Multiplanetary Systems from Simulated TESS Transit Timing Variations[1]

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[1]This is just a very basic cover page produced by LaTeX – when the thesis is done you can get a more formal cover page from Eva Jurlander.

(this page will contain some more official information in the final version)

Abstract

The abstract is a short summary describing the content of the main text. This should give enough information about the contents to decide for the intended audience whether further reading will be useful. The size should be about half a page, best written at the end, after most of the thesis is written.

Populärvetenskaplig beskrivning

När vi letar efter exoplaneter finns det ett antal olika metoder för att hitta dem. Den mest framgångsrika är transitmetoden där ljusstyrkan hos en stjärna studeras under en längre tid. När en planet passerar mellan sin stjärna och en observatör kan en minsking i stjärnans ljusstyrka ses. Uppreras detta i regelbunda intervall kan slutsatsen att det finns en planet runt stjärnan. Genom att studera minskningen i ljusstyrka kan storleken på planeten beräknas vilket kombinerat med massan som fås av andra metoder ger en insikt i hur och vad planeter är uppbygd av. En transit är detta fenomen då en planet passerar mellan stjärnan och en observatör.

Genom att jämföra tiden mellan varje transit för en planet kan ibland variationer ses. Detta beror på att det finns fler planeter runt stjärnan som med hjälp av gravitationskraften accelererar eller decelerera planeten som bevakas. Detta resulterar i att det är möjligt att hitta planeter som i andra metoder är osynliga.

Keplerteleskopet är ett rymdbaserat teleskop som använder transitmetoden för att hitta exoplaneter. Det har sedan 2009 hittat över 1000 bekräftade exoplaneter vilket gör den till det hittils mest framgångsfulla upgradet i jakten på exoplaneter. TESS, vilket står för Transiting-Exoplanet Survet Satellite, är ett teleskop som ska skjutas upp under våren 2018 och använda transitmetoden för att hitta exoplaneter. TESS kommer bli den första rymdbaserade teleskopet att studera hela himlen och kommer observera över 200 000 stjärnor under uppdragets upsrungliga längd på två år.

Detta projekt kommer använda data från Keplerteleskopet och simulera data från TESS för att sedan använda den datan för att leta efter TTV. Detta ska ge en uppfattning om hur många system har fler än en planet och resultatet kommer kunna ses som en katalog över multi-planet system vilket kan underlätta framtida forskning där en katalog av detta slag kan vara till användning.

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Chapter 1

Introduction

This document is meant as a technical tutorial for writing an astronomy/astrophysics thesis in LaTeX. Detailed rules about the *contents* of the thesis (Bachelor's thesis or Master's thesis) can be found at the course websites.

1.1 Transits

A planet in orbit around it's host star may sometimes cross the line of sight of an observer. When this happens a slight decrease in the stars brightness can be measured. This is called a transit and is today used as a main method to discover exoplanets. From transits the radius of the planet can be determined but it can also be used to find additional planets around the host star which may not be transiting. This will be discussed in section 1.1.1. With the radius known from the transit method and the mass obtained from different methods such as, for example, the radial velocity method the density of the planet can be calculated. The density is important to understand what the planet is made of and the structure of it.

1.1.1 Variations

When measuring the time of one transit one may discover variations in the period which are called Transit-Timing Variations or TTVs. These variations arise from another planet in the system whose gravitational pull accelerates or decelerate the observed planet which results in increased or decreased transit times. An advantage of studying transits in search for TTVs is that planets which does not transit their star can be discovered through TTVs (Nesvorný et al. 2013). As most planets does not transit their star this can increase the number of known exoplanets drastically.

1.2 Kepler

The Kepler satellite launched in spring 2009 on a mission to study stars in a small patch in the sky to discover Earth-sized exoplanets within the habitable zone, where liquid water can exist on the planetary surface. The brightness of a large amount of stars are measured and then analyzed in order to detect transiting exoplanets.

Kepler started by looking at a very small patch of the sky but in July 2012 one of the four wheels used to keep the patch in focus broke. The telescope requires at least three wheels to function which kept the mission alive. In May 2013 a third wheel failed which resulted in the telescope no longer being able to collect data. The satellite was nonfunctional until the so-called "Second Light (K2)" in early 2014. This mission would use the telescopes remaining two wheels to study stars over a much larger area but for shorter periods.

According to Johnson (2018) Kepler found over 2300 confirmed exoplanets and about 2200 candidates which require further studies before they can be confirmed during the main mission, before the second wheel broke down. Since the start of K2 about 300 exoplanets have been confirmed and close to 500 candidate exoplanets. These numbers makes Kepler the most successful exoplanet hunting mission to this date.

1.3 TESS

The Transiting Exoplanet Survey Satellite, TESS, is a satellite due to launch spring 2018. The satellite is equipped with four cameras which will study the brightness of over 200 000 stars over a two year period. It is the first all-sky transit survey taking place in space.

TESS will study the whole sky by splitting it into 26 sectors which are observed for 27 days each. An illustration of this can be seen in figure 1.1 where the number of times TESS will observe each sector is shown.

1.4 TTVFast

TTVFast is a program created by Deck et al. (2014) which simulates planetary systems using an n-body integrator. It requires information about the system in the form of:

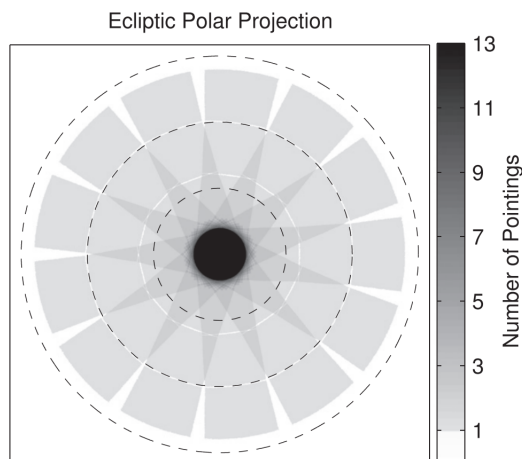- Gravitational constant in $AU^3 \text{day}^{-2} M_\odot^{-1}$

Figure 1.1: Illustration of the number of times TESS will observe each sector in the sky.
Source: Sullivan et al. (2015)

- Mass of the star

And also for each planet in the system:

- Period in days

- Eccentricity

- Inclination

- Longitude of ascending node, long node for short

- Argument of perihelion, argument for short

- Mean anomaly at the reference time

Where Longitude of ascending node and argument of perihelion are orbital elements. The reference time is the time of the start of the integration, in this paper: $t_ref = 0$. The program also requires parameters regarding the integration which are given in a setup file:

- Path to file containing info regarding the planets in the system.

- Reference time

- Time step which is 1/20 of the period

- Final time which in this paper is the duration of the integration

- Number of planets

- Input flag which specifies in which coordinate system the input parameters are given. This paper uses Jacobi coordinates which relate to a input flag $= 0$.

How these parameters are determined and "given" to TTVFast will be discussed in section 2.1 and 2.2.

Chapter 2

Method

The code used are written in Python and can be seen in abstract (REF ABSTRACT). It is executed by a bash script which runs the necessary components to create artificial planetary systems, run TTVFast on these systems to generate transit times and then analyze these times in order to find TTVs. These systems are simulated over a long time by the use of WHFast in order to determine the stability of them.

2.1   Simulation of TESS objects

The bash script starts by running the program to create the artificial systems. By combining data from Kepler obtained from the NASA Exoplanet Archive and the results from Sullivan et al. (2015), which contains one planet for each system, TESS data are simulated. The planets are separated into two groups based on the effective temperature of their host star. Planets around stars with an effective temperature below 4000 K are put in one group while planets around stars with effective temperature above 4000 K are put into another group. This prevents planets around cold stars to get "matched" with planets around hot stars.

For each planet in the Sullivan catalogue, a similar planet, in radius and period, are selected from the NASA archive. The ratio of radius and period between the two planets are calculated and multiplied with the Sullivan planets radius and period. This results in that the two planets are identical in radius and period. These ratios are then applied to the rest of the planets in this selected Kepler system to create an artificial system of planets.

The mass of the planet is required to simulate the system and is approximated

using equation 2.1 and 2.2 obtained from Sullivan et al. (2015):

$$M_p = M_\oplus \left[0,440 \left(\frac{R_p}{R_\oplus} \right)^3 + 0,614 \left(\frac{R_p}{R_\oplus} \right)^4 \right] \tag{2.1}$$

for planets with $R_p < 1,5\ \mathrm{R_\oplus}$ where $R_\oplus$ is the radius of Earth and $M_\oplus$ is the mass of Earth. For planets with $R_p \geq 1,5$ the equation changes to:

$$M_p = 2,69 \cdot M_\oplus \left(\frac{R_p}{R_\oplus} \right)^{0,93} \tag{2.2}$$

The mean anomaly is required for each planet and is acquired from the number of transits and the orbital period of the planet. By using a reference point specified when a planet is directly in front the the host star as seen from an observers point of view. This reference point corresponds to a mean anomaly of 90° at some time T_i, where i is the number of the planet in the system. For a two planet system this means that $M_1 = 90°$ at some time T_1 and $M_2 = 90°$ at some time T_2. In order to calculate the mean anomaly at some time a time reference point is defined as $t = 0$ and the goal is the calculate the mean anomaly of some planet i. This can be done by using the mean anomaly at $t = T_i$ and subtracting the number of degrees, $\mathrm{num_{deg}}$, the planet have traveled since then:

$$M_i(t = 0) = M_i(t = T_i) - \mathrm{num_{deg}} \tag{2.3}$$

$M_i(t = T_i) = 90°$ and the number of degrees traveled is 360° multiplied by the number of orbits since t_0:

$$M_i(t = 0) = 90 - 360 \cdot \frac{T_{epoch}}{P_i} \tag{2.4}$$

where T_{epoch} is the transit epoch and P_i is the period of the planet.

TTVFast also requires inclination, eccentricity, long node and argument. These cannot be simply obtained and need to be assumed. For simplicity the inclination is assumed to be 90° for all planets which results in the long node to be 0. The eccentricity is obtained from a Rayleigh distribution with mode $\sigma = 0,03$ in order to not get eccentricities above 0.1 as that leads to unstable systems. The argument is obtained from a uniform distribution where $0 < \omega < 360$. The code to obtain the input parameters can be seen in appendix A.

How long a system will be observed depends on where in the sky it is located. This time can be obtained from the Web TESS Target tool (https://heasarc.gsfc.nasa.gov/cgi-bin/tess/webtess/wtm.py) if the right ascension, RA, and declination, dec, are known.

This tool accepts csv files with RA and dec of the systems and outputs the number of times TESS will observe that system. This is then used in the simulation of the systems.

2.2 TTVFast

The next step is to use the systems generated in the previous section and simulate them in TTVFast. The parameters from section 1.4 are given to the program to simulate each system. To run TTVFast the parameters are required to be in a specific format and each system requires a setup file mentioned in section 1.4. The bash script creates a new setup file for each system before running the simulation.

2.3 Analyzing results from TTVFast

When all systems have been simulated with TTVFast the bash script executes the next part of the program seen in abstract (REF HERE). The transit times need to be corrected as TTVFast outputs the time of a transit. This is done by fitting a linear fit to the times and subtracting this fit. In order to easier see the amplitude of the TTV signals the times are corrected by subtracting the average time from every value which moves the middle of the graph to $y = 0$. In order to obtain the amplitude of the TTVs the average of the maximum and minimum transit time are calculated. This is used as the amplitude and the corrected transit times are plotted.

In order to observe interesting systems further the position of the systems are required which is obtained from the NASA archive. The positions are given in RA and dec and plotted in a sky map. These coordinates are compensated with Earth's obliquity which is about 23°. These sky maps are colour coded according to the TTV amplitude and the multiplicity, i.e. the number of planets, of the systems.

2.4 WHFast

The artificial systems that are created need to be checked for stability to determine if the assumptions and method of creating them results in realistic stable systems. For this Rebound, more specifically the WHFast integrator (Rein & Tamayo 2015), is used. WHFast is an Wisdom-Holman integrator used for long duration planetary system simulations.

Chapter 3

Results

3.1   Simulated TESS objects

3.2   TTV signals from TESS objects

Table 3.1: Example table from template

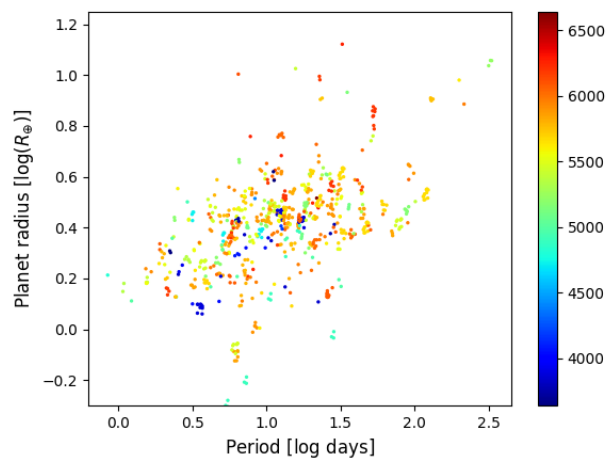| Id of star	I	V	Var.?
1234	15.6	17.3	No
5677	13.4	12.3	Yes

Figure 3.1: Diagram with the radius
distribution as a function of period for the simulated TESS objects.
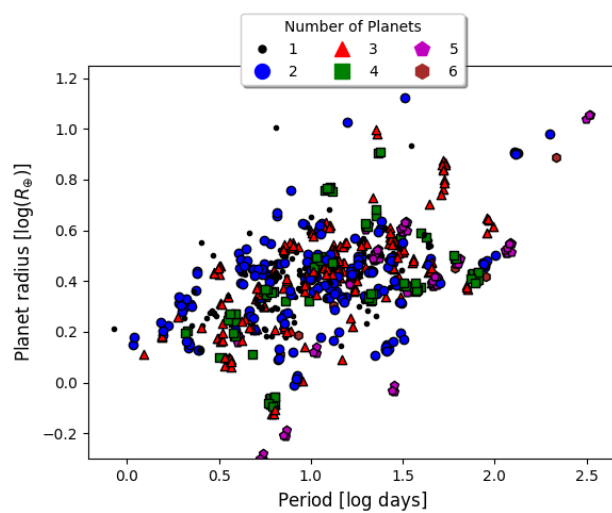

Figure 3.2: Diagram with the radius
distribution as a function of period for the simulated TESS objects where the
colour and shape corresponds to the number of planets in the system.
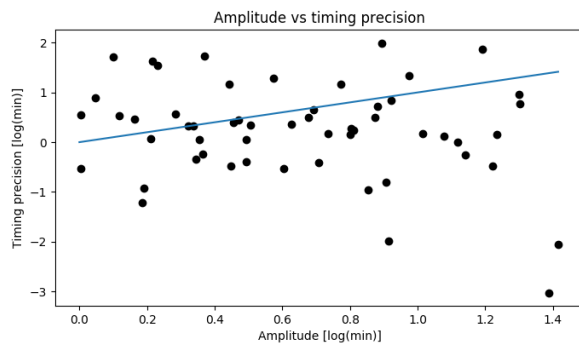
Figure 3.3: Diagram with the position of each observed objects color-coded to show the number of times the object is observed.
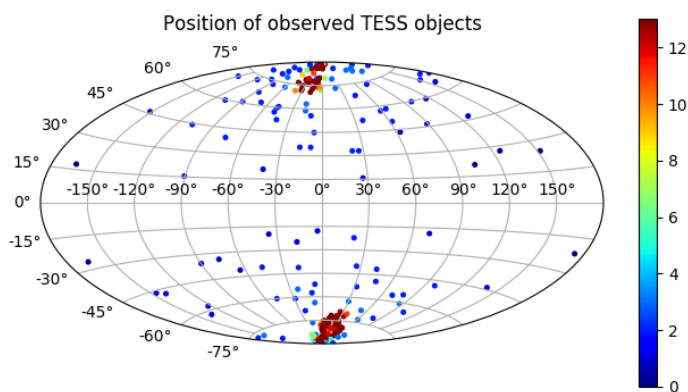

Figure 3.4: Diagram with the position of each observed objects color-coded to show the number of times the object is observed.

Chapter 4

Discussion

Further studies: CHEOPS, James Webb
TTV amplitude: fit instead of average

Chapter 5

Conclusions

Acknowledgements

There is no acknowledgements section in the regular LaTeX, but you can easily make one yourself.

Bibliography

Deck, K. M., Agol, E., Holman, M. J., & Nesvorný, D. 2014, ApJ, 787, 132

Johnson, M. 2018, How many exoplanets has Kepler discovered?

Nesvorný, D., Kipping, D., Terrell, D., et al. 2013, The Astrophysical Journal, 777, 3

Rein, H. & Tamayo, D. 2015, MNRAS, 452, 376

Sullivan, P. W., Winn, J. N., Berta-Thompson, Z. K., et al. 2015, ApJ, 809, 77

Appendix A

This is an appendix

You can put long mathematical derivations or tables in appendices.

Appendix B

This is another appendix