

# PLY-THICKNESS EFFECT ON FIBER-MATRIX INTERFACE CRACK GROWTH

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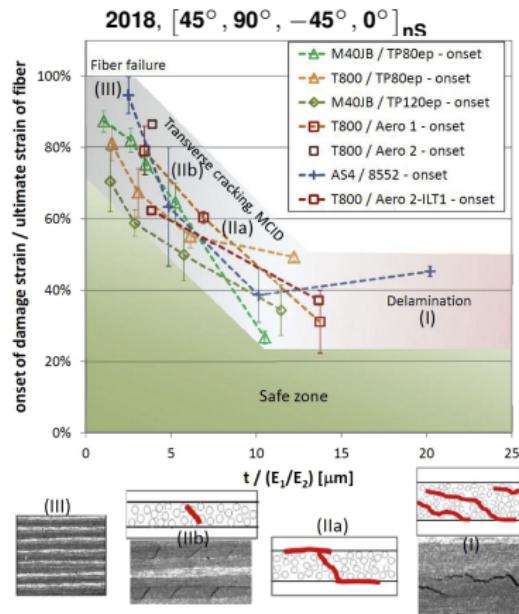
## Outline

- ➔ Initiation of Transverse Cracks in Thin-plies
- ➔ Modeling the Fiber-Matrix Interface Crack
- ➔ Debond Energy Release Rate
- ➔ Conclusions



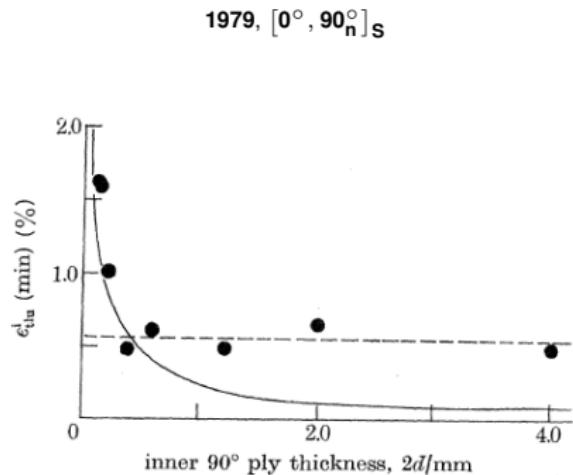
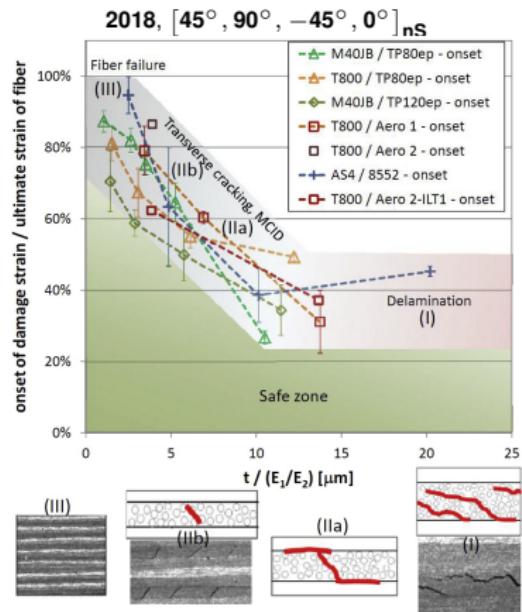
# INITIATION OF TRANSVERSE CRACKS IN THIN-PLIES

## The Thin-ply "Advantage": new material



Cugnoni et al., Compos. Sci. Technol. **168**, 2018.

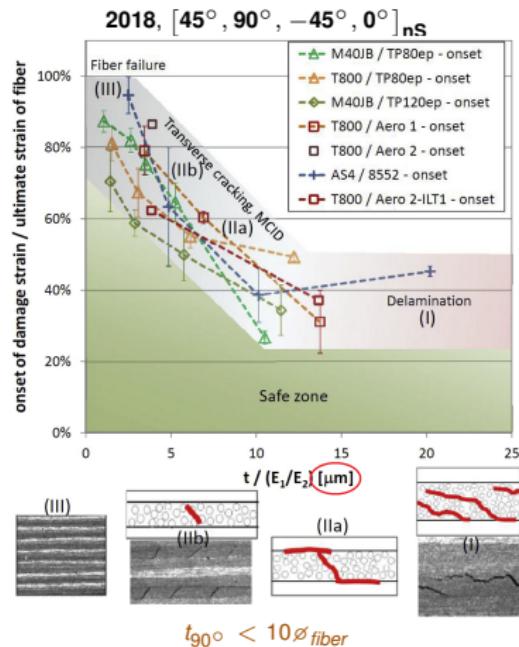
## The Thin-ply "Advantage": new material, old result



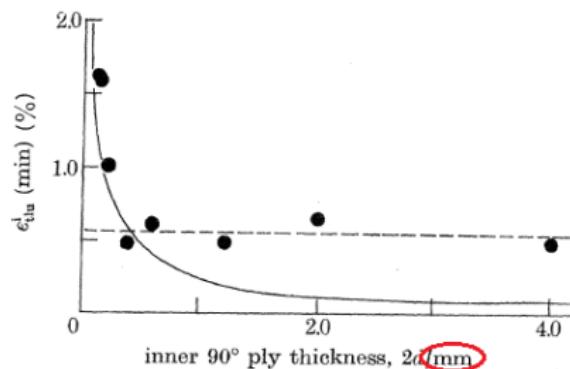
Cugnoni et al., Compos. Sci. Technol. **168**, 2018.

Bailey et al., P. Roy. Soc. A-Math. Phys. **366** (1727), 1979.

## The Thin-ply "Advantage": new material, old result?



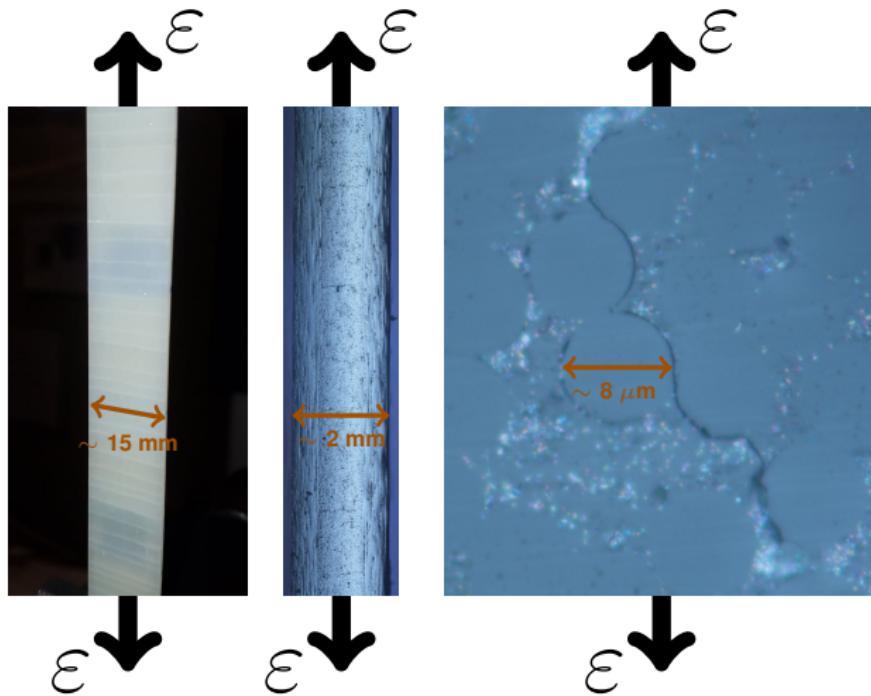
Cugnoni et al., Compos. Sci. Technol. **168**, 2018.



$t_{90^\circ} > 100 \varnothing_{fiber}$

Bailey et al., P. Roy. Soc. A-Math. Phys. **366** (1727), 1979.

## Micromechanics of Initiation



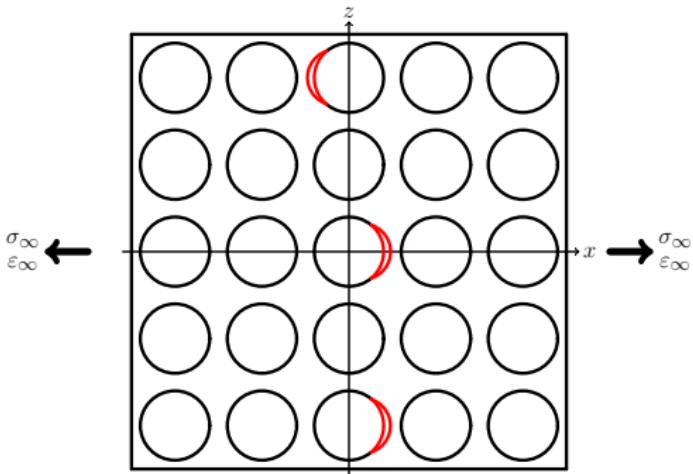
**Left:**  
front view of [0, 90]<sub>S</sub>,  
visual inspection.

**Center:**  
edge view of [0, 90]<sub>S</sub>,  
optical microscope.

**Right:**  
edge view of [0, 90]<sub>S</sub>,  
optical microscope.

## Micromechanics of Initiation

### Stage 1: isolated debonds



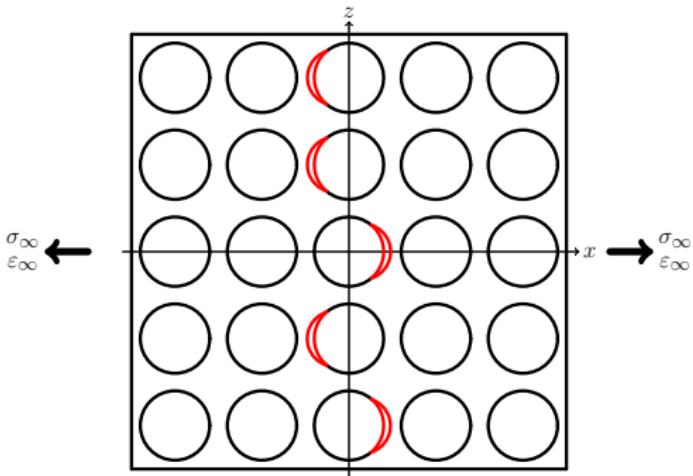
Bailey et al., P. Roy. Soc. A-Math. Phy. **366** (1727), 1979.

Bailey et al., J. Mater. Sci. **16** (3), 1981.

Zhang et al., Compos. Part A-Appl. S. **28** (4), 1997.

## Micromechanics of Initiation

### Stage 2: consecutive debonds



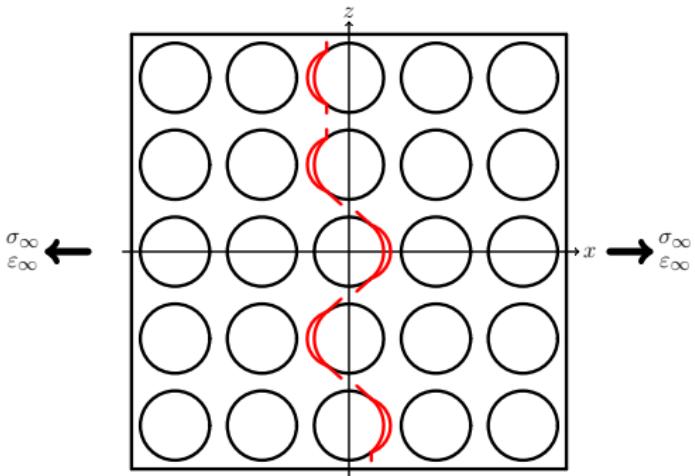
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Bailey et al., J. Mater. Sci. **16** (3), 1981.

Zhang et al., Compos. Part A-Appl. S. **28** (4), 1997.

## Micromechanics of Initiation

### Stage 3: kinking



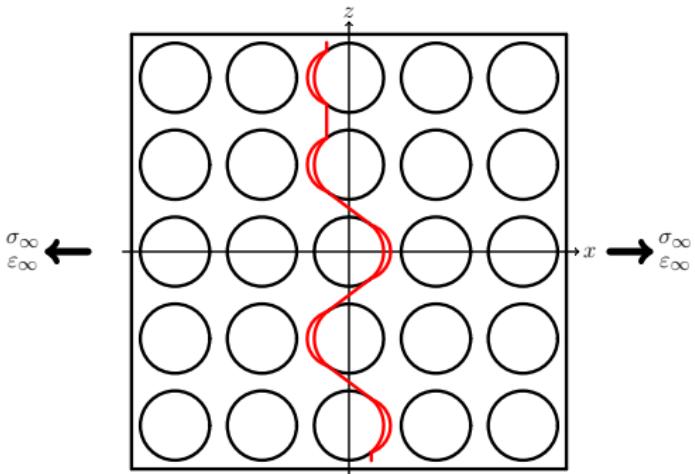
Bailey et al., P. Roy. Soc. A-Math. Phy. **366** (1727), 1979.

Bailey et al., J. Mater. Sci. **16** (3), 1981.

Zhang et al., Compos. Part A-Appl. S. **28** (4), 1997.

## Micromechanics of Initiation

### Stage 4: coalescence

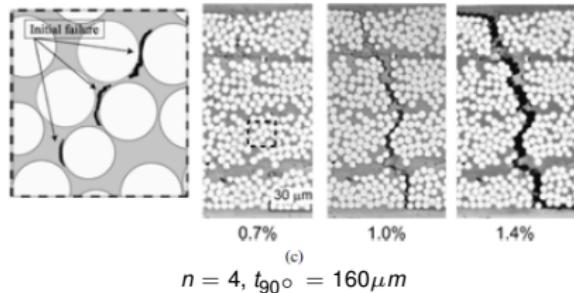


Bailey et al., P. Roy. Soc. A-Math. Phy. **366** (1727), 1979.

Bailey et al., J. Mater. Sci. **16** (3), 1981.

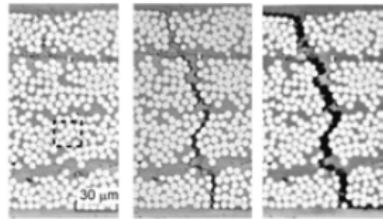
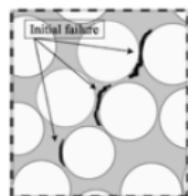
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## A Counter-intuitive Observation

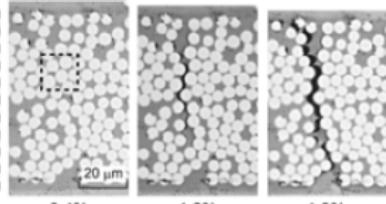
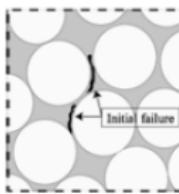
 $[0^\circ, 90_n^\circ]_S$ 

## A Counter-intuitive Observation

$[0^\circ, 90_n^\circ]_S$



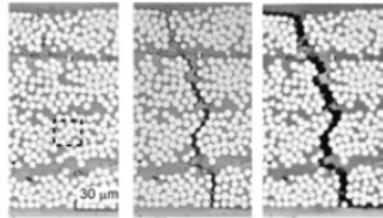
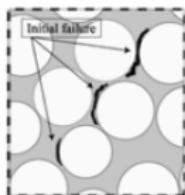
$$n = 4, t_{90^\circ} = 160 \mu m$$



$$n = 2, t_{90^\circ} = 80 \mu m$$

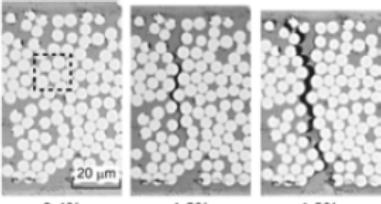
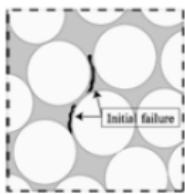
## A Counter-intuitive Observation

$[0^\circ, 90_n^\circ]_S$



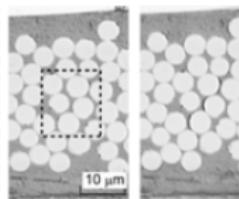
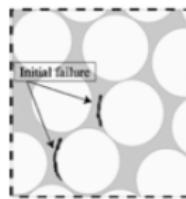
$$n = 4, t_{90^\circ} = 160 \mu m$$

(c)



$$n = 2, t_{90^\circ} = 80 \mu m$$

(b)



(a)

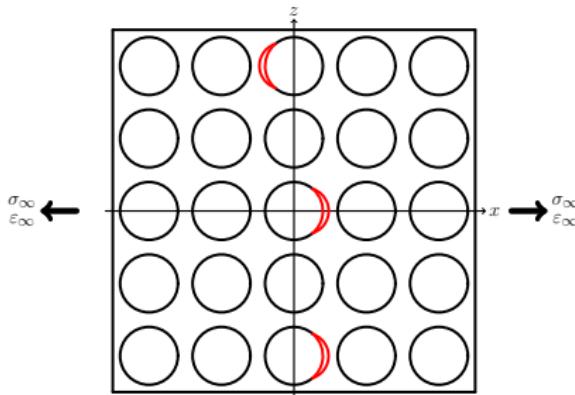
$$n = 1, t_{90^\circ} = 40 \mu m$$

Saito et al., Adv. Compos. Mater. 21 (1), 2012.

## Objective of the Study

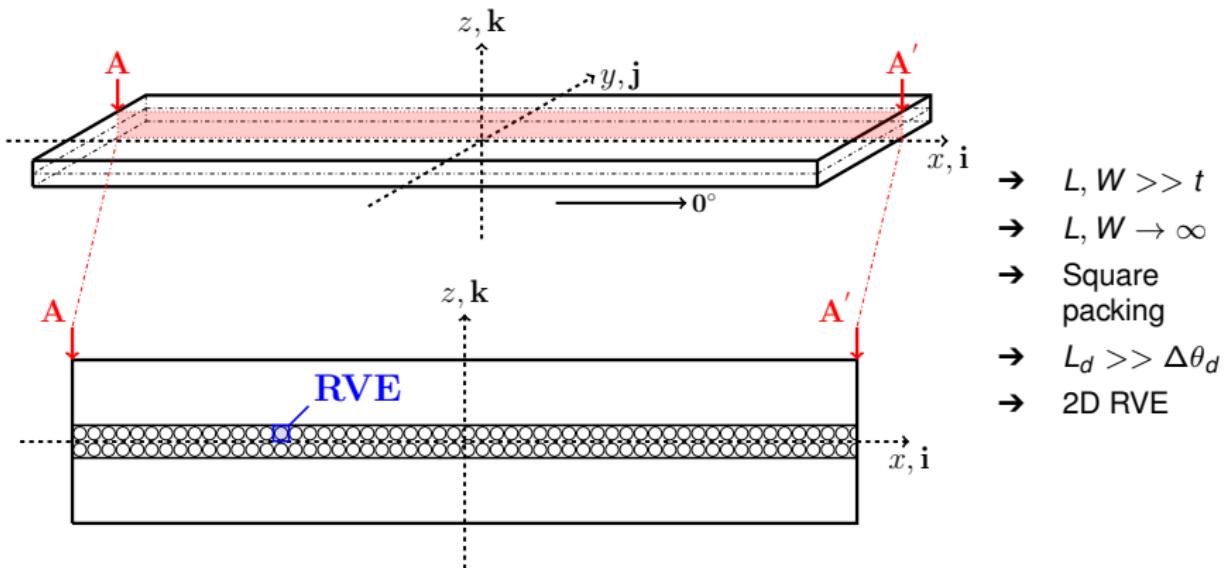
Can we talk about a ply-thickness effect for the fiber-matrix interface crack?

### Stage 1: isolated debonds

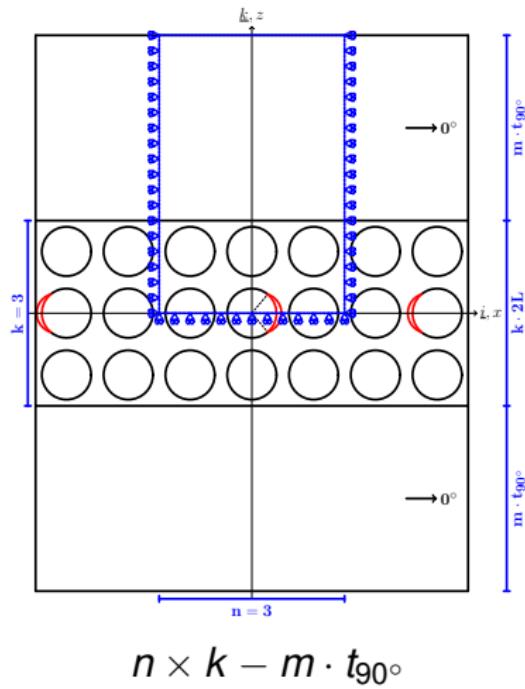
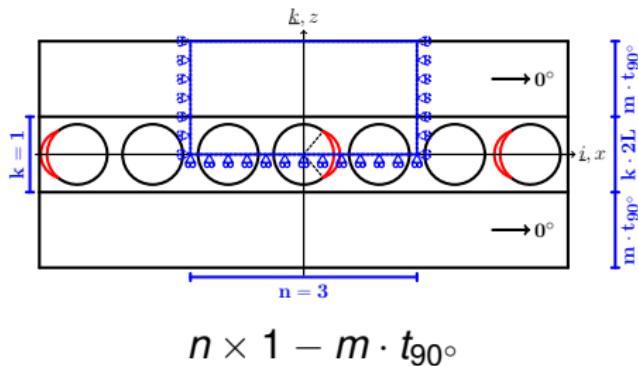


# **MODELING THE FIBER-MATRIX INTERFACE CRACK**

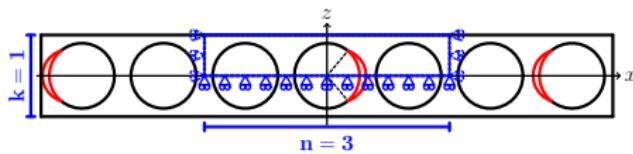
## Geometry



## Representative Volume Elements



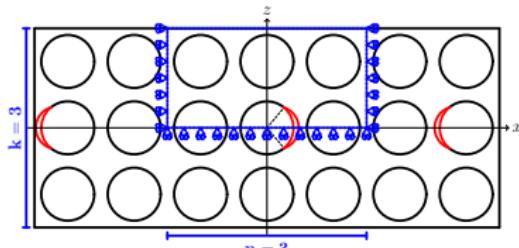
## Representative Volume Elements



— free

$n \times 1$  — coupling

— coupling +  $H$

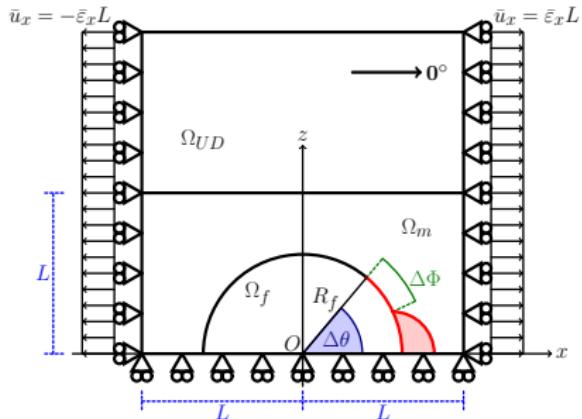


— free

$n \times k$  — coupling

— coupling +  $H$

## Assumptions

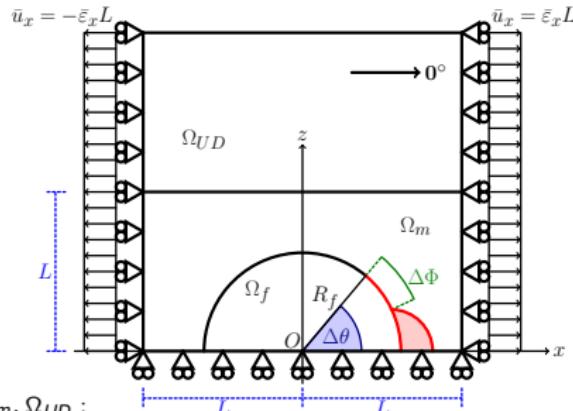


$$R_f = 1 \text{ } [\mu\text{m}] \quad L = \frac{R_f}{2} \sqrt{\frac{\pi}{V_f}}$$

- Linear elastic, homogeneous materials
- Concentric Cylinders Assembly with Self-Consistent Shear Model for UD
- Plane strain
- Frictionless contact interaction
- Symmetric w.r.t. x-axis
- Coupling of x-displacements on left and right side (repeating unit cell)
- Applied uniaxial tensile strain  $\bar{\varepsilon}_x = 1\%$
- $V_f = 60\%$

Material	$V_f$ [%]	$E_L$ [GPa]	$E_T$ [GPa]	$\mu_{LT}$ [GPa]	$\nu_{LT}$ [-]	$\nu_{TT}$ [-]
Glass fiber	-	70.0	70.0	29.2	0.2	0.2
Epoxy	-	3.5	3.5	1.25	0.4	0.4
UD	60.0	43.442	13.714	4.315	0.273	0.465

## Solution



in  $\Omega_f, \Omega_m, \Omega_{UD}$  :

$$\frac{\partial^2 \varepsilon_{xx}}{\partial z^2} + \frac{\partial^2 \varepsilon_{zz}}{\partial x^2} = \frac{\partial^2 \gamma_{zx}}{\partial x \partial z} \quad \text{for } 0^\circ \leq \alpha \leq \Delta\theta : \\ (\vec{u}_m(R_f, \alpha) - \vec{u}_f(R_f, \alpha)) \cdot \vec{n}_\alpha \geq 0$$

$$\varepsilon_y = \gamma_{xy} = \gamma_{yz} = 0 \quad \text{for } \Delta\theta \leq \alpha \leq 180^\circ :$$

$$\frac{\partial \sigma_{xx}}{\partial x} + \frac{\partial \tau_{zx}}{\partial z} = 0 \quad \vec{u}_m(R_f, \alpha) - \vec{u}_f(R_f, \alpha) = 0$$

$$\frac{\partial \tau_{zx}}{\partial x} + \frac{\partial \sigma_{zz}}{\partial z} = 0 \quad \sigma_{ij} = E_{ijkl} \varepsilon_{kl}$$

$$\sigma_{yy} = \nu (\sigma_{xx} + \sigma_{zz})$$

→ Oscillating singularity

$$\sigma \sim r^{-\frac{1}{2}} \sin(\varepsilon \log r), \quad V_f \rightarrow 0$$

$$\varepsilon = \frac{1}{2\pi} \log \left( \frac{1-\beta}{1+\beta} \right)$$

$$\beta = \frac{\mu_2 (\kappa_1 - 1) - \mu_1 (\kappa_2 - 1)}{\mu_2 (\kappa_1 + 1) + \mu_1 (\kappa_2 + 1)}$$

$$\rightarrow G = \frac{\partial W}{\partial A} - \left( \frac{\partial U}{\partial A} + \frac{\partial E_k}{\partial A} \right)$$

→ Finite Element Method (FEM)  
in Abaqus™

→ 2<sup>nd</sup> order shape functions

→ 6-nodes triangles & 8-nodes quadrilaterals

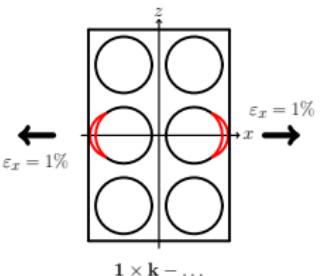
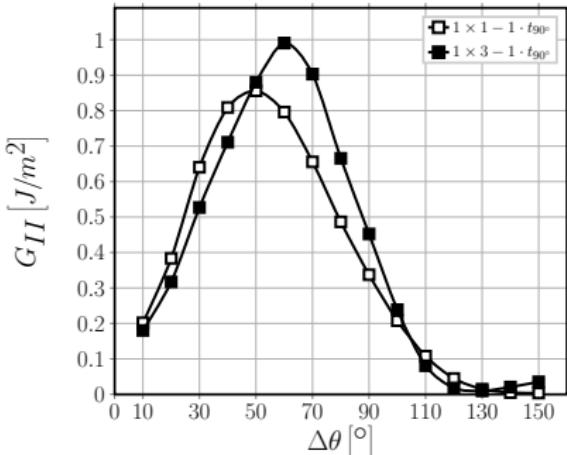
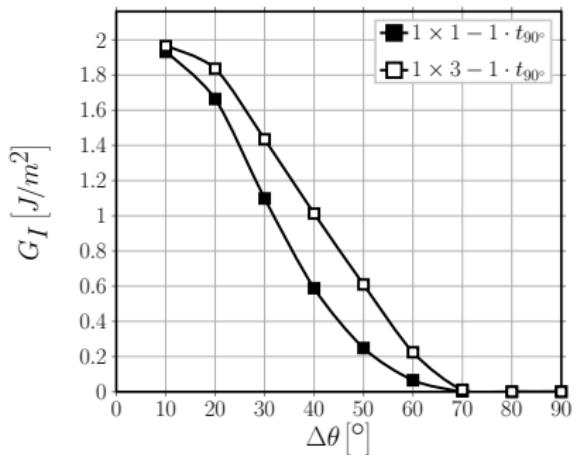
→ regular mesh of quadrilaterals  
at the crack tip:

- $AR \sim 1$
- $\delta = 0.05^\circ$

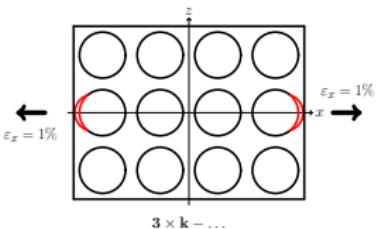
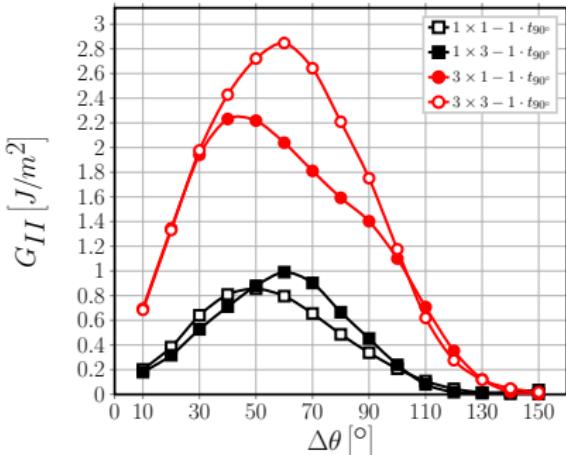
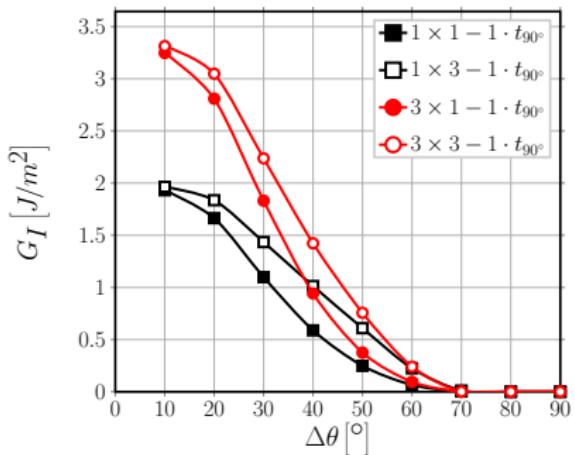
Initiation of Transverse Cracks in Thin-plies   Modeling the Fiber-Matrix Interface Crack   Debond Energy Release Rate   Conclusions  
Interaction of Debonds   Effect of 0° ply thickness   Effect of 90° ply thickness

## DEBOND ENERGY RELEASE RATE

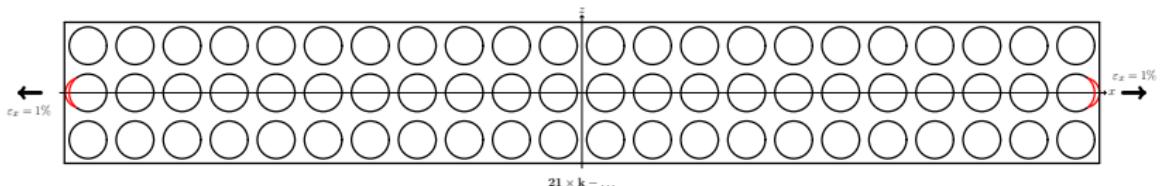
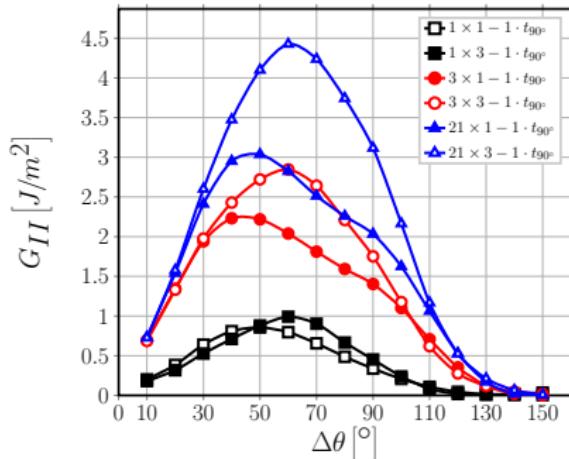
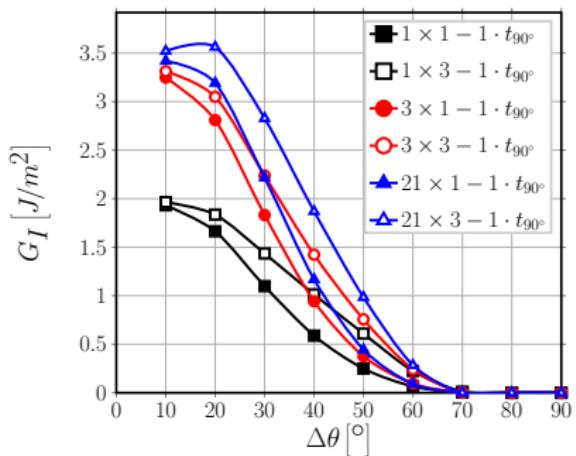
## Interaction of Debonds: Strain Magnification



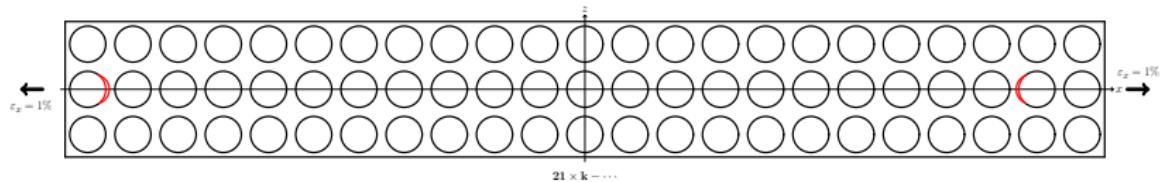
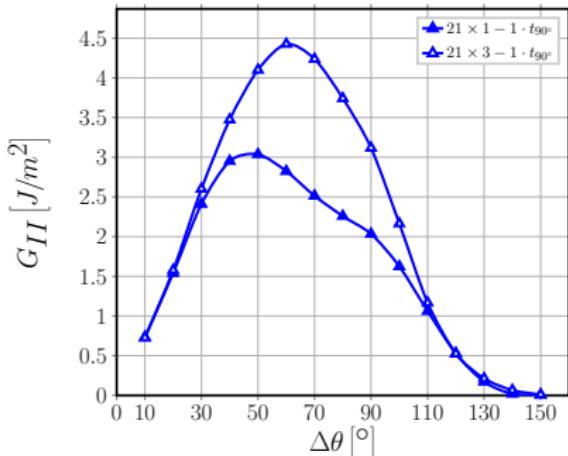
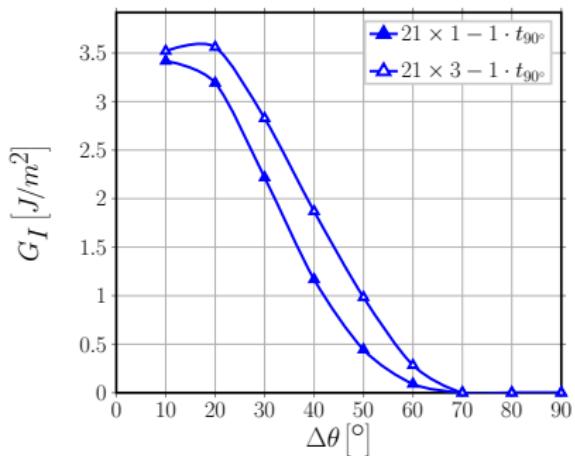
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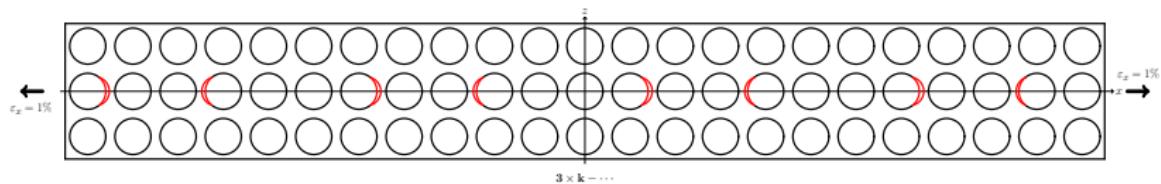
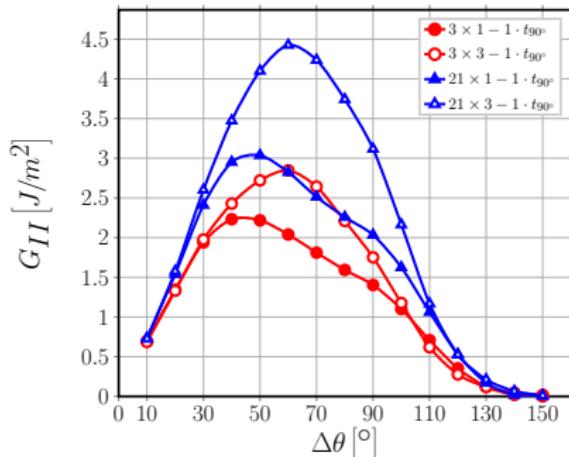
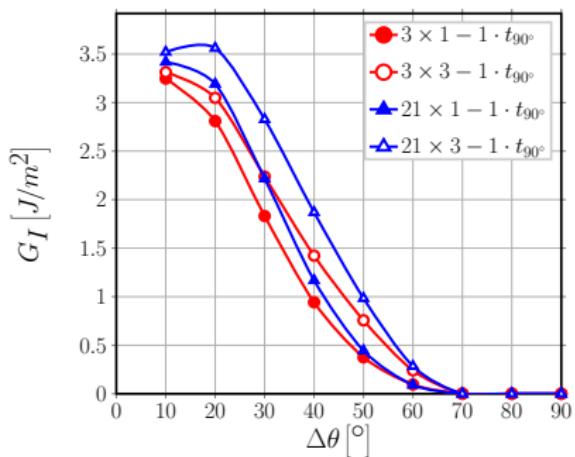
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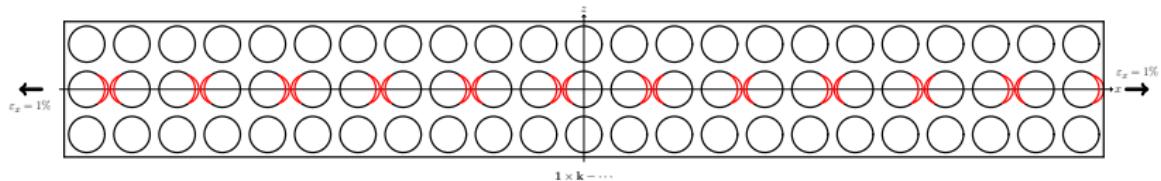
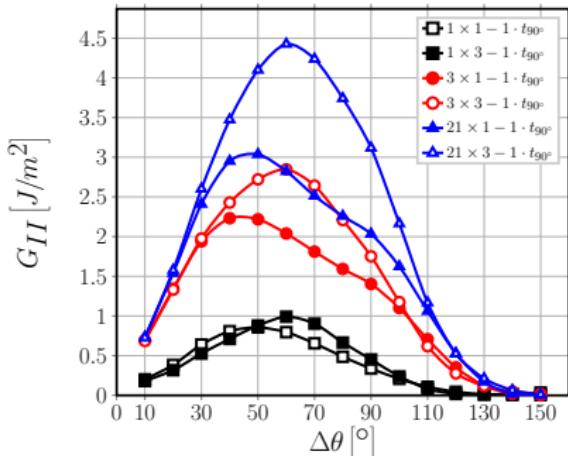
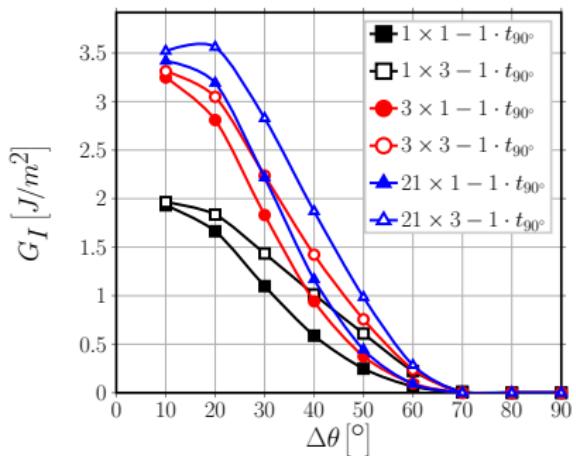
## Interaction of Debonds: Crack Shielding



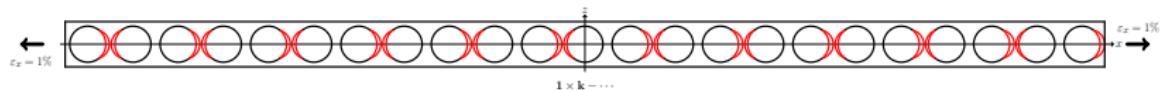
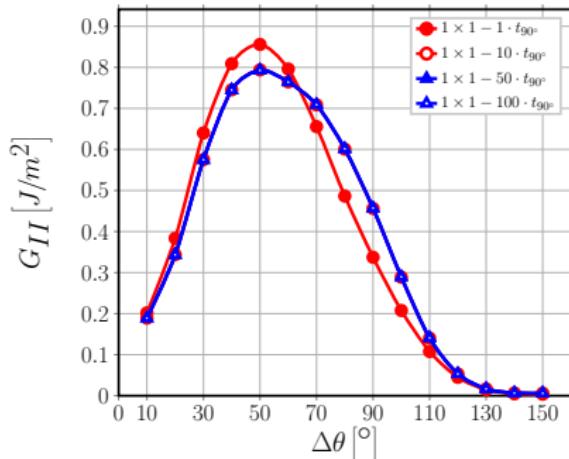
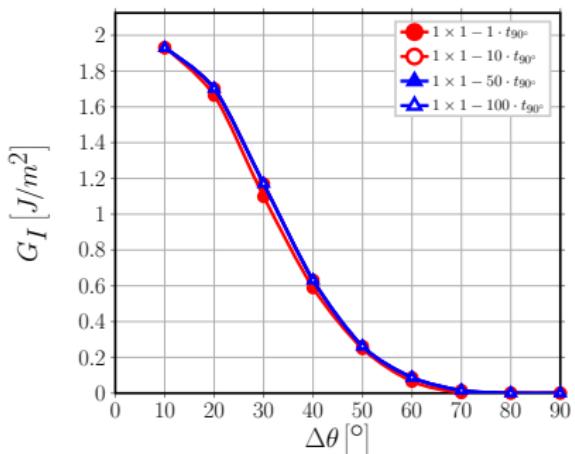
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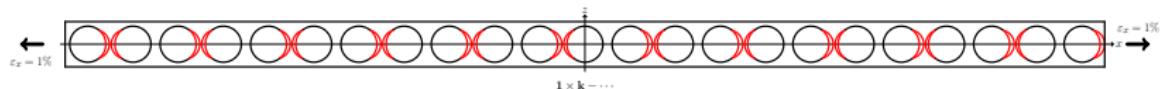
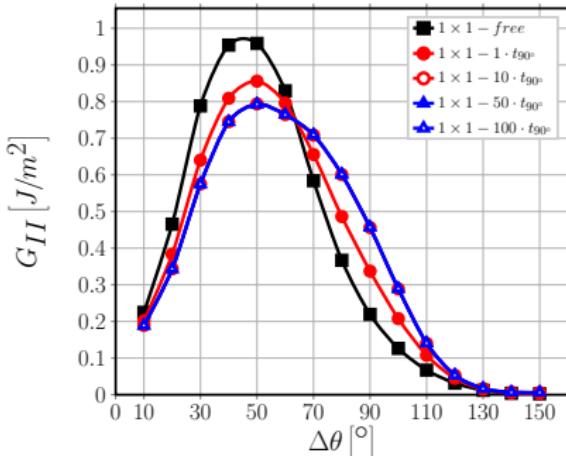
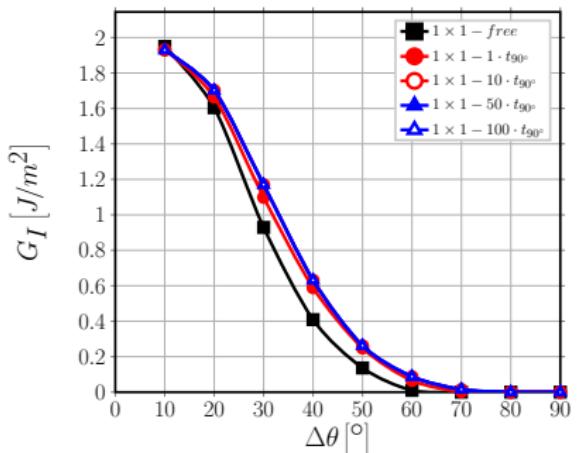
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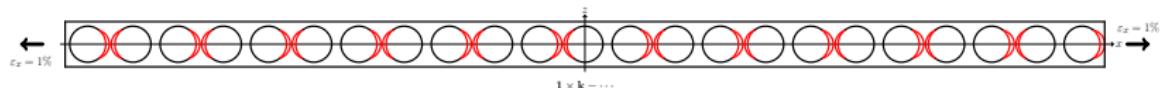
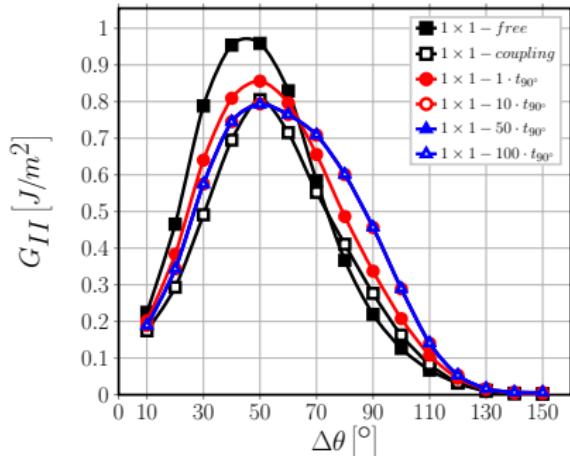
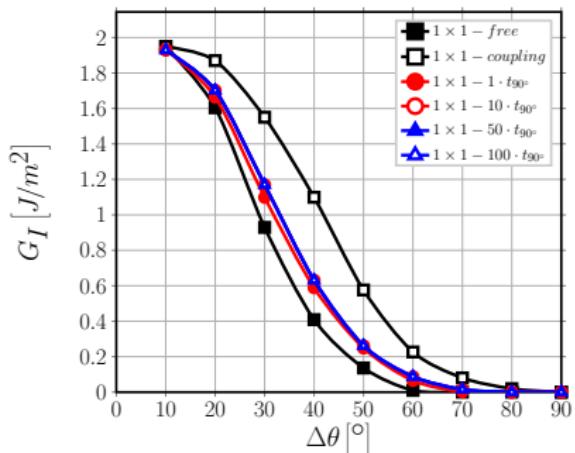
## Effect of $0^\circ$ ply thickness



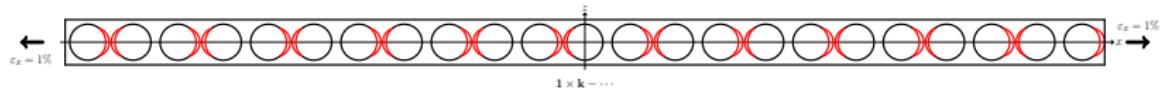
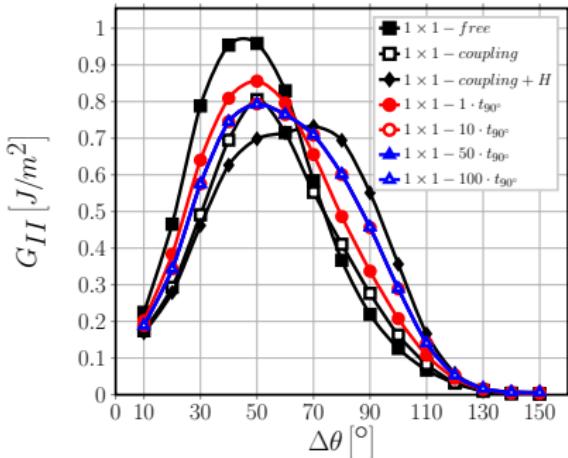
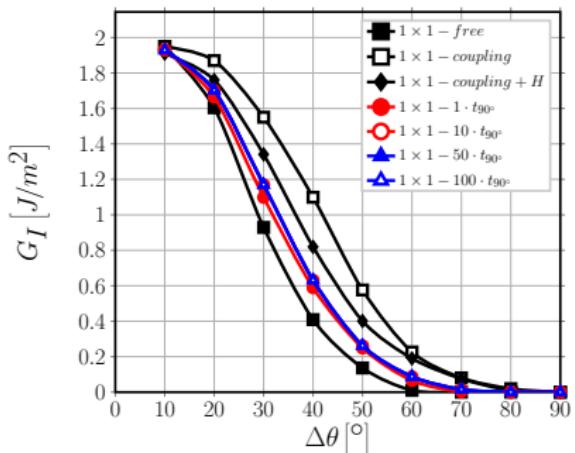
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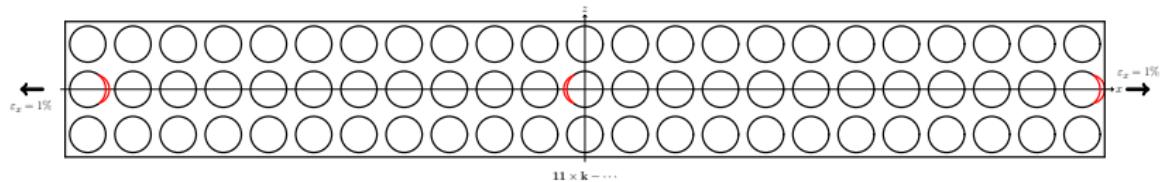
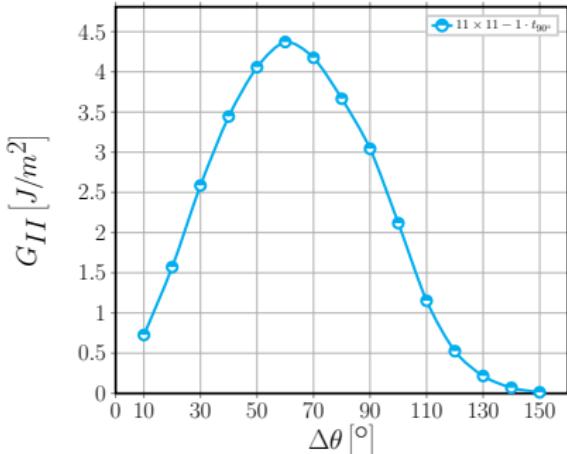
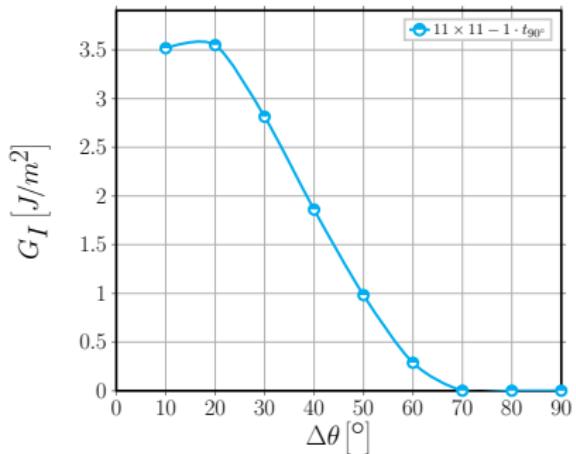
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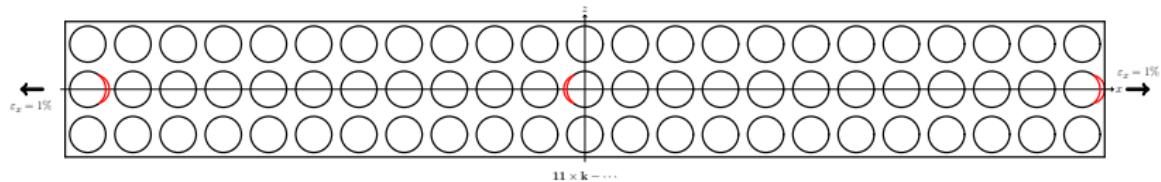
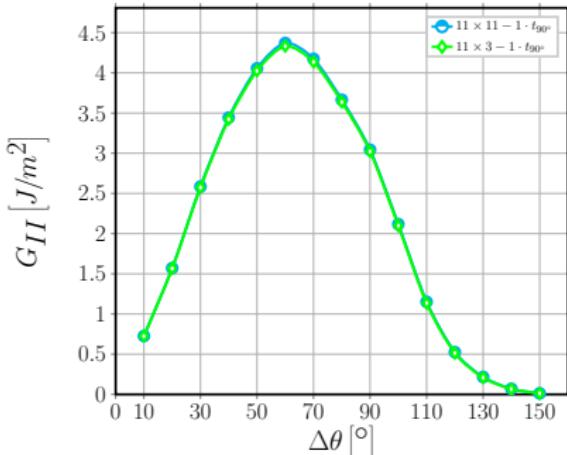
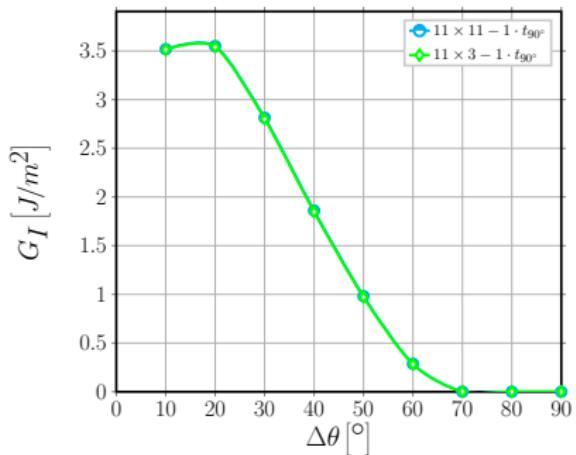
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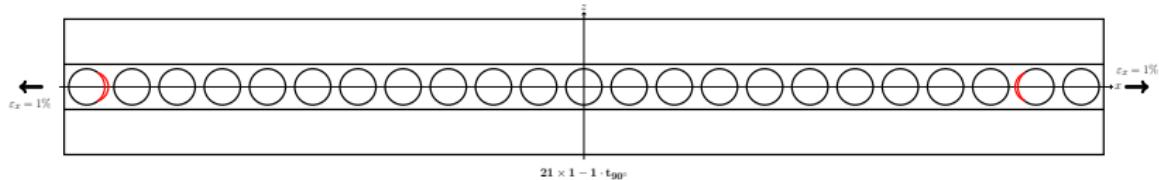
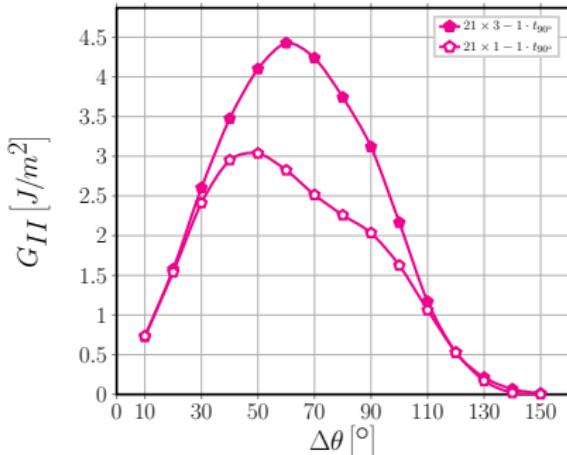
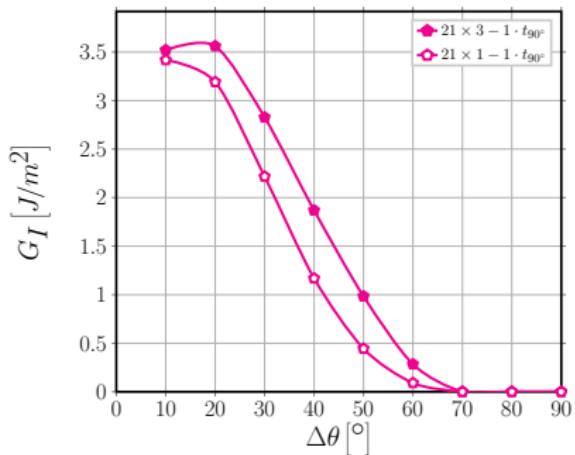
## Effect of 90° ply thickness



## Effect of 90° ply thickness



## Effect of 90° ply thickness



## CONCLUSIONS

## Conclusions

- No effect of  $90^\circ$  ply thickness can be observed when  $t_{90^\circ}$  is at least  $\sim 3\varnothing_{fiber}$
- Only if  $t_{90^\circ}$  is reduced to  $1\varnothing_{fiber}$ , ERR is reduced for a given level of applied strain, i.e. debond growth is delayed to higher levels of applied strain ( $G \sim \varepsilon_{applied}^2$ )
- No effect of  $0^\circ$  ply thickness can be observed when  $t_{0^\circ}/t_{90^\circ} > 1$
- A small difference can be observed when  $t_{0^\circ} = t_{90^\circ}$ , due to the smaller bending stiffness of a thinner  $0^\circ$  layer



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Education and Culture

Erasmus Mundus