

Graphs

Topological sort

```
// Tri topologique
// O(|E|)
namespace Toposort {
    vector<bool> seen;
    vector<int> order;

    void dfs(const vector<vector<int>>& adj, int u) {
        seen[u] = true;
        for (int v: adj[u])
            if (!seen[v])
                dfs(adj, v);
        order.push_back(u);
    }

    vector<int> make(const vector<vector<int>> adj) {
        int n = (int)adj.size();
        seen = vector<bool>(n);
        order = vector<int>(0);
        for (int u = 0; u < n; ++u)
            if (!seen[u])
                dfs(adj, u);
        reverse(order.begin(), order.end());
        return order;
    }
};
```

Strongly connected components

```
// CFC
// O(|E|)
struct SCC {
    // scc[u] : CFC du noeud u
    vector<int> scc;
    // sccadj[i] : liste d'adjacence de la i-eme CFC
    vector<vector<int>> sccgraph;
    int nb_scc;

    vector<bool> seen;
    vector<vector<int>> adj;
    vector<vector<int>> adjt;

    void mark_scc(int u, int idscc) {
        scc[u] = idscc;
        seen[u] = true;
        for (int v: adjt[u])
            if (!seen[v])
                mark_scc(v, idscc);
    }

    void create_scc_graph(int u) {
        seen[u] = true;
        for (int v: adj[u]) {
            if (scc[v] != scc[u])
```

```
        sccgraph[scc[u]].push_back(scc[v]);
        if (!seen[v])
            create_scc_graph(v);
    }
}

SCC(vector<vector<int>> adj) {
    int n = (int)adj.size();
    this->adj = adj;
    adjt = vector<vector<int>>(n, vector<int>(0));
    for (int u = 0; u < n; ++u)
        for (int v: adj[u])
            adjt[v].push_back(u);

    vector<int> order = Toposort::make(adj);
    scc = vector<int>(n);
    nb_scc = 0;
    seen = vector<bool>(n);
    for (int t = n - 1; t >= 0; --t) {
        int u = order[t];
        if (!seen[u])
            mark_scc(u, nb_scc++);
    }

    // (optionnel) construction du DAG des CFC
    sccgraph = vector<vector<int>>(nb_scc, vector<int>(0));
    fill(seen.begin(), seen.end(), false);
    for (int u = 0; u < n; ++u)
        if (!seen[u])
            create_scc_graph(u);
    }
};
```

2-SAT

```
// 2-SAT
// O(n + m)
struct SAT2 {
    vector<bool> values;
    bool is_satisfiable;

    vector<int> order;
    vector<vector<int>> adj;
    int timer;

    // Formule a satisfaire :
    // (maxterms[0].fst ou maxterms[0].snd) et
    // (maxterms[1].fst ou maxterms[1].snd) et
    // ...
    // (maxterms[p].fst ou maxterms[p].snd)
    // littéral ::= 2*x pour x
    //                2*x+1 pour non(x)
    // 0 <= minterms[0].fst/snd < 2*m
    SAT2(vector<pair<int, int>> maxterms, int m) {
        int n = (int)maxterms.size();
        adj = vector<vector<int>>(2 * m, vector<int>(0));
```

```

    for (int i = 0; i < n; ++i) {
        adj[maxterms[i].first ^ 1].push_back(maxterms[i].second);
        adj[maxterms[i].second ^ 1].push_back(maxterms[i].first);
    }

    SCC scc(adj);
    is_satisfiable = true;
    for (int u = 0; u < 2 * m; u += 2)
        if (scc.scc[u] == scc.scc[u + 1])
            is_satisfiable = false;

    if (is_satisfiable) {
        values = vector<bool>(m);
        for (int u = 0; u < m; ++u)
            values[u] = scc.scc[2 * u] > scc.scc[2 * u + 1];
    }
};

```

Hopcroft-Karp

```

// Nombre max de noeuds
const int MAXN = 50 * 1000;
// assert(INF > MAXN)
const int INF = 1000 * 1000 * 1000;

// Hopcroft-Karp
// Max cardinality matching en O(|E| sqrt(|V|))
struct HopcroftKarp {
    const int NIL = MAXN;
    vector<int> adj[MAXN + 1];
    int pairu[MAXN + 1];
    int pairv[MAXN + 1];
    int dist[MAXN + 1];
    int nl, nr;

    HopcroftKarp() {}
    // nl : #noeuds a gauche
    // nr : #noeuds a droite
    HopcroftKarp(int nl, int nr) : nl(nl), nr(nr) {}

    void add_edge(int u, int v) {
        adj[u].push_back(v);
    }

    bool bfs() {
        queue<int> q;

        for (int u = 0; u < nl; ++u) {
            if (pairu[u] == NIL) {
                dist[u] = 0;
                q.push(u);
            } else {
                dist[u] = INF;
            }
        }
    }

```

```

        dist[NIL] = INF;
        while (!q.empty()) {
            int u = q.front();
            q.pop();

            if (dist[u] >= dist[NIL])
                continue;

            for (int v: adj[u]) {
                if (dist[pairv[v]] != INF) continue;
                dist[pairv[v]] = dist[u] + 1;
                q.push(pairv[v]);
            }
        }

        return dist[NIL] != INF;
    }

    bool dfs(int u) {
        if (u == NIL)
            return true;

        for (int v: adj[u]) {
            if (dist[pairv[v]] == dist[u] + 1 && dfs(pairv[v])) {
                pairv[v] = u;
                pairu[u] = v;
                return true;
            }
        }

        dist[u] = INF;
        return false;
    }

    int maxmatching() {
        fill(pairu, pairu + nl, NIL);
        fill(pairv, pairv + nr, NIL);
        int ans = 0;
        while (bfs())
            for (int u = 0; u < nl; ++u)
                if (pairu[u] == NIL && dfs(u))
                    ++ans;
        return ans;
    }
};

```

Hungarian algorithm

```

// Inspire de http://e-maxx.ru/algo/assignment_hungary
// Algorithme hongrois
// Matching parfait de poids min
// Complexite : O(nm)
// Applications :
// - Max matching min weight
// - Max matching max weight (poids < 0)
// - Decomposer un DAG en un nombre min de chemins disjoints
// - Coloriage d'un arbre k-aire avec k couleurs, le coloriage de chaque noeud

```

```
// par une certaine couleur a un certain cout -> trouver un coloriage de cout
// min (dp[v][c] = cout min de colorier le sous-arbre en v sachant c(v) = c)
// - Etant donnee une matrice a[1..n][1..m], trouver deux tableaux u[1..n] et
// v[1..m] tq pour tout i,j : u[i] + v[j] <= a[i][j] et la somme des elements
// de u et v est max.
```

```
struct Hungarian {
    // p[i] = si 1 <= i <= m, vaut le noeud matche avec i (entre 1 et n)
    // vaut 0 si non matche
    vector<int> p;
```

```
// a doit etre de taille (n + 1) x (m + 1), avec n <= m
```

```
Hungarian(vector<vector<double>> a, int n, int m) {
```

```
    vector<double> u(n + 1), v(m + 1);
```

```
    vector<int> way(m + 1);
```

```
    p = vector<int>(m + 1);
```

```
    for (int i = 1; i <= n; ++i) {
```

```
        p[0] = i;
```

```
        int j0 = 0;
```

```
        vector<double> minv(m + 1, INF);
```

```
        vector<bool> used(m + 1, false);
```

```
        do {
```

```
            used[j0] = true;
```

```
            int i0 = p[j0], j1;
```

```
            double delta = LLINF;
```

```
            for (int j = 1; j <= m; ++j)
```

```
                if (!used[j]) {
```

```
                    double cur = a[i0][j] - u[i0] - v[j];
```

```
                    if (cur < minv[j]) {
```

```
                        minv[j] = cur;
```

```
                        way[j] = j0;
```

```
                    }
```

```
                    if (minv[j] < delta) {
```

```
                        delta = minv[j];
```

```
                        j1 = j;
```

```
                    }
```

```
                }
```

```
            for (int j = 0; j <= m; ++j)
```

```
                if (used[j]) {
```

```
                    u[p[j]] += delta;
```

```
                    v[j] -= delta;
```

```
                } else {
```

```
                    minv[j] -= delta;
```

```
                }
```

```
            j0 = j1;
```

```
        } while (p[j0] != 0);
```

```
        do {
```

```
            int j1 = way[j0];
```

```
            p[j0] = p[j1];
```

```
            j0 = j1;
```

```
        } while (j0 != 0);
```

```
    }
```

```
};
```

Dinic

```
// Nombre max de noeuds
```

```
const int MAXN = 10 * 1000;
```

```
// assert(INF > maxflow)
```

```
const ll INF = 1ll << 53;
```

```
// Dinic
```

```
// Flot max en  $O(V^2 * E)$ 
```

```
struct Dinic {
```

```
    struct Edge { int u, v; ll cap, flow; };
```

```
    vector<int> adj[MAXN];
```

```
    vector<Edge> edges;
```

```
    int dist[MAXN];
```

```
    int idnext[MAXN];
```

```
    int n;
```

```
Dinic() {}
```

```
Dinic(int n) : n(n) {}
```

```
// ajoute l'arete u -> v de capacite c
```

```
void add_edge(int u, int v, int c) {
```

```
    edges.push_back({u, v, c, 0});
```

```
    adj[u].push_back((int)edges.size() - 1);
```

```
    edges.push_back({v, u, 0, 0});
```

```
    adj[v].push_back((int)edges.size() - 1);
```

```
}
```

```
bool bfs(int s, int t) {
```

```
    queue<int> q;
```

```
    fill(dist, dist + n, -1);
```

```
    dist[s] = 0;
```

```
    q.push(s);
```

```
    while (!q.empty()) {
```

```
        int u = q.front();
```

```
        q.pop();
```

```
        for (int e: adj[u]) {
```

```
            int v = edges[e].v;
```

```
            if (dist[v] == -1 && edges[e].flow < edges[e].cap) {
```

```
                dist[v] = dist[u] + 1;
```

```
                q.push(v);
```

```
            }
```

```
        }
```

```
    }
```

```
    return dist[t] != -1;
```

```
}
```

```
int dfs(int u, int t, ll flow) {
```

```
    if (flow == 0) return 0;
```

```
    if (u == t) return flow;
```

```
    for (; idnext[u] < (int)adj[u].size(); ++idnext[u]) {
```

```
        int e = adj[u][idnext[u]];
```

```
        int v = edges[e].v;
```

```
        if (dist[v] != dist[u] + 1) continue;
```

```

    ll pushed = dfs(v, t, min(flow, edges[e].cap - edges[e].flow));
    if (pushed > 0) {
        edges[e].flow += pushed;
        edges[e ^ 1].flow -= pushed;
        return pushed;
    }
}

return 0;
}

// maxflow entre s et t
ll maxflow(int s, int t) {
    ll ans = 0;
    while (bfs(s, t)) {
        fill(idnext, idnext + n, 0);
        ll pushed = 0;
        while ((pushed = dfs(s, t, INF)) > 0)
            ans += pushed;
    }
    return ans;
}
};

```

Push-relabel

```

// Remarques sur max flow :
// - probleme avec une borne inf :
// 1) trouver un flot arbitraire entre S et T tq
//     cmin[u][v] <= flot[u][v] <= cmax[u][v]
// Ajouter une nouvelle source S' et un nouveau puits T'
// Poser c[u][v] := cmax[u][v] - cmin[u][v]
//     c[S'][v] := sum(cmin[u][v], u in V)
//     c[u][T'] := sum(cmin[u][v], v in V)
//     c[T][S] := INF
// (Theoreme) L'ancien graphe a un flot qui verifie les conditions ssi. le
// nouveau graphe a un flot saturant, ie. si sa valeur est exactement
//     sum(cmin[u][v], u, v in V)
// (et si c'est le cas, c'est forcément un flot max dans le nouveau graphe)
// 2) trouver le flot min verifiant ces conditions : dichotomie sur la valeur
// de INF ?
const int INF = 1000 * 1000 * 1000;

// Max flow en O(V^3))
struct PushRelabel {
    // utiliser flow[u][v] a la fin de l'algo
    vector<vector<ll>> flow;

    // cap[1 .. n][1 .. n]
    // cap[u][v] = capacite entre les noeuds u et v
    // sur un graphe non complet, prendre cap[u][v] = 0 si not [(u, v) in E]
    // Calcule le flot max entre s et t avec les capacites cap
    PushRelabel(vector<vector<ll>> cap, int s, int t) {
        int n = cap.size();

        // sans perte de generalite
        for (int u = 0; u < n; ++u) cap[u][u] = 0;
    }
};

```

```

flow = vector<vector<ll>>(n, vector<ll>(n));
vector<ll> e(n);
vector<int> h(n);
h[s] = n - 1;
for (int i = 0; i < n; ++i) {
    flow[s][i] = cap[s][i];
    flow[i][s] = -flow[s][i];
    e[i] = cap[s][i];
}

vector<int> maxh(h);
int sz = 0;
while (true) {
    if (sz == 0)
        for (int i = 0; i < n; ++i)
            if (i != s && i != t && e[i] > 0) {
                if (sz > 0 && h[i] > h[maxh[0]]) sz = 0;
                if (sz == 0 || h[i] == h[maxh[0]]) maxh[sz++] = i;
            }

    if (sz == 0) break;

    while (sz > 0) {
        int i = maxh[sz - 1];
        bool pushed = false;
        for (int j = 0; j < n && e[i] > 0; ++j)
            if (cap[i][j] > flow[i][j] && h[i] == h[j] + 1) {
                pushed = true;
                ll addf = min(cap[i][j] - flow[i][j], e[i]);
                flow[i][j] += addf;
                flow[j][i] -= addf;
                e[i] -= addf;
                e[j] += addf;
                if (e[i] == 0) --sz;
            }

        if (!pushed) {
            h[i] = INF;
            for (int j = 0; j < n; ++j)
                if (cap[i][j] > flow[i][j] && h[i] > h[j] + 1)
                    h[i] = h[j] + 1;
            if (h[i] > h[maxh[0]]) {
                sz = 0;
                break;
            }
        }
    }
}
};

```

Min-cost max-flow

```

// Tire de https://github.com/stjepang/snippets/blob/master/mcmf_dijkstra.cpp
// Min-cost max-flow (uses DFS)
//

```

```

// Given a directed weighted graph, source, and sink, computes the minimum cost
// of the maximum flow from source to sink.
// This version uses DFS to find shortest paths and gives good performance on
// very "shallow" graphs: graphs which have very short paths between source
// and sink (e.g. at most 10 edges).
// In such cases this algorithm can be orders of magnitude faster than the
// Dijkstra version.
//
// To use, call init(n), then add edges using edge(x, y, c, w), and finally
// call run(src, sink).
//
// Functions:
// - init(n) initializes the algorithm with the given number of nodes
// - edge(x, y, c, w) adds an edge x->y with capacity c and weight w
// - run(src, sink) runs the algorithm and returns {total_cost, total_flow}
//
// Time complexity:  $O(V * E^3)$ 
//
// Constants to configure:
// - MAXV is the maximum number of vertices
// - MAXE is the maximum number of edges (i.e. twice the calls to function edge)
// - oo is the "infinity" value
namespace Mcmf_dfs {
    const int MAXV = 1000100;
    const int MAXE = 1000100;
    const ll oo = 1e18;

    int V, E;
    int last[MAXV], curr[MAXV], bio[MAXV];
    ll pi[MAXV];
    int next[MAXE], adj[MAXE];
    ll cap[MAXE], cost[MAXE];

    void init(int n) {
        V = n;
        E = 0;
        fill(last, last + V, -1);
        fill(pi, pi + V, 0);
    }

    void edge(int x, int y, ll c, ll w) {
        adj[E] = y; cap[E] = c; cost[E] = +w; next[E] = last[x]; last[x] = E++;
        adj[E] = x; cap[E] = 0; cost[E] = -w; next[E] = last[y]; last[y] = E++;
    }

    ll push(int x, int sink, ll flow) {
        if (x == sink) return flow;
        if (bio[x]) return 0;
        bio[x] = true;

        for (int &e = curr[x]; e != -1; e = next[e]) {
            int y = adj[e];

            if (cap[e] && pi[x] == pi[y] + cost[e])
                if (ll f = push(y, sink, min(flow, cap[e])))
                    return cap[e] -= f, cap[e ^ 1] += f, f;
        }
    }
}

```

```

    }
    return 0;
}

pair<ll, ll> run(int src, int sink) {
    ll total = 0;
    ll flow = 0;
    pi[src] = oo;

    for (;;) {
        fill(bio, bio + V, false);
        for (int i = 0; i < V; ++i) curr[i] = last[i];

        while (ll f = push(src, sink, oo)) {
            total += pi[src] * f;
            flow += f;
            fill(bio, bio + V, false);
        }

        ll inc = oo;
        for (int x = 0; x < V; ++x)
            if (bio[x])
                for (int e = last[x]; e != -1; e = next[e]) {
                    int y = adj[e];
                    if (cap[e] && !bio[y]) inc = min(inc, pi[y] + cost[e] - pi[x]);
                }

        if (inc == oo) break;

        for (int i = 0; i < V; ++i)
            if (bio[i])
                pi[i] += inc;
    }
    return {total, flow};
}

// Min-cost max-flow (uses Dijkstra's algorithm)
//
// Given a directed weighted graph, source, and sink, computes the minimum cost
// of the maximum flow from source to sink.
// This version uses Dijkstra's algorithm and gives good performance on all
// kinds of graphs.
//
// To use, call init(n), then add edges using edge(x, y, c, w), and finally
// call run(src, sink).
//
// Functions:
// - init(n) initializes the algorithm with the given number of nodes
// - edge(x, y, c, w) adds an edge x->y with capacity c and weight w
// - run(src, sink) runs the algorithm and returns {total_cost, total_flow}
//
// Time complexity:  $O(V * E^2 \log E)$ 
//
// Constants to configure:
// - MAXV is the maximum number of vertices

```

```
// - MAXE is the maximum number of edges (i.e. twice the calls to function edge)
// - oo is the "infinity" value
namespace Mcmf_dijkstra {
    const int MAXV = 1000100;
    const int MAXE = 1000100;
    const ll oo = 1e18;

    int V, E;
    int last[MAXV], how[MAXV]; ll dist[MAXV];
    int next[MAXE], from[MAXE], adj[MAXE]; ll cap[MAXE], cost[MAXE];

    struct cmpf {
        bool operator () (int a, int b) {
            if (dist[a] != dist[b]) return dist[a] < dist[b];
            return a < b;
        }
    };
    set<int, cmpf> S;

    void init(int n) {
        V = n;
        E = 0;
        fill(last, last + V, -1);
    }

    void edge(int x, int y, ll c, ll w) {
        from[E] = x; adj[E] = y; cap[E] = c; cost[E] = +w;
        next[E] = last[x]; last[x] = E++;
        from[E] = y; adj[E] = x; cap[E] = 0; cost[E] = -w;
        next[E] = last[y]; last[y] = E++;
    }

    pair<ll, ll> run(int src, int sink) {
        ll total = 0;
        ll flow = 0;

        for (;;) {
            fill(dist, dist + V, oo);
            dist[src] = 0;

            for (;;) {
                bool done = true;
                for (int x = 0; x < V; ++x)
                    for (int e = last[x]; e != -1; e = next[e]) {
                        if (cap[e] == 0) continue;

                        int y = adj[e];
                        ll val = dist[x] + cost[e];

                        if (val < dist[y]) {
                            dist[y] = val;
                            how[y] = e;
                            done = false;
                        }
                    }
            }
            if (done) break;

```

```
        }

        if (dist[sink] >= oo / 2) break;

        ll aug = cap[how[sink]];
        for (int i = sink; i != src; i = from[how[i]])
            aug = min(aug, cap[how[i]]);

        for (int i = sink; i != src; i = from[how[i]]) {
            cap[how[i]] -= aug;
            cap[how[i] ^ 1] += aug;
            total += cost[how[i]] * aug;
        }
        flow += aug;
    }
    return {total, flow};
}
}
```

Circulation

```
// Tire de https://github.com/stjepang/snippets/blob/master/circulation.cpp
// Circulation
//
// Given a directed weighted graph, computes the minimum cost to run the maximum
// amount of circulation flow through the graph.
//
// Configure: MAXV
// Configure: MAXE (at least 2 * calls_to_edge)
//
// Functions:
// - init(n) initializes the algorithm with the given number of nodes
// - edge(x, y, c, w) adds an edge x->y with capacity c and weight w
// - run() runs the algorithm and returns total cost
//
// Time complexity: No idea, but it should be fast enough to solve any problem
// where V and E are up to around 1000.
//
// Constants to configure:
// - MAXV is the maximum number of vertices
// - MAXE is the maximum number of edges (i.e. twice the calls to function edge)

```

```
namespace Circu {
    const int MAXV = 1000100;
    const int MAXE = 1000100;

    int V, E;
    int how[MAXV], good[MAXV], bio[MAXV], cookie = 1; ll dist[MAXV];
    int from[MAXE], to[MAXE]; ll cap[MAXE], cost[MAXE];

    void init(int n) { V = n; E = 0; }

    void edge(int x, int y, ll c, ll w) {
        from[E] = x; to[E] = y; cap[E] = c; cost[E] = +w; ++E;
        from[E] = y; to[E] = x; cap[E] = 0; cost[E] = -w; ++E;
    }
}

```

```

void reset() {
    fill(dist, dist + V, 0);
    fill(how, how + V, -1);
}

bool relax() {
    bool ret = false;
    for (int e = 0; e < E; ++e)
        if (cap[e]) {
            int x = from[e];
            int y = to[e];

            if (dist[x] + cost[e] < dist[y]) {
                dist[y] = dist[x] + cost[e];
                how[y] = e;
                ret = true;
            }
        }
    return ret;
}

ll cycle(int s, bool flip = false) {
    int x = s;
    ll c = cap[how[x]];
    do {
        int e = how[x];
        c = min(c, cap[e]);
        x = from[e];
    } while (x != s);

    ll sum = 0;
    do {
        int e = how[x];
        if (flip) {
            cap[e] -= c;
            cap[e ^ 1] += c;
        }
        sum += cost[e] * c;
        x = from[e];
    } while (x != s);
    return sum;
}

ll push(int x) {
    for (++cookie; bio[x] != cookie; x = from[how[x]]) {
        if (!good[x] || how[x] == -1 || cap[how[x]] == 0) return 0;
        bio[x] = cookie;
        good[x] = false;
    }
    return cycle(x) >= 0 ? 0 : cycle(x, true);
}

ll run() {
    reset();
    ll ret = 0;
    for (int step = 0; step < 2 * V; ++step) {

```

```

        if (step == V) reset();
        if (!relax()) continue;

        fill(good, good + V, true);
        for (int i = 0; i < V; ++i)
            if (ll w = push(i)) {
                ret += w;
                step = 0;
            }
        }
    }
    return ret;
}

```

Directed MST

```

// Tire de https://github.com/stjepang/snippets/blob/master/directed\_mst.cpp
// Directed minimum spanning tree
//
// Given a directed weighted graph and root node, computes the minimum spanning
// directed tree (arborescence) on it.
//
// Complexity:  $O(N * M)$ , where  $N$  is the number of nodes, and  $M$  the number
// of edges
struct Edge { int x, y, w; };

int dmst(int N, vector<Edge> E, int root) {
    const int oo = 1e9;

    vector<int> cost(N), back(N), label(N), bio(N);
    int ret = 0;

    for (;;) {
        fill(cost.begin(), cost.end(), oo);
        for (auto e : E) {
            if (e.x == e.y) continue;
            if (e.w < cost[e.y]) cost[e.y] = e.w, back[e.y] = e.x;
        }
        cost[root] = 0;

        for (int i = 0; i < N; ++i)
            if (cost[i] == oo)
                return -1;

        for (int i = 0; i < N; ++i)
            ret += cost[i];

        int K = 0;
        fill(label.begin(), label.end(), -1);
        fill(bio.begin(), bio.end(), -1);

        for (int i = 0; i < N; ++i) {
            int x = i;
            for (; x != root && bio[x] == -1; x = back[x]) bio[x] = i;

            if (x != root && bio[x] == i) {
                for (; label[x] == -1; x = back[x]) label[x] = K;

```

```

        ++K;
    }
}
if (K == 0) break;

for (int i = 0; i < N; ++i)
    if (label[i] == -1)
        label[i] = K++;

for (auto &e : E) {
    int xx = label[e.x];
    int yy = label[e.y];
    if (xx != yy) e.w -= cost[e.y];
    e.x = xx;
    e.y = yy;
}

root = label[root];
N = K;
}

return ret;
}

```

Maths

Extended euclidian algorithm

```

// Euclide etendu
// Retourne PGCD(a, b)
// et u, v contiennent a l'issue de l'algo des bons couples de Bezout
// et |u| + |v| minimal, u <= v en cas d'egalite
ll gcd(ll a, ll b, ll& u, ll& v) {
    if (b == 0) {
        u = 1;
        v = 0;
        return a;
    }
    ll d = gcd(b, a % b, u, v);
    ll oldu = u;
    u = v;
    v = oldu - v * ll(a / b);
    return d;
}

```

Gauss

```

// Inspire de https://github.com/stjepang/snippets/blob/master/gauss.cpp
// Elimination de Gauss
// Resout un systeme d'equations lineaires
// Complexite : O(nb_lins * nb_cols^2)
// Si le systeme a au moins une solution, value contiendra une solution possible
const int MAX_NB_COLS = 250;
const double eps = 1e-8;

struct Gauss {
    // posnz[i] = -1 si la i-eme composante est libre
    int posnz[MAX_NB_COLS];
    // value[i] = la valeur de X(i) verifiant l'equation ci-dessous
    double value[MAX_NB_COLS];
    // vrai ssi. le systeme a >= 1 solution
    bool has_solution;

    // mat[0 .. nb_lins-1][0 .. nb_cols-1] * X = mat[0 .. nb_lins-1][nb_cols]
    Gauss(double mat[][MAX_NB_COLS + 1], int nb_lins, int nb_cols) {
        fill(posnz, posnz + nb_cols, -1);

        int posnz_cur = 0;
        for (int col = 0; col < nb_cols; ++col) {
            int max_lin = posnz_cur;

            for (int lin = max_lin + 1; lin < nb_lins; ++lin)
                if (fabs(mat[lin][col]) > fabs(mat[max_lin][col]))
                    max_lin = lin;

            // La colonne est nulle
            // Condition de la forme == 0 si on est dans les entiers
            if (fabs(mat[max_lin][col]) < eps) continue;

            for (int i = 0; i <= nb_cols; ++i)
                swap(mat[max_lin][i], mat[posnz_cur][i]);
        }
    }
};

```



```

    for (int lin = 0; lin < nb_lins; ++lin) {
        if (lin == posnz_cur) continue;
        // Pour Gauss modulaire : remplacer par l'inverse de mat[posnz_cur][col]
        double factor = mat[lin][col] / mat[posnz_cur][col];
        for (int i = 0; i <= nb_cols; ++i)
            mat[lin][i] -= factor * mat[posnz_cur][i];
        // Gauss mod : rajouter le modulo
    }

    posnz[col] = posnz_cur++;
}

// Genere une solution valide
for (int col = 0; col < nb_cols; ++col) {
    if (posnz[col] != -1)
        value[col] = mat[posnz[col]][nb_cols] / mat[posnz[col]][col];
    // Gauss mod
    else
        value[col] = 0;
}

// Verifie que la solution generee est valide
has_solution = true;
for (int lin = 0; lin < nb_lins; ++lin) {
    double sum = 0;
    for (int col = 0; col < nb_cols; ++col)
        sum += mat[lin][col] * value[col]; // Gauss mod
    if (fabs(sum - mat[lin][nb_cols]) > eps) // Gauss mod
        has_solution = false;
}
}
};

```

Prime list

```

// Calcule la liste des nombres premiers dans [2, n]
// Stocke egalement pour tout i lp[i] le plus petit diviseur premier de i
// (permet de factoriser en temps lineaire)
// Complexite : O(n)
struct PrimeList {
    // primes[i] = i-eme premier de [2, n]
    vector<int> primes;
    // lp[i] = plus petit diviseur premier de i
    vector<int> lp;

    PrimeList(int n) {
        lp = vector<int>(n + 1);
        for (int i = 2; i <= n; ++i) {
            if (lp[i] == 0) {
                lp[i] = i;
                primes.push_back(i);
            }
            for (int j = 0; j < (int)primes.size() && primes[j] <= lp[i]
                && i * primes[j] <= n; ++j)
                lp[i * primes[j]] = primes[j];
        }
    }
};

```

```

}

// n > 0
// retourne la liste des facteurs premiers de n
// (ex: factorize(12) = [2, 2, 3])
vector<int> factorize(int n) {
    vector<int> ans;
    while (n > 1) {
        ans.push_back(lp[n]);
        n /= lp[n];
    }
    return ans;
}
};

```

Factorization

```

// factorise n en produit de ses facteurs premiers
// Complexite : O(sqrt(n))
vector<int> factorize(int n) {
    vector<int> ans;
    for (int i = 2; i * i <= n; ++i)
        while (n % i == 0) {
            ans.push_back(i);
            n /= i;
        }
    if (n > 1)
        ans.push_back(n);
    return ans;
}

```

FFT

```

// From https://github.com/stjepang/snippets
//
// Fast Fourier transform
//
// Caling mult(a, b, c, len) is identical to:
//     REP(i, 2*len) tmp[i] = 0
//     REP(i, len) REP(j, len) tmp[i+j] += a[i] * b[j];
//     REP(i, 2*len) c[i] = tmp[i];
//
// There is also a variant with modular arithmetic: mult_mod.
//
// Common use cases:
// - big integer multiplication
// - convolutions in dynamic programming
//
// Time complexity: O(N log N), where N is the length of arrays
//
// Constants to configure:
// - MAX must be at least 2^ceil(log2(2 * len))
#define MY_PI 3.14159265358979323846
#define REP(i, n) for (int i = 0; i < (n); ++i)

namespace FFT {
    const int MAX = 1 << 20;
};

```

```

typedef ll value;
typedef complex<double> comp;

int N;
comp omega[MAX];
comp a1[MAX], a2[MAX];
comp z1[MAX], z2[MAX];

void fft(comp *a, comp *z, int m = N) {
    if (m == 1) {
        z[0] = a[0];
    } else {
        int s = N / m;
        m /= 2;

        fft(a, z, m);
        fft(a + s, z + m, m);

        for (int i = 0; i < m; ++i) {
            comp c = omega[s * i] * z[m + i];
            z[m + i] = z[i] - c;
            z[i] += c;
        }
    }
}

// len = longueur de a et b
// c = a * b
void mult(value *a, value *b, value *c, int len) {
    N = 2 * len;

    while (N & (N - 1))
        ++N;

    assert(N <= MAX);
    fill(a1, a1 + N, 0);
    fill(a2, a2 + N, 0);
    for (int i = 0; i < len; ++i) {
        a1[i] = a[i];
        a2[i] = b[i];
    }

    for (int i = 0; i < N; ++i)
        omega[i] = polar(1., 2 * MY_PI / N * i);

    fft(a1, z1, N);
    fft(a2, z2, N);

    for (int i = 0; i < N; ++i) {
        omega[i] = comp(1, 0) / omega[i];
        a1[i] = z1[i] * z2[i] / comp(N, 0);
    }

    fft(a1, z1, N);
    for (int i = 0; i < 2 * len; ++i)

```

```

        c[i] = round(z1[i].real());
    }

    // len = longueur de a et b
    // c = a * b [mod]
    void mult_mod(value *a, value *b, value *c, int len, int mod) {
        static value a0[MAX], a1[MAX];
        static value b0[MAX], b1[MAX];
        static value c0[MAX], c1[MAX], c2[MAX];

        for (int i = 0; i < len; ++i) {
            a0[i] = a[i] & 0xFFFF;
            a1[i] = a[i] >> 16;
            b0[i] = b[i] & 0xFFFF;
            b1[i] = b[i] >> 16;
        }

        FFT::mult(a0, b0, c0, len);
        FFT::mult(a1, b1, c2, len);

        for (int i = 0; i < len; ++i) {
            a0[i] += a1[i];
            b0[i] += b1[i];
        }

        FFT::mult(a0, b0, c1, len);

        for (int i = 0; i < 2 * len; ++i) {
            c1[i] -= c0[i] + c2[i];
            c1[i] %= mod;
            c2[i] %= mod;
            c[i] = (c0[i] + (c1[i] << 16) + (c2[i] << 32)) % mod;
        }
    }
}

```

Simplex

```

// Simplexe
// Tire de https://github.com/jaehyunp/stanfordacm/
typedef long double DOUBLE;
typedef vector<DOUBLE> VD;
typedef vector<VD> VVD;
typedef vector<int> VI;
const DOUBLE EPS = 1e-9;

struct LPSolver {
    int m, n;
    VI B, N;
    VVD D;

    LPSolver(const VVD &A, const VD &b, const VD &c) :
        m(b.size()), n(c.size()), N(m + 1), B(m), D(m + 2, VD(n + 2)) {
        for (int i = 0; i < m; ++i)
            for (int j = 0; j < n; ++j)
                D[i][j] = A[i][j];
        for (int i = 0; i < m; ++i) {

```

```

    B[i] = n + i;
    D[i][n] = -1;
    D[i][n + 1] = b[i];
}
for (int j = 0; j < n; j++) {
    N[j] = j;
    D[m][j] = -c[j];
}
N[n] = -1; D[m + 1][n] = 1;
}

void Pivot(int r, int s) {
    for (int i = 0; i < m + 2; i++) if (i != r)
        for (int j = 0; j < n + 2; j++) if (j != s)
            D[i][j] -= D[r][j] * D[i][s] / D[r][s];
    for (int j = 0; j < n + 2; j++) if (j != s) D[r][j] /= D[r][s];
    for (int i = 0; i < m + 2; i++) if (i != r) D[i][s] /= -D[r][s];
    D[r][s] = 1.0 / D[r][s];
    swap(B[r], N[s]);
}

bool Simplex(int phase) {
    int x = phase == 1 ? m + 1 : m;
    while (true) {
        int s = -1;
        for (int j = 0; j <= n; j++) {
            if (phase == 2 && N[j] == -1) continue;
            if (s == -1 || D[x][j] < D[x][s] || D[x][j] == D[x][s] && N[j] < N[s])
                s = j;
        }
        if (D[x][s] > -EPS) return true;
        int r = -1;
        for (int i = 0; i < m; i++) {
            if (D[i][s] < EPS) continue;
            if (r == -1 || D[i][n + 1] / D[i][s] < D[r][n + 1] / D[r][s] ||
                (D[i][n + 1] / D[i][s]) == (D[r][n + 1] / D[r][s]) && B[i] < B[r])
                r = i;
        }
        if (r == -1) return false;
        Pivot(r, s);
    }
}

DOUBLE Solve(VD &x) {
    int r = 0;
    for (int i = 1; i < m; i++)
        if (D[i][n + 1] < D[r][n + 1])
            r = i;
    if (D[r][n + 1] < -EPS) {
        Pivot(r, n);
        if (!Simplex(1) || D[m + 1][n + 1] < -EPS)
            return -numeric_limits<DOUBLE>::infinity();
        for (int i = 0; i < m; i++) if (B[i] == -1) {
            int s = -1;
            for (int j = 0; j <= n; j++)
                if (s == -1 || D[i][j] < D[i][s] || D[i][j] == D[i][s] && N[j] < N[s])

```

```

            s = j;
            Pivot(i, s);
        }
    }
    if (!Simplex(2)) return numeric_limits<DOUBLE>::infinity();
    x = VD(n);
    for (int i = 0; i < m; i++) if (B[i] < n) x[B[i]] = D[i][n + 1];
    return D[m][n + 1];
}
};

```

Geometry

```

// Geometrie
// Tire de https://github.com/jaehyunp/stanfordacm/
double INF = 1e100;
double EPS = 1e-12;

struct PT {
    double x, y;
    PT() {}
    PT(double x, double y) : x(x), y(y) {}
    PT(const PT &p) : x(p.x), y(p.y) {}
    PT operator + (const PT &p) const { return PT(x + p.x, y + p.y); }
    PT operator - (const PT &p) const { return PT(x - p.x, y - p.y); }
    PT operator * (double c) const { return PT(x * c, y * c); }
    PT operator / (double c) const { return PT(x / c, y / c); }
    void print() const { printf("(%f,%f)", x, y); }
};

double dot(PT p, PT q) { return p.x * q.x + p.y * q.y; }
double dist2(PT p, PT q) { return dot(p - q, p - q); }
double cross(PT p, PT q) { return p.x * q.y - p.y * q.x; }

// rotate a point CCW or CW around the origin
PT RotateCCW90(PT p) { return PT(-p.y, p.x); }
PT RotateCW90(PT p) { return PT(p.y, -p.x); }
PT RotateCCW(PT p, double t) {
    return PT(p.x * cos(t) - p.y * sin(t), p.x * sin(t) + p.y * cos(t));
}

// project point c onto line through a and b
// assuming a != b
PT ProjectPointLine(PT a, PT b, PT c) {
    return a + (b - a) * dot(c - a, b - a) / dot(b - a, b - a);
}

// project point c onto line segment through a and b
PT ProjectPointSegment(PT a, PT b, PT c) {
    double r = dot(b - a, b - a);
    if (fabs(r) < EPS) return a;
    r = dot(c - a, b - a) / r;
    if (r < 0) return a;
    if (r > 1) return b;
    return a + (b - a) * r;
}

```

```

// compute distance from c to segment between a and b
double DistancePointSegment(PT a, PT b, PT c) {
    return sqrt(dist2(c, ProjectPointSegment(a, b, c)));
}

// compute distance between point (x,y,z) and plane ax+by+cz=d
double DistancePointPlane(double x, double y, double z,
                           double a, double b, double c, double d)
{
    return fabs(a * x + b * y + c * z - d) / sqrt(a * a + b * b + c * c);
}

// determine if lines from a to b and c to d are parallel or collinear
bool LinesParallel(PT a, PT b, PT c, PT d) {
    return fabs(cross(b - a, c - d)) < EPS;
}

bool LinesCollinear(PT a, PT b, PT c, PT d) {
    return LinesParallel(a, b, c, d)
        && fabs(cross(a - b, a - c)) < EPS
        && fabs(cross(c - d, c - a)) < EPS;
}

// determine if line segment from a to b intersects with
// line segment from c to d
bool SegmentsIntersect(PT a, PT b, PT c, PT d) {
    if (LinesCollinear(a, b, c, d)) {
        if (dist2(a, c) < EPS || dist2(a, d) < EPS ||
            dist2(b, c) < EPS || dist2(b, d) < EPS) return true;
        if (dot(c - a, c - b) > 0 && dot(d - a, d - b) > 0 && dot(c - b, d - b) > 0)
            return false;
        return true;
    }
    if (cross(d - a, b - a) * cross(c - a, b - a) > 0) return false;
    if (cross(a - c, d - c) * cross(b - c, d - c) > 0) return false;
    return true;
}

// compute intersection of line passing through a and b
// with line passing through c and d, assuming that unique
// intersection exists; for segment intersection, check if
// segments intersect first
PT ComputeLineIntersection(PT a, PT b, PT c, PT d) {
    b = b - a; d = c - d; c = c - a;
    assert(dot(b, b) > EPS && dot(d, d) > EPS);
    return a + b * cross(c, d) / cross(b, d);
}

// compute center of circle given three points
PT ComputeCircleCenter(PT a, PT b, PT c) {
    b = (a + b) / 2;
    c = (a + c) / 2;
    return ComputeLineIntersection(b, b + RotateCW90(a - b), c,
                                   c + RotateCW90(a - c));
}

```

```

// determine if point is in a possibly non-convex polygon (by William
// Randolph Franklin); returns 1 for strictly interior points, 0 for
// strictly exterior points, and 0 or 1 for the remaining points.
// Note that it is possible to convert this into an *exact* test using
// integer arithmetic by taking care of the division appropriately
// (making sure to deal with signs properly) and then by writing exact
// tests for checking point on polygon boundary
bool PointInPolygon(const vector<PT> &p, PT q) {
    bool c = 0;
    for (int i = 0; i < p.size(); i++) {
        int j = (i + 1) % p.size();
        if ((p[i].y <= q.y && q.y < p[j].y ||
            p[j].y <= q.y && q.y < p[i].y) &&
            q.x < p[i].x + (p[j].x - p[i].x) * (q.y - p[i].y) / (p[j].y - p[i].y))
            c = !c;
    }
    return c;
}

// determine if point is on the boundary of a polygon
bool PointOnPolygon(const vector<PT> &p, PT q) {
    for (int i = 0; i < p.size(); i++)
        if (dist2(ProjectPointSegment(p[i], p[(i + 1) % p.size()], q), q) < EPS)
            return true;
    return false;
}

// compute intersection of line through points a and b with
// circle centered at c with radius r > 0
vector<PT> CircleLineIntersection(PT a, PT b, PT c, double r) {
    vector<PT> ret;
    b = b - a;
    a = a - c;
    double A = dot(b, b);
    double B = dot(a, b);
    double C = dot(a, a) - r * r;
    double D = B * B - A * C;
    if (D < -EPS) return ret;
    ret.push_back(c + a + b * (-B + sqrt(D + EPS)) / A);
    if (D > EPS)
        ret.push_back(c + a + b * (-B - sqrt(D)) / A);
    return ret;
}

// compute intersection of circle centered at a with radius r
// with circle centered at b with radius R
vector<PT> CircleCircleIntersection(PT a, PT b, double r, double R) {
    vector<PT> ret;
    double d = sqrt(dist2(a, b));
    if (d > r + R || d + min(r, R) < max(r, R)) return ret;
    double x = (d * d - R * R + r * r) / (2 * d);
    double y = sqrt(r * r - x * x);
    PT v = (b - a) / d;
    ret.push_back(a + v * x + RotateCCW90(v) * y);
    if (y > 0)
        ret.push_back(a + v * x - RotateCCW90(v) * y);
}

```

```

    return ret;
}

// This code computes the area or centroid of a (possibly nonconvex)
// polygon, assuming that the coordinates are listed in a clockwise or
// counterclockwise fashion. Note that the centroid is often known as
// the "center of gravity" or "center of mass".
double ComputeSignedArea(const vector<PT> &p) {
    double area = 0;
    for(int i = 0; i < p.size(); i++) {
        int j = (i + 1) % p.size();
        area += p[i].x * p[j].y - p[j].x * p[i].y;
    }
    return area / 2.0;
}

double ComputeArea(const vector<PT> &p) {
    return fabs(ComputeSignedArea(p));
}

PT ComputeCentroid(const vector<PT> &p) {
    PT c(0, 0);
    double scale = 6.0 * ComputeSignedArea(p);
    for (int i = 0; i < p.size(); i++){
        int j = (i + 1) % p.size();
        c = c + (p[i] + p[j]) * (p[i].x * p[j].y - p[j].x * p[i].y);
    }
    return c / scale;
}

// tests whether or not a given polygon (in CW or CCW order) is simple
bool IsSimple(const vector<PT> &p) {
    for (int i = 0; i < p.size(); i++) {
        for (int k = i + 1; k < p.size(); k++) {
            int j = (i + 1) % p.size();
            int l = (k + 1) % p.size();
            if (i == l || j == k) continue;
            if (SegmentsIntersect(p[i], p[j], p[k], p[l]))
                return false;
        }
    }
    return true;
}

```

Data structures

Binary indexed trees

```

// Fenwick tree - sommes sur intervalle
// Generalisation a d'autres operations inversibles
// Requetes de sommes/mises a jour : O(log n)
// Memoire : O(n)
struct FenwickTree {
    vector<ll> tree;
    // a = [0 .. n-1]
    FenwickTree(int n) {
        tree = vector<ll>(n);
    }
    // a[x] += v
    void add(int x, ll v) {
        for (; x < (int)tree.size(); x |= (x + 1))
            tree[x] += v;
    }
    // a[0] + ... + a[r]
    ll sum(int r) {
        ll ans = 0;
        for (; r >= 0; r = (r & (r + 1)) - 1)
            ans += tree[r];
        return ans;
    }
    // a[l] + ... + a[r]
    ll sum(int l, int r) {
        return sum(r) - sum(l - 1);
    }
};

// Fenwick Tree 2D classique - Sommes sur rectangles
// Temps : O(log^2 n) par requete
// Memoire : O(n^2)
struct FenwickTree2D {
    vector<vector<int>>> tree;
    // a = [1 .. n][1 .. m]
    FenwickTree2D(int n, int m) {
        tree = vector<vector<int>>>(n);
        for (int i = 0; i < n; ++i)
            tree[i] = vector<int>(m);
    }
    // a[x][y] += v
    void add(int x, int y, int v) {
        for (; x < (int)tree.size(); x |= (x + 1))
            for (int j = y; j < (int)tree[x].size(); j |= (j + 1))
                tree[x][j] += v;
    }
    // sum (0 <= i <= x; 0 <= j <= y) a[i][j]
    int sum(int x, int y) {
        int ans = 0;
        for (; x >= 0; x = (x & (x + 1)) - 1)
            for (int j = y; j >= 0; j = (j & (j + 1)) - 1)
                ans += tree[x][j];
        return ans;
    }
}

```

```

// sum (x1 <= x <= x2; y1 <= y <= y2) a[x][y]
int sum(int x1, int y1, int x2, int y2) {
    return sum(x2, y2) - sum(x1 - 1, y2) - sum(x2, y1 - 1) +
           sum(x1 - 1, y1 - 1);
}
};

// Fenwick tree 2D compresse
// Necessite deux passes sur les requetes
// Temps : O(log^2 n) par requete
// Memoire : O(n log n)
// /\ type
struct FenwickTree2DCompressed {
    vector<vector<int>> tree;
    vector<vector<int>> nodes;
    // a = [1 .. n][1 .. m]
    FenwickTree2DCompressed(int n) {
        tree = vector<vector<int>>(n);
        nodes = vector<vector<int>>(n);
    }
    // premiere passe : a appeler sur toutes les requetes prevues
    void init_add(int x, int y) {
        for (; x < (int)tree.size(); x |= (x + 1))
            nodes[x].push_back(y);
    }
    void init_sum(int x, int y) {
        for (; x >= 0; x = (x & (x + 1)) - 1)
            nodes[x].push_back(y);
    }
    void init_sum(int x1, int y1, int x2, int y2) {
        init_sum(x2, y2);
        init_sum(x1 - 1, y2);
        init_sum(x2, y1 - 1);
        init_sum(x1 - 1, y1 - 1);
    }
    // a appeler a la fin de la premiere passe
    void init() {
        for (int x = 0; x < (int)tree.size(); ++x) {
            sort(nodes[x].begin(), nodes[x].end());
            tree[x] = vector<int>(nodes[x].size());
        }
    }
    // a[x][y] += v
    void add(int x, int y, int v) {
        for (; x < (int)tree.size(); x |= (x + 1))
            for (int j = lower_bound(nodes[x].begin(), nodes[x].end(), y)
                 - nodes[x].begin(); j < (int)nodes[x].size(); j |= (j + 1))
                tree[x][j] += v;
    }
    // sum (0 <= i <= x; 0 <= j <= y) a[i][j]
    int sum(int x, int y) {
        int ans = 0;
        for (; x >= 0; x = (x & (x + 1)) - 1)
            for (int j = lower_bound(nodes[x].begin(), nodes[x].end(), y)
                 - nodes[x].begin(); j >= 0; j = (j & (j + 1)) - 1)
                ans += tree[x][j];
    }
};

```

```

    return ans;
}
// sum (x1 <= x <= x2; y1 <= y <= y2) a[x][y]
int sum(int x1, int y1, int x2, int y2) {
    return sum(x2, y2) - sum(x1 - 1, y2) - sum(x2, y1 - 1) +
           sum(x1 - 1, y1 - 1);
}
};

```

LCA

```

// Plus petit ancetre commun
// Pretraitement : O(n log n)
// Requete : O(log n)
// Memoire : O(n)
struct LCA {
    vector<vector<int>> adj;
    vector<vector<int>> prev;
    int h;
    vector<int> tin, tout;
    int timer;

    void dfs(int u, int p = 0) {
        tin[u] = ++timer;
        prev[u][0] = p;
        for (int i = 1; i < h; ++i)
            prev[u][i] = prev[prev[u][i - 1]][i - 1];
        for (int v: adj[u])
            if (v != p)
                dfs(v, u);
        tout[u] = ++timer;
    }

    // adj : liste d'adjacence de l'arbre
    // peut contenir eventuellement des aretes vers un parent
    LCA(vector<vector<int>> adj, int root) {
        int n = (int)adj.size();
        this->adj = adj;
        for (h = 0; (1 << h) <= n; ++h)
            ;
        prev = vector<vector<int>>(n, vector<int>(h));
        timer = 0;
        tin = vector<int>(n);
        tout = vector<int>(n);
        dfs(root);
    }

    bool is_ancestor(int u, int v) {
        return tin[u] <= tin[v] && tout[v] <= tout[u];
    }

    int lca(int u, int v) {
        if (is_ancestor(u, v)) return u;
        if (is_ancestor(v, u)) return v;
        for (int i = h - 1; i >= 0; --i) {
            if (!is_ancestor(prev[u][i], v))
                u = prev[u][i];
        }
    }
};

```

```

    }
    return prev[u][0];
}
};

```

HLD

// A adapter au probleme (par exemple avec des poids)

```

struct Edge {
    int u, v;

    Edge() {}
    Edge(int u, int v) : u(u), v(v) {}

    void read() {
        scanf("%d%d", &u, &v);
        --u, --v;
    }

    int next(int x) {
        return x == u ? v : u;
    }

    bool operator == (const Edge& e) const {
        return u == e.u && v == e.v;
    }
};

```

// HLD

```

struct HLD {
    vector<vector<Edge>> adj;
    vector<int> subtreesz;
    vector<int> nodechain;
    vector<int> nodepos;
    vector<int> head;
    vector<int> tail;
    vector<int> length;
    vector<Edge> prev;
    vector<Edge> next;
    int nb_chains;

    void compute_subtree(int u, int p = -1) {
        subtreesz[u]++;
        for (Edge e: adj[u]) {
            int v = e.next(u);
            if (v != p) {
                prev[v] = e;
                compute_subtree(v, u);
                subtreesz[u] += subtreesz[v];
            }
        }
    }

    void construct(int u, int p = -1) {
        nodechain[u] = nb_chains - 1;
        nodepos[u] = length[nb_chains - 1]++;
        if (nodepos[u] == 0)

```

```

        head[nb_chains - 1] = u;
        tail[nb_chains - 1] = u;
        if (adj[u].size() == 1 && adj[u][0].next(u) == p) return;
        Edge maxe = adj[u][0].next(u) == p ? adj[u][1] : adj[u][0];
        int maxv = maxe.next(u);
        for (Edge e: adj[u]) {
            int v = e.next(u);
            if (v != p && subtreesz[v] > subtreesz[maxv]) {
                maxv = v;
                maxe = e;
            }
        }
        next[u] = maxe;
        construct(maxv, u);
        for (Edge e: adj[u]) {
            int v = e.next(u);
            if (v != p && v != maxv) {
                nb_chains++;
                construct(v, u);
            }
        }
    }
};

```

```

HLD(vector<vector<Edge>> adj, int root) {
    int n = (int)adj.size();
    this->adj = adj;
    subtreesz = vector<int>(n);
    prev = vector<Edge>(n);
    compute_subtree(root);
    nodechain = vector<int>(n);
    nodepos = vector<int>(n);
    tail = vector<int>(n);
    head = vector<int>(n);
    length = vector<int>(n);
    next = vector<Edge>(n);
    nb_chains = 1;
    construct(root);
}
};

```

Link-cut

// Link cut trees
// Tire de <https://github.com/jaehyunp/stanfordacm/>
enum { LEFT, RIGHT };

```

struct node {
    node * parent, * child[2];
    int value, subtree_value;
    bool flip;

    void update(bool change = false, int new_value = 0) {
        if (change) value = new_value;
        subtree_value = value;
        FOR (d, 2)
            if (child[d] != nullptr)
                subtree_value += child[d]->subtree_value;
    }
};

```

```

}

void propagate() {
    if (!flip) return;
    swap(child[LEFT], child[RIGHT]);
    FOR (d, 2) if (child[d] != nullptr) child[d]->flip ^= 1;
    flip = false;
}

void set_child(bool d, node * x) {
    if ((child[d] = x) != nullptr) x->parent = this;
    update();
}

bool has_child(node * x) { return child[LEFT] == x || child[RIGHT] == x; }
bool is_root() { return parent == nullptr || !parent->has_child(this); }
bool child_direction(node * x) { return (child[LEFT] == x) ? LEFT : RIGHT; }

void rotate() {
    node *g = parent->parent;

    if (g != nullptr) g->propagate();
    parent->propagate();
    this->propagate();

    bool d = parent->child_direction(this);
    parent->set_child(d, child[!d]);
    this->set_child(!d, parent);
    if (g == nullptr || !g->has_child(parent)) parent = g;
    else g->set_child(g->child_direction(parent), this);
}

node * splay() {
    while (!is_root()) {
        node * p = parent;
        rotate();
        if (!is_root()) rotate();
        if (has_child(p->parent)) p->rotate();
    }
    return this;
}

node * leftmost_child() {
    for (node * x = this; ; x = x->child[LEFT]) {
        x->propagate();
        if (x->child[LEFT] == nullptr)
            return x->splay();
    }
}

} nodes[MAXN];

node * expose(node * v) {
    node * old_preferred = nullptr;
    for (node * x = v; x != nullptr; x = x->parent) {
        x->splay()->propagate();
        x->set_child(RIGHT, old_preferred);
    }
}

```

```

    old_preferred = x;
}
return v->splay();
}

void reroot(node * v) {
    expose(v)->flip ^= 1;
    v->parent = nullptr;
}

node * find_root(node * v) {
    return expose(v)->leftmost_child();
}

bool connected(node * u, node * v) {
    expose(u);
    return expose(v)->parent != nullptr;
}

bool link(node * u, node * v) {
    if (find_root(u) == find_root(v)) return false;
    reroot(v);
    v->parent = u;
    return true;
}

bool cut(node * u, node * v) {
    reroot(u);
    expose(v);
    if (v->child[RIGHT] != u || u->child[LEFT] != nullptr) return false;
    v->child[RIGHT]->parent = nullptr;
    v->child[RIGHT] = nullptr;
}

int query(node * u, node * v) {
    if (find_root(u) != find_root(v)) return -1;
    reroot(u);
    return expose(v)->subtree_value;
}

```

Convex hull trick

```

// Convex hull trick "statique"
// Recurrence de la forme : dp[i] = min(dp[j] + b[j] * a[i], j < i)
// Hypotheses : a[i] <= a[i+1] (requetes croissantes)
//               b[i] >= b[i+1] (coefficients directeurs décroissants)
const int MAX_NB_LINES = 100 * 1000;
struct ConvexHullTrick {
    ll a[MAX_NB_LINES], b[MAX_NB_LINES];
    ll hd, tl;

    ConvexHullTrick() {hd = tl = 0;}

    // ajoute y = a0 * x + b0
    void add(ll a0, ll b0) {
        while (tl - hd >= 2) {
            ll a1 = a[tl - 1], b1 = b[tl - 1];

```



```

    ll a2 = a[t1 - 2], b2 = b[t1 - 2];
    if ((long double)(b0 - b2) * (a1 - a0) <
        (long double)(b0 - b1) * (a2 - a0))
        break;
    //if ((long double)1 * (b0 - b2) / (a2 - a0) <
    //    (long double)1 * (b0 - b1) / (a1 - a0))
    //    break;
    t1--;
}
a[t1] = a0;
b[t1++] = b0;
}

// valeur de l'enveloppe min sur la droite d'equation x = x0
ll query(ll x0) {
    while (t1 - hd >= 2) {
        if (x0 * a[hd] + b[hd] < x0 * a[hd + 1] + b[hd + 1])
            break;
        ++hd;
    }
    return x0 * a[hd] + b[hd];
}
};

// Inspire de https://github.com/niklasb/contest-algos/
// Variante du precedent sans hypothese sur les a[i] et les b[i]
const ll QUERY = -(1LL << 62);
struct Line {
    ll a, b;
    mutable function<const Line *()> succ;

    bool operator < (const Line& other) const {
        if (other.b != QUERY)
            return a > other.a;
        const Line *s = succ();
        if (s == NULL) return false;
        return b - s->b > (s->a - a) * other.a;
    }
};

struct DynamicConvexHullTrick : public multiset<Line> {
    bool bad(iterator y) {
        auto z = next(y);
        if (y == begin()) {
            if (z == end()) return false;
            return y->a == z->a && y->b >= z->b;
        }
        auto x = prev(y);
        if (z == end())
            return y->a == x->a && y->b >= x->b;
        return (long double)(x->b - y->b) * (z->a - y->a) >=
            (long double)(y->b - z->b) * (y->a - x->a);
    }

    void add(ll a, ll b) {
        auto y = insert({a, b, nullptr});

```

```

y->succ = [=] { return next(y) == end() ? 0 : &*next(y); };

if (bad(y)) {
    erase(y);
    return;
}

while (next(y) != end() && bad(next(y)))
    erase(next(y));

while (y != begin() && bad(prev(y)))
    erase(prev(y));
}

ll query(ll x) {
    auto l = *lower_bound((Line){x, QUERY, nullptr});
    return l.a * x + l.b;
}
};

```

Segment tree

```

// Segment tree
template <typename T>
struct SegmentTree {
    function<void (vector<T>&, int, int, int)> push_up;
    function<int (vector<T>&, int, int, int, T, T)> combine_results;
    function<void (vector<T>&, int, int, int, T)> update_node;
    function<void (vector<T>&, int, int, int, T)> update_push;
    function<void (vector<T>&, vector<T>&, int, int, int)> push_down;
    vector<T> tree;
    vector<T> push_tree;
    T neutral;
    int n;

    SegmentTree(int n, T neutral = T(),
                function<void (vector<T>&, int, int, int)>
                    push_up = nullptr,
                function<int (vector<T>&, int, int, int, T, T)>
                    combine_results = nullptr,
                function<void (vector<T>&, int, int, int, T)>
                    update_node = nullptr,
                function<void (vector<T>&, int, int, int, T)>
                    update_push = nullptr,
                function<void (vector<T>&, vector<T>&, int, int, int)>
                    push_down = nullptr) {
        this->neutral = neutral;
        this->push_up = push_up;
        this->combine_results = combine_results;
        this->update_node = update_node;
        this->update_push = update_push;
        this->push_down = push_down;
        int h;
        for (h = 0; (1 << h) < n; ++h)
            ;
        this->n = n = 1 << h;
        tree = vector<T>(2 * n, neutral);
    }
};

```

```

    push_tree = vector<T>(2 * n, neutral);
}

void update(int ql, int qr, int l, int r, int u, T val) {
    if (ql <= l && r <= qr) {
        update_node(tree, u, l, r, val);
        if (update_push) update_push(push_tree, u, l, r, val);
        return;
    }
    if (push_down) push_down(tree, push_tree, u, l, r);
    int m = (l + r) / 2;
    if (ql <= m)
        update(ql, qr, l, m, 2 * u, val);
    if (qr > m)
        update(ql, qr, m + 1, r, 2 * u + 1, val);
    push_up(tree, u, l, r);
}

void update(int ql, int qr, T val) {
    update(ql, qr, 0, n - 1, 1, val);
}

T query(int ql, int qr, int l, int r, int u) {
    if (ql <= l && r <= qr)
        return tree[u];
    if (push_down) push_down(tree, push_tree, u, l, r);
    int m = (l + r) / 2;
    if (qr <= m)
        return combine_results(tree, u, l, r,
                                query(ql, qr, l, m, 2 * u), neutral);
    if (ql > m)
        return combine_results(tree, u, l, r, neutral,
                                query(ql, qr, m + 1, r, 2 * u + 1));
    return combine_results(tree, u, l, r,
                            query(ql, qr, l, m, 2 * u),
                            query(ql, qr, m + 1, r, 2 * u + 1));
}

T query(int ql, int qr) {
    return query(ql, qr, 0, n - 1, 1);
}
};

```

Treap

```

// Treap
// Titre de https://github.com/jaehyunp/stanfordacm/
typedef int value;

enum { LEFT, RIGHT };
struct node {
    int size, priority;
    value x, subtree;
    node *child[2];
    node(const value &x): size(1), x(x), subtree(x) {
        priority = rand();
        child[0] = child[1] = nullptr;
    }
};

```

```

    }
};

inline int size(const node *a) { return a == nullptr ? 0 : a->size; }

inline void update(node *a) {
    if (a == nullptr) return;
    a->size = size(a->child[0]) + size(a->child[1]) + 1;
    a->subtree = a->x;
    if (a->child[LEFT] != nullptr)
        a->subtree = a->child[LEFT]->subtree + a->subtree;
    if (a->child[RIGHT] != nullptr)
        a->subtree = a->subtree + a->child[RIGHT]->subtree;
}

node *rotate(node *a, bool d) {
    node *b = a->child[d];
    a->child[d] = b->child[!d];
    b->child[!d] = a;
    update(a); update(b);
    return b;
}

node *insert(node *a, int index, const value &x) {
    if (a == nullptr && index == 0) return new node(x);
    int middle = size(a->child[LEFT]);
    bool dir = index > middle;
    if (!dir) a->child[LEFT] = insert(a->child[LEFT], index, x);
    else a->child[RIGHT] = insert(a->child[RIGHT], index - middle - 1, x);
    update(a);
    if (a->priority > a->child[dir]->priority) a = rotate(a, dir);
    return a;
}

node *erase(node *a, int index) {
    assert(a != nullptr);
    int middle = size(a->child[LEFT]);
    if (index == middle) {
        if (a->child[LEFT] == nullptr && a->child[RIGHT] == nullptr) {
            delete a;
            return nullptr;
        } else if (a->child[LEFT] == nullptr) a = rotate(a, RIGHT);
        else if (a->child[RIGHT] == nullptr) a = rotate(a, LEFT);
        else a = rotate(a, a->child[LEFT]->priority < a->child[RIGHT]->priority);
        a = erase(a, index);
    } else {
        bool dir = index > middle;
        if (!dir) a->child[LEFT] = erase(a->child[LEFT], index);
        else a->child[RIGHT] = erase(a->child[RIGHT], index - middle - 1);
    }
    update(a);
    return a;
}

void modify(node *a, int index, const value &x) {
    assert(a != nullptr);
}

```

```

    int middle = size(a->child[LEFT]);
    if (index == middle) a->x = x;
    else {
        bool dir = index > middle;
        if (!dir) modify(a->child[LEFT], index, x);
        else      modify(a->child[RIGHT], index - middle - 1, x);
    }
    update(a);
}

value query(node *a, int l, int r) {
    assert(a != nullptr);
    if (l <= 0 && size(a) - 1 <= r) return a->subtree;
    int middle = size(a->child[LEFT]);
    if (r < middle) return query(a->child[LEFT], l, r);
    if (middle < l) return query(a->child[RIGHT], l - middle - 1, r - middle - 1);
    value res = a->x;
    if (l < middle && a->child[LEFT] != nullptr)
        res = query(a->child[LEFT], l, r) + res;
    if (middle < r && a->child[RIGHT] != nullptr)
        res = res + query(a->child[RIGHT], l - middle - 1, r - middle - 1);
    return res;
}

```

Monotonic queue

```

// File monotone (min/max sur une fenetre glissante)
// Par default : file MIN
template<class T>
struct MonotonicQueue {
    deque<pair<T, int>> q;

    // ajoute elt a la file au "temps" t
    // t doit etre croissant au fur et a mesure des appels a add
    void add(T elt, int t) {
        while (!q.empty() && q.back().first > elt)
            q.pop_back();
        q.push_back({elt, t});
    }

    // supprime l'element issu du temps t
    // retourne vrai ssi. il y a effectivement un tel element
    // les appels successifs a remove doivent etre les memes qu'a add
    // (et dans le meme ordre)
    bool remove(int t) {
        if (!q.empty() && q.front().second == t) {
            q.pop_front();
            return true;
        }
        return false;
    }

    T get() {
        return q.front().first;
    }
};

```

Union-Find

```

// Union-Find
// Temps : O(alpha(n)) amorti par requete
// Memoire : O(n)
struct UnionFind {
    vector<int> cc;
    vector<int> ccsz;

    UnionFind() {}

    UnionFind(int n) {
        cc = vector<int>(n);
        ccsz = vector<int>(n);
        for (int i = 0; i < n; ++i)
            cc[i] = i;
    }

    int find(int i) {
        if (cc[i] != i)
            cc[i] = find(cc[i]);
        return cc[i];
    }

    bool merge(int i, int j) {
        i = find(i);
        j = find(j);
        if (i == j) return false;
        if (ccsz[i] < ccsz[j])
            swap(i, j);
        ccsz[i] += ccsz[j];
        cc[j] = i;
        return true;
    }
};

```

Strings

Aho-Corasick

```
// Tire de https://github.com/stjepang/snippets/blob/master/aho_corasick.cpp
// Aho Corasick
//
// Given a set of patterns, it builds the Aho-Corasick trie. This trie allows
// searching all matches in a string in linear time.
//
// To use, first call 'node' once to create the root node, then call 'insert'
// for every pattern, and finally initialize the trie by calling 'init_aho'.
// Note: It is assumed all strings contains uppercase letters only.
//
// Globals:
// - V is the number of vertices in the trie
// - trie[x][c] is the child of node x labeled with letter 'A' + c
// - fn[x] points from node x to it's "failure" node
//
// Time complexity: O(N), where N is the sum of lengths of all patterns
//
// Constants to configure:
// - MAX is the maximum sum of lengths of patterns
// - ALPHA is the size of the alphabet (usually 26)
const int MAX = 1000;
const int ALPHA = 26;
int V;
int trie[MAX][ALPHA];
int fn[MAX];

int node() {
    for (int i = 0; i < ALPHA; ++i) trie[V][i] = 0;
    fn[V] = 0;
    return V++;
}

int insert(char *s) {
    int t = 0;
    for (; *s; ++s) {
        int c = *s - 'A';
        if (trie[t][c] == 0) trie[t][c] = node();
        t = trie[t][c];
    }
    return t;
}

void init_aho() {
    queue<int> Q;
    Q.push(0);

    while (!Q.empty()) {
        int t = Q.front(); Q.pop();

        for (int c = 0; c < ALPHA; ++c) {
            int x = trie[t][c];
            if (x) {
                Q.push(x);
            }
        }
    }
}
```

```
if (t) {
    fn[x] = fn[t];
    while (fn[x] && trie[fn[x]][c] == 0) fn[x] = fn[fn[x]];
    if (trie[fn[x]][c]) fn[x] = trie[fn[x]][c];
}
}
}
```

Palindromic tree

```
// Tire de https://github.com/stjepang/snippets/blob/master/palindromic_tree.cpp
// Palindromic tree
//
// Given a string, consider all its palindromic substrings.
// Denote every palindrome by its radius inside out. For example, denote the
// palindrome 'abcba' by 'cba'.
// This algorithm constructs a trie of all such radiuses.
//
// The algorithm is very similar to Aho-Corasick.
// More information:
// - http://adilet.org/blog/25-09-14/
// - http://codeforces.com/blog/entry/13959
//
// To run, set N and s, then call paltree().
// Note: It is assumed the string contains uppercase letters only.
//
// Globals:
// - N is the length of the string
// - s is the string
// - V is the number of vertices in the trie
// - trie[x][c] is the child of node x labeled with letter 'A' + c
// - fn[x] points from node x to it's "failure" node
// - len[x] is the depth of node x
//
// The root of even palindromes is node 0.
// The root of odd palindromes is node 1.
//
// Time complexity: O(N)
//
// Constants to configure:
// - MAX is the maximum length of the string
// - ALPHA is the size of the alphabet (usually 26)
const int MAX = 1000;
const int ALPHA = 26;
int N;
char s[MAX];

int V;
int trie[MAX][ALPHA];
int fn[MAX], len[MAX];

int node() {
    for (int i = 0; i < ALPHA; ++i) trie[V][i] = 0;
    fn[V] = len[V] = 0;
}
```

```

    return V++;
}

int suffix(int t, int i) {
    while (i - len[t] - 1 < 0 || s[i - len[t] - 1] != s[i])
        t = fn[t];
    return t;
}

void paltree() {
    V = 0; node(); node();
    len[0] = 0; fn[0] = 1;
    len[1] = -1; fn[1] = 0;

    int t = 0;
    for (int i = 0; i < N; ++i) {
        int c = s[i] - 'A';
        t = suffix(t, i);

        int &x = trie[t][c];
        if (!x) {
            x = node();
            len[x] = len[t] + 2;
            fn[x] = t == 1 ? 0 : trie[suffix(fn[t], i)][c];
        }
        t = x;
    }
}

```

Suffix array

```

// Suffix Array & LCP
// Construction en O(n log^2 n)
struct SuffixArray {
    // sa[i] = pos du premier caractere du i-eme suffixe dans l'ordre
    // lexicographique
    vector<int> sa;
    // pos[i] a l'issue du constructeur : position de s[i .. n-1] dans sa
    vector<int> pos;
    // lcp[i] : plus grand prefixe commun a sa[i] et sa[i+1]
    vector<int> lcp;
    int gap;
    int n;

    struct Compare {
        const SuffixArray& s;
        Compare(const SuffixArray& s) : s(s) {}

        bool operator () (int i, int j) const {
            if (s.pos[i] != s.pos[j]) return s.pos[i] < s.pos[j];
            i += s.gap;
            j += s.gap;
            return i < s.n && j < s.n ? s.pos[i] < s.pos[j] : i > j;
        }
    };

    SuffixArray(string s) {

```

```

        n = (int)s.length();
        sa = vector<int>(n);
        vector<int> tmp = vector<int>(n);
        pos = vector<int>(n);
        lcp = vector<int>(n - 1);

        // Construction de sa et pos
        for (int i = 0; i < n; ++i) {
            sa[i] = i;
            pos[i] = s[i];
        }

        for (gap = 1; gap <= n; gap *= 2) {
            sort(sa.begin(), sa.end(), Compare(*this));
            for (int i = 1; i < n; ++i)
                tmp[i] = tmp[i - 1] + Compare(*this)(sa[i - 1], sa[i]);
            for (int i = 0; i < n; ++i) pos[sa[i]] = tmp[i];
        }

        // Construction de lcp (peut etre supprime si non necessaire)
        int k = 0;
        for (int i = 0; i < n; ++i)
            if (pos[i] != n - 1) {
                int j = sa[pos[i] + 1];
                while (s[i + k] == s[j + k]) ++k;
                lcp[pos[i]] = k;
                if (k > 0) --k;
            }
    }
};

```

Z function

```

// Fonction Z : s[0 .. n-1] -> z[0 .. n-1]
// z[i] = longueur du plus grand prefixe commun de s[0 .. n-1] et s[i .. n-1]
// Calcul en O(n)
// Applications
// - Trouver toutes les occurrences d'un motif dans une chaine en O(n+p).
// - Nombre de sous-chaines distinctes quand on ajoute un caractere en tete.
// - Factorisation
vector<int> compute_z(string s) {
    int n = (int)s.length();
    vector<int> z(n);
    int l = 1, r = 0;
    for (int i = 1; i < n; ++i) {
        if (i <= r)
            z[i] = min(r - i + 1, z[i - l]);
        while (i + z[i] < n && s[z[i]] == s[i + z[i]])
            ++z[i];
        if (i + z[i] - 1 > r) {
            l = i;
            r = i + z[i] - 1;
        }
    }
    z[0] = n;
    return z;
}

```

Prefix function

```
// Fonction prefixe : s[0 .. n-1] -> pref[0 .. n-1]
// pref[i] = max(0 <= k <= i | s[0 .. k-1] = s[i-k+1 .. i])
// O(n)
// Applications :
// - Trouver toutes les occurrences d'un motif (KMP)
// - Compter le nombre d'occurrences de chaque prefixe de s dans s
// - Nombre de sous-chaines distinctes dans s
// - Factorisation
vector<int> compute_prefix(string s) {
    int n = (int)s.length();
    vector<int> pref(n);
    for (int i = 1; i < n; ++i) {
        int j = pref[i - 1];
        while (j > 0 && s[i] != s[j])
            j = pref[j - 1];
        if (s[i] == s[j])
            ++j;
        pref[i] = j;
    }
    return pref;
}
```

Min rotation

```
// Tire de https://github.com/stjepang/snippets/blob/master/min_rotation.cpp
// Lexicographically minimum rotation of a sequence
//
// Given a sequence s of length N, min_rotation(s, N) returns the start index
// of the lexicographically minimum rotation.
//
// Note: array s must be of length of at least 2 * N.
//
// Time complexity: O(N)
int min_rotation(int *s, int N) {
    for (int i = 0; i < N; ++i)
        s[N + i] = s[i];

    int a = 0;
    for (int b = 0; b < N; ++b)
        for (int i = 0; i < N; ++i) {
            if (a + i == b || s[a + i] < s[b + i]) {
                b += max(0, i - 1);
                break;
            }
            if (s[a + i] > s[b + i]) {
                a = b;
                break;
            }
        }
    return a;
}
```

Manacher

// Tire de <https://github.com/stjepang/snippets/blob/master/manacher.cpp>

```
// Finds all palindromes in a string
//
// Given a string s of length N, finds all palindromes as its substrings.
//
// After calling manacher(s, N, rad), rad[x] will be the radius of the largest
// palindrome centered at index x / 2.
// Example:
//   s   = b a n a n a a
//   rad = 0000102010010
//
// Note: Array rad must be of length at least twice the length of the string.
// Also, "invalid" characters are denoted by -1, therefore the string must not
// contain such characters.
//
// Time complexity: O(N)
//
// Constants to configure:
// - MAX is the maximum length of the string
const int MAX = 1000;
void manacher(char *s, int N, int *rad) {
    static char t[2 * MAX];
    int m = 2 * N - 1;
    fill(t, t + m, -1);
    for (int i = 0; i < N; ++i) t[2 * i] = s[i];

    int x = 0;
    for (int i = 1; i < m; ++i) {
        int& r = rad[i] = 0;
        if (i <= x + rad[x])
            r = min(rad[x + x - i], x + rad[x] - i);
        while (i - r - 1 >= 0 && i + r + 1 < m && t[i - r - 1] == t[i + r + 1])
            ++r;
        if (i + r >= x + rad[x])
            x = i;
    }

    for (int i = 0; i < m; ++i)
        if (i - rad[i] == 0 || i + rad[i] == m - 1)
            ++rad[i];

    for (int i = 0; i < m; ++i)
        rad[i] /= 2;
}
```

Suffix automaton

```
// Automate suffixe
// Tire de https://github.com/ngthanhtung23/ACM_Notebook_new/
struct Node {
    int len, link; // len = max length of suffix in this class
    int next[33];
};
Node s[MN * 2];
set<pair<int, int>> order; // in most application we'll need to sort by len

struct Automaton {
    int sz, last;
```

```

Automaton() {
    order.clear();
    sz = last = 0;
    s[0].len = 0;
    s[0].link = -1;
    ++sz;
    // need to reset next if necessary
}

void extend(char c) {
    c = c - 'A';
    int cur = sz++, p;
    s[cur].len = s[last].len + 1;
    order.insert(make_pair(s[cur].len, cur));

    for (p = last; p != -1 && !s[p].next[c]; p = s[p].link)
        s[p].next[c] = cur;
    if (p == -1) s[cur].link = 0;
    else {
        int q = s[p].next[c];
        if (s[p].len + 1 == s[q].len) s[cur].link = q;
        else {
            int clone = sz++;
            s[clone].len = s[p].len + 1;
            memcpy(s[clone].next, s[q].next, sizeof s[q].next);
            s[clone].link = s[q].link;
            order.insert(make_pair(s[clone].len, clone));

            for (; p != -1 && s[p].next[c] == q; p = s[p].link)
                s[p].next[c] = clone;
            s[q].link = s[cur].link = clone;
        }
    }
    last = cur;
}

};

// Construct:
// Automaton sa; for(char c : s) sa.extend(c);
// 1. Number of distinct substr:
//     - Find number of different paths --> DFS on SA
//     - f[u] = 1 + sum( f[v] for v in s[u].next
// 2. Number of occurrences of a substr:
//     - Initially, in extend: s[cur].cnt = 1; s[clone].cnt = 0;
//     - for(it : reverse order)
//         p = nodes[it->second].link;
//         nodes[p].cnt += nodes[it->second].cnt
// 3. Find total length of different substrings:
//     - We have f[u] = number of strings starting from node u
//     - ans[u] = sum(ans[v] + d[v] for v in next[u])
// 4. Lexicographically k-th substring
//     - Based on number of different substring
// 5. Smallest cyclic shift
//     - Build SA of S+S, then just follow smallest link
// 6. Find first occurrence

```

```

// - firstpos[cur] = len[cur] - 1, firstpos[clone] = firstpos[q]

```

String hash

```

// Hash
// P premier de l'ordre de la taille de l'alphabet
// P = 31 pour les minuscules, 53 pour tous les caracteres alphabetiques
//
// (Quelques) applications :
// - Recherche de motifs (Rabin-Karp)
// - Nombre de sous-chaines distinctes
// - Requetes : est-ce que la sous-chaine est un palindrome ?
//
// /\ Ne pas utiliser les hash modulo 2^64
// http://codeforces.com/blog/entry/4898(
//
// Utiliser un modulo suffit generalement (/\ paradoxe des anniversaires)
// Sinon utiliser deux mod
// Quelques premiers de l'ordre de 10^9 : 10^9 + 7 ; 10^9 + 9 ; 10^9 + 123
// Trouver le reste entre 0 et M - 1 de a/M : (a % M + M) % M
typedef long long ll;
ll posmod(ll a, ll M) { return (a % M + M) % M; }

struct StringHash {
    ll mod;
    vector<ll> ppows;
    // hashesuff[i] = s[i] + s[i+1] * P + s[i+2] * P^2 + ... + s[n-1] * P^(n-1-i)
    // [mod]
    vector<ll> hashesuff;

    StringHash() {}

    StringHash(string s, ll base, ll mod) {
        this->mod = mod;
        int n = (int)s.length();
        ppows = vector<ll>(n);
        hashesuff = vector<ll>(n + 1);
        ppows[0] = 1;
        for (int i = 1; i < n; ++i)
            ppows[i] = posmod(ppows[i - 1] * base, mod);
        hashesuff[n] = 0;
        for (int i = n - 1; i >= 0; --i)
            hashesuff[i] = posmod(hashesuff[i + 1] * base + s[i], mod);
    }

    // [l, r]
    // 0 <= l <= r <= n
    ll get_hash(int l, int r) {
        return posmod(hashesuff[l] - hashesuff[r + 1] * ppows[r + 1 - l], mod);
    }
};

const int BASE = 31;
const int NB_MODS = 2;
const ll MOD[NB_MODS] = {1000 * 1000 * 1000 + 9, 1000 * 1000 * 1000 + 7};

// Premiers :

```

```
//
// 2 3 5 7 11 13 17 19 23 29
// 31 37 41 43 47 53 59 61 67 71
// 73 79 83 89 97 101 103 107 109 113
// 127 131 137 139 149 151
//
// ...
//
// 1009 1013 1019 1021 1031 1033 1039 1049 1051 1061
//
// ...
//
// 1000003 1000033 1000037 1000039
// 1000081 1000099 1000117 1000121
// 1000133 1000151 1000159 1000171
// 1000183 1000187 1000193 1000199
// 1000211 1000213 1000231 1000249
//
// ...
//
// 1000000007 1000000009 1000000021 1000000033
// 1000000087 1000000093 1000000097 1000000103
// 1000000123 1000000181 1000000207 1000000223
// 1000000241 1000000271 1000000289 1000000297
// 1000000321 1000000349 1000000363 1000000403
```

Formulas

Maths

Bernoulli numbers:

| n | 0 | 1 | 2 | 4 | 6 | 8 | 10 | 12 |
|-------|---|------|-----|-------|------|-------|------|-----------|
| B_n | 1 | -1/2 | 1/6 | -1/30 | 1/42 | -1/30 | 5/66 | -691/2730 |

$B_{2n+3} = 0$

$(m+1)B_m = -\sum_{k=0}^{m-1} \binom{k}{m+1} B_k$

$\sum_{k=1}^n k^m = \frac{1}{m+1} \sum_{k=0}^m \binom{m+1}{k} B_k n^{m+1-k}.$

$\sum_{k=a}^{b-1} f(k) = \int_a^b f(t)dt + \sum_{k=1}^n \frac{B_k}{k!} \left(f^{(k-1)}(b) - f^{(k-1)}(a) \right) + \frac{(-1)^{n+1}}{n!} \int_a^b B_n(t) f^{(n)}(t)dt.$

$n \geq 1. \zeta(2n) = (-1)^{n-1} 2^{2n-1} \frac{B_{2n}}{(2n)!} \pi^{2n}.$

Pick's theorem: $A = I + \frac{1}{2}B - 1.$ (A area polygon, I number of interior points, B number of boundary points).

Triangle geometry

$p = \frac{a+b+c}{2}.$

Area: $A = \frac{\sin \alpha}{a} = \sqrt{p(p-a)(p-b)(p-c)}.$

Incircle: $r = \frac{A}{p}. I = \frac{a}{2p}A + \frac{b}{2p}B + \frac{c}{2p}C.$

Length of the angle bissector through A : $i_a = \frac{2}{b+c} \sqrt{p(p-a)bc}.$

Circumcircle: $R = \frac{abc}{4A} = \frac{a}{2 \sin \alpha}. O = \frac{1}{\sin(2\alpha)+\sin(2\beta)+\sin(2\gamma)} (\sin(2\alpha)A + \sin(2\beta)B + \sin(2\gamma)C).$

Orthocenter: $H = \frac{1}{\tan \alpha + \tan \beta + \tan \gamma} (\tan(\alpha)A + \tan(\beta)B + \tan(\gamma)C).$

Law of cosines: $c^2 = a^2 + b^2 - 2ab \cos(\gamma).$