

cse13s asgn5 DESIGN.pdf

Lucas Lee; CruzID: luclee

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1 Program Details

We will create three functions: one that creates a public and private key pair using large prime numbers, one that encrypts a file using a public key, and one that decrypts the file using the private key. We will use a randomizer to generate the large primes for the keys.

2 functions and pseudocode

for each function that needs random states, declare global variable state.

1. randstateinit(seed)
 - (a) set Mersenne Twister initializer to state
 - (b) set srandom to seed
 - (c) set randseed with variable state to random seed
2. randstateclear()
 - (a) clear memory of state
3. powmod(out, base, exponent, mod)
 - (a) create mpz temp variables to store parameters so they do not change
 - (b) $v = 1$
 - (c) $p = \text{base}$
 - (d) tempexpo
 - (e) while tempexpo $\neq 0$

- i. if tempexpo is odd
 - A. $v = (v \times p) \bmod(\text{mod})$
 - ii. $p = (p \times p) \bmod(\text{mod})$
 - iii. tempexpo = tempexpo floor division by 2
 - (f) out = v
 - (g) clear mpz variables
- 4. isprime(n, iters)
 - (a) return true if n is less than 4
 - (b) return false if n is even
 - (c) $r = (n-1) / 2^s$. r should be odd
 - i. create mpz values s, r, temp to hold values in the above equation
 - ii. $s = 0, r = 1, \text{temp} = n-1$
 - iii. while temp is not 1
 - A. floor divide temp by 2
 - B. $s += 1$
 - C. if temp is odd
 - D. $r = \text{temp}$
 - E. break loop
 - (d) for loop from 1 - iters
 - i. create mpz variables to store temporary values for calculations
 - ii. a = random number from (2, n-2)
 - iii. $y = \text{powmod}(a, r, n)$
 - iv. if y is not 1 or n-1
 - A. $j = 1$
 - B. while j less than or equals s-1 and y not equals n -1
 - C. if $y == 1$, clear mpz vars and return
 - D. $j = j + 1$
 - E. if y not equals n - 1. clearn mpz vars and return false
 - (e) clear all mpz vars used in function
 - (f) return true

5. makeprime(p, bits, iters)

- (a) create mpz variables to store temporary values. bitcount, prime, randombits
- (b) bitcount = bits
- (c) bitcount = 2^{bits}
- (d) set p = bitcount
- (e) set randombits = bits -1
- (f) set prime to a random number from $2^b + 2^b - 1$ if b = bits
- (g) test using isprime(p, iters)
 - i. keep randomizing prime to a number in the same range to test for each iteration iters
- (h) clear mpz variables and p should be set to the prime number

6. gcd(d, a, b)

- (a) make temp variables so d, a, and b are not altered by function
- (b) while tempb is not 0
 - i. t = tempb
 - ii. tempb = tempa mod tempb
 - iii. tempa = t
- (c) d = tempa
- (d) clear mpz vars

7. modinverse(i, a, n)

- (a) make temp mpz variables to store
- (b) r = n
- (c) rp = a

- (d) $t = 0$
- (e) $tp = 1$
- (f) while rp not equal to 0
 - i. $q = r/rp$
 - ii. $r = rp$
 - iii. $rp = r - q \times rp$
 - iv. $t = tp$
 - v. $tp = t - q \times tp$
- (g) if r greater than 1: $i = 0$
- (h) if t less than 0: $t = t + n$
- (i) $i = t$
- (j) return i

8. `rsamakepub(p, q, n, e, nbits, iters)`

- (a) p, q = prime numbers, n = product of p and q , e = exponent
- (b) `makeprime()` to make p and q
- (c) $\log_2(n)$ should be greater than $nbits$
- (d) p bits in range $(nbits/4, (3 \times nbits) / 4)$
- (e) q gets remaining bits from the calculation
- (f) random number using `random()` and `iters` to check prime
- (g) $\lambda(n) = \text{lcm}(p-1, q-1)$
 - i. do this by calculating $\text{gcd}(p-1, q-1)$ and comparing it to the product of $p-1$ and $q-1$
 - ii. $\text{lcm}(p-1, q-1) = \text{absolute value}(p-1 * q-1) / \text{gcd}(p-1, q-1)$
- (h) get random numbers around $nbits$

- (i) get the gcd of each random number to find $\lambda(n)$
 - (j) while $\gcd(e, \lambda(n))$ is not 1 (not coprime)
 - i. randomize e from 0 - nbits
 - (k) coprime number $\lambda(n) = \text{public exponent } e$
 - (l) clear mpz variables
9. `rsawritepub(n,e,s, char username, file *pbfile)`
- (a) open pbfile for writing (if not already open)
 - (b) print n in hex with a newline
 - (c) print e in hex with a newline
 - (d) print s in hex with a newline
 - (e) print username with newline
 - (f) close pbfile
10. `rsareadpub(n,e,s, char username, file *pbfile)`
- (a) open pbfile for reading(if not already open)
 - (b) scan each line to read then into variables
 - (c) scan first line = n
 - (d) scan second line = e
 - (e) scan third line = s
 - (f) scan fourth line = username
 - (g) close pbfile
11. `rsamakepriv(d,e,p,q)`
- (a) d = private key to be created, e = public exponent, p and q = primes

- (b) $d = \text{modinverse}(e, \text{lcm})$
12. `rsawritepriv(n,d,file *pvfile)`
- (a) open pvfile for writing (if not already open)
 - (b) write n as a hexstring followed by newline
 - (c) write d as a hexstring followed by newline
 - (d) close pvfile
13. `rsareadpriv(n,d, file *pvfile)`
- (a) open pvfile for reading(if not already open)
 - (b) scan lines to assign values to variables
 - (c) n = scan first line
 - (d) d = scan second line
14. `rsa_encrypt(c,m,e,n)`
- (a) use powermod to compute c
 - (b) $c = m^e \pmod{n}$
15. `rsa_encrypt file(file *infile, file *outfile, n, e)`
- (a) encrypt in blocks from infile to outfile
 - (b) create block size $k = \lfloor (\log_2(n) - 1/8) \rfloor$
 - (c) malloc to allocate array that can hold k bytes as a uint8
 - (d) set array at 0 to 0xFF
 - (e) while unprocessed bytes in infile (using fread - bytes may not be numbers, so scan wont work)
 - i. read k - 1 bytes from infile and place them into the allocated block array starting from 1 (fread)

- ii. convert the read bytes including array(0) into mpz_t m (use mpz_import for this)
 - iii. encrypt m using rsa_encrypt() and write it to outfile as a hexstring with a newline.
- (f) close files (unless closed in functions) and free array
- 16. rsa_decrypt(m, c, d, n)
 - (a) compute message m using powermod
 - (b) $m = c^d \pmod{m}$
- 17. rsa_decrypt_file(file_infile, file_outfile, n, d)
 - (a) allocate memory for block size similar to encrypt file
 - (b) while unprocessed bytes in infile (use feof() to indicate when the end of the file is reached)
 - i. scan hexstring, save hexstring in variable.
 - ii. convert each hexstring back into bytes using mpz_export()
 - j = number of bytes read
 - iii. write out j-1 bytes starting from array(1) to outfile
 - (c) print newline to outfile for syntax
 - (d) free array and close files (unless closed in functions)
- 18. rsa_sign(s, m, d, n)
 - (a) calculate s by using power mod
 - (b) $s = m^d \pmod{n}$
- 19. rsa_verify(m, s, e, n)
 - (a) calculate t by using power mod
 - (b) var t = $s^e \pmod{n}$
 - (c) if t = m: return true
 - (d) else: return false

3 main files and command line inputs

Key Generator

- (a) -b = minimum bits for mod(n)
- (b) -i = number of iterations to test prime numbers. Default 50
- (c) -n pbfile = specifies file that has public key. Default rsa.pub
- (d) -d pvfile = specifies file that has private key. Default rsa.priv
- (e) -s = specifies random seed for random state. Default time(NULL)
- (f) -v = verbose output
- (g) -h = synopsis and usage
- (h) set file permissions to 0600 using fchmod and fileno
- (i) fileno returns int, so store it in a variable and use it for fchmod
- (j) fchmod(fileno integer, 0600 permissions)
- (k) randstate init(s)
- (l) make public and private keys
- (m) getenv(USER) to get username as string
- (n) convert username using mpz set str() with a base of 62
- (o) write public key to pbfile and private key to pvfile
- (p) if verbose output:
 - i. sizeinbase(mpz, base2) to get bit numbers
 - ii. print username with newline
 - iii. print signature s with newline
 - iv. print prime p with newline
 - v. print prime q with newline
 - vi. print mod(n) with newline

- vii. print exponent e with newline
- viii. print private key d with newline
- ix. each of these lines should have number of bits for each and the decimal value that corresponds to them
- x. randstate clear() and close/clear all files and variables

Encrypt

- i. -i = input file to encrypt. Default = stdin
- ii. -o = output file to encrypt to. Default = stdout
- iii. -n = file containing public key. Default = rsa.pub
- iv. -v = verbose output
- v. -h = synopsis and usage
- vi. open file and exit program if there is a problem opening the file
- vii. read public key from pbfile
- viii. if verbose:
 - A. print username with newline
 - B. print signature s with newline
 - C. print mod(n) with a newline
 - D. print exponent e with a newline
 - E. print each with their number of bits and their values as a decimal
- ix. convert username to mpz using set_str() and verify it using rsa_verify()
- x. encrypt file using rsa_encrypt_file()
- xi. close pbfile and clear mpz variables

Decrypt

- i. -i = input file to decrypt. Default = stdin
- ii. -o = output file to decrypt to. Default = stdout
- iii. -n = specifies file containing private key. Default = rsa.priv
- iv. -v = verbose output
- v. -h = synopsis and usage
- vi. open private key file. Print error if failed
- vii. read private key from pvfile
- viii. if verbose:
 - A. print $\text{mod}(n)$ with newline
 - B. print private key e with newline
 - C. both should print number of bits and their values in decimal
- ix. decrypt file using `rsa_decrypt file()`
- x. close pvfile and clear mpz variables