

Statistics : Science of planning studies & experiment, obtaining data, organizing, summarizing, presenting, analyzing, interpreting data & drawing conclusions from there.

Data : collection of observations such as measurements, genders, survey response etc.

Population : elements / individuals / items whose characteristics are being studied

Sample : A portion of population selected for study

Arithmetic mean

$$\mu = \frac{\sum_{i=1}^n x_i}{n}, \quad n = \text{population}$$

Median

• data sorted ascendingly

• value right in the middle.

$$\text{if even } n, \text{ median} = \frac{x_{\frac{n}{2}} + x_{(\frac{n}{2}+1)}}{2}$$

$$\text{if odd } n, \text{ ceil} \left(\frac{n}{2} \right).$$

Mode

• most common occurrence.

Bimodal : 2 values repeat the most 22, 22, 23, 23, 4, 5, 6.

Multi modal : >2 values repeat 22, 22, 22, 25, 25, 25, 26, 26, 26, 1, 7, 5

No mode : No repeat 1, 4, 7, 8

Range

• Highest value - lowest value.

Outlier

• A datapoint that differs significantly from other observations

Causes:

• Variability in measurement

• result of experimental error.

• indication of novel data.

Variance

Dispersion : • Extent in which data values differ from their average.

• How spread out each data is from the mean : $x_i - \bar{x}$

eg: $A = 2, 3, 5, 6.$

$$\bar{x} = \frac{2+3+5+6}{4} = 4$$

• variance is 1 way to measure dispersion

• Range is another way to measure dispersion (only 2 datapoints used, not descriptive of entire data)

$$\text{population variance } \sigma^2 = \frac{\sum_{i=1}^N (x_i - \mu)^2}{N} \quad \text{to convert -ve values to +ve.}$$

$$\text{sample variance } s^2 = \frac{\sum_{i=1}^n (x_i - \bar{x})^2}{n-1}$$

$n-1$ ← empirically found that $n-1$ closer approximation to σ^2

Standard deviation

• Another way to calculate dispersion.

$$\text{population SD } \sigma = \sqrt{\sigma^2}$$

$$\text{sample SD } s = \sqrt{s^2}$$