

# Classification

## Logistic regression

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**3** Evaluation metrics

**CLASSIFICATION**

## CLASSIFICATION

- Classification problems have an **independent categorical variable**  $Y$ .
- They are processes that consist on identifying to which category or class belongs a determined object, according to their dependent variables.
- Examples:
  - Fraud detection
  - Definition of a target in a marketing campaign
  - Medical diagnosis
  - Image classification

# CLASSIFICATION

## STEPS

### 1. Training:

We build a classifier (model) learning from a labeled train set.

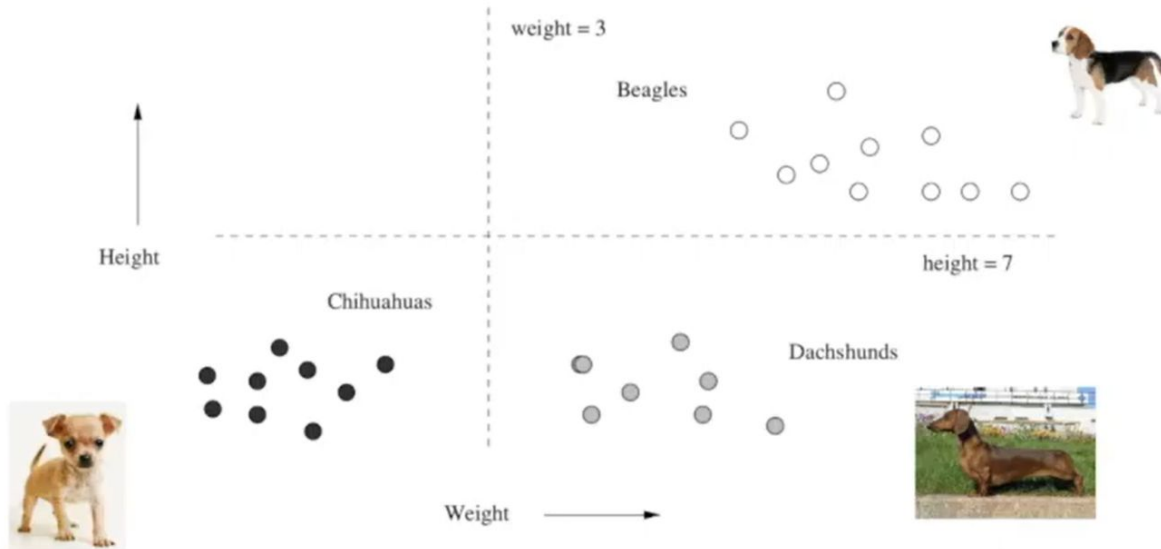
### 2. Classification:

We use the model to classify.

### 3. Evaluation:

We evaluate the model. This step can be included in the previous one.

# CLASSIFICATION



REGLA

```
if height > 7:  
    print('Beagle')  
elif weight < 3:  
    print('Chihuahua')  
else:  
    print('Dachshund')
```

## CLASSIFICATION

**Life is not so easy: we cannot always develop clear rules** 😞

To solve this kind of problem, we have machine learning models that **predict the probability of a given observation to belong to a particular class:**

- Bayesian models
- Logistic regression
- Decision Trees - Random forests
- Neural networks
- And more!!

## CLASSIFICATION

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# LOGISTIC REGRESSION

## LOGISTIC REGRESSION

- Logistic Regression is a classification model, which is very easy to realize and achieves very good performance with linearly separable classes.

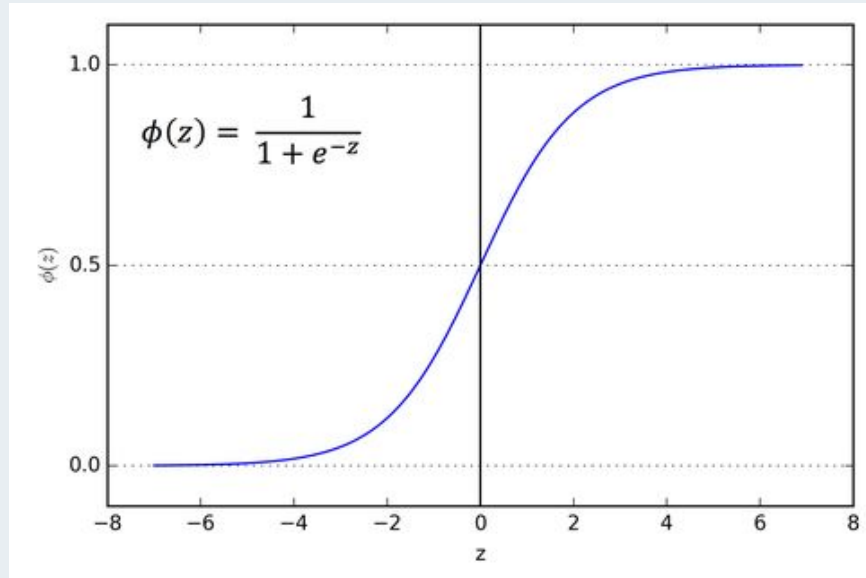
- Assumption about  $y$ :

$$y \sim \text{binomial}(1, p) \Rightarrow y \begin{cases} 1 & p \\ 0 & 1-p \end{cases}$$

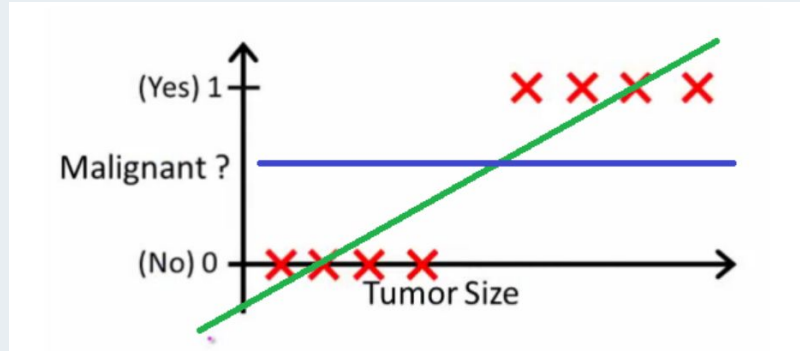
- The predictor variables must be linearly independent.
- It is necessary to standardize the variables.
- It is a very sensitive model to atypical values or outliers .
- Logistic regression can be generalized to problems of more than two classes.

## LOGISTIC REGRESSION

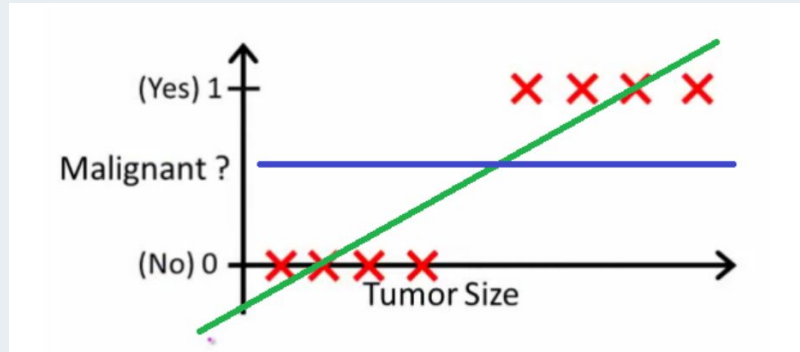
- It uses a logistic function



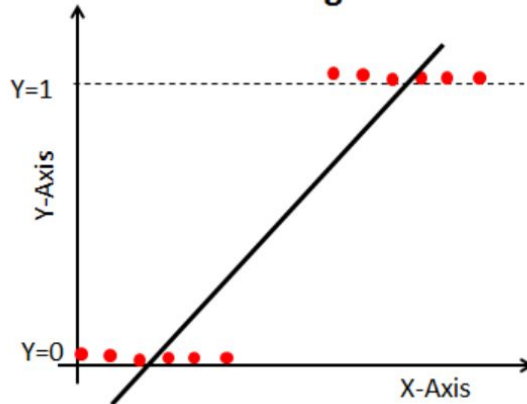
## LOGISTIC REGRESSION



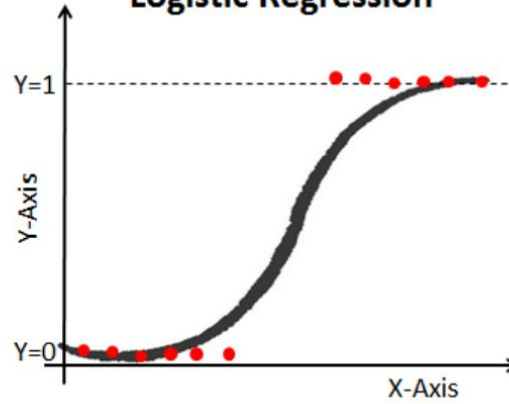
# LOGISTIC REGRESSION



Linear Regression



Logistic Regression



## LOGISTIC REGRESSION

$$\hat{y}^{(i)} = \beta_0 + \beta_1 x_1^{(i)} + \dots + \beta_p x_p^{(i)}$$



$$\phi(z) = \frac{1}{1 + e^{-z}} = \frac{1}{1 + \exp(-(\beta_0 + \beta_1 x_1^{(i)} + \dots + \beta_p x_p^{(i)}))}$$

# **EVALUATION METRICS**

## EVALUATION METRICS

# CONFUSION MATRIX

There are 4 possible values:

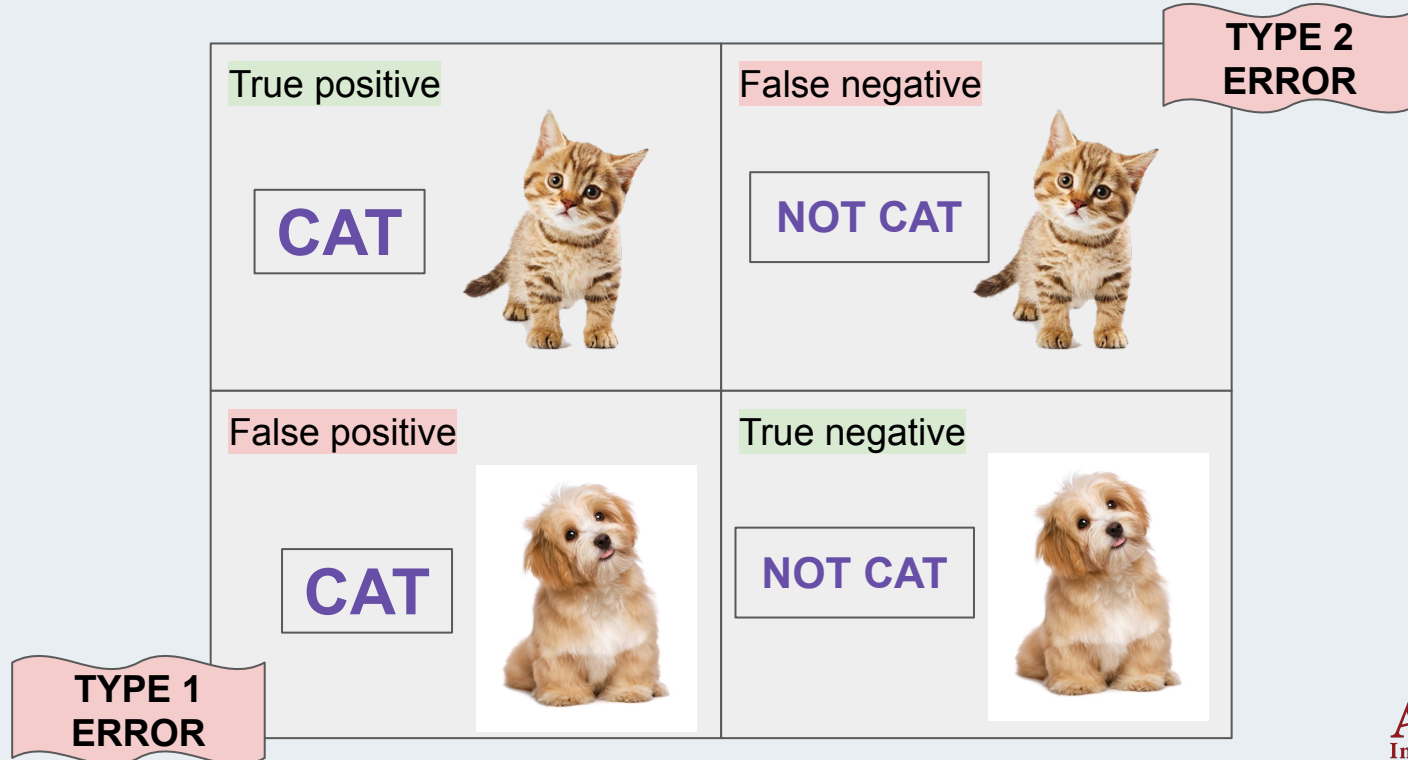
- True Positives (TP)
- True Negatives (TN)
- False Positives (FP)
- False Negatives (FN)

Actual	Positive	Negative
	TP	FN
Negative	FP	TN
	Positive	Negative
	Predicted	



## EVALUATION METRICS

# CONFUSION MATRIX



## EVALUATION METRICS

# METRICS

- **Accuracy** : Percentage of cases in which our model was correct
- **Precision** : Percentage of values that have been classified as positive are actually positive
- **Recall** : Percentage of positive values that are identified
- **F1 Score** : Combines accuracy and comprehensiveness

$$accuracy = \frac{TP + TN}{TP + TN + FP + FN}$$

$$precision = \frac{TP}{TP + FP}$$

$$recall = \frac{TP}{TP + FN}$$

$$F1 = 2 \cdot \frac{precision \cdot recall}{precision + recall}$$

## EVALUATION METRICS

# ROC CURVE

- Represents the percentage of **true positives** (TPR or Recall) **against the false positives** ratio (FPR).
- Its values range from 0 to 1.

