

BruteForce method:

```
vector<double> BruteForce(vector<pair<double,double> > vec, int size, int& count)
{
    double min = FLT_MAX;
    vector<double> v(5);
    for(int i=0; i<size; i++){
        for(int j=i+1; j<size; j++){
            count ++;
            if(dist(vec[i], vec[j]) < min){
                min = dist(vec[i], vec[j]);
                v[0] = (dist(vec[i], vec[j]));
                v[1] = (vec[i].first);
                v[2] = (vec[i].second);
                v[3] = (vec[j].first);
                v[4] = (vec[j].second);
            }
        }
    }
    return v;
}
```

Time complexity is $O(n^2)$ because there are two for loops, which is $n*n$.

Plot: Compare point by point, record it as the shortest distance, min. If there is a d shorter than min, min = d. At the end of the comparison, min will be the shortest distance.

Divide and conquer method

```
vector<double> findmin(vector<pair<double,double> > v, int n, int& count)
{
    if (n <= 3)
    {
        return bruteForce(v, n, count);
    }
    int mid = n/2;
    pair<double,double> midPoint = v[mid];

    vector<pair<double,double> > v1(v.begin(), v.begin() + mid);
    vector<double> left = findmin(v1, mid, count);
    vector<pair<double,double> > v2(v.begin() + mid, v.end());
    vector<double> right = findmin(v2, n-mid, count);
    vector<double> d = min(left, right);
    double dis = d[0];
}
```

```

count++;

vector<pair<double,double> > strip;//holds points in strip
for (int i=0; i<n; i++){
    if (abs(v[i].first - midPoint.first) < dis){
        strip.push_back(v[i]);
    }
}
sort(strip.begin(), strip.end(), myComparison);//strip sorted
count = count + strip.size();
return min(d, stripClosest(strip, strip.size(), dis, count));
}

```

Time complexity of divide and conquer is $O(n(\log n)^2)$. The reason why there is a $(\log n)^2$ is because I use merge sort algorithm to sort y coordinate instead of directly merge(which takes $O(n)$)

Plot: Divide all the points into half and keep doing so until groups have points less or equal than 3. Then use brute force find min distance d in each group. For each adjacent group, collect points which have distance $< d$ (d is the min of two adjacent group) into a vector(strip). Then sort all the points in terms of y coordinate. Then compute shortest distance in this strip. If it is smaller than d , then make it min. Recursively doing so, we will get the shortest distance.