## CES-27 Processamento Distribuído

**Deadlock Detection** 

### Outline

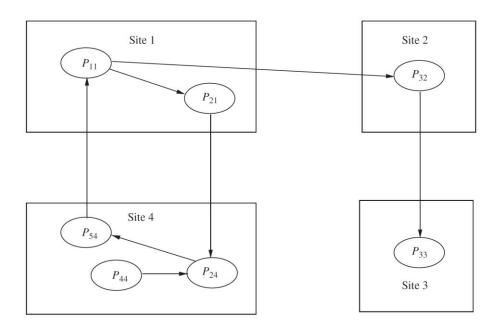
- Deadlock
- Prevention
- Detection
- Chandy-Misra-Haas for AND
- Chandy-Misra-Haas for OR

### Definition

- **Permanent** blocking of a set of processes that compete for system resources (database records, communication lines, etc.)
  - Deadlock occurs when a set of processes are in a wait state
  - Each process is waiting for a resource held by some other waiting process
  - Therefore, all deadlocks involve conflicting resources needs by two or more processes
- 1971 Coffman conditions: four necessary conditions for deadlock
  - Mutual Exclusion: processes require exclusive control of its resources (not sharing)
  - Hold and Wait: process holds some resources and waits for other resources, before it can finish the job
  - No Pre-emption: process will not give up a granted resource, voluntarily and by another process, until it is finished with it
    - Preemption: act of temporarily interrupting a task, without its cooperation, and with the intention of resuming it later
  - Circular Wait: each process in the chain holds a resource requested by another

# Example of Deadlock

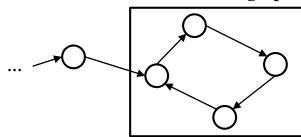
- The state of a distributed system can be modeled by a Wait-For Graph (WFG)
- WFG is a directed graph where nodes are processes and edges P1  $\rightarrow$  P2 represents that P1 is blocked because it is waiting for P2 to release some resource
  - Attention: P44 and P33 are not waiting for other processes in the graph, so they should not be blocked by definition. However, many references consider that they are blocked and it may lead to misunderstandings



### Conventions for WFG

- In this material, consider these conditions:
  - Blocked process (not filled): it is waiting for some resource, i.e., it must have at least one outgoing edge
  - Active process (filled): it has a resource that it will release in the future
  - Blocked subgraph (dashed circle and not filled): it represents a subgraph where all processes are blocked and waiting for the other processes, i.e., a deadlock
    - Blocked process, waiting for other process
    - Active process, it can release resources
    - Blocked subgraph, i.e., the subgraph is in deadlock

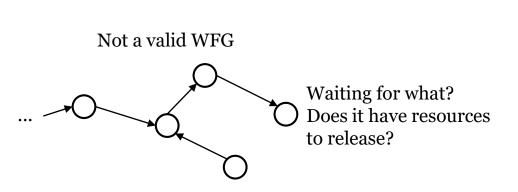
#### Blocked subgraph

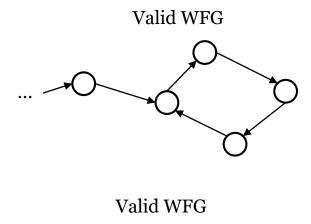




### Conventions for WFG

- Result: A WFG graph cannot have a blocked process without at least one outgoing edge
- In other materials, if you see a WFG like the one below (not a valid WFG)
  with an end (leaf) node without outgoing edge, check the semantic of this
  node
  - It can be an active process that will release resources, or
  - It can be a deadlocked subgraph like the two examples on the right below
- See additional material, in the end, for a discussion about it





# Deadlock Handling Strategies

- Dealing with deadlock may be very difficult, especially in distributed systems
- Ignoring deadlock is a surprisingly common approach
  - Yes, the system will crash
- Ostrich Algorithm
  - "stick one's head in the sand and pretend there is no problem"
- Reasonable if deadlocks occur very rarely or cost of prevention is very high
  - Trade off between convenience and correctness
- According to many sources
  - Unix, Linux and Windows take this approach for some of the more complex resource relationships to manage
  - Is it fake? I don't know © (tell me if you discover it)
  - At least for previous versions, it looks like it is true

# Ostrich Approach



# Ostrich Approach (São Paulo)

Proud of São Paulo for using the same engineering best practices than Unix, Linux and Windows!

> Faria Lima x Juscelino Kubitschek 01/15/2008



Fontes: 15/01/2008 [by Silvio Tanaka at Google building]

## SP in all slides of O.S. and D.S.

Faria Lima x Juscelino Kubitschek 02/02/2017

Note: I can't stand waiting for January/February of 2019

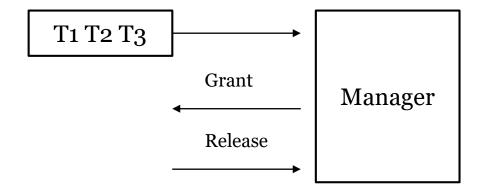


# Deadlock Handling Strategies

- Prevention (pessimistic approach): design the system with restrictions so that deadlock is impossible a priori
  - e.x. compile-time/statically, by design
  - Conservative but it can limit access to resources and impose so much restrictions on processes (reduced throughput)
- Avoidance: resources are granted only if the global state is safe; a request may be denied
  - run-time/dynamically, before it happens
  - Main difference: this approach keeps all necessary conditions for deadlock, but it makes dynamically decisions that are free of deadlocks
  - It requires the global state of the system (done by a mutual exclusion for safe checking) in order to check for safe states
    - Each process has to store the knowledge of all processes, which implies on large capacity of storage and traffic over the network for D.S.
  - Not a very practical solution due to a lot of problems
- Detection & Recovery (optimistic approach): let the deadlock occur, detect it, then recover it
  - run-time/dynamically, after it happens
  - Usual approach for D.S.

### Deadlock Avoidance

- Centralized deadlock avoidance
  - Central unit knows everything and control all processes
- Banker's Algorithm
  - We will not see it



"Years" in idle state or multithreading idea

### Outline

- Deadlock
- Prevention
- Detection
- Chandy-Misra-Haas for AND
- Chandy-Misra-Haas for OR

#### **Deadlock Prevention**

- One of the four necessary conditions (Coffman) is broken
- Mutual Exclusion
  - Systems with only simultaneously shared resources (readonly) is generally not possible or very restricted
  - Not a good approach
- Hold and Wait
  - Disallow waiting while holding resources, i.e., a process can only request a resource if it does not hold any others;
  - Non-waiting requests, i.e., a request that cannot be satisfied immediately will fail;
  - Or, request all required resources at once before execution begins, i.e., it holds nothing while waiting and takes all or nothing

#### **Deadlock Prevention**

- One of the four necessary conditions (Coffman) is broken
- No Preemption
  - If a process is denied access to a resource, then it must release all resources it currently held;
  - Preempted resources (taken way) from a process are added to its waiting list;
  - Process restarts only when can regain all resources it requested
  - This approach may imply on rollbacks or return errors
- Circular Wait
  - The classic approach

#### First Prevention Solution

- Example of resource ordering: assign a total ordering on all the resources, then allow a process to request resources only in increasing order (Direct Acyclic Graph)
  - If a process requested the resource type A, then it may subsequently request only those following A in the ordering
- Requests
  - P1(a), P1(b), P1(f)
  - P2(b), P2(d), P2(e)
  - P3(d), P3(e)
- If P1 has just a, P2 cannot get b
  - P1 can request b
- If P1 has a, b, and f, then P3 can get d
  - P1 cannot request c, d and e
- Very restrictive solution

- Example of central prevention by avoiding circular wait
- Tasks (Processes/Transactions) declare the resources they need

```
T1: x, yT2: y, zT3: z, x
```

- In this case, we will use the relation  $\Rightarrow$  (potentially block)
  - If  $A \Rightarrow B$ , then A potentially block B
- Tasks arrive in this order: T1, T2, T3
- Possible resource scheduling

```
□ O(1,x), O(2,y), O(3,z), i.e., x to T1, y to T2, z to T3
□ O(1,x): T1 \Rightarrow T3
□ O(1,x), O(2,y): T2 \Rightarrow T1 \Rightarrow T3
□ O(1,x), O(2,y), O(3,z): T3 \Rightarrow T2 \Rightarrow T1 \Rightarrow T3 (cycle)
```

- Dynamically prevention of deadlock
  - Besides z is available, O(3,z) is blocked because it creates a cycle
- This approach usually congests the manager if the distributed system is large

- In a distributed solution, each site Si has some resources and knows just the dependences of them
  - In this example the site Sa has the resource a
- Requests
  - □ T1: x, y
  - □ T2: y, z
  - □ T3: z, x

Sx	Sy	Sz
T1	T1	T2
Т3	T2	Т3

- Resource scheduling
  - O(1,x), O(2,y), O(3,z), i.e., x to T1, y to T2, x to T3
  - O(1,x) at  $Sx: T1 \Rightarrow T3$
  - O(2,y) at Sy:  $T2 \Rightarrow T1$
  - $^{\circ}$  O(3,z) at Sz: T3 ⇒ T2 (it cannot prevent deadlock)
- Consider a total ordering of the requests (ex. using logical clock)
  - It means that there are no equal timestamps
  - TSi is the timestamp of Ti
  - Ti can be executed before Tj iff (TSi < TSj)</li>

- Distributed solution with total ordering by logical clocks
- Requests
  - T1: x, yT2: y, zT3: z, x
- Resource scheduling
  - O(1,x), O(2,y), O(3,z), i.e., x to T1, y to T2, x to T3
  - Timestamps: TS1<TS2<TS3 imposes T1 before T2 before T3</li>
  - O(1,x) at Sx: TS1<TS3 and T1  $\Rightarrow$  T3
  - $\circ$  O(2,y) at Sy: TS1<TS2 but T2 ⇒ T1 (potential cycle)
  - O(3,z) at Sz: TS2<TS3 but T3  $\Rightarrow$  T2 (potential cycle)
- O(2,y) is not allowed because T2  $\Rightarrow$  T1, and this would create a potential cycle once TS1<TS2
- Same for O(3,z)

- The previous approach is very restrictive, but we may "improve" it
- Another approach is not to block the tasks, but rollback them when a conflict occur
  - In this case, just the timestamps are sufficient
  - No resource declaration is used
- Two main approaches of prevention
  - Wait-Die(no preemption): An older task (higher priority) is allowed to wait, and a younger is aborted
  - Wound-Wait(preemption): An older task causes the preemption (abort) of a younger one, and a younger is allowed to wait
- New timestamps may cause starvation

```
Wait-Die (no preemption): Ti→Tj(resource)

if TSi < TSj
    block Ti // wait

else
    // restart Ti (same timestamp)

Wound-Wait (preemption): Ti→Tj(resource)

if TSi < TSj
    abort Tj // wound
    // restart Tj (same timestamp)

else
    block Ti // wait</pre>
```

### Outline

- Deadlock
- Prevention
- Detection
- Chandy-Misra-Haas for AND
- Chandy-Misra-Haas for OR

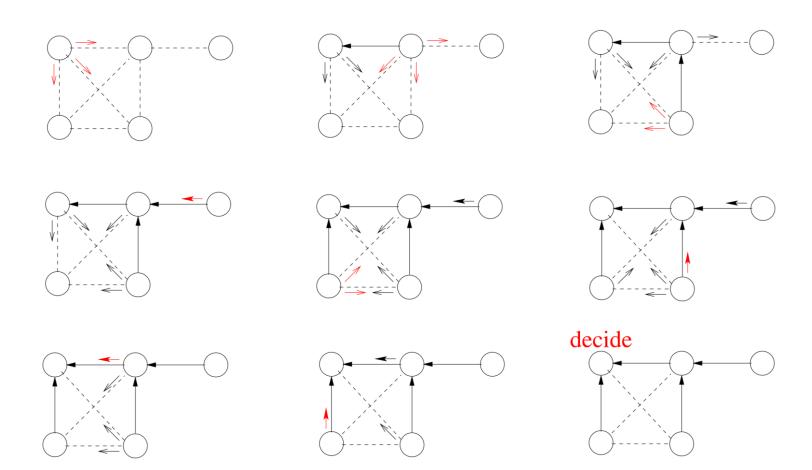
#### **Detection Solutions**

- 1987 Knapp's Classification: distributed deadlock detection algorithms can be divided into four classes
  - Path-pushing
    - Build a global WFG for each site of the distributed system
    - During a detection, each site sends its local WFG to all the neighboring sites; After a update, the new WFG is then passed along to other sites until one site has a sufficiently complete picture of the global state to announce or not a deadlock
  - Edge-chasing
    - It detects cycles in a distributed system by propagating special messages called *probes* along the edges of the WFG
    - The formation of a cycle is detected by a site if it receives the matching *probe* sent by it previously (probe messages are usually small)

#### **Detection Solutions**

- 1987 Knapp's Classification: distributed deadlock detection algorithms can be divided into four classes
  - Diffusing computation-based
    - It detects deadlock by sending echo messages along the WFG, i.e., computation is diffused through the WFG
    - Active processes ignore the diffusion (example in the next slide)
  - Global state detection
    - A deadlock in a distributed system is a stable property that holds at any moment
    - This approach takes a snapshot of the distributed system and check for the deadlock

# Echo Messages



Fontes: Deadlock [Kshemkalyani, Singhal]

#### Models of Deadlock

#### AND deadlock (resource)

 Blocked until all resources requested by the process is granted, i.e., it can continue the computation just with all resources (e.g. transactions)

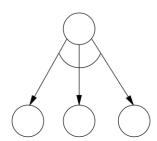
#### OR deadlock (communication)

 Blocked untill any of the resources requested by the process is granted, i.e., it can continue the computation with just one resource (e.g. waiting for work messages)

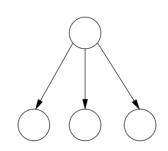
#### P-out-of-Q deadlock

- General case, blocked until P resources of Q requests is granted
- It is the OR model when P=1, and AND model when P=Q

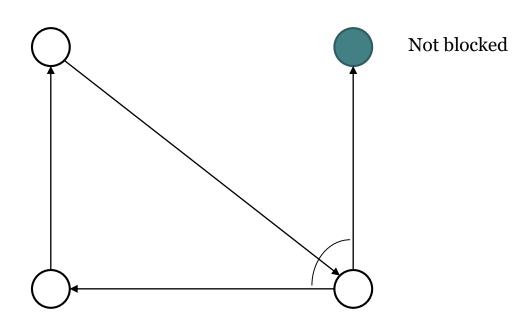
#### P-out-of-Q WFG representation



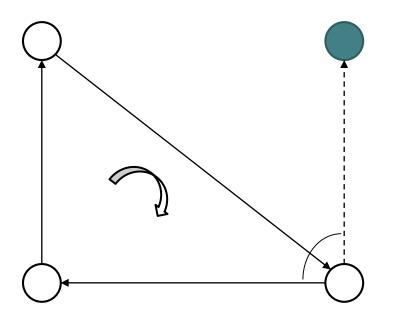
AND (3-out-of-3) request



OR (1-out-of-3) request



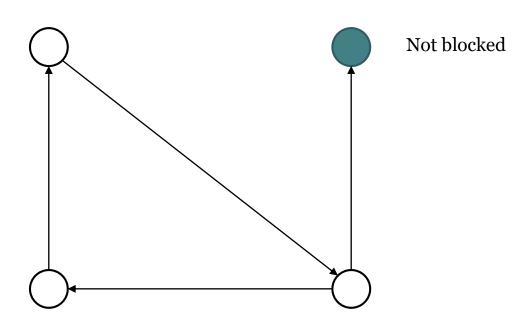
Static analysis of an AND-deadlock by reduction of a WFG snapshot

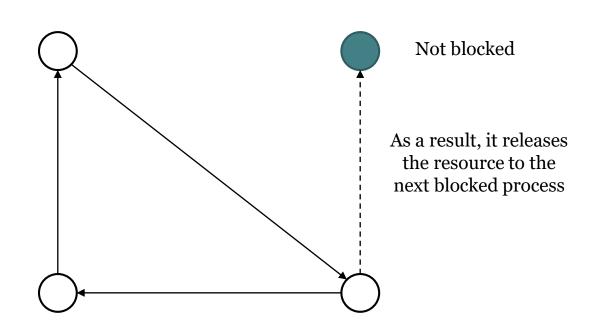


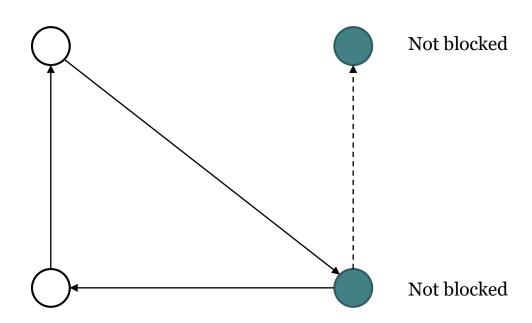
Not blocked

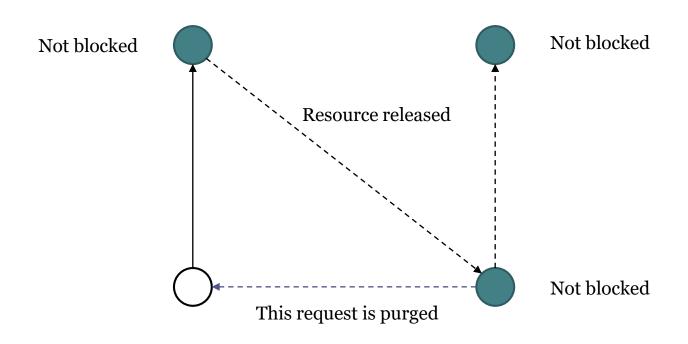
Still blocked because it needs all requested resources

A cycle in an AND model results in deadlock

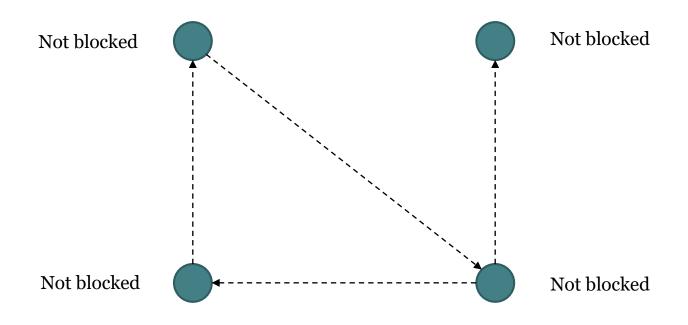








Static analysis of an OR-deadlock by reduction of a WFG snapshot



No deadlock! A cycle is not a sufficient condition for models: OR and P-out-of-Q

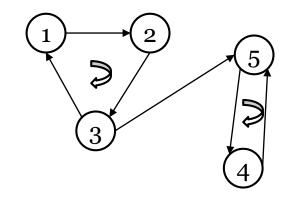
#### Knot

- Knot is a sufficient condition to OR and P-out-of-Q
- Ri is the reachable set of Pi
  - Set of all processes there is a path from Pi
- A nonempty set of process S is said to be a knot, if
  - $\neg \forall Pi \in S \text{ are blocked}$
  - $Pi \in S \text{ iff } \forall Pj \in Ri \rightarrow Pi \in Rj$ 
    - · i.e., every process reached from a process Pi of a knot also reaches Pi
  - There is no grant message (releasing of resource) over the network among these processes

```
R1={P2,P3,P1,P5,P4}
R2={P3,P1,P2,P5,P4}
R3={P1,P2,P3,P5,P4}
R4={P5,P4}, R5={P4,P5}
```

S={P1,P2,P3} is not a knot (deadlock) because P5 is in R1, R2, R3, but P5 does not reach P1, P2 and P3

S={P4,P5} is a knot (deadlock) because P4 is reachable from each one in R4 and P5 is reachable from each one in R5 Two cycles (two AND deadlock)



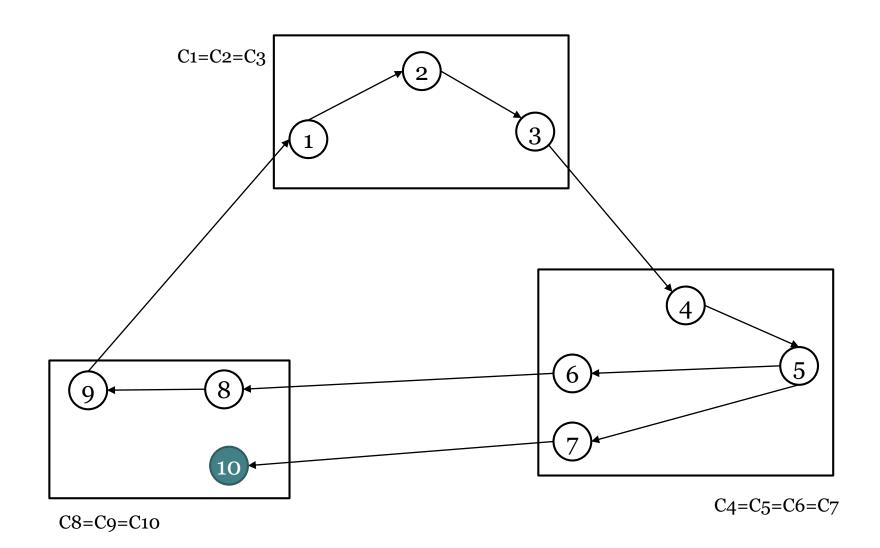
### Outline

- Deadlock
- Prevention
- Detection
- Chandy-Misra-Haas for AND
- Chandy-Misra-Haas for OR

## Chandy-Misra-Haas AND

- 1983 Chandy, Misra, Haas, "Distributed Deadlock Detection", ACM TOCS, vol. 1, no 2, May 1983.
- Algorithm for the AND model (edge-chasing)
  - Resource deadlock detection
- There are some mechanism to deal with local deadlocks
  - Consider n processes P1, P2, ... Pn in a single site/controller
  - $^{□}$  P1 is locally dependent if P1  $\rightarrow$  P2  $\rightarrow$  ... Pn and Pn  $\rightarrow$  P1
- Sites Ci may have more than one process Pi
  - Single site Ci can have more than one label (reference)
  - Ex.: if Pi and Pj are inside Ck, then Ck=Ci=Cj is a single site
- The algorithm detects if a blocked process is deadlocked among different sites/controllers with a partial view of the WFG

# Chandy-Misra-Haas AND



- It uses a special message called *probe*, which is a triplet (i, j, k), denoting that it belongs to a deadlock detection initiated for process Pi and it is being sent by the home site of process Pj to the home site of process Pk
  - Probe messages travel among sites along the edges of the global WFG graph

#### Data Structures

- Processes Pk have a boolean array: dependent[k,i]
- dependent[k,i]=true if Ck knowns that  $Pi \rightarrow Pk$
- Initially, dependent[k,i]=false for all k, i

#### Summary

- A cycle in WFG is sufficient to detect an AND-deadlock
- A deadlock for Pi is detected when a probe message returns to the initial process Pi

```
Start from Pi (site Ci):
    if Pi is locally dependent
        declare deadlock
    else ∀ Pj, Pk: Pi → Pj → Pk, Pj ∈ Ci, Pk ∉ Ci
        send probe(i,j,k) to site Ck (Pk)
```

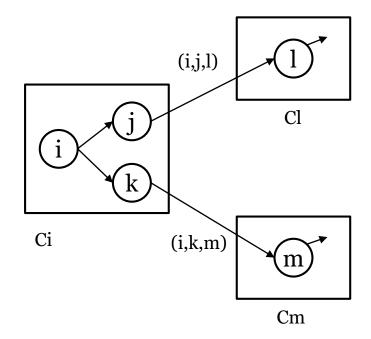
Another mechanism deal with local deadlocks

```
Start from Pi (site Ci):
    if Pi is locally dependent
        declare deadlock
    else ∀ Pj, Pk: Pi → Pj → Pk, Pj ∈ Ci, Pk ∉ Ci
        send probe(i,j,k) to site Ck (Pk)
```

Another mechanism deal with local deadlocks

A blocked process (task) Pi starts deadlock detection in Ci

Ci sends probe(i,j,k) messages to all dependent sites Ck



```
Start from Pi (site Ci):
   if Pi is locally dependent
      declare deadlock
   else ∀ Pj, Pk: Pi → Pj → Pk, Pj ∈ Ci, Pk ∉ Ci
      send probe(i,j,k) to site Ck (Pk)
```

Active Pk:
 dependent[k,i] = false

When a process Pk becomes active (receive the resource), it does not wait for other process; so, its boolean array is cleared

```
Start from Pi (site Ci):
   if Pi is locally dependent
       declare deadlock
   else \forall P_i, P_k : P_i \rightarrow P_i \rightarrow P_k, P_i \in C_i, P_k \notin C_i
       send probe(i,j,k) to site Ck (Pk)
Receiving probe(i,j,k) (site Ck):
   if (
     Pk is blocked/idle,
     dependent[k,i] = false, and
     Pk has not replied to all requests Pi
       dependent[k,i] = true
       if k=i
           declare Pi as deadlocked
       else \forall Pm, Pn : Pk \rightarrow Pm \rightarrow Pn, Pm \in Ci, Pn \notin Ci
           send probe(i,m,n) to site Cn (Pn)
Active Pk:
   dependent[k,i] = false
```

When a process Pk receives probe(i,j,k), it ignores the probe if it is active

It forwards the detection if it is the first time that the detection from i reaches Pk i.e. Now, Pk knows that  $Pi \rightarrow Pk$ 

```
Start from Pi (site Ci):
   if Pi is locally dependent
       declare deadlock
   else \forall P_i, P_k : P_i \rightarrow P_i \rightarrow P_k, P_i \in C_i, P_k \notin C_i
       send probe(i,j,k) to site Ck (Pk)
Receiving probe(i,j,k) (site Ck):
   if (
     Pk is blocked/idle,
     dependent[k,i] = false, and
     Pk has not replied to all requests Pj
                                                                     During the forward
                                                                     1 – mark the dependence
       dependent[k,i] = true
                                                                     discovered: Pi \rightarrow Pk
       if k=i
           declare Pi as deadlocked
       else \forall Pm, Pn : Pk \rightarrow Pm \rightarrow Pn, Pm \in Ci, Pn \notin Ci
           send probe(i,m,n) to site Cn (Pn)
Active Pk:
   dependent[k,i] = false
```

```
Start from Pi (site Ci):
   if Pi is locally dependent
       declare deadlock
   else \forall P_i, P_k : P_i \rightarrow P_i \rightarrow P_k, P_i \in C_i, P_k \notin C_i
       send probe(i,j,k) to site Ck (Pk)
Receiving probe(i,j,k) (site Ck):
   if (
    Pk is blocked/idle,
     dependent[k,i] = false, and
     Pk has not replied to all requests Pi
       dependent[k,i] = true
       if k=i
           declare Pi as deadlocked
       else \forall Pm, Pn : Pk \rightarrow Pm \rightarrow Pn, Pm \in Ci, Pn \notin Ci
           send probe(i,m,n) to site Cn (Pn)
Active Pk:
   dependent[k,i] = false
```

During the forward

1 − mark the dependence
discovered: Pi → Pk

2 − forward the detection to new
sites (more than one send may
occur)

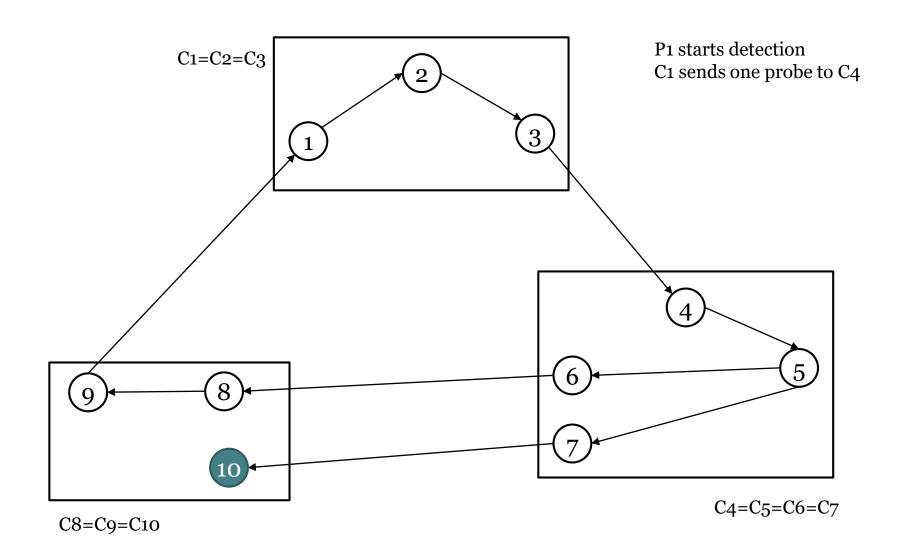
```
Start from Pi (site Ci):
   if Pi is locally dependent
       declare deadlock
   else \forall P_i, P_k : P_i \rightarrow P_i \rightarrow P_k, P_i \in C_i, P_k \notin C_i
       send probe(i,j,k) to site Ck (Pk)
Receiving probe(i,j,k) (site Ck):
   if (
    Pk is blocked/idle,
    dependent[k,i] = false, and
    Pk has not replied to all requests Pi
       dependent[k,i] = true
       if k=i
           declare Pi as deadlocked
       else \forall Pm, Pn : Pk \rightarrow Pm \rightarrow Pn, Pm \in Ci, Pn \notin Ci
           send probe(i,m,n) to site Cn (Pn)
Active Pk:
   dependent[k,i] = false
```

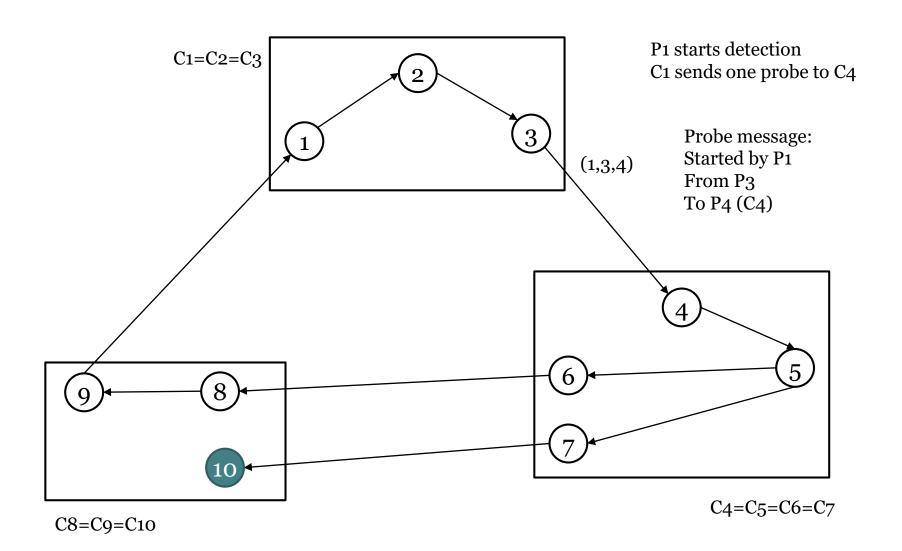
During the forward

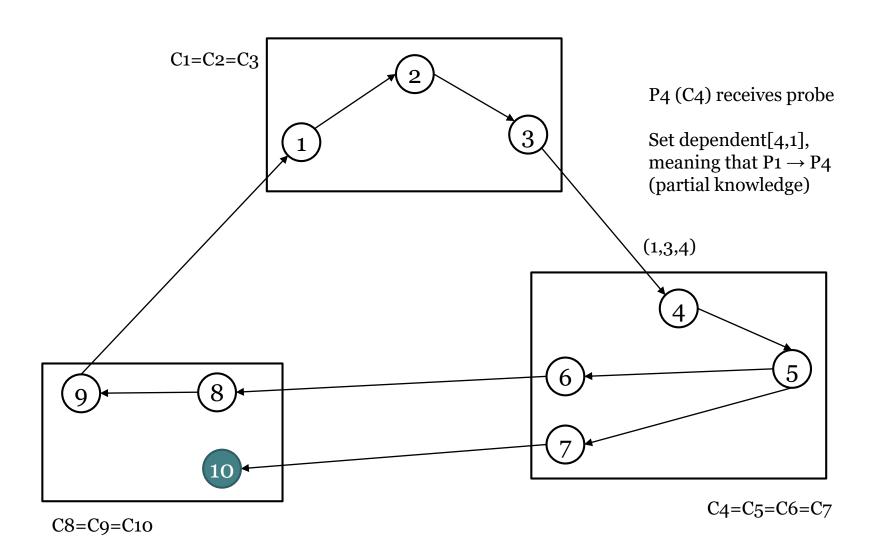
1 – mark the dependence
discovered: Pi → Pk

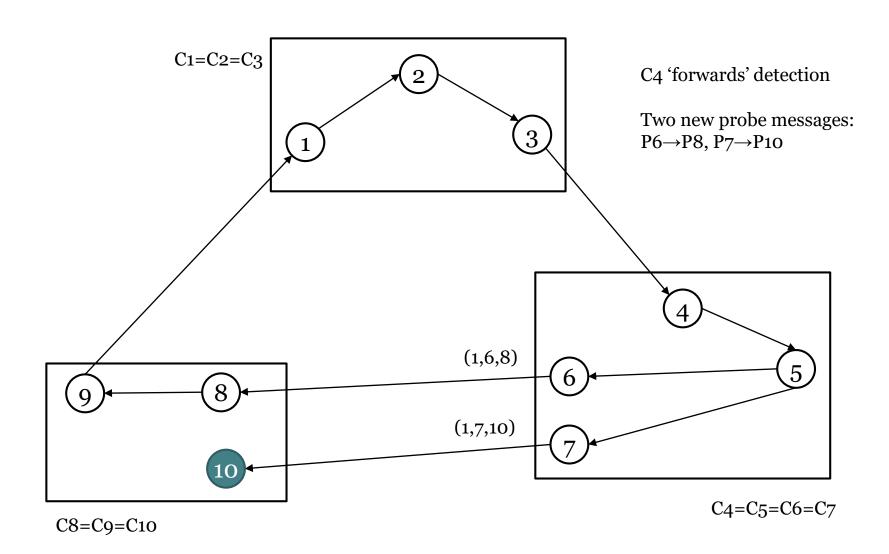
2 – forward the detection to
new sites (more than one send
may occur)

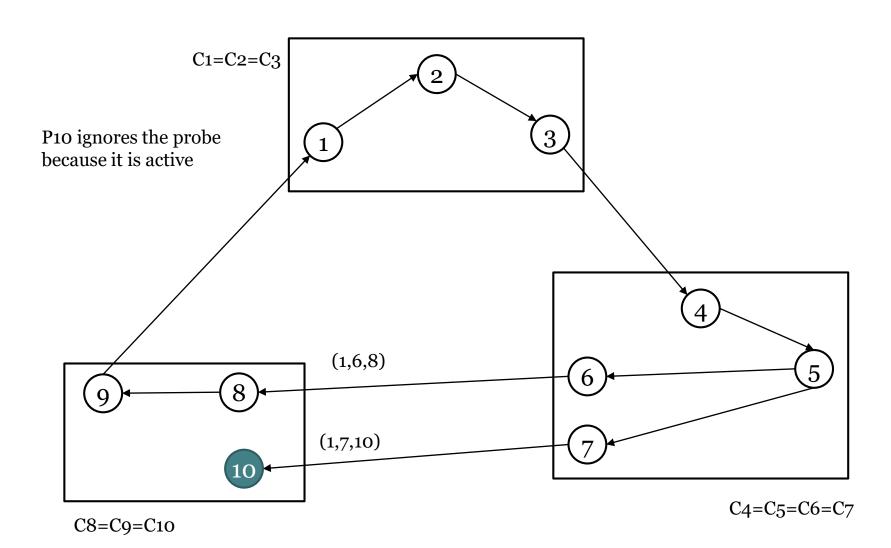
Deadlock, when a probe completes a cycle (return to origin)

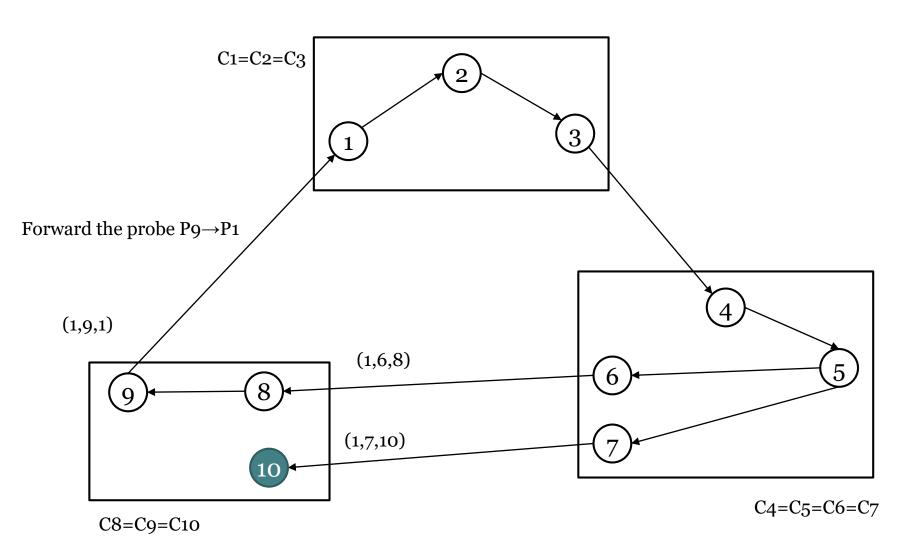


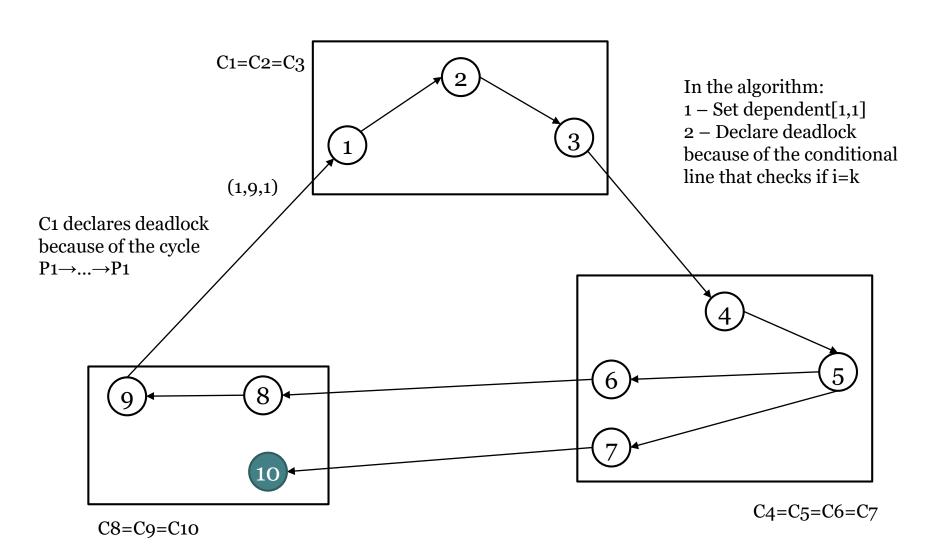




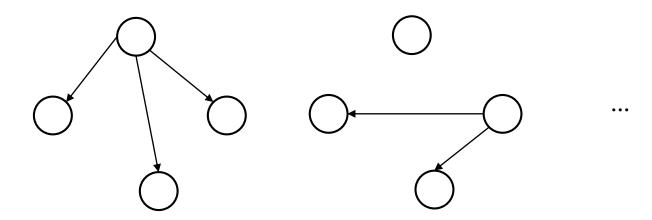








- One probe message (per detection initiation) is sent on every edge of a cycle of the WFG among different sites
- Delay of the deadlock detection is O(n)
- According to Mikhail Nesterenko, Kshemkalyani & Singhal:
  - Consider that there is at least one site per process in deadlock
  - If a process is waiting for n-1 other process, and
  - The next process is waiting for n-2 other process, and
  - The next process is waiting for n-3 other process, and
  - ...
  - Then, the worst case is n(n-1)/2 messages:  $O(n^2)$



- After the detection of deadlock by Pi, Pi may kill itself breaking the cycle
- Now, consider that all processes start deadlock detection at the same time. What will happen?
  - i.e., for *n* processes, there are *n* probe messages traveling on the cycle

- After the detection of deadlock by Pi, Pi may kill itself breaking the cycle
- Now, consider that all processes start deadlock detection at the same time. What will happen?
  - i.e., for *n* processes, there are *n* probe messages traveling on the cycle
- Mass suicide!
- We may include the largest or smallest process ID within the probe during the cycle
- Smarter solutions can kill the process with more cycles, thus reducing the side effect

#### Outline

- Deadlock
- Prevention
- Detection
- Chandy-Misra-Haas for AND
- Chandy-Misra-Haas for OR

- 1983 Chandy, Misra, Haas, "Distributed Deadlock Detection", ACM TOCS, vol. 1, no 2, May 1983
- Algorithm for the OR model (diffusing)
  - Communication deadlock detection
- The algorithm detects if a blocked process is deadlocked with a diffusion on the WFG
- Any blocked process may start the detection: root of the diffusion computation
- Two types of messages are used in this diffusion computation:
  - Query(i,m,j,k): the m-th query (detection) initiated by Pi, sending from Pj to Pk
  - Reply(i,m,k,j): reply from Pk to Pj referring to the query(i,m,j,k) of Pj

#### Summary

- A blocked process Pi starts the detection by sending query messages to all processes it is waiting for: set WFi
- Active processes ignore all messages: query and reply
- Each blocked process Pj forwards a new query (detection)
   and reply to a repeated query
  - If forwarded again, the algorithm never finishes
- When a blocked process Pj receives all pending replies, it can also reply, once all processes below them in the diffusion tree also replied, i.e., they are all blocked and waiting for resources
  - If Pj is the root of the diffusion, it declares deadlock

- Data Structures
- Each process Pk has four arrays of size *n* (for a total of *n* process)
  - latest[i]: highest m of all queries(i,m,j,k) (initially zero)
  - engager[i]: register the process to reply (initially any value). It is j if Pj is responsible for latest[i],  $i \neq j$
  - num[i]: number of pending replies (initially zero), i.e., amount of queries(i,m,k,j) sent by Pk less replies(i,m,j,k) received by Pk
  - wait[i]: check if Pk did not wake up (initially false); true iff Pk is waiting (blocked) since the last update of lasted[i]
- Note: engager[i] and num[i] register information of the diffusion tree
- Note: An engaging query is the first m-th query(i,m,j,k) received by Pk for the detection initiated by Pi

```
Start from Pi:
    latest[i]++; m=latest[i]
    wait[i]=true; num[i]=|WF<sub>i</sub>|
    ∀ Pj ∈ WF<sub>i</sub>: send query(i,m,i,j)

Active Pk:
    wait[...]=false
    ignore any reply and query
```

A process Pi starts its m-th detection by incrementing latest[i] and setting its position in the array wait

Then, Pi checks the processes it is waiting for and sends query for all of them

Now, num[i] is set with |WFi| pending replies

```
Blocked Pk receives a query(i,m,j,k):
    // if engaging query for Pi
    if (m>latest[i]) {
        latest[i]=m; engager[i]=j
        wait[i]=true; num[i]=|WF<sub>k</sub>|
        ∀ Pr ∈ WF<sub>k</sub>: send query(i,m,k,r)

// if not engaging query
    } else if wait[i] and m=latest[i]
        send reply(i,m,k,j)
```

When a blocked process receives a query message ( $Pi \rightarrow Pj \rightarrow Pk$ )

If it is an engaging query, it forwards the detection:

- save j in engager[i] to reply in the future (parent in the diffusion tree)
- Save the amount of pending replies (num[i]) it must wait before it can reply to its engager[i]

```
Blocked Pk receives a query(i,m,j,k):
    // if engaging query for Pi
    if (m>latest[i]) {
        latest[i]=m; engager[i]=j
        wait[i]=true; num[i]=|WF<sub>k</sub>|
        ∀ Pr ∈ WF<sub>k</sub>: send query(i,m,k,r)

// if not engaging query
    } else if wait[i] and m=latest[i]
        send reply(i,m,k,j)
```

In a knot, directly or indirectly, every process is waiting for all other processes

So, we have to add a boundary condition to stop the forwarding of queries

We stop it by avoiding duplication of forwarding

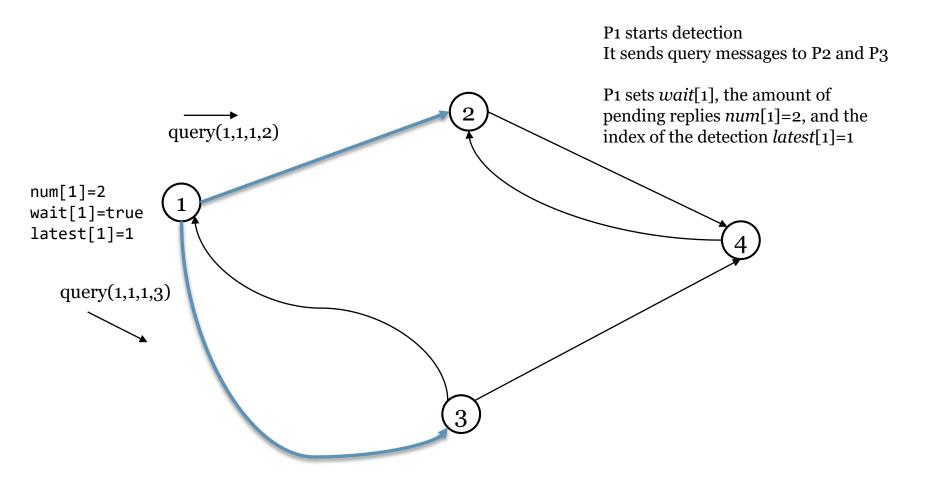
```
Blocked Pk receives a query(i,m,j,k):
   // if engaging query for Pi
   if (m>latest[i]) {
      latest[i]=m; engager[i]=j
      wait[i]=true; num[i]=|WF,|
      \forall Pr \in WF_k: send query(i,m,k,r)
   // if not engaging query
   } else if wait[i] and m=latest[i]
      send reply(i,m,k,j)
Blocked Pk receives a reply(i,m,r,k):
   if wait[i] and m=latest[i]
      num[i]--
      if num[i]=0
         if i=k
            declare Pk as deadlocked
         eLse
            send reply(i,m,k,engager[i])
```

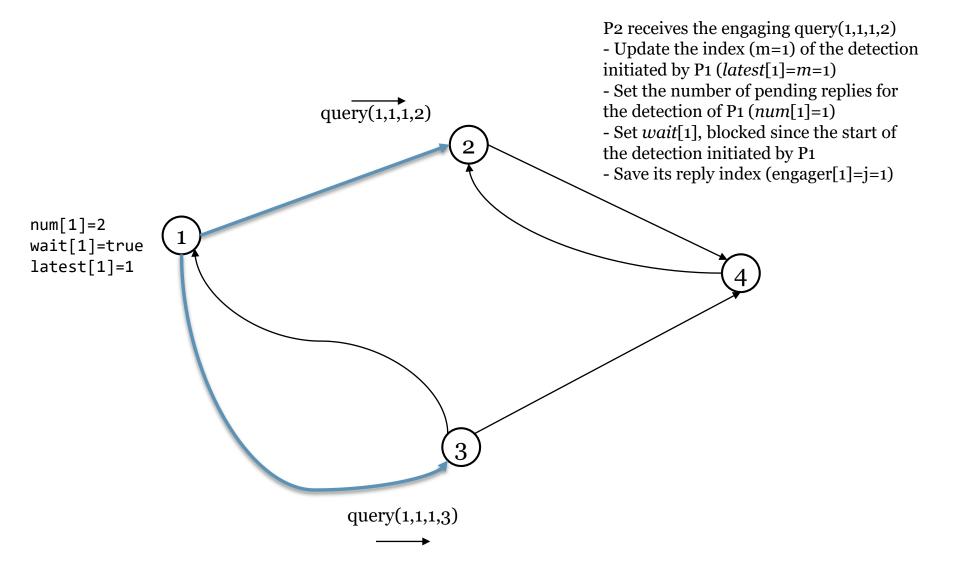
Pk may receive a reply from an old detection initiated by Pi

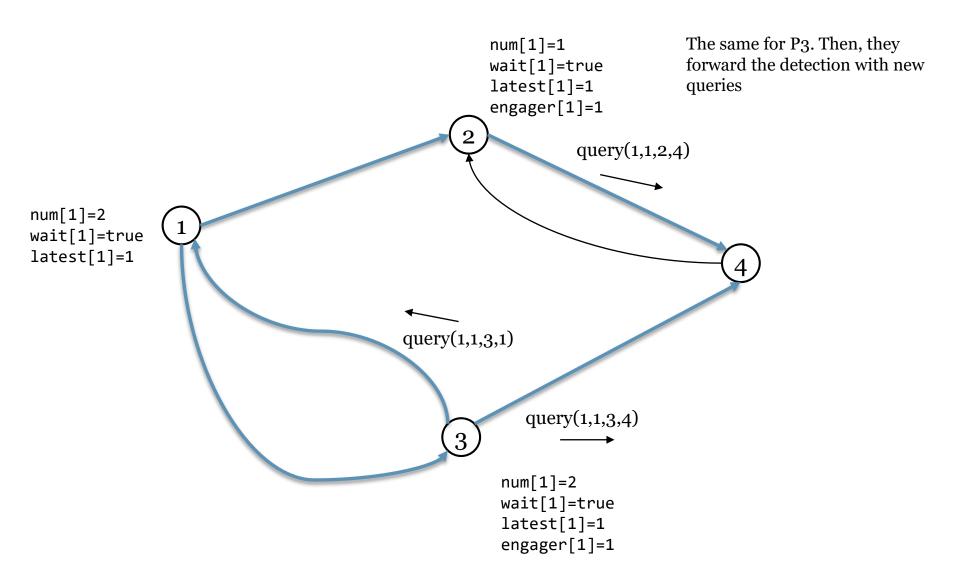
When Pk receives a correct reply (m is equal latest[i]) and it is still blocked

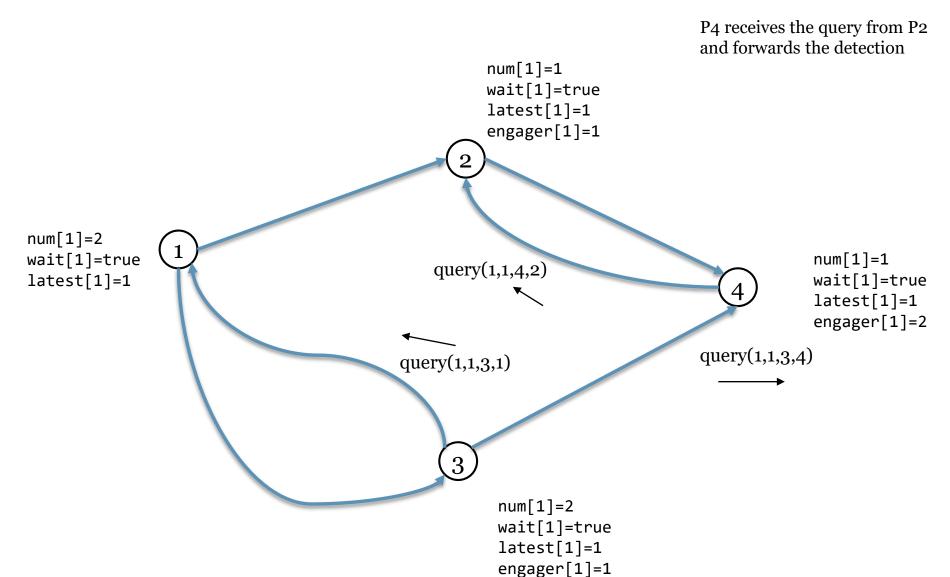
If there is no more pending replies, it sends its reply to engager[i] or declares deadlock if Pk has started the detection

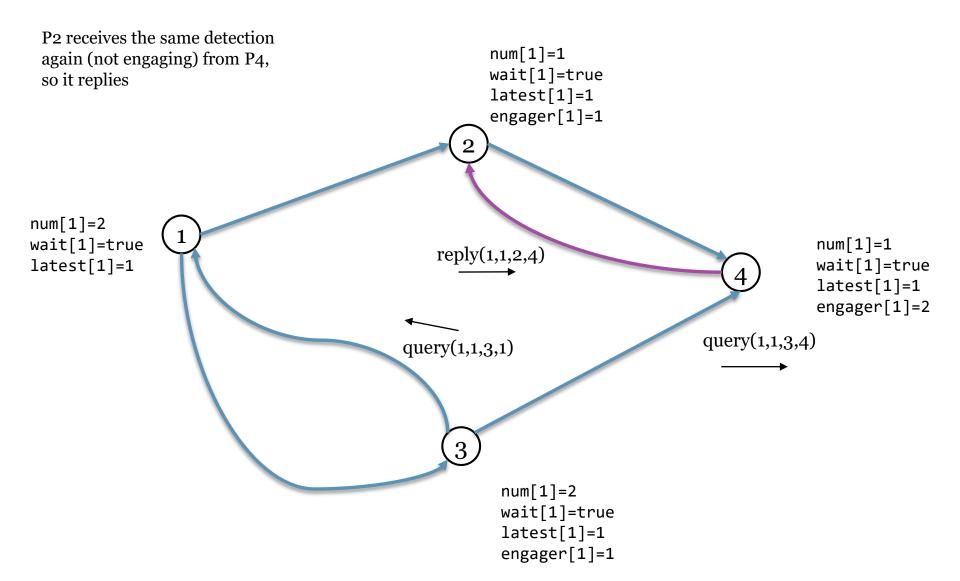
In other words, the processes of the knot in the WTG are blocked and waiting for some resources and there is no active process that will release resources, once active processes ignore queries and do not send replies

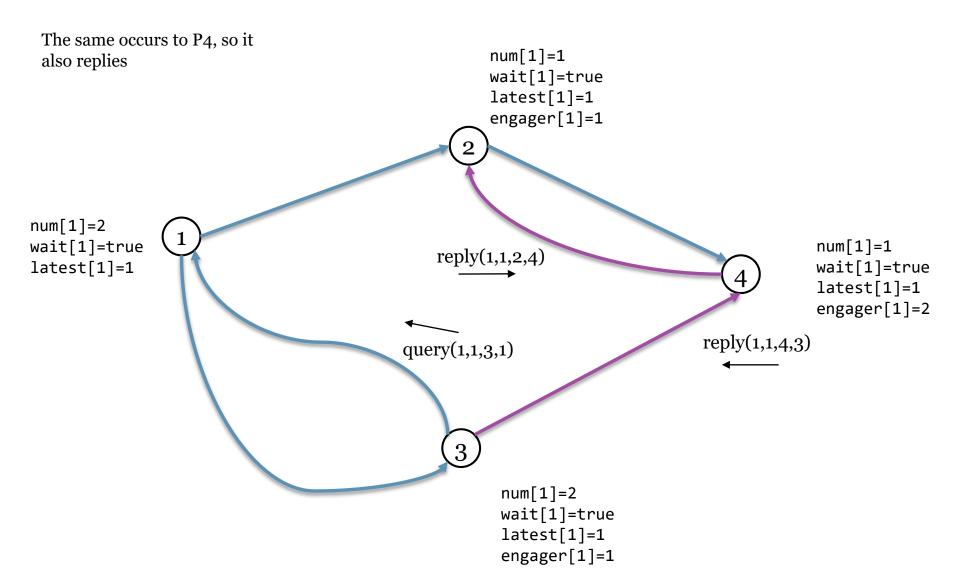


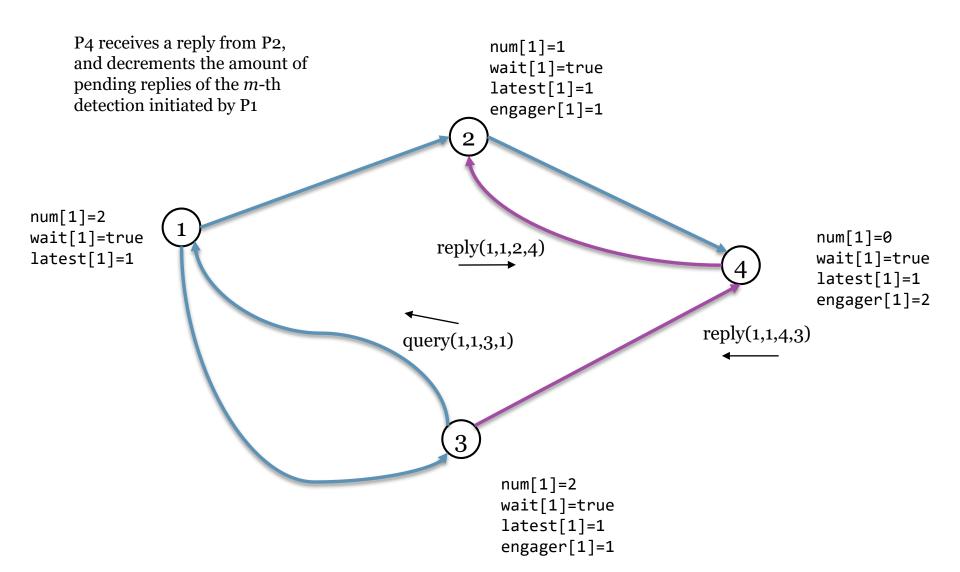


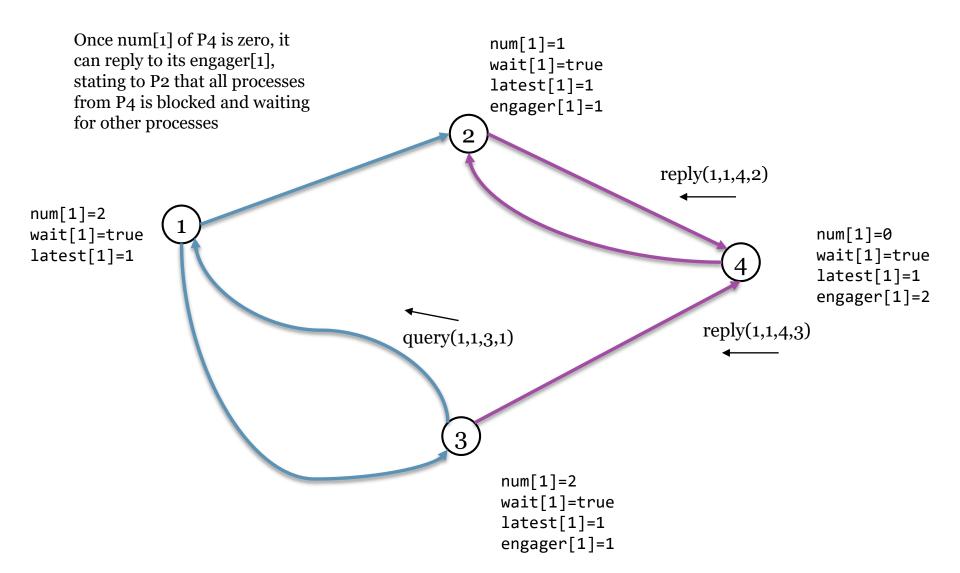


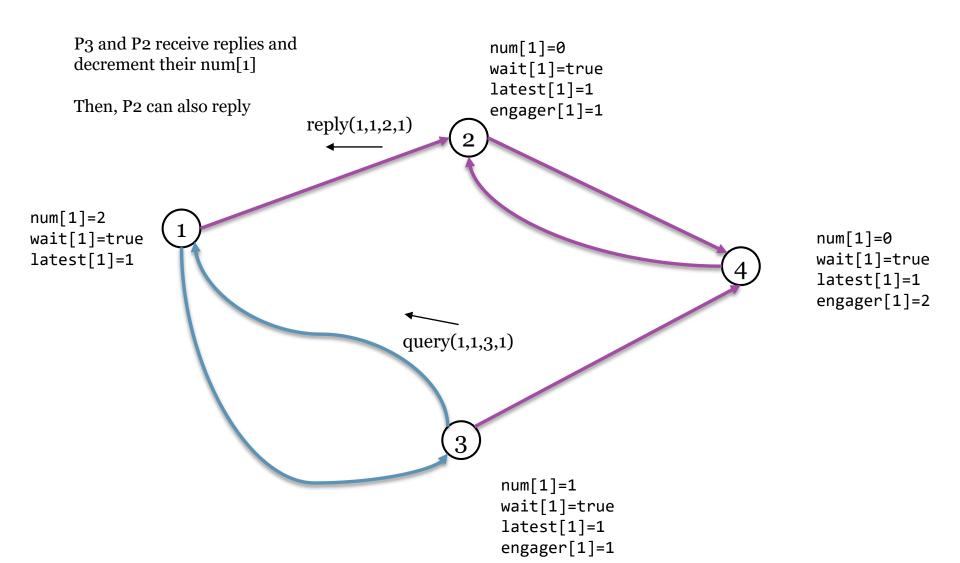


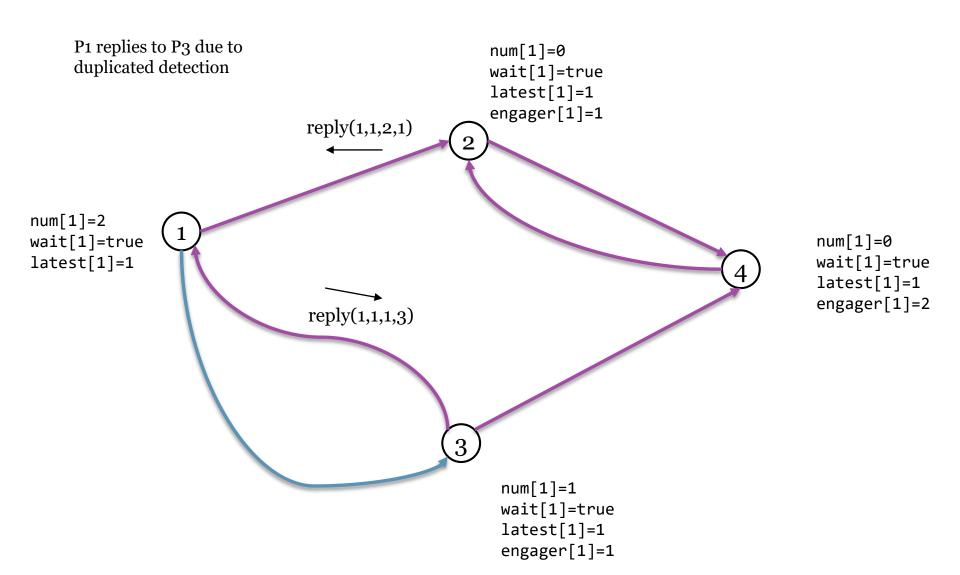


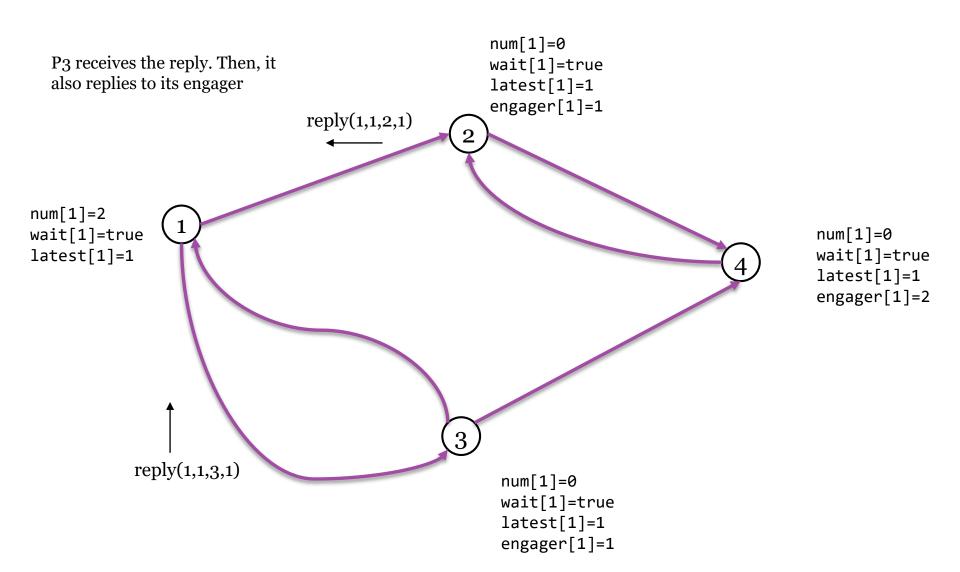


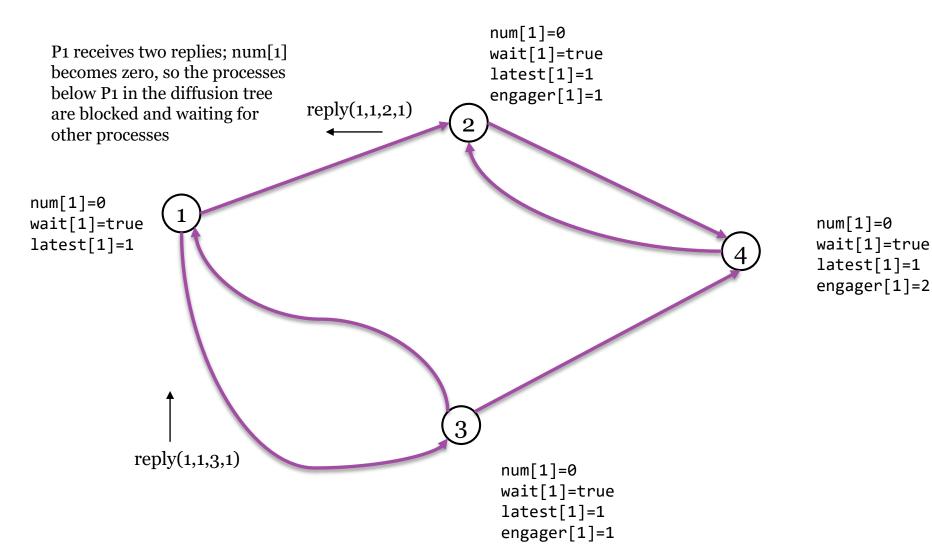








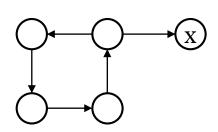




- Every edge of the knot is painted twice (query and reply), resulting O(n)
- As all processes may start detection at the same time, worst case is O(n²)

#### Additional Material about WFG

- Many other materials may consider an end (leaf) node of a WFG as a blocked node, i.e., the node is blocked and waiting for another resource even if not explicit by the WFG (e.g. the node *x* below)
- If you consider it valid, you should consider that a blocked node may have no outgoing edge, e.g., |WFx| = zero
- In this case, the description of some algorithms may be wrong, once they may expect that blocked processes have at least one outgoing edge
- One example is the Chandy-Misra-Haas algorithm for distributed detection of OR-deadlock
  - The descriptions of the algorithm in the literature do not reply to a query if an end node has no outgoing edges, e.g., the node *x* below would not reply even being blocked
  - In order to correct it, we should change the code like the one on the right



```
Blocked Pk receives a query(i,m,j,k):
    // if engaging query for Pi
    if (m>latest[i]) {
        latest[i]=m; engager[i]=j
        wait[i]=true; num[i]=|WF<sub>k</sub>|
        ∀ Pr ∈ WF<sub>k</sub>: send query(i,m,k,r)
        if num[i]=0
            send reply(i,m,k,j)
        // if not engaging query
    } else if wait[i] and m=latest[i]
        send reply(i,m,k,j)
```

#### Additional Material about WFG

- Instead of changing the description of the codes and to be coherent with the definition of blocked processes, we just prefer to accept blocked processes with at least one outgoing edge in WFGs
- In other materials, if you see it and the author stated that this process is blocked, you may interpret it as a blocked subgraph in deadlock, as the example below
  - In this case, you do not have to change the original description of the algorithms

