

MTH 317.3 Numerical Methods (3-1-3)

	Theory	Practical	Total
Sessional	30	20	50
Final	50	-	50
Total	80	20	100

Course Objectives:

To be familiar with the theory of numerical analysis for solving algebraic and transcendental equations, solution of ordinary and partial differential equations related to engineering problems, numerical differentiation and integration.

Course Contents:

1. Solution of Nonlinear Equations (10 hrs)

Review of calculus and Taylor's theorem, Errors in numerical calculations. Trial and error method, Bisection method, Newton's method, secant method and their convergence, Fixed point iteration and its convergence.

2. Interpolation and Approximation (8 hrs)

Lagrang's polynomials, Newton's interpolation using difference and divided differences. Cubic spline interpolation, Least squares method for linear and nonlinear data.

3. Numerical Differentiation and Integration (5 hrs)

Newton's differentiation formulas, Maxima and minima of tabulated function, Newton-Cote's quadrature formulas, Gaussian integration algorithm, Romberg integration formulas.

4. Solution of Linear Algebraic Equations (10 hrs)

Review of the existence of solutions and properties of matrices, Gaussian elimination method, pivoting, ill-conditioning, Gauss-Jordan method, Inverse of matrix using Gauss elimination method, Method of factorization, Dolittle algorithm, Cholesky's factorization, Iterative solutions, Solving eigen value problems using power method.

5. Solution of Ordinary Differential Equations (7 hrs)

Review of differential equations, Initial value problem, Taylor series method, Picard's method, Euler's method and its accuracy, Heun's method, Runge-Kutta methods, Solution of the higher order equations, Boundary value problems: Shooting method and its algorithm.

6. Solution of Partial Differential Equations (5 hrs)

Review of partial differential equations, Deriving difference equations, Laplacian equation and Poisson's equation, Engineering examples.

Laboratory :

The laboratory experiments will consist of program development and testing of non-linear equations, interpolation, numerical integration and differentiation, linear algebraic equations, ordinary and partial differential equations.

Text Book :

1. C.F. Gerald and P.O. Wheatley, *Applied Numerical Analysis*, 5th Edition, Addison Wesley, ISBN: 0201435837.
2. Mathews, John H., *Numerical Mathematics for Mathematics, Science and Engineering*, Second Edition, PHI, ISBN: 81-203-0845-X.

Reference Books:

1. W. Cheney and D. Kincaid, *Numerical Mathematics and Computing*, 2nd Edition, Brooks/Cole Publishing Co., 1985.
2. W.H. Press, B.P. Flannery et.al., *Numerical Recipes in C*, 1st Edition, Cambridge Press, 1988.
3. S. Yakwitz and F. Szidarovszky, *An Introduction to Numerical Computations*, 2nd Edition, Macmillan Publishing Co., New York.