

Cryptography Basics

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Cryptography is a handy tool in information security, being the basis of many security mechanisms that offer services such as:

1. confidentiality;
2. integrity;
3. authentication;
4. non-repudiation.

However:

- Cryptography is not the solution to all security problems!
- If not properly implemented, cryptographic tools may leak information very subtly without you realizing it!

Cryptographic technologies

There are two main classes of cryptographic constructions:

1. Based on **symmetric** (**secret**) **keys**.

Rough meaning: use the same secret key to encrypt and also decrypt;

2. Based of **asymmetric** (**public**) **keys**. An asymmetric key is a pair (pk, sk) consisting of a public key pk and a private key sk .

Rough meaning: use the public key to encrypt and the private key to decrypt.

Symmetric key technology usually requires a key distribution mechanism!

Proving security in cryptography

Two main approaches to proving security:

1. Trying to find an attack, such as: brute-force, man-in-the-middle, meet-in-the-middle, frequency analysis, replay, birthday, dictionary etc. attack. Then:
 - Attack found \Rightarrow system insecure;
 - Attack not found \Rightarrow ???
2. Trying to prove that the scheme is secure (**provable security**). Two milestones along this approach:
 - 2.1 **Perfect security** (Shannon (1949));
 - 2.2 **Computational security** (Goldwasser and Micali (1984)).

Perfect security



Claude Shannon: "The father of Information Theory"

C. Shannon. Communication Theory of Secrecy Systems, Bell System Technical J., vol. 28, no. 4, 1949, pp. 656–715.

Perfect security or **unconditional security** or **information-theoretic security** means that the ciphertext reveals no information about the plaintext to an adversary with unlimited power.



Shafira Goldwasser: Gödel Prize (1993, 2001),
Turing Award (2012)



Silvio Micali: Gödel Prize (1993), Turing Award
(2012)

Semantic security: an adaptation of Shannon's perfect security to the computational setting, considering only adversaries having bounded computational resources.

Provable security

Provable security also known as reductionist security: security can be proven by reduction to well-studied (hard) problems.

Provable security entails:

- A security model \mathcal{S} for the cryptographic scheme, consisting of:
 1. Security goal, such as semantic security (SS), indistinguishability (IND), non-maleability (NM), collision resistance, non-forgery etc.;
 2. Attack model, such as chosen plaintext attack (CPA) or chosen ciphertext attack (CCA1 and CCA2);
- A problem together with a hardness assumption \mathcal{H} about it;
- A reductionist proof: $\mathcal{H} \leq \mathcal{S}$.

Many of the ciphers used today in practice are not proven secure nor known attack methods against them!

References

- Goldwasser, S. and Micali, S. (1984). Probabilistic encryption. *Journal of Computer and System Sciences*, 28:270–299.
- Shannon, C. E. (1949). Communication theory of secrecy systems. *The Bell System Technical Journal*, 28(4):656–715.