

Thesis submitted to obtain the title of Doctor of Philosophy

Doctoral School of Engineering Science Field: Computer Science

### Real-time Soft Tissue Modelling on GPU for Medical Simulation

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### Part I

Introduction

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### MEDICAL SIMULATION

- 1.1 General context and goal: medical training, patientspecific planning and per-operative guidance
- 1.2 Challenges (trade-off between accuracy and real-time)

### SOFT-TISSUE MODELLING

As seen in the previous chapter, realistic modelling of organs' deformation is a challenging research field that opens the door to new clinical applications including: medical training and rehearsal systems, patient-specific planning of surgical procedure and per-operative guidance based on simulation. In all these cases the clinician needs fast updates of the deformation model to obtain a real-time display of the computed deformations. If for medical training devices the haptic feedback from touching organs merely needs to feel real, the accuracy of the information provided to the clinician in the cases of planning or per-operative guidance is crucial. Therefore a substantial comprehension of the mechanics involved and a knowledge of physical properties of anatomical structures are both mandatory in our quest to realistically model organs' deformation. This chapter will first introduce a few necessary basic concepts of continuum mechanics. It will then present the different theoretical models able to describe organs' mechanical behaviours.

### 2.1 Necessary background in continuum mechanics

#### 2.1.1 What is continuum mechanics

In our everyday life matter appears smooth and continuous: from the wood used to build your desk to the water you drink. But this is just illusion. The concept that matter is composed of discrete units has been around for millennia. In fact we know with certainty that our world is composed of microscopic atoms and molecules separated by empty space since the beginning of the twentieth century Lautrup (2005). However, certain physical phenomena can be predicted with theories that pay no attention to the molecular structure of materials. Consider for instance the deformation of the horizontal board of a bookshelf under the weight of the books. The bending of the shelf can be modelled without considering its molecular composition. The branch of physics in which materials are treated as continuous is known as continuum mechanics. In this theory matter is assumed to exist as a continuum, meaning that the matter in the body is continuously distributed and fills the entire region of space it occupies Lai et al. (1996). Whether the approximation of continuum mechanics is justified in a given situation is a matter of experimental test.

Continuum mechanics studies the response of materials to different loading conditions and can be divided into two main parts: general principles common to all media and constitutive equations defining idealised materials.

### 2.1.2 General principles

### 2.1.2.1 Deformation tensor and strain tensor

#### 2.1.2.2 Stress

#### 2.1.3 Idealised materials

So far we have described the state of stress and strain and these concepts are valid for every continuum. However these equations are not sufficient to describe the response of a specific material due to a given loading.

### 2.1.3.1 Constitutive laws

### 2.2 Tissue characterisation

### 2.2.1 Material models for organs (non-linear, visco-elastic and anisotropic)

### 2.2.2 Measure/estimation of model parameters?

# MAIN PRINCIPLES OF FINITE ELEMENT METHOD (OR HOW TO SOLVE EQUATIONS OF CONTINUUM MECHANICS FROM PREVIOUS SECTION)

- 3.1 Discretisation
- 3.2 Derivation of element equations
- 3.3 Assembly of element equations
- 3.4 Solution of global problem

### Part II

Solid organs modelling

STATE OF ART: FEM

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## LINEAR NOT ACCURATE => NON-LINEAR FEM => INTRODUCTION OF TLED

- 5.1 Differences with classic FEM and reasons of its efficiency
- 5.2 Visco-elasticity and anisotropy added (MICCAI 2008; MedIA 2009)

### GPU IMPLEMENTATION OF TLED

- 6.1 What is GPGPU
- 6.2 Re-formulation of the algorithm for its Cg implementation
- 6.3 CUDA implementation/optimisations (ISBMS 2008a)

### IMPLEMENTATION IN SOFA

- 7.1 Presentation of SOFA project and architecture
- 7.2 Implementation in SOFA and TLED released in open-source

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### Part III

Hollow organs modelling

### STATE OF ART: HOLLOW STRUCTURES

- 8.1 Non-physic approaches (computer graphics stuff)
- 8.2 Physically accurate approches (plates/shells)

### $_{\text{CHAPTER}}\,9$

# WHY A SHELL FEM? COLONOSCOPY SIMULATOR PROJECT

- 9.1 Project introduction
- 9.2 Mass-spring model for colon implemented on GPU (ISBMS 2008b)

# MORE ACCURATE: A CO-ROTATIONAL TRIANGULAR SHELL MODEL (ISBMS 2010)

- 10.1 Model description
- 10.2 Validation
- 10.3 Application to implant deployment simulation in cataract surgery

### 'SHELL MESHING' TECHNIQUE

(MICCAI 2010)

- 11.1 State of art: reconstruction/simplification
- 11.2 Our method

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### APPLICATIONS TO MEDICAL SIMULATION

- 12.1 Nice medical stuff to show
- 12.2 Interaction solid/hollow organs

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### Part IV

Conclusion

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### References

[Lai et al., 1996] W. Lai, D. Rubin and E. Krempl. *Introduction to Continuum Mechanics*. Butterworth-Heinemann, third ed., 1996.

[Lautrup, 2005] B. Lautrup. Physics of continuous matter: exotic and everyday phenomena in the macroscopic world. Institute of Physics Publishing, 2005.

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