

cse13s asgn5 DESIGN.pdf

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1 Program Details

We will create three functions: one that creates a public and private key pair using large prime numbers, one that encrypts a file using a public key, and one that decrypts the file using the private key. We will use a randomizer to generate the large primes for the keys.

2 functions and pseudocode

1. randstateinit(seed)
 - (a) allocate memory for "state"
 - (b) set srandom to seed
 - (c) use "state" as a global variable to keep track of random state
2. randstateclear()
 - (a) clear memory of state and free memory
3. powmod(out, base, exponent, mod)
 - (a) temp = 1
 - (b) temp2 = base
 - (c) while exponent \neq 0
 - i. if exponent is odd
 - A. temp = (temp x temp2) mod(mod)
 - ii. temp2 = (temp2 x temp2) mod(mod)
 - iii. exponent = exponent floor division by 2
 - (d) out = temp

4. isprime(n, iters)
 - (a) $r = (n-1) / 2^s$. r should be odd
 - (b) for loop from 1 - iters
 - i. $a = \text{random number from } (2, n-2)$
 - ii. $y = \text{powmod}(a, r, n)$
 - iii. if y is not 1 or $n-1$
 - A. $j = 1$
 - B. while j less than or equals $s-1$ and y not equals $n-1$
 - C. if $y == 1$ return
 - D. $j = j + 1$
 - E. if y not equals $n-1$. Return false
 - (c) return true
5. makeprime(p, bits, iters)
 - (a) generates prime number and stores in p
 - (b) set number of bits of p to bits
 - (c) test using isprime(p , iters)
6. gcd(d, a, b)
 - (a) while b is not 0
 - i. $t = b$
 - ii. $b = a \bmod b$
 - iii. $a = t$
 - (b) return a
7. modinverse(i, a, n)
 - (a) $r = n$
 - (b) $rp = a$
 - (c) $t = 0$
 - (d) $tp = 1$

- (e) while rp not equal to 0
 - i. $q = r/rp$
 - ii. $r = rp$
 - iii. $rp = r - q \times rp$
 - iv. $t = tp$
 - v. $tp = t - q \times tp$
 - (f) if r greater than 1: return no inverse
 - (g) if t less than 0: $t = t + n$
 - (h) return t
8. `rsamakepub(p, q, n, e, nbits, iters)`
- (a) p, q = prime numbers, n = product of p and q , e = exponent
 - (b) `makeprime()` to make p and q
 - (c) $\log_2(n)$ should be greater than $nbits$
 - (d) p bits in range $(nbits/4, (3 \times nbits) / 4)$
 - (e) q gets remaining bits from the calculation
 - (f) random number using `random()` and `iters` to check prime
 - (g) $\lambda(n) = \text{lcm}(p-1, q-1)$
 - i. do this by calculating $\text{gcd}(p-1, q-1)$ and comparing it to the product of $p-1$ and $q-1$
 - (h) get random numbers around $nbits$
 - (i) get the gcd of each random number to find $\lambda(n)$
 - (j) coprime number $\lambda(n)$ = public exponent
9. `rsawritepub(n,e,s, char username, file *pbfile)`
- (a) open `pbfile` for writing (if not already open)
 - (b) print n in hex with a newline

- (c) print e in hex with a newline
 - (d) print s in hex with a newline
 - (e) print username with newline
 - (f) close pbfile
10. rsareadpub(n,e,s, char username, file *pbfile)
- (a) open pbfile for reading(if not already open)
 - (b) scan each line to read then into variables
 - (c) scan first line = n
 - (d) scan second line = e
 - (e) scan third line = s
 - (f) scan fourth line = username
 - (g) close pbfile
11. rsamakepriv(d,e,p,q)
- (a) d = private key to be created, e = public exponent, p and q = primes
 - (b) d = inverse of e mod $\lambda(n)$
12. rsawritepriv(n,d,file *pvfile)
- (a) open pvfile for writing (if not already open)
 - (b) write n as a hexstring followed by newline
 - (c) write d as a hexstring followed by newline
 - (d) close pvfile
13. rsareadpriv(n,d, file *pvfile)
- (a) open pvfile for reading(if not already open)

- (b) scan lines to assign values to variables
 - (c) $n = \text{scan first line}$
 - (d) $d = \text{scan second line}$
14. `rsa_encrypt(c,m,e,n)`
- (a) $c = m^e \pmod{n}$
15. `rsa_encrypt_file(file *infile, file *outfile, n, e)`
- (a) encrypt in blocks from infile to outfile
 - (b) block values cannot be 0 or 1
 - (c) create block size $k = \lfloor (\log_2(n) - 1/8) \rfloor$
 - (d) malloc to allocate array that can hold k bytes as a uint8
 - (e) set array at 0 to 0xFF
 - (f) while unprocessed bytes in infile
 - i. read k - 1 bytes from infile and place them into the allocated block array starting from 1
 - ii. convert the read bytes including array(0) into mpzt m.
 - iii. encrypt m using `rsa_encrypt()` and write it to outfile as a hexstring with a newline.
16. `rsa_decrypt(m, c, d, n)`
- (a) compute message m
 - (b) $m = c^d \pmod{n}$
17. `rsa_decrypt_file(file infile, file outfile, n, d)`
- (a) allocate memory for block size similar to encrypt file
 - (b) while unprocessed bytes in infile
 - i. scan hexstring, save hexstring in variable.

- ii. convert each hexstring back into bytes using `mpxexport()` `j`
= number of bytes converted
 - iii. write out `j-1` bytes starting from `array(1)` to outfile
- 18. `rsa sign(s,m,d,n)`
 - (a) $s = m^d \pmod{n}$
- 19. `rsa verify(m,s,e,n)`
 - (a) `var t = se mod n`
 - (b) if `t = m`: return true
 - (c) else: return false

3 main files and command line inputs

Key Generator

- (a) `-b` = minimum bits for `mod(n)`
- (b) `-i` = number of iterations to test prime numbers. Default 50
- (c) `-n pbfile` = specifies file that has public key. Default `rsa.pub`
- (d) `-d pvfile` = specifies file that has private key. Default `rsa.priv`
- (e) `-s` = specifies random seed for random state. Default `time(NULL)`
- (f) `-v` = verbose output
- (g) `-h` = synopsis and usage
- (h) set file permissions to 0600 using `fchmod` and `fileno`
- (i) `randstate init(s)`
- (j) make public and private keys
- (k) `getenv()` to get username as string
- (l) convert username using `mpz set str()` with a base of 62

- (m) write public key to pbfile and private key to pvfile
- (n) if verbose output:
 - i. print username with newline
 - ii. print signature s with newline
 - iii. print prime p with newline
 - iv. print prime q with newline
 - v. print mod(n) with newline
 - vi. print exponent e with newline
 - vii. print private key d with newline
 - viii. each of these lines should have number of bits for each and the decimal value that corresponds to them
 - ix. randstate clear() and close/clear all files and variables

Encrypt

- i. -i = input file to encrypt. Default = stdin
- ii. -o = output file to encrypt to. Default = stdout
- iii. -n = file containing public key. Default = rsa.pub
- iv. -v = verbose output
- v. -h = synopsis and usage
- vi. open file and exit program if there is a problem opening the file
- vii. read public key from pbfile
- viii. if verbose:
 - A. print username with newline
 - B. print signature s with newline
 - C. print mod(n) with a newline
 - D. print exponent e with a newline
 - E. print each with their number of bits and their values as a decimal
- ix. convert username to mpzt and verify it using rsa verify()
- x. encrypt file using rsa encrypt file()
- xi. close pbfile and clear mpz variables

Decrypt

- i. -i = input file to decrypt. Default = stdin
- ii. -o = output file to decrypt to. Default = stdout
- iii. -n = specifies file containing private key. Default = rsa.priv
- iv. -v = verbose output
- v. -h = synopsis and usage
- vi. open private key file. Print error if failed
- vii. read private key from pvfile
- viii. if verbose:
 - A. print $\text{mod}(n)$ with newline
 - B. print private key e with newline
 - C. both should print number of bits and their values in decimal
- ix. decrypt file using `rsa decrypt file()`
- x. close pvfile and clear mpz variables