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Multi-Resolution seismic Attenuation Tomography

Version 3.0

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MuRAT in Brief

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MuRAT is a Matlab Package for Seismic Attenuation, Scattering and Absorption Tomography using Body and Coda Waves.

Features

What it does: *MuRAT* is a software package for measuring seismic attenuation, scattering, and absorption from passive and active data, and model 3D variations of these parameters in space.

The first MuRAT: *MuRAT1.0* was developed by Luca De Siena during his PhD at the INGV-Osservatorio Vesuviano, Italy, and *published in 2014* while he was research assistant at the Westfälisches Wilhelms Universität, Münster. Three sample papers published using this code are: *De Siena et al. 2017, SR, Prudencio et al. 2020*, and *Sketsiou et al. 2021*;

In 2D: *MuRAT2D* is the result of the activity of the *Volcano Earth Imaging group*. It produces 2D seismic scattering and absorption maps at multiple frequencies and is suited for largely undetermined problems. Three sample papers published using this code are: *De Siena et al. 2017, GRL, Napolitano et al. 2020*, and *Sketsiou et al. 2020*;

In 3D: *MuRAT3D* is the current standard for measuring total attenuation, scattering and absorption - the project started in 2021 and there are still no published papers. This guide describes this code.

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Chapter 1

Introduction

This document describes how to use the Matlab software package MuRAT to perform seismic tomography: however, it does not follow the traditional path of imaging *seismic velocity* with travel times, or *phase/group velocities* using surface-waves. MuRAT is a code for *seismic attenuation tomography*.

To understand the difference consider the following seismogram, produced by a volcanic earthquake:

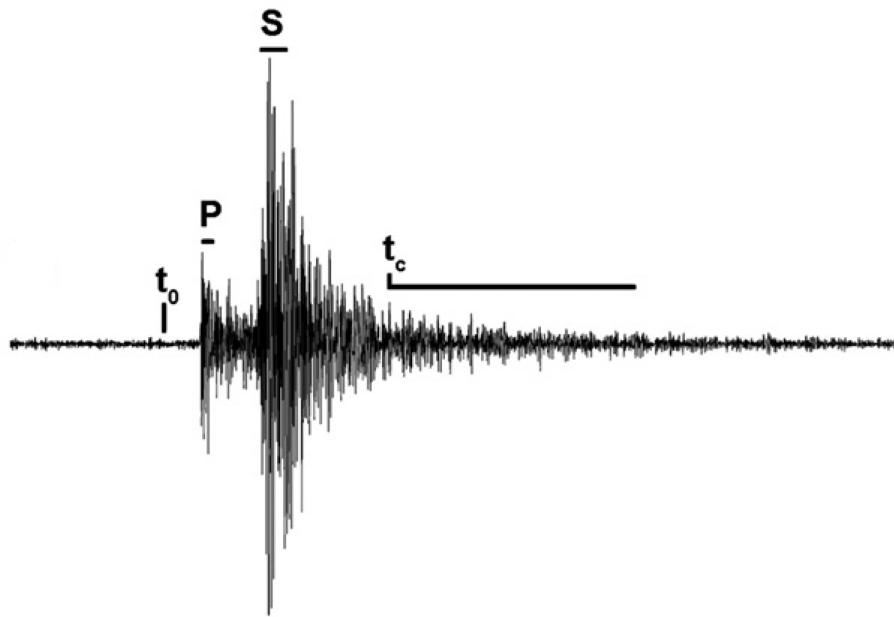


Figure 1.1: A seismogram. MuRAT measures the heterogeneous loss of seismic energy using different seismic attributes

We are used to picking phases on it - for example, the P-wave arrival. By modelling the source-station path followed by the corresponding wave packet with a *ray-tracing* approach, we measure velocity changes over different paths. Travel-time tomography requires a *non-linear inversion*, where we need to update the paths followed by the waves, the corresponding velocity model, and seismic locations jointly to find a reliable solution. There are multiple codes that do this: our favourites are LOTOS

and FMTOMO - just click on their names to go to their internet site. However, MuRAT is part of a wider framework working across multiple languages (Matlab, Python and Julia). This comprises codes that allow the user to measure and image body-wave and surface wave velocity in space (from earthquake and noise) (seispy, interfaced with python) and full waveform inversions (FWI, in Julia). This framework especially couples seismology with outputs from Geodynamics codes efficiently. It is highly recommended to combine MuRAT with the partner codes for a complete imaging of the area under study.

MuRAT deals with the loss of energy suffered by seismic waves while they propagate through the heterogeneous Earth. It fills the gap of an open-access tool to measure attenuation, separate the processes that lead to it, and model them in space. To our knowledge, the first mention of an *attenuation tomography* was given by Ho-Liu et al. (1988) in the Coso Valley. More than 30 years afterwards, this technique is a standard with applications at the global, regional and local scales. Yet, different mechanisms attenuate seismic waves while they propagate. While codes to model total attenuation in space exist, no open-access code can measure attenuation, separate the mechanisms that produce it and model their variations in space with seismic inversion. No code can certainly do it using as input seismograms downloaded from the data servers.

We define here the mechanisms causing seismic attenuation:

1. Seismic energy progressively spreads over larger volumes while propagating far from the source. Energy thus decreases with distance due to *geometric spreading*. This mechanism is independent of frequency for a given phase. However, depending on frequency, often more than one phase are included in a *window of time* measured on a seismogram - in Fig. 1.1 it is challenging to distinguish between S-waves and surface waves produced right after them.
2. Seismic energy is lost into the heterogeneous Earth depending on the ratio between the wavelength (λ) and the dimension of the heterogeneity (a). Energy thus decreases with distance due to *scattering losses*. This mechanism depends on frequency and comprises complex physics, as those described by multi-pathing and diffractions. Reflection and refraction can be described as scattering processes.
3. Seismic energy interacts with the heterogeneous Earth losing heat for each cycle. Energy thus decreases with distance due to *absorption losses* in the materials they pass through. This mechanism depends on frequency. How much energy the Earth absorbs is difficult to quantify, but such a quantification allows connecting seismology with other disciplines.

4. The sum of scattering and absorption losses gives *total attenuation*. This is the attenuation experienced by direct wave-packets while they propagate through the heterogeneous Earth. When we talk about seismic attenuation we generally refer to total attenuation. However, this is only valid in specific circumstances and for specific phases.

MuRAT measures and models total attenuation, scattering attenuation and absorption in space using single seismogram observations. The first three chapters offer an overview of the theory underlying attenuation tomography in these three forms.

In chapter 2, we revise the theory behind measurement and modelling of the energy lost by direct waves (P and S, Fig. 1.1). The method used to model total attenuation in chapter 2 is the *coda normalisation* (CN) method (Aki, 1980; Yoshimoto et al., 1993). In tomography, the method has been introduced by Del Pezzo et al. (2006). At the core of MuRAT, there is this seminal paper, which has been developed by De Siena et al. (2009) and De Siena et al. (2010) for multi-scale applications. De Siena et al. (2010) benchmark the CN with the standard spectral slope (t^*) method, applied by the global community. For a decade, the method has only been applied to volcanoes. The reason is the need for a relevant *coda* (t_c , Fig. 1.1) to normalise direct-wave information. The method has the great advantage of removing source and site effects from direct wave measurements, but suffers from an inexact description of the process. MuRAT uses the standard description of geometric spreading, r^α , with r is the hypocentral distance and α the geometric spreading coefficient, measuring α with its uncertainty. By comparing the results to the assumed value of α for direct wave energies ($\alpha = 1$) the user knows how far this is from the theory. MuRAT3D deals with the problem associated with direct-wave measurements and modelling, using theoretical and computational results obtained throughout the last decade.

In chapter 3, we revise the theory behind the use of *peak delays* as markers of scattering losses (Saito et al., 2002; Takahashi et al., 2007, 2009; Tripathi et al., 2010; Calvet and Margerin, 2013; Calvet et al., 2013; De Siena et al., 2016; Sato, 2016). Peak-delays are a focus of the early-warning community and a quantity important to seismic source modelling in the near field. The standard theory recognises peak delay as a marker of scattering losses in the far field, modelled by the Markov approximation (Saito et al., 2002), in the case scattering is produced only by long wavelength component ($\lambda \ll a$). However, recent research also suggests a dependence of peak-delay on scattering when λ is of the order of propagation distance and correlation length of heterogeneity (Napolitano et al., 2020; Di Martino

et al., 2021). Here, phenomena like diffraction and trapping take over. The chapter discusses the standard application, theoretical limitations and future outlooks.

In chapter 4, we revise the theory behind the use of *late-time coda attenuation* as marker of seismic absorption (Wegler and Lühr, 2001; Prudencio et al., 2013; Calvet and Margerin, 2013; Del Pezzo et al., 2016; De Siena et al., 2016, 2017a; Del Pezzo et al., 2018; Sketsiou et al., 2020). Its application relies on a preliminary Multiple-Lapse-Time-Window-Analysis (MLTWA - Fehler et al. (1988)). Coda attenuation can be described using single and multiple scattering. MuRAT provides the tools to test the onset of equipartition, a necessary condition for diffusion, where coda attenuation is equivalent to seismic absorption. The embedded sensitivity kernels model coda attenuation in space based on Paasschens equations (Paasschens, 1997) and the approximations of Pacheco and Snieder (2005). The theory is inexact in the case of sharp vertical or lateral boundaries, so much so that diffusion could never onset Morozov (2008). However, in zones where the Moho is thick and for sufficient amount of data, the theory generally produces stable results (Sketsiou et al., 2020). New work has been recently developed to include the effect of sharp boundaries and vertical velocity variations on coda attenuation measurements (Sanborn et al., 2017; Cormier and Sanborn, 2019; Nardoni et al., 2021). MuRAT currently provides the tool to invert for coda attenuation using a diffusive approximation and sensitivity kernels.

From chapter 5, this manual describes how to use the code, so you can start from there if you already know the theory.

Chapter 5 describes the installation procedures for MuRAT. MuRAT 3.0 is available on GitHub. We discuss why the code is released in proprietary language and the corresponding installation procedures.

Chapter 6 describes data preparation for MuRAT. MuRAT 3.0 accepts only Seismic Analysis Code (SAC) data. SAC is a standard for seismologists, and the favourite format when converting miniseeds on data servers like IRIS. It is possible you have been processing data with another software. In this chapter, we will discuss the conversions necessary to create a readable dataset for MuRAT and the tools you can use to assess if the data are in the right format.

Chapter 7 describes the input files for MuRAT. We offer three example applications (Mount St. Helens, US - Toba, Indonesia - Vrancea, Romania). In theory, these are the only files the users need to edit, once data files are in the correct format.

Chapter 8 describes the implementation of 3D velocity models, which is optional for MuRAT.

Chapter 9 describes the tests offered by MuRAT to check the reliability of the results.

Chapter 10 describes the regionalisation and inversion procedures.

Chapter 11 describes file outputs and plotting.

Chapter 2

Direct-wave attenuation: Q

Timeline in papers.		
Paper	Descriptor	Where
(Aki and Chouet, 1975)	S-wave CN method	Link
(Yoshimoto et al., 1993)	P-wave CN method	Link
(Del Pezzo et al., 2006)	S-wave CN tomography	Link
(De Siena et al., 2010)	Benchmark with t^* method	Link
(De Siena et al., 2014a)	MuRAT1.0 for CN method published	Link
(De Siena et al., 2014b)	P-wave coda-normalisation tomography	Link
(Prudencio et al., 2015)	Active CN tomography	Link
(De Siena et al., 2017b)	CN tomography measuring Q_c	Link

2.1 Parameters

Input Parameters for MuRAT		
Symbol	Descriptor	Where
t_P or t_S (s)	P-wave or S-wave arrivals	SAC Haeder
t_l (s)	Length of P- or S-wave window	Set in input file
t_0 (s)	Origin time	SAC Haeder
t_c (s)	Lapse time from origin time	Set in input file
t_w (s)	Length of coda window	Set in input file

2.2 The coda normalisation method in pills

The method measures direct and coda-wave energies and divides them to obtain a quantity that only depends on Q , allowing for a linearized inversion.

Pros of measuring direct-wave attenuation using coda-normalised energies

1. Single-station measurements - you can get all the info from a single seismogram.
2. No need for correcting source and site effects - these are particularly relevant in the heterogeneous Earth.

Cons of measuring direct-wave attenuation using coda-normalised energies

1. Uncertain sensitivity of coda waves to Earth structures - the assumption of homogeneous coda wave sensitivity is generally unfulfilled. *Tackled by MuRAT estimating the measurable coda-wave energy at the chosen lapse time and assuming a diffusive behaviour.*
2. Correction of radiation pattern - increasing direct wave windows smooths it at the expense of focusing. *Tackled by working with different windows to measure direct-wave energy.*

Figure 2.1 is a visual representation of the method.

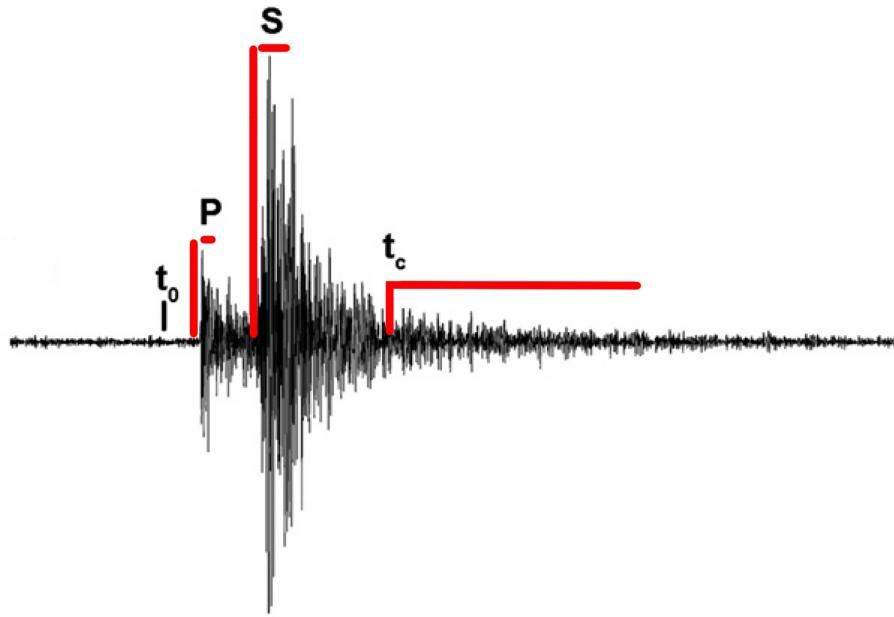


Figure 2.1: The CN method measures the spectral energies of direct and coda waves and inverts for Q. In red the P and S wave energies and the normalizing coda energies.

2.3 The theory bit

The coda-normalisation (CN) method normalises P- and S-wave energy for coda energy (Aki, 1980; Yoshimoto et al., 1993). Seismic wave energies can be modelled as the convolution of the source, path, site, and instrument functions, so that the spectral energy of direct waves (E) is:

$$E(f, r) = R_{\theta\phi} S_S(f) r^{-\gamma} I(f) G(f, \Psi) \exp\left(-\frac{2\pi f}{Q(f)v} r\right) \quad (2.1)$$

where f is the frequency, r is the source-receiver distance, t_c is the coda-wave central lapse time from the origin time of the event (t_0), $R_{\theta\phi}$ is the source radiation pattern (θ and ϕ the azimuth and take-off angle for a source-receiver ray), $S_S(f)$ is the source function, γ the geometrical spreading exponent, $I(f)$ the known instrumental response, $G(f, \Psi)$ is the site amplification factor (with Ψ being the incident angle of the ray at the station), Q is the direct-wave quality factor and v the average velocity in the medium (Yoshimoto et al., 1993).

The spectral energy of coda waves (E_c) can be written as:

$$E_c(f, t_c) = S_S(f)P(f, t_c)G(f)I(f). \quad (2.2)$$

The attenuation of coda waves can then be expressed as (Aki and Chouet, 1975):

$$P(f, t_c) \simeq t_c^{-n} \exp(-2\pi f Q_c^{-1} t_c) \quad (2.3)$$

In this equation, n is the envelope spectral decay, Q_c is the coda quality factor, and $A_c(f, t_c)$ does not include the effect of the source radiation pattern. We will discuss more about this term in chapter 4.

Eq. 2.1 can be divided by Eq. 2.2 to normalize the energy of the spectral energy of direct waves using the spectral energy of coda waves:

$$\frac{E(f, t_c)}{R_{\theta\phi} E_c(f, t_c)} = r^{-\gamma} \frac{G(f, \Psi)}{G(f)} \exp\left(-\frac{2\pi f}{Q(f)v} r\right) \frac{1}{P(f, t_c)} \quad (2.4)$$

where the source function $S_S(f)$ and the instrumental response $I(f)$ contributions disappear. By measuring direct-wave energy over a window of sufficient length (t_l), we smooth the azimuthal contribution of the radiation pattern (De Siena et al., 2009, 2010). If the length of the direct-wave window is chosen appropriately, the contribution of the source radiation pattern $R_{\theta\phi}$ is negligible (De Siena et al., 2009) so that $R_{\theta\phi} = 1$ and $\frac{G(f, \Psi)}{G(f)} = 1$. Since early coda consists of randomly scattered waves, the coherency and the source radiation pattern is eventually lost (Takemura et al., 2009). De Siena et al. (2010) demonstrate that a coda window of 2 s is sufficient to make the radiation pattern quasi-isotropic in a volcanic caldera. Still, the window length must be carefully chosen at each frequency to avoid near-receiver onset of surface waves (Gabrielli et al., 2020).

At fixed frequency band and starting lapse-time for coda windows, $P(f, t_c)$ is assumed to be constant in the standard coda-normalisation method (Del Pezzo et al., 2006; Sato et al., 2012). Taking the

logarithm, Eq. 2.4 becomes:

$$\ln \left[\frac{E(f, t_c)}{E_c(f, t_c)} \right] = -\ln P(f, t_c) - \gamma \ln(r) - \frac{2\pi f}{Q(f)v} r, \quad (2.5)$$

a linear equation solved for three unknown ($\ln P(f, t_c)$, γ , Q) once the hypocentral distance is known and the frequency is set. If Q_c is known for each source station pair, one can pre-estimate $P(f, t_c)$ using equation 2.3, as done by De Siena et al. (2017b):

$$\frac{1}{2\pi f} \ln \left[\frac{E(f, t_c)}{E_c(f, t_c)} \right] + \frac{1}{2\pi f} \ln P(f, t_c) = -\frac{\gamma \ln(r)}{2\pi f} - Q(f)^{-1} t, \quad (2.6)$$

where t is the travel time of the corresponding direct phase. The system can be solved with a linear inversion for γ and $Q(f)^{-1}$. This is the method implemented in MuRAT3.0.

2.3.1 Applicability

For the applicability of the CN method, one must measure direct-wave energy. This seems simple enough, but it can become very problematic depending on frequency, heterogeneity and source-station distance. To check the validity, one must always look at relationship between direct-wave energy and epicentral distance. Is there a dependence? If not, near field or strong scattering might be prevalent. Does the relationship follow standard geometrical spreading, like those for direct wave energy? How important is the surface wave component? A positive is that generally where you cannot measure *direct-wave energy*, you can use codas, i.e., diffusion onsets pretty quickly (see chapter 4).

2.4 MuRAT workflow

MuRAT works in analogy to De Siena et al. (2010), De Siena et al. (2014a) and Sketsiou et al. (2021) when mapping peak delays. These authors show that one must check the relationship between hypocentral distance (or travel time) and measured energy ratio. In Figures 2.2, we show an example at Mount St. Helens volcanoes, where sources and stations can be either on or inside the volcanic edifice and near surroundings (red dots) or far from them (cyan dots). The expected decrease of energy with hypocentral distance is unfulfilled at small distances, where surface and trapped waves dramatically increase coda energy.

The energy in the coda can be back-traced to mark the position and intensity of the corresponding

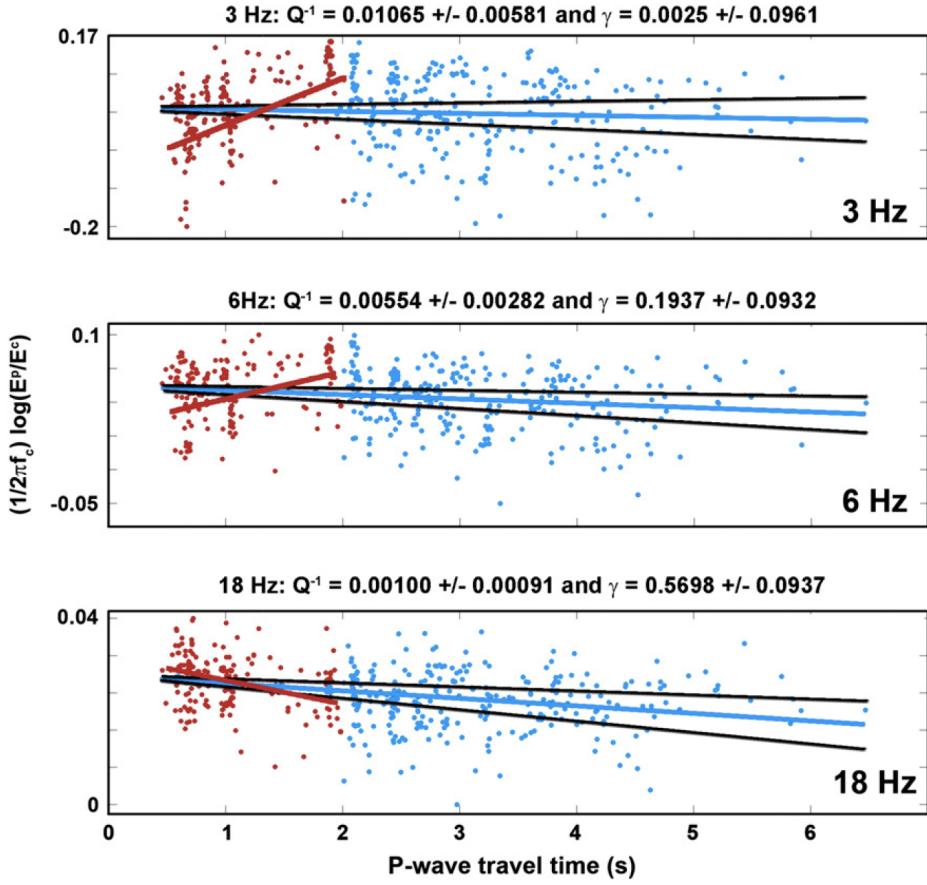


Figure 2.2: A plot of the logarithm of the P-wave direct-to-coda energy ratios (red and cyan dots, computed at MSH in three frequency bands) versus the P-wave travel times at Mount St. Helens volcano. The red lines show the linear fit obtained by using only data between travel times of 0 and 2 s, affected by surface waves inside the volcanic edifice. The cyan lines represent the least squares fit for the entire dataset. The black lines are the maximum uncertainties. The geometrical spreading and the average Q obtained from the inversion are shown above each plot. Notice the progressive change with increasing frequency. From De Siena et al. (2014a).

scatterers (De Siena et al., 2014b), using scattering tomography (also known as Nishigami (1991) technique). The method can still be applied, but fixing the geometrical spreading will trade-off measurements at low frequencies. Sketsiou et al. (2020) discusses the corresponding trade-offs in volcanic, fault and regional settings. In Fig. 2.3 we show the same plot for the normalised S-wave energy at Mount Vesuvius, where all sources and stations are inside the more heterogeneous domain of the

volcanic edifice and feeding system. Here, only data at 18 Hz can be used. Following De Siena et al. (2014a), measurements above (below) the logarithmic linear trend shows high (low) attenuation. This procedure is inverted by this version of MuRAT using a ray bending approach (Block, 1991; De Siena et al., 2010), discussed computationally in Chapter ???.

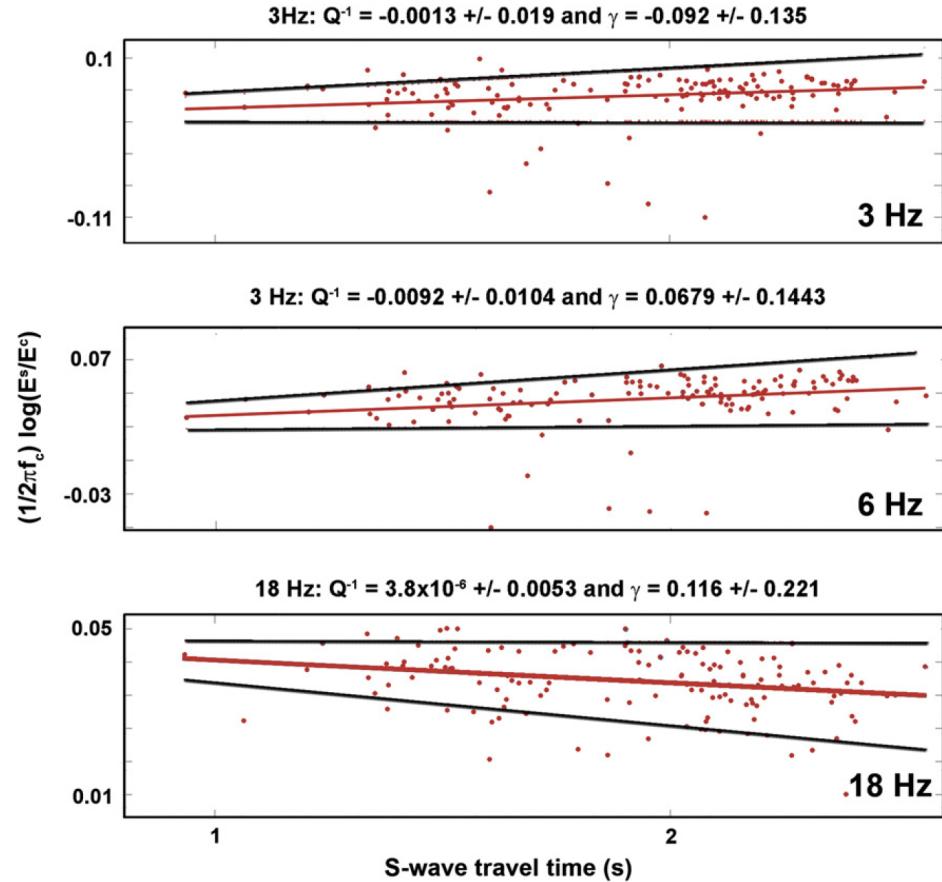


Figure 2.3: Same as Fig. 2.2 for Mount Vesuvius, where earthquakes and stations are all comprised under the volcanic edifice. Notice the negative Q at low frequencies. From De Siena et al. (2014a).

Chapter 3

Scattering attenuation: *peak delays*

Timeline in papers.		
Paper	Descriptor	Where
(Saito et al., 2002)	Markov approximation	Link
(Takahashi et al., 2007)	Peak-delay regionalisation	Link
(Takahashi et al., 2009)	Peak-delay tomography	Link
(Calvet et al., 2013)	Peak delay regionalisation + Qc: crust	Link
(De Siena et al., 2016)	Peak delay + Qc: volcano	Link
(Sato, 2016)	Peak delays - short and long λ	Link

3.1 Parameters

Input Parameters for MuRAT		
Symbol	Descriptor	Where
t_{min}	minimum peak delay allowed	Set in input file
t_{max}	maximum peak delay allowed	Set in input file
t_0 (s)	Origin time	SAC Header

3.2 The peak delay method in pills

The method measures the delay of the maximum energy of the envelope of the direct way to model scattering attenuation with regionalization.

Pros of measuring scattering attenuation using peak delay

1. Single-station measurements - you can get all the info from a single seismogram.
2. Proven sensitivity to structural information and geologic boundaries.

Cons of measuring scattering attenuation using peak delay

1. Assumptions underlying the Markov approximation could be unfulfilled. *Tackled by MuRAT estimating parameters at different frequencies.*
2. No inversion, only regionalization. *Still not tackled by MuRAT.*

Figure 3.1 is a visual representation of the method.

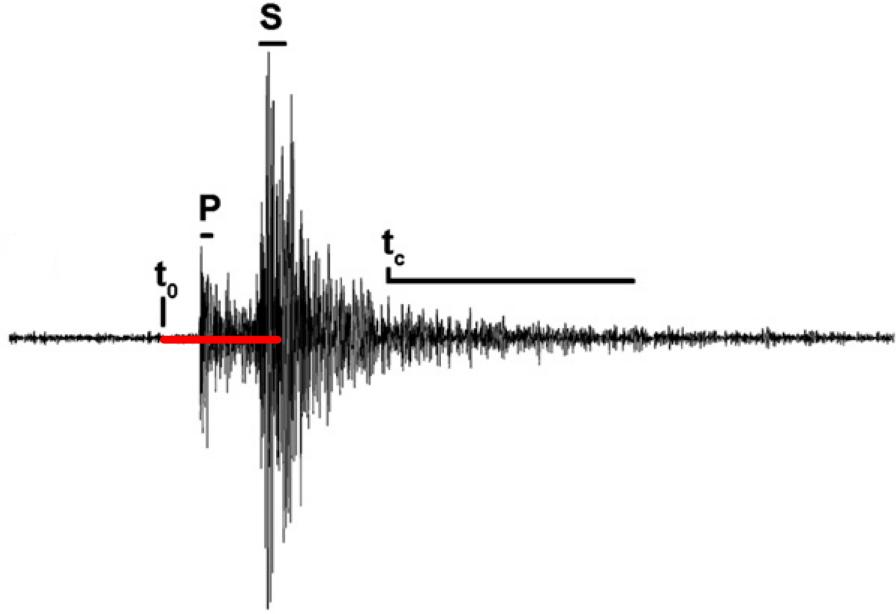


Figure 3.1: The PD method measures the delay of the maximum of the envelope from either the arrival time or the origin time of the event.

3.3 The theory bit

While travelling, direct wave packets broaden because of scattering and diffraction. The seminal work for the application of *peak delay* (envelope broadening) imaging are Aki and Chouet (1975), who demonstrate that coda of high-frequency seismograms originate from random inhomogeneity in elastic properties, and (Sato, 1989), who first proposed peak-delays as a tool to characterise random heterogeneity. Fehler et al. (2000) proved that the Markov approximation for the parabolic wave equation can synthesise seismic waveforms in two dimensions, including early and intermediate coda. The seminal work for the technique is Saito et al. (2002), who developed the equations for forward modelling envelopes for spherically outgoing media characterised by von Kármán power spectral density functions (PSDF).

Saito et al. (2002) provides both an historical view and a discussion of the assumptions underlying the method:

- The primary assumption of the method is that the wavelength ($\lambda = 2\pi/k$) is smaller than the

correlation distance (a), so that if this is multiplied by the wavenumber: $ak \gg 1$. Obviously, the estimation of a is challenging but it appears likely that the assumption will be broken at low frequencies, where *diffraction* takes over.

- Propagation is entirely constrained within a single parallelepiped of average velocity V_0 . The velocity field depends on space (r) as:

$$V(r) = V_0(1 + \xi(r)) \quad (3.1)$$

where $\xi(r) \ll 1$ are random velocity fluctuations. For a wider description of how to derive auto-correlation and power spectral density functions describing fluctuation distributions refer to Sato et al. (2012). These quantities are controlled by ϵ (the root-mean-square of velocity fluctuations), a (the correlation length) and κ (tuning the richness of short-wavelength components of the random medium).

- Frequencies are above 1 Hz, as below that the wavelength grows to a level where most assumptions are invalid in lithospheric settings.

The original definition models envelope duration (t_q) as the quantity related to the characteristic time of envelope broadening (t_M) (Saito et al., 2002). It is instructive to look at the definition of t_M given by Sato (2016):

$$t_M(\kappa, \zeta, k_c, r_0) = \frac{\epsilon^2}{2V_0 a} C_L(\kappa, \zeta, k_c) r_0^2; \quad (3.2)$$

where ζ , which is a number varying between 0.25 and 1.75. Sato (2016) defines it as a tuning parameter and separates random media between long- and short-scale components, so that the correlation distance for small-scale component is : $a_S^{-1} = \zeta k_c$.

This quantity fully defines scattering in the case of long wavelength heterogeneities, depending on average velocity (V_0), hypocentral distance (r_0 , which in a homogeneous medium is the product of V_0 and travel time of the phase t), correlation distance (a), and mean squared velocity fluctuations (ϵ^2), the wavenumber, depending on the angular frequency (ω_c) as $k_c = \frac{\omega_c}{V_0}$ and where:

$$C_L(\kappa, \zeta, k_c) = \begin{cases} \frac{\pi^{1/2} \Gamma(\kappa + \frac{1}{2})}{(2\kappa - 1)\Gamma(\kappa)} (1 - (\zeta a k_c)^{1-2\kappa}) & \kappa \neq \frac{1}{2} \\ 2 \ln(\zeta a k_c) & \kappa = \frac{1}{2} \end{cases} \quad (3.3)$$

The dependency on V_0 and a seem straightforward, at least until we do not make r_0 and $C_L(\kappa, \zeta, k_c)$ explicit. Let's see what happens for $\kappa = \frac{1}{2}$:

$$t_M(\kappa = \frac{1}{2}, \zeta, k_c, r_0) = \frac{\epsilon^2}{2V_0a} V_0^2 t^2 2 \ln(\zeta a k_c) = \frac{\epsilon^2 V_0 t^2 \ln(\zeta a k_c)}{a}; \quad (3.4)$$

in which case:

- The characteristic time increases quadratically with travel time, hence the need for correcting this dependency to focus on scattering.
- A sure way to increase scattering is to increase ϵ^2 -beware that these variations are generally limited.
- Characteristic times increase with frequency and ζ although only logarithmically.
- For actual ranges of correlation distances, t_M can change a lot.

3.3.1 Applicability

The important assumption for the applicability of peak-delay analysis is that scattering is produced by long-scale components. To check the validity, one must always test the following conditions: $\zeta a k_c \gg 1$. In general, this means frequency above 1 Hz. In this case, we can rewrite:

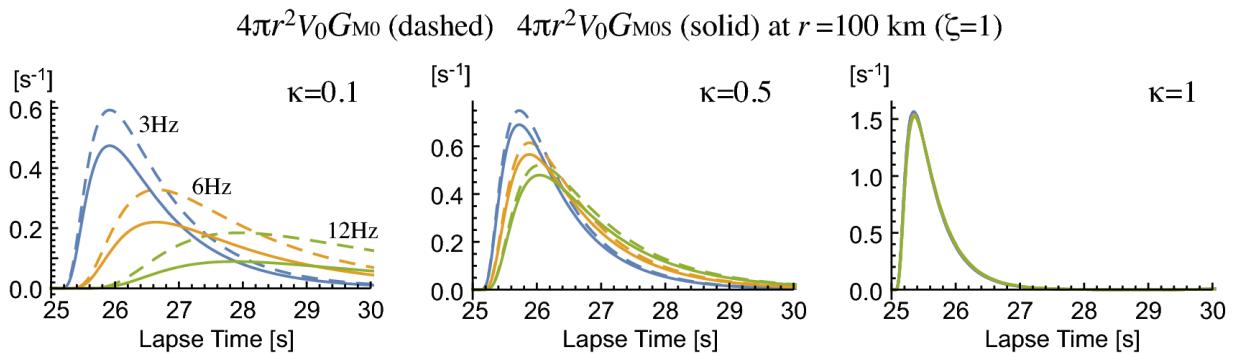


Figure 3.2: Broadening for different κ values. For parameters used, see Sato (2016).

$$t_M(\kappa, \zeta, k_c, r) = \begin{cases} \frac{\epsilon^2}{2V_0a} r^2 \frac{\pi^{\frac{1}{2}} \Gamma(\kappa + \frac{1}{2})}{(1-2\kappa)\Gamma(\kappa)} (\zeta a k_c)^{1-2\kappa} & \kappa < \frac{1}{2} \\ \frac{\epsilon^2}{2V_0a} r^2 \ln(\zeta a k_c) & \kappa = \frac{1}{2} \\ \frac{\epsilon^2}{2V_0a} r^2 \frac{\pi^{\frac{1}{2}} \Gamma(\kappa + \frac{1}{2})}{(2\kappa - 1)\Gamma(\kappa)} & \kappa > \frac{1}{2} \end{cases} \quad (3.5)$$

This is probably the most important relationship as it shows the lack of changes with frequency for $\kappa > \frac{1}{2}$ and the slow dependency for $\kappa = \frac{1}{2}$. Characteristic times, envelopes and scattering are strongly frequency-dependent when $\kappa < \frac{1}{2}$. This gives us an immediate test on our data. Do waveform broaden dramatically at high frequencies (Fig. 3.2)? This is already an indication of the richness in long wave numbers (short-scale components). The first check the user should do is then visual on the data.

3.4 MuRAT workflow

MuRAT works in analogy to Takahashi et al. (2007), Tripathi et al. (2010) and Calvet et al. (2013) when mapping peak delays. These authors show that above 1 Hz one must check the relationship between hypocentral distance and measured peak delay. In Figures 3.3-3.4, we show two examples for different hypocentral distances. It is clear that there is a threshold over which you can apply the approximation. Hence Murat shows you the same plot for your dataset - we will discuss in Chapter ?? the examples at Mount St. Helens, Vrancea and Toba. The peak-delay method requires the same ray tracing approach used for the CN method, discussed computationally in Chapter ???.

Following Takahashi et al. (2007), measurements above (below) the logarithmic linear trend shows high (low) scattering. This procedure is regionalized by this version of MuRAT. It means that positive and negative variations are allocated via their average over blocks after raytracing. The variation is weighted by the length of each segment. Takahashi et al. (2009) show that there are better procedure to invert for the characteristics of power spectral density function using peak delay: we leave it for future versions of the code.

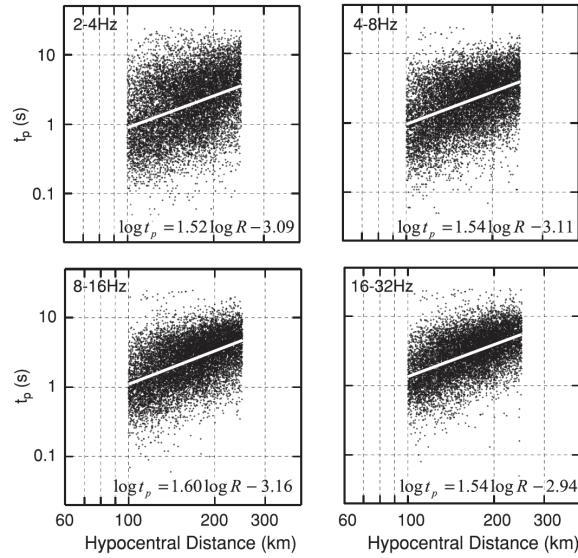


Figure 3.3: Logarithmic plot of peak delay times against hypocentral distances. Black dots represent the data used in this study. White lines are regression lines. From Takahashi et al. (2007).

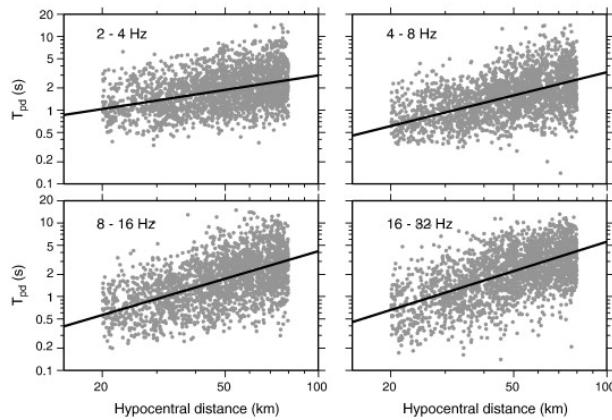


Figure 3.4: Logarithmic plot of peak delay times (in seconds) as a function of the hypocentral distance (in kilometers) for crustal S waves in four frequency bands. Gray dots are the data, and black lines are the regression lines: $\log_{10}(T_{pd}) = Ar(f) + Br(f)\log_{10}R$. From Calvet et al. (2013).

Chapter 4

Absorption: *coda attenuation*

Timeline in papers.		
Paper	Descriptor	Where
(Aki and Chouet, 1975)	Origin of Coda	Link
(Fehler et al., 1992)	MLTWA	Link
(Calvet et al., 2013)	Peak delay regionalisation + Qc: crust	Link
(De Siena et al., 2016)	Peak delay + Qc: volcano	Link
(Del Pezzo et al., 2016)	2D RTT sensitivity kernels: analytic	Link
(De Siena et al., 2017a)	2D inversion with analytic kernels	Link
(Del Pezzo et al., 2018)	3D RTT sensitivity kernels: diffusive	Link
(Akande et al., 2019)	3D inversion with diffusive kernels	Link
(Sketsiou et al., 2020)	Absorption tomography	Link

4.1 Parameters

Input Parameters for MuRAT		
Symbol	Descriptor	Where
t_k	starting lapse time	Set in input file
t_w	coda window length	Set in input file
t_0 (s)	Origin time	SAC Haeder

4.2 The Qc method in pills

The method measures the decay of the envelope from a given lapse time as a way to model absorption with an inversion procedure.

Pros of measuring absorption using Qc

1. Single-station measurements - you can get all the info from a single seismogram.
2. Proven sensitivity to fluids.
3. High-resolution information on near-source and near-station structures.
4. Full inversion procedure.

Cons of measuring scattering attenuation using peak delay

1. The diffusive assumption is rarely fulfilled, with the onset of surface waves corrupting especially low frequencies. *Tackled by MuRAT estimating parameters at different frequencies.*

2. Assumption of single highly-diffusive layer rarely fulfilled. *Still not tackled by MuRAT.*

Figure 4.1 is a visual representation of the method.

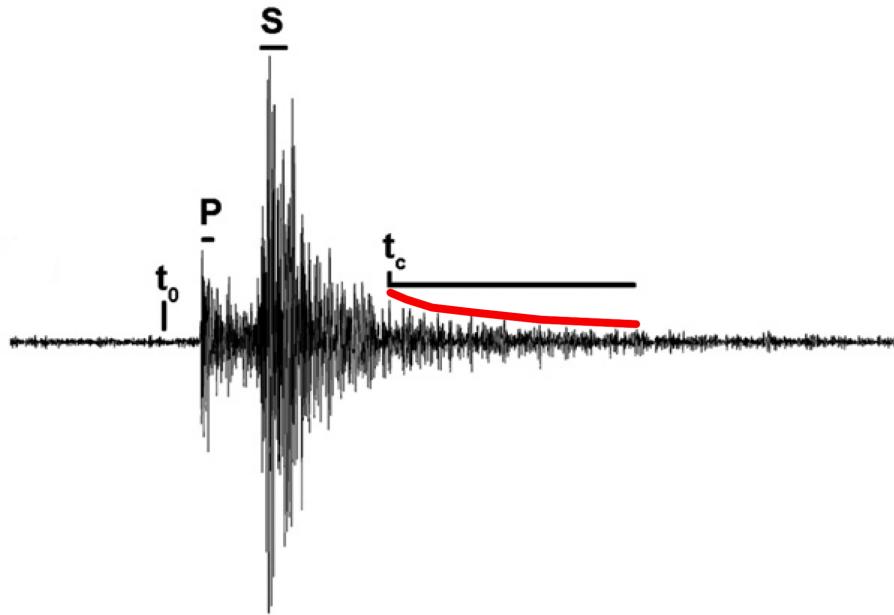


Figure 4.1: The Qc method measures the decay of the envelope from a given lapse time from the origin time of the event.

4.3 The theory bit

4.3.1 MLTWA

Coda waves can be used for more than just normalizing direct wave energies. Starting from the seminal work of Aki and Chouet (1975), coda waves have been used to characterize the tectonic state of the Earth. This has lead to the development of the Multiple Lapse Time Window Analysis (MLTWA) technique Fehler et al. (1992) to separate scattering attenuation Q_s^{-1} from absorption Q_i^{-1} . It does so by measuring extinction length ($L_e = Q_s^{-1} + Q_i^{-1}$) and seismic albedo ($B_0 = \frac{Q_s^{-1}}{L_e}$).

Two assumptions are necessary to apply the MLTWA technique: the direct S-wave dominates the early portion of an S-wave seismogram; the S-coda comprises scattered S-waves. While in its first portion

the S-wave amplitude is controlled by the total attenuation of the medium, coda-waves are a product of scattering (Sato et al., 2012). The filtered seismograms are divided into three time-windows, starting from the S arrival, defined by a starting time t_k and window length t_w . The time integrals $E_k(r)$ of the seismic energy density $E(r, t)$ in each window k is:

$$E_k(r) = \int_{t_k}^{t_k + \Delta t} E(r, t) dt \quad k = 1 \dots 3 \quad (4.1)$$

where the energy is still a function of the source-station distance r . The wave energy decay for each cycle $-\Delta E/E$ is a function of the total quality factor Q (related to the attenuation coefficient η) via the following equation:

$$-\frac{\Delta E}{E} = \frac{2\pi}{Q} = 2\pi \left(\frac{1}{Q_i} + \frac{1}{Q_s} \right) = \frac{v\eta}{f} \quad (4.2)$$

where v is the average wave speed and f is the frequency, respectively. The next step consists in the correction of the energy of each window $E_k(r)$ for both the geometrical spreading and the integral of the t_w -seconds-long normalisation window (the last window in time). This procedure removes source and site effects (Mayeda et al., 1992):

$$E_k^{obs}(r) = \log_{10} \left(4\pi r^2 \frac{E_k(r)}{\int_{t_{coda}}^{t_{coda} + \Delta t} E_k(r, t) dt} \right) \quad (4.3)$$

The resulting logarithms are plotted versus distance in the four frequency bands considered and fitted to the theoretical normalised energies. The theoretical curves are modelled using the L2-norm misfit function for a number of waveforms from i to N :

$$M(L_e^{-1}, B_0) = \sum_{i=1}^N \sum_{k=1}^3 [E_k^{obs}(r_i) - E_k^{theo}(r_i, L_e^{-1}, B_0)]^2 \quad (4.4)$$

$E_k^{theo}(r_i, L_e^{-1}, B_0)$ is the theoretical normalised energy computed at distance r_i for the k -th time-window, fixing the L_e^{-1} and B_0 obtained from MLTWA. M is minimised with a grid search in the B_0 and L_e^{-1} parameter space, and the best-fit values \hat{L}_e^{-1} and \hat{B}_0 are given by the minima of the function. The isolines of the variable $M_{norm} = M(L_e^{-1}, B_0)/M(\hat{L}_e^{-1}, \hat{B}_0)$ give the error estimates on \hat{L}_e^{-1} and \hat{B}_0 . Being M_{norm} an F-variable (Del Pezzo and Bianco, 2010), the model parameters can

be estimated using an F distribution (Pisconti et al., 2015), with a level of confidence higher than F=0.68.

4.3.2 Sensitivity kernels

Due to the increased lateral sensitivity compared to ray-dependent techniques, coda waves are theoretically the ideal tool to image the Earth. In practice, apart for the cases of single scattering and diffusion, there is generally no simple analytical solution, and envelopes have to be dealt with Radiative Transfer Theory (Sato et al., 2012), possibly mixed with ray-tracing techniques that model direct wave information (Sanborn et al., 2017). However, if the wave field is diffusive, one can obtain coda sensitivity kernels with Paasschens equations (Paasschens, 1997) and the approximations of Pacheco and Snieder (2005). Several authors have obtained 2D diffusive kernels based on Radiative Transfer Theory (Obermann et al., 2013; Margerin, 2013; Mayor et al., 2014; Del Pezzo et al., 2016). These kernels have maximum sensitivity at source and receiver (they show a pole at their exact location that must be interpolated) and are all very similar (see e.g. Figs. 4.2) despite being obtained with different approximations. They are primarily aimed at coda-wave interferometry but have found applications in coda-attenuation imaging at regional and local scales (Mayor et al., 2016; De Siena et al., 2017a; Napolitano et al., 2020; Sketsiou et al., 2020). (Calvet et al., 2013) first noticed the contribution of surface waves to low-frequency observations, an effect modelled in 2D by Obermann et al. (2013) and fit on data by Gabrielli et al. (2020). Del Pezzo et al. (2018) have extended the formulation to 3D media, setting the spatial and frequency limits of the kernel applicability and discuss the assumptions behind the applicability of the kernels.

There are two published approaches to map coda attenuation in the 3D space with kernels. The first is regionalization (Del Pezzo et al., 2018) in analogy to peak-delay mapping. An excellent review paper on this approach is Del Pezzo and Ibáñez (2020). MuRAT follows instead the pathway laid down by De Siena et al. (2017a). It assumes that all coda energy is contained within the propagation grid at the chosen lapse time. If this is true, then coda attenuation in space can be obtained from source-station measurement with a standard inversion. Sketsiou et al. (2020) provides an extensive discussion of the differences between regionalization and inversion. Akande et al. (2019) is the first 3D kernel-based coda attenuation model obtained with 3D sensitivity kernels and an inversion approach.

As anticipated in Chapter 1, the combined effect of coherent and incoherent scattering as well as the trade off induced by changing scattering regimes (from Rayleigh to Mie scattering, Cormier and Sanborn (eg 2019)) can deeply affect the reliability of the kernels. In order for these to be applied,

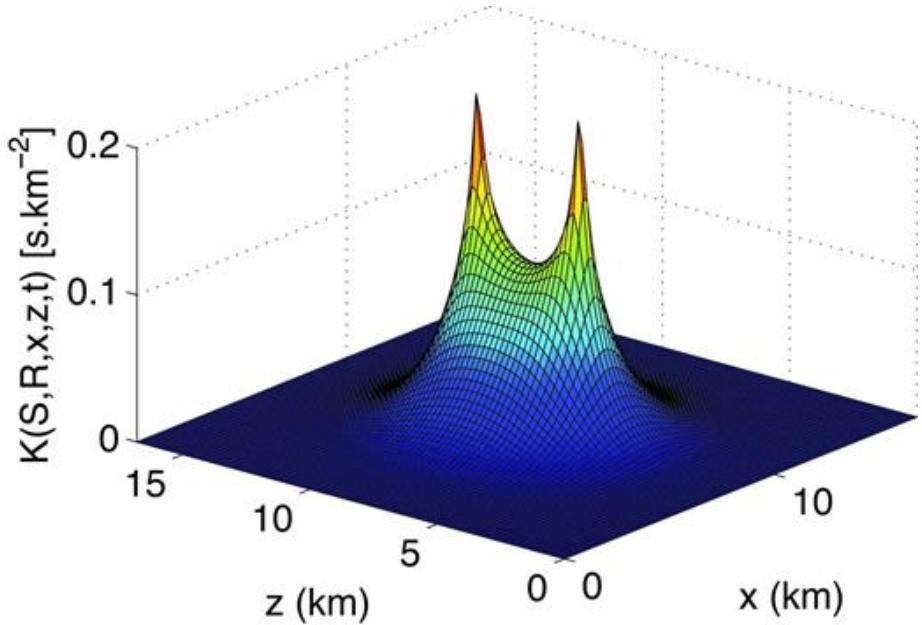


Figure 4.2: Diffusive sensitivity kernels at time 3.6 s obtained by Obermann et al. (2013)

there is a need for a volume with uniform (or gradually-changing) scattering properties, which is rarely valid at all frequencies investigated. Surface Obermann et al. (2013) and resonant Margerin (2013); De Siena et al. (2013) waves, sharp horizontal transitions in scattering (Wegler, 2005; Margerin, 2017; Nardoni et al., 2021) and more generally not accounting properly for the trade-offs with geometrical spreading (Morozov, 2011) all bring to inexact, if not incorrect, images of the Earth's scattering and absorption properties.

4.3.3 Applicability

Coda attenuation is measured by MuRAT in the diffusive assumption, hence one must check that Q_c^{-1} does not vary with hypocentral distance (Calvet et al., 2013). However, this only attests that equipartition is in place, a necessary but insufficient condition for diffusion. The analysis of coda attenuation with frequency is central to test the applicability of both MLTWA and sensitivity kernels (Sketsiou et al., 2020). Also, as we are using the inversion procedure, it is central to test that most of coda energy remains inside the inversion grid (Akande et al., 2019).

MuRAT offers tools to test these approximations and the effect of Q_c on measurements of total

attenuation (chapter 3).

4.3.4 MuRAT workflow

MuRAT works in analogy to Mayor et al. (2016), De Siena et al. (2017a) and Akande et al. (2019) when modelling coda attenuation. These authors show that above 1 Hz one must check the relationship between hypocentral distance and measured coda attenuation. In Figure 4.3, we show the expected relation of coda attenuation versus hypocentral distance for the applicability of the theory and interpretation of Q_c as measurement of absorption. It is clear that the standard assumption of twice the S-wave travel time (Aki and Chouet, 1975) does not work. Hence Murat shows you the same plot for your dataset - we will discuss in Chapter ?? the examples at Mount St. Helens and in Vrancea. However, the ideal threshold (100 s in this particular case) removes too many data for reliable coverage. Figures 4.3c shows the acceptable compromise.

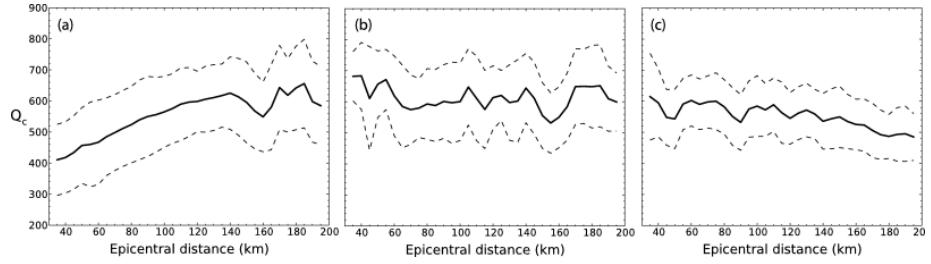


Figure 4.3: (a) Q_c as a function of the epicentral distance in the 4–8 Hz frequency band. The duration of the coda window is fixed ($t_w = 50$ s). The solid and dashed lines show the mean dependence of Q_c with the epicentral distance and the associated uncertainties, respectively. The analysis is performed on the onset of coda window t_k equal to (a) $2tS$ (b) 100 s and (c) 70 s. From Mayor et al. (2016)

MuRAT also outputs the sensitivity kernels in two grids: (1) the fine propagation grid, extending generally well beyond the area of inversion, and (2) the inversion grid. The first is used to compute the full kernels and interpolate the poles at source and receiver locations (Akande et al., 2019). The boundaries of the second are chosen by the user depending on source-station coverage. The code shows what percentage of the energy is still contained inside the inversion grid.

Chapter 5

Getting started

5.1 Installation and set up in a nutshell

The current version of the code works following these steps:

1. Download or clone the package at [the corresponding GitHub page](#);
2. Work in the downloaded folder after moving it to an appropriate location on your system;
3. Check that the IRTools have been downloaded in the corresponding folder in the working directory. Otherwise download them from [the corresponding GitHub page](#);
4. Open one of the three input .mlx files, providing a step-by-step explanation of all inputs (*Murat_inputMSH.mlx*, *Murat_inputRomania.mlx*, or *Murat_inputToba.mlx*) and create your own;
5. MuRAT works with SAC files that must be stored into a single folder and corrected for the instrument function. The files must have populated headers, although the code can work using just some header fields (see Chapter 6);
6. Run MuRAT3.mlx and select the name of the input file desired.

5.2 Matlab

MuRAT wants to be an open-access code, yet it also comes in Matlab format:
why?

- The first reason is historical. The code has been designed with core Matlab program, with legacy bash and Fortran codes embedded in it. Passing from Matlab to Python, the obvious

choice for open-access interfaces, was not straightforward. Passing from Matlab to Julia has been way easier. Evolving through a decade, the Matlab version of MuRAT has reached the format presented here. Yet, MuRAT3.0 will be the last release in Matlab.

- The second reason is simplicity of learning. MuRAT has been thought from start as a way to introduce students to computational seismology. Matlab an ideal interface to teach computational codes to students in Earth Sciences. MuRAT has also been developed with the wider geological community in mind, which until recently was often lacking training in computation. The average geology student understands Matlab better than other codes.
- The third reason is that Python is becoming the standard in seismology, especially thanks to tools like Obspy, yet this is not so obvious for the rest of Earth Sciences. For example, Matlab is (has been) the favourite language interface for most of the Geodynamics community - see for example Taras Gerya's Introduction to Numerical Geodynamic Modelling. The geodynamics community is embracing Julia as its natural successor. MuRAT does the same.

5.2.1 Requirements and installations

- **DOWNLOAD:** MuRAT from Github. Ideally, fork or star the code to get updates. This guide explains how to work with GitHub Desktop.
- **SYSTEM:** The program works on Mac, Linux and Windows systems equipped with Matlab R2019a or later.

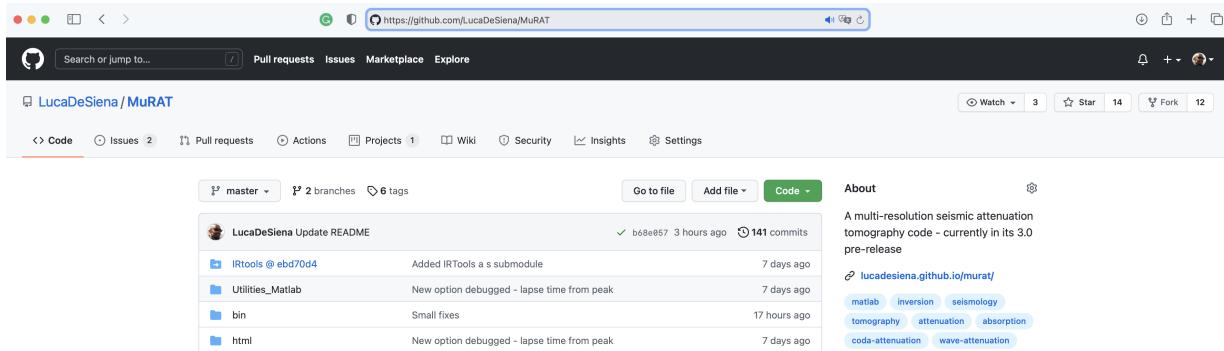


Figure 5.1: The MuRAT page on GitHub.

- **NECESSARY TOOLBOXES:** Signal Processing, Curve Fitting, Image Processing and Mapping Toolboxes. The Parallel Computing Toolbox is recommended for speed.
- **EXAMPLE DATASETS:** Three sample datasets (Mount St. Helens, Romania, and Toba) are included in the package and allow the user to obtain sample models. The datasets work with the input .mlx files that are provided in the working directory.

5.2.2 Changing folder

a)

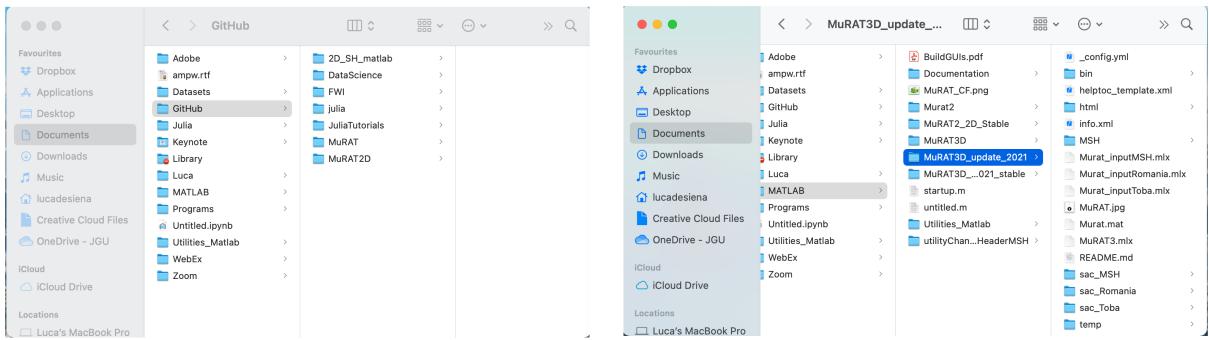


Figure 5.2: How I work with MuRAT in Matlab. a) The folder where the branched code is downloaded (left) vs the working directory (right). b) The Workspace in Matlab. Notice only the Matlab input files are present and must be edited.

In this example, MuRAT is cloned from the corresponding page (Fig. 5.1) to a folder inside GitHub Desktop. As a developer or user of MuRAT for multiple datasets, you might want to copy this folder on your system at a different location (Fig. 5.2). In the example (Fig. 5.2,a), we show how you download automatically the main version of the code in a folder contained in the Github folder. Depending on your system, the path to this folder could be different. It is recommended to copy and rename the folder to another path (Fig. 5.2,b), and leave the original MuRAT folder where it is downloaded. When finished with your work or if cooperating on that specific dataset with someone, you can then substitute your edited folder in Github. This will allow you to push a new branch that might be used as repository for codes and results. These repositories are now a requirement for most journals and allow you to get the seminal version of your results in case of reviews.

5.3 Julia

MuRAT will be an open-access code developed in Julia from this version onward.

Julia is FAST. Julia is EASY. Julia is more similar to Matlab. Hence, the choice to switch from Matlab to Julia. Is it better than Python? This is an absurd question for two languages developed in different decades. If you need to call a Python script (and sometimes you do), you can do it from Julia. Please have a read at this interesting comparison to know more about how the two codes compare.

Chapter 6

Data preparation

6.1 SAC files

The Seismic Analysis Code has been the standard in seismology for at least 20 years. In order to process the SAC data in Matlab, we use the MatSAC tools created by Prof. Zhigang Peng from Georgia Tech. MuRAT owes a lot to the format defined by Peng with his *fget_sac* function:

$$[t, data, SACHdr] = fget_sac(pathSACFile) \quad (6.1)$$

where, given the path of the SAC file, the user obtains two variables (*time* and *data*) and especially a structure (*SACHdr*) that stores the fields of the header.

This chapter deals with the original SAC files and how you must populate their header in order to work with MuRAT. By populating the header, the user will need no additional file related to data processing.

6.2 Parameters

The aim in MuRAT has always been to do attenuation imaging using SAC files that can be downloaded from online servers. These data are provided via miniseed that must be unpacked. The resulting SAC might have already populated headers: it is up to the user to populate the parameters shown in the following table if they are blank (or -1234 as by SAC standard).

Necessary Parameters in SAC header		
SAC field	Descriptor	Name in Matsac header
<i>o</i> (s)	origin time	<i>SAChdr.times.o</i>
<i>a</i> (s)	P-wave pick	<i>SAChdr.times.a</i>
<i>t0</i> (s)	S-wave pick	<i>SAChdr.times.t0</i>
<i>stla</i> (deg)	station latitude	<i>SAChdr.station.stla</i>
<i>stlo</i> (deg)	station longitude	<i>SAChdr.station.stlo</i>
<i>stel</i> (m)	station elevation	<i>SAChdr.station.stel</i>
<i>evla</i> (deg)	event latitude	<i>SAChdr.event.evla</i>
<i>evlo</i> (deg)	event longitude	<i>SAChdr.event.evlo</i>
<i>evdp</i> (km)	event depth	<i>SAChdr.event.evdः</i>

6.3 *sac_datafolder* - checking data

The bold-faced parameters in the above table are mandatory. The user can check the parameters in the header of each SAC file: before doing it, the user can run the utilities *Murat_test.m* and *Murat_testAll.m*, in the **Utilities** folder. After running MuRAT the first time, this folder will be added to your path. Otherwise just work copying them in your working directory folder.

6.3.1 *Murat_test* - testing single waveforms

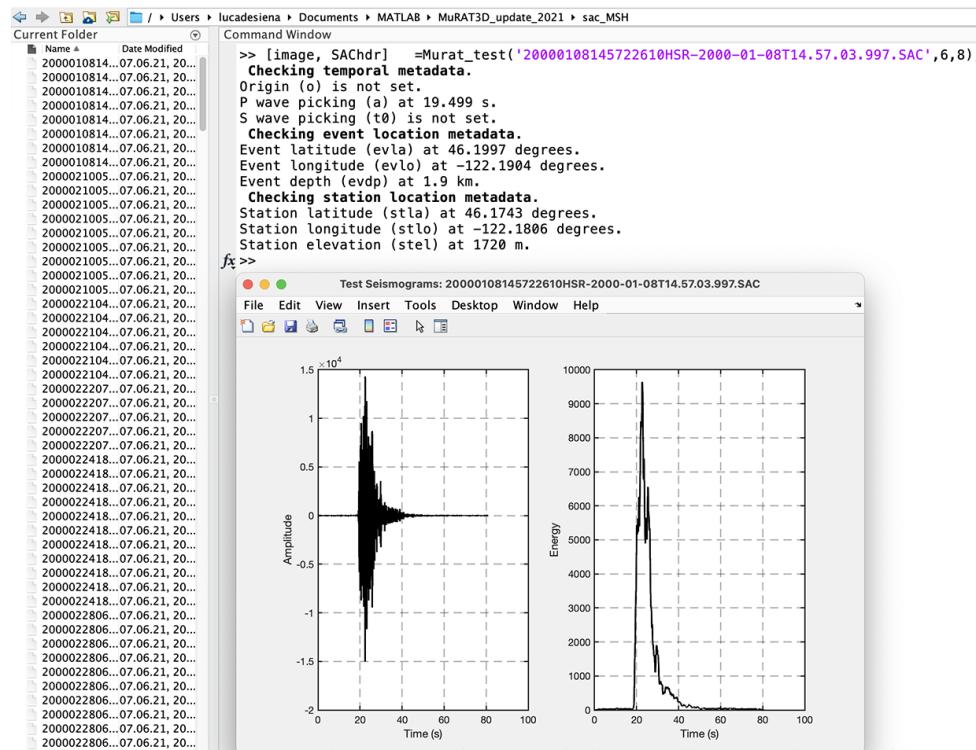


Figure 6.1: Example run of *Murat_test*. The image is shown while the SACheader is created in the workspace. All the necessary parameters are checked. Notice the missing S-wave picking - it is possible that the variable storing this parameter is different from t0.

```

% function [image, SAChdr] = Murat_test(nameWaveform, ...
% centralFrequencies, smoothingC, figOutput, verboseOutput)
% TEST seismogram envelopes for changes in broadening

```

```

% CREATES a figure with seismograms and envelopes for different frequencies
%
% Input Parameters:
%   nameWaveform:           name of the SAC file
%   centralFrequencies:     vector of frequencies (Hz), if [] no filter
%   smoothingCoefficient:   coefficient to smooth envelopes
%   figOutput:              decide if you want to show figures (set to 1)
%   verboseOutput:          decide if you want to show messages (set to 1)
%
% Output:
%   image:                  image with envelope at specified frequency
%   SAChdr:                 header of the SAC file
%
```

The function used the path of a waveform, a vector of central frequencies, and a smoothing coefficient as inputs. There are two additional flags, that allow to show the corresponding seismogram and envelope (set *figOutput* = 1) and the output messages (set *verboseOutput* = 1). It provides the user with the header structure (SAChdr). The fields necessary to apply MuRAT can be checked in the workspace and the command window, or displayed directly with the *verboseOutput* on. Figure 6.1 shows an example run of Murat _ test for a file stored in the sac _ MSH folder, filtered at 6 Hz with smoothing of 8 samples per cycle.

6.3.2 Murat _ testData.m - creating a file to check all headers in dataset

MuRAT checks that all the parameters in the headers for a dataset are populated. It produces error messages for the missing parameters, pointing at the corresponding waveform. Finally it outputs the excel file *DataHaeders.xlsx* in the results, providing an overview of all the required parameters. Fig. 6.2 shows this file after a run over the data folder sac _ MSH. Missing parameters will be blank in the file. The origin and S-wave peaking (searched for the SAC variables *o* and *t0*) are missing. These are optional parameters if using P waves so the code will work anyway.

Screenshot of Microsoft Excel showing a data file named "DataHeaders.xls". The file contains a single sheet with data starting from row 1. Row 1 is a header row with columns labeled A through J. The data rows (rows 2 to 7) contain entries for seismic wave files, each with a unique identifier, path, and various parameters like Origin, P, S, EvLat, EvLon, EvDepth, StLat, StLon, and StElev.

	A	B	C	D	E	F	G	H	I	J
1	Names									
2	/Users/lucadesiena/Documents/MATLAB/MuRAT3D_update_2021/sac_MSH/20000108145722610FL2-2000-01-08T14.57.03.997.SAC	21.27791595	P	S	EvLat	EvLon	EvDepth	StLat	StLon	StElev
3	/Users/lucadesiena/Documents/MATLAB/MuRAT3D_update_2021/sac_MSH/20000108145722610HSR-2000-01-08T14.57.03.997.SAC	19.4989624		46.1996994	-122.1903992	1.899999976	46.1962204	-122.3514862	1378	
4	/Users/lucadesiena/Documents/MATLAB/MuRAT3D_update_2021/sac_MSH/20000108145722610JLK-2000-01-08T14.57.03.997.SAC	20.0832901		46.1996994	-122.1903992	1.899999976	46.17427826	-122.1806488	1720	
5	/Users/lucadesiena/Documents/MATLAB/MuRAT3D_update_2021/sac_MSH/20000108145722610LVP-2000-01-08T14.57.03.997.SAC	22.92701912		46.1996994	-122.1903992	1.899999976	46.06594849	-122.4019318	1130	
6	/Users/lucadesiena/Documents/MATLAB/MuRAT3D_update_2021/sac_MSH/20000108145722610MTM-2000-01-08T14.57.03.997.SAC	22.4595849		46.1996994	-122.1903992	1.899999976	46.02532959	-122.2128677	1121	
7	/Users/lucadesiena/Documents/MATLAB/MuRAT3D_update_2021/sac_MSH/20000108145722610SHW-2000-01-08T14.57.03.997.SAC	19.65478325		46.1996994	-122.1903992	1.899999976	46.19347	-122.2363351	1425	

Figure 6.2: Example file after running MuRAT for the MSH example. All the necessary parameters are checked. Notice the missing S-wave picking - it is possible that the variable storing this parameter is different from t0.

Chapter 7

Input files

MuRAT3 offers three input files as examples (Fig. 7.1). A new user needs to edit these files in order to run the code. The details of the files are given into each *mlx* file. The Mount St. Helen input file is shown in Appendix A. The new user can use this *Murat_inputMSH mlx* file to learn what each parameter does; however, users soon switch to a simpler *.m* file, as the one stored in the same folder of the standard release (*Murat_inputMSH.m*). The input files are divided into sections, whose inputs are described in the following. For a more precise description, consult the *.mlx* files.

Current Folder		Date Modified
	Name	
>	bin	19.10.21, 16:13
>	html	15.08.21, 11:43
>	IRtools	20.09.21, 08:53
>	sac_MSH	10.09.21, 19:20
>	sac_Romania	20.11.20, 16:21
>	sac_Toba	10.09.21, 19:20
>	velocity_models	19.10.21, 15:19
	_config.yml	11.10.20, 15:14
	Documentation_MuRAT.pdf	19.10.21, 13:29
	helptoc_template.xml	09.12.20, 17:14
	info.xml	09.12.20, 17:11
	MuRAT.jpg	19.10.21, 13:29
	MuRAT3mlx	19.10.21, 12:05
	Murat_inputMSH.m	23.10.21, 16:27
	Murat_inputMSH mlx	18.10.21, 14:47
	Murat_inputRomaniamlx	18.10.21, 15:15
	Murat_inputTobamlx	18.10.21, 15:16
	README.md	19.10.21, 13:29

Figure 7.1: Input files are provided as *Murat_input..mlx* files. There are three sample inputs (Mount St. Helens - MSH, Romania and Toba caldera) in the standard release.

7.1 The fields of the input

- GENERAL FIELDS:

Murat.input.dataDirectory: Define the name of folders where data are located

Murat.input.label: Define the name of the folder where results will be stored

Murat.input.workers: Number of cores if parallelized, leave empty for sequential code

- WAVEFORM DATA

Murat.input.originTime: Define the variable that stores the origin time, or leave empty

Murat.input.PTime: Define the variable that stores the P-time

Murat.input.STime: Define the variable that stores the S-time, or leave empty

Murat.input.PorS: Define if the analysis is for P- or S-waves

Murat.input.centralFrequency: Define the set of central frequencies analyzed

Murat.input.components: Define the number of components

- PEAK DELAY

Murat.input.minimumPeakDelay: Minimum peak delay allowed

Murat.input.maximumPeakDelay: Maximum peak delay allowed

- DIRECT WAVE ATTENUATION

Murat.input.spectralDecay: Spectral decay of coda, for surface, diffusive or body waves

Murat.input.bodyWindow: Window to measure body waves and noise in seconds

Murat.input.startNoise: Seconds to start noise window from start of recording

Murat.input.thresholdNoise: Minimum signal-to-noise ratios allowed

- CODA ATTENUATION

Murat.input.lapseTimeMethod: Define the method used to measure coda waves

Murat.input.startLapseTime: Define start of coda waves

Murat.input.codawindow: Define the length of coda window

Murat.input.Albedo: Measured Albedo from MLTWA

Murat.input.extinctionLength: Measured Extinction Length from MLTWA

Murat.input.QcMeasurement: Decide if using a Linearized or Non-Linear approach

Murat.input.kernelThreshold: Define coefficient to make kernels more accurate or quicker to compute

- GEOMETRY AND VELOCITY

Murat.input.origin: Define the origin of the spatial grid

Murat.input.end: Define the end of the spatial grid

Murat.input.gridLat: Number of nodes across latitude

Murat.input.gridLon: Number of nodes across longitude

Murat.input.gridZ: Number of nodes across depth

Murat.input.sections: Location of sections where you will get the maps

Murat.input.availableVelocity: Decides if a 3D model is available

Murat.input.namev: Defines the name of the velocity model

Murat.input.averageVelocityP: Defines the average P-wave velocity

Murat.input.averageVelocityS: Defines the average S-wave velocity

- INVERSION AND PLOTTING

Murat.input.inversionMethod: Inverts with zero-order Tikhonov or Iteratively

Murat.input.lCurve: Decides if selecting the damping during computation

Murat.input.lCurveQc: Damping parameters for different frequencies, Qc inversion

Murat.input.lCurveQ: Damping parameters for different frequencies, Q inversion

Murat.input.sizeCheck: Decides if doubling or making node space 4 times in checkerboard

Murat.input.highCheck: Decides the maximum inverse attenuation in the checkerboard

Murat.input.lowCheck: Decides the minimum inverse attenuation in the checkerboard

Murat.input.spikeLocationOrigin: Origin of the spike block

Murat.input.spikeLocationEnd: End of the spike block

Murat.input.spikeValue: Value of attenuation in the block

Appendices

Appendix A

MuRAT input file - Mount St Helens

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INPUT MuRAT3D - MSH

This is an input file for the program Multi-Resolution Attenuation Tomography (MuRAT), version 3. It refers to the following area:

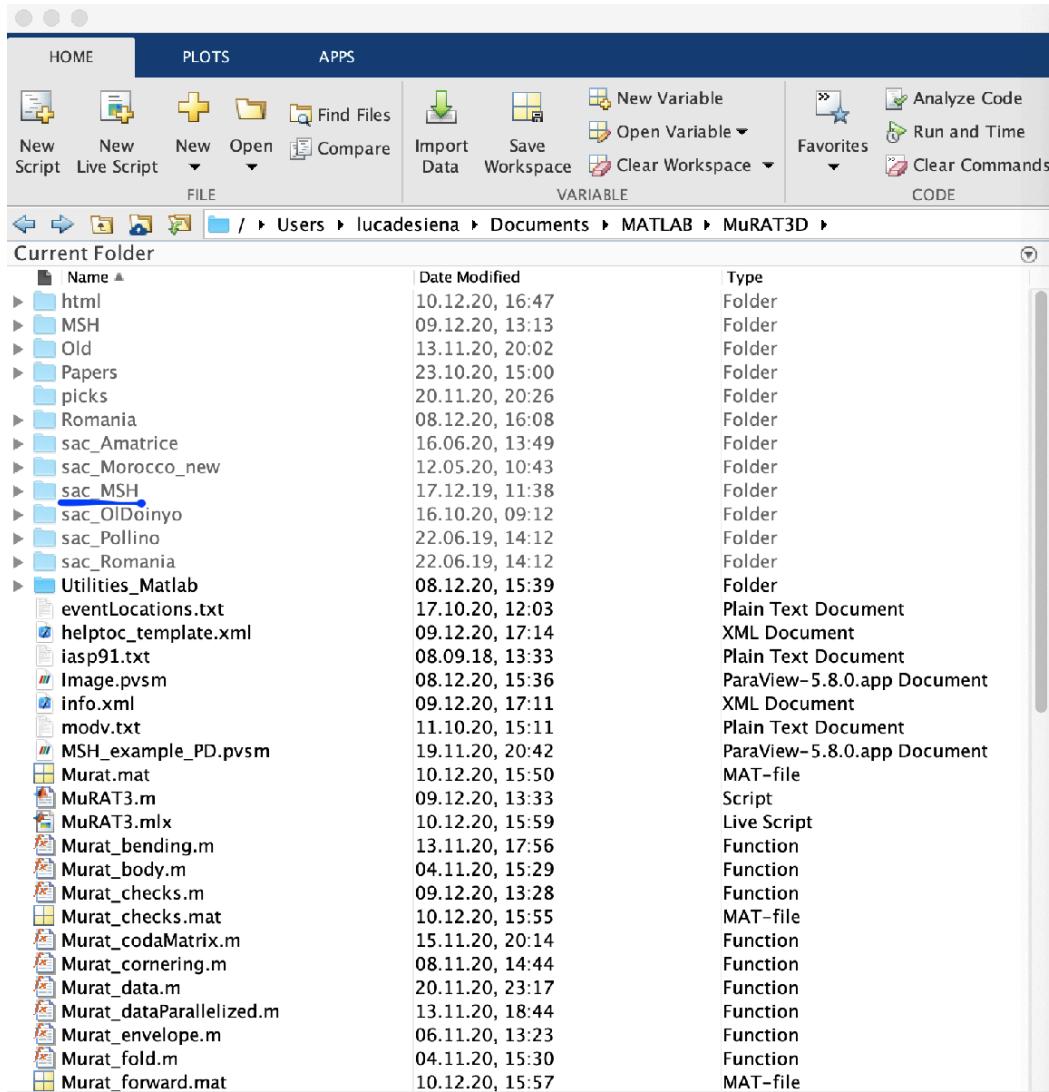
MOUNT ST HELENS VOLCANO

The working directory is the folder where you downloaded MuRAT: move it anywhere in your system.

GENERAL FIELDS

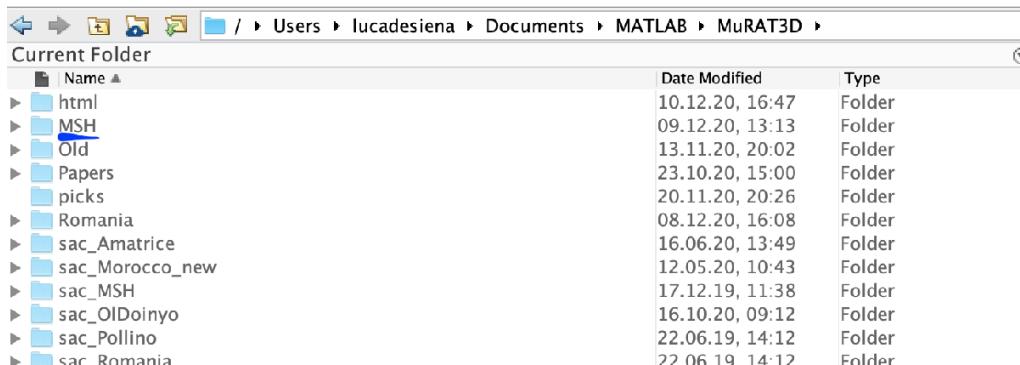
The user needs a data directory containing .sac files (beware of the difference between .sac and .SAC). If you want to use two or three-component recordings, you have to store them into a single folder, but the three components must be in the exact order **E,N,Z**. For an example see Toba. For this example we will use data in the **sac_MSH** folder. Inside this folder, only vertical (**Z**) seismograms are stored:

```
Murat.input.dataDirectory      =      'sac_MSH';
```



Best practice is to create a new folder to store your results. The code will create this folder inside the working directory. Specify the name of the folder that will store text files and figures, and will appear in your working directory:

```
Murat.input.label = 'MSH';
```



In MuRAT3D you can choose between a sequential or parallelized forward loop. In the parallelized case, just set a number of workers (cores). In this example, we are working with the parallelized code and a computer with 8 cores. Otherwise, set *Murat.input.workers* as empty ([]).

```
Murat.input.workers = 8;
```

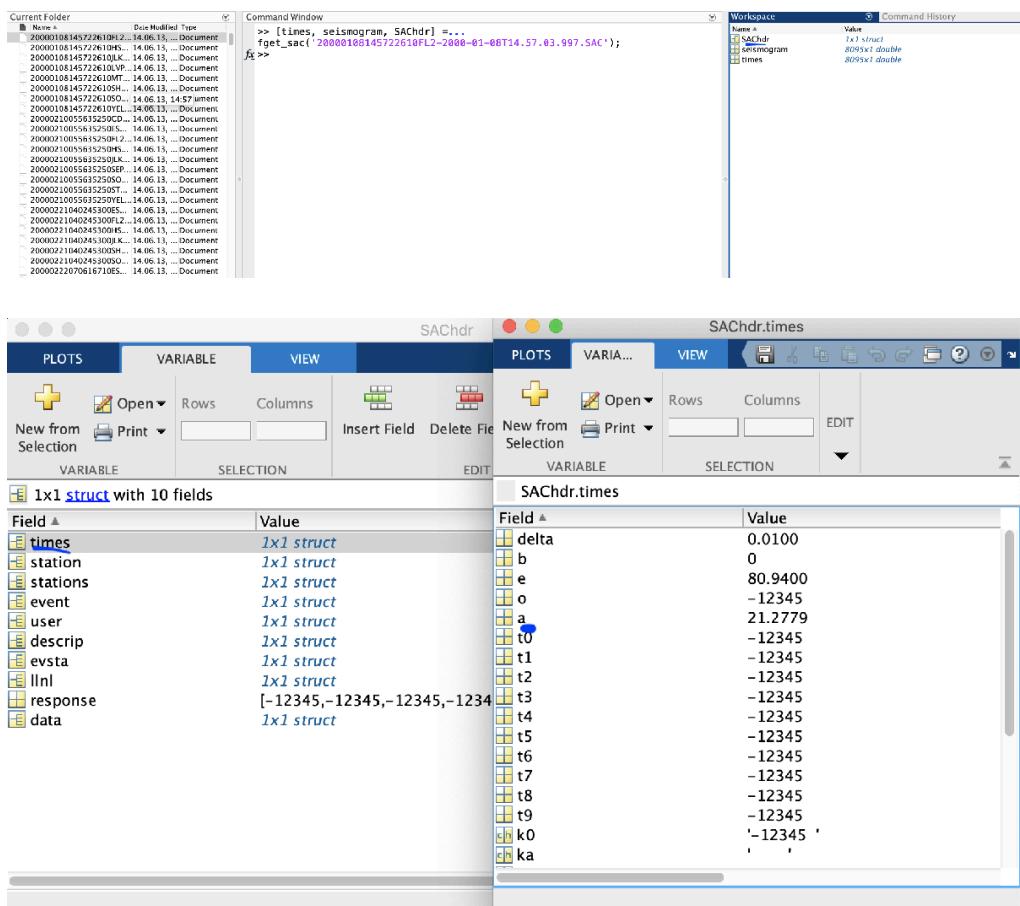
WAVEFORM DATA

Set all the variables required by data processing. This includes data choices, as setting the name of the variables in SAC and all the attributes that are needed for the three kinds of imaging. The routines for loading the files have been mostly created by [Zhigang Peng](#) and co-workers and downloaded from their [Introduction to SAC](#) webpage.

MuRAT3D is designed to work with sac files only, so it is necessary to set the name of the variable containing their peakings and zero time. Files have to have populated headers. Set the name of the variable containing the origin time, P-wave peaking and S-wave pickings - in this example there is only the mandatory P-wave picking. If you don't have the origin time and S-wave times at hand you can mark them as empty ([]):

```
Murat.input.originTime = [];
Murat.input.PTime = 'a';
Murat.input.STime = [];
```

SAChdr is a structure that contains all the fields you saved in the SAC header. In this example the P-wave picking has been stored inside variable *a*. You always find these variables in the *times* subfield:



Then choose the coherent phase you are analyzing - P-(2) or S-(3). In our case it is P- as we have no S-wave picking:

```
Murat.input.POOrS = 2;
```

You need to set the central frequencies (Hz) according to your spectrograms. General practice is to vary it across your spectra (see [De Siena et al. 2016, EPSL](#)) for absorption and scattering mapping or focus on a given frequency ([De Siena et al. 2014, JGR](#)) for direct-wave attenuation imaging. Here, they cover the interval [1.5-24] Hz:

```
Murat.input.centralFrequency = [3 6 12 18];
```

You can work with 1 vertical or horizontal (1), 2 horizontal (2) or three components(3). If using more than one component, the order *MUST BE: WE, SN, Vertical or SN, WE, Vertical*. In this example we work with the vertical component only:

```
Murat.input.components = 1;
```

PEAK DELAY

Scattering (peak delay) measurements rely on the existence of coherent waves. Peak delay is a standard measurements of forward scattering in regional scale-mapping since [Takahashi et al. 2007, GJI](#). Here, we approach the problem by adding a ray-tracing strategy to the system, assuming that the sensitivity follows the seismic ray. Also, we bring it to 3D and apply it to P-waves (see [De Siena et al. 2016, EPSL](#)).

To do so we need to set a minimum peak delay (s) considering scattering in the area and frequency. If using P wave this is important, as they can be sometimes more energetic than S-waves, biasing our measurements. We also need to set the maximum peack-delay (s) to avoid picking surface waves.

```
Murat.input.minimumPeakDelay = 0.1;
Murat.input.maximumPeakDelay = 7;
```

DIRECT WAVE ATTENUATION

Total attenuation (inverse Q) measurements also relies on the existence of coherent waves. Total attenuation with the coda-normalization method is today astandard in volcano tomography ([Del Pezzo et al. 2006, PEPI](#), [De Siena et al. 2010, JGR](#); [De Siena et al. 2014, JGR](#), [Prudencio et al. 2015, Prudencio & Manga, 2020](#)).

The method relies on the measurements of both direct and coda wave energy. Therefore we need to set the spectral energy decay of the coda wavefield. The spectral decay has to be set for prdominance of 2D surface (0.5), diffusive (1.5) or body waves (2). Here it is it is the first case:

```
Murat.input.spectralDecay = 0.5;
```

Then we set the length of the window used to measure direct-wave energy, trying to smooth radiation pattern effects. The code uses the lame length to measure noise energy. Discussions on the topic can be found in [De Siena et al. 2009, PEPI](#) and [De Siena et al. 2010, JGR](#), but the choise is as usual dependent on data:

```
Murat.input.bodyWindow = 1;
```

We also need the start of the window used to measure noise a few seconds after the start of the recording (in seconds).

```
Murat.input.startNoise = 5;
```

The coda-to-noise energy ratio is used by the weighted inversion. Here you set the minimum accepted energy ratio.

```
Murat.input.thresholdNoise = 3;
```

CODA ATTENUATION

Coda attenuation (inverse Qc) is measured from the decay of the coda with lapse time from the origin time of the earthquake, and requires energetic scattering. Qc is a well known parameter for assessing tectonic structures ([Sato et al. 2012, Springer](#)). In recent years it has been used as an imaging attribute at the regional ([Calvet et al. 2013, Tectonophysics](#); [Borleanu et al. 2017, Tectonophysics](#)), fault ([Napolitano et al. 2020; Sketsiou et al. 2020, PEPI](#)) and, especially, volcanic scales ([Prudencio et al. 2013a, GJI](#); [Prudencio et al. 2013b GJI](#); [De Siena et al. 2016, EPSL](#); [De Siena et al. 2017, GRL](#); [Gabrielli et al. 2020, GJI](#)).

Lapse times and sensitivity kernels

In MuRAT3D, we use the full 3D computational kernels devised by [Del Pezzo et al. 2018, Geosciences](#) in the inversion approach proposed first by [De Siena et al. 2017, GRL](#).

Here you choose the start of the window used to measure coda wave energy and model kernels. The starting time of the coda window can be set directly in seconds ('Constant'), from the envelope peak ('Peak'), or depending on the P- or S-wave travel time, for example twice the S-wave travel time ('Travel'). If the chosen method is **Constant**, set start and length of the window.

```
Murat.input.lapseTimeMethod = 'Constant';
```

If the chosen method is **Constant**, set the start of the window in seconds after the origin time. If it is **Peak**, set it to **[]**. If it is **Travel** select *Murat.input.startLapseTime* as the multiplicative factor of the phase you are using (e.g., **2** or **3**). Avoid this method if you do not know the S-wave time.

```
Murat.input.startLapseTime = 15;
```

Finally set the length of the coda window in seconds. The true lapse time at which we calculate the kernels is half of the window. The window is also used (after normalizing for its length) in the coda normalization method.

```
Murat.input.codaWindow = 15;
```

The **MLTWA** is the standard method to find the average parameters necessary to calculate the kernels. It provides albedo and extinction length:

```
Murat.input.albedo = 0.5;
Murat.input.extinctionLength = 0.02;
```

As the kernels are computational intensive and require a full matrix of nodes to avoid singularities, we also use a computational factor to reduce the computational time. This number divides the input grid, meaning that higher numbers give more precise results at the expense of computational time. Minimum is **1**. A figure will output the kernel in this grid.

```
Murat.input.kernelThreshold = 2;
```

Measurement of Qc

MuRAT3D implements either a linearised approach or a grid search approach to measure Qc. The linearised approach is the standard proposed first by Aki (e.g., [Havskov et al. 2016, BSSA](#)) to best fit Qc after taking the logarithm of the energy. The uncertainties are derived from the simple minimum R-squared (fitThresholdLinear) and needs to be defined by a number between 0 and 1. It is advisable to set a minimum of 0.1.

The non linear approach models energy data measured on one-second windows across the envelope and minimizes the difference between data and model with a 1D grid search algorithm ([Napolitano et al. 2020](#)). Uncertainties are given by the experimental probability density function of the misfit. In both cases, uncertainties play as a weight in the final inversion. In the second case, leave the fitThresholdLinear = [].

The user needs to choose between the two options '**Linearized**' and '**NonLinear**':

```
Murat.input.QcMeasurement = 'Linearized';
Murat.input.fitThresholdLinear = 0.1;
```

GEOMETRY AND VELOCITY

This section sets the details of the inversion grid and availability of velocity model. In MuRAT3D the coordinates of the model are in lat/lon, then they get converted in km. The vertical is in altitude above sea level. The velocity model can be 1D or 3D - if 3D all points must be given in lat/long formats. You start by setting the origin and end points of your inversion grid.

```
Murat.input.origin = [45.9805 -122.5030 3350];
Murat.input.end = [46.3900 -122.0000 -22650];
```

Then you need to set the number of nodes in the three directions. This is obviously dependent on the scale of your area. You will be playing a lot with this to test your effective resolution capabilities.

```
Murat.input.gridLat = 10;
Murat.input.gridLong = 12;
Murat.input.gridZ = 6;
```

MuRAT3D now saves everything in Paraview format (.VTK) but some checks in Matlab can be useful. All these sections are saved in the *Label* folder. You will see all of your figures on three sections cutting the models WE (degrees), SN (degrees), and horizontally (meters or km) at:

```
Murat.input.sections = [46.12 -122.20 -1000];
```

With this version of the code you are always using an underlying velocity model: the 3D is either unavailable(**0**) or a available (**1**) velocity model. For the 1D case MuRAT provides you *iasp91.txt*, the standard [IASPEI velocity](#)

model and expands it to a false 3D. However, a standard crustal model is generally available everywhere on the Earth, so use that - but change it to the same format as the file provided, first column is depth, second is distance from the centre of the Earth, then third and fourth are P- and S-wave velocity. Store the file in the folder **velocity_models**. See the Romania example file. At Mount St. Helens, we use the 3D local earthquake tomography model of [Waite and Moran, 2009, JVGR](#), (*modvMSH.txt*), stored in the folder **velocity_model**:

	1	2	3	4
4.5978252e+01	-1.2250525e-02	3.3500000e+03	3.5750000e+00	
4.5978252e+01	-1.2250525e-02	1.3500000e+03	4.5475000e+00	
4.5978252e+01	-1.2250525e-02	-6.5000000e+02	5.5825000e+00	
4.5978252e+01	-1.2250525e-02	-2.6500000e+03	5.9350000e+00	
4.5978252e+01	-1.2250525e-02	-4.6500000e+03	6.0075000e+00	

whose coordinates are Lat/Long/Altitude/Velocity in meters. So we set:

```
Murat.input.availableVelocity      = 1;
Murat.input.namev                 = 'modvMSH.txt';
```

Even if we set the velocity model we still need the average crustal velocities if you have no info of origin time. It is highly recommended you have the origin in the header, at variables '**o**'!

```
Murat.input.averageVelocityP     = 6;
Murat.input.averageVelocityS     = 3;
```

INVERSION

The code implements either a standard Tikhonov inversion based on singular value decomposition (**'Tikhonov'**) and an iterative conjugate gradient least square inversion minimizing both model norm and Laplacian (**'Iterative'**). For the first, we rely on the [regtools Matlab suite](#) from Per Christian Hansen. The second uses the [IR TOOLS for iterative regularization](#). Copies of both packages are linked to MURAT3:

```
Murat.input.inversionMethod      = 'Iterative';
```

As you need to select the damping you can choose to output the L curves between residual and norm length ([Aster et al. 2013](#) - case **'Tikhonov'**) or the cost functions (case **'Iterative'**). Set either **1** or **0**. In the latter case, set the damping for both Qc and Q inversions. You will likely test many different damping parameters and likely want to avoid seeing the same figure again, so you can just declare the damping for Qc and Q after looking at the figures. Remember doing it for each frequency.

```
Murat.input.lCurve              = 0;
Murat.input.lCurveQc             = [0.1 0.1 0.05 0.02];
Murat.input.lCurveQ              = [1 1 0.5 0.2];
```

A great reference for the best sort of testing is [Rawlinson & Spakman, 2016](#). If you want to test your results you need to create a checkerboard. The size of the checks can be twice (2) or four times (4) node spacing:

```
Murat.input.sizeCheck           = 2;
```

with each cell having alternating values of attenuation:

```
Murat.input.highCheck      = 0.02;  
Murat.input.lowCheck      = 0.001;
```

In MuRAT3D you can also set the origin and end locations of a spike as well as its attenuation value:

```
Murat.input.spikeLocationOrigin = [46.05 -122.40 0];  
Murat.input.spikeLocationEnd   = [46.12 -122.30 -6000];  
Murat.input.spikeValue        = 0.02;
```

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