### Problem 7

A half-wave dipole antenna radiates 10 W at a frequency of 5 GHz. A short dipole antenna situated at a distance of 100 m is used as a receiving antenna. If both antennas are symmetrically placed in the *xy* plane and the medium is free space, (a) determine the effective area of each antenna and (b) the power absorbed by the receiving antenna. (c) If the minimal received power of 1 nW, what is the maximal distance allowed?

Answers: (a)... and  $A_{e\_short\ dipole} = 4.3\ cm^2$ , (b)..., and (c)?49 m.

$$R_0 = 10W$$
  $N = \frac{C}{f} = 0.06$   
 $f = 56$   
 $Y = 100 \text{ m}$ 

(a) 
$$Aer = \frac{\lambda^{2}}{4\pi}D_{V} = \frac{0.0b^{2}}{4\pi} \cdot 1.5 = 4.297 \cdot (\overline{0}^{4} \text{ m}_{\chi}^{2})$$

$$Aet = \frac{\lambda^{2}}{4\pi}D_{t} = \frac{0.0b^{2}}{4\pi} \cdot 1.69 = 4.841 \cdot (\overline{0}^{4} \text{ m}_{\chi}^{2})$$
(b)  $\frac{P_{V}}{P_{t}} = \frac{AetAer}{\lambda^{2}V^{2}} \Rightarrow P_{V} = 5.78 \cdot (\overline{0}^{8})$  (W)

$$\frac{Pr}{Pt} = \frac{AetAer}{\lambda^{2}r^{2}}$$

$$\frac{In}{10} = \frac{4.3\cdot10^{4}\cdot4.8\cdot10^{4}}{0.06^{2}r^{2}}, \quad r = 149 \text{ m}$$

Half -wave:
$$\overrightarrow{A} = \overrightarrow{az} \frac{M \cdot I}{2\pi V} \frac{e^{7\beta V}}{5\pi V^2} \cos \left(\frac{7}{2}\cos 5\theta\right)$$

$$\overrightarrow{H} = \frac{1}{M \cdot 0} \nabla \times \overrightarrow{A} = \overrightarrow{ap} \frac{JI}{2\pi V} \frac{e^{3\beta V}}{2\pi V} \cos \left(\frac{7}{2}\cos 5\theta\right)$$

$$\overrightarrow{Pavg} = \frac{1}{2} \frac{1}{V} + \frac{1}{2} \frac{1}{V} \cos \theta$$

$$= \frac{15I^2}{V^2 \sin^2 \theta \lambda} \cos \left(\frac{7}{2}\cos \theta\right) \approx \frac{15}{2} \frac{I^2}{V^2} \sin^3 \theta$$

$$U(\theta, \phi) = \overrightarrow{Pavg} \cdot V^2 = \frac{15}{2} I^2 \sin^3 \theta$$

$$\Rightarrow U_{\text{Max}} = \frac{15}{2} I^2 \left| \theta = 90 \right|$$

$$\text{Prad} = \int_0^{2\pi} \int_0^{\pi} \frac{15I^2}{\pi V} \sin \theta d\theta d\phi$$

$$= 30 I^2 \cdot \frac{3}{8} \lambda = \frac{45}{4} \lambda I^2$$

$$D = \frac{U_{\text{Max}}}{U_{\text{avg}}} = \frac{U_{\text{Max}}}{V_{\text{Avg}}} = \frac{1.698}{4\lambda} = 7 + \frac{1}{2} \frac{1}{2} \cos \theta$$

Short dipole =
$$\overrightarrow{A} = \overrightarrow{az} \frac{\mu_0 I d\ell}{4\pi v} e^{-i\beta r}$$

$$\overrightarrow{H} = \mu_0 \nabla \times \overrightarrow{A} \approx \overrightarrow{a\phi} \frac{I d\ell}{4\pi} 5\pi n 0 \frac{j\beta}{r} e^{-i\beta r}$$

$$\overrightarrow{Pavg} = \frac{1}{2} \int_{0}^{2\pi} H \phi^{2} \overrightarrow{ar} = \frac{J\beta^{2} I d\ell^{2}}{32\pi^{2} r^{2}} 5\pi n^{2} 0$$

$$U(\theta_{1} \phi) = \overrightarrow{Pavg} \cdot r^{2} = \frac{I5}{4\pi} \beta^{2} I^{2} d\ell^{2} 5\pi n^{2} 0$$

$$Prad = \int_{0}^{2\pi} \int_{0}^{2\pi} U(\theta_{1} \phi) 5\pi n \theta d\theta d\phi$$

$$= \frac{J\pi}{3} I^{2} \left[\frac{d\ell}{2\pi}\right]^{2}$$

$$D = \frac{U_{Max}}{U_{avg}} = \frac{U_{Max}}{V_{avg}} \frac{p_{rad}}{4\pi} = \frac{3}{2} 5\pi n^{2} \theta |_{uax}$$

$$= 1.5 |_{\theta} = 90^{\circ}$$

$$= Dv$$

### Problem 8

The Arecibo Observatory in Puerto Rico has a gigantic dish antenna of diameter of 1000 ft (304.8 m). It transmits power of 2.5 MW at a frequency of 430 MHz. (a) Assuming a 60 percent effective area, what is its gain in dB? (b) What is *its half-power beam width* in degrees? (c) If used as a radar and the minimum detectable received power is –130 dBW, what is its maximum range for detecting a target of radar cross-section of 1 m<sup>2</sup>?

Answers:  $(a)..., (b) 0.1?^{\circ}, and (c)?408 \text{ km}.$ 

$$d = 304.8m = 27. Y = 152.4m$$

$$Pe = 215 M W$$

$$f = 430 MHZ$$
(a)
$$Ae = \pi r^{2}. 0.b = 43779.5$$

$$= \frac{\lambda^{2}}{4\pi}D$$

$$\lambda = \frac{1}{4} = \frac{30}{43}$$
i.  $D = 1.13 \text{ M} = (0, \log(1.13)) \text{ dB}$ 

$$= 60.53 \text{ dB}_{34}$$

(b)  

$$HPBW = \frac{70x}{d}$$
  
 $= 0.16 \text{ m} \approx 0.16 \text{ } \text{\#}$ 

(c) 
$$P_r = -130 dB = 10^{13} W$$
 $O = 1m^2$ 

by Radar transmission eg,

$$\frac{10^{13}}{2.5M} = \frac{\left(\frac{30}{43} \cdot 1.13M\right)^2 \cdot 1}{\left(4\pi\right)^3 \cdot \gamma^4}$$

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$$P_t = 10 \omega$$
  
 $\lambda = \frac{c}{f} = 0.06 \quad (f = 56)$   
 $Y = (00 m)$ 

Answers: (a)... and  $A_{e \text{ short divole}} = 4.3 \text{ cm}^2$ , (b)..., and (c)?49 m.

a. Area effective receiving =  $Aer = \frac{\lambda^2}{4\pi}Dr = \frac{0.06}{4\pi} \cdot 1.5 = \frac{4.3 \times 10^{-4} \text{ m}^2}{4\pi}$ Area effective transmit =  $Aet = \frac{\lambda^2}{4\pi}Dt = \frac{0.06}{4\pi} \cdot 1.64 = \frac{4.7 \times 10^{-4} \text{ m}^2}{4\pi}$ 

$$\Rightarrow Pr = \frac{\text{Aee} \cdot \text{Aer}}{\lambda^{2} \cdot r^{2}} \cdot P_{t} = 5.8 \times 10^{-8} \text{ cw}$$

$$10w.$$

C Prmin = 
$$|nw|$$
 =  $\frac{|r|}{|r|}$  =  $\frac{|nw|}{|r|}$  =  $\frac{|$ 

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#### Problem 8

The Arecibo Observatory in Puerto Rico has a gigantic dish antenna of diameter of 1000 ft (304.8 m). It transmits power of 2.5 MW at a frequency of 430 MHz. (a) Assuming a 60 percent effective area, what is its gain in dB? (b) What is its half-power beam width in degrees? (c) If used as a radar and the minimum detectable received power is -130 dBW, what is its maximum range for detecting a target of radar cross-section of 1 m2?

d = 304.8m

Y = 152,4 m

f = 430 M Hz

Pt = 25 MW

Answers: (a)..., (b) 0.1?°, and (c)?408 km.

Answers: (a)..., (b)0.17°, and (c)?408 km.

a. 
$$Ae = Y^{*} \cdot \nabla \cdot 0.6 = 43779.5 = \frac{Q^{*}}{4\pi}D$$
 in  $D = 1122.753.9 = 1.1 M = 60.5 dB$ 

b. HPBW = 
$$\frac{20\lambda}{d} = 20.4 = 0.1607°$$

$$\frac{Pr}{Pt} = \frac{(\times P)^{3} \circ r^{2}}{(4\pi)^{3} \cdot r^{2}} \Rightarrow \frac{10^{-13}}{2.5 \times 10^{6}} = \frac{(0.7 \cdot (.1M)^{2} \cdot 1)^{3}}{(4\pi)^{3} \cdot r^{4}}$$