### UNIVERSITY OF LILLE 1 DOCTORAL SCHOOL OF ENGINEERING SCHOOL

#### PHD THESIS

to obtain the title of

#### PhD of Science

of the University of Lille 1

Specialty: Computer Science

Defended by Olivier COMAS

#### Real-time Soft Tissue Modelling on GPU for Medical Simulation

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#### Contents

Co	onter	nts	i
Ι	Int	roduction	1
1	Med	dical simulation	3
	1.1	General context and goal: medical training, patient-specific planning	
		and per-operative guidance	3
	1.2	Challenges (trade-off between accuracy and real-time)	3
2	One	e key point in medical simulation: soft-tissue modelling	5
	2.1	Necessary background in continuum mechanics	5
		2.1.1 Deformation tensor and strain tensor	5
		2.1.2 Stress and constitutive laws	5
	2.2	Tissue characterisation	5
		2.2.1 Material models for organs (non-linear, visco-elastic and	
		anisotropic)	5
		2.2.2 Measure/estimation of model parameters	5
3	Mai	in principles of Finite Element Method (or how to solve equa-	
	tion	s of continuum mechanics from previous section)	7
	3.1	Discretisation	7
	3.2	Derivation of element equations	7
	3.3	Assembly of element equations	7
	3.4	Solution of global problem	7
II	So	olid organs modelling	9
4	Stat	te of art: FEM	11
5		$ m ear \ not \ accurate => Non-linear \ FEM => Introduction \ of$	
	TLI		13
	5.1	Differences with classic FEM and reasons of its efficiency	13
	5.2	Visco-elasticity and anisotropy added (MICCAI 2008; MedIA 2009) .	13
6	GP	U implementation of TLED	15
	6.1	What is GPGPU	15
	6.2	Re-formulation of the algorithm for its Cg implementation	15
	6.3	CUDA implementation/optimisations (ISBMS 2008a)	15

ii Contents

7	Implementation in SOFA	17
	7.1 Presentation of SOFA project and architecture	17 17
II	Hollow organs modelling	19
8	State of art: hollow structures	21
	8.1 Non-physic approaches (computer graphics stuff)	21 21
	0.2 I hysically accurate approches (plates/shells)	21
9	Colonoscopy simulator project	<b>23</b>
	9.1 Project introduction	23
	9.2 Mass-spring model for colon implemented on GPU (ISBMS 2008b) .	23
10	More accurate: a co-rotational triangular shell model (ISBMS	
	2010)	<b>25</b>
	10.1 Model description	25
	10.2 Validation	25
	10.3 Application to implant deployment simulation in cataract surgery	25
11	'Shell meshing' method (MICCAI 2010)	27
	11.1 State of art: reconstruction/simplification	27
	11.2 Our method	27
<b>12</b>	Applications to medical simulation	29
	12.1 Nice medical stuff to show	29
	12.2 Interaction solid/hollow organs	29
ΙV	Conclusion	31
R	ferences	33

### Part I Introduction

#### Medical simulation

- 1.1 General context and goal: medical training, patientspecific planning and per-operative guidance
- 1.2 Challenges (trade-off between accuracy and real-time)

### One key point in medical simulation: soft-tissue modelling

- 2.1 Necessary background in continuum mechanics
- 2.1.1 Deformation tensor and strain tensor
- 2.1.2 Stress and constitutive laws
- 2.2 Tissue characterisation
- 2.2.1 Material models for organs (non-linear, visco-elastic and anisotropic)
- 2.2.2 Measure/estimation of model parameters

# Main principles of Finite Element Method (or how to solve equations of continuum mechanics from previous section)

- 3.1 Discretisation
- 3.2 Derivation of element equations
- 3.3 Assembly of element equations
- 3.4 Solution of global problem

## Part II Solid organs modelling

CHAPTER 4

State of art: FEM

## $\begin{array}{c} {\rm Linear~not~accurate} => \\ {\rm Non\text{-}linear~FEM} => {\rm Introduction} \\ {\rm of~TLED} \end{array}$

- 5.1 Differences with classic FEM and reasons of its efficiency
- 5.2 Visco-elasticity and anisotropy added (MICCAI 2008; MedIA 2009)

#### GPU implementation of TLED

- 6.1 What is GPGPU
- 6.2 Re-formulation of the algorithm for its Cg implementation
- 6.3 CUDA implementation/optimisations (ISBMS 2008a)

#### Implementation in SOFA

- 7.1 Presentation of SOFA project and architecture
- 7.2 Implementation in SOFA and TLED released in open-source

## Part III Hollow organs modelling

#### State of art: hollow structures

- 8.1 Non-physic approaches (computer graphics stuff)
- 8.2 Physically accurate approches (plates/shells)

#### Colonoscopy simulator project

- 9.1 Project introduction
- 9.2 Mass-spring model for colon implemented on GPU (ISBMS 2008b)

## More accurate: a co-rotational triangular shell model (ISBMS 2010)

- 10.1 Model description
- 10.2 Validation
- 10.3 Application to implant deployment simulation in cataract surgery

### 'Shell meshing' method (MICCAI 2010)

- 11.1 State of art: reconstruction/simplification
- 11.2 Our method

#### Applications to medical simulation

- 12.1 Nice medical stuff to show
- $12.2 \quad Interaction \ solid/hollow \ organs$

### Part IV Conclusion

#### References