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Resolução prova

6. a,  $y = \ln(5x + 3x^7)$   
 $y' = \frac{1}{5x + 3x^7} \cdot (5 + 21x^6)$   $y' = \frac{5 + 21x^6}{(5x + 3x^7)}$   $\frac{5 + 21}{5 + 3} = \frac{26}{8} = \frac{13}{4}$

b,  $y = 2 \cdot e^{3x+7}$   
 $y' = 2 \cdot e^{3x+7} \cdot 3$   
 $y' = 6e^{3x+7} = 6e^{10}$

1-  $f(x) = 3x^6 - x^5 - 2x^4 + 2x - 2$   
 $f'(x) = 18x^5 - 5x^4 - 8x^3 + 2$   
 $f''(x) = 90x^4 - 20x^3 - 24x^2 + 2$   
 $f'''(x) = 360x^3 - 60x^2 - 48x$   
 $f^{IV}(x) = 1080x^2 - 120x - 48$   
 $f^{V}(x) = 2160x - 120$

$f(2) = 2160 \cdot 2 - 120 = 4200,,$

2-  $f(t) = 2t^4 + 3t^2 - 6t$   
 $f'(t) = 8t^3 + 6t - 6$   
 $f''(t) = 24t^2 + 6$

$f(2) = 24 \cdot 2^2 + 6$   
 $f(2) = 102 \text{ m/s}^2$

3.  $m = ?$ 

$$f(x) = x^2 + 2x + 5$$

$$m = f'(x) = 2x + 2$$

$$m = 6$$

$$y = m \cdot x + b$$

$$13 = 6 \cdot 2 + b$$

$$13 - 12 = b$$

$$b = 1$$

$$y = m \cdot x + b$$

$$y = 6x + 1$$

$$4. f(x) = (x^2 \cdot \cot x) - 1/x^2$$

$$u' \cdot v + u \cdot v'$$

$$(2x \cdot \cot x) + (x^2 \cdot -\operatorname{cosec}^2 x) - x^{-2}$$

$$2x \cot x - x^2 \operatorname{cosec}^2 x + 2x^3$$

$$5. a \frac{(3x^2 + 6)}{2x^2 - 7} = \frac{-66x}{(2x^2 - 7)^2}$$

$$6. (2 - x - 3x^2)^{1/2}$$

$$y'(x) = 1/2 \cdot (2 - x - 3x^2)^{-1/2} \cdot (-1 - 6x)$$

$$y'(x) = (-12 - 108x^2) \cdot (2 - x - 3x^2)^{-3/2}$$

$$7. -1 = 8 \cdot 3 + b$$

$$-24 - 1 = b$$

$$b = -25$$

$$y = 8x - 25$$

9.

$$9. f(x) = 3x^2 + 2x^2 + 5x + 1$$

$$f(2) = 2^2 + 8 + 10 + 1 = 43 \quad (2, 43)$$

$$f'(x) = 9x^2 + 4x + 5$$

$$f'(2) = 36 + 8 + 5 = 49$$

$$(2, 49)$$

$$y = m \cdot x + b$$

$$43 = 49 \cdot 2 + b$$

$$43 - 98 = b$$

$$b = -45$$

$$y = 49x - 45$$

$$10. f(x) = 3x^3 + 5x^2 - 3x + 4$$

$$f'(x) = 9x^2 + 10x - 3$$

$$f''(x) = 18x + 10$$

$$f'(0) = 9 \cdot 0 + 10 \cdot 0 - 3$$

$$f'(0) = -3,,$$

$$f'(0) + f''(-3)$$

$$-3 - 44$$

$$f''(-3) = 18 \cdot (-3) + 10$$

$$f''(-3) = -54 + 10 = -44,,$$

$$-3 - (-44)$$

$$41$$