Design and analysis of a K.E.R.S. system for sports car

Vehicle System Dynamics Project

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June 29, 2020

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1 Introduction

The dependence of the transportation sector on non-renewable sources of energy as fossil fuels and the need for a rapid response to the global warming challenge has in the last two decades encouraged a strong effort for the development of fuel efficient vehicle propulsion systems. In this context, a particular attention has been devoted to the concept of regenerative breaking. A regenerative brake is a mechanism that reduces the vehicle speed by converting some of its kinetic energy into some other kind of useful forms of energy, such as mechanical, electrical or hydraulic energy [1]. The core devices of regenerative brakes are therefore reversible energy conversion components like electric motors/generators and hydraulic pumps/motors. For example, an electric regenerative brake makes use of an electric motor that acts as a generator. This device, which is usually made integral with the vehicle wheel trough a gear train, is indeed able to generate electrical energy thanks to the inputted kinetic energy that is associated to the vehicle at the end of any acceleration phase. A type of regenerative braking is called KERS, KERS, which stands for Kinetic Energy Recovery System, is an automotive system for recovering a moving vehicle's kinetic energy under braking. The recovered energy is stored in a reservoir, as for example a flywheel, a battery or a super capacitor, for later use under acceleration [2]. Embedding such a system in a vehicle allows several potential advantages. First of all, KERS systems may be included in the class of energy harvesting devices [3], which are likely to have a consistent impact in the scenario of green technologies and environment-friendly solutions. In fact, the partial regeneration of the energy that is usually dissipated by the service brake in conventional systems may allow impactful fuel economy strategies, thus reducing the fossil fuel demand and the consequent green-house gases (CO2) emissions. Another important advantage that such a system introduces is the reduced service brake wear. In fact, since during regenerative brakes an electric/hydraulic motor is used to slow down the vehicle in place of the conventional disk brake, this component will as well benefit from a longer lifetime.

2 Implementation alternatives

In this section, we give a description and a comparison of the principle KERS systems that have been proposed in the literature and on the market.

2.1 Mechanical KERS

2.1.1 Architecture and working principle

The Flywheel Hybrid System (FHS) is a type of KERS which consists of a rotating mass, or flywheel, as the energy storage device, a continuous variable transmission system (CVT) to control and transfer the energy to and from the driveline and a clutch which connects this system to the primary shaft of the transmission (Fig. 1).

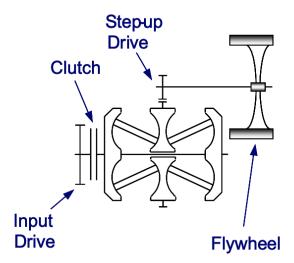


Figure 1: Schematic of Flywheel Hybrid System

When the brakes are applied or the vehicle decelerates, the clutch connecting the flywheel system to the driveline/transmission is engaged, causing energy to be transferred to the flywheel via the CVT.

The use of the CVT guarantees a smooth transfer of energy thanks to the fact that it has an infinite number of gear ratios between the maximum and minimum value of the speed. The Toroidal CVT must continuously adjust the ratio between the speed of the vehicle and the rotation of the flywheel. Any change in the CVT ratio can be viewed as the transfer of kinetic energy between the flywheel inertia and vehicle.

The flywheel stores this energy as rotational energy and can rotate up to a maximum speed of 60000 [rpm]. When the vehicle stops, or the flywheel reaches its maximum speed, the clutch disengages the flywheel unit from the transmission allowing the flywheel to rotate independently. Whenever this stored energy is required, the clutch is engaged and the flywheel transmits this energy back to the wheels, via the CVT. To optimise efficiency, the flywheel runs in a high vacuum and is enclosed within a housing that provides containment in the event of failure. The major function of the vacuum chamber is to minimize the air resistance as the flywheel rotates. Without the vacuum chamber, the friction caused by air resistance is enough to cause significant energy losses and heat the carbon fibre rim to its glass transition temperature. In Fig. 2 we can see the design of a flywheel.

Another important part of the system are the bearings on which the flywheel is mounted. Magnetic bearings have replaced mechanical bearings as they greatly reduce losses due to friction. Further magnetic bearings are able to operate in vacuum which leads to even better efficiency. The magnetic bearings support the flywheel by the principle of magnetic levitation. It is important that the bearings are able to operate inside a vacuum because the flywheel in a flywheel-based KERS must rotate at high speeds for maximum efficiency. The best performing bearing is the high-temperature super-conducting (HTS) magnetic bearing.

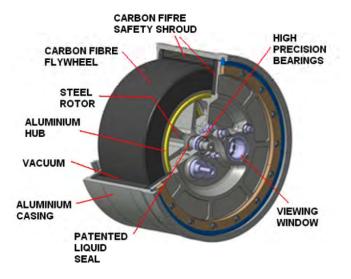


Figure 2: Section of the flywheel

We have also the presence of a step—up gearing system consisting of epicyclic gears is connected between the CVT and the flywheel unit. This system is used to reduce the speed of the flywheel to a manageable one outside the vacuum chamber, in order to have a smooth transfer of energy to the CVT.

The clutch instead is used to couple the flywheel hybrid system to the transmission. It engages the system while the flywheel is accelerating from rest and disengaging while the flywheel is rotating and the vehicle is at rest. Torque is transferred through clutch between the flywheel and vehicle. Hence, the power transmitted in the flywheel system can be controlled by a clutch that could continuously manipulate the torque.

2.1.2 Advantages, disadvantages and fields of application

The advantages include high efficiency, low fuel consumption, and low cost compared to electric hybrids. Although the system has a few drawbacks, most of it can be outweighed by the benefits. One main advantage of this KERS system is its weight. Due to the lightweight design of the flywheel and accompanying components, the additional weight is insignificant when analysing fuel efficiency. Moreover, the system is contained in a compact package, making it easy to incorporate into the rear of a vehicle. Another advantage is the ability of the flywheel to store energy efficiently. This is because there is no transformation of energy from one form to another which greatly reduces energy losses in the system. Tests have proven that flywheel-based KERS can recover and store over 70% of the vehicle's energy. Probably the only losses that occur in the system might be due to friction and air resistance to the flywheels rotation. However, the magnetic bearings and vacuum chamber mentioned previously have been developed to minimize these effects. Cars with a flywheel based energy recovery system, though significantly more expensive than cars without this system, have more power and better fuel efficiency. It has been proved that the system could reduce fuel consumption by as much as 20% and give a four-cylinder

engine acceleration like a six-cylinder unit.

The system has low maintenance costs and it reduces break wear.

As with any technology, the flywheel KERS system has its shortcomings as well. The flywheels found in a kinetic energy recovery system can store up to 400 kJ of energy, which means that failure while rotating at 60000 [rpm] could cause immense amounts of damage. The flywheel—based KERS is not designed to be a stand-alone source of power for a vehicle, like batteries are in electric cars. It is designed for temporary energy storage that is to be used frequently and in smaller amounts. Its purpose is to reduce fuel consumption by providing additional power during the acceleration of a vehicle. Periods of acceleration, especially from a stop, are when the efficiency of the vehicle is at its lowest.

2.2 Electric KERS

Electric KERS is a type of KERS which makes use of batteries or/and supercapacitors as storage system. This regenerative brake system can be used both in the case of internal combustion engine, electric vehicle and hybrid vehicle.

2.2.1 Architecture and working principle

There are different implementations in literature of electric KERS (e-KERS) and each architecture is more suitable for particular application. In Fig. 3 e-KERS with supercapacitor as principal and unique storage system is described. The scheme is composed by: the supercapacitor (SC) which is the energy storage part of the system, it is electrically interfaced to the motor-generator unit (MGU) through power converter (PC). MGU is connected to drive shaft.

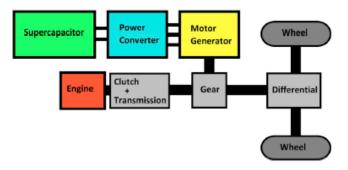


Figure 3: Drivetrain layout with e-KERS

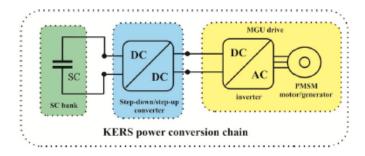


Figure 4: E-kers scheme

There exists also the dual of this implementation which is the one in which there are only batteries used as storage system. These two implementations have several limitations. SC as single energy storage element can be used only when large spaces and weight were allowed (i.e. electric city rail, hybrid city bus). Batteries have high energy density(Liion batteries, that are the most installed batteries on electric vehicle, have specific energy density around 75–200Wh/kg) but low power density. For automotive applications, specifically in hard braking and traction maneuvers, batteries present several weaknesses related to the chemical reactions taking place while charging/discharging. Li-Ion batteries cannot respond to high-dynamic power profiles resulting from an acceleration or a regenerative braking since charge transfer occurs through reduction and oxidation reactions. These profiles, if happened, will overstress the batteries which negatively affect the longevity of their lifespan. It is convenient to implement in the energy storage system, a storage element characterized by its ability to provide the necessary power required by the traction and braking systems. This secondary storage element will substitute the battery during extreme power demand. Among all the existing storage elements, the supercapacitors are potential candidates to meet those requirements. This element has high power density and high cycle life. On the other hand, it presents a low energy density, a high acquisition cost and a high self-discharge. The hybrid energy storage system (HESS) will combine the high energy density storage element (Li-Ion battery), known as primary storage element, and the high power density storage element (supercapacitor). HESS implementation is described in Fig. 5

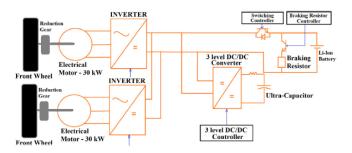


Figure 5: Hybrid e-kers scheme

It is possible to see in Fig. 6 the power flow from wheel to storage system during brake

phase.

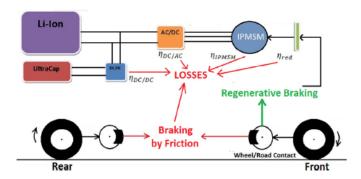


Figure 6: Hybrid e-kers scheme

2.2.2 Advantages, disadvantages and fields of application

It is possible to evaluate and to compare electrical energy storage system by using some performance metrics like the cycle efficiency, the cost per unit capacity (\$\frac{1}{2}kWh or \$\frac{1}{2}kW\), specific energy (Wh/kg), specific power (W/kg), energy density (Wh/l), power density (W/l), cycle life. The battery has shorter cycle life due to unavoidable chemical deterioration. No single type of electrical energy storage element can simultaneously fulfill all the desired characteristics. There will be a need to combine higher energy density insured by the battery, as primary source, with a higher power density energy storage elements, like ultracapacitors or flywheel. This means that the best e-KERS implementation is the hybrid one which makes use of primary and secondary source. The use of supercapacitor as unique storage solution in electric vehicles remains limited since their energy density cannot compete with batteries. It is possible to use only supercapacitors as storage system if a low driving range can be accepted and if there is enough space available to install supercapacitors and when there are no weight constraints as in the case of electric city rail or hybrid city bus, where energy saving of about 40% were obtained. Both HEV and FCHEV usually implement electric KERS, exploiting the main storage system used for the traction in conjunction with supercapacitors, which allow a reduction of batteries intervention during vehicle regenerative braking or startup, thus enhancing batteries life cycle and maintaining their capacity performance. Regenerative braking has been intensively studied and implemented on hybrid electric vehicles (HEV) and fuel cell hybrid electric vehicles (FCHEV) because the presence of powerful electric machines (generator and motor) interfaced to high capacity energy storage as batteries easily allows to convert and store vehicle kinetic energy into electric energy. Stored energy can be employed for vehicle propulsion or for electronic components supply. Stationary flywheels have important dimensions and excessive weight. Onboard flywheels need space in the bogic requiring more space than ultracapacitors. After the diffusion of UCs, the use of flywheels in electrified railways has been reduced because of the superior properties of UCs in terms of maintenance, weight and size [21]. Other authors conclude that flywheel ensures a steady voltage and power level, which is independent of load, temperature and state of charge. In fact the combination battery/flywheel can achieve better performance, regarding voltage fluctuation, than other types of combinations (battery/UC or UC/flywheel), as reported by [46]. Unlike electrified vehicles, internal combustion engine vehicles are not equipped with generator, electric motor and batteries of adequate power and capacity to allow the conversion of the vehicle kinetic energy into electric energy. For this reason, the kinetic energy recovery systems successfully tested for ICEV application are mainly based on mechanical and hydraulic energy storage devices. Unfortunately, the energy recovered through the flywheel cannot be stored for a long time, due to mechanical and fluid dynamics friction on the flywheel.

2.3 Hydraulic KERS: Series Hydraulic Hybrid systems

Series Hydraulic Hybrid Systems(SHH) represent a type of KERS that makes use of hydraulic accumulators as energy storage units. Unlike the older *parallel* implementations, the *series* architecture is characterized by the fact that prime-mover and vehicle speeds are entirely decoupled through a continuously variable hybrid hydraulic transmission. In other words, the conventional mechanical driveline is completely removed.

2.3.1 Architecture and working principle

The system (Fig. 7) is made of four principal components [4] the working fluid (usually oil), the ICE, hydro-pneumatic accumulators and pumps/motors, which are often variable displacement axial piston machines.

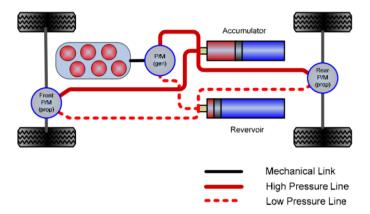


Figure 7: SHH scheme for a 4x4 vehicle

The IC engine is mechanically coupled to the hydraulic pump/motor designated as P/M(gen). The P/M(gen) is used as a motor only when starting the engine. In all the other working conditions, the fluid pumped by P/M(gen) flows towards the P/M(prop-s) and the high pressure accumulator. Traction pumps/motors (P/M(gen)) are connected to the wheels through a differential to provide propulsion. The pump/motor is a reversible energy conversion component. In particular, operating the P/M(gen) in the motor mode

propels the vehicle, while regenerative braking requires switching to the pump mode. During the breaking phase, the hydro-pneumatic accumulator allows energy storage: as the P/M(prop), working as a pump, transfers the hydraulic fluid from the reservoir into the accumulator, the pressure of the gas sealed inside it increases, thus storing energy [5]. In the accumulator (Fig. 8), a bladder is used to separate the working fluid from the pressurized inert gas (e.g. nitrogen), which can be thus treated as a closed system. In a later acceleration event, the energy stored in the high pressure fluid contained in the accumulator is used, together with an amount delivered by the P/M(gen), to provide torque to the wheels. The pressure difference between the accumulator and the reservoir determines the maximum torque available from the hydraulic motor. In this phase, the working fluid is at least partially returned to the reservoir.



Figure 8: Commercial bladder-type hydraulic accumulator

The Reservoir is structurally similar to the accumulator but the gas that it contains is kept at low pressures and serves primarily to assist the transfer of fluid to-and-from the accumulator, with a minimal impact on the overall energy conversion.

2.3.2 Advantages, disadvantages and fields of application

In contrast to its electric counterpart, fluid power technology is characterized by a higher power density and lower energy density [6]. Energy density, which is also known as specific energy, represents the amount of energy that can be stored in a given mass of the system. On the other hand, energy density does not give information on how quickly this energy can be used: this knowledge is contained in the system's power density, which describes the rate at which its energy can be outputted. Moreover, since they release their energy more quickly, higher power density systems can also recharge more quickly. This feature makes hydraulic hybridization particularly interesting for applications with high and fast power transients. In particular, utilization of hydraulic propulsion and energy storage components can offer significant advantages for those heavy vehicles that are required frequent start-stop operations, such as city buses, delivery vehicles and refuse trucks. It's worth

noticing that, in those fields of application, the stored energy is not necessarily limited to aid subsequent acceleration events, but can potentially represent a power source for the activation of ancillary equipment, as for example the compacting and packing mechanisms of refuse trucks. In addition, hydraulic KERS are also likely to have a longer operating life than battery-powered systems. Another remarkable advantage of those systems is their high energy conversion efficiency: the state-of-the art bladder type accumulators with elastomeric foam can reach a round-trip efficiency of about 95%. Once again, the combination of high efficiency and high charging-discharging rates enables particularly effective regeneration and re-use of hydraulic energy in heavy vehicles. The main disadvantage of hydro-pneumatic KERS is represented by their high weight, which is mainly due to the presence of the working fluid and accumulators. This causes the specific energy of those systems to be relatively low. As a result, hydraulic hybrid systems encounter important limitations where consistent levels of power are required for extended periods at near constant speeds, such as in long-distance cruising. Additional costs, which may represent 10–15% of the total for the vehicle, is undoubtedly a further important drawback.

2.4 Hydro-electric KERS

This type of KERS is called also HESS (*hydro electric synergy system*). It is an alternative of the above described pure hydraulic KERS, because of the introduction of a second energy storage system.

2.4.1 Architecture and working principle

The HESS is composed by two main parts:

- 1. **Hydraulic System**. It is the main energy recovery system, characterized by high power density. It includes:
 - Pump or motor (Fig. 9) (depending on the usage phase). During the acceleration phase, it behaves like a motor, providing torque to the shaft, whereas during deceleration it behaves like a pump, storing the fluid from the reservoir into the high–pressure accumulator;



Figure 9: Commercial hydraulic pump

- Accumulator;
- Reservoir.
- 2. **Electric System**. It constitutes the secondary energy recovery system, characterized by a high energy density. It is used only when a high amount of power is requested by the user or when there is a fault on the hydraulic machinery. This allows to maintain the battery around its optimal state of charge (SoC). It includes:
 - Battery. Usually a nickel-metal-hydrid (Ni-MH) one is used. It is linked to the electric motor (EM) through a DC/DC converter;
 - Electric motor. It can be used as a motor or as a generator, depending on the usage phase;
 - DC/DC converter.

A typical realization scheme for the HESS can be seen in Fig. 10.

The overall system is driven by a centralized controller which decides the action to be performed depending on the nature of the torque applied by the human (positive if the vehicle is accelerating). The primary task of the control action, as in all KERS, is to maximize the fuel economy.

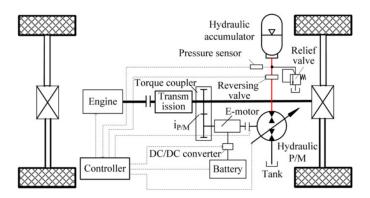


Figure 10: HESS scheme

2.4.2 Advantages, disadvantages and fields of application

HESS results to have better performances in the urban scenario because of the existence of a lot of braking conditions. In fact, in the city, the driver is obliged to stop many times, wasting a lot of thermal energy while slowing down the vehicle. This means that the amount of renewable energies in the city is much higher than, for instance, during a race.

Due to the presence of the hydraulic storage system, it should be used on heavy vehicles like trucks and buses, on which a high power is requested in a short amount of time to accelerate or to decelerate. Simulations and previous works shows that this hybrid system can save about 20% of fuel.

Furthermore, it has overall better performances than a full electric energy recovery system because it weights much lesser and it operates in an optimal region of the Ni–MH battery. On the contrary, a pure electric system with battery and ultra–capacitors tends to deteriorate the battery in a small amount of time, because the SoC continuously changes very rapidly.

Eventually, it must be said that the main con is that this hybrid system is very expensive (it constitutes about 40% of the cost of an entire vehicle). Moreover, it is quite difficult to model from a mathematical point of view due to the nonlinearities needed to represent the fluid and the gas movements in the accumulator chamber.

3 Flybrid's KERS system

The kinetic energy recovery system we make reference to in the present work is inspired by the mechanical KERS device invented by the Flybrid[®][12]. This system includes a high-speed flywheel which is connected, through a proper transmission, to the vehicle powertrain. In particular, two main configurations for the KERS integration are proposed. In the first option, the MKERS is arranged to provide power to the car driving wheels, together with the power amount coming from the conventional main-drive transmission. In this case, the KERS transmission may be connected to the layshaft of a manual gearbox (Fig. 11). This design choice has the advantage of increasing the KERS efficiency thanks to the use of the main drive transmission speed ratios as well, indeed increasing the total number of available speeds which are made available by the KERS transmission alone.

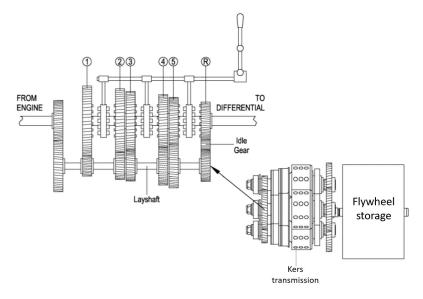


Figure 11: Gearbox connection case

Alternatively, the MKERS may be arranged to provide power to the car non-driving wheels (typically the rear ones). In this configuration (Fig. 12), the KERS transmission output is connected directly to the differential gear of the rear axle. This second configuration

ration offers the advantage of treating the KERS as an optional, namely as a module that is completely separated from the driving wheels (the front ones in the present example) conventional powertrain.

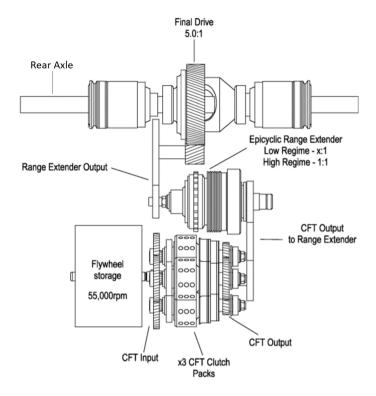


Figure 12: Non-driving wheels connection case

As above illustrated (Fig. 12), the MKERS transmission includes a cascade of two ratio sets connected in series: a clutched flywheel transmission (CFT) and a range extender. The CFT proposed in the invention includes three ratio sets arranged in series, each of which comprise two selectable ratios connected in parallel ("2x2x2" configuration). All ratios of each of the three ratio sets are selectable by friction clutches (Fig. 13). Moreover, all ratio sets include two clutches in such a way to have $2^3 = 8$ possible combinations of KERS ratios.

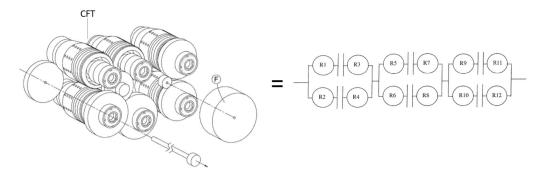


Figure 13: CFT

The CFT output is connected via transfer gears to a range extender (Fig. 12). This

second component provides a second ratio set for increasing the number of MKERS selectable ratios. This second ratio set comprises a plurality of selectable ratios, each in parallel with one another. For example, an epicyclic gear train with two clutches would provide two selectable ratios. A range-extended CFT may offer marked performance enhancements over a non-range extended one in terms of efficiency of energy transfer from the wheels to the flywheel and back. As shown in (Fig. 11), this second component may be excluded from the KERS transmission in the connection layout provided as first option. In fact, the number of available ratios to be exploited in the energy transfer process optimization is in this case already augmented by the ones provided by the conventional vehicle transmission (i.e. the gearbox). An additional clutch may be as well included in the system to disconnect the MKERS from the vehicle powertrain under specific operating conditions. As far as the numerical guidelines are concerned, the flywheel should be designed to have a storage capacity of 210 kJ and top rotational speeds of the order of 55.000 [rpm]. Moreover, the KERS transmission should be provided with a ratio spread (i.e. the maximum achievable ratio divided by the minimum one) of about 11, therefore outperforming the one offered by typical CVTs, which are usually characterized by a ratio spread ranging in the interval 4-7.

4 MKERS model

The hybrid powertrain that has been considered in the present work is shown in fig.14.

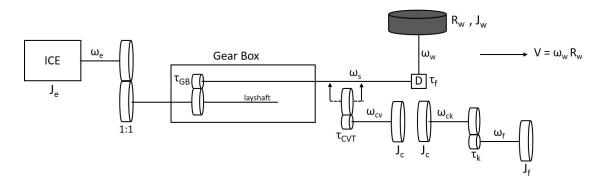


Figure 14: Hybrid powertrain model

With respect to a standard powertrain, the proposed one is characterized by the presence of a high-speed flywheel, which is connected to the main driveline *in parallel* with the prime mover (ICE). In particular, the flywheel powertrain uses a CVT (Torotrak® model) for a smooth and fast charging and discharging of the flywheel and is as well provided with a 2x2x2 CFT device. The connection and disconnection operations of the flywheel from the system main driveline are carried out via a dedicated clutch. The model parameters that have been considered are the ones of a typical 2013 F1 car and are summarized in Tables 1 and 2.

Parameter	Numerical Value
J_e	$0.3 \ [m^2 * Kg]$
J_w	$0.49 \ [m^2 * Kg]$
R_w	$0.33 \ [m]$
J_c	$0.1 \ [m^2 * Kg]$
J_f	$0.026 \ [m^2 * Kg]$
M	770 [Kg]
$ au_f$	1/4.38
$ au_{cvt}$	0.4 - 2.5
$ au_k$	1/12 - 11/12

Table 1: model parameters and variables

Transmission ratio	Numerical Value
$ au_1$	1/3.08
$ au_2$	1/2.18
$ au_3$	1/1.63
$ au_4$	1/1.29
$ au_5$	1/1.03
$ au_6$	1/0.84
$ au_7$	1/0.69

Table 2: Gearbox parameters

In addition, four more simplifying assumptions have been considered. In particular, we assumed to have:

- Infinitely rigid suspensions;
- Lossless transmission (unitary transmission efficiency);
- Pure headway motion (zero slip coefficient);
- Instantaneous CVT ratio variation $(\dot{\tau}_{cvt} = \infty)$.

This last assumption is justified by the fact that the time constants that characterize a typical CVT dynamic behaviour are of the order of $[10^{-1}]s$ [13], whereas the overall energy transfer transient has a duration in the order of $[10^{0}]s$. In this respect, the CVT ratio variation can be considered instantaneous at a first approximation.

4.1 Equivalent model

In order to focus on the KERS clutch engagement process, an equivalent model can be associated to the one of fig. 14. In particular, the aim of this kind of analysis is finding two equivalent inertias that are respectively reduced to the two shafts that are connected to the two different sides of the KERS clutch (Fig. 15). From now on, we will address to these equivalent inertias as $J_{eq,v}$ and $J_{eq,k}$, where v and k stands respectively for vehicle and kers sides. In other words, the target model can be as follows represented:

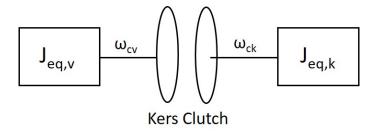


Figure 15: Hybrid powertrain equivalent model

At this purpose, let us first of all consider all the kinematic constraints that characterize the original system:

$$\omega_{ck} = \tau_k \omega_f \tag{1}$$

$$\omega_s = \tau_{cvt}\omega_{cv} \tag{2}$$

$$\omega_w = \tau_f \omega_s \tag{3}$$

$$\omega_s = \tau_{qb}\omega_e \tag{4}$$

These equalities yield

$$\omega_{cv} = \frac{\omega_w}{\tau_f * \tau_{cvt}} \Leftrightarrow \omega_{cv} = \frac{v}{\tau_f * \tau_{cvt} * R_w}$$
 (5)

The overall vehicle kinetic energy can be written as

$$T_{vehicle} = \frac{1}{2}Mv^2 + \frac{1}{2}J_e\omega_e^2 + \frac{1}{2}(4J_w\omega_w^2) + \frac{1}{2}J_c\omega_{cv}^2$$
(6)

$$= \frac{1}{2}M(\tau_f \tau_{cvt} Rw)^2 \omega_{cv}^2 + \frac{1}{2}J_e \left(\frac{\tau_{cvt}}{\tau_{gb}}\right)^2 \omega_{cv}^2 + \frac{1}{2}\left[4J_w \left(\tau_f \tau_{cvt}\right)^2\right] \omega_{cv}^2 + \frac{1}{2}J_c \omega_{cv}^2$$
 (7)

$$= \frac{1}{2} \left[M (\tau_f \tau_{cvt} Rw)^2 + J_e \left(\frac{\tau_{cvt}}{\tau_{gb}} \right)^2 + 4J_w \left(\tau_f \tau_{cvt} \right)^2 + J_c \right] \omega_{cv}^2$$
 (8)

$$\triangleq \frac{1}{2} J_{eq,v} \omega_{cv}^2 \tag{9}$$

The same kind of analysis can be performed on KERS side

$$T_{kers} = \frac{1}{2}J_c\omega_{ck}^2 + \frac{1}{2}J_f\omega_f^2 \tag{10}$$

$$= \frac{1}{2}J_c\omega_{ck}^2 + \frac{1}{2}\frac{J_f}{\tau_k^2}\omega_{ck}^2 \tag{11}$$

$$= \frac{1}{2} \left(J_c + \frac{J_f}{\tau_t^2} \right) \omega_{ck}^2 \tag{12}$$

$$\triangleq \frac{1}{2} J_{eq,k} \omega_{ck}^2 \tag{13}$$

5 Static analysis

The complete energy transfer process consists of two main consecutive phases:

- 1. KERS clutch engagement process
- 2. KERS charge/discharge process

At a first stage of the project, we have focused on the clutch engagement phase only by performing a static analysis of this process. In particular, with reference to the equivalent model derived in section 4.1, it is possible to model the KERS clutch engagement as an inelastic collision between the two rotating bodies $J_{eq,v}$ and $J_{eq,k}$. In this respect, if we denote by ω_c the clutch angular velocity after the collision, then we can apply as follows the angular momentum conservation law:

$$J_{eq,v}\omega_{cv} + J_{eq,k}\omega_{ck} = (J_{eq,v} + J_{eq,k})\omega_c \implies \omega_c = \frac{J_{eq,v}\omega_{cv} + J_{eq,k}\omega_{ck}}{J_{eq,v} + J_{eq,k}}$$
(14)

5.1 KERS discharge

Let's first of all focus on the KERS discharge process, which takes place during a vehicle acceleration event. For the sake of simplicity, suppose that the initial vehicle velocity v_0 is zero (i.e. the vehicle is initially at standstill). The variation of the vehicle kinetic energy due to the clutch engagement can be calculated as

$$\Delta E_{vehicle} = \frac{1}{2}Mv_f^2 - \frac{1}{2}Mv_0^2 \tag{15}$$

$$= \frac{1}{2}M(\tau_f \tau_{cvt} Rw)^2 \omega_c^2 - \frac{1}{2}Mv_0^2$$
 (16)

$$= \frac{1}{2}M \left(\frac{J_{eq,v}\omega_{cv} + J_{eq,k}\omega_{ck}}{J_{eq,v} + J_{eq,k}}\right)^2 (\tau_f \tau_{cvt} Rw)^2 - \frac{1}{2}Mv_0^2$$
 (17)

Letting $v_0 = 0$, we get

$$\Delta E_{vehicle} = \frac{1}{2} M \left(\frac{J_{eq,k}}{J_{eq,v} + J_{eq,k}} \right)^2 (\tau_f \tau_{cvt} Rw)^2 \omega_{ck}^2$$
 (18)

$$= \frac{T_{0,k}}{J_f} M \left(\frac{J_{eq,k}}{J_{eq,v} + J_{eq,k}} \right)^2 (\tau_f \tau_{cvt} Rw)^2 \tau_k^2$$
 (19)

where

$$T_{0,k} = \frac{1}{2} J_f \omega_{f,0}^2 \tag{20}$$

Under the aforementioned assumptions, the vehicle kinetic energy variation can be therefore simply written as a linear function of the KERS initial kinetic energy. Once the vehicle energy profiles have been computed (Fig.16), the vehicle velocity profiles can be as well derived by exploiting the following equation

$$\Delta v_{vehicle} = v_f = \sqrt{\frac{2\Delta E_{vehicle}}{M}}$$
 (21)

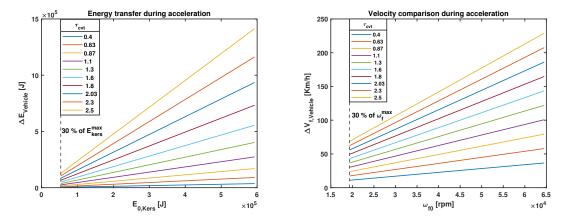


Figure 16: Energy (left) and velocity (right) gained by the vehicle thanks to the kers' clutch engagement

In particular, the above profiles have been calculated by plugging into (19) the values of the KERS initial energy for all the possible initial flywheel angular velocities in the interval $[0.3\omega_f^{max}, \omega_f^{max}]$, where the maximum admissible value for the flywheel angular velocity has been set to $\omega_f^{max} = 64500$ [rpm]. This value is in general upper-limited by the characteristics of the material that the flywheel is made of. In fact, increasing the flywheel velocity beyond the critical stress levels that material can withstand could result in flywheel damage and destruction.

Furthermore, the curves are parameterized with respect to $\tau_{cvt,f}$. In other words, we assumed that, at the beginning of the process, $\tau_{cvt,0} = \tau_{min} = 0.4$ and we also assumed that τ_{cvt} is let free to evolve during the engagement process up to its maximum admissible value $\tau_{cvt,f} = \tau_{max} = 2.5$. In this respect, all the quantities before the collision are

calculated with respect to $\tau_{cvt,0}$ and all the quantities after the collision are parameterized with respect to $\tau_{cvt,f}$.

However, the only really feasible choice is to keep $\tau_{cvt,f} = \tau_{cvt,0} = \tau_{min}$ during the whole engagement transient. In fact, the aim of the clutch engagement process is in this case to dissipate a certain amount of the KERS kinetic energy in such a way to *enter* the CVT admissibility range. In other words, the flywheel speed has to be reduced (and the vehicle one has to be increased) in such a way that

$$\tau_{min} < \tau_{cvt} \left(= \frac{\omega_w}{\omega_f \tau_f \tau_k} \right) < \tau_{max}$$
(22)

Once this condition is met, the clutch can be considered as completely engaged (i.e. the slipping between the clutch disks is zero) and the second phase of the energy transfer process can take place: the τ_{cvt} is now let free to change and opposite angular accelerations of the vehicle wheel and flywheel are established, which allows the mechanical energy transfer between the two components to take place. In other words, the τ_{cvt} parameter plays the role of a feedback control action, whose expression (22) is univocally determined by the systems kinematic constraints, and whose value is saturated between τ_{min} and τ_{max} . The clutch slipping transient allows the system to escape the saturation limits of this component. This operation is fundamental in such a way to allow the energy transfer process to continue also after the clutch full engagement, which is indeed only possible with a time-varying transmission ratio between wheels (sink) and flywheel (source). For these reasons, the only curve of Fig. 16 we should make reference to is the one parametrized in $\tau_{cvt} = 0.4$. This shows that, during the clutch engagement process only, the vehicle can gain an average speed of about 25 [Km/h].

For completeness, the same analysis has been repeated by considering the energy transfer also as a function of each of the eight selectable ratios τ_k of the 2x2x2 CFT. In particular, in Fig. 17 the results obtained for $\omega_{f,0} = \omega_f^{max}$ are reported.

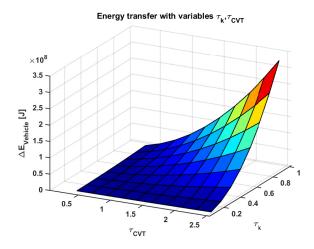


Figure 17: Energy gained by the vehicle thanks to the kers' clutch engagement

This kind of bivariate analysis shows that the most convenient choice for τ_k is in this case $tau_{k,max}$. Note that, differently from τ_{cvt} , τ_k remains fixed during the whole energy transfer process.

5.2 KERS charge

A similar study can be performed in the opposite situation, to which we have been referring as regenerative breaking. Supposing now that $\omega_{f,0} = 0$ [rpm], we get

$$\Delta E_{kers} = \frac{1}{2} J_f \omega_{f,f}^2 \tag{23}$$

$$= \frac{1}{2} J_f \frac{\omega_c^2}{\tau_k^2} \tag{24}$$

$$= \frac{1}{2} J_f \left(\frac{J_{eq,v}}{J_{eq,v} + J_{eq,k}} \right)^2 \frac{\omega_{cv}^2}{\tau_k^2} \tag{25}$$

$$= \frac{T_{0,v}}{M} J_f \left(\frac{J_{eq,v}}{J_{eq,v} + J_{eq,k}}\right)^2 \left(\frac{1}{\tau_f \tau_{cvt} Rw}\right)^2 \frac{1}{\tau_k^2}$$
(26)

where

$$T_{0,v} = \frac{1}{2}Mv_0^2. (27)$$

Once again the KERS speed variation can be calculated as

$$\Delta\omega_{kers} = \omega f, f = \sqrt{\frac{2\Delta E_{kers}}{J_f}}$$
 (28)

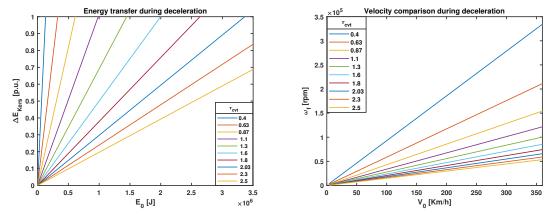


Figure 18: Energy (left) and velocity (right) gained by the kers thanks to the kers' clutch engagement

The energy and velocity curves are this time computed considering all possible initial vehicle speeds in the range [0, 360] [Km/h]. For the same reasons above explained, the clutch engagement process should be this time carried out keeping τ_{cvt} constant at its maximum value $\tau_{cvt,max}$. In fact, the clutch slip will allow in this case to dissipate some

of the initial vehicle kinetic energy until the Torotrak saturation limit (i.e. $\tau_{cvt,max}$) is overcome and the second phase of the energy transfer process can take place.

As a consequence, the curve of Fig. 18 we make reference to is the one parametrized by $\tau_{cvt} = 2.5$. This shows that, during the clutch engagement process only, the kers can be re-charged up to the 70% of its full charge. A similar bivariate analysis to the one provided for the discharge process has been in this case as well performed:

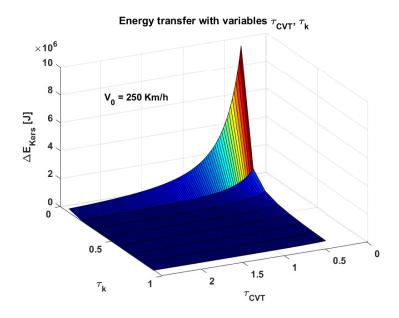


Figure 19: Energy gained by the kers thanks to the kers' clutch engagement

The obtained profiles show that the best-performing choice for the 2x2x2 CFT ratio during the KERS re-charge is $\tau_k = \tau_{k,min}$.

6 Dynamic analysis

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