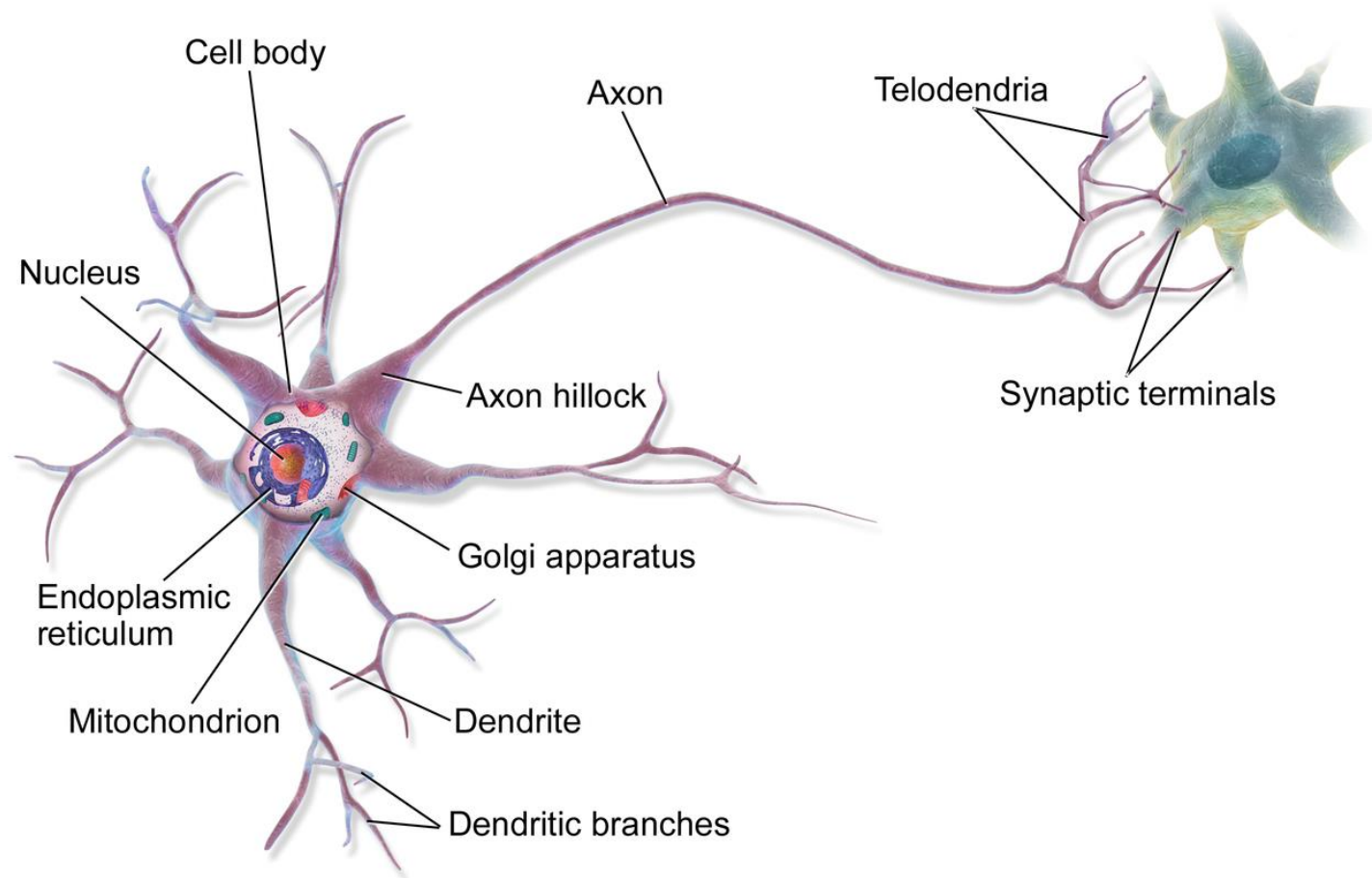


# Neural Networks

Andrey Sozykin

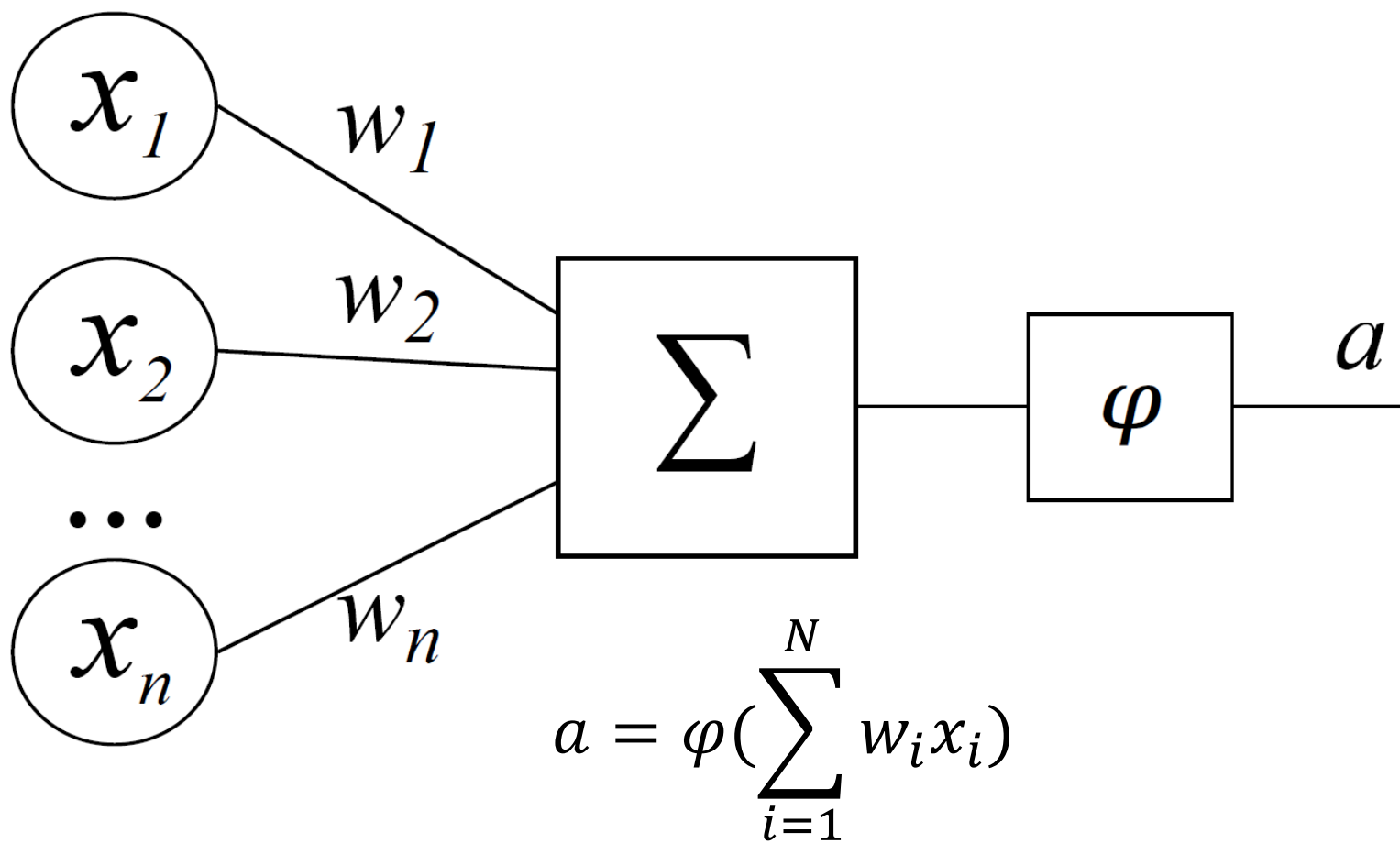
Andrey.Sozykin@urfu.ru

# Biological Neuron



Source: <https://en.wikipedia.org/wiki/Neuron>

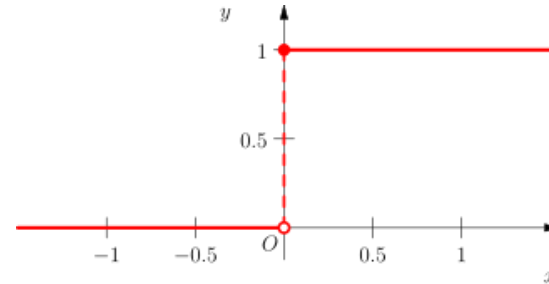
# Artificial Neuron



# Activation functions

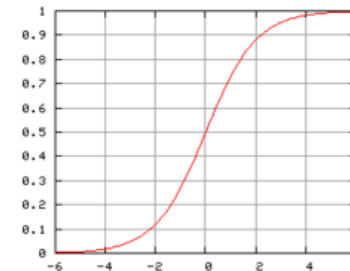
- Heaviside function

$$- \theta(x) = \begin{cases} 0, & x < 0 \\ 1, & x > 0 \end{cases}$$



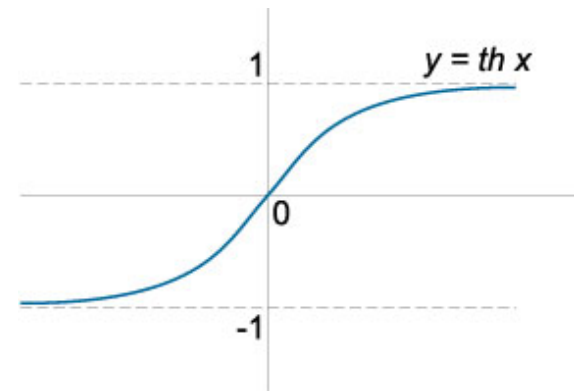
- Sigmoid functions

$$- \sigma(x) = \frac{1}{1+e^{-x}} \text{ (logistics)}$$

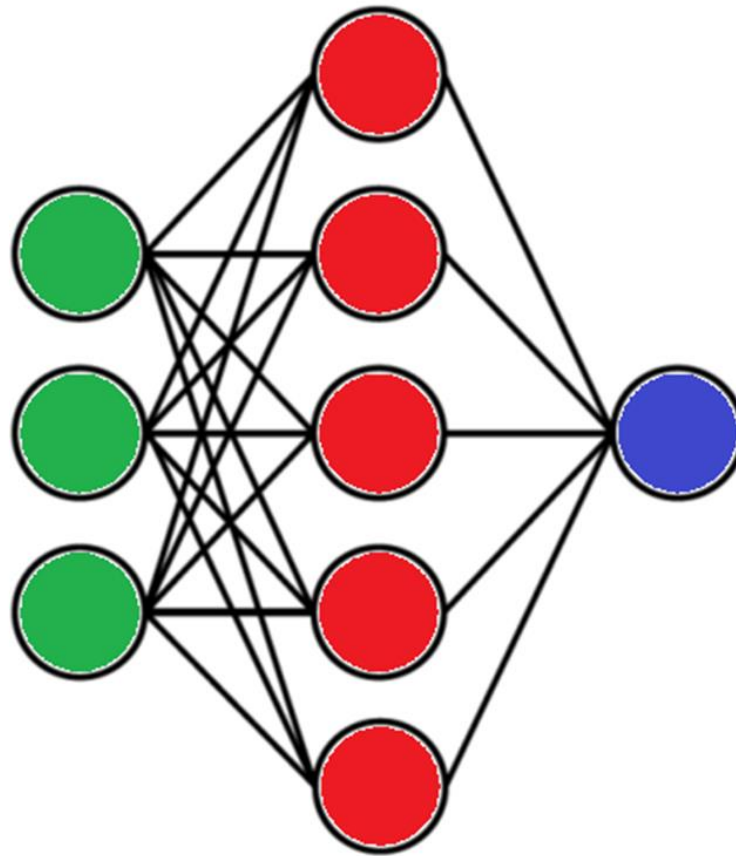


$$- th(x) = \frac{e^{2x}-1}{e^{2x}+1}$$

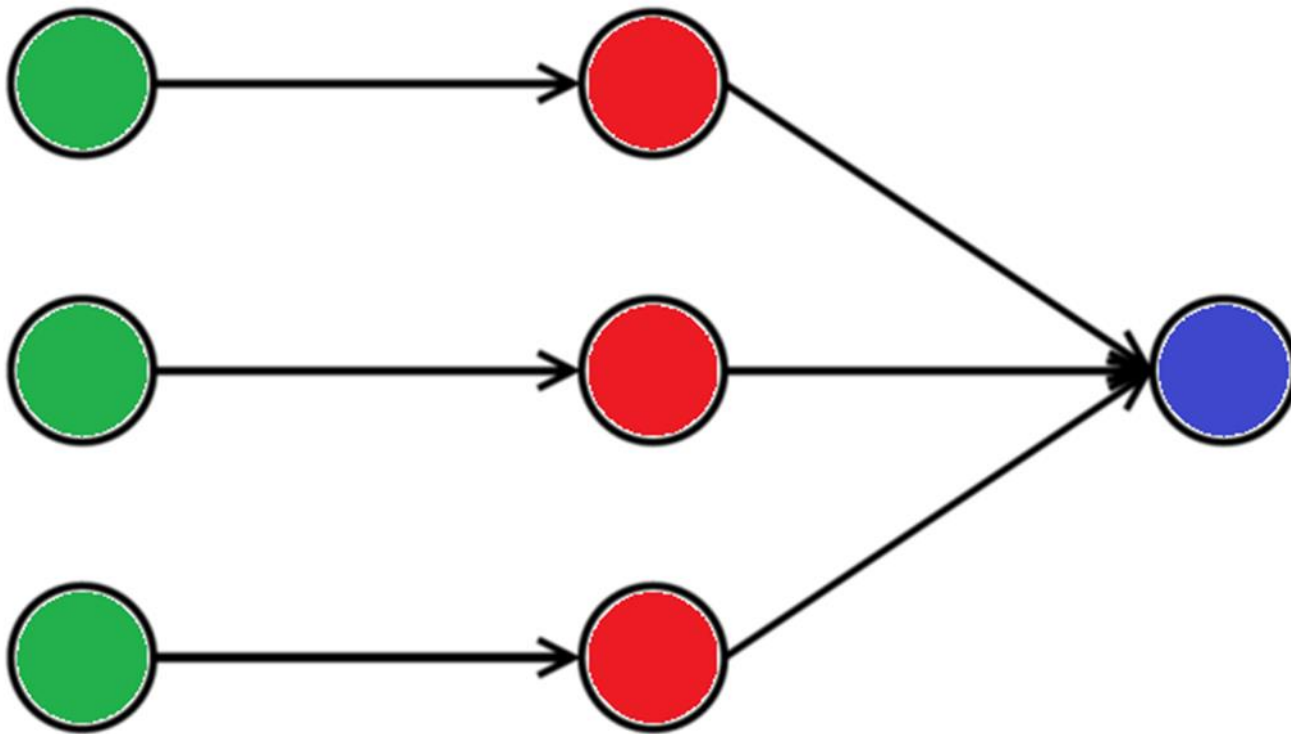
(hyperbolic tangent)



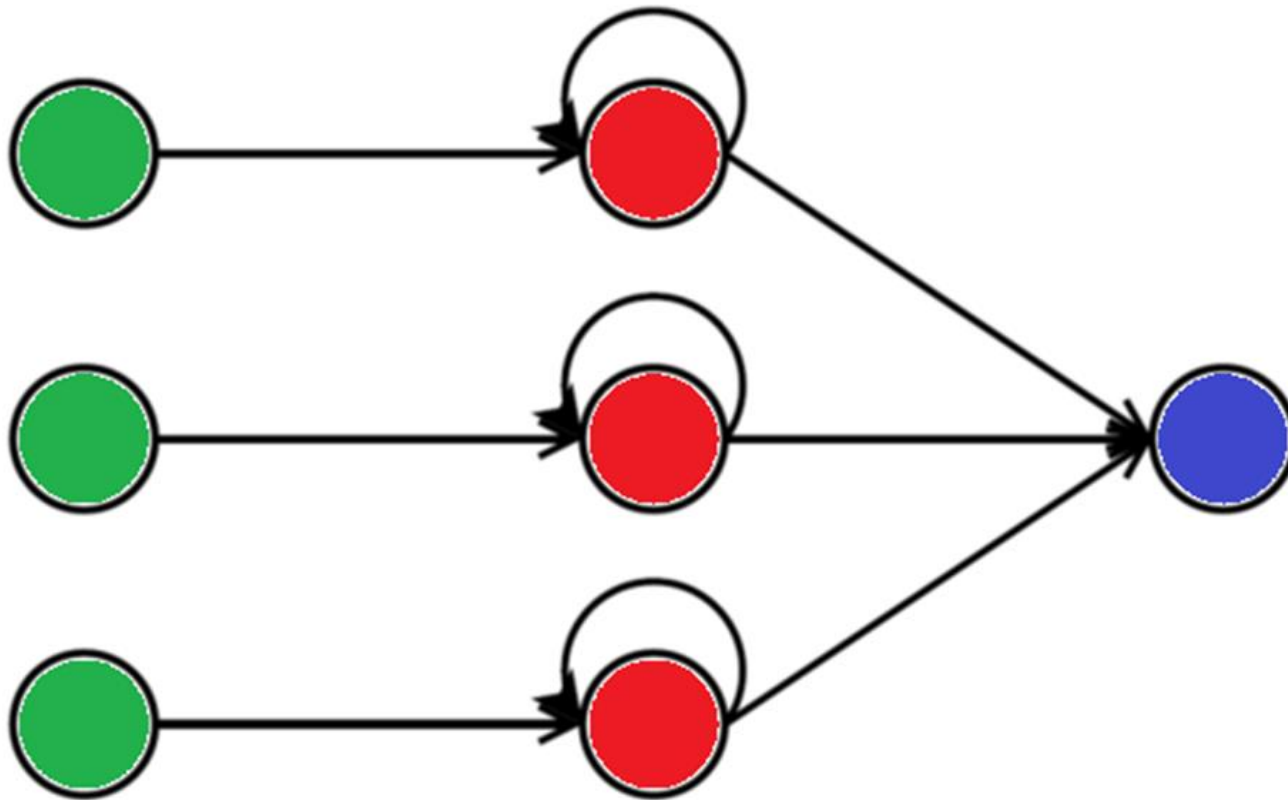
# Neural Network



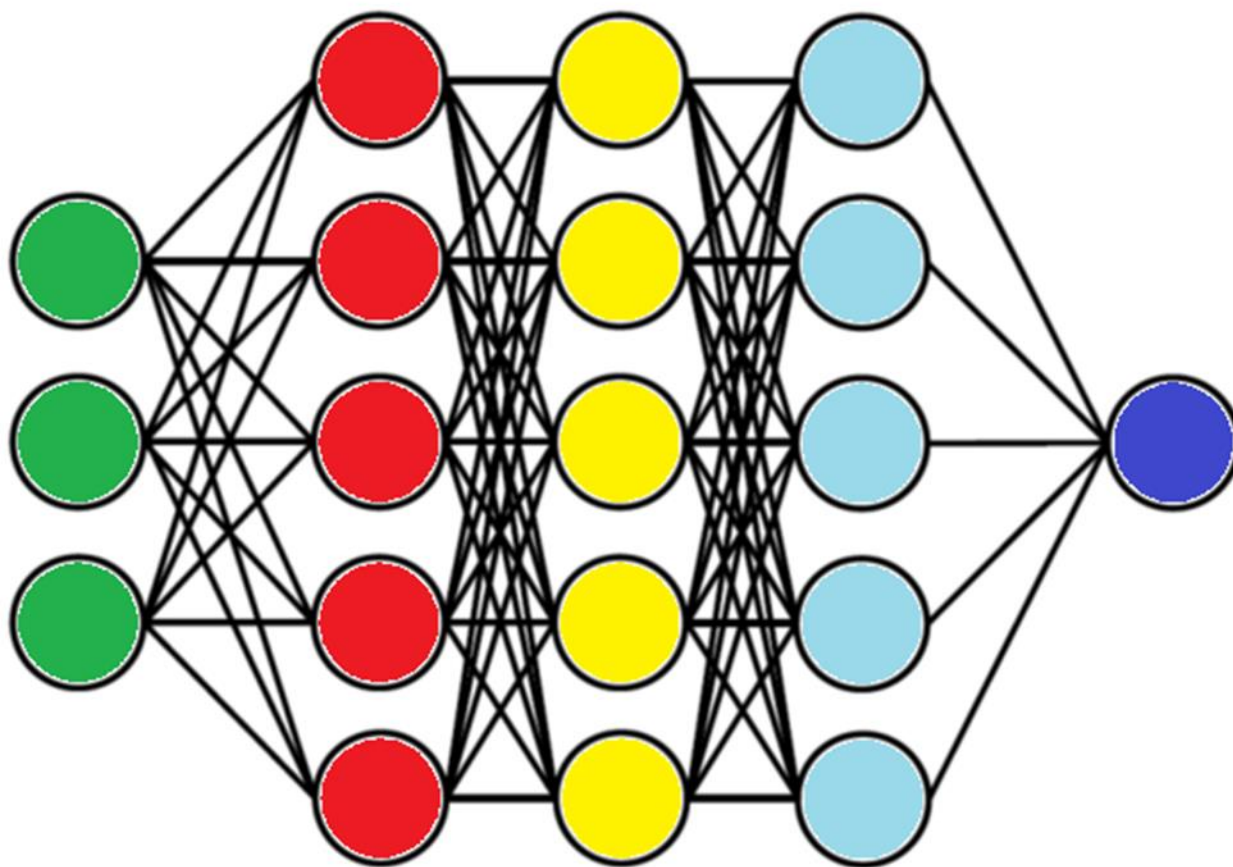
# Feed Forward Network



# Recurrent Neural Network



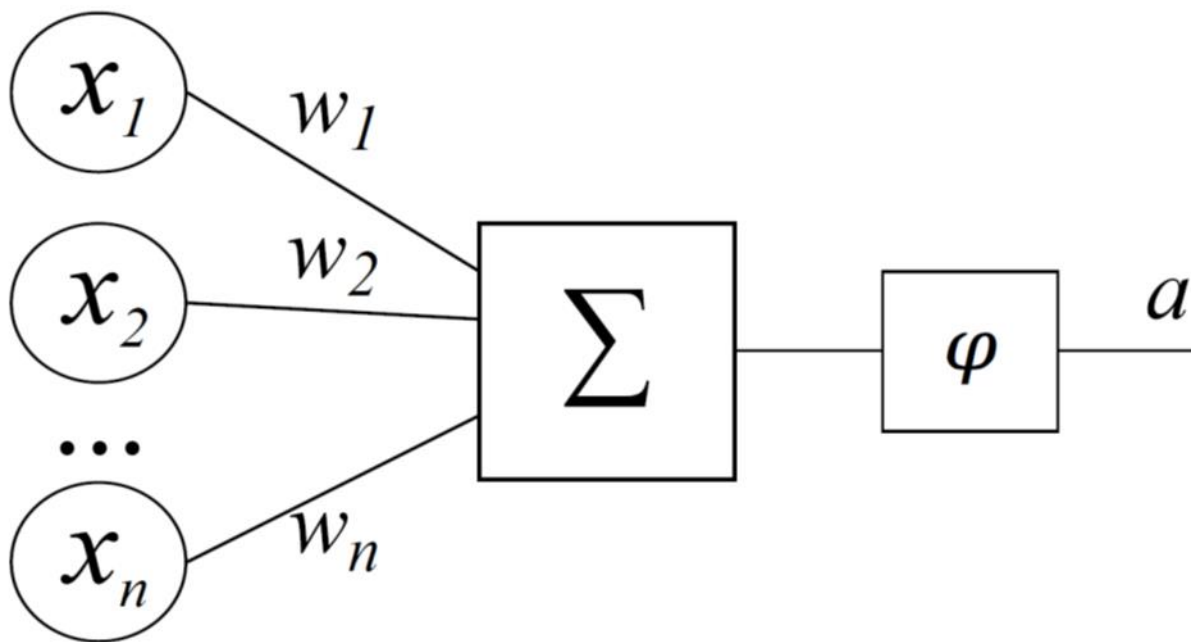
# Deep Neural Network



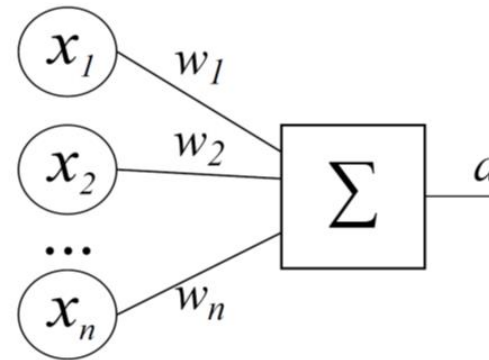


# Training Neural Network

Training a model means setting its parameters so that the model best fits the training set.



# Training Linear Neuron



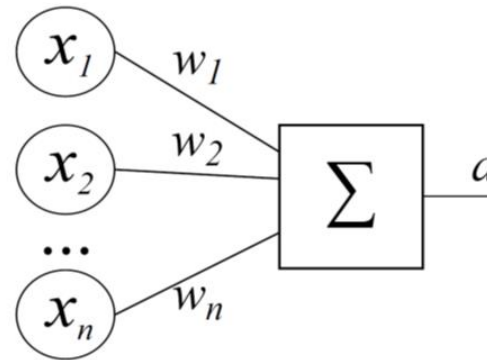
- Neuron output:

$$a = \sum_{i=1}^N w_i x_i$$

- Mean Square Error:

$$\varepsilon = \frac{1}{M} \sum_{j=1}^M (a_j - y_j)^2$$

# Delta rule

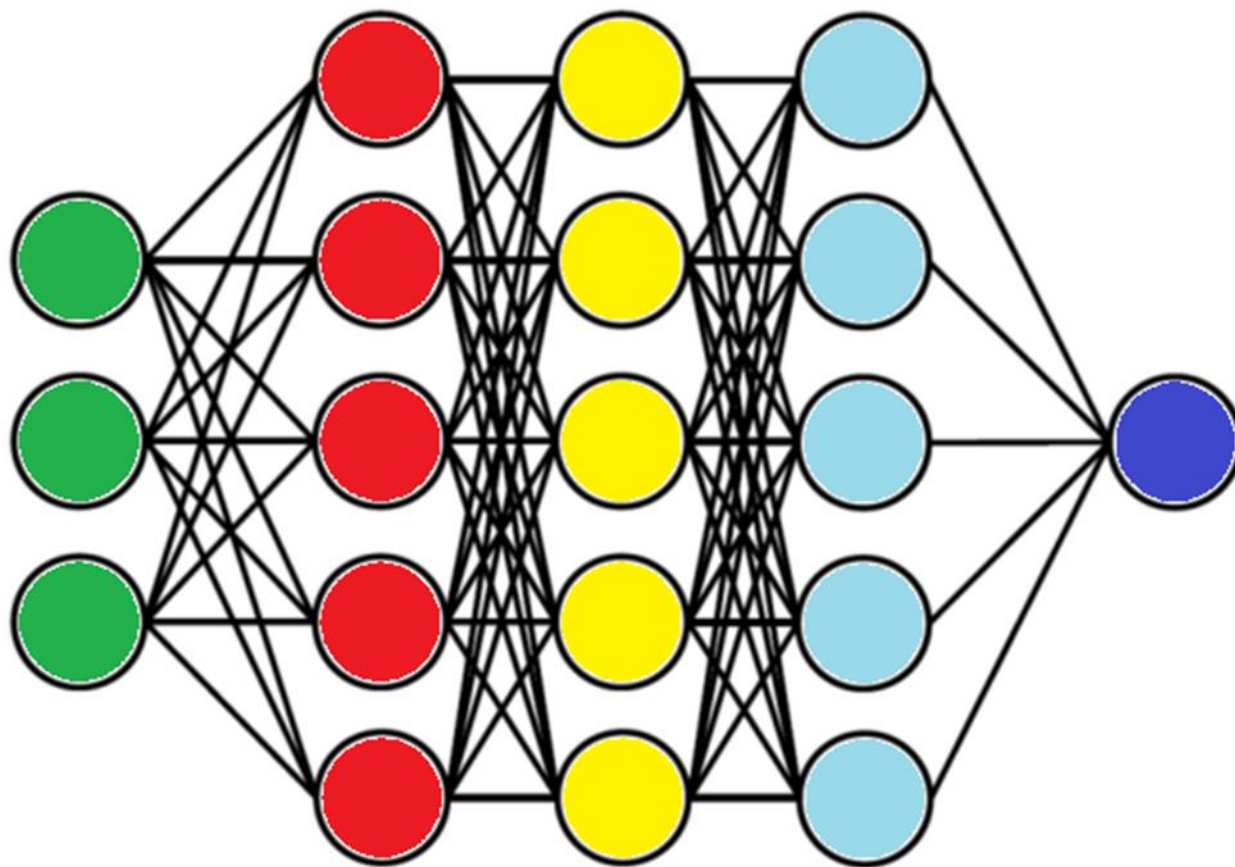


- Changing the weights:

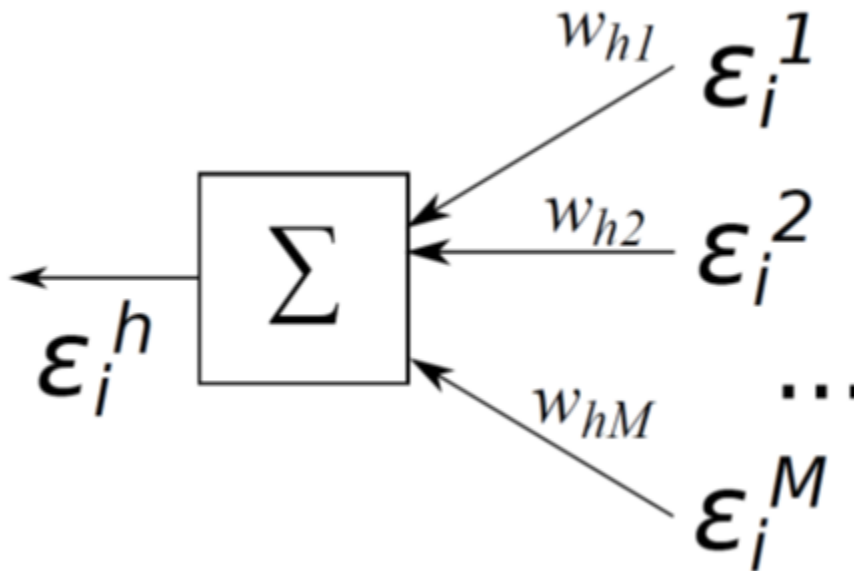
$$w_i = w_i - \eta \frac{2}{M} \sum_{j=1}^M x_j^i (a_j - y_j)$$

$\eta$  – learning rate

# Backpropagation Algorithm



# Error Backpropagation



$$\epsilon_i^h = \sum_{m=1}^M \epsilon_i^m w_{hm}$$

# Deep Learning Libraries



Caffe

PYTORCH



theano

DEEPLARNING4J



# Deep Learning Stack



# MNIST Dataset

Mixed National Institute of Standards and Technology  
database



Back-Propagation Applied to Handwritten Zip Code Recognition / Y. LeCun,  
B. Boser, J. S. Denker et al. 1989



# Neural Net for MNIST Recognition

- Input layer:
  - 800 neurons
- Output layer:
  - 10 neurons (the number of classes)
- Examples of the neural network architectures for MNIST
  - [https://en.wikipedia.org/wiki/MNIST\\_database](https://en.wikipedia.org/wiki/MNIST_database)

# How to prevent overfitting

- Training dataset
  - Dataset for training the neural network
- Test dataset:
  - Dataset for evaluating the performance and generalization of the neural network after the training

# Parameters and hyperparameters

- Parameters of the neural network (learned during training):
  - Weights of the neuron inputs
- Hyperparameters of the neural network (must be specified by developer):
  - Number of layers in the network
  - Number of neurons in the layers
  - Type of layers (dense, convolutional, recurrent, etc.)
  - Learning rate
  - Number of epoch for training

# How to prevent overfitting

- Training dataset
  - Dataset for training the neural network
- Validation dataset
  - Dataset for evaluating the performance and generalization of the neural network **during the training** for tuning **hyperparameters**
- Test dataset:
  - Dataset for evaluating the performance and generalization of the neural network **after the training**

# Thank you!