ADVANCED DATA ANALYSIS FOR PSYCHOLOGICAL SCIENCE

Extra slides: Introduction to R

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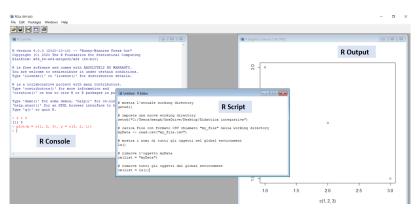
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- Download R from https://www.r-project.org/
 CRAN (Comprehensive R Archive Network): network of servers that provide upated software versions and related documentation
- Select CRAN from the Download menu on the left, then select a mirror mirror (e.g., the first or the uniPD's one), then select your OS (Linux, MacOS, or Windows)
- 3. Install R by opening the downloaded .exe (Windows) or .pkg (MacOS) or by following the commands required by your Linux version

The basic interfance



- · Console: to rapidly write (>) and execute (Enter key) the commands
- Script (File menu > New R Script): to write, modify, and save sequences of commands (saved with the .R format)
- Outputs (e.g., plot): graphical windows that opens when you run the command

RStudio

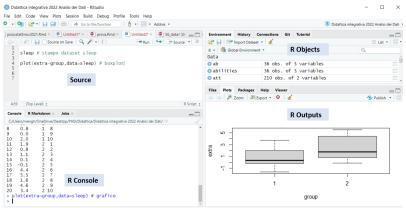
RStudio is a development environment for R using an optimized graphical interface to make it more simple (e.g., accessing files, objects, plots, datasets, etc.). It was founded in 2009 by J. J. Allaire (written in Java and C++) and is managed and developed by an international research group. Like R, it is free and open-source (GNU General Public Licence) + paid premium versions.

How to install RStudio

(note: after installing R)

- 1. Download RStudio from https://rstudio.com
- Select Download in the top menu, then select the "free" version of RStudio Desktop, then select your OS
- 3. Install RStudio by opening the downloaded file

The RStudio interface



- Source: R Scripts (.R), documents and presentations (.Rmd), applications (.app), etc. To
 run one or multiple commands, select them and tap on Ctrl + Enter or click on the Run
 button on the top-right of the window
- Environment: objects included in the workspace and History (history of executed commands)

[1] 21.81623

2

[1] 5

Some elementary commands

```
Comments (#)
# this is a comment
Simple mathematical operations
2 + 2 # sum
Γ17 4
2 * 2 # multiplication
[1] 4
log(3) # natural logarithm
[1] 1.098612
exp(1) # exponential function
[1] 2.718282
Longer expressions (with round brackets)
sart(5) * ((4 - 1/2)^2 - pi/2^(1/3))
```

```
Assigning values to objects (<-)
x \leftarrow 3 # creates the 'x' object with value 3
x # pint the value of x
[1] 3
Objects' names can include letters, numbers,
underscores, and, dots (e.g. tony, tony32.
tony.32, tony_32)
tony_32 <- x / 3 # assign a value to the object
tony_32 # print the object's value
[1] 1
R is kev-sensitive!
But it is not sensitive to spaces
3+2
Γ17 5
```

Hands on **Q**: Arithmetic operations

Perform the following operations using R. (solutions):

Source: Psicostat intro to R

$$1. \quad \frac{(45+21)^3 + \frac{3}{4}}{\sqrt{32 - \frac{12}{17}}}$$

Get started

2.
$$\frac{\mathbf{v}}{3(45-34)}$$

3.
$$\sqrt[3]{12 - e^2} + \ln(10\pi)$$

4.
$$\frac{\sin(\frac{3}{4}\pi)^2 + \cos(\frac{3}{2}\pi)}{\log_7 e^{\frac{3}{2}}}$$

5.
$$\frac{\sum_{n=1}^{10} r}{10}$$

Extra: Assign the result of operation #4 to the object x, then assign the result of operation #3 to the object y, and sum x and y. The result should be 5.76.

Hands on **R**: Relational & logical operators

Relational operators

Get started

```
3 == 3 # equal to
[1] TRUE
3 != 3 # different from
[1] FALSE
x >= 3 # higher than or equal to
[1] TRUE
5 %in% c(3, 5, 8) # included in
[1] TRUE
```

Logical operators

[1] TRUE

```
x <- TRUE
y <- !x # negation of
y
[1] FALSE
x & (5 < 2) # joined condition
[1] FALSE</pre>
```

x | (5 < 2) # inclusive disjoint

Exercises on relational & logical operators:

Source: Psicostat intro to B

- Define a proposition to test the following condition: "x is a number included between -4 and -2 or a number included between 2 and 4"
- Define two TRUE relationships and two
 FALSE relationship that let you test the
 results of all possible combinations using
 the logical operators & and |
- 3. Run the following operations: 4 ^ 3 %in% c(2,3,4) and 4 * 3 %in% c(2,3,4). What do you note in the execution order of the operators?

Objects & functions

Objects: identifying the values that have been saved in the workspace
 (Environment). Values are assigned to objects by using the <- symbol (minor and minus). To call an object, just write its name.

```
tony_32 <- 2 # assign a value to an object
tony_32 # print object
[1] 2
tony_32 <- tony_32 + 1 # update object
tony_32 # print again
[1] 3</pre>
```

Functions: labels associated to sequences of commands that were programmed
to return a specific output (called value) based on 1+ input values (called
argument). The function name is always followed by rounded brakes that include
the arguments. If no arguments are specified, default values are used.

```
sqrt(x = 9) # root square of the value assigned to the argument x [1] 3 seq(from = 1, to = 5) # numerical sequence between the 'from' and 'to' [1] 1 2 3 4 5
```

Types (classes) of objects

Logical

```
x <- TRUE
x <- T # writing "TRUE" or "T" is the same
class(x)
[1] "logical"</pre>
```

Numeric

```
x <- 1.4 class(x)
```

[1] "numeric"

Integer

```
as.integer(x)
[1] 1
```

Character

```
x <- "I like R"

x # within "" the space matters!
```

Vector: series of values with the same class (e.g., all numeric) combined with the function c() (combine)

```
x <- c(1, 10.5, 3, 2)

x + 1

[1] 2.0 11.5 4.0 3.0

sqrt(x)

[1] 1.000000 3.240370 1.732051 1.414214

y <- c("I","like", "R")
```

Matrix: table with nrow * ncol

An object of class vector is a sequence of values with the same class. It can be created with the combine function c() or with other functions.

```
x <- c(1, 10.5, 3, 2) # create a numeric vector
y <- 1:10 # create another numeric vector
(z <- rep(c(TRUE, FALSE), each = 2)) # create a logical vector
[1] TRUE TRUE FALSE FALSE
as.character(x) # convert the vector class from numeric to character
[1] "1" "10.5" "3" "2"
as.numeric(z) # from logical to numeric (FALSE = 0, TRUE = 1)
[1] 1 1 0 0</pre>
```

If we use a function on a vector, it applies to all the vectors' values.

```
y*2 # multiply all y values by 2
[1] 2 4 6 8 10 12 14 16 18 20
round(sqrt(y), 2) # root squared of y values, rounded at 2 digits
[1] 1.00 1.41 1.73 2.00 2.24 2.45 2.65 2.83 3.00 3.16
```

Some functions return a single value from a vector of values.

```
length(y) # return the number of vector elements
Γ17 10
```

For instance, functions that compute descriptive statistics:

```
sum(y) # sum the elements of y
Γ17 55
max(y) # maximum value
[1] 10
mean(y) # mean value
Γ13 5.5
median(y) # median value
Γ17 5.5
var(y) # variance
[1] 9.166667
sd(v) # standard deviation
[1] 3.02765
```

Squared brakes [] allow to select 1+ elements of the vector

```
tony32 <- c("one", "two", "three", "four", "five") # vector of characters
tony32[3] # select the third element
[1] "three"
tony32[3:5] # select from the third to the fifth element
[1] "three" "four" "five"
tony32[c(4, 2)] # fourth and second (not "tony32[4,2]"!)
[1] "four" "two"</pre>
```

For instance, we can \mathbf{select} those $\mathbf{elements}$ $\mathbf{meeting}$ $\mathbf{certain}$ $\mathbf{conditions}$ by using logical and relational operators:

```
y[y <= 3 | y > 8] # y values lower/equal to 3 or higher than 8

[1] 1 2 3 9 10

tony32[tony32 != "two"] # all values different from "two"

[1] "one" "three" "four" "five"

tony32[substr(tony32, 2, 2) == "w"] # values with the letter "w" in the 2nd position

[1] "two"
```

The which() function returns the position of the values meeting the condition

```
substr(tony32, 2, 2) == "w" # test equivalence for each value
[1] FALSE TRUE FALSE FALSE
which(substr(tony32, 2, 2) == "w") # position of values meeting the cond.
[1] 2
tony32[substr(tony32,2,2)=="w"] == tony32[which(substr(tony32,2,2)=="w")]
[1] TRUE
```

To replace 1+ values of a vector, use the symbol <-

```
tony32[1] <- "three"
```

To $\mathbf{remove}\ 1+\ \mathrm{values}\ \mathrm{from}\ \mathrm{a}\ \mathrm{vector},\ \mathrm{use}\ \mathrm{the}\ \mathrm{symbol}\ \mathsf{-}$

```
tony32[-c(2, 4)]
[1] "three" "three" "five"
```

An object of class factor is a special type of vector used in R to work with categorical variables (nominal and ordinal). The possible values of a factor are called levels, which are ordered increasingly by default (i.e., numeric or alphabetic order).

```
as.factor(tony32) # from character to factor
[1] three two
               three four five
Levels: five four three two
# summmarize the values of a vector
summary(tonv32)
  Length
              Class
                         Mode
        5 character character
# with factors, it shows the freq. by level
summary(as.factor(tony32)) # equivalent to table()
five four three
```

```
(y \leftarrow rep(c(2,4,6),3)) # numeric vector
[1] 2 4 6 2 4 6 2 4 6
as.factor(v) # from numeric to factor
[1] 2 4 6 2 4 6 2 4 6
Levels: 2 4 6
summary(y) # summary of numeric vector
  Min. 1st Qu. Median
                           Mean 3rd Qu.
                                             Max.
                                       6
                                                6
summary(as.factor(y)) # summary of factor
2 4 6
3 3 3
```

```
Create a factor with the function factor():
factor(x = c("C", rep("A", 3), c("B", "A", "C")))
[1] CAAABAC
Levels: A B C
(x <- factor(x = c("C", "A", "B", "A"), # vector
             levels = c("C", "A", "B"))) # levels
[1] CABA
Levels: C A B
levels(x) # levels() print the levels
[1] "C" "A" "B"
factor(x, levels=c("B","A","C")) # change order
[1] CABA
Levels: B A C
levels(x) <- c("Uno", "Due", "Tre") # change names</pre>
Х
[1] Uno Due Tre Due
Levels: Uno Due Tre
```

Factor levels can be **ordered** by setting the argument **ordered** = TRUE, which returns an ordrdinal variable based on the order defined by the levels argument.

```
# unordered factor (default)
vec <- c("Maria", "Mauro", "Teresa", "Carlo")</pre>
factor(x = vec)
[1] Maria Mauro Teresa Carlo
Levels: Carlo Maria Mauro Teresa
# ordered factor (default alphabetical order)
factor(x = vec. ordered = TRUE)
[1] Maria Mauro Teresa Carlo
Levels: Carlo < Maria < Mauro < Teresa
# ordered factor (setting a different order)
factor(x = vec, ordered = TRUE,
       levels=c("Teresa", "Mauro", "Maria", "Carlo"))
[1] Maria Mauro Teresa Carlo
```

Levels: Teresa < Mauro < Maria < Carlo

Classes of objects: matrix

A matrix is a bidimensional structure (nrow * ncol) of values with the same class, which can be created with the function:

```
matrix(data, nrow = , ncol = , byrow = FALSE)
```

```
(x \leftarrow matrix(1:12, nrow = 3, ncol = 4))
     [,1] [,2] [,3] [,4]
[1,]
                    10
[2,]
       2 5
                    11
[3,]
       3
          6
                 9 12
matrix(1:12, nrow = 3, ncol = 4, byrow = TRUE)
     [,1] [,2] [,3] [,4]
[1,]
            2
[2,]
       5
          6
[3.]
            10
                11
                     12
matrix(c("Mar", "Mau", "Ter", "Car"), nrow = 2)
     [,1] [,2]
[1.] "Mar" "Ter"
[2.] "Mau" "Car"
```

To select 1+ values from a matrix, we use again squared brackets, but this time we use the syntax matrix_name[row_number, col_number]

```
x[1,2] # 1st row, 2nd column
[1] 4
x[2,1] # 2nd row, 1st column
[1] 2
x[1:3,2] # rows 1-3, second column
[1] 4 5 6
x[1,] # 1st row, all columns
[1] 1 4 7 10
x[,2] # 2nd column, all rows
[1] 4 5 6
```

Classes of objects: matrix

```
x # print the matrix x
     [,1] [,2] [,3] [,4]
Γ1.7
                     10
Γ2.1
             5
                      -11
[3.]
        3
             6
                  9
                      12
Join 1+ matrices with cbind() and rbind()
cbind(x,matrix(rep(3,6),nrow=3)) # by column
     [,1] [,2] [,3] [,4] [,5] [,6]
Γ1.7
                      10
Γ2.1
        2
             5
                      11
                            3
                                  3
[3.]
             6
                      12
                            3
rbind(x,matrix(rep(3,4),ncol=4)) # by row
     [.1] [.2] [.3] [.4]
Γ1.7
                     10
Γ2.1
             5
                      11
Γ3.1
             6
                      12
[4,]
        3
             3
                  3
                       3
```

```
Setting row and column names:
```

```
rownames(x) <- c("a", "b", "c") # row names
colnames(x) <- 1:4 # column names
х
  1234
a 1 4 7 10
b 2 5 8 11
c 3 6 9 12
c(nrow(x), ncol(x)) # No. of rows and cols = dim(x)
Γ17 3 4
t(x) # transpose matrix (inverting rows and cols)
   a b c
     2 3
4 10 11 12
```

data.frame(name_var1 = c(...), name_var2 = c(...), ...)

Data structures: data.frame

A dataframe is a bidimensional structure of vectors that can have different classes (e.g., numeric, character, and factor) that can be created with the function:

```
(x <- data.frame(Num = 1:4,
                Char = c("a","b","c","d"),
                Logi = rep(c(TRUE, FALSE), 2)))
 Num Char Logi
           TRUE
1
2
        b FALSE
3
   3
         c TRUE
        d FALSE
str(x) # structure of the dataframe
'data frame':
                4 obs. of 3 variables:
$ Num : int 1 2 3 4
$ Char: chr "a" "b" "c" "d"
```

\$ Logi: logi TRUE FALSE TRUE FALSE

While str(df_name) returns the structure of a dataframe, summary(df_name) returns a summary for each column.

```
summary(x)
      Num
                    Char
                                      Logi
      :1.00
                Length:4
                                   Mode :logical
Min.
1st Qu.:1.75
                Class : character
                                   FALSE: 2
 Median : 2.50
                Mode :character
                                   TRUE :2
Mean
      :2.50
3rd Qu.:3.25
Max.
       :4.00
```

Data structures: data frame

Manipulating a dataframe is very similar to what we saw for matrices.

```
Selecting values and joining two dataframes:
x[2, 2:3] # 2nd row, 2nd and 3rd column
  Char Logi
     b FALSE
cbind(x,data.frame(new=4:1)) # join by col
  Num Char Logi new
         a TRUE
                   4
2
    2
         b FALSE
3
    3
         c TRUE
         d FALSE
                   1
rbind(x[1:3,],data.frame(Num=10, # join by row
                         Char="z", Logi=FALSE))
  Num Char Logi
         a TRUE
2
    2
         b FALSE
3
    3
         c TRUE
         Z FALSE
   10
```

```
Name and number of rows and columns:
```

```
rownames(x) # default = 1:nrow(x)
[1] "1" "2" "3" "4"
colnames(x)[2] # 2nd column name
[1] "Char"
nrow(x) # no. of rows
Γ17 4
ncol(x) # no. of cols
[1] 3
```

```
Transpose of a dataframe:
```

```
t(x)
              [,2]
                              [,4]
     [,1]
                      [,3]
                       11311
                               11411
Nıım
Char "a"
             "b"
                               "4"
Logi "TRUE" "FALSE" "TRUE" "FALSE"
```

Data structures: dataframe



To select a column (vector) from a dataframe, we can use the \$ symbol with the syntax df_name\$column_name:

```
x$Char # selecting the Char column
[1] "a" "b" "c" "d"
x$Char[2] # second value from the Char column
Г17 "ъ"
x$Char[2] == x[2,2] # equivalent commands
[1] TRUE
x$Char <- NULL # removing the Char column
x[x$Num < 3,] # selecting cases with Num < 3
  Num Logi
    1 TRUE
    2 FALSE
# same result with subset(x, Num < 3)
```

```
Alternative way to select the columns:
```

```
x[,"Logi"] # write col names within ""

[1] TRUE FALSE TRUE FALSE

x[1:2,c("Num","Logi")]

Num Logi

1 1 TRUE

2 2 FALSE
```

"Head" and "tail" of a dataframe:

```
head(x, n = 2) # first 2 rows

Num Logi

1 1 TRUE

2 2 FALSE

tail(x, 1) # last row

Num Logi

4 4 FALSE
```

Data structures: list

A *list* is a **collection of objects** that can have **different classes** (es. vector, matrix, and data.frame) e **different length** (contrarily to matrices and dataframes). It is the most complex and versatile structure in R, which can be created with the function list(nome oggetto1 = ..., nome oggetto2 = ..., ...)

```
x \leftarrow list(Num = 1:4,
          Matr = matrix(1:12, nrow=3),
          df = x,
          lst = list(1:3,2:3))
str(x) # structure of the list
List of 4
 $ Num : int [1:4] 1 2 3 4
 $ Matr: int [1:3, 1:4] 1 2 3 4 5 6 7 8 9 10 ...
 $ df :'data.frame': 4 obs. of 2 variables:
  ..$ Num : int [1:4] 1 2 3 4
  .. $ Logi: logi [1:4] TRUE FALSE TRUE FALSE
 $ lst :List of 2
  ..$: int [1:3] 1 2 3
  ..$: int [1:2] 2 3
```

To select 1+ objects from a list, we still use squared brakets

```
x[1] # single = create a sub-list
$Num
[1] 1 2 3 4
class(x[1])
[1] "list"
x[[1]] # double = extract the object
[1] 1 2 3 4
class(x[[1]])
[1] "integer"
x[[3]][2,1]
[1] 2
```



There are 5 students (Gina, Pina, Tina, Maria, and Lina), each with a registration number (507, 535, 566, 955, 515) and a score at the exam (19, 27, 28, 25, 25).

Source: Pastore, M. (2021). Master's degree course on "Data analysis in community psychology".

- Create 3 vectors including, respectively, students' name, serial numbers, and exam score
- 2. Join the 3 vectors to create a dataframe
- Delete the 3 original vectors from the workspace (only the dataframe should remain)
- 4. Select and print Maria's grade
- 5. Select the row including all the values belonging to Pina
- Select all students with exam score equal to 25 (you can also use the subset() function - see ?subset)
- Select all students with an exam score higher than 20 () (you can also use the subset())
- 8. Compute the mean and standard deviation of the exam scores

Functions & pakages

Many things in R can be done by using **functions**, which always include the following elements: function name, arguments (arg_name = arg_value or without name, based on the default position), and returned value.

```
sqrt(x = c(1,2,3))
[1] 1.000000 1.414214 1.732051
sqrt(c(1,2,3))
[1] 1.000000 1.414214 1.732051
```

R Help system: To know the details of any function (arguments, value, etc.), just add the ? symbol before the function name

```
?sqrt
```

R packages: To get additional functions than those included in the base R packages, you need to install and open the related package

```
install.packages("pkg_name") # installing a package
library(pkg_name) # open a package
pkg_name::function_name() # using a function without loading the pkg
```

Objects, functions, and workspace

When we assign a value to an object, the latter is recorded in the **workspace**: the place that includes all objects and functions defined by the user (Environment tab in Rstudio).

The ls() function returns the name of any object and function included in the workspace, whereas the rm() function removes the object(s) selected:

```
x \leftarrow 1 # assign value to x
y <- 2 # assign value to y
1s() # show all objects in the workspace
[1] "x" "v"
rm(y) # remove object y
ls()
[1] "x"
```

Combining the two functions, the command rm(list=ls()) empties the workspace, removing all objects and functions (very useful at the beginning of any script!)

```
rm(list = ls()) # remove all objects & functions
```

Some packages are **installed in R by default**, they do not require to be opened, and they are not shown in the workspace.

```
rm(list=ls()) # remove all objects & functions
head(sleep,4) # 'sleep' dataset from the 'datasets' pkg
 extra group ID
1 0.7
           1 1
2 - 1.6 1 2
3 -0.2 1 3
4 -1.2
           1 4
mean(sleep$extra) # 'mean()' function from the 'base' pkg
[1] 1.54
letters[2] # constant values from the 'base' pkg
[1] "b"
1s() # yet the workpace looks empty!
character(0)
```

Objects & functions from outside R: The working directory

To read a file from a specific folder, you should first get (and possibly set) the **working** directory, that is the folder where input files are searched and where output files are saved.

```
getwd() # returns the current working directory
[1] "C:/Users/mengh/OneDrive/Desktop/PHD/Didattica/advancedDataAnalysisPsy"
dir()[1:3] # names of the first 3 files in the WD
[1] "-$img.pptx"
[2] "-$llabus corso ADVANCED DATA ANALYSIS FOR PSYCHOLOGICAL SCIENCE.docx"
[3] "1-course-intro.Rmd"
```

```
setwd("data") # moving WD to the 'data' subfolder
setwd("C:/Users/mengh/OneDrive/Desktop") # set new WD
```

Trick with RStudio: when you start a new project (e.g., data analysis for the thesis, report), create a new R project (.Rproj) from the menu File > New R Project by selecting an existing folder or by creating a new one, which will be the default WD for any file related to that project.

The first step in any data analysis with R is to read a dataset and save it in the workspace. To do so, we need to use a specific function based on the data format (e.g., CSV, xlsx, txt, sav). The default R data format is RData.

```
# file .RData
load(file = "data/studqs.RData") # import
save(qs, file = "data/studqs.RData") # export
```

R can read and export further data formats, some of which require to install additional packages.

```
# file .CSV (comma separated values)
qs <- read.csv(file = "data/studqs.csv") # import
write.csv(x = qs,"data/studqs.csv", row.names = FALSE) # export
# file .SAV (da SPSS)
library(foreign)
qs <- read.spss("data/studqs.sav", to.data.frame=TRUE) # import</pre>
```

Reading & saving a dataset (2/2)

A fast (but poorly reproducible!) way to read a file in R is by using the function file.choose() rather than the name of the file. This allows reading a file without setting the WD.

```
qs <- read.csv(file = file.choose())
```

If you have doubts on the function to be used for reading a file, you can use the Rstudio menu File > Import Dataset

Hands on **Q**:

- Open or create a file .xlsx on your PC, save it in a .csv (comma separated values) format and read it in R
- Now try to directly read the .xlsx file (if you have doubts, just Google "how to read xlsx file with R" (a)
- In both cases, note the class and the structure of the imported object

Hands on **Q**: Course questionnaire

- Download the files studqs.RData and studqs.csv from Github (4-data folder; select File > Raw > Download or right click > Save as) or Moodle ("Data" folder), save the file in a folder and set that folder as the working directory.
- 2. Read both files with R: what are their class? What is the class of the variables included in each of them?
- Use the describe() function from the psych package to compute the descriptive statistics of the variable numVar and use the function hist() to visualize its histogram plot (try changing the argument breaks).
- 4. Use the function table() to create a frequency table of the variable Q02 (i.e., "On which weekday would you prefer to have the lectures?")
- Repeat point #4 but only consider the students that replied "Si" (yes) to the question Q01 (i.e., "Do you plan to attend all lectures?")
- 6. Cross the frequency of the variables Q02 and Q03 (i.e., "Will you participate even if the lectures will be on a different day than the one you prefer?") using table()

Descriptive statistics (univariate)

```
x \leftarrow c(1.1.1.2.8.9) # create numeric vector
                                                       х
                                                       1289
c(mean(x),median(x)) # mean & median
                                                       3 1 1 1
[1] 3.666667 1.500000
as.numeric(which.max(table(x))) # mode
                                                       х
Γ17 1
                                                          1
c(var(x),sd(x)) # variance & standard dev.
[1] 14.266667 3.777124
quantile(x,probs=0.90) # 90° percentile
90%
8.5
                                                       1289
quantile(x,probs=c(0.25,0.50,0.75,1)) # quartiles
                                                       3 4 5 6
 25% 50% 75% 100%
 1.0 1.5 6.5 9.0
round(rank(x)/length(x),2) # sample rank
[1] 0.33 0.33 0.33 0.67 0.83 1.00
```

```
table(x) # absolute frequencies
round(table(x)/length(x),2) # relative freq
0.50 0.17 0.17 0.17
cumsum(x) # cumulative sum
[1] 1 2 3 5 13 22
cumsum(table(x)) # absolute cumulative sums
round(cumsum(table(x)/ # relative cumulative freq
              length(x)),2)
0.50 0.67 0.83 1.00
```

Descriptive statistics (bivariate)

```
y \leftarrow -x - 1 # values inversely proport. to x
z <- round(rnorm(n=length(x)),1) # random values
(df <- data.frame(x,y,z)) # new data frame
  x
           z
1 1 -2 -2.2
2 1 -2 -1.2
3 1 -2 -0.4
4 2 -3 0.4
5 8 -9 -2.2
6 9 -10 0.0
Correlation & covariance
cov(x,y) # covariance btw x & y
[1] -14.26667
cor(x,y) # correlation
Γ17 -1
```

With more than 2 variables

```
x y z
x 14.26666667 -14.26666667 -0.01333333
y -14.26666667 14.26666667 0.01333333
z -0.01333333 0.01333333 1.24266667

cor(df) # correlation matrix
x y z
x 1.000000000 -1.000000000 -0.003166651
y -1.000000000 1.000000000 0.003166651
z -0.003166651 0.003166651 1.000000000
```

Graphics in R: Main functions

High-level functions (stand alone)

```
# basic function (plot depends on object class)
plot() # scatter plot
# distributions
boxplot() # boxplot
qqnorm() # quantile-quantile plot
# frequencies
barplot() # barplot (categorical variables)
hist() # histogram (continuous variables)
pie() # pie chart
# interactions
interaction.plot()
```

Lower-level functions (add ellements to the former)

```
points() # add dots
lines() # add lines
text() # add text
# linear regression line
abline(a = ..., b = ...)
# more complex elements
rect() # add rectangles
polygon() # add polygons
# other graphical featurs
axis() # change the plot axes
legend() # add a legend
```

Graphical parameters

Run the command ?par to see all graphical parameters that can be changed.

Some of them can be set by using the arguments of graphical functions:

```
# dimension
cex = 2 # text & simbol dimension (multiplier)
1wd = 0.5 # line width
# color & shape
col = "red" # (see ?colors)
ltv = 2 # tupe of line (1=solid, 2=dashed, ...)
pch = 19 # shape of dots (see ?points)
# titles
main = "Plot title"
xlab = "x-axis title"
```

Other parameters should be set within the par() function, which should be executed before generating the plot:

```
# margins (bottom,left,top,right)
mai # in inches
mar # in text lines

# multiple panels
mfrow=c(nrow, ncol)
# e.g. two plots next to each other
mfrow=c(2,1)
# es. one above and one below
mfrow=c(1,2)
```

Univariate distributions: Continuous variables

```
X <- rnorm(n=100, mean=0, sd=1) # generating random values from the stand. norm. distr.

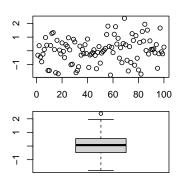
par(mfrow = c(2,2), mai = c(0.3,0.5,0.2,0.5)) # plot 4 graphs in a single window

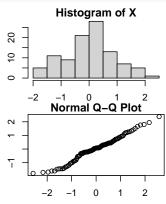
plot(X) # scatter plot (variability)

hist(X) # histogram: frequency distr. by class

boxplot(X) # box plot: (1st & 3rd quartile +/- 1.5 IQR

qqnorm(X) # Q-Q plot: cumulative distribution of X vs. normal cumulative distr.
```





Univariate distributions: Categorical variables

```
Y <- factor(sample(x=c("A","B","C"),size=100,replace=TRUE)) # generating random factor

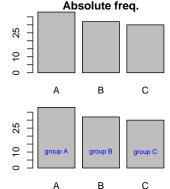
par(mfrow = c(2,2), mai = c(0.3,0.5,0.2,0.5)) # plot 4 graphs in a single window

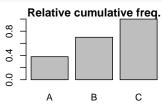
barplot(table(Y), main="Absolute freq.") # bar plot: absolute frequencies

barplot(round(cumsum(table(Y)/length(Y)),2), main="Relative cumulative freq.")

barplot(table(Y)) # same graph but adding blue text

text(x=c(0.7,1.9,3.1),y=10,labels=c("group A","group B","group C"),col="blue",cex=0.7)
```

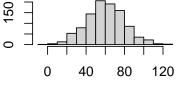


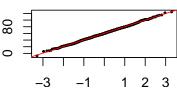


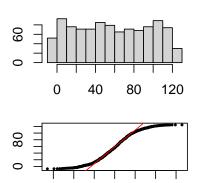
Assessing the normality of a distribution (1/3)

```
X <- rnorm(n = 1000, mean = 60, sd = 20) # norm
par(mfrow=c(2,1),mai=rep(0.3,4),mar=rep(1.8,4))
hist(X,main="",xlab="",ylab="") # histogram
qqnorm(X,cex=0.5,main="",pch=20) # Q-Q plot
qqline(X,col="red") # adding normal line</pre>
```

Y <- runif(n=1000,min=min(X),max=max(X)) # unif
par(mfrow=c(2,1),mai=rep(0.3,4),mar=rep(1.8,4))
hist(Y,main="",xlab="",ylab="") # histogram
qqnorm(Y,cex=0.5,main="",pch=20) # Q-Q plot
qqline(Y,col="red") # adding normal line

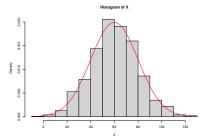




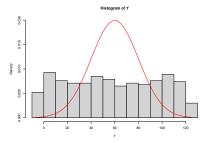


Assessing the normality of a distribution (2/3)

```
# Empirical distribution
hist(X, freq = FALSE)
# Theoretical (expected) distribution
curve(dnorm(x, mean = 60, sd = 20),
    from = min(X), to = max(X),
    col = "red", lwd = 2,
    add = TRUE)
```



```
# Empirical distribution
hist(Y, freq = FALSE, ylim = c(0,0.02))
# Theoretical (expected) distribution
curve(dnorm(x, mean = 60, sd = 20),
    from = min(Y), to = max(Y),
    col = "red", lwd = 2,
    add = TRUE)
```



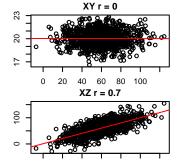
Assessing the normality of a distribution (3/3)

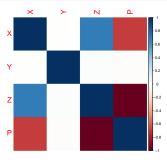
```
# skewness & kurtosis
library(moments) # skewness & kurtosis
c(skewness(X), kurtosis(X)) # (ok if ~ 0)
                                                       c(skewness(Y), kurtosis(Y)) # (ok if ~ 0)
[1] 0.0264805 3.0280811
                                                       [1] 0.02750876 1.76147352
# Kolmogorov-Smirnov test (HO: X is normal)
                                                       # Kolmogorov-Smirnov test (HO: X is normal)
ks.test(X, v="pnorm", mean=mean(X), sd=sd(X))
                                                      ks.test(Y, v="pnorm", mean=mean(Y), sd=sd(Y))
    Asymptotic one-sample Kolmogorov-Smirnov test
                                                           Asymptotic one-sample Kolmogorov-Smirnov test
                                                      data: Y
data: X
                                                      D = 0.069329, p-value = 0.0001337
D = 0.015772, p-value = 0.9647
                                                      alternative hypothesis: two-sided
alternative hypothesis: two-sided
                                                       # Shapiro-Wilk test (HO: X is normal)
# Shapiro-Wilk test (HO: X is normal)
shapiro.test(X)
                                                       shapiro.test(Y)
    Shapiro-Wilk normality test
                                                           Shapiro-Wilk normality test
data: X
                                                      data: Y
W = 0.99911, p-value = 0.9249
                                                      W = 0.95032, p-value < 2.2e-16
```

Bivariate distributions: Continuous variables

```
Y <- rnorm(1000, mean=20, sd=1) # Y (independent from X)
Z <- X + rnorm(1000, sd = 20) # Z (proportional to X)
# Scatter plot
par(mfrow=c(2,1),mai=rep(0.3,4),mar=rep(1.8,4),cex=.5)
plot(X, Y, main = paste("XY r =",round(cor(X, Y),2)))
abline(lm(Y-X),col="red") # linear regression line
plot(X, Z, main = paste("XZ r =",round(cor(X, Z),2)))
abline(lm(Z-X),col="red") # tilde (-) with Alt + 1-2-6
```



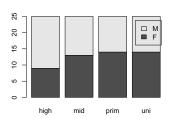




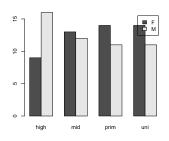
Bivariate distributions: Categorical variables

```
table(df) # crossed frequencies
  edu

sex high mid prim uni
  F 9 13 14 14
  M 16 12 11 11
par(mai=rep(0.4,4))
barplot(table(df),legend.text = TRUE) # bar plot
```

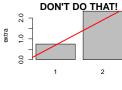


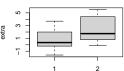


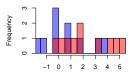


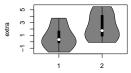
Bivariate distributions: Continuous & categorical

```
par(mfrow = c(2,2), mai = c(0.5,1,0.2,0.5)) # setting graphical parameters
barplot(tapply(sleep$extra, sleep$group, FUN=mean), # barplot for means (DON'T DO THAT!)
        main="DON'T DO THAT!", cex.main=1.5, ylab = "extra"); abline(a=0,b=1,col="red",lwd=2)
hist(sleep[sleep$group==1,"extra"], breaks=10, col = rgb(0,0,1,alpha=0.5),
    xlim = c(min(sleep$extra), max(sleep$extra)), xlab="", main="") # hist by group
hist(sleep[sleep$group==2,"extra"], breaks=10, col = rgb(1,0,0,alpha=0.5), add = TRUE)
boxplot(extra ~ group, data = sleep) # box plot by group
vioplot::vioplot(extra ~ group, data = sleep) # violin plot: density by group
```









Saving a plot

```
# 1. open new file with PNG format
png(filename = "graFico.png", # file name
    width = 350, height = 350) # width & height
# 2. create the plot
plot(sleep$group, sleep$extra,
     xlab = "group", ylab = "extra", col = "#2E9FDF")
# 3. close the file
dev.off() # this will save the plot in your WD
pdf
 2
```

```
Alternative formats (see ?png)

png() # Portable Network Graphics

bpm() # bitmap

jpeg() # Joint Photographic Experts Group

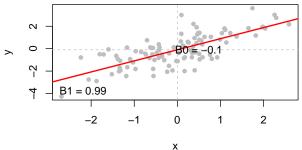
tiff() # Tagged Image File Format
```

Hands on **Q**

- Download and read the file studgs.RData (it's the same dataset used in the previous exercise)
- 2. Generate the histogram of the variable numVar separately for those that replied "Si" (yes) to question Q01 ("Do you plan to attend all lectures?") and those that replied "Non a tutti" (not all lectures); add a vertical red line corresponding to the mean value of numVar for the two groups
- 3. Generate a normal QQ plot of the variable numVar. Is it normally distributed?
- 4. Generate the box plot of the variable numVar by the variable Q01: which group has the highest median? Which has the hugest variability?
- Create a new variable numVar2 corresponding to numVar2 2 * rnorm(nrow(qs), sd = 20)
- Generate the scatter plot of numVar2 vs numVar, add the regression line with the abline()function, and compute the correlation coefficient between the two variables

Linear regression

- Regression allows to determinate the asymmetrical and functional relation between two variables, to quantify whether one variable (predictor) predicts another variable (dependent or response)
- Linear regression determines the link between two variables through a linear function: $y_i = \beta_0 + \beta_1 x_i + \epsilon_i$
- Such a function can be graphically represented as a **straight line**, where β_0 is the **intercept** (value assumed by y when x = 0) and β_1 is the **slope** (predicted change in y when x increases by 1 unit)



Using the dataset gambling from the ADati pkg. We want to fit models that predict frequency of gamig behavior based on gender and risk (risk perception).

```
data(gambling,package = "ADati")
```

R uses the lm() function with the arguments formula (syntax: dependent - pred1 + pred2 + ..., where the symbol "~" is the tilde, on Windows: Alt + 126) and data (dataframe that includes the variables in the formula)

 Null model: frequency scores are only predicted by the intercept β₀, that is the mean value of frequency in the sample.

```
m0 <- lm(formula = frequency ~ 1, data = gambling)

coefficients(m0) # coefficient estimates (intercept)

(Intercept)

10.55997

mean(gambling%frequency) # mean of the frequency variable

[1] 10.55997
```

m1 <- lm(formula = frequency ~ gender, data = gambling)

Fitting a linear regression model (2/3)

Simple linear regression model: frequency is predicted by the intercept β₀ (expected value of frequency when gender is "f") and the slope coefficient β₁, expressing the 'mean' difference m - f.

Multiple linear regression model: frequency is predicted by the intercept β₀
(expected frequency when gender = f and risk = 0) and the coefficients β₁ ('mean' gender difference when risk = 0) and β₂ (effect of risk net to gender differences)

```
m2 <- lm(formula = frequency - risk + gender, data = gambling)

coefficients(m2)

(Intercept) risk genderm

18.951650 -1.393899 2.008555
```

Interactive model: frequency is predicted by the intercept β₀ and the coefficients β₁
 ('media' gender difference when risk = 0) and β₂ (effect of risk when gender = "f")
 and β₃ (effect of risk when gender = "m")

```
m3 <- lm(formula = frequency ~ risk * gender, data = gambling)

coefficients(m3)

(Intercept) risk genderm risk:genderm

16.9206907 -1.0994674 5.9744077 -0.6087177
```

Assessing linear model assumptions (1/3)

- 1. Independence of observations: all pairs of errors ϵ_i and ϵ_i are independent for any $i \neq j$. This assumption does not require particular procedures, just think: are my observations independent?
- 2. Idependence of predictors and errors: residuals (estimates of the error component ϵ_i) should not be associated with the predictors gender and risk.

But what are residuals?

```
gambling$RESIDUALS <- residuals(m3) # model residuals with residuals()
gambling$PREDICTED <- fitted(m3) # predicted values with fitted()
head(gambling[.c("frequency", "PREDICTED", "RESIDUALS")],5) # RESIDUALS = OBSERVED - PREDICTED
   frequency PREDICTED RESIDUALS
        4.78 7.553228 -2.7732283
6
       36.98 9.605418 27.3745820
8
        4.78 7.553228 -2.7732283
10
18
       11.16 11.335396 -0.1753962
        5.62 7.828095 -2.2080952
19
```

Assessing linear model assumptions (2/3)

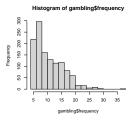
- 2. Idependence of predictors and errors: residuals (estimates of the error component ϵ_i) should not be associated with the predictors gender and risk. Here, we do not see substantal gender differences or a substantial relationship with risk.
- 3. Constant variance (Homogeneity of variances): residual variance is constant for any value of X. Here, we see that residual variance is slightly (but not substantially) higher in males than in females.

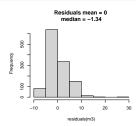
```
par(mfrow=c(1,2), mar=c(5,4,0,2)+0.1)
plot(RESIDUALS ~ gender, data=gambling)
plot(RESIDUALS ~ risk, data=gambling, col="gray")
abline(lm(RESIDUALS ~ risk, data=gambling))
     20
                                                        2
RESIDUALS
                                                  RESIDUALS
     10
                                                        9
     0
                                                        0
     10
                                   m
                                                              2
                                                                                           8
                        gender
                                                                            risk
```

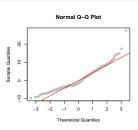
Assessing linear model assumptions (3/3)

- 4. Linearity: the expected value of residuals for a given X value is zero. Practically, residuals should have mean zero (as in this case).
- 5. Normality: residuals should be normally distributed.

Here, the fit is not very nice but we can accept it...







Comparing multiple models

Likelihood ratio test: testing the ratio of the loglikelihood (probability of data functional to the parameter estimates)

library(lmtest)

```
lrtest(m0,m1,m2,m3)
Likelihood ratio test
Model 1: frequency ~ 1
Model 2: frequency ~ gender
Model 3: frequency ~ risk + gender
Model 4: frequency ~ risk * gender
  #Df LogLik Df Chisa Pr(>Chisa)
    2 -3687.3
2
    3 -3629.4 1 115.843 < 2.2e-16 ***
    4 -3480.6 1 297.484 < 2.2e-16 ***
3
    5 -3472.6 1 16.149 5.853e-05 ***
```

Information criteria: penalizing models based on specific criteria (e.g., low likelihood and parsimony)

```
# Akaike information criterion (AIC)
AIC(m0,m1,m2,m3)$AIC # the lower the better
[1] 7378.599 7264.756 6969.272 6955.122

# Akaike weights: from 0 (-) to 1 (+)
library(MuMIn)
Weights(AIC(m0,m1,m2,m3)) # Aw
model weights
[1] 0.000 0.000 0.001 0.999
```

Inference on regression coefficients

Based on the NHST approach, we can test the statistical significance of the regression coefficients. In R, such tests are conducted by default when we fit the model.

```
summary(m3) coefficients # command summary() shows the model summary

Estimate Std. Error t value Pr(>|t|)

(Intercept) 16.9206907 0.7416563 22.814733 3.337032e-96

risk -1.0994674 0.1051711 -10.454087 1.484438e-24

genderm 5.9744077 1.0163116 5.878519 5.339754e-09

risk:genderm -0.6087177 0.1512209 -4.025355 6.040343e-05
```

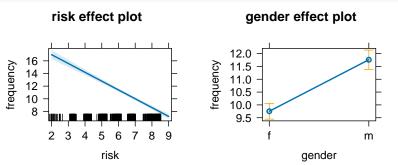
Determination coefficient R^2 :

```
# the model explains the 29% of the variance in frequency
summary(m3)$r.squared
[1] 0.2965382
```

Visualizing the cofficient estimates

To visualize the estimated "effects" (regression line + 95% confidence intervals), we can use the effects package.

```
library(effects)
plot(allEffects(m2))
```



Credits

The present slides are partially based on:

- Pastore, M. (2015). Analisi dei dati in psicologia (e applicazioni in R). Il Mulino.
- $\bullet\,$ Zandonella, C., Gambarota, F. (2021). Introduction to R (in Italian). Corso per imparare le basi di R

Other resources/books introducing R

- R Core Team. The R Manuals. Manuals in pdf format: https://cran.r-project.org/manuals.html (particularly: "An Introduction to R (with many examples)"; "R Data Import/Export")
- UniGlasgow PsyTheacR. Interactive and free course on data analysis with R: https://psyteachr.github.io/
- Dalgaard, P. (2008). Introductory statistics with R. New York: Springer.
- Murrell (2011) R Graphics (II edition). New York: Chapman and Hall/CRC. Examples with code from the website:

https://www.stat.auckland.ac.nz/~paul/RGraphics/rgraphics.html