$$1) f_{(x)} = (x+1)^{2}$$

$$f'_{(x)} = \lim_{\Delta x \to 0} \frac{((x+\Delta x)+1)^{2} - (x+1)^{2}}{\Delta x} =$$

$$f'_{(x)} = \lim_{\Delta x \to 0} \frac{(x+\Delta x+1)^{2} - (x+1)^{2}}{\Delta x} =$$

$$f'_{(x)} = \lim_{\Delta x \to 0} \frac{(x^{2} + \Delta x^{2} + 1 + 2x\Delta x + 2x + 2\Delta x) - (x^{2} + 2x + 1)}{\Delta x} =$$

$$f'_{(x)} = \lim_{\Delta x \to 0} \frac{x^{2} + \Delta x^{2} + 1 + 2x\Delta x + 2x + 2\Delta x - x^{2} - 2x - 1}{\Delta x} =$$

$$f'_{(x)} = \lim_{\Delta x \to 0} \frac{\Delta x^{2} + 2x\Delta x + 2\Delta x}{\Delta x} =$$

$$f'_{(x)} = \lim_{\Delta x \to 0} \frac{\Delta x(\Delta x + 2x + 2)}{\Delta x} =$$

$$f'_{(x)} = \lim_{\Delta x \to 0} \Delta x + 2x + 2 =$$

$$f'_{(x)} = 0 + 2x + 2$$

$$f'_{(x)} = 2 + 2x = 2(x + 1)$$