Equal Tree Partition

Given a binary tree with n nodes, your task is to check if it's possible to partition the tree to two trees which have the equal sum of values after removing **exactly** one edge on the original tree.

Example 1:

Input:

/\ 2 3

Output: True

Explanation:

5 / 10

Sum: 15

10 / \ 2 3

Sum: 15

Example 2:

Input:

Output: False

Explanation: You can't split the tree into two trees with equal sum after removing ex actly one edge on the tree.

Note:

- 1. The range of tree node value is in the range of [-100000, 100000].
- 2. 1

Solution 1

The idea is to use a hash table to record all the different sums of each subtree in the tree. If the total sum of the tree is sum, we just need to check if the hash table constains sum/2.

The following code has the correct result at a special case when the tree is [0, -1,1], which many solutions dismiss. I think this test case should be added.

Java version:

```
public boolean checkEqualTree(TreeNode root) {
    Map<Integer, Integer> map = new HashMap<Integer, Integer>();
    int sum = getsum(root, map);
    if(sum == 0) return map.getOrDefault(sum, 0) > 1;
    return sum%2 == 0 && map.containsKey(sum/2);
}

public int getsum(TreeNode root, Map<Integer, Integer> map ){
    if(root == null)return 0;
    int cur = root.val + getsum(root.left, map) + getsum(root.right, map);
    map.put(cur, map.getOrDefault(cur, 0) + 1);
    return cur;
}
```

C++ version:

```
bool checkEqualTree(TreeNode* root) {
    unordered_map<int, int> map;
    int sum = getsum(root, map);
    if(sum == 0) return map[sum] > 1;
    return sum%2 == 0 && map.count(sum/2);
}

int getsum(TreeNode* root, unordered_map<int, int>& map){
    if(root == NULL)return 0;
    int cur = root->val + getsum(root->left, map) + getsum(root->right, map);
    map[cur]++;
    return cur;
}
```

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Solution 2

Cutting an edge means cutting off a proper subtree (i.e., a subtree but not the whole tree). I collect the sums of these proper subtrees in a set and check whether half the total tree sum is a possible cut.

```
def checkEqualTree(self, root):
    def sum(node):
        if not node:
            return 0
        s = node.val + sum(node.left) + sum(node.right)
        if node is not root:
            cuts.add(s)
        return s
    cuts = set()
    return sum(root) / 2 in cuts
```

Alternatively, I collect all subtree sums in a *list* so that the whole tree's sum is at the end. No need for a hash set's searching speed, as I'm searching the collection only once.

```
def checkEqualTree(self, root):
    def sum(root):
        if not root:
            return 0
        sums.append(root.val + sum(root.left) + sum(root.right))
        return sums[-1]
    sums = []
    sum(root)
    return sums.pop() / 2 in sums
```

Oh, an alternative ending (not sure what I like better):

```
sums = []
return sum(root) / 2 in sums[:-1]
```

Note: I used Python 3. In Python 2, change the / 2 to / 2. . written by StefanPochmann original link here

Solution 3

```
class Solution {
   boolean equal = false;
   long total = 0;
   public boolean checkEqualTree(TreeNode root) {
        if (root.left == null && root.right == null) return false;
        total = getTotal(root);
        checkEqual(root);
        return equal;
   }
   private long getTotal(TreeNode root) {
        if (root == null) return 0;
        return getTotal(root.left) + getTotal(root.right) + root.val;
   }
   private long checkEqual(TreeNode root) {
        if (root == null || equal) return 0;
        long curSum = checkEqual(root.left) + checkEqual(root.right) + root.val;
        if (total - curSum == curSum) {
            equal = true;
            return 0;
        return curSum;
   }
```

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From Leetcoder.