

Research project report title page

Candidate 1234N

"Hands at the Ready: Bringing Pronto to Kubernetes"

Declaration

I, 1234N, being a candidate for Part III of the Computer Science Tripos, hereby declare that this report and the work described in it are my own work, unaided except as may be specified below, and that the report does not contain material that has already been used to any substantial extent for a comparable purpose. In preparation of this report, I adhered to the Department of Computer Science and Technology AI Policy. I am content for my report to be made available to the students and staff of the University.

Date:

Abstract

Pronto is a federated asynchronous, memory-limited algorithm proposed for online task-scheduling across large-scale networks of hundreds of workers. Each individual node to update their own local model basd on the workload seen so far and generate a rejection signal which reflects the overall node responsiveness and whether it can accept an incoming task. In addition, aggregating the local models builds a global view of the system. Kubernetes is an existing open-source container orchestration system that automates the deployment, scaling and management of containerized applications. It can run production workloads, having becoming the foundation for many cloud computing services like Google Cloud and AWS, while also being portable and extensible with a rapidly growing ecosystem of support and tools.

The standard Kubernetes scheduler uses fixed node and pod information to make scheduling decisions. I propose to apply Pronto to the Kubernetes ecosystem. The aim is to implement an online scheduler that uses online methods to both maximies resource utilisation and minimise per-pod latency while still being competitive with the industry-standard Kubernetes scheduler. During this project I had to modify the mathematics behind Pronto, proposing novel sub-space merging techniques, as well as a new signal function. In addition, I implemented a prototype of the Pronto-based Kubernetes scheduler, comparing it against the standard Kubernetes scheduler. These experiments demonstrate that Pronto is able to achieve a significantly lower pod completion time distribution while remaining competitive (Include values). Thus, Pronto may exceed in situations were pod completion is weighted more than throughput of pods, such as serverless compute.

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Introduction

Task scheduling is the process of organising, prioritising and allocating tasks or activities to resources. Task-scheduling is classifed as a NP-hard problem, thus requiring practical solutions to juggle the quality of scheduling decisions and the computation required to reach those decisions; resources spent determing allocations could instead be spent performing the tasks. This balancing act becomes ever more difficult with online schedulers [1]: schedulers which receive tasks over time, and must schedule the tasks without any knowledge of the future. Without entirely knowing of all tasks to come, the scheduler can't guarantee optimal schedules. As a result, much research has been focused on finding efficient scheduling algorithms that guarantee solutions as close to optimal as possible.

Task scheduling as a problem spans multiple domains and scale: OS-level CPU and IO schedulers (e.g. CFQ and FCFS), workflow orchestrators (Airflow), batch scheduling workloads in datacenters with thousands of machines. This project aims to tackle container orchestration within Kubernetes [2], an extensible open-source platform for managing containerized workloads and services. Originally created by Google, and thus inspired by existing in-house systems [?], it became open-source in 2014.

Kubernetes employs kube-scheduler, an In-Tree (default) scheduler that performs bin-packing, balanced allocation, topology-aware placement and preemption. In addition, kube-scheduler implements the **Scheduling Framework**, providing extension points on top of which Out-of-Tree (replacement) schedulers can extend the scheduler behaviour.

Talk about existing Kubernetes extension. Look at quality of Service plugins and how the current Kubernetes can't support that with bin-packing. Talk about rather than trying to blindly optimise for throughput, consider QoS. Look into how to combine in Serverless Compute / Lambda functions.

- Why Pronto? Pronto is a federated, asynchronous, memory-limited algorithm for online task scheduling across large-scale networks of hundreds of workers - Each node executes scheduling decisions on whether to accept an incoming job independently based on the workload seen thus far. In addition, aggregating local models can contstruct a holistic view of the system

Talk about how there has been few to no signal based kubernetes plugins. Thus, this project aimed to transport Pronto into the domain of Kubernetes.

[Give an overview of the system structure: Central scheduler, remote scheduler and aggregate server]

Talk about modifying the mathematics behind Pronto to get it to work in this domain. Talk about creating the allocation function, the need for a reserve function.

To sum up, this project makes the following contributions:

- Implement a Pronto-based scheduler for Kubernetes
 - Modify the subspace merge operations to take into account a different vector space
 - Introduce signal processing techniques to calculate reserve amount
 - Implement TCP flow-control inspired technique to push throughput while still ensuring QoS
- Demonstrate that this prototype can achieve competitive throughput with substantial reduction in per-pod completion time.

Potentially discuss the drawbacks.

TODO: Check if there are any existing QoS schedulers that do not use predefined constraints. What is a use case in which one does not know exactly how much resources a task will take.

In Chapter 2, we go over existing Kubernetes schedulers and why they do not achieve true online QoS (no prior knowledge of pod resource usage and requirement). In Chapter 3, we explain our proposed system: outlining the mathematics, the system design, allocation algorithm and optimisations. In Chapter 4, we evaluate the performance of Pronto against the standard kube-scheduler, showing how it greatly reduces individual pod completion time. Lastly, we conclude our work and propose potential future directions.

Background

2.1 Online Schedulers

Online Schedulers: This chapter formalises the scheduling problem as well as high-lighting the additional challenges of online scheduling vs offline scheduling. In addition, it will list existing scheduler taxonomies, highlighting their use cases, advantages and disadvantages.

2.2 Kubernetes Overview

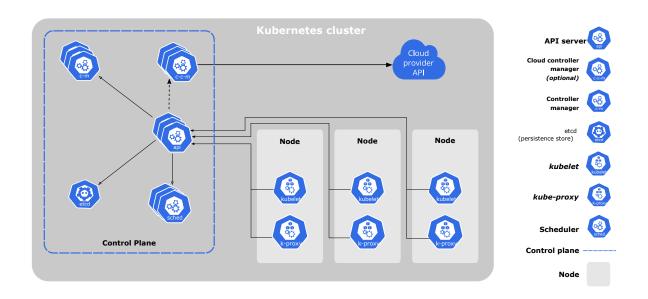


Figure 2.1: The components of a Kubernetes cluster

A Kubernetes cluster consists of a control plane and one or more worker nodes. Components in the control plane manage the overall state of the cluster. The kube-apiserver exposes the Kubernetes HTTP API, which is used to publish objects such as Deployments, DaemonSets and Jobs. The kube-server looks for pods not yet bound to a pod,

and assigns each Pod to a suitable node. Each node in the cluster contains a set of components which maintain the running pods and provide the Kubernetes runtime environment. kubelet manages Pods and ensures they and their containers are running. The kubelet uses a container runtime: software responsible for running containers.

Kubernetes objects are persistent entities in the Kubernetes system. They act as "records of intent" and describe the cluster's desired state: once created, the Kubernetes system will constantly work to esnure that the objects exists. The Kubernetes API is used to create, modify or delete Kubernetes objects. Almost every Kubernetes object includes two fields: spec and status. spec is used on creation as a description of the characteristics you want the resource to have, while status describes the current state of the object, supplied and updated by the Kuberentes system. These fields are crucial for scheduling pods as they behave like resource constraints, with which the Kubernetes schedulers can use to determine optimal pod placement.

2.3 Analysis of Scheduling Approaches and QoS-Aware Trends

Different Kubernetes schedulers take varied approaches to plod placement, from simple heuristics to gloabl optimisations and machine learning. This diversity reflects the wide range of workload requirements and cluster scales seen in practice. In the following subsections, we compare how different schedulers leverage different data inputs for decision-making, which fundamentaly influences their scheduling strategy and resulting quality of service (QoS) for workloads.

2.3.1 Pod Spec-Only Scheduling vs Telemetry-Aware Scheduling

Pod Description-Based schedulers rely soley on the information declared in the pod specification and cluster configuration (static data). The default Kubernetes scheduler [] and similar schedulers like Yunikorn or Volcano [] fall in this category. They consider factors such as requested CPU/memory, labels and selectors, affinity/anti-affinity rules, and priority. This approach is more reliable for ensuring that the declared needs of a pod are met. For example, a pod will only be placed on anode that has enough free capacity according to a resource requests, and it will honor policies like zone spreading or node affinity.

Benefits of this method are predictability and simplicity: by using static reservations, the scheduler guarantees that if every opd accurately requests its needs, no node will be over-committed at scheduling time. This can protect critical workloads by giving them guaranteed resources (as in Kubernetes Guaranteed QoS class). It also enables fairness

policies at high level (e.g. Yunikorn's queues and priorities ensure no team monopolises the cluster).

However, the downside is a lack of visibility into actual runtime conditions - the scheduler is blind to fluctuations in load or hardware state. As a result, static-only scheduling may lead to less optimal placements: for instance, a new pod might be placed on a node that technically has room (per requests) but is currently experience high CPU utilisation from other processes, leading to contention. Meanwhile, an underutilised node could be ignored because its capacity appears full due of over-requested resources or sticky allocations. In summary, purely spec-based scheduling treats the cluster as a static partioning of resources; it ensures each workload's declared needs are met, but it can't respond to real-time perforamance variations.

Telemetry-Based schedulers, incorporate live metrics and feedback from the cluster's current state to make more informed decisions. These schedulers actively monitor CPU usage, memory pressure, I/O rates, cache misses, network latency, etc., either via the Kubernetes Metrics APU, Prometheus, or custom telemetry pipelines. Examples include Intel's Telemetry Aware Scheduling [] (which uses fine-grained platform metrics like LLC cache hit rates and CPU temperature) and the Trimaran plugin suite for Kubernetes [] that uses real-time utilisation stats.

By using this data, telemetry-driven scheduling can avoid placing pods on nodes that are struggling or overloaded in real-time. For instance, a telemetry-aware scheduler might detect that Node A's CPU is 90% busy and Node B's is 20% and therefore prefer Node B for a new pod - even if, by static allocation, both nodes had equall allocable capacity remaining. This dynamic adaptability directly imporves QoS: workloads get more stable performance because they are less likely to be scheduled to an over-taxed machine. Moreover, telemetry-based rules can target specific QoS concerns: Intel's TAS can steer latency-sensitive network functions awway from nodes with high cache thrashing, preventing unpredictable latency spikes []. The benefits of telemetry awareness is higher efficiency and resiliency - clusters can run closer to their true capacity (Trimaran's TargetLoad-Packing can pack workloads until it observes near-saturation) but back off when needed to maintain performance. It also helps in maintaining SLAs by reacting to early warning signals before they become failures.

The challenge, however, is complexity: collecting and reacting to metrics adds overhead and potential instability (the scheduler decisions are now as dynamic as the metrics themselves). Careful design is required to smooth out decisions. telemetry-based scheduling brings an automated, feedback-driven approach that can greatly boost perforamance and utilisation, but it must be tuned to avoid thrashing and to scale metric collection overhead.

Hybrid Approaches combine both static pod descriptions and dynamic telemetry to get the best of both worlds: guarantee the fundamental resource requests/constraints from pod specs while using telemetry to fine-tune the choice among feasible nodes. For example, Firmament (via Poseidon) [] respects each pod's requirements, but when multiple multiple pods are viable it uses a global optimisation incorporating utilisation metrics to choose the optimal placement. Koordinator [] similarly uses class-based static partitioning (dedicating some portion of resources or priorities to LC vs. best-effor pods) and thuen uses live node feedback to adjust placements and even migrate workloads at runtime. By blending static and dynamic data, hybrid scheduling strategies can enforce high-level policies (like fairness, or priority), and ensure those policies aren't undermined by unfore-seen runtinme conditions. The outcome is often superior QoS in multiple dimensions, but come at the cost of the most complexity.

2.3.2 Impact on QoS (Latency, Throughput, Fairness)

The choice of data inputs in scheduling directly impacts various QoS metrics:

Latency and Response Time: Schedulers that can account for real-time load significantly reduce latency for individual requirests. A telemetry-aware scheduler will avoid placing a latency-critical pod onto a node with high CPU or IO wait, thereby ensuring that the pod can get CPU time quickly. In contrast, a purely static scheduler might inadvertently colocate many heavy pods on the same node (if their requests were low but actual usage is high), leading to contention and higher latency for all pods there. Thus telemetry-driven or hybrid schedling is better for meeting low-latency SLAs.

Throughput and Completion Time: For batch workloads, scheduling strategies affects job completion times and overall throughput of the cluster. Volcano's [] gang scheduling ensures all tasks of a parallel job start together so the job can finish as quickly as possible with no stragglers waiting for resources. This improves throughput of a batch workload and avoids resource waste. Similarly, a scheduler using telemetry can balance load by preventing certain nodes from becoming bottlenecks. However, using utilisation metrics does not always guarantee optimal throughput. For example, when 5 pods are running on a node, the node may advertise 100% CPU usage. When running an additional pod, CPU utilisation will remain at 100% but the resulting pod completion times may increase sub-linearly with the number of pods and thus result in higher-throughput. This example highlights how utilisation metrics can be misleading when detecting pod contention.

Fairness and Resource Isolation: Fairness can be considered from multi-tenant perspectives (each user gets a fair share) and from a workload isolation perspective (no noisy neighbor dominates a node to the detriment of others). Pod spec schedulers address the former via quotas, priority classes, etc., and the latter only indirectly (e,g, by requiring all pods to declare resources, which if done correctly prevents one pod from consuming what another needs). Telemetry-based approaches tackle isolation by detecting noisy-neighbour effects - for instance, Koordinator monitors interference metrics and will separate batch

Figure 2.2: % CPU Utilisation and mean pod completion time against number of pods concurrently running on a node

jobs from latency-senesitive ones if the interference crosses a threshold.

Resource Utilisation: Spec-only scheduling often reulies on over-requesting (adding safety margins to resource requests) which can leave nodes underused. Therefore, these schedulers might not be able to completely use all of a node's capacity because they can't safely pack workloads beyond the declared requirest. If a user under-requests, it can lead to CPU throttling and OOM kills and degrade application QoS. On the other hand, telemetry-aware scheduler can confidently increase utilisation up to a safe limits for example, Trimaran's TargetLoadPacking will keep filling a node until it observes the node is about to hit a predefined utilisation limit.

TODO: Should I include example workloads where incorrectly specifying requests can result in sub-par performance?

2.3.3 Summary of Related Work

The earlier survey compared how existing Kubernetes schedulers used two difference classes of input data - static pod information and telemetry - to guide their scheduling decisions. Pod description-based scheduling ensures that fundamental resource guarantees are respected. Telemetry-based scheduling can more precisely allocate pods to nodes at the cost of increased complexity. Hybrid schedulers combine these methods to provide guarantees of fundamental resource requests while fine tuning scheduling decisions. However, their reliance on predefined pod requirements still limits the QoS they can achieve. Without careful consideration and engineering, erroneous pod resource requests can result in under-utilisation or high resource contention.

2.3.4 Shortcomings of Common Telemetrics

Many telemetry-aware Kubernetes schedulers [] use utilisation statistics, such as % CPU used, % memory used, as these metrics are available in most computer systems and can be efficiently collected. While they are easy to process, high values do not always just overcontention

From figure 2.2, we can see that when running more than 5 pods on a single node, CPU Utilisation reaches 100 %. However, further increasing the pod count results in a sublinear increase in mean pod completion time. This highlights how these metrics struggle to define the true capacity of a node.

Few Kubernetes schedulers use deeper contention indicators (e.g. cache pressure, memory pressure and CPU throttling) [? ?]. I believe that metrics can be used to better inform scheduling decisions compared to the standard utilisation metrics.

Summary of Related Work: In this chapter I will summarise the existing approaches to scheduling within the Kubernetes ecosystem. I will outline strengths and weakness of these systems with respect to reactive QoS. The goal of this chapter is to set up why I chose to apply Pronto to Kubernetes.

2.4 Pronto

Pronto is a federated asynchronous, memory-limited algorithm proposed for online task-scheduling across large-scale networks of hundreds of workers. Each individual node updates a local model based on telemetric data and generates a rejection signal which reflects the overall node responsiveness and whether it can accept an incoming task. In addition, aggregation is performed on the local models to build a global view of the system. Pronto takes the existing CPU Ready metric generated by the VMware vSphere and proposes a novel method that uses it as a task scheduling predictor. I believe the methodology behind Pronto can be used with both utilisation metrics and other existing Linux-based contention indicators.

2.4.1 Overview

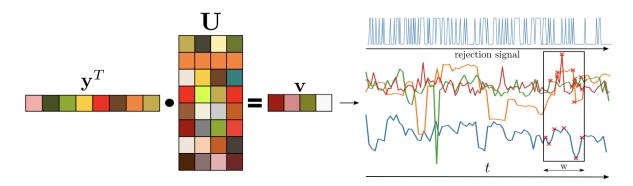


Figure 2.3: Projection of incoming $y \in \mathbb{R}^d$ onto embedding $U \in \mathbb{R}^{d \times r}$ producing R projections in $v \in \mathbb{R}^{1 \times r}$. Projections are tracked over time for detecting spikes which form the basis of the rejection signal. The sliding window for spike detection for each projection is of size w also shown in the figure.

PCA is a powerful dimensionality reduction technique, used to simplify complex, high-dimensional datasets while retaining the most information. Pronto use Federated PCA (a privacy preserving distributed approach to PCA) to extract features which represent the "directions" with greatest variance. Pronto can then project telemetry data onto these vector directions to predict future spikes which indicate resource contention.

Pronto makes use of the following property: The PCA of a matrix can be calculated by mean centering the data, performing SVD on the resulting matrix to give U, the directions of the principle components, and Σ the variance along these directions. As

Pronto aims to be memory-limited, it can't store all of the collected telemetry and must instead take a streaming approach. It periodically measures the CPU Ready metric at a given frequency. To perform FPCA, every new batch of b samples is iteratively merged into the latest subspace using Incremental-SVD. In addition, to perform global model aggregation, SVD is performed on the concatenated bases of two local models. Pronto can further reduce the required computation by using Low-Rank approximations, reducing the dimensionality to r where r < m. It uses the assumption that the first r eignenvalues contain the majority of the information of the dataset.

Once a node has a local model, it can periodically generate a signal by projecting the latest telemetry data onto the principle component subspace U and identifies all the spikes in the projections. If the weighted sum of the spikes exceeds a threshold, then a rejection signal is raised which indicates that node is experiencing performance problems and a job should not be scheduled.

2.4.2 Evaluation

In the Pronto paper, a scheduler's effectiveness was qunatified by its ability to raise a rejection signal that precedes a CPU-Ready spike within a pre-defined window, while minimising the number of false positives that do not precede CPU-Ready spikes. Protono was compared against non-distributed dimensionality-reduction methods [], and was shown to predict CPU-Ready signals effectively while keeping false-positives low. Pronto's better performance over non-distributed strategies implies that there were correlations between job's resource usages on different nodes at the same point in time. As a result, FPCA could use telemetry across multiple nodes to more acurrately compute the principle components and thus give better CPU-Ready predictions.

These properties make Pronto an attractive technique that could be incorporated into scheduling within a Kubernetes cluster.

2.5 Summary

This chapter introduced the core concepts of online scheduling. I explored existing Kubernetes schedulers, investigating the merits of using pod description-based schedulers vs. telemetry-based schedulers. From the brief survey, I identified that few Kubernetes schedulers use deeper contention indicators, such as cache pressure and memory pressure. Finally, I introduce Pronto, a novel approach to task scheduling predictor that uses the CPU-Ready performance metric generated by the VMware vSphere virtualisation platform.

Related work

This chapter covers relevant (and typically, recent) research which you build upon (or improve upon). There are two complementary goals for this chapter:

- 1. to show that you know and understand the state of the art; and
- 2. to put your work in context

Ideally you can tackle both together by providing a critique of related work, and describing what is insufficient (and how you do better!)

The related work chapter should usually come either near the front or near the back of the dissertation. The advantage of the former is that you get to build the argument for why your work is important before presenting your solution(s) in later chapters; the advantage of the latter is that don't have to forward reference to your solution too much. The correct choice will depend on what you're writing up, and your own personal preference.

Design and implementation

Design and Implementation: In this section, I will outline the goals of my system. I will give a brief overview of the chapture structure, summarising each core section and what I achieve.

4.1 Applying Pronto to Containers

Applying Pronto to Containers: In this section I will outline the reasons for why I made modifications to the Pronto system.

4.1.1 CPU-Ready Metric

CPU Ready Metric: I will talk about the problems of using CPU Ready or a CPU-Ready-like metric. Pronto uses CPU Ready which is only available to VMs, and thus not applicable to a Kubernetes clusters where nodes are possibly also physical and virtual machines. Since Linux 4.20+, the kernel can track how long tasks are stalled waiting for the CPU at a cgroup granularity. By inspecting the the root cgroup's CPU pressure file using cat /proc/pressure/cpu you can measure the total time all processes spent waiting for the CPU to be available.

While this type of metric can be used to alert of performance degradation, this metric has a few shortcomings. Firstly, it only reports CPU-centric information. This is not always representative measure of resource contention as memory-heavy workloads may starve for RAM resources while metrics like CPU-Ready and /proc/pressure/cpu remain unaffected.

Secondly, a significant amount of resources are used starting up or deleting containers. This results in large spikes in y (observed data point) which are difficult to distinguish from genuine CPU-Ready spikes and can result in false rejections. This rejection on start-up would reduce the rate at which pods are assigned to nodes and could result in lower throughput.

I decided to adapt Pronto to use fine-grained time-series measurements such as the CPU utilisation, memory consumption to provide real-time performance data of individual nodes as proposed in [3].

4.1.2 Rejection Signal

Rejection Signal: In this section I will discuss the possible drawbacks to using a binary rejection signal. Pronto proposes a means of predicting resource contention but does not include a means for allocating based on the Rejection-Signal.

The Pronto paper assumes a system with no communication latency, which also implicitly includes no pod start-up latency. This simplifies scheduling decisions as the effects of prior decisions are immediately visible in the next signal update (typically 100ms-1s later). However, in Kubernetes, pod start-up can take from 1s-10s. If trying to schedule pods with a high throughput (the Kubernetes scheduler can support a throughput of ≈ 1000 pods per second [4]), this can result in hundreds of pods waiting to start-up on a node while it still advertises an Accept-Signal.

In addition, a binary signal is difficult to use when trying to score nodes and determine the optimal Pod placement. Therefore, I decided to extend Pronto's output to a continous signal in \Re . By allowing nodes to advertise their responsiveness along a finite scale, more fine-grained comparisons can be made between nodes.

4.1.3 Name TBD

Name TBD: In this section I outline a new Pronto-based system. I summarise the core changes: different metrics, new subspace merging, new signal function.

4.1.4 Resource Usage Subspace

Resource Usage Subspace: In this section I outline the new vector space over which indivdual nodes build their local model. I decided to collect CPU utilisation and memory usage as these metrics are easily accessible and are used in a variety of industry-standard schedulers [5, 6]. These metrics give the proportion of a resource currently being used, ranging from [0,1].

Metric Server is a cluster-level add-on that provides near real-time CPU and memory usage metircs for Pods and Nodes. These metrics are easily accessed through the metrics.k8s.io/v1 APIService and are updated by the Metric Server scraper periodically (default every 15s). This method of metric collection is not suitable. Certain Pods may complete in less than 15 seconds and thus may not be detected by the signal. In addition, it would take 15 × batch size seconds between model updates (required to collect a single batch before performing subspace merging), and would result in a less representative and out-of-date model of "current" resource usage.

Instead, I decided to have a pod running on each node, scraping metrics from files within the Linux /proc directory. /proc/stat reports the cumulative count of "jiffies" (typically hundredths of a second) each cpu spent in a specific mode [7]. I can then calculate cpu utilisation using:

$$CPU~Usage\% = 1 - \frac{\Delta (idle + iowait}{\Delta \Sigma all~fields}$$

/proc/meminfo shows a snapshot of memory usage in kilobytes. The percentage of memory used can then be calculated from the provided fields:

$$Memory\ Used\% = 1 - \frac{MemFree + Buffers + Cached}{MemTotal}$$

Due to the higher refresh rate, we can poll these files more frequently (≈ 10 Hz), and can remove the network latency that would come from making calls to the Metric Server APIService.

4.1.5 Subspace Merge

Resource Usage Subspace: In this section I outline the new subspace merge operations. These metrics give the proportion of a resource currently being used, and thus the original Pronto subspace operations have different meanings. Performing the original mean-centering as part of FPCA would result in the following matrices:

- U defines the principle components of the variance within the collected telemetry performance data.
- ullet Σ represents the variance along those principle components.

While this could be used to detect spikes in resource usage, positive spikes do not translate to possible resource-contetion. TODO: Include a diagram of how this signal would falsely predict contention when spiking from 30% to 70% usage but falsely predict no contention when a resource is at 100% usage.

Instead we can perform Incremental-SVD directly on the raw [0,1] metrics. This results in the following matrices:

- U The principle components of the resource usage experienced by the node.
- ullet Σ The sum of the projected distances of all the samples measured in the directions given by U

TODO: Include proofs in the appendices The column eigenvectors of U and the eigenvalues of Σ predict the resource usage characteristics of the pods running on a node. This was achieved without prior knowledge of pod resource usage.

As we are no longer mean-normalising the matrices before performing SVD, the resulting Σ grows with every iterative-SVD. TODO: Include proof in the appendices. TODO: Give example of Sigma exploding To overcome this issues, scale both input matrices by $1/\sqrt{2}$. The resulting matrix from this Subspace Merge behaves similar to an EMA with a forgetting factor of 0.5.

TODO: Investigate whether the modified aggregation function is correct.

4.1.6 Pronto Signal

Pronto Signal: In this section I outline the new Signal function:

$$y_{expected} = y + k \sum_{i} \frac{\sigma_{i} u_{i}}{Tr(\Sigma)} max_{k}. \forall i : y_{expected} < 1$$

Explain how the weighted sum of the eigenvectors gives the expected increase in resource usage. As the signal has no concept of the total number of pods, k instead gives a measurement of the available capacity that a node predicts a future pods could use. TODO: Include a diagram or example showing how given a high usage in CPU, if a model predicts pods are memory centric then it will still give a high signal value.

4.1.7 Denoising Signal

Denoising Signal: In this section, I introduce the problem that comes with measure resource usage directly. TODO: Include a diagram showing Container Events and how the signal fluctuates due to higher CPU usage. In addition, include the dampened signal Mention how this noise could slow down scheduling decisions, cause phantom spikes in the signal after which the resource usage dropped once pods were running. Point out how we want to measure the resource usage of pods and not the container environment which lasts less than a second. In addition, mention how this would have made it difficult later on to determine the impact of a pod on a signal and thus its reserve amount.

Explain how I used a Dynamic EMA filter. The filter starts of with a slow exponential (≈ 0.01), but after more than 4 high samples it switches to a faster exponential (≈ 0.25). This number of samples was decided from an investigation into Container Events (resource usage spikes from container creation or deleting typically lasted less than 100ms).

TODO: Could do a more thorough investigation with a table containing event time distribution

Explain that applying the filter to the direct collected metrics, rather than the signal was better to reduce the noise being introduced into a node's local model.

4.2 System Design

4.2.1 Overview

Overview: In this section, I give a brief overview of the Pronto system. I outline the individual remote schedulers which reside on each node and collect resource usage metrics and generate the acceptance signal.

In addition, outline the Aggregation Service, with a central server and the remote schedulers which act as clients. The remote schedulers send their latest local model and the aggregate server responds with the latest aggregate model. To reduce latency, the aggregate model services each aggregation request by first enqueuing the local model to be aggregated and immediately sending a response with the latest version of the global model. This system trades consistency for latency, which is important when scaling to hundreds of nodes.

TODO: Investigate the latency of throughput/limit of the aggregation server.

Finally, give a brief overview of the central scheduler. Explain how it is a Framework Scheduler and thus replaces the Filter and Score functions

4.2.2 Framework Scheduler

Framework Scheduler: In this section, I explain design of the central scheduler. I will give the reasons for why I decided to use a Framework Scheduler: use of efficient data structures, extensibility allows me to encode the new Filter and Score behaviour. Briefly explain the Filter, Score and Reserve semantics.

4.2.3 Reserve Function

Framework Scheduler: In this section, I explain how I calculated the reserve quantity. I needed a method to estimate the amount of the signal to reserve when assigning a pod such that following scheduling decisions can see the future impact of the pod without having to wait for the signal to update / wait for the pod to start running. Explain how I used several methods:

- Fixed cost determined before initialisation. Does not adapt to different workloads.
- Kalman Filter to predict the change in signal given the number of pods added.

 Difficult to perform when multiple pods are being added and deleted at a time.

 Hard to extract the actual impact of a pod.
- 2D Kalman Filter to predict the signal based on the underlying equation: signal = capacity + per pod cost × no. of pods. This method was relatively accurate, but would result in oscillations as the learned covariance between capcity and per-pod-cost resulted in fluctuations. In addition, trying to increase reactivity to changes in the signal, resulted in this fluctuations becoming extreme.
- 2 separate 1D Kalman Filters, one predicting the per-pod-cost while the other predicts the capacity. This method worked the best. By separating the variables, I was able to prevent the oscillations in the previous method.

4.2.4 Optimisations

Optimisations: In this section I explain the optimisation I implemented to improve scheduler throughput. I will include a figure of node utilisation when using the standard system, showing how extra capacity remains do to error between the true per-pod-cost and the estimated value.

I also show the relation of pod-completion time to number of pods running on a node, alongside the signal. I will argue there are downsides to using CPU Utilisation. That once a CPU is fully utilised (no "jiffies" are spent in the idle state), the addition of more pods can't increase the CPU Utilisation and thus the signal does not change. In addition, the relation between pod-completion time vs pod count is typically sub-linear and thus encourages packing more pods on a node, even when the signal identifies full resource utilisation.

An optimisation I proposed was to borrow the concept from TCP flow-control. This method uses a moving window of the latest n pod completion times, which it uses to identify trends or potential spikes. The challenge in this situation is that the method needs to be as efficient as possible while also being able to handle pods of different workloads and completion times without prior knowledge of different classes.

I compare the change in the sum of square completion times against a threshold. I use the sum of squares to penalize more an increase in the completion of longer running jobs. This is because a proportional increase in completion time has a worse impact the longer the job runs for. Whenever an incoming entry keeps the sum below the threshold, the overprovision capacity increases, while any completion times that exceed the threshold result in the overprovision capacity to halve. This results in a similar saw-tooth behaviour seen in TCP and allows nodes to accept more pods while keeping.

Evaluation

5.1 CPU-centric workloads

CPU-Centric Metric: In this section, I will compare Pronto against the Kubernetes scheduler when running simple CPU-based pods. I will measure job completion time, resource utilisation and individual pod completion time distribution

5.2 Short and Long Workloads

Short and Long Workloads: In this section, I will compare Pronto against the kubernetes scheduler when running pods of variable run-times.

5.3 Multi-Resource Workloads

Multi-Resource Workloads: Finally, I will compare Pronto against the kubernetes scheduelr when running pods.

5.4 Limitation

Limitations: In this section, I will go over the limitations of the system. I will highlight how certain metrics like CPU-Utilisations don't give any more information once saturated. I will also have to mention how due to the sub-linear pod completion time, the kubernetes scheduler is able to achieve higher job throughput by packing more pods into nodes.

5.5 Summary

Summary: In this section, I will summarise the results of my evaluation section, highlighting key findings and reasoning.

Conclusion and Future Work

- 6.1 Summary
- 6.2 Future Work

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Appendix A

Technical details, proofs, etc.

Appendices are for optional material that is not essential to understanding the work, and that the examiners are not expected to read, but that will be of value to readers interested in additional, in-depth technical detail.

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