2 Keys Keyboard

Initially on a notepad only one character 'A' is present. You can perform two operations on this notepad for each step:

1. `Copy All`: You can copy all the characters present on the notepad (partial copy is not allowed).
2. `Paste`: You can paste the characters which are copied **last time**.

Given a number `n`. You have to get **exactly** `n` 'A' on the notepad by performing the minimum number of steps permitted. Output the minimum number of steps to get `n` 'A'.

Example 1:

```
Input: 3
Output: 3
Explanation:
Intitally, we have one character 'A'.
In step 1, we use Copy All operation.
In step 2, we use Paste operation to get 'AA'.
In step 3, we use Paste operation to get 'AAA'.
```

Note:

1. The `n` will be in the range [1, 1000].

Solution 1

```
    public int minSteps(int n) {
        int[] dp = new int[n+1];

        for (int i = 2; i <= n; i++) {
            dp[i] = i;
            for (int j = i-1; j > 1; j--) {
                if (i % j == 0) {
                    dp[i] = dp[j] + (i/j);
                    break;
                }

            }
        }
        return dp[n];
    }
```

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Solution 2

We look for a divisor `d` so that we can make `d` copies of `(n / d)` to get `n`

The process of making `d` copies takes `d` steps (`1` step of **Copy All** and `d - 1` steps of **Paste**)

We keep reducing the problem to a smaller one in a loop.

```
    public int minSteps(int n) {
        int s = 0;
        for (int d = 2; d <= n; d++) {
            while (n % d == 0) {
                s += d;
                n /= d;
            }
        }
        return s;
    }
```

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Solution 3

```
/**
 * It take 2 op to double, 3 ops to triple, ...
 * if n % 2 == 0, then f(n) = f(n/2) + 2
 * if n % 3 == 0, then f(n) = f(n/3) + 3
 * 2 * 2 = 2 + 2, 2 * 3 > 2 + 3, 4 * 4 > 4 + 4, so it is always better to divide wh
enever possible.
 * now it became a problem for finding all possible factors;
 */
class Solution {
public:
    int minSteps(int n) {
        if (n == 1) return 0;
        for (int i = 2; i < n; i++)
            if (n % i == 0) return i + minSteps(n / i);
        return n;
    }
};
```

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