L$  possible genotypes in  $S$
- Each genotype is a point in the search space
- Genotypes are neighbours if they differ by one mutation

The structure of a search space determines how hard it will be to search

The search space can be visualised as a fitness landscape where the fitness of each genotype is the height at that point.

### Landscape Structures:

Needle-in-a-haystack:

All genotypes except for one have the same low fitness value, this is a very hard landscape to search. The fitness function is unhelpful as it has no gradient to exploit.

Random Landscape:

Hard to search since it's full of suboptimal genotypes that give us no information about the optimal solution.

A Nice Landscape:

- Local smoothness, nearby points have similar fitness = Correlation Structure
- High peaks are broad = Non-deceptive
- Can be divided into parts = Decomposable

We can define the distance between points  $a$  and  $b$  in terms of how easy it is for the algorithm to move between them

- $a$  and  $b$  are neighbours if  $a$  can reach  $b$  in one genetic operation (a single mutation)

### Modality:

- A landscape with one global optimum is **unimodal**
- A landscape with two optima is **bimodal**
- A landscape with many optima is **multimodal**

- A set of points that lie of hill-climbing routes that terminate at one local optimum are said to lie within the **basin of attraction** of that local optima.