



DEPARTAMENTO
DE COMPUTACIÓN

Facultad de Ciencias Exactas y Naturales - UBA

Backing and Undercutting in DeLP (Extended-DeLP)

- Guillermo R. Simari



*Laboratorio de Investigación y
Desarrollo en Inteligencia
Artificial (LIDIA)*

Instituto de Ciencias e Ingeniería de la Computación
Departamento de Ciencias e Ingeniería de la Computación



UNIVERSIDAD NACIONAL DEL SUR
Bahía Blanca - ARGENTINA



Structured Argumentation

*See Argument & Computation, Vol 5 No 1, 2014
for a set of tutorials on Structured Argumentation.*

Conceptual View

Definition of Status of Arguments

Definition of Defeat among Arguments

Definition of Conflict among Arguments

Definition of Argument

Definition of the Underlying (Logical) Language



*Backing and
Undercutting in
Defeasible Logic
Programming*

Introduction

- *We will present Extended Defeasible Logic Programming (E-DeLP)*
- *Introduces the possibility of attacking and supporting defeasible rules:*
 - *Attack for defeasible rules allows for the representation of Pollock's undercutting defeaters (to be discussed).*
 - *Support for defeasible rules allows for the representation of Toulmin's backings.*

Defeasible Logic Programming (DeLP)

*García, A.J., Simari, G.R.: Defeasible logic programming:
An argumentative approach. Theory and Practice of Logic
Programming 4(1-2), 95–138. 2004*

*Also, see Argument & Computation Vol 5 No 1, 2014 for a
set of tutorials on Structured Argumentation.*

Defeasible Logic Programming (DeLP)

- KR&R: *Combines Logic Programming and Argumentation.*
- *Allows for the representation of strict and defeasible knowledge.*
- *A defeasible argumentation inference mechanism warrants the entailed conclusions through a dialectical process.*
- *Allows for the representation of rebutting defeaters.*

DeLP – Knowledge Representation

A *DeLP program* $\mathcal{P} = (\Pi, \Delta)$

Facts and Strict Rules

chicken
scared
 $\text{bird} \leftarrow \text{chicken}$

Defeasible Rules

$\text{flies} \prec \text{bird}$
 $\sim\text{flies} \prec \text{chicken}$
 $\text{flies} \prec \text{chicken, scared}$
 $\text{nests_in_trees} \prec \text{flies}$

Consistent

*Potentially
Contradictory*

DeLP – Arguments

Argument $\langle \mathcal{A}, L \rangle$ for L

- 1) $\mathcal{A} \subseteq \Delta$
- 2) $\Pi \cup \mathcal{A} \vdash L$
- 3) $\Pi \cup \mathcal{A} \not\vdash P, \neg P$
- 4) There is no $\mathcal{A}' \subset \mathcal{A}$
satisfying 2) and 3)

chicken
scared
bird \leftarrow chicken

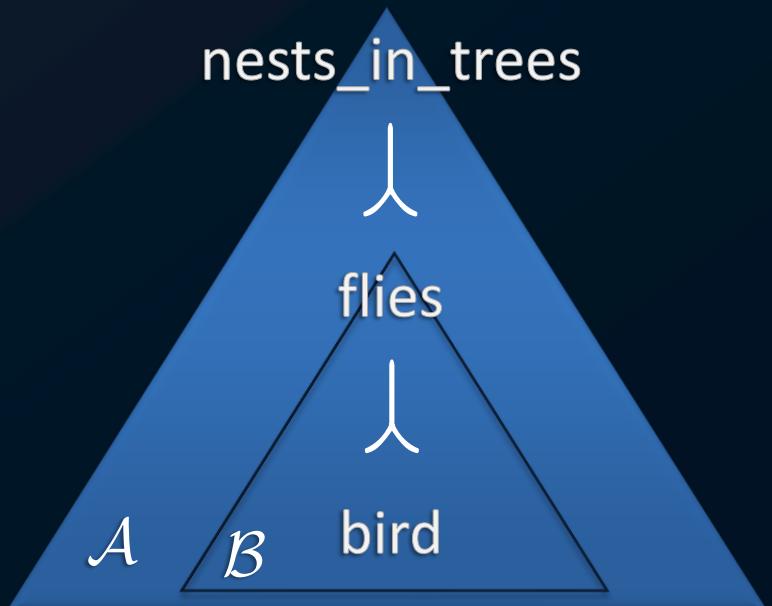
flies \leftarrow bird
 \neg flies \leftarrow chicken
flies \leftarrow chicken, scared
nests_in_trees \leftarrow flies

DeLP – Arguments

Argument $\langle \mathcal{A}, L \rangle$ for L

- 1) $\mathcal{A} \subseteq \Delta$
- 2) $\Pi \cup \mathcal{A} \vdash L$
- 3) $\Pi \cup \mathcal{A} \nvDash P, \neg P$
- 4) There is no $\mathcal{A}' \subset \mathcal{A}$ satisfying 2) and 3)

chicken	flies \leftarrow bird
scared	\neg flies \leftarrow chicken
bird \leftarrow chicken	flies \leftarrow chicken, scared
	nests_in_trees \leftarrow flies



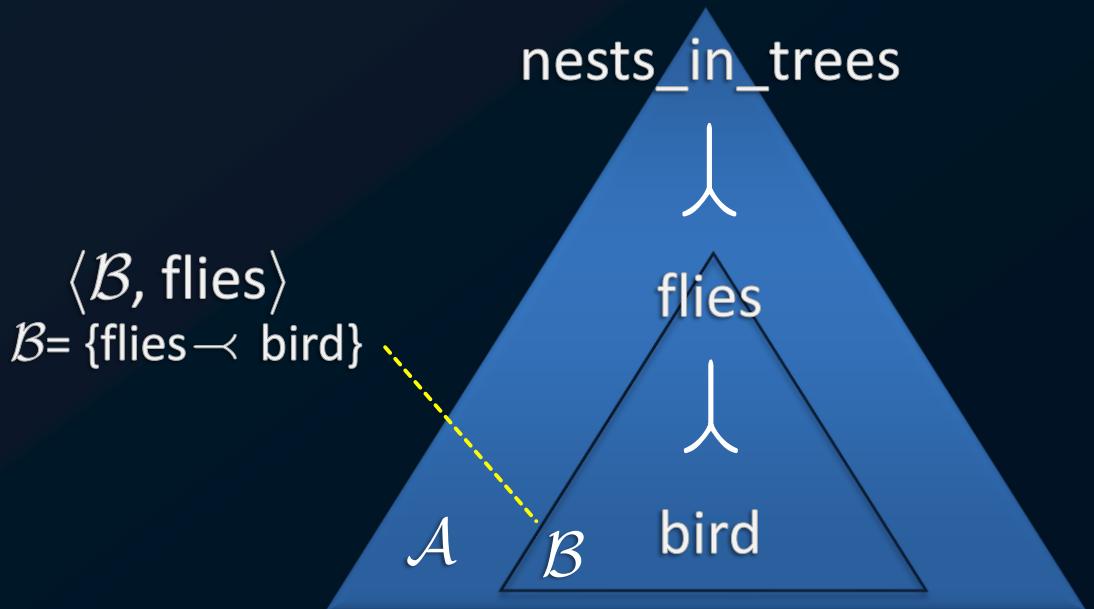
$\mathcal{A} = \{\text{nests_in_trees} \leftarrow \text{flies}, \text{flies} \leftarrow \text{bird}\}$
 $\langle \mathcal{A}, \text{nests_in_trees} \rangle$

DeLP – Arguments

Argument $\langle \mathcal{A}, L \rangle$ for L

- 1) $\mathcal{A} \subseteq \Delta$
- 2) $\Pi \cup \mathcal{A} \vdash L$
- 3) $\Pi \cup \mathcal{A} \not\vdash P, \sim P$
- 4) There is no $\mathcal{A}' \subset \mathcal{A}$ satisfying 2) and 3)

An argument $\langle \mathcal{B}, H \rangle$ is a sub-argument of $\langle \mathcal{A}, L \rangle$ if $\mathcal{B} \subseteq \mathcal{A}$



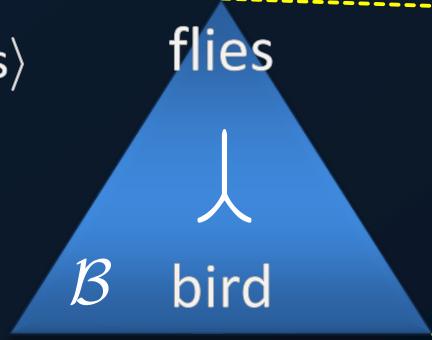
DeLP – Arguments

Argument $\langle \mathcal{A}, L \rangle$ for L

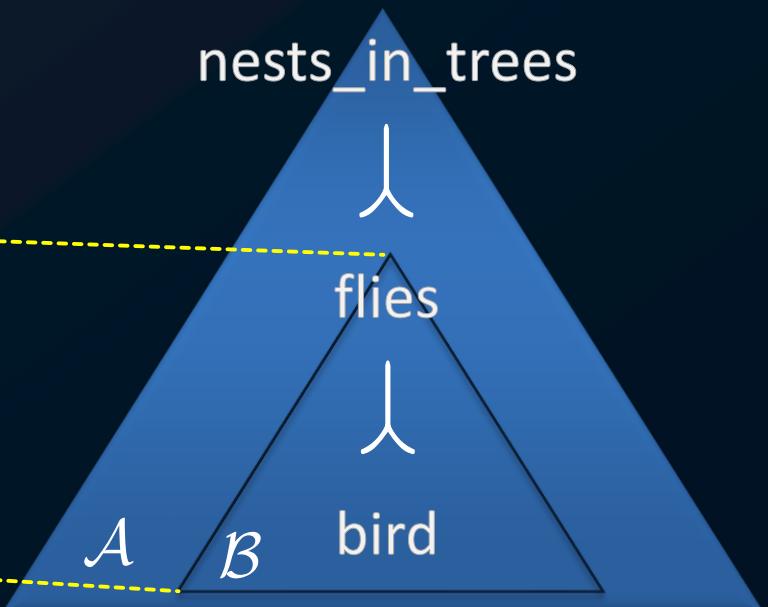
- 1) $\mathcal{A} \subseteq \Delta$
- 2) $\Pi \cup \mathcal{A} \vdash L$
- 3) $\Pi \cup \mathcal{A} \not\vdash P, \neg P$
- 4) There is no $\mathcal{A}' \subset \mathcal{A}$ satisfying 2) and 3)

An argument $\langle \mathcal{B}, H \rangle$ is a sub-argument of $\langle \mathcal{A}, L \rangle$ if $\mathcal{B} \subseteq \mathcal{A}$

$\langle \mathcal{B}, \text{flies} \rangle$



$\mathcal{B} = \{\text{flies} \leftarrow \text{bird}\}$



$\mathcal{A} = \{\text{nests_in_trees} \leftarrow \text{flies}, \text{flies} \leftarrow \text{bird}\}$
 $\langle \mathcal{A}, \text{nests_in_trees} \rangle$

DeLP – *Defeat*

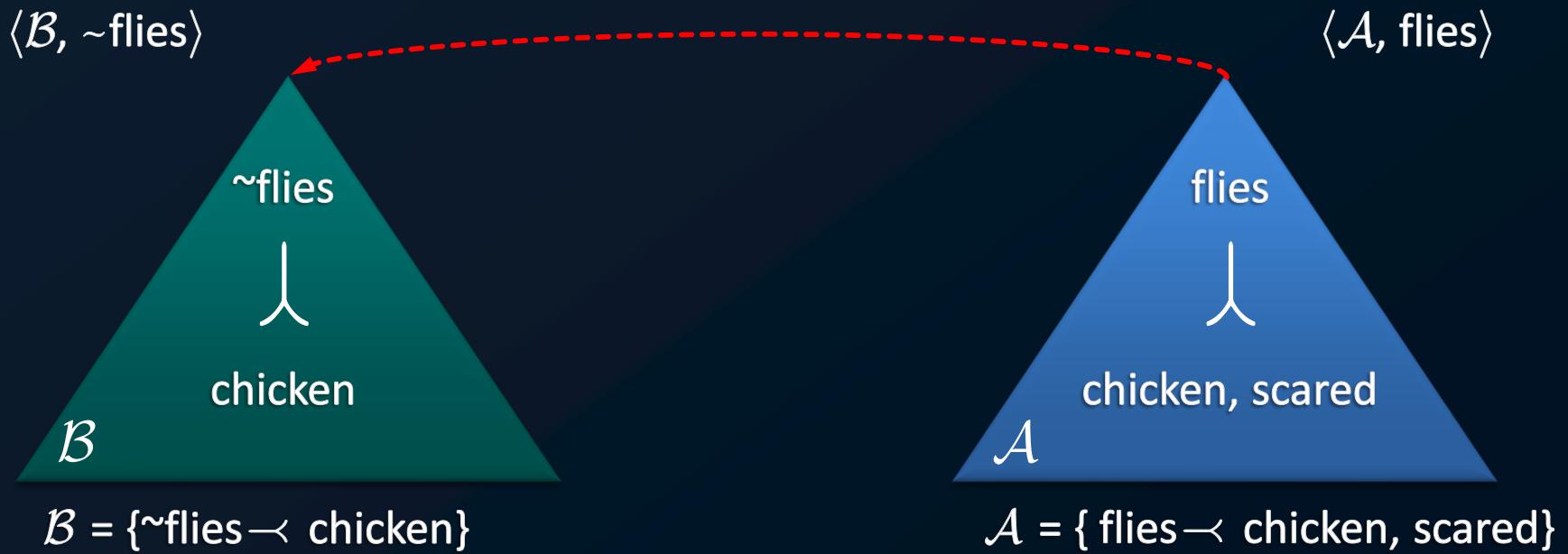
An argument $\langle A, L \rangle$ defeats another argument $\langle B, Q \rangle$ if there exists a sub-argument $\langle C, R \rangle$ of $\langle B, Q \rangle$ such that:

- $\langle A, L \rangle$ is in conflict with $\langle C, R \rangle$
- $\langle A, L \rangle$ is preferred or unrelated to $\langle C, R \rangle$

A comparison criterion is required to define a preference among arguments.

An argument $\langle \mathcal{A}, L \rangle$ defeats another argument $\langle \mathcal{B}, Q \rangle$ if there exists a sub-argument $\langle \mathcal{C}, R \rangle$ of $\langle \mathcal{B}, Q \rangle$ such that

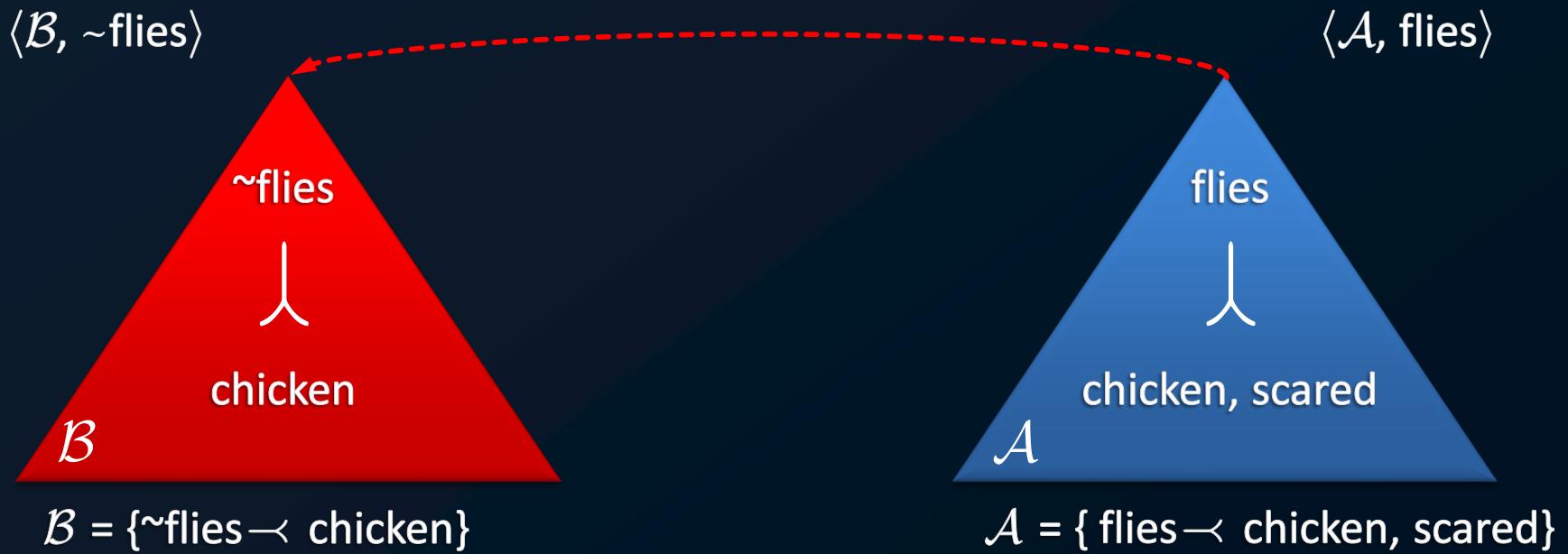
- $\langle \mathcal{A}, L \rangle$ is in conflict with $\langle \mathcal{C}, R \rangle$
- $\langle \mathcal{A}, L \rangle$ is preferred or unrelated to $\langle \mathcal{C}, R \rangle$



Using generalized specificity as the comparison criterion

An argument $\langle \mathcal{A}, L \rangle$ defeats another argument $\langle \mathcal{B}, Q \rangle$ if there exists a sub-argument $\langle \mathcal{C}, R \rangle$ of $\langle \mathcal{B}, Q \rangle$ such that

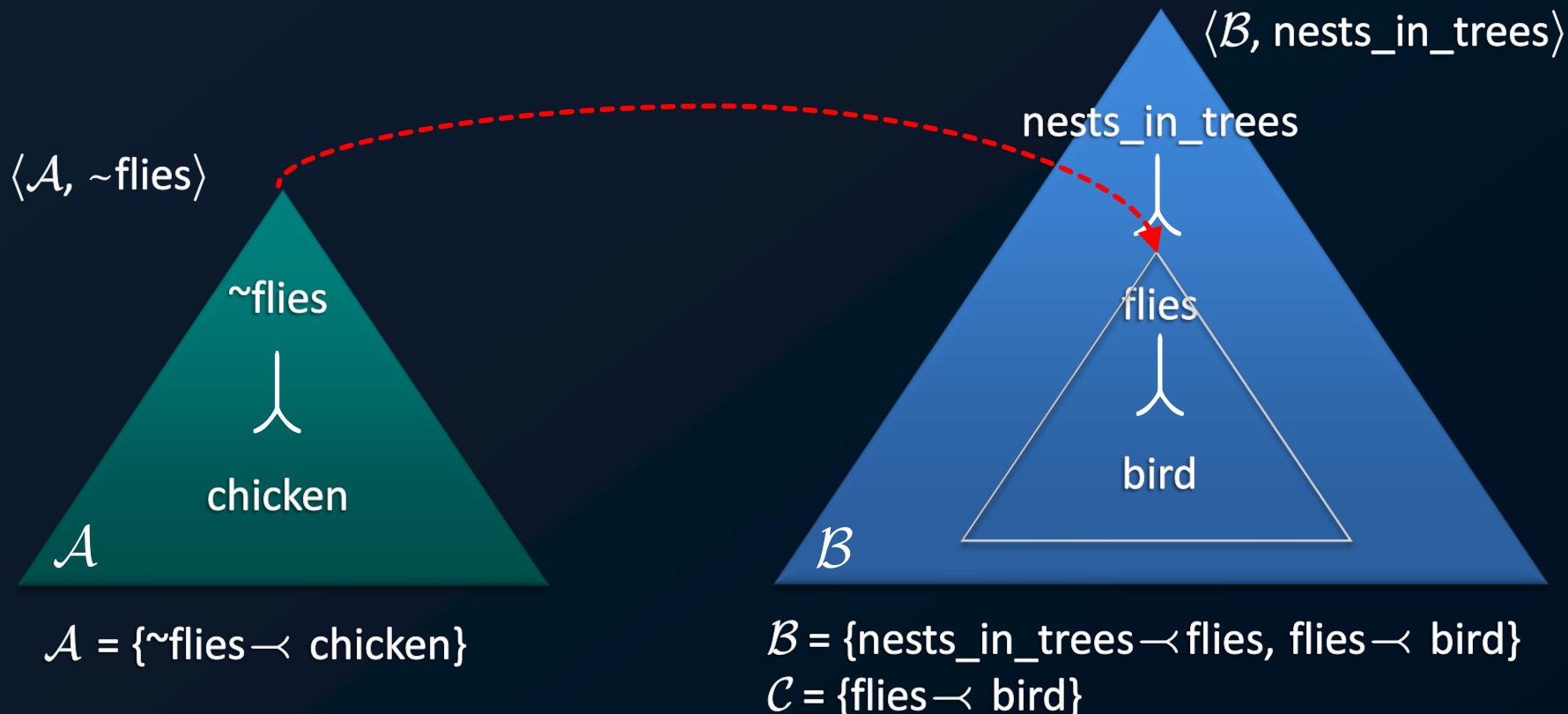
- $\langle \mathcal{A}, L \rangle$ is in **conflict** with $\langle \mathcal{C}, R \rangle$
- $\langle \mathcal{A}, L \rangle$ is **preferred** or **unrelated** to $\langle \mathcal{C}, R \rangle$



Using generalized specificity as the comparison criterion

An argument $\langle \mathcal{A}, L \rangle$ defeats another argument $\langle \mathcal{B}, Q \rangle$ if there exists a sub-argument $\langle \mathcal{C}, R \rangle$ of $\langle \mathcal{B}, Q \rangle$ such that

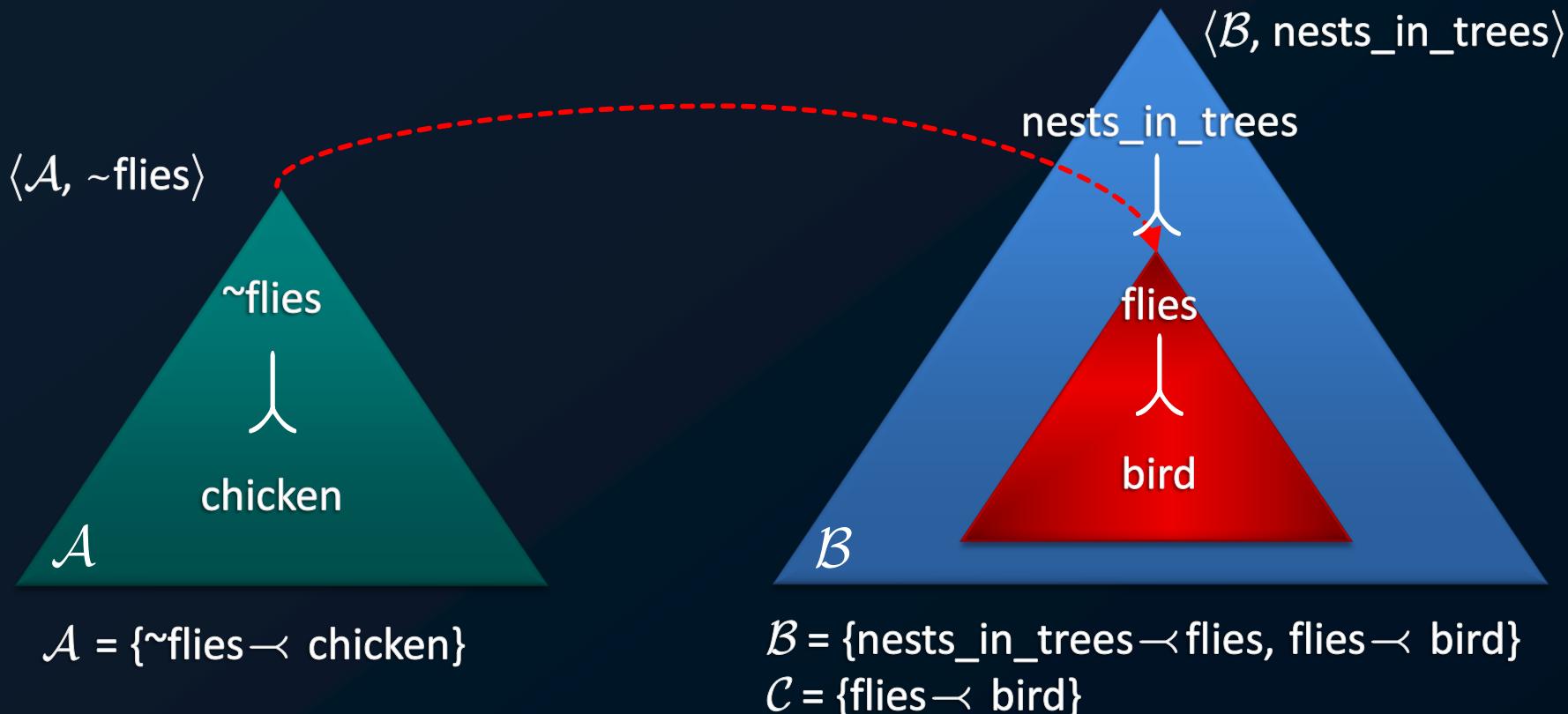
- $\langle \mathcal{A}, L \rangle$ is in **conflict** with $\langle \mathcal{C}, R \rangle$
- $\langle \mathcal{A}, L \rangle$ is **preferred** or **unrelated** to $\langle \mathcal{C}, R \rangle$



Using generalized specificity as the comparison criterion

An argument $\langle \mathcal{A}, L \rangle$ defeats another argument $\langle \mathcal{B}, Q \rangle$ if there exists a sub-argument $\langle \mathcal{C}, R \rangle$ of $\langle \mathcal{B}, Q \rangle$ such that

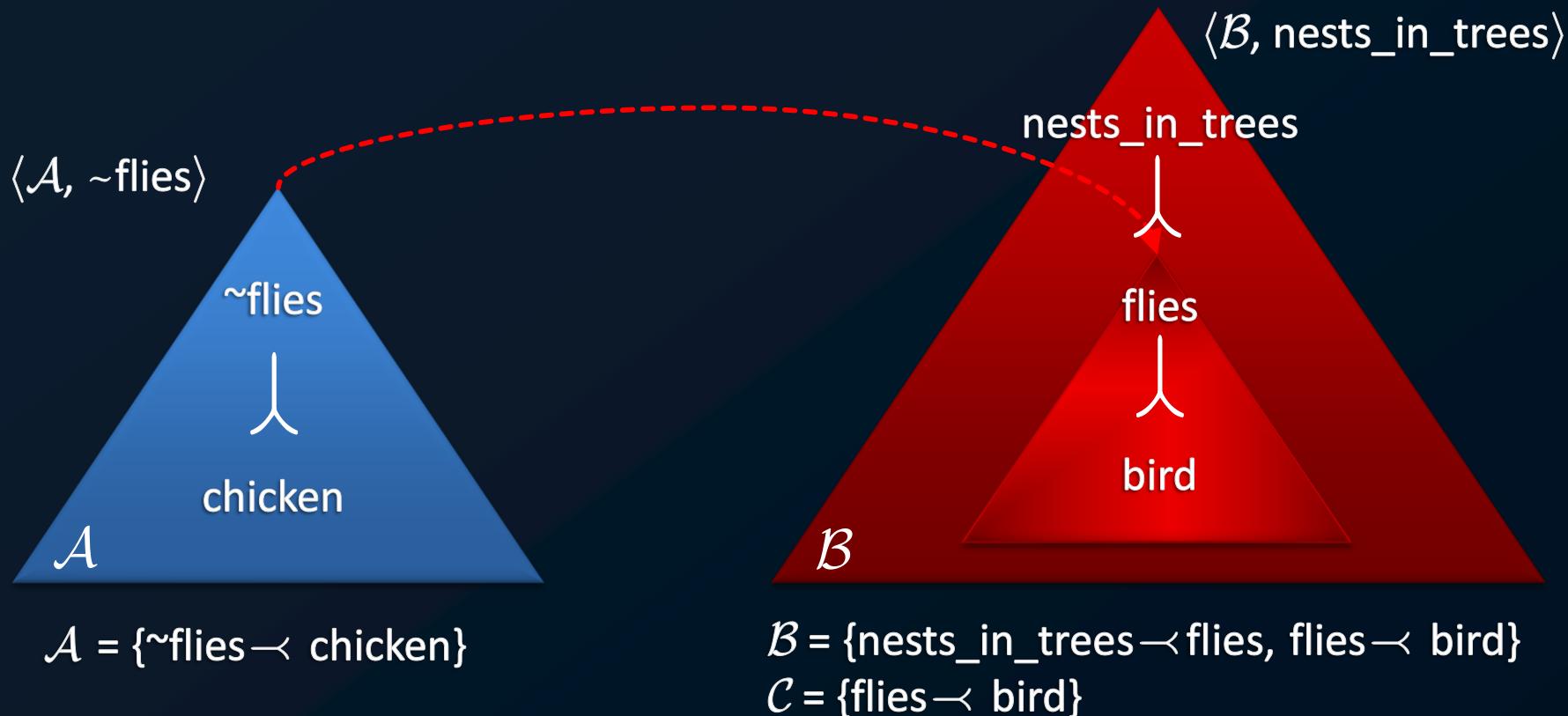
- $\langle \mathcal{A}, L \rangle$ is in conflict with $\langle \mathcal{C}, R \rangle$
- $\langle \mathcal{A}, L \rangle$ is preferred or unrelated to $\langle \mathcal{C}, R \rangle$



Using generalized specificity as the comparison criterion

An argument $\langle \mathcal{A}, L \rangle$ defeats another argument $\langle \mathcal{B}, Q \rangle$ if there exists a sub-argument $\langle \mathcal{C}, R \rangle$ of $\langle \mathcal{B}, Q \rangle$ such that

- $\langle \mathcal{A}, L \rangle$ is in conflict with $\langle \mathcal{C}, R \rangle$
- $\langle \mathcal{A}, L \rangle$ is preferred or unrelated to $\langle \mathcal{C}, R \rangle$

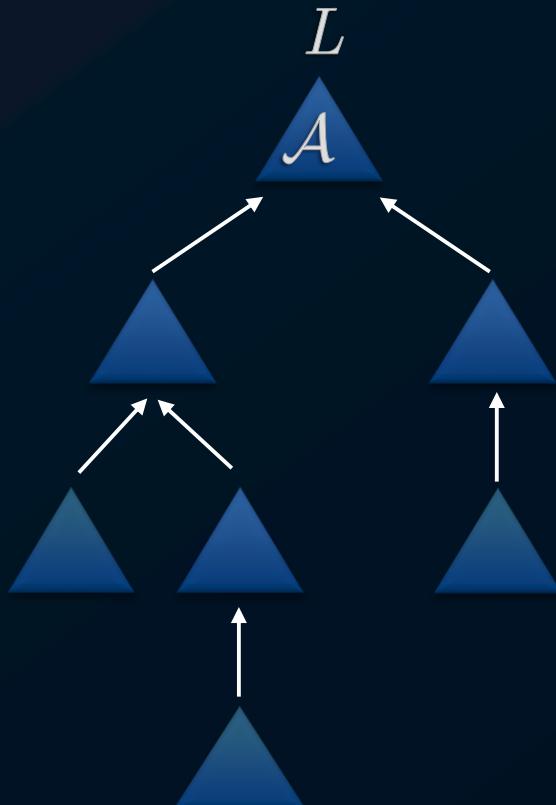


Using generalized specificity as the comparison criterion

DeLP – *Dialectical Process*

*To determine whether an argument $\langle A, L \rangle$ is finally acceptable, a **dialectical tree** with root $\langle A, L \rangle$ is built.*

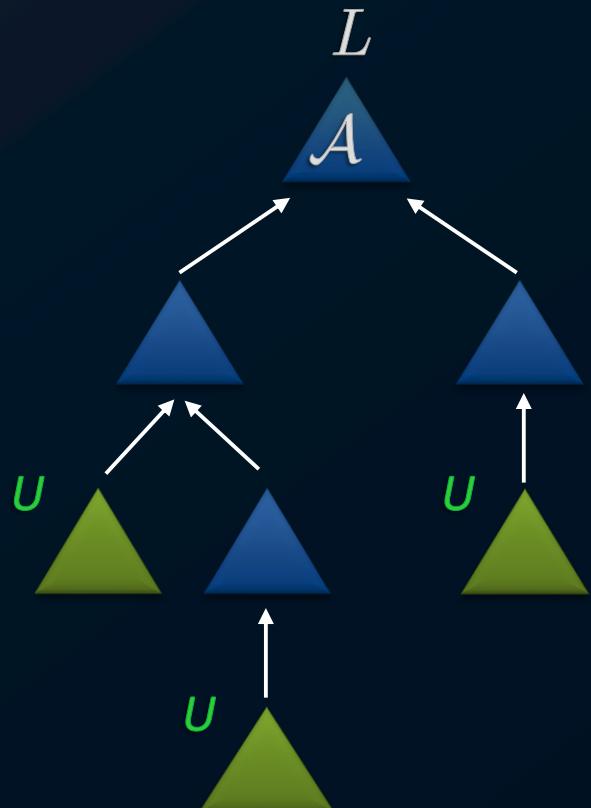
- Leaves are marked as **U**.



DeLP – *Dialectical Process*

To determine whether an argument $\langle A, L \rangle$ is finally acceptable, a dialectical tree with root $\langle A, L \rangle$ is built.

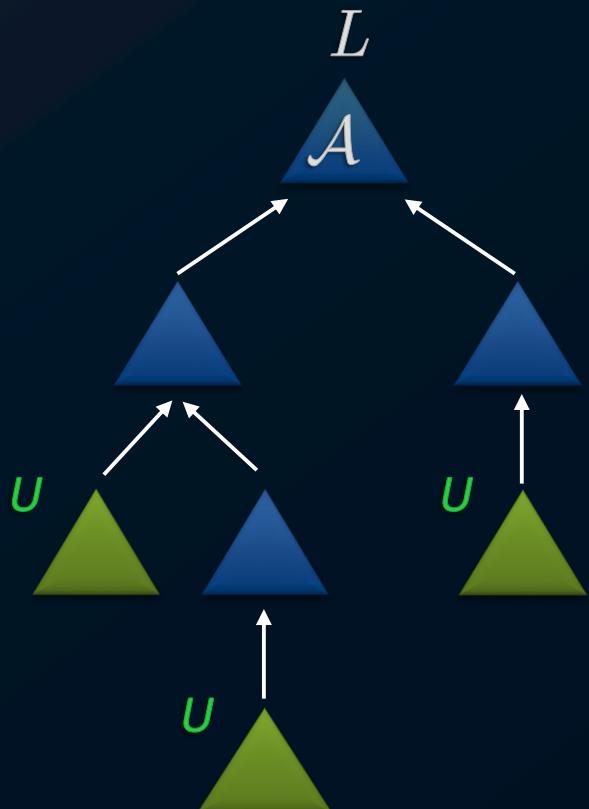
- Leaves are marked as U .



DeLP – *Dialectical Process*

*To determine whether an argument $\langle A, L \rangle$ is finally acceptable, a **dialectical tree** with root $\langle A, L \rangle$ is built.*

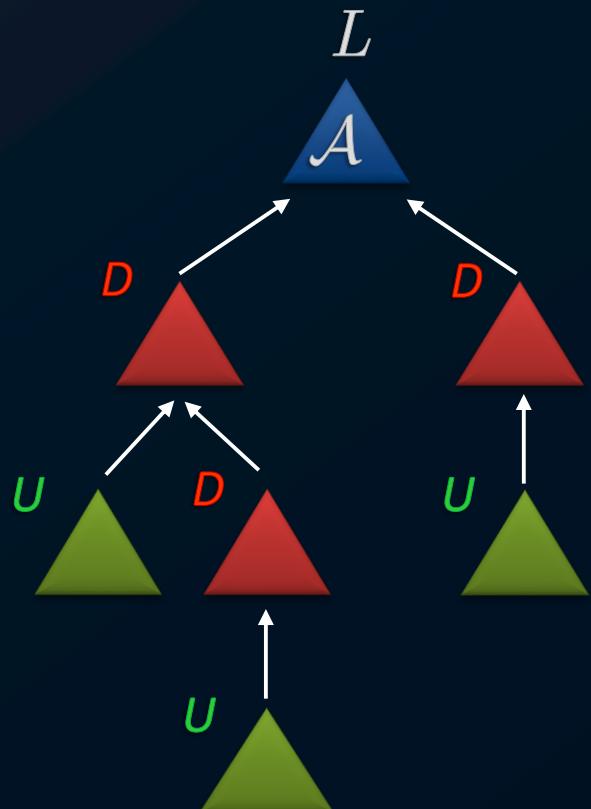
- Leaves are marked as **U**.
- An inner node is marked as **U** iff all its **children** are **D-nodes**.



DeLP – *Dialectical Process*

To determine whether an argument $\langle A, L \rangle$ is finally acceptable, a dialectical tree with root $\langle A, L \rangle$ is built.

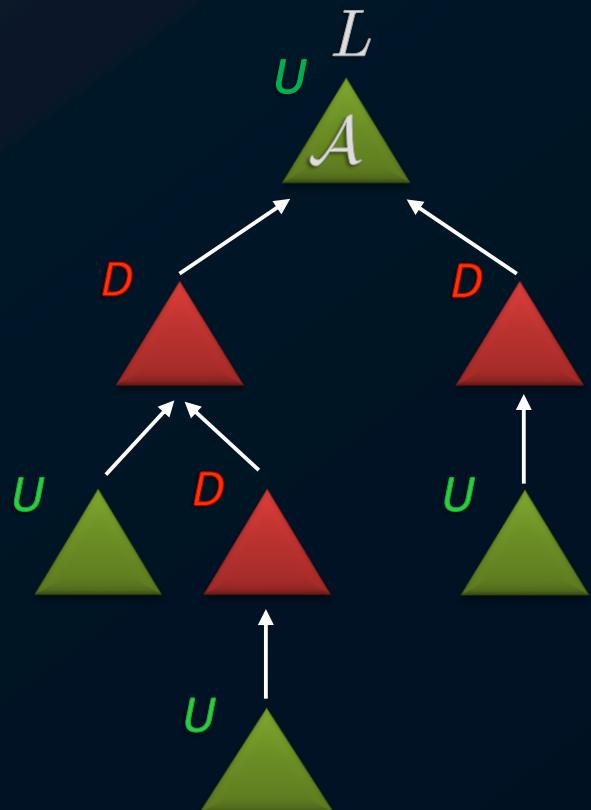
- Leaves are marked as **U**.
- An inner node is marked as **U** iff all its children are **D-nodes**.



DeLP – *Dialectical Process*

To determine whether an argument $\langle A, L \rangle$ is finally acceptable, a dialectical tree with root $\langle A, L \rangle$ is built.

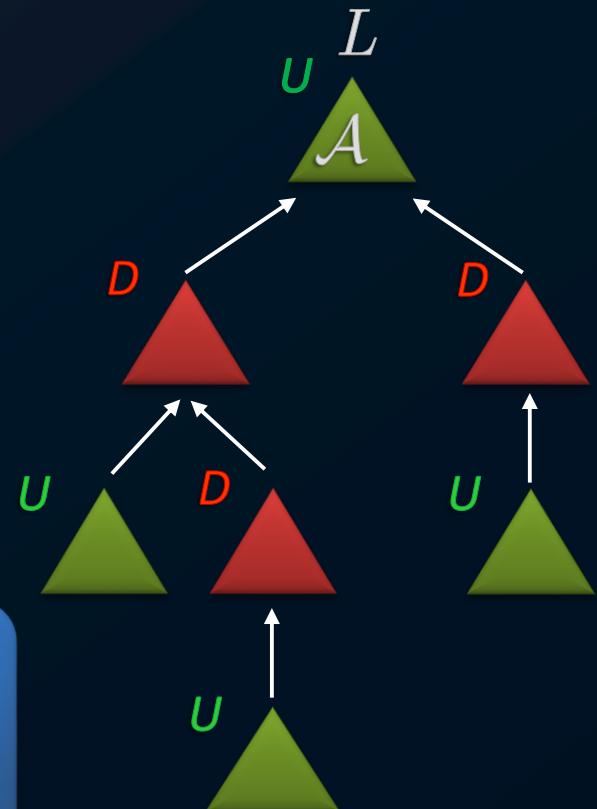
- Leaves are marked as **U**.
- An inner node is marked as **U** iff all its children are **D-nodes**.
- An inner node is marked as **D** iff at least one of its children is an **U-node**.



DeLP – Dialectical Process

To determine whether an argument $\langle A, L \rangle$ is finally acceptable, a dialectical tree with root $\langle A, L \rangle$ is built.

- Leaves are marked as **U**.
- An inner node is marked as **U** iff all its children are **D-nodes**.
- An inner node is marked as **D** iff at least one of its children is an **U-node**.

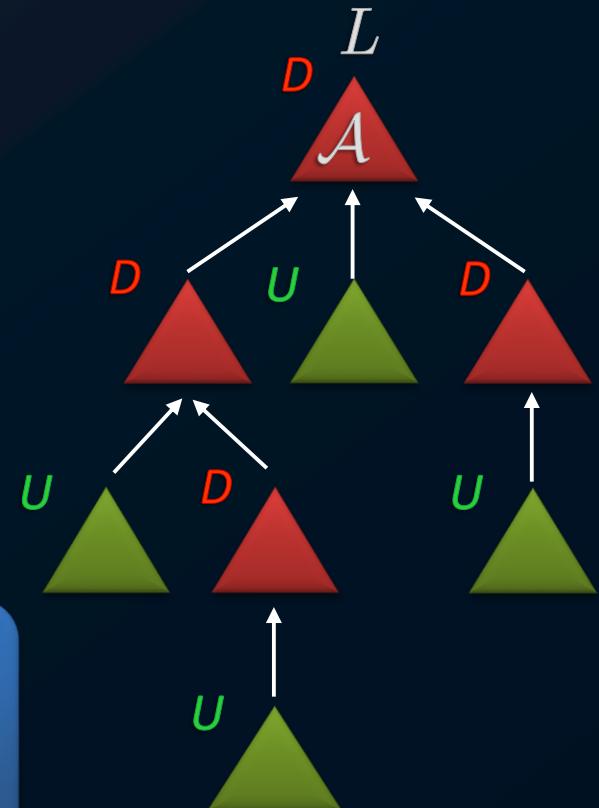


If the root $\langle A, L \rangle$ is marked as **U**, then **L** is *warranted*

DeLP – Dialectical Process

To determine whether an argument $\langle A, L \rangle$ is finally acceptable, a dialectical tree with root $\langle A, L \rangle$ is built.

- Leaves are marked as **U**.
- An inner node is marked as **U** iff all its children are **D-nodes**.
- An inner node is marked as **D** iff at least one of its children is an **U-node**.



If the root $\langle A, L \rangle$ is marked as **U**, then L is **not warranted**

*Motivation for
E-DeLP*

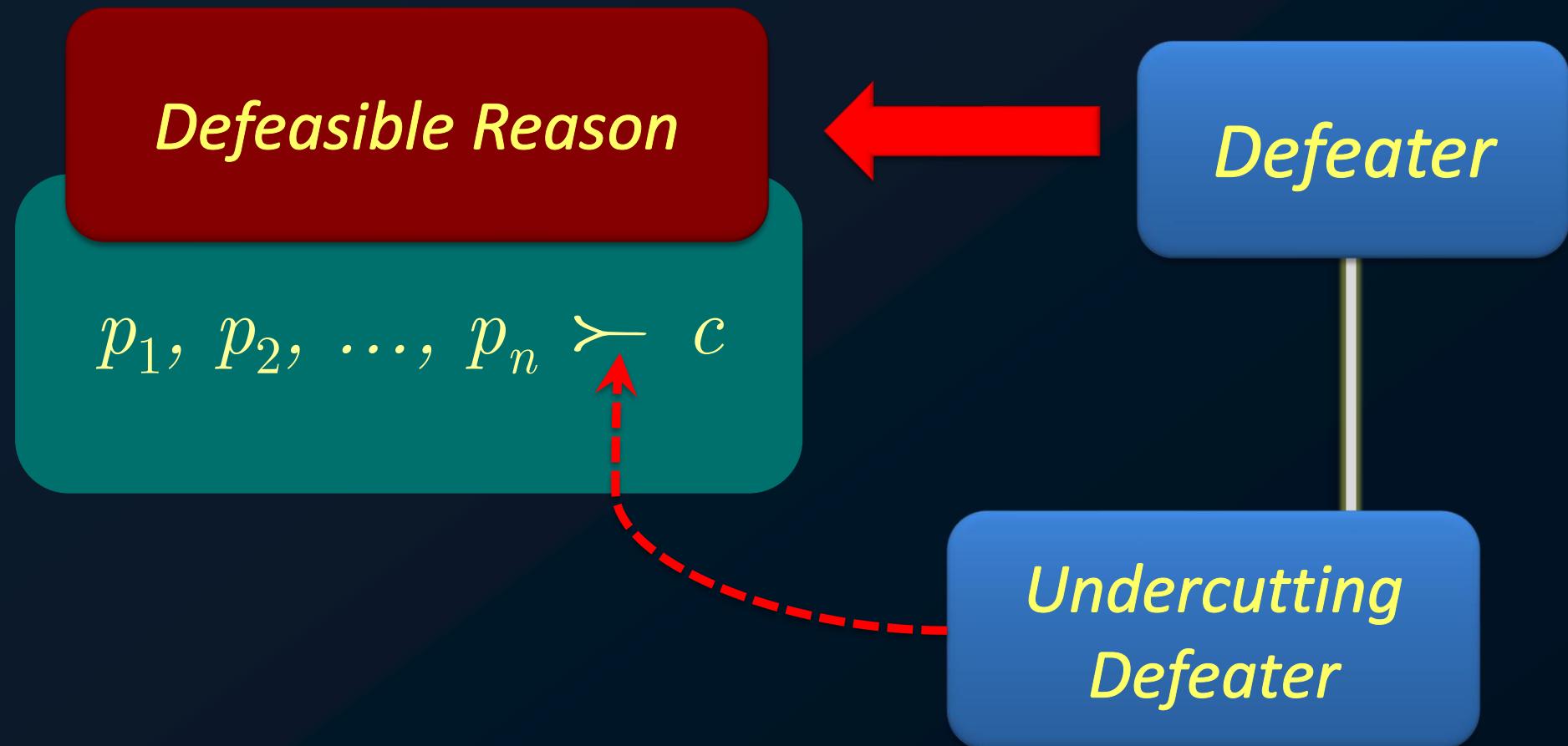
Pollock's Undercutting Defeaters

Defeasible Reason

Defeater

$$p_1, p_2, \dots, p_n \succ c$$

Pollock's Undercutting Defeaters



Example

Object looks red

*Object **is** red*



Example

Object looks red



Object is red

*Object is
illuminated by red lights*



Example

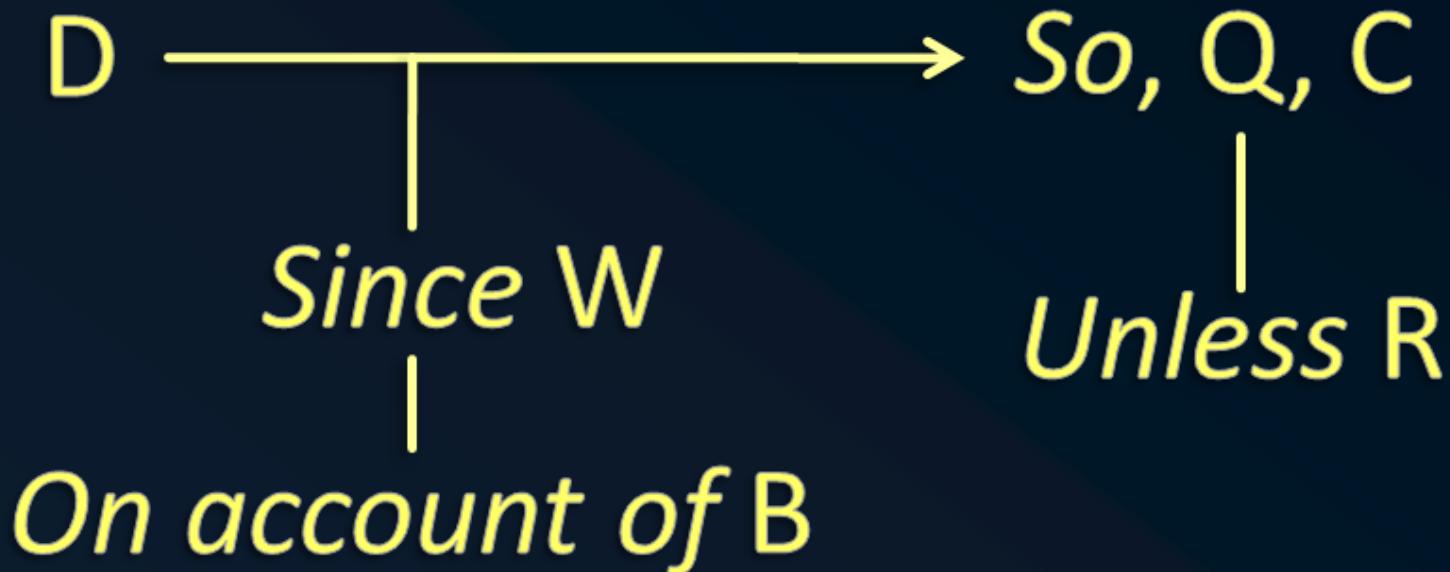
Object looks red



*Object **is** red*



Toulmin's Scheme

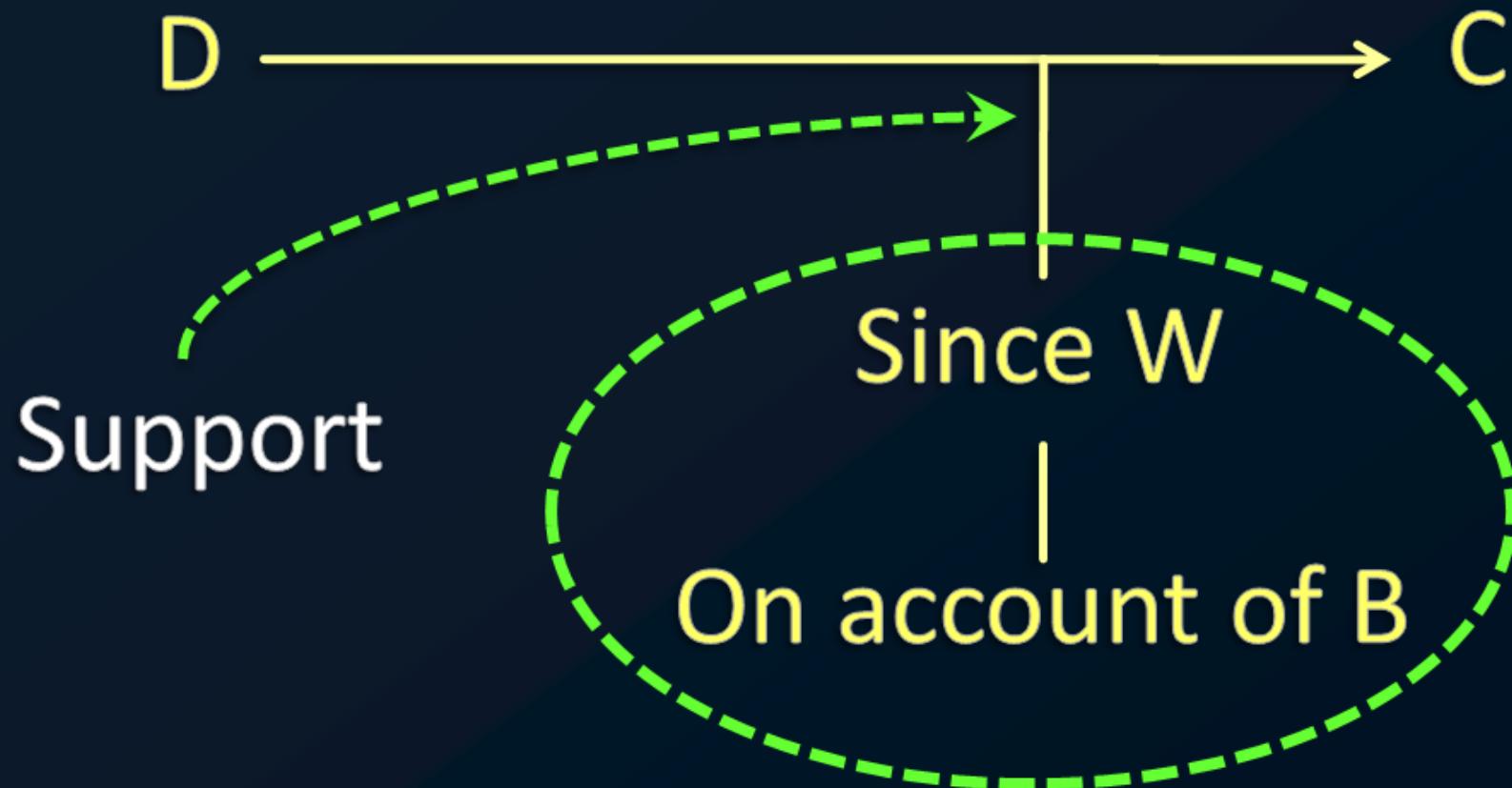


C: *Claim*
D: *Data*

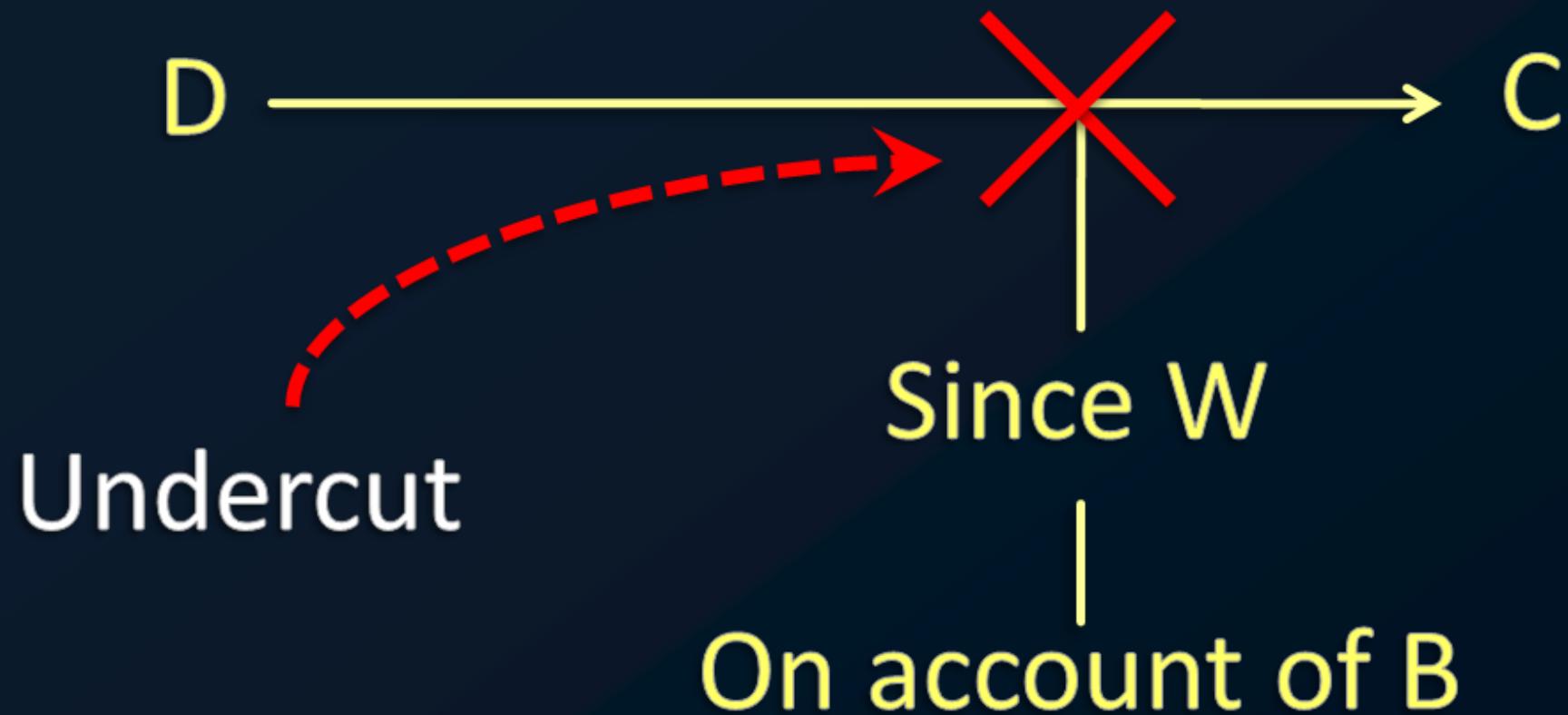
W: *Warrant*
B: *Backing*

R: *Rebuttal*
Q: *Qualifier*

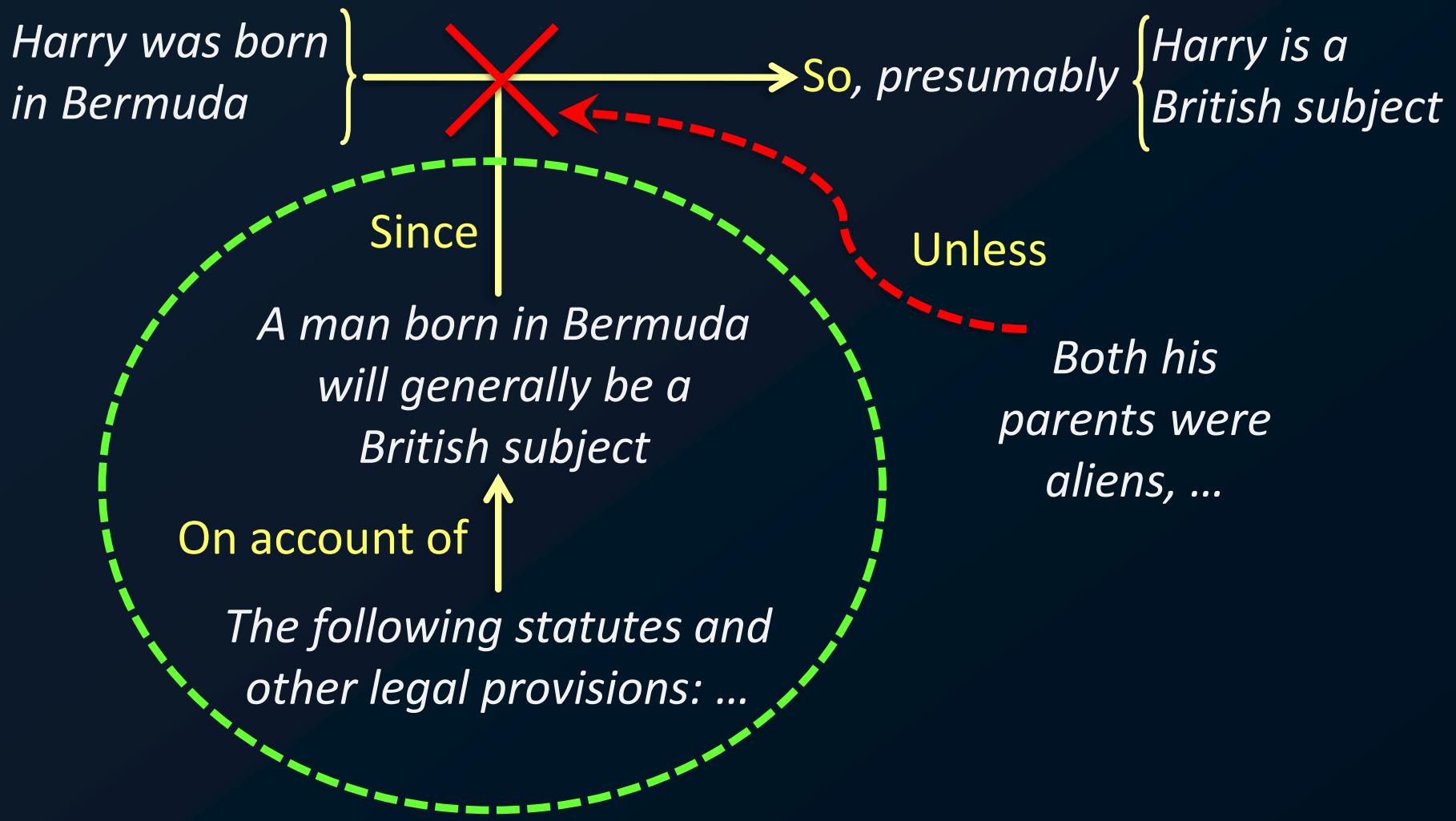
Toulmin's Backings



Pollock's Undercutting Defeaters



Toulmin's Example



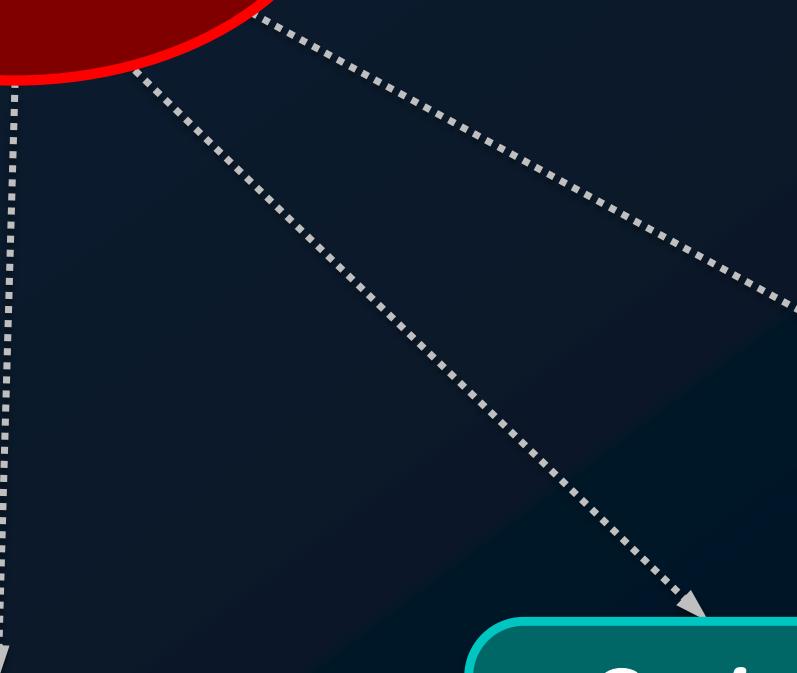
Extended
Defeasible Logic
Programming
(E-DeLP)

*E-DeLP
Language*

*Defeasible
Rules*

Facts

*Strict
Rules*



*E-DeLP
Language*

*Backing and
Undercutting
Rules*

*Defeasible
Rules*

Facts

*Strict
Rules*



E-DeLP – The Language

$$\Pi \left\{ \begin{array}{l} \text{- } \textit{Facts: ground literal } L \\ \text{- } \textit{Strict rules: } L_0 \leftarrow L_1, \dots, L_n \end{array} \right\} DeLP$$
$$\Delta \left\{ \text{- } \textit{Defeasible rules: } L_0 \prec L_1, \dots, L_n \right\}$$

E-DeLP – The Language

- $$\Pi \left\{ \begin{array}{l} \text{- } \textit{Facts: ground literal } L \\ \text{- } \textit{Strict rules: } L_0 \leftarrow L_1, \dots, L_n \end{array} \right.$$
- $$\Delta \left\{ \begin{array}{l} \text{- } \textit{Defeasible rules: } L_0 \prec L_1, \dots, L_n \\ \text{- } \textit{Backing rules: } [d\text{-rule}] \leftarrow \bigoplus [L_1, \dots, L_n] \end{array} \right.$$

E-DeLP – The Language

- $$\Pi \left\{ \begin{array}{l} \text{- } \textit{Facts: ground literal } L \\ \text{- } \textit{Strict rules: } L_0 \leftarrow L_1, \dots, L_n \end{array} \right.$$
- $$\Delta \left\{ \begin{array}{l} \text{- } \textit{Defeasible rules: } L_0 \prec L_1, \dots, L_n \\ \text{- } \textit{Backing rules: } [d\text{-rule}] \leftarrow \oplus [L_1, \dots, L_n] \\ \text{- } \textit{Undercutting rules: } [d\text{-rule}] \leftarrow \otimes [L_1, \dots, L_n] \end{array} \right.$$

E-DeLP – The Language

Π	{	- <i>Facts: ground literal L</i>
	-	<i>Strict rules:</i> $L_0 \leftarrow L_1, \dots, L_n$
Δ	{	- <i>Defeasible rules:</i> $L_0 \prec L_1, \dots, L_n$
	-	<i>Backing rules:</i> $[d\text{-rule}] \leftarrow \oplus [L_1, \dots, L_n]$
Σ	{	- <i>Undercutting rules:</i> $[d\text{-rule}] \leftarrow \otimes [L_1, \dots, L_n]$

Extended defeasible logic program:

$$\mathcal{P} = (\Pi, \Delta, \Sigma)$$

Example

A possible representation for Toulmin's example in E-DeLP:

$$\mathcal{P}_1 = (\Pi_1, \Delta_1, \Sigma_1)$$

$\Pi_1 = \{ \text{born_in_bermuda(harry)}, \text{british_parliament_acts}, \text{alien_parents(harry)} \}$

$\Delta_1 = \{ \text{british_subject}(X) \prec \text{born_in_bermuda}(X) \}$

$\Sigma_1 = \{ [\text{british_subject}(X) \prec \text{born_in_bermuda}(X)] \leftarrow \otimes [\text{alien_parents}(X)],$

$[\text{british_subject}(X) \prec \text{born_in_bermuda}(X)] \leftarrow \oplus [\text{british_parliament_acts}] \}$

E-DeLP – Arguments

From an extended defeasible logic program (e-de.l.p.) \mathcal{P} , three different types of arguments can be obtained:

- *Claim Argument*
- *Undercutting Argument*
- *Backing Argument*

E-DeLP – Arguments

Claim Argument $\langle \mathcal{A}, L \rangle$ for a literal L :

- 1) $\mathcal{A} \subseteq (\Delta \cup \Sigma)$
- 2) $\Pi \cup \mathcal{A} \succsim L$
- 3) $\Pi \cup \mathcal{A}$ is non-contradictory
- 4) \mathcal{A} is minimal: there is no $\mathcal{B} \subsetneq \mathcal{A}$ satisfying 2) and 3)

E-DeLP – Arguments

Undercutting Argument $\langle \mathcal{A}, r \rangle_u$ for a d-rule r is

$\mathcal{A} = \{ [r] \leftarrow \otimes [L_1, \dots, L_n] \} \cup \mathcal{A}'$ and:

- 1) $\mathcal{A} \subseteq (\Delta \cup \Sigma)$
- 2) $\Pi \cup \mathcal{A}' \vdash_{\mathcal{P}} L_i \quad (1 \leq i \leq n)$
- 3) $\Pi \cup \mathcal{A}'$ is non-contradictory
- 4) \mathcal{A}' is minimal: there is no $\mathcal{B} \subsetneq \mathcal{A}'$ satisfying
2) and 3)

E-DeLP – Arguments

Backing Argument $\langle \mathcal{A}, r \rangle_b$ for a d-rule r is

$\mathcal{A} = \{ [r] \leftarrow \bigoplus [L_1, \dots, L_n] \} \cup \mathcal{A}'$ and:

- 1) $\mathcal{A} \subseteq (\Delta \cup \Sigma)$
- 2) $\Pi \cup \mathcal{A}' \vdash_{\mathcal{P}} L_i \quad (1 \leq i \leq n)$
- 3) $\Pi \cup \mathcal{A}'$ is non-contradictory
- 4) \mathcal{A}' is minimal: there is no $\mathcal{B} \subsetneq \mathcal{A}'$ satisfying 2) and 3)

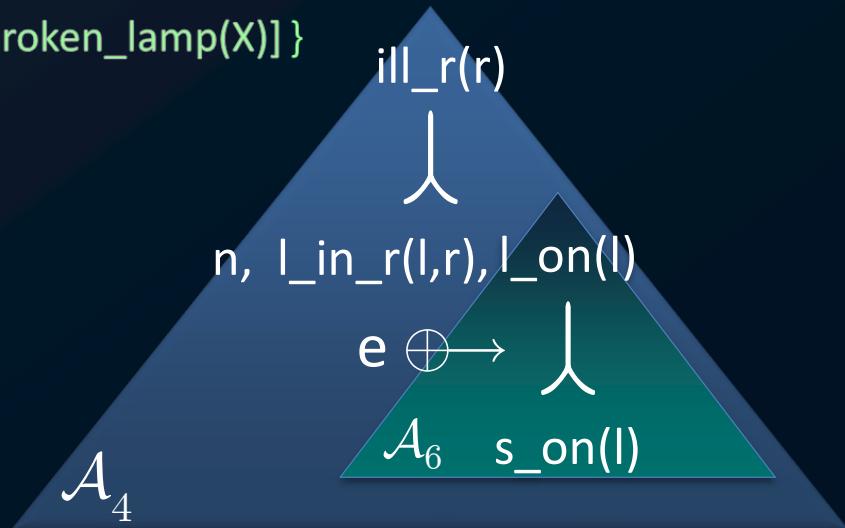
Example

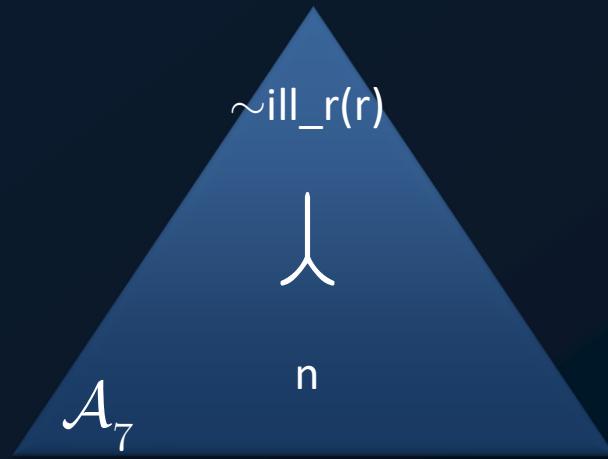
$$\mathcal{P}_2 = (\Pi_2, \Delta_2, \Sigma_2)$$

$$\Pi_2 = \{ \text{switch_on}(l), \text{night}, \text{lamp_in_room}(l,r), \text{electricity}, \text{broken_lamp}(l) \}$$

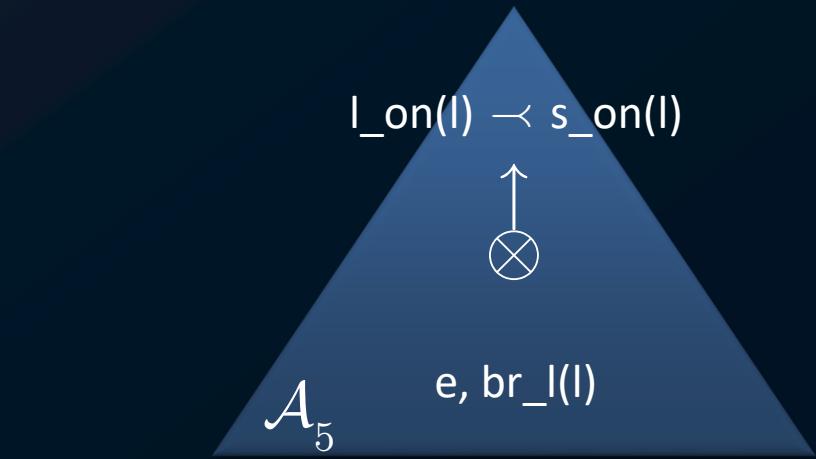
$$\begin{aligned} \Delta_2 = \{ & \quad \text{light_on}(X) \prec \text{switch_on}(X) \\ & \text{illuminated_room}(X) \prec \text{day} \\ & \sim \text{illuminated_room}(X) \prec \text{night} \\ & \text{illuminated_room}(X) \prec \text{night}, \text{lamp_in_room}(Y, X), \text{light_on}(Y) \} \end{aligned}$$

$$\begin{aligned} \Sigma_2 = \{ & [\text{light_on}(X) \prec \text{switch_on}(X)] \leftarrow \oplus [\text{electricity}] \\ & [\text{light_on}(X) \prec \text{switch_on}(X)] \leftarrow \oplus [\sim \text{electricity}, \text{emergency_lamp}(X)] \\ & [\text{light_on}(X) \prec \text{switch_on}(X)] \leftarrow \otimes [\sim \text{electricity}] \\ & [\text{light_on}(X) \prec \text{switch_on}(X)] \leftarrow \otimes [\text{electricity}, \text{broken_lamp}(X)] \} \end{aligned}$$

$\Pi_2 = \{ \text{switch_on}(l), \text{night}, \text{lamp_in_room}(l,r), \text{electricity}, \text{broken_lamp}(l) \}$
 $\Delta_2 = \{ \begin{aligned} & \text{light_on}(X) \prec \text{switch_on}(X) \\ & \text{illuminated_room}(X) \prec \text{day} \\ & \sim \text{illuminated_room}(X) \prec \text{night} \\ & \text{illuminated_room}(X) \prec \text{night}, \text{lamp_in_room}(Y,X), \text{light_on}(Y) \end{aligned} \}$
 $\Sigma_2 = \{ \begin{aligned} & [\text{light_on}(X) \prec \text{switch_on}(X)] \leftarrow \oplus [\text{electricity}] \\ & [\text{light_on}(X) \prec \text{switch_on}(X)] \leftarrow \oplus [\sim \text{electricity}, \text{emergency_lamp}(X)] \\ & [\text{light_on}(X) \prec \text{switch_on}(X)] \leftarrow \otimes [\sim \text{electricity}] \\ & [\text{light_on}(X) \prec \text{switch_on}(X)] \leftarrow \otimes [\text{electricity}, \text{broken_lamp}(X)] \end{aligned} \}$
 $\langle \mathcal{A}_4, \text{ill_r}(r) \rangle$
 $\mathcal{A}_4 = \{ \begin{aligned} & \text{ill_r}(r) \prec n, l_{\text{in_r}}(l,r), l_{\text{on}}(l) \\ & l_{\text{on}}(l) \prec s_{\text{on}}(l) \\ & [l_{\text{on}}(l) \prec s_{\text{on}}(l)] \leftarrow \oplus [e] \end{aligned} \}$

 $\langle \mathcal{A}_6, l_{\text{on}}(l) \prec s_{\text{on}}(l) \rangle_b$
 $\mathcal{A}_6 = \{ [l_{\text{on}}(l) \prec s_{\text{on}}(l)] \leftarrow \oplus [e] \}$

$\Pi_2 = \{ \text{switch_on}(l), \text{night}, \text{lamp_in_room}(l,r), \text{electricity}, \text{broken_lamp}(l) \}$
 $\Delta_2 = \{ \begin{aligned} & \text{light_on}(X) \prec \text{switch_on}(X) \\ & \text{illuminated_room}(X) \prec \text{day} \\ & \sim \text{illuminated_room}(X) \prec \text{night} \\ & \text{illuminated_room}(X) \prec \text{night}, \text{lamp_in_room}(Y,X), \text{light_on}(Y) \end{aligned} \}$
 $\Sigma_2 = \{ \begin{aligned} & [\text{light_on}(X) \prec \text{switch_on}(X)] \leftarrow \oplus [\text{electricity}] \\ & [\text{light_on}(X) \prec \text{switch_on}(X)] \leftarrow \oplus [\sim \text{electricity}, \text{emergency_lamp}(X)] \\ & [\text{light_on}(X) \prec \text{switch_on}(X)] \leftarrow \otimes [\sim \text{electricity}] \\ & [\text{light_on}(X) \prec \text{switch_on}(X)] \leftarrow \otimes [\text{electricity}, \text{broken_lamp}(X)] \end{aligned} \}$


$\langle \mathcal{A}_7, \sim \text{ill_r}(r) \rangle \quad \mathcal{A}_7 = \{ \sim \text{ill_r}(r) \prec n \}$



$\langle \mathcal{A}_5, l_{\text{on}}(l) \prec s_{\text{on}}(l) \rangle_u \quad \mathcal{A}_5 = \{ [l_{\text{on}}(l) \prec s_{\text{on}}(l)] \leftarrow \otimes [e, br_l(l)] \}$

E-DeLP – Attack

Rebutting Attack: $\langle \mathcal{A}_1, L_1 \rangle$ *rebuts* $\langle \mathcal{A}_2, L_2 \rangle$ at the literal L if there exists a *claim sub-argument* $\langle \mathcal{A}, L \rangle$ of argument $\langle \mathcal{A}_2, L_2 \rangle$ such that L and L_1 disagree.

Undercutting Attack: An undercutting argument $\langle \mathcal{A}, r \rangle$ *undercuts* $\langle \mathcal{B}, L \rangle$ at the *rule* r if $r \in \mathcal{B}$.

Undermining Attack: $\langle \mathcal{A}_1, L_1 \rangle$ *undermines* $\langle \mathcal{A}_2, L_2 \rangle$ at the literal P if $\langle \mathcal{A}_1, L_1 \rangle$ *rebuts* $\langle \mathcal{A}_2, L_2 \rangle$ at the literal P , and P is a *presumption*.

E-DeLP - Defeat

Three forms of defeat may occur between arguments:

Rebutting Defeat: $\langle \mathcal{A}_1, L_1 \rangle$ rebuts $\langle \mathcal{A}_2, L_2 \rangle$ at the literal L , and the attacked sub-argument $\langle \mathcal{A}, L \rangle$ of $\langle \mathcal{A}_2, L_2 \rangle$ is such that $\langle \mathcal{A}, L \rangle \not\proves \langle \mathcal{A}_1, L_1 \rangle$.

Undercutting Defeat: $\langle \mathcal{A}, R \rangle$ undercuts $\langle \mathcal{B}, H \rangle$ at the defeasible rule R , if $R \in \mathcal{B}$.

Undermining Defeat: $\langle \mathcal{A}_1, L_1 \rangle$ undermines $\langle \mathcal{A}_2, L_2 \rangle$ at the literal L , and the attacked sub-argument $\langle \mathcal{A}, L \rangle$ of $\langle \mathcal{A}_2, L_2 \rangle$ is such that $\langle \mathcal{A}, L \rangle \not\proves \langle \mathcal{A}_1, L_1 \rangle$.

ill_r(r)

\nwarrow

$n, \text{l_in_r(l,r)}, \text{l_on}(l)$

$e \oplus \rightarrow \nwarrow$

$\mathcal{A}_6 \quad s_{\text{on}}(l)$

\mathcal{A}_4

$\sim \text{ill_r(r)}$

\nwarrow

n

\mathcal{A}_7

$\Pi_2 = \{ \text{switch_on}(l), \text{night}, \text{lamp_in_room}(l,r), \text{electricity}, \text{broken_lamp}(l) \}$

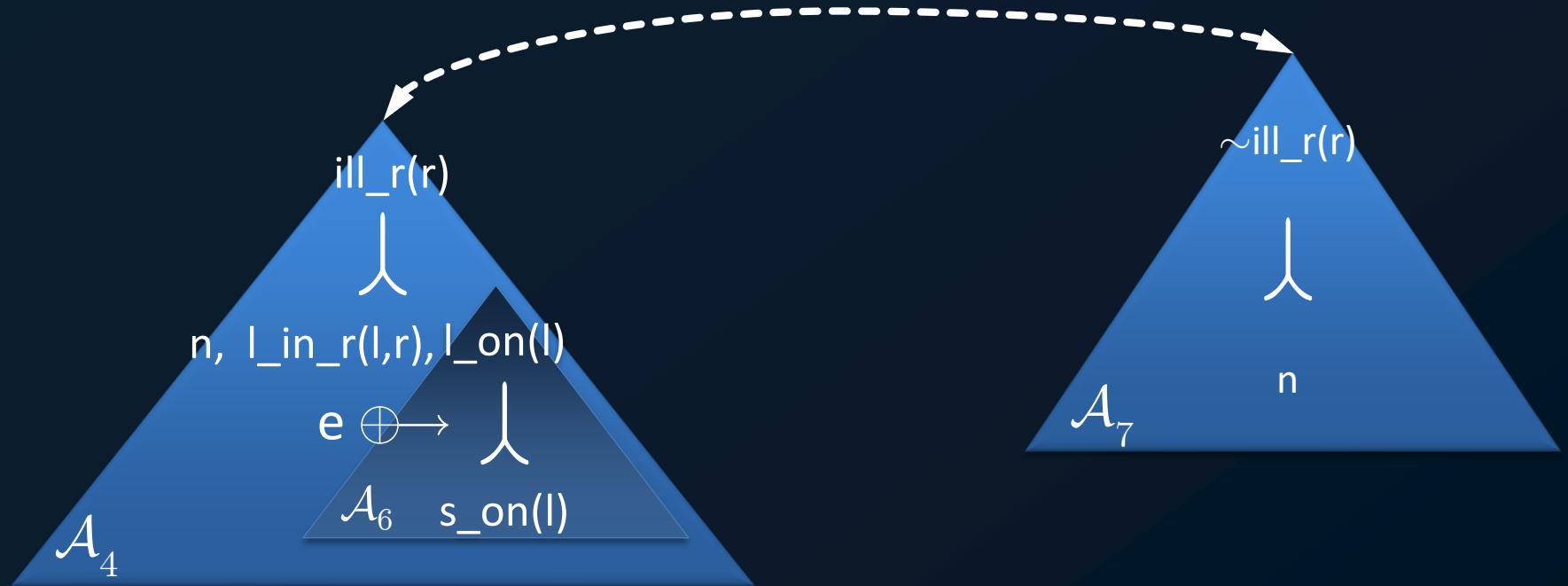
$\Delta_2 = \{ \text{light_on}(X) \prec \text{switch_on}(X)$
 $\text{illuminated_room}(X) \prec \text{day}$
 $\sim \text{illuminated_room}(X) \prec \text{night}$
 $\text{illuminated_room}(X) \prec \text{night}, \text{lamp_in_room}(Y,X), \text{light_on}(Y) \}$

$\text{l_on}(l) \prec s_{\text{on}}(l)$

\uparrow
 \otimes

$\Sigma_2 = \{ [\text{light_on}(X) \prec \text{switch_on}(X)] \leftarrow \oplus [\text{electricity}]$
 $[\text{light_on}(X) \prec \text{switch_on}(X)] \leftarrow \oplus [\sim \text{electricity}, \text{emergency_lamp}(X)]$
 $[\text{light_on}(X) \prec \text{switch_on}(X)] \leftarrow \otimes [\sim \text{electricity}]$
 $[\text{light_on}(X) \prec \text{switch_on}(X)] \leftarrow \otimes [\text{electricity}, \text{broken_lamp}(X)] \}$

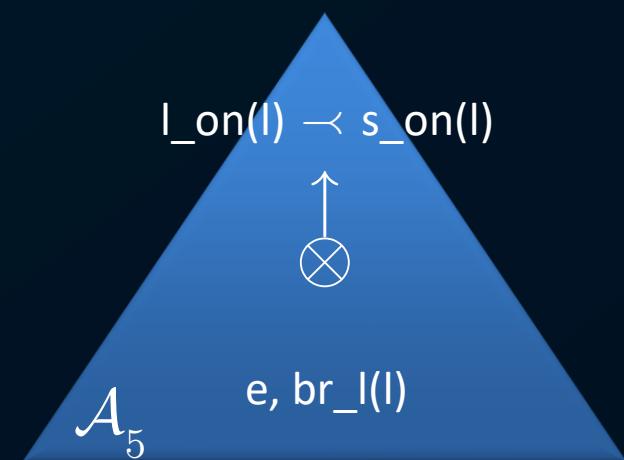
$\mathcal{A}_5 \quad e, \text{br_l}(l)$

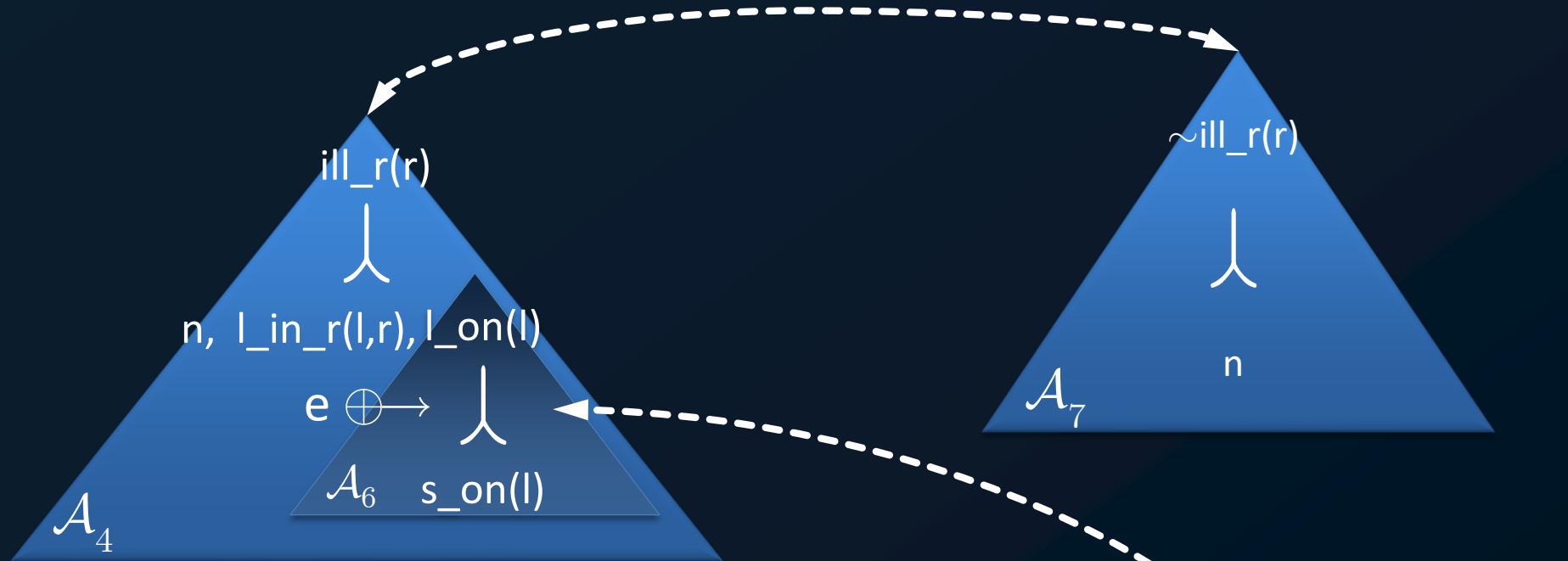


$\Pi_2 = \{ \text{switch_on}(l), \text{night}, \text{lamp_in_room}(l,r), \text{electricity}, \text{broken_lamp}(l) \}$

$\Delta_2 = \{ \text{light_on}(X) \leftarrow \text{switch_on}(X)$
 $\text{illuminated_room}(X) \leftarrow \text{day}$
 $\sim\text{illuminated_room}(X) \leftarrow \text{night}$
 $\text{illuminated_room}(X) \leftarrow \text{night}, \text{lamp_in_room}(Y,X), \text{light_on}(Y) \}$

$\Sigma_2 = \{ [\text{light_on}(X) \leftarrow \text{switch_on}(X)] \leftarrow \oplus [\text{electricity}]$
 $[\text{light_on}(X) \leftarrow \text{switch_on}(X)] \leftarrow \oplus [\sim\text{electricity}, \text{emergency_lamp}(X)]$
 $[\text{light_on}(X) \leftarrow \text{switch_on}(X)] \leftarrow \otimes [\sim\text{electricity}]$
 $[\text{light_on}(X) \leftarrow \text{switch_on}(X)] \leftarrow \otimes [\text{electricity}, \text{broken_lamp}(X)] \}$

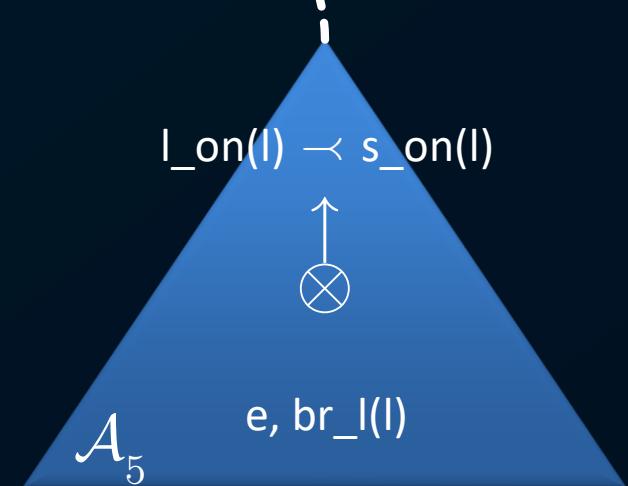


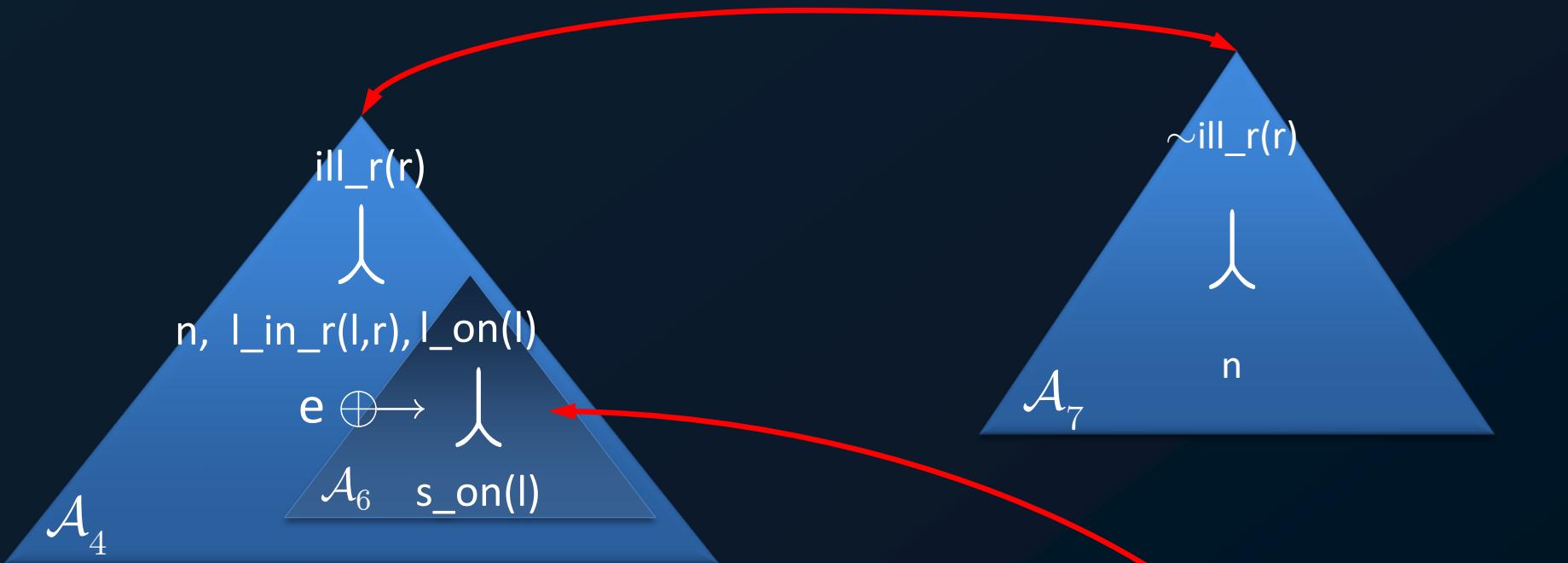


$\Pi_2 = \{ \text{switch_on}(l), \text{night}, \text{lamp_in_room}(l,r), \text{electricity}, \text{broken_lamp}(l) \}$

$\Delta_2 = \{ \text{light_on}(X) \prec \text{switch_on}(X)$
 $\text{illuminated_room}(X) \prec \text{day}$
 $\sim \text{illuminated_room}(X) \prec \text{night}$
 $\text{illuminated_room}(X) \prec \text{night}, \text{lamp_in_room}(Y, X), \text{light_on}(Y) \}$

$\Sigma_2 = \{ [\text{light_on}(X) \prec \text{switch_on}(X)] \leftarrow \oplus [\text{electricity}]$
 $[\text{light_on}(X) \prec \text{switch_on}(X)] \leftarrow \oplus [\sim \text{electricity}, \text{emergency_lamp}(X)]$
 $[\text{light_on}(X) \prec \text{switch_on}(X)] \leftarrow \otimes [\sim \text{electricity}]$
 $[\text{light_on}(X) \prec \text{switch_on}(X)] \leftarrow \otimes [\text{electricity}, \text{broken_lamp}(X)] \}$





$\Pi_2 = \{ \text{switch_on}(l), \text{night}, \text{lamp_in_room}(l,r), \text{electricity}, \text{broken_lamp}(l) \}$

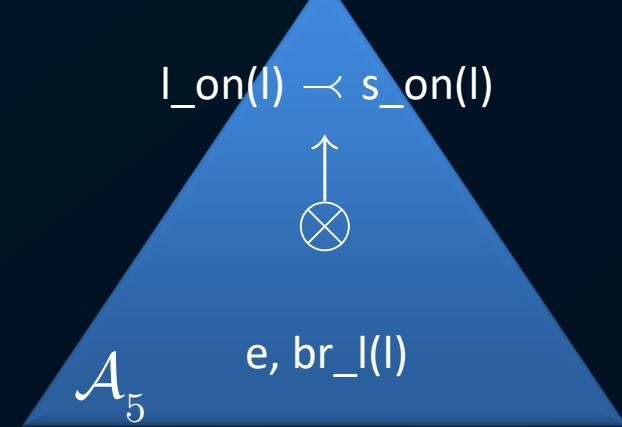
$\Delta_2 = \{ \text{light_on}(X) \rightsquigarrow \text{switch_on}(X)$
 $\text{illuminated_room}(X) \rightsquigarrow \text{day}$
 $\sim \text{illuminated_room}(X) \rightsquigarrow \text{night}$
 $\text{illuminated_room}(X) \rightsquigarrow \text{night}, \text{lamp_in_room}(Y,X), \text{light_on}(Y) \}$

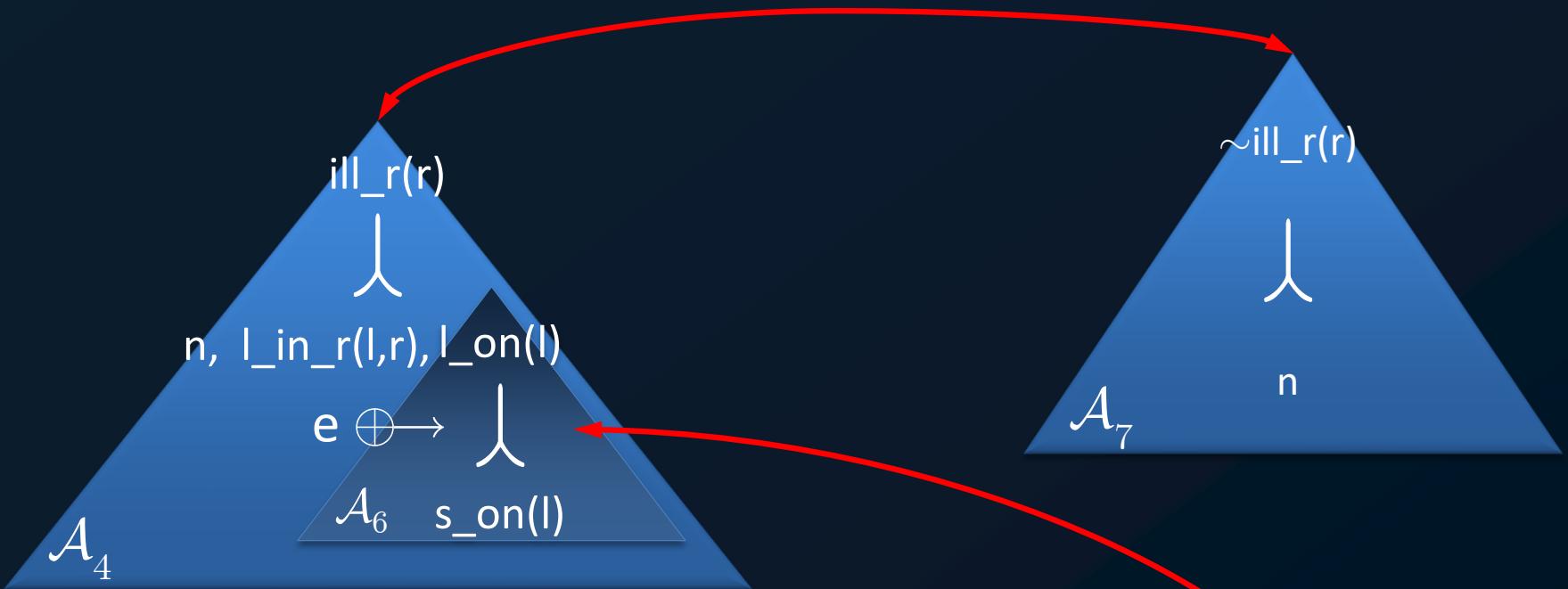
$\Sigma_2 = \{ [\text{light_on}(X) \rightsquigarrow \text{switch_on}(X)] \leftarrow \oplus [\text{electricity}]$
 $[\text{light_on}(X) \rightsquigarrow \text{switch_on}(X)] \leftarrow \oplus [\sim \text{electricity}, \text{emergency_lamp}(X)]$
 $[\text{light_on}(X) \rightsquigarrow \text{switch_on}(X)] \leftarrow \otimes [\sim \text{electricity}]$
 $[\text{light_on}(X) \rightsquigarrow \text{switch_on}(X)] \leftarrow \otimes [\text{electricity}, \text{broken_lamp}(X)] \}$

Criterion:

$$\langle \mathcal{A}_4, \text{ill_r_}(r) \rangle \succ \langle \mathcal{A}_7, \sim \text{ill_r}(r) \rangle$$

$$\langle \mathcal{A}_5, \text{l_on}(l) \rightsquigarrow \text{s_on}(l) \rangle_u \succ \langle \mathcal{A}_6, \text{l_on}(l) \rightsquigarrow \text{s_on}(l) \rangle_b$$





$\Pi_2 = \{ \text{switch_on}(l), \text{night}, \text{lamp_in_room}(l,r), \text{electricity}, \text{broken_lamp}(l) \}$

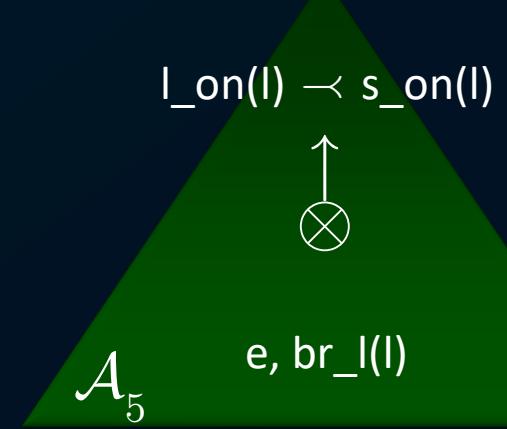
$\Delta_2 = \{ \text{light_on}(X) \prec \text{switch_on}(X)$
 $\text{illuminated_room}(X) \prec \text{day}$
 $\sim \text{illuminated_room}(X) \prec \text{night}$
 $\text{illuminated_room}(X) \prec \text{night}, \text{lamp_in_room}(Y,X), \text{light_on}(Y) \}$

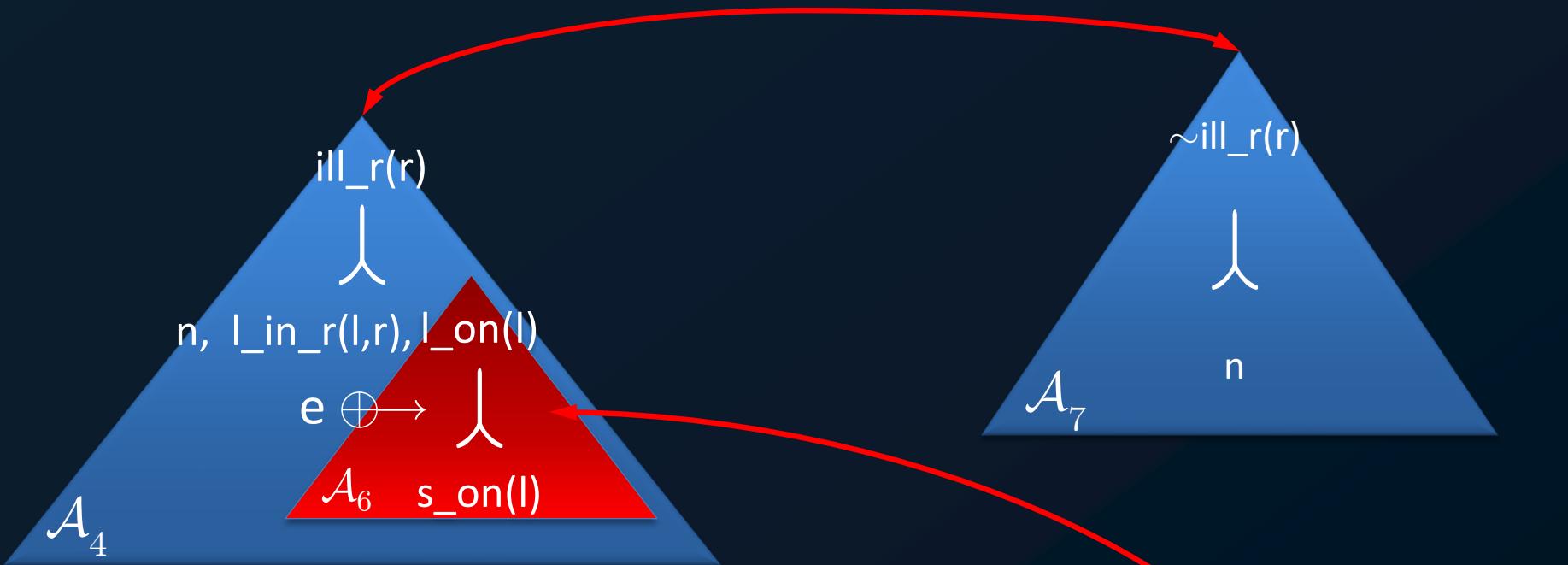
$\Sigma_2 = \{ [\text{light_on}(X) \prec \text{switch_on}(X)] \leftarrow \oplus [\text{electricity}]$
 $[\text{light_on}(X) \prec \text{switch_on}(X)] \leftarrow \oplus [\sim \text{electricity}, \text{emergency_lamp}(X)]$
 $[\text{light_on}(X) \prec \text{switch_on}(X)] \leftarrow \otimes [\sim \text{electricity}]$
 $[\text{light_on}(X) \prec \text{switch_on}(X)] \leftarrow \otimes [\text{electricity}, \text{broken_lamp}(X)] \}$

Criterion:

$$\langle \mathcal{A}_4, \text{ill_r_}(r) \rangle \succ \langle \mathcal{A}_7, \sim \text{ill_r}(r) \rangle$$

$$\langle \mathcal{A}_5, l_{\text{on}}(l) \prec s_{\text{on}}(l) \rangle_u \succ \langle \mathcal{A}_6, l_{\text{on}}(l) \prec s_{\text{on}}(l) \rangle_b$$





$\Pi_2 = \{ \text{switch_on}(l), \text{night}, \text{lamp_in_room}(l, r), \text{electricity}, \text{broken_lamp}(l) \}$

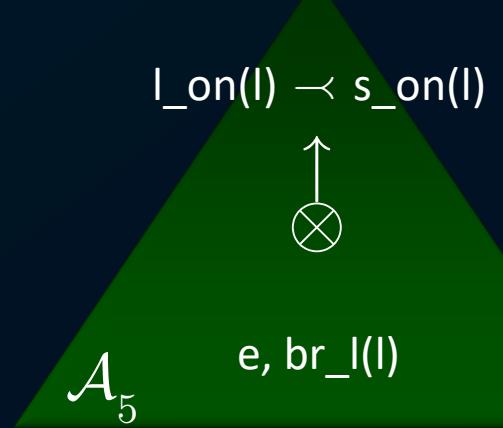
$\Delta_2 = \{ \text{light_on}(X) \prec \text{switch_on}(X)$
 $\text{illuminated_room}(X) \prec \text{day}$
 $\sim \text{illuminated_room}(X) \prec \text{night}$
 $\text{illuminated_room}(X) \prec \text{night}, \text{lamp_in_room}(Y, X), \text{light_on}(Y) \}$

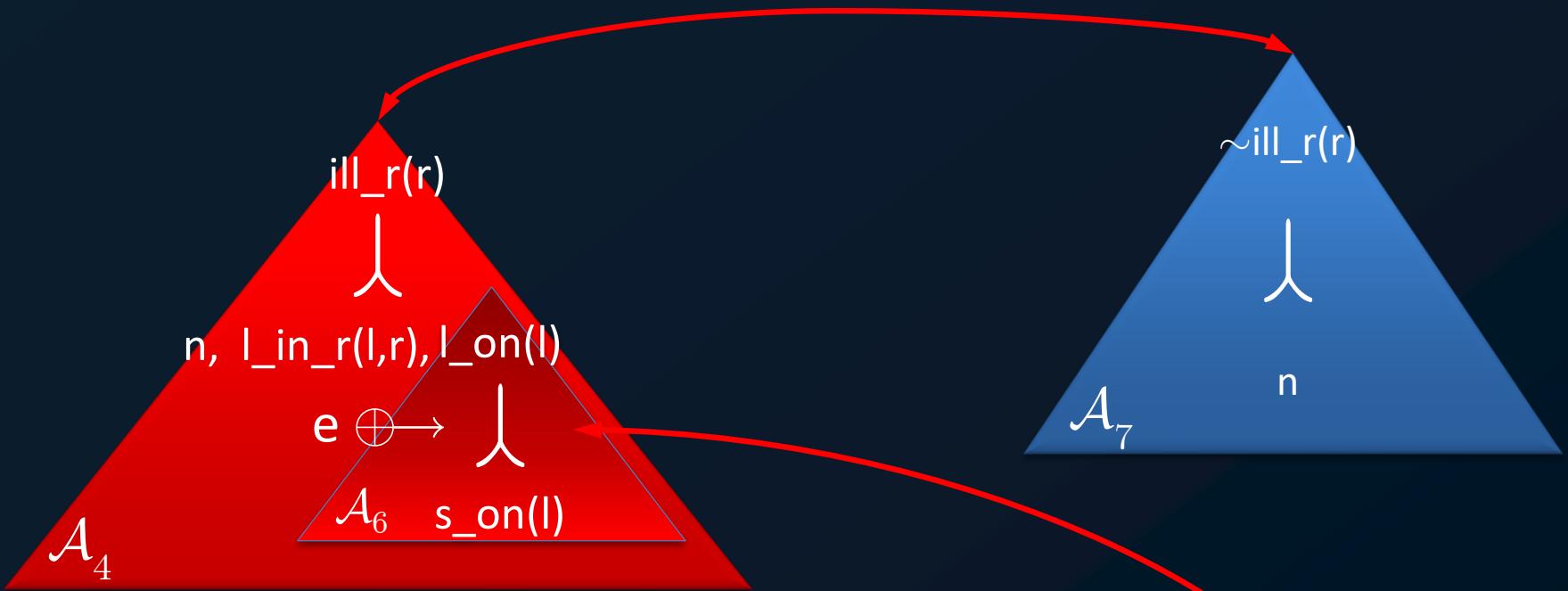
$\Sigma_2 = \{ [\text{light_on}(X) \prec \text{switch_on}(X)] \leftarrow \oplus [\text{electricity}]$
 $[\text{light_on}(X) \prec \text{switch_on}(X)] \leftarrow \oplus [\sim \text{electricity}, \text{emergency_lamp}(X)]$
 $[\text{light_on}(X) \prec \text{switch_on}(X)] \leftarrow \otimes [\sim \text{electricity}]$
 $[\text{light_on}(X) \prec \text{switch_on}(X)] \leftarrow \otimes [\text{electricity}, \text{broken_lamp}(X)] \}$

Criterion:

$$\langle \mathcal{A}_4, \text{ill_r_r} \rangle \succ \langle \mathcal{A}_7, \sim \text{ill_r_r} \rangle$$

$$\langle \mathcal{A}_5, l_{\text{on}}(l) \prec s_{\text{on}}(l) \rangle_u \succ \langle \mathcal{A}_6, l_{\text{on}}(l) \prec s_{\text{on}}(l) \rangle_b$$





$\Pi_2 = \{ \text{switch_on}(l), \text{night}, \text{lamp_in_room}(l,r), \text{electricity}, \text{broken_lamp}(l) \}$

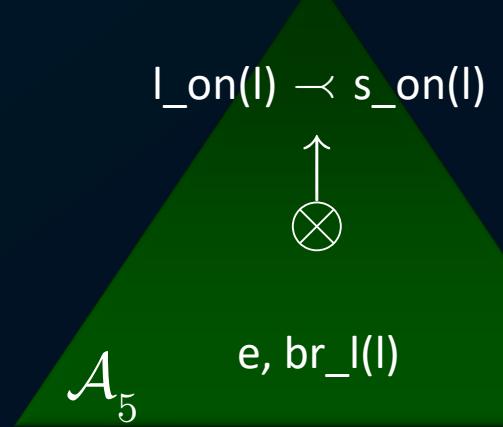
$\Delta_2 = \{ \text{light_on}(X) \prec \text{switch_on}(X)$
 $\text{illuminated_room}(X) \prec \text{day}$
 $\sim \text{illuminated_room}(X) \prec \text{night}$
 $\text{illuminated_room}(X) \prec \text{night}, \text{lamp_in_room}(Y,X), \text{light_on}(Y) \}$

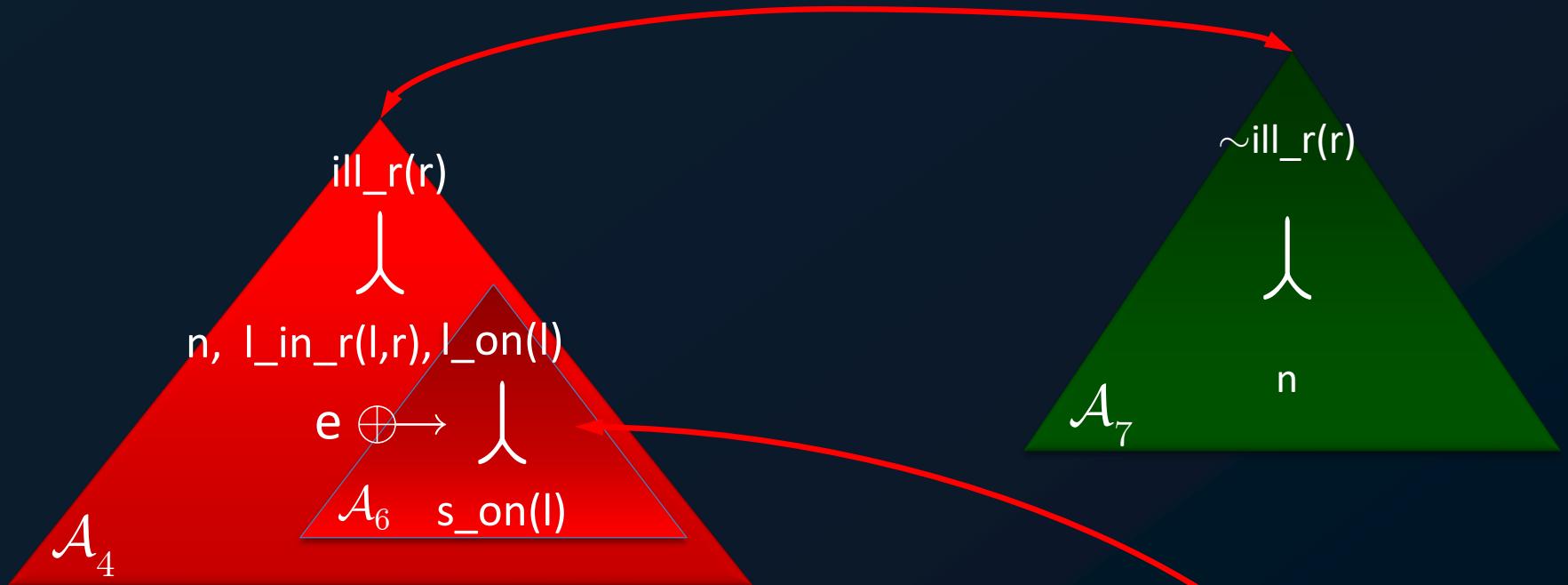
$\Sigma_2 = \{ [\text{light_on}(X) \prec \text{switch_on}(X)] \leftarrow \oplus [\text{electricity}]$
 $[\text{light_on}(X) \prec \text{switch_on}(X)] \leftarrow \oplus [\sim \text{electricity}, \text{emergency_lamp}(X)]$
 $[\text{light_on}(X) \prec \text{switch_on}(X)] \leftarrow \otimes [\sim \text{electricity}]$
 $[\text{light_on}(X) \prec \text{switch_on}(X)] \leftarrow \otimes [\text{electricity}, \text{broken_lamp}(X)] \}$

Criterion:

$$\langle \mathcal{A}_4, \text{ill_r_r} \rangle \succ \langle \mathcal{A}_7, \sim \text{ill_r_r} \rangle$$

$$\langle \mathcal{A}_5, \text{l_on}(l) \prec \text{s_on}(l) \rangle_u \succ \langle \mathcal{A}_6, \text{l_on}(l) \prec \text{s_on}(l) \rangle_b$$





$\Pi_2 = \{ \text{switch_on}(l), \text{night}, \text{lamp_in_room}(l, r), \text{electricity}, \text{broken_lamp}(l) \}$

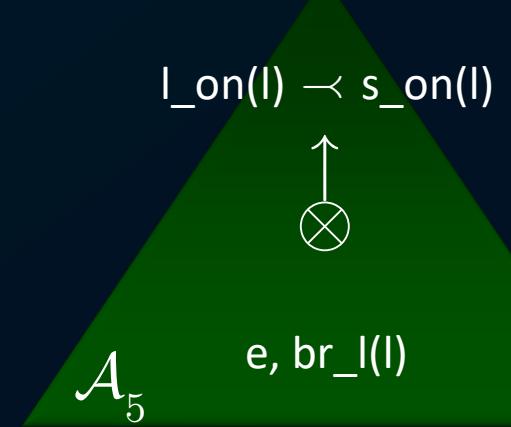
$\Delta_2 = \{ \text{light_on}(X) \prec \text{switch_on}(X)$
 $\text{illuminated_room}(X) \prec \text{day}$
 $\sim \text{illuminated_room}(X) \prec \text{night}$
 $\text{illuminated_room}(X) \prec \text{night}, \text{lamp_in_room}(Y, X), \text{light_on}(Y) \}$

$\Sigma_2 = \{ [\text{light_on}(X) \prec \text{switch_on}(X)] \leftarrow \oplus [\text{electricity}]$
 $[\text{light_on}(X) \prec \text{switch_on}(X)] \leftarrow \oplus [\sim \text{electricity}, \text{emergency_lamp}(X)]$
 $[\text{light_on}(X) \prec \text{switch_on}(X)] \leftarrow \otimes [\sim \text{electricity}]$
 $[\text{light_on}(X) \prec \text{switch_on}(X)] \leftarrow \otimes [\text{electricity}, \text{broken_lamp}(X)] \}$

Criterion:

$$\langle \mathcal{A}_4, \text{ill_r}(r) \rangle \succ \langle \mathcal{A}_7, \sim \text{ill_r}(r) \rangle$$

$$\langle \mathcal{A}_5, l_{\text{on}}(l) \prec s_{\text{on}}(l) \rangle_u \succ \langle \mathcal{A}_6, l_{\text{on}}(l) \prec s_{\text{on}}(l) \rangle_b$$



Conclusions

- We have extended DeLP to capture two important notions in modeling argumentation
- And, *Backing & Undercutting Rules* are used to represent these notions:
 - Toulmin's backings are represented by providing support for defeasible rules
 - Pollock's undercutting defeaters can be expressed by an attack to a defeasible rule

Thank you!

Questions?

