

# Package ‘CollessLike’

March 28, 2018

**Type** Package

**Title** Distribution and Percentile of Sackin, Cophenetic and  
Colless-Like Balance Indices of Phylogenetic Trees

**Version** 1.0

**Date** 2018-03-28

**Author** Arnau Mir, Francesc Rossello, Lucia Rotger

**Maintainer** Lucia Rotger <lucia.rotger@uib.es>

**Description** Computation of Colless-Like, Sackin and cophenetic balance indices of a phylogenetic tree and study of the distribution of these balance indices under the alpha-gamma model. For more details see A. Mir, F. Rossello, L. Rotger (2013) <doi:https://doi.org/10.1016/j.mbs.2012.10.005>, M. J. Sackin (1972) <doi:https://doi.org/10.1093/sysbio/21.1.15>, less (1982) <doi:10.2307/2413420>.

**License** GPL (>= 2)

**URL** <https://github.com/LuciaRotger/CollessLike>

**LazyData** true

**Depends** R (>= 3.3.0)

**Imports** ape, igraph

**RoxygenNote** 6.0.1

**Encoding** UTF-8

**NeedsCompilation** no

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CollessLike-package	<i>Distribution and Percentile of Sackin, Cophenetic and Colless-Like Balance Indices of Phylogenetic Trees</i>
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## Description

Computation of Colless-Like, Sackin and cophenetic balance indices of a phylogenetic tree and study of the distribution of these balance indices under the alpha-gamma model. For more details see A. Mir, F. Rossello, L. Rotger (2013) <doi:<https://doi.org/10.1016/j.mbs.2012.10.005>>, M. J. Sackin (1972) <doi:<https://doi.org/10.1093/sysbio/21.2.225>>, D. H. Colless (1982) <doi:[10.2307/2413420](https://doi.org/10.2307/2413420)>.

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## phylogenetic tree

**Author(s)**

Arnau Mir, Francesc Rossello, Lucia Rotger  
 Maintainer: Lucia Rotger <lucia.rotger@uib.es>

**References**

B. Chen, D. Ford, M. Winkel, A new family of Markov branching trees: the alpha-gamma model. *Electr. J. Probab.* **14** (2009), 400-430.  
 A. Mir, F. Rossello, L. Rotger, A Colless-like balance index for multifurcating phylogenetic trees.  
 A. Mir, F. Rossello, L. Rotger, A new balance index for phylogenetic trees. *Mathematical Biosciences* **241** (2013), 125-136.  
 M. J. Sackin, "Good" and "bad" phenograms. *Sys. Zool.* **21** (1972), 225-226.

**Examples**

```
# A random phylogenetic tree of 5 leaves between all trees with 5 leaves
# following the alpha-gamma model with alpha=0.5 and gamma=0.3
a.g.tree = a.g.model(5,0.5,0.3)
# To compute the percentile of that tree of the Colless-Like,
# Sackin and cophenetic normalized balance indices under the alpha-gamma
# model with alpha=0.5 and gamma=0.3, and a distribution plot.
#distribution(a.g.tree,0.5,0.3,db.path=getwd())
# For a percentile plot set the parameter percentile.plot as TRUE
#distribution(a.g.tree,0.5,0.3,db.path=getwd(),percentile.plot=TRUE)

# Computation of the Colless-Like, Sackin and cophenetic balance indices
# of a sample of 50 trees that follow the alpha-gamma distribution
# with alpha=0.5 and gamma=0.3 with 5 leaves.
indices.data = indices.simulation(5,0.5,0.3,50)
# Computation of the percentile of the random tree using the previous
# generated sample
distribution(a.g.tree,0.5,0.3,set.indices=indices.data)
```

a.g.model

*Generates a random tree***Description**

Given alpha, gamma and the number of leaves n, generates a random phylogenetic tree between all trees with n leaves following the alpha-gamma model.

**Usage**

```
a.g.model(n, alpha, gamma)
```

**Arguments**

n	the number of leaves in the tree.
alpha	parameter of the alpha-gamma model, between 0 and 1.
gamma	parameter of the alpha-gamma model, between 0 and alpha.

**Value**

An igraph object that represents the generated phylogenetic tree.

**Author(s)**

Lucia Rotger

**References**

B. Chen, D. Ford, M. Winkel, A new family of Markov branching trees: the alpha-gamma model. *Electr. J. Probab.* **14** (2009), 400-430.

**Examples**

```
# A phylogenetic tree with 10 leaves and parameters alpha=0.8 and gamma=0.1
tree = a.g.model(10,0.8,0.1)
plot(tree,layout=layout.reingold.tilford(tree,root=which(degree(tree,mode="in")==0)))
```

---

balance.indices	<i>Computes Colles-like, Sackin and cophenetic balance indices of a phylogenetic tree.</i>
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**Description**

Given a phylogenetic tree, computes Colles-like, Sackin and cophenetic balance indices of that tree.

**Usage**

```
balance.indices(tree, norm = FALSE)
```

**Arguments**

tree	a single phylogenetic tree. It can be entered as a string in Newick format, as a 'phylo' object (ape package) or as an 'igraph' object (igraph package).
norm	a logical variable that indicates whether the indices should be normalized or not.

**Details**

The Colless-like index is the generalization of the Colless' index for non-binary trees (see Mir et al. , 2017).

The Sackin's index is computed as the sum of the number of ancestors for each leaf of the tree (see Mir et al. , 2013).

The cophenetic index is computed as the sum of the depths of the least common ancestor (LCA) of every pair of leaves of the tree(see Sackin et al, 1972).

**Value**

A numeric vector with the three computed balance indices of the tree: Colless-like, Sackin and Cophenetic values.

**Author(s)**

Lucia Rotger

**References**

- A. Mir, F. Rossello, L.Rotger, A Colless-like balance index for multifurcating phylogenetic trees.  
 A. Mir, F. Rossello, L.Rotger, A new balance index for phylogenetic trees. *Mathematical Biosciences* **241** (2013), 125-136.  
 M. J. Sackin, "Good" and "bad" phenograms. *Sys. Zool.*, **21** (1972), 225-226.

**Examples**

```
# Computation of the Colless-Like, Sackin and Cophenetic
# balance indices of trees entered in newick format:
balance.indices("(1,2,3,4,5);")
balance.indices("(1,(2,(3,(4,5))))");")

# Computation of the Colless-Like, Sackin and Cophenetic
# balance indices of a tree entered as a phylo object:
require(ape)
random.tree = rtree(5,rooted=TRUE)
balance.indices(random.tree)

# Computation of the Colless-Like, Sackin and Cophenetic
# balance indices of a tree entered as a igraph object.
# The tree is randomly generated from all trees with 5
# leaves following the alpha-gamma model with alpha=0.5
# and gamma=0.3.
a.g.tree = a.g.model(5,0.5,0.3)
balance.indices(a.g.tree)

# All of them can be normalized (values between 0 and 1)
balance.indices("(1,2,3,4,5);",norm=TRUE)
balance.indices("(1,(2,(3,(4,5))))",norm=TRUE)
balance.indices(random.tree,norm=TRUE)
balance.indices(a.g.tree,norm=TRUE)
```

---

colless.like.index	<i>Computes the Colless-like balance index of a phylogenetic tree</i>
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---

**Description**

Given a phylogenetic tree, computes the Colless-like balance index of that phylogenetic tree.

**Usage**

```
colless.like.index(tree, f.size = "ln", diss = "MDM", norm = FALSE)
```

## Arguments

tree	a single phylogenetic tree. It can be entered as a string in Newick format, as a 'phylo' object (ape package) or as an 'igraph' object (igraph package).
f.size	function to compute the f-size of the tree. See (Mir et al. , 2017) for details. Its default value is "ln" for $f(n)=\ln(n+e)$ . Other value can be "exp" ( $f(n)=\exp(n)$ ). It can also be a user-defined function but in this case, the index cannot be normalized
diss	by default, the dissimilarity used to compute the balance index. See (Mir et al. , 2017) for details. Its default value is MDM (mean deviation from the median). Other values can be set as "sd" (sample standard deviation) or "var" (sample variance) . It can also be a user-defined function but in this case the index cannot be normalized.
norm	a logical object indicating if the indices should be normalized or not.

## Details

The Colless-Like balance index is the generalization of the Colless balance index (see Colless,1982) for non-binary trees.

Given a function that computes the f-size of a tree and a dissimilarity function that computes the difference of the f-sizes of the subtrees rooted at the children of every internal node of the tree, the Colless-Like index is defined as the sum of these dissimilarities for all internal nodes of the tree. (Mir et al. , 2017)

By default, the f-size function is  $f(n)=\exp(n)$  and the dissimilarity is the mean deviation from the median (MDM). It is possible to change them by specifying it with the parameters `f.size` and `diss`, with "exp" the f-size would be  $f(n)=\exp(n)$ , and with "var" (or "sd") the dissimilarity would be the sample variance (or the sample standard deviation). It is also possible to set a new function for both parameters, see "References".

## Value

A numeric value.

## Author(s)

Lucia Rotger

## References

- A. Mir, F. Rossello, L.Rotger, A Colless-like balance index for multifurcating phylogenetic trees.  
 D. H. Colless, Review of "Phylogenetics: the theory and practice of phylogenetic systematics". *Sys. Zool.*, **31** (1982), 100–104.

## Examples

```
# Computation of the Colless-Like balance index of trees
# entered in newick format:
colless.like.index("(1,2,3,4,5);")
colless.like.index("(1,(2,(3,(4,5))))");

# Computation of the Colless-Like balance index of trees
# entered as a phylo object:
require(ape)
```

```

random.tree = rtree(5,rooted=TRUE)
colless.like.index(random.tree)

# Computation of the Colless-Like balance index of a tree
# entered as a igraph object. The tree is randomly
# generated from all trees with 5 leaves following
# the alpha-gamma model with alpha=0.5 and gamma=0.3.
a.g.tree = a.g.model(5,0.5,0.3)
colless.like.index(a.g.tree)

# All of them can be normalized (values between 0 and 1)
colless.like.index("(1,2,3,4,5);",norm=TRUE)
colless.like.index("(1,(2,(3,(4,5))));",norm=TRUE)
colless.like.index(random.tree,norm=TRUE)
colless.like.index(a.g.tree,norm=TRUE)

# Computation of the Colless-Like balance index of the
# previous generated tree with f-size function f(n)=exp(n):
colless.like.index(a.g.tree,f.size="exp")

# Computation of the Colless-Like balance index of the
# previous generated tree that sets the sample variance
# and the sample standard deviation as dissimilarity.
colless.like.index(a.g.tree,diss="var")
colless.like.index(a.g.tree,diss="sd")

# Computation of the Colless-Like balance index of the
# previous generated tree with f-size function f(n)=exp(n)
# that sets the sample variance and the sample standard
# deviation as dissimilarity.
colless.like.index(a.g.tree,f.size="exp",diss="var")
colless.like.index(a.g.tree,f.size="exp",diss="sd")

```

---

cophen.index

---

*Computes the cophenetic balance index of a phylogenetic tree*


---

## Description

Given a phylogenetic tree, computes the cophenetic balance index of that phylogenetic tree.

## Usage

```
cophen.index(tree, norm = FALSE)
```

## Arguments

tree	a single phylogenetic tree. It can be entered as a string the Newick format, as a 'phylo' object (ape package) or as an 'igraph' object (igraph package).
norm	a logical variable that indicates whether the index should be normalized or not.

## Details

The cophenetic index is computed as the sum of the depths of the least common ancestor (LCA) of every pair of leaves.

**Value**

A numeric value.

**Author(s)**

Lucia Rotger

**References**

A. Mir, F. Rossello, L.Rotger, A new balance index for phylogenetic trees. *Mathematical Biosciences* **241** (2013), 125-136.

**Examples**

```
# Computation of the cophenetic balance index of trees
# entered in newick format:
cophen.index("(1,2,3,4,5);")
cophen.index("(1,(2,(3,(4,5))))");

# Computation of the cophenetic balance index of trees
# entered as a phylo object:
require(ape)
random.tree = rtree(5,rooted=TRUE)
cophen.index(random.tree)

# Computation of the cophenetic balance index of a tree
# entered as a igraph object. The tree is randomly
# generated from all trees with 5 leaves following
# the alpha-gamma model with alpha=0.5 and gamma=0.3.
a.g.tree = a.g.model(5,0.5,0.3)
cophen.index(a.g.tree)

#All of them can be normalized (values between 0 and 1)
cophen.index("(1,2,3,4,5);",norm=TRUE)
cophen.index("(1,(2,(3,(4,5))))",norm=TRUE)
cophen.index(random.tree,norm=TRUE)
cophen.index(a.g.tree,norm=TRUE)
```

---

distribution

*Plot the distribution of Colless-Like, Sackin and cophenetic normalized balance indices under the alpha-gamma model and computes the percentile of a tree from previous distributions.*

---

**Description**

Given alpha, gamma and a phylogenetic tree, plot the distribution of the Colless-Like, Sackin and cophenetic normalized balance indices under the alpha-gamma model and computes the percentile of that tree of the previous normalized balance indices under the alpha-gamma model.



## Usage

```
distribution(tree, alpha = NA, gamma = NA, set.indices = NULL,
  new.simulation = FALSE, repetitions = 1000,
  legend.location = "topright", cex = 0.75, percentile.plot = FALSE,
  db.path = getwd())
```

## Arguments

tree	a single phylogenetic tree. It can be entered as a string in Newick format, as a "phylo" object (ape package) or as an "igraph" object (igraph package).
alpha	parameter of the alpha-gamma model, between 0 and 1.
gamma	parameter of the alpha-gamma model, between 0 and alpha.
set.indices	If NULL (default) the values of the balance indices are taken from stored data or from a new simulated data (See "Details"). If not, it must be a 3-column data.frame with the three balance indices (Colles-like, Sackin, Cophenetic). See <a href="#">indices.simulation</a> .
new.simulation	if FALSE(default) the values of the balance indices are taken from a data.frame entered by the user or from our database. If TRUE, the values of the balance indices are computed from a new simulation. See <a href="#">indices.simulation</a> .
repetitions	if the value of the new.simulation parameter is TRUE, the number of trees to be generated.
legend.location	location of the legend. See "Details".
cex	expansion factor of the legend. See "Details".
percentile.plot	if FALSE (default), density plots of the normalized balance indices are shown. if TRUE, percentiles plots of the normalized balance indices are shown.
db.path	the current working directory. If our database is used, the db.path parameter should be the directory where the database is located.

## Details

Two plots are available: one represents the percentile plots of the normalized balance indices (percentile.plot=TRUE), and the other one represents the density plots of the normalized balance indices (percentile.plot=FALSE).

The trees stored in our database have between 3 and 50 leaves and the values of the parameters alpha and gamma are in {0,0.1,...,1} such that  $\gamma \leq \alpha$ . If the introduced parameters are not in the list, a new computation is done with them and a new dataset of trees is generated, and their indices are also computed. The number of trees generated can be modified by the parameter repetitions (see [indices.simulation](#) for more information). This computation may take some time, therefore you can compute them separately with [indices.simulation](#), save their values and then call this function by setting the parameter set.indices=NULL.

Our database is available to download at <https://github.com/LuciaRotger/CollessLike/tree/master/CollessLikeDataBase>.

The legend is placed with the graphics function legend(), so its location can be specified by setting legend.position to a single keyword from the list "bottomright", "bottom", "bottomleft", "left", "topleft", "top", "topright", "right" and "center". The expansion factor for the legend is controlled by the parameter cex, by default cex=1. See [legend](#).

**Value**

A numeric vector with the three percentiles.

**Author(s)**

Lucia Rotger

**References**

B. Chen, D. Ford, M. Winkel, A new family of Markov branching trees: the alpha-gamma model. *Electr. J. Probab.* **14** (2009), 400-430.

A. Mir, F. Rossello, L. Rotger, A Colless-like balance index for multifurcating phylogenetic trees.

A. Mir, F. Rossello, L. Rotger, A new balance index for phylogenetic trees. *Mathematical Biosciences* **241** (2013), 125-136.

M. J. Sackin, "Good" and "bad" phenograms. *Sys. Zool.* **21** (1972), 225-226.

**See Also**

[legend](#), [indices.simulation](#), [balance.indices](#)

**Examples**

```
#The parameter folder contains the location of the database
#If not specified folder=getwd()

## Different ways to introduce the tree
#From a newick string
distribution("(1,2,3,4,5);",0.5,0.3,db.path=folder)
distribution("(1,(2,(3,(4,5))));",0.5,0.3,db.path=folder)

#From a phylo object
require(ape)
random.tree = rtree(5,rooted=TRUE)
distribution(random.tree,0.5,0.3,db.path=folder)

#An example of a tree generated by the alpha-gamma model (igraph object)
a.g.tree = a.g.model(5,0.5,0.3)
distribution(a.g.tree,0.5,0.3,db.path=folder)

## Different indices data
# From our data base
distribution(a.g.tree,0.5,0.3,db.path=folder)

# From a data.frame generated by 'indices.simulation'
# ('Repetitions' set as 10 for a fast example)
indices.data = indices.simulation(5,0.5,0.3,10)
distribution(a.g.tree,0.5,0.3,set.indices=indices.data)

# Allow the function to do a new generation of data and compute their indices
distribution(a.g.tree,0.5,0.3,new.simulation=TRUE,repetitions=10)
# WARNING! it might take a long time, it depends on the parameters
# 'n' (number of leaves) and 'repetition' (number of repetitions)
```

---

indices.simulation	<i>Generates random trees and compute their balance indices</i>
--------------------	---

---

## Description

Generates a list of trees according to the introduced parameters for the alpha-gamma model. Then, this 3 balance index are calculated: Colless-like, Sackin and Cophenetic.

## Usage

```
indices.simulation(n, alpha = NA, gamma = NA, repetitions = 1000,
  norm = FALSE)
```

## Arguments

n	the number of leaves of the tree.
alpha	parameter of the alpha-gamma model, between 0 and 1.
gamma	parameter of the alpha-gamma model, between 0 and alpha.
repetitions	the number of trees to generate.
norm	a logical object indicating if the indices should be normalized or not.

## Details

Given a number of leaves, the function generates a tree with that number of leaves and computes the three indices of balance (Colless-like, Sackin and Cophenetic with function [balance.indices](#)). This is done as many times as it is set by 'repetitions' parameter, and it generates a 3-column data.frame of indices.

The trees are generated according to the alpha-gamma model. These parameters can be specified by alpha and gamma parameters of the function. The following cases are distinguished:

- alpha = NA and gamma = NA : All the 66 combinations of alpha in { 0, 0.1, 0.2, ... ,0.9, 1 } and gamma in { 0, 0.1, ... ,alpha } are done.
- alpha in [0,1] and gamma = NA : Since alpha is fixed, all the combinations with that alpha and gamma in { 0, 0.1, ... ,alpha } are done.
- alpha in [0,1] and gamma in [0,alpha] : Both parameters are fixed. Then, only that combination is done.

## Value

A 3-column data.frame with the Colless-like, Sackin and Cophenetic balance indices for every generated tree. If more than one data.frame has to be generated, then the returned value is a data.frame list (its names specify which alpha and gamma parameters have generated that data.frame, for instance "a0.5g0.3" indicates alpha=0.5 and gamma=0.3).

## Author(s)

Lucia Rotger

## References

- B. Chen, D. Ford, M. Winkel, A new family of Markov branching trees: the alpha-gamma model. *Electr. J. Probab.* **14** (2009), 400-430.
- A. Mir, F. Rossello, L. Rotger, A Colless-like balance index for multifurcating phylogenetic trees.
- A. Mir, F. Rossello, L. Rotger, A new balance index for phylogenetic trees. *Mathematical Biosciences* **241** (2013), 125-136.
- M. J. Sackin, "Good" and "bad" phenograms. *Sys. Zool.* **21** (1972), 225-226.

## See Also

[balance.indices](#)

## Examples

```
#('Repetitions' set as 100 for a fast example)
indices.table = indices.simulation(5,0.5,0.3,repetitions=10)
head(indices.table)

#Normalized indices (between 0 and 1)
indices.table = indices.simulation(5,0.5,0.3,repetitions=10,norm=TRUE)
head(indices.table)

#Without specifying alpha and gamma
indices.list = indices.simulation(5,repetitions=100)
#by default alpha=seq(0,1,0.1) and gamma=seq(0,alpha,0.1), thus
length(indices.list) #=66
#all the elements of the list have a name that identifies its parameters
indices.list$a0.5g0.3
indices.list$a0.7g0.2
```

---

sackin.index

---

*Computes the Sackin balance index of a phylogenetic tree*


---

## Description

Given a phylogenetic tree, computes the Sackin balance index of that phylogenetic tree.

## Usage

```
sackin.index(tree, norm = FALSE)
```

## Arguments

- |      |  |
|------|--|
| tree | a single phylogenetic tree. It can be entered as a string in Newick format, as a 'phylo' object (ape package) or as an 'igraph' object (igraph package). |
| norm | a logical variable that indicates whether the index should be normalized or not.   |

## Details

The Sackin's index is computed as the sum of the number of ancestors for each leave of the tree.

**Value**

numeric value.

**Author(s)**

Lucia Rotger

**References**

M. J. Sackin, "Good" and "bad" phenograms. *Sys. Zool.* **21** (1972), 225-226.

**Examples**

```
# Computation of the Sackin balance index of trees
# entered in newick format:
sackin.index("(1,2,3,4,5);")
sackin.index("(1,(2,(3,(4,5))));")

# Computation of the Sackin balance index of trees
# entered as a phylo object:
require(ape)
random.tree = rtree(5,rooted=TRUE)
sackin.index(random.tree)

# Computation of the Sackin balance index of a tree
# entered as a igraph object. The tree is randomly
# generated from all trees with 5 leaves following
# the alpha-gamma model with alpha=0.5 and gamma=0.3.
a.g.tree = a.g.model(5,0.5,0.3)
sackin.index(a.g.tree)

#All of them can be normalized (values between 0 and 1)
sackin.index("(1,2,3,4,5);",norm=TRUE)
sackin.index("(1,(2,(3,(4,5))))",norm=TRUE)
sackin.index(random.tree,norm=TRUE)
sackin.index(a.g.tree,norm=TRUE)
```

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