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1 Environment

1.1 .vimrc

```
set tabstop=4
set shiftwidth=4
set autoindent
set cindent
set number
syntax on
inoremap {<tab> {}<left><return><up><end><return>
imap ` < c-n >
inoremap <c-l> <up><end><space>{<down><end><cr>}<up><end>
inoremap <c-k> <up><end><bs><down><down><esc>ddi<up><end>
set timeoutlen=150
set cino=1-s
set filetype=cpp
iab 11 long long
iab opn freopen("input", "r", stdin)
autocmd BufNewFile *.cpp Or ~/template.cpp
```

1.2 .bashrc

```
alias g++='g++ -Wall -Wextra -g -fsanitize=undefined -std=c++14'
```

2 Mathematics

2.1 Miller Rabin and Pollard Rho

```
namespace MillerRabin {
   long long Mul(long long a,long long b,long long mo){
        long long tmp=a*b-(long long)((long double)a/mo*b+1e-8)*mo;
        return (tmp%mo+mo)%mo;
   }
   long long Pow(long long a,long long b,long long mo){
        long long res=1;
        for(;b;b>>=1,a=Mul(a,a,mo))if(b&1)res=Mul(res,a,mo);
        return res;
   }
   bool IsPrime(long long n){
        if(n==2)return 1;
        if(n<2||!(n&1))return 0;
        static const int P=9,num[P]={2,3,5,7,11,13,17,19,23};
        long long x=n-1; int t=0;
        for(;!(x&1);x>>=1)++t;
        for(int i=1;i<P;++i){</pre>
            long long a=num[i](n-1)+1,res=Pow(an,x,n),last=res;
            for(int j=1;j<=t;++j){</pre>
                res=Mul(res,res,n);
```

```
if(res==1&&last!=1&&last!=n-1)return 0;
                last=res;
            }
            if(res!=1)return 0;
        }
        return 1;
    }
}
namespace PollardRho {
    using namespace MillerRabin;
    unsigned long long seed;
    long long Rand(long long mo){
        return (seed+=417934045419982028911)%mo;
    }
    long long F(long long x,long long c,long long mo){
        return (Mul(x,x,mo)+c)%mo;
    }
    long long gcd(long long a,long long b){
        return b?gcd(b,a%b):a;
    }
    long long Get(long long c,long long n){
        long long x=Rand(n),y=F(x,c,n),p=n;
        for (;x!=y\&\&(p==n||p==1);x=F(x,c,n),y=F(F(y,c,n),c,n))
            p=x>y?gcd(n,x-y):gcd(n,y-x);
        return p;
    }
    void Divide(long long n,long long p[]){
        if(n<2)return;</pre>
        if(IsPrime(n)){p[++*p]=n;return;}
        for(;;){
            long long tmp=Get(Rand(n-1)+1,n);
            if(tmp!=1\&\&tmp!=n){
                Divide(tmp,p);
                Divide(n/tmp,p);
                return;
            }
        }
    }
}
```

2.2 Simplex

```
namespace Simplex {//(<=)+(Maximize)
  const int XN=0,XM=0;
  const double eps=1e-5,inf=1e100;</pre>
```

```
int sgn(double const &x) {
        return (x>-eps)-(x<eps);</pre>
    }
    int n,m;
    double a[XM][XN],b[XM],c[XN],v;
    void Pivot(int 1,int e) {
        b[1]/=a[1][e];
        for(int i=1;i<=n;++i)</pre>
             if(i!=e) a[l][i]/=a[l][e];
        a[1][e]=1/a[1][e];
        for(int i=1;i<=m;++i)</pre>
             if(i!=1 && sgn(a[i][e])) {
                 b[i] -= a[i][e]*b[1];
                 for(int j=1; j<=n;++j)</pre>
                     if(j!=e)
                          a[i][j]-=a[i][e]*a[1][j];
                 a[i][e]*=-a[1][e];
             }
        v+=c[e]*b[1];
        for(int i=1;i<=n;++i)</pre>
             if(i!=e)
                 c[i]-=c[e]*a[l][i];
        c[e]*=-a[1][e];
    }
    double Run() {
        for(int l,e;(e=std::find if(c+1,c+1+n,[&](double const &x)->bool {
                          return sgn(x)>0;} )-c)!=n+1;) {
             double lim=inf;
             for(int i=1;i<=m;++i)</pre>
                 if(IsPositive(a[i][e]) && Reduce(lim,b[i]/a[i][e]))
             if(lim==inf)
                 return inf;
             else
                 Pivot(1,e);
        return v;
    }
}
```

2.3 Gauss

```
typedef double Square[XN][XN];
void Gauss(Square A,int n) {
    for(int i=1;i<=n;++i) {
        int id=i;
        for(int j=i+1;j<=n;++j)
            if(abs(A[j][i])>abs(A[id][i]))
            id=j;
```

```
std::swap_ranges(A[i]+1,A[i]+n+2,A[id]+1);
         for(int k=i+1; k<=n+1; ++k)</pre>
              A[i][k]/=A[i][i];
         A[i][i]=1;
         for(int j=i+1; j<=n;++j) {</pre>
              for(int k=i+1; k<=n+1;++k)</pre>
                  A[j][k] = A[j][i] * A[i][k];
              A[j][i]=0;
         }
    }
    for(int i=n;i>=1;--i) {
         for(int j=i+1; j<=n;++j) {</pre>
              A[i][n+1] = A[j][n+1] * A[i][j];
              A[i][j]=0;
         }
    }
}
```

2.4 Determinant

```
typedef int Square[XN][XN];
//Matrix-Tree 度数-邻接
int Determinant(Square a,int n) {
    for(int i=1;i<=n;++i)</pre>
        for(int j=1; j<=n;++j)</pre>
             ((a[i][j]\%=P)+=P)\%=P;
    int f=1;
    for(int i=1;i<=n;++i) {</pre>
        int &A=a[i][i];
        for(int j=i+1; j<=n;++j) {</pre>
             for(int &B=a[j][i];B;f=P-f) {
                 int t=A/B;
                 for(int k=1; k<=n; ++k)</pre>
                      a[i][k]=Minus(a[i][k],Mul(a[j][k],t));
                 std::swap_ranges(a[i]+1,a[i]+1+n,a[j]+1);
             }
        }
    }
    int res=f;
    for(int i=1;i<=n;++i)</pre>
        res=Mul(a[i][i],res);
    return res;
}
```

2.5 Simpson Formula

```
typedef std::pair<double,double> Point;
double Simpson(Point const &1,Point const &r,Point const &mid) {
   return (r.first-l.first)/6*(l.second+r.second+4*mid.second);
}
```

3 Geometry

3.1 Basic Definations

```
const double eps=1e-10;
int sgn(double const &x) {
   return (x>-eps)-(x<eps);</pre>
}
double p2(double const &x) {
   return x*x;
}
struct Point {
   double x,y;
   double Length() const {
        return sqrt(x*x+y*y);
   }
   Point Normal() const {
        return {-y,x};
   }
   Point Unit() const {
        double len=Length();
        return Point{x/len,y/len};
   }
   friend Point operator +(const Point &a,const Point &b) {
        return {a.x+b.x,a.y+b.y};
   }
   friend Point operator -(const Point &a,const Point &b) {
```

```
return {a.x-b.x,a.y-b.y};
   }
   friend Point operator *(const Point &a,const double &k) {
        return Point{a.x*k,a.y*k};
   }
   friend Point operator /(const Point &a,const double &k) {
        return Point{a.x/k,a.y/k};
   }
   friend double Inner(const Point &a,const Point &b) {
        return a.x*b.x+a.y*b.y;
   }
   friend double Outer(const Point &a,const Point &b) {
        return a.x*b.y-a.y*b.x;
   }
};
struct Line {
   Point p,v;
   double ang;
};
double Dist(const Point &a,const Point &b) {
   return (a-b).Length();
}
double Dist(const Point &a,Line const &1) {
   return fabs(Outer(a-1.p,1.v))/1.v.Length();
}
Point Cross(Line const &11, Line const &12) {
   double t=Outer(12.v,11.p-12.p)/Outer(11.v,12.v);
   return l1.p+l1.v*t;
}
```

3.2 Convex Hull

3.3 Half Plane Intersect

```
bool OnLeft(const Point &p,Line const &l) {
   return sgn(Outer(1.v,p-1.p))>0;
}
bool Paral(Line const &11,Line const &12) {
    return sgn(Outer(11.v,12.v))==0;
}
int Intersect(Line 1[],int n,Line uni[]) {
    std::sort(l+1,l+1+n,[](Line const &a,Line const &b) { return a.ang<b.ang; });
    static Point Qp[XN];static Line Ql[XN];
   int head,tail;Ql[head=tail=1]=1[1];
    for(int i=2;i<=n;++i) {</pre>
        while(tail-head>=1 && !OnLeft(Qp[tail-1],1[i]))
            tail--;
        while(tail-head>=1 && !OnLeft(Qp[head],1[i]))
            head++;
        Q1[++tail]=1[i];
        if(Paral(Q1[tail-1],Q1[tail])){
            --tail;
            if(OnLeft(l[i].p,Ql[tail]))
                Q1[tail]=1[i];
        }
        if(tail-head>=1)
            Qp[tail-1]=Cross(Ql[tail-1],Ql[tail]);
   }
   while(tail-head>=1 && !OnLeft(Qp[tail-1],Ql[head]))
        tail--:
    if(tail-head>=1) {
        std::copy(Ql+head,Ql+tail+1,uni+1);
        return tail-head+1;
   } else
        return 0;
}
```

3.4 Minimal Covering Circle

```
struct Circle {
   Point o;
```

```
double r;
   Circle(Point o,double r):o(o),r(r) {}
};
Point CircleCenter(Point p1,Point p2,Point p3) {
    long double a1=p2.x-p1.x,b1=p2.y-p1.y,c1=(a1*a1+b1*b1)/2;
    long double a2=p3.x-p1.x,b2=p3.y-p1.y,c2=(a2*a2+b2*b2)/2;
   long double d=a1*b2-a2*b1;
   return {p1.x+(c1*b2-c2*b1)/d,p1.y+(a1*c2-a2*c1)/d};
}
Circle MinCoveringCircle(Point p[],int n) {
    std::random shuffle(p+1,p+1+n);
   Point o=p[1];double r=0;
   for(int i=2;i<=n;i++)</pre>
        if(sgn(Dist(o,p[i])-r)>0) {
            o=p[i],r=0;
            for(int j=1; j<i; j++)</pre>
                 if(sgn(Dist(o,p[j])-r)>0) {
                     o=(p[i]+p[j])/2;
                     r=Dist(o,p[i]);
                     for(int k=1;k<j;k++)</pre>
                         if(sgn(Dist(o,p[k])-r)>0) {
                             o=CircleCenter(p[i],p[j],p[k]);
                             r=Dist(o,p[k]);
                         }
                }
   return Circle(o,r);
}
```

3.5 Diameter of Point Set

```
double MaxDist(Point p[],int n) {
    //
    if(n==2) {
        return Dist(p[1],p[2]);
    } else {
        double res=0;
        for(int i=1,cp=2;i<=n;++i) {
            Line cl(p[i],p[i%n+1]-p[i]);
            while(Dist(p[cp],cl)<Dist(p[cp%n+1],cl))
            cp=cp%n+1;
            Enlarge(res,std::max(Dist(p[cp],p[i]),Dist(p[cp],p[i%n+1])));
        }
        return res;
    }
}</pre>
```

3.6 Shortest Distance Between Points

```
double DC(int L,int R) {
    if(L==R)
        return inf;
    else {
        int M=(L+R)/2; double x0=p[M].x;
        double h=std::min(DC(L,M),DC(M+1,R));
        static Point s1[XN],s2[XN],t[XN];
        int c1=0,c2=0;
        for(int i=L;i<=M;++i)</pre>
             if(x0-p[i].x \le h)
                 s1[++c1]=p[i];
        for(int i=M+1;i<=R;++i)</pre>
             if(p[i].x-x0 \le h)
                 s2[++c2]=p[i];
        for(int p1=1,p2=1;p1<=c1;++p1) {</pre>
             while (p2 \le c2 \&\& s1[p1].y-s2[p2].y>h)
                 ++p2;
             for(int i=p2;i<=c2 && s2[i].y<=s1[p1].y+h;++i)</pre>
                 Reduce(h,Dist(s2[i],s1[p1]));
        }
        std: merge(p+L,p+M+1,p+M+1,p+R+1,t+L,[\&](auto const \&a,auto const
         return a.y!=b.y?a.y<b.y:a.x<b.x;</pre>
        });
        std::copy(t+L,t+R+1,p+L);
        return h;
    }
}
```

4 Data Structures

4.1 Splay

```
double DC(int L,int R) {
    if(L==R)
        return inf;
    else {
        int M=(L+R)/2; double x0=p[M].x;
        double h=std::min(DC(L,M),DC(M+1,R));
        static Point s1[XN],s2[XN],t[XN];
        int c1=0,c2=0;
        for(int i=L;i<=M;++i)</pre>
             if(x0-p[i].x \le h)
                 s1[++c1]=p[i];
        for(int i=M+1;i<=R;++i)</pre>
             if(p[i].x-x0 \le h)
                 s2[++c2]=p[i];
        for(int p1=1,p2=1;p1<=c1;++p1) {</pre>
             while (p2 \le c2 \&\& s1[p1].y-s2[p2].y>h)
                 ++p2;
```

4.2 Static Edge-Based DC

```
double DC(int L,int R) {
    if(L==R)
        return inf;
    else {
        int M=(L+R)/2; double x0=p[M].x;
        double h=std::min(DC(L,M),DC(M+1,R));
        static Point s1[XN],s2[XN],t[XN];
        int c1=0,c2=0;
        for(int i=L;i<=M;++i)</pre>
             if(x0-p[i].x \le h)
                 s1[++c1]=p[i];
        for(int i=M+1;i<=R;++i)</pre>
             if(p[i].x-x0 \le h)
                 s2[++c2]=p[i];
        for(int p1=1,p2=1;p1<=c1;++p1) {</pre>
             while (p2 \le c2 \&\& s1[p1].y-s2[p2].y>h)
                 ++p2;
             for(int i=p2;i<=c2 && s2[i].y<=s1[p1].y+h;++i)</pre>
                 Reduce(h, Dist(s2[i],s1[p1]));
        }
        std::merge(p+L,p+M+1,p+M+1,p+R+1,t+L,[&](auto const &a,auto const
         return a.y!=b.y?a.y<b.y:a.x<b.x;</pre>
        });
        std::copy(t+L,t+R+1,p+L);
        return h;
    }
}
```

4.3 Static Vertex-Based DC

```
double DC(int L,int R) {
   if(L==R)
      return inf;
   else {
      int M=(L+R)/2; double x0=p[M].x;
      double h=std::min(DC(L,M),DC(M+1,R));
```

```
static Point s1[XN],s2[XN],t[XN];
         int c1=0,c2=0;
        for(int i=L;i<=M;++i)</pre>
             if(x0-p[i].x<=h)
                 s1[++c1]=p[i];
        for(int i=M+1;i<=R;++i)</pre>
             if(p[i].x-x0 \le h)
                 s2[++c2]=p[i];
        for(int p1=1,p2=1;p1<=c1;++p1) {</pre>
             while (p2 \le c2 \&\& s1[p1].y-s2[p2].y>h)
             for(int i=p2;i<=c2 && s2[i].y<=s1[p1].y+h;++i)</pre>
                 Reduce(h, Dist(s2[i],s1[p1]));
        }
        std::merge(p+L,p+M+1,p+M+1,p+R+1,t+L,[&](auto const &a,auto const
           &b)->bool {
             return a.y!=b.y?a.y<b.y:a.x<b.x;</pre>
         });
        std::copy(t+L,t+R+1,p+L);
        return h;
    }
}
```

4.4 Treap

```
double DC(int L,int R) {
    if(L==R)
        return inf;
    else {
        int M=(L+R)/2; double x0=p[M].x;
        double h=std::min(DC(L,M),DC(M+1,R));
        static Point s1[XN],s2[XN],t[XN];
        int c1=0,c2=0;
        for(int i=L;i<=M;++i)</pre>
            if(x0-p[i].x \le h)
                 s1[++c1]=p[i];
        for(int i=M+1;i<=R;++i)</pre>
            if(p[i].x-x0 \le h)
                 s2[++c2]=p[i];
        for(int p1=1,p2=1;p1<=c1;++p1) {</pre>
            while (p2 \le c2 \&\& s1[p1].y-s2[p2].y>h)
                 ++p2;
            for(int i=p2;i<=c2 && s2[i].y<=s1[p1].y+h;++i)</pre>
                 Reduce(h,Dist(s2[i],s1[p1]));
        }
        std::merge(p+L,p+M+1,p+M+1,p+R+1,t+L,[&](auto const &a,auto const
         return a.y!=b.y?a.y<b.y:a.x<b.x;</pre>
        });
        std::copy(t+L,t+R+1,p+L);
        return h;
    }
```

}

4.5 Virtual Tree

```
double DC(int L,int R) {
    if(L==R)
        return inf;
    else {
        int M=(L+R)/2; double x0=p[M].x;
        double h=std::min(DC(L,M),DC(M+1,R));
        static Point s1[XN],s2[XN],t[XN];
        int c1=0,c2=0;
        for(int i=L;i<=M;++i)</pre>
            if(x0-p[i].x \le h)
                s1[++c1]=p[i];
        for(int i=M+1;i<=R;++i)</pre>
            if(p[i].x-x0 \le h)
                s2[++c2]=p[i];
        for(int p1=1,p2=1;p1<=c1;++p1) {
            while (p2 \le c2 \&\& s1[p1].y-s2[p2].y>h)
                ++p2;
            for(int i=p2;i<=c2 && s2[i].y<=s1[p1].y+h;++i)</pre>
                Reduce(h,Dist(s2[i],s1[p1]));
        }
        std::merge(p+L,p+M+1,p+M+1,p+R+1,t+L,[&](auto const &a,auto const
         return a.y!=b.y?a.y<b.y:a.x<b.x;</pre>
        });
        std::copy(t+L,t+R+1,p+L);
        return h;
    }
}
```

4.6 Aho-Corasick Automaton

```
double DC(int L,int R) {
    if(L==R)
        return inf;
    else {
        int M=(L+R)/2; double x0=p[M].x;
        double h=std::min(DC(L,M),DC(M+1,R));
        static Point s1[XN],s2[XN],t[XN];
        int c1=0,c2=0;
        for(int i=L;i<=M;++i)</pre>
             if(x0-p[i].x \le h)
                 s1[++c1]=p[i];
        for(int i=M+1;i<=R;++i)</pre>
             if(p[i].x-x0 \le h)
                 s2[++c2]=p[i];
        for(int p1=1,p2=1;p1<=c1;++p1) {</pre>
             while (p2 \le c2 \&\& s1[p1].y-s2[p2].y>h)
```

4.7 BitSet

```
double DC(int L,int R) {
    if(L==R)
        return inf;
    else {
        int M=(L+R)/2; double x0=p[M].x;
        double h=std::min(DC(L,M),DC(M+1,R));
        static Point s1[XN],s2[XN],t[XN];
        int c1=0,c2=0;
        for(int i=L;i<=M;++i)</pre>
             if(x0-p[i].x \le h)
                 s1[++c1]=p[i];
        for(int i=M+1;i<=R;++i)</pre>
             if(p[i].x-x0 \le h)
                 s2[++c2]=p[i];
        for(int p1=1,p2=1;p1<=c1;++p1) {</pre>
             while (p2 \le c2 \&\& s1[p1].y-s2[p2].y>h)
                 ++p2;
             for(int i=p2;i<=c2 && s2[i].y<=s1[p1].y+h;++i)</pre>
                 Reduce(h,Dist(s2[i],s1[p1]));
        }
        std::merge(p+L,p+M+1,p+M+1,p+R+1,t+L,[&](auto const &a,auto const
         return a.y!=b.y?a.y<b.y:a.x<b.x;</pre>
        });
        std::copy(t+L,t+R+1,p+L);
        return h;
    }
}
```

4.8 Block-Divided Tree

```
double DC(int L,int R) {
   if(L==R)
     return inf;
   else {
     int M=(L+R)/2;double x0=p[M].x;
```

```
double h=std::min(DC(L,M),DC(M+1,R));
        static Point s1[XN],s2[XN],t[XN];
        int c1=0,c2=0;
        for(int i=L;i<=M;++i)</pre>
             if(x0-p[i].x \le h)
                 s1[++c1]=p[i];
        for(int i=M+1;i<=R;++i)</pre>
             if(p[i].x-x0 \le h)
                 s2[++c2]=p[i];
        for(int p1=1,p2=1;p1<=c1;++p1) {</pre>
             while (p2 \le c2 \&\& s1[p1].y-s2[p2].y>h)
                 ++p2;
             for(int i=p2;i<=c2 && s2[i].y<=s1[p1].y+h;++i)</pre>
                 Reduce(h,Dist(s2[i],s1[p1]));
        }
        std::merge(p+L,p+M+1,p+M+1,p+R+1,t+L,[&](auto const &a,auto const
         return a.y!=b.y?a.y<b.y:a.x<b.x;</pre>
        });
        std::copy(t+L,t+R+1,p+L);
        return h;
    }
}
```

4.9 Dynamic Chain-Based DC

```
double DC(int L,int R) {
    if(L==R)
        return inf;
    else {
        int M=(L+R)/2; double x0=p[M].x;
        double h=std::min(DC(L,M),DC(M+1,R));
        static Point s1[XN],s2[XN],t[XN];
        int c1=0,c2=0;
        for(int i=L;i<=M;++i)</pre>
            if(x0-p[i].x \le h)
                s1[++c1]=p[i];
        for(int i=M+1;i<=R;++i)</pre>
            if(p[i].x-x0 \le h)
                s2[++c2]=p[i];
        for(int p1=1,p2=1;p1<=c1;++p1) {
            while (p2 \le c2 \&\& s1[p1].y-s2[p2].y>h)
            for(int i=p2;i<=c2 && s2[i].y<=s1[p1].y+h;++i)
                Reduce(h,Dist(s2[i],s1[p1]));
        }
        std: merge(p+L,p+M+1,p+M+1,p+R+1,t+L,[\&](auto const \&a,auto const
         return a.y!=b.y?a.y<b.y:a.x<b.x;</pre>
        });
        std::copy(t+L,t+R+1,p+L);
        return h;
```

```
}
}
```

4.10 FHQTreap

```
double DC(int L,int R) {
    if(L==R)
        return inf;
    else {
        int M=(L+R)/2; double x0=p[M].x;
        double h=std::min(DC(L,M),DC(M+1,R));
        static Point s1[XN],s2[XN],t[XN];
        int c1=0,c2=0;
        for(int i=L;i<=M;++i)</pre>
             if(x0-p[i].x \le h)
                 s1[++c1]=p[i];
        for(int i=M+1;i<=R;++i)</pre>
             if(p[i].x-x0 \le h)
                 s2[++c2]=p[i];
        for(int p1=1,p2=1;p1<=c1;++p1) {</pre>
             while (p2 \le c2 \&\& s1[p1].y-s2[p2].y>h)
                 ++p2;
             for(int i=p2;i<=c2 && s2[i].y<=s1[p1].y+h;++i)</pre>
                 Reduce(h,Dist(s2[i],s1[p1]));
        }
        std: merge(p+L,p+M+1,p+M+1,p+R+1,t+L,[\&](auto const \&a,auto const
         return a.y!=b.y?a.y<b.y:a.x<b.x;</pre>
        });
        std::copy(t+L,t+R+1,p+L);
        return h;
    }
}
```

4.11 KDTree

4.12 Leftist

```
double DC(int L,int R) {
    if(L==R)
        return inf;
    else {
        int M=(L+R)/2; double x0=p[M].x;
        double h=std::min(DC(L,M),DC(M+1,R));
        static Point s1[XN],s2[XN],t[XN];
        int c1=0,c2=0;
        for(int i=L;i<=M;++i)</pre>
             if(x0-p[i].x \le h)
                 s1[++c1]=p[i];
        for(int i=M+1;i<=R;++i)</pre>
             if(p[i].x-x0 \le h)
                 s2[++c2]=p[i];
        for(int p1=1,p2=1;p1<=c1;++p1) {</pre>
             while (p2 \le c2 \&\& s1[p1].y-s2[p2].y>h)
                 ++p2;
             for(int i=p2;i<=c2 && s2[i].y<=s1[p1].y+h;++i)</pre>
                 Reduce(h,Dist(s2[i],s1[p1]));
        }
        std::merge(p+L,p+M+1,p+M+1,p+R+1,t+L,[&](auto const &a,auto const
         return a.y!=b.y?a.y<b.y:a.x<b.x;</pre>
        std::copy(t+L,t+R+1,p+L);
        return h;
    }
}
```

4.13 Link-Cut Trees

```
double DC(int L,int R) {
   if(L==R)
     return inf;
   else {
```

```
int M=(L+R)/2; double x0=p[M].x;
        double h=std::min(DC(L,M),DC(M+1,R));
        static Point s1[XN],s2[XN],t[XN];
        int c1=0,c2=0;
        for(int i=L;i<=M;++i)</pre>
            if(x0-p[i].x \le h)
                 s1[++c1]=p[i];
        for(int i=M+1;i<=R;++i)</pre>
            if(p[i].x-x0 \le h)
                 s2[++c2]=p[i];
        for(int p1=1,p2=1;p1<=c1;++p1) {
            while (p2 \le c2 \&\& s1[p1].y-s2[p2].y>h)
                 ++p2;
            for(int i=p2;i<=c2 && s2[i].y<=s1[p1].y+h;++i)
                 Reduce(h,Dist(s2[i],s1[p1]));
        }
        std: merge(p+L,p+M+1,p+M+1,p+R+1,t+L,[\&](auto const \&a,auto const
         return a.y!=b.y?a.y<b.y:a.x<b.x;</pre>
        });
        std::copy(t+L,t+R+1,p+L);
        return h;
    }
}
```

4.14 Scapegoat

```
double DC(int L,int R) {
    if(L==R)
        return inf;
    else {
        int M=(L+R)/2; double x0=p[M].x;
        double h=std::min(DC(L,M),DC(M+1,R));
        static Point s1[XN],s2[XN],t[XN];
        int c1=0,c2=0;
        for(int i=L;i<=M;++i)</pre>
            if(x0-p[i].x \le h)
                 s1[++c1]=p[i];
        for(int i=M+1;i<=R;++i)</pre>
            if(p[i].x-x0 \le h)
                 s2[++c2]=p[i];
        for(int p1=1,p2=1;p1<=c1;++p1) {</pre>
            while (p2 \le c2 \&\& s1[p1].y-s2[p2].y>h)
                 ++p2;
            for(int i=p2;i<=c2 && s2[i].y<=s1[p1].y+h;++i)</pre>
                 Reduce(h,Dist(s2[i],s1[p1]));
        }
        std::merge(p+L,p+M+1,p+M+1,p+R+1,t+L,[&](auto const &a,auto const
         return a.y!=b.y?a.y<b.y:a.x<b.x;</pre>
        });
        std::copy(t+L,t+R+1,p+L);
```

```
return h;
}
```

5 String

5.1 Suffix Array

```
struct SuffixArray {
    int sa[XN],rank[XN],height[XN],n;
    SuffixArray(const char *s):n(strlen(s+1)) {
        static int temp[2][XN],cnt[XN],*x=temp[0],*y=temp[1];
        int m=256;
        std::fill(cnt+1,cnt+1+m,0);
        for(int i=1;i<=n;++i) cnt[x[i]=s[i]]++;</pre>
        std::partial_sum(cnt+1,cnt+1+m,cnt+1);
        for(int i=n;i>=1;--i) sa[cnt[x[i]]--]=i;
        for(int len=1;len<n;len<<=1) {</pre>
            int p=0;
            for(int i=n-len+1;i<=n;++i) y[++p]=i;</pre>
            for(int i=1;i<=n;++i) if(sa[i]>len) y[++p]=sa[i]-len;
            std::fill(cnt+1,cnt+1+m,0);
            for(int i=1;i<=n;++i) cnt[x[i]]++;
            std::partial sum(cnt+1,cnt+1+m,cnt+1);
            for(int i=n;i>=1;--i) sa[cnt[x[y[i]]]--]=y[i];
            std::swap(x,y);x[sa[1]]=p=1;
            for(int i=2;i<=n;++i)</pre>
                 x[sa[i]]=y[sa[i-1]]==y[sa[i]]
                          (sa[i-1]+len <= n?y[sa[i-1]+len]:0) == (sa[i]+len <= n?y[sa[i]+len]:0
            if((m=p)==n) break;
        }
        for(int i=1;i<=n;++i) rank[sa[i]]=i;</pre>
        for(int i=1,len=0;i<=n;++i)</pre>
            if(rank[i]!=1) {
                 int j=sa[rank[i]-1];
                 while(s[i+len]==s[j+len]) ++len;
                height[rank[i]]=len;
                 if(len) len--;
            }
    }
};
```

5.2 Suffix Automaton

```
struct SuffixAutomata {
    struct Node {
        std::map<int,Node*> son;
        Node *par;
}
```

```
int maxRight;
        Node(int maxRight=0):par(0),maxRight(maxRight) {}
    }*root,*last;
    long long cnt;
    SuffixAutomata():root(new Node),last(root),cnt(0) {}
    void Extend(int x) {
        Node *p=last,*nx=new Node(last->maxRight+1);
        for(;p && !p->son[x];p->son[x]=nx,p=p->par);
         if(p==0) {
             nx->par=root;
        } else {
             Node *ox=p->son[x];
             if(p->maxRight+1==ox->maxRight) {
                 nx->par=ox;
             } else {
                 Node *o=new Node(*ox);
                 o->maxRight=p->maxRight+1;
                 ox->par=nx->par=o;
                 for(;p && p \rightarrow son[x] = ox; p \rightarrow son[x] = o, p = p \rightarrow par);
             }
        }
        cnt+=nx->maxRight-nx->par->maxRight;
         last=nx;
    }
};
```

5.3 Suffix Balanced Tree

```
struct SuffixBalancedTree {
    static const double alpha=0.8;
   struct Node {
        Node *son[2];
        double 1,r,tag;
        int size,ndct;
        bool exist;
        char ch;
        Node *next;
        Node (double 1, double r, char ch, Node
        *next):1(1),r(r),tag((1+r)/2),size(1),ndct(1),exist(1),ch(ch),next(next)
           {
            son[0]=son[1]=null;
        Node(void*) {
            size=ndct=exist=0;
            ch=0;
            tag=-1;
            son[0] = son[1] = 0;
```

```
}
    void Up() {
        ndct=son[0] \rightarrow ndct+1+son[1] \rightarrow ndct;
        size=son[0]->size+exist+son[1]->size;
    }
    bool Unbalanced() {
        return ndct*alpha<std::max(son[0]->ndct,son[1]->ndct);
}*root;
std::stack<Node*> nodes;
static Node *null;
SuffixBalancedTree():root(null) {
    nodes.push(null);
}
Node *&Insert(Node *&pos, double 1, double r, char ch, Node *next) {
    if(pos==null) {
        pos=new Node(1,r,ch,next);
        nodes.push(pos);
        return null;
    } else {
        Node *&goat=ch<pos->ch || (ch==pos->ch && next->tag<pos->next->tag)
                     ?Insert(pos->son[0],1,(1+r)/2,ch,next)
                     :Insert(pos->son[1],(1+r)/2,r,ch,next);
        pos->Up();
        return pos->Unbalanced()?pos:goat;
    }
}
static Node *Flatten(Node *pos,Node *app) {
    if(pos==null)
        return app;
    else {
        pos->son[1]=Flatten(pos->son[1],app);
        return Flatten(pos->son[0],pos);
    }
}
static std::pair<Node*,Node*> Rebuild(Node *begin,double 1,double r,int n) {
    if(n==0) {
        return std::pair<Node*,Node*>(null,begin);
    } else {
        int mid=(1+n)/2;
        std::pair<Node*,Node*> left=Rebuild(begin,1,(1+r)/2,mid-1);
        Node *pos=left.second;
        std::pair<Node*, Node*> right=Rebuild(pos->son[1],(1+r)/2,r,n-mid);
        pos->son[0]=left.first;
```

```
pos->son[1]=right.first;
        pos -> l = 1, pos -> r = r, pos -> tag = (l + r)/2;
        pos->Up();
        return std::pair<Node*,Node*>(pos,right.second);
    }
}
static void Rebuild(Node *&root) {
    Node *begin=Flatten(root,null);
    root=Rebuild(begin,root->1,root->r,root->ndct).first;
}
static void Delete(Node *pos,Node *del) {
    if(pos==del) {
        pos->exist=0;
        pos->Up();
    } else {
        Delete(pos->son[pos->tag<del->tag],del);
        pos->Up();
    }
}
int LessCount(const char *s) {
    int res=0;
    for(Node *pos=root;pos!=null;) {
        Node *p=pos;
        const char *c=s;
        while(p->ch==*c) {
            p=p->next;
            ++c;
        }
        if(p\rightarrow ch < *c) {
            res+=pos->son[0]->size+pos->exist;
            pos=pos->son[1];
        } else
            pos=pos->son[0];
    }
    return res;
}
void Append(char ch) {
    Node *&goat=Insert(root,0,1,ch,nodes.top());
    if(goat!=null)
        Rebuild(goat);
}
void Pop() {
    Delete(root, nodes.top());
    nodes.pop();
}
int Count(char *s,int len) {
```

```
s[len+1]=CHAR_MAX;
int res=LessCount(s+1);
s[len+1]=CHAR_MIN;
res-=LessCount(s+1);
//null's ch must satisfy CHAR_MIN < ch < ALL
return res;
}
};
const double SuffixBalancedTree::alpha;
SuffixBalancedTree::Node *SuffixBalancedTree::null=new
SuffixBalancedTree::Node((void*)0);</pre>
```

5.4 Extended KMP

```
//nxt \pm {}^{\circ}B[i..m] B\mu {}^{i \ll 1 \times 2}\tilde{\gamma}
//extend \pm {}^{\circ}A[i..n] B\mu {}^{1}\ll {}^{1}2\check{\jmath}{}^{3}\pi ¶
void exKMP(char *A,char *B,int nxt[],int extend[]) {
    int n=strlen(A+1),m=strlen(B+1),x=1;
    nxt[1]=m;
    for(; x \le M \& B[x] == B[x+1]; ++x);
    nxt[2]=x-1;x=2;
    for(int i=3;i<=m;++i)</pre>
          if(i+nxt[i-x+1]-1<nxt[x]+x-1)nxt[i]=nxt[i-x+1];</pre>
          else{
               int j=nxt[x]+x-i+1;
               if(j<1)j=1;
               for(;j+i-1 \le m \&\&B[j] == B[j+i-1];++j);
               nxt[i]=j-1;
               if(nxt[x]<=nxt[i])x=i;</pre>
          }
    x=1;
    for(;A[x] ==B[x];++x);
    extend[1]=x-1;
    x=1;
    for(int i=2;i<=n;++i)</pre>
          if(i+nxt[i-x+1]-1 < extend[x]+x-1) = extend[i]=nxt[i-x+1];
          else{
               int j=extend[x]+x-i+1;
               if(j<1)j=1;
               for(;j+i-1 \le n \&\&B[j] == A[j+i-1];++j);
               nxt[i]=j-1;
               if(nxt[x]<=nxt[i])x=i;</pre>
          }
```

5.5 Manacher

```
void Manacher(char *str,int rad[])//str @ ma \acute{E} ^{\varrho} iI _{l} 《 ^{\circ} @\mu\dot{I} 볤 \P {
```

```
int len=strlen(str+1),l=0;
    for(int i=1;i<=len;++i){</pre>
          s[++1]='$';
          s[++1]=str[i];
    }
     s[++1]='$';s[0]='#';//s Æ
                                       o -®
    rad[1]=1;
    int R=1, ID=1; //R \ \acute{g} \pm \check{j} \ \rlap{/}/ \ll^3 \ \rlap{/} x \gg
                                       \mathbb{R}\mu Ķ IDIR¶ \muĻ
    for(int i=1;i<=1;++i){</pre>
          if(i<R)</pre>
               rad[i]=min(rad[2*ID-i],R-i+1);//2*ID-iIi \pm j = >
                                                                                       \mu
          else
               rad[i]=1;
          for(;s[i+rad[i]]==s[i-rad[i]];++rad[i]);
          if(R<rad[i]+i-1){
               R=rad[i]+i-1;
               ID=i;
          }
    }
     // ** @\mu >>
                    ®Imax{rad[i]-1}
}
```

5.6 Minimum Representation

6 Graph Theory

6.1 Kth Shortest Path with AStar

6.2 Min Cost-Max Flow

6.3 Edge Biconnected Component

6.4 Vertex Biconnected Component

```
int MinimumRepresentation(int *a,int n) {
    ++a;
    int p1=0,p2=1,len=0;
    while(p1<n && p2<n && len<n) {</pre>
```

6.5 Strongly Connected Component

6.6 Cut Edge

6.7 Cut Vertex

6.8 Dijkstra

6.9 Hungary

```
return std::min(p1,p2)+1;
}
```

6.10 ISAP

6.11 Kuhn-Munkres

7 Number Theory

7.1 Discrete Logarithm with BSGS

7.2 Extended Lucas

7.3 Lucas Theorem

7.4 Min25

```
int MinimumRepresentation(int *a,int n) {
    ++a;
    int p1=0,p2=1,len=0;
    while(p1<n && p2<n && len<n) {</pre>
```

7.5 Polynomial

8 Uncategorized

8.1 Array Pointer

```
template <class T>
struct ArrayPointer {
    int id;

    ArrayPointer(T *x=0) {
        if(!x)
            id=-1;
        else
            a[id=cnt++]=*x;
    }

    T *operator ->() {
        return a+id;
    }

    T &operator *() {
        return a[id];
```

```
static T *a;
static int cnt;
};

/*
template <> TypeName
    *ArrayPointer<TypeName>::a=(TypeName*)malloc(SIZE*sizeof(TypeName));
template <> int ArrayPointer<TypeName>::cnt=0;
overload operator_new
*/
```

8.2 Shared Pointer

```
template <class T>
struct SharedPointer {
   T *ptr;
   int *cnt;
   void Release() {
        if(ptr && --*cnt==0) {
            delete ptr;
            delete cnt;
        }
   }
   SharedPointer():ptr(0),cnt(0) {}
   SharedPointer(T *p):ptr(0) {
        *this=p;
   }
   SharedPointer(SharedPointer const &other):ptr(0) {
        *this=other;
   }
    ~SharedPointer() {
        Release();
   }
   T *operator ->() {
       return ptr;
   }
   T &operator *() {
        return *ptr;
   }
   bool operator ==(SharedPointer const &other) const {
        return ptr==other.ptr;
    }
```

```
bool operator !=(SharedPointer const &other) const {
        return ptr!=other.ptr;
    }
    SharedPointer & operator = (T *p) {
        Release();
        if(p) {
            ptr=p;
            (*(cnt=new int))=1;
        } else {
            ptr=0;
            cnt=0;
        }
        return *this;
    }
    SharedPointer & operator = (SharedPointer const & other) {
        Release();
        if(other.ptr) {
            ptr=other.ptr;
            (*(cnt=other.cnt))++;
        } else {
            ptr=0;
            cnt=0;
        }
        return *this;
    }
};
```

8.3 Mo Tree

```
//By SiriusRen
#include <cmath>
#include <cstdio>
#include <cstring>
#include <algorithm>
using namespace std;
const int N=100050;
int n,m,q,xx,yy,Block,block[N],cnt=1,fa[N][20],tot,top,cnt1,cnt2,op,num[N];
int first[N],next[N*2],v[N*2],C[N],stk[N],deep[N],V[N],W[N],last[N],vis[N];
typedef long long ll;ll Ans[N],ans;
struct Query{
    int l,r,lca,id,time;Query(){}
    Query(int ll,int rr,int zz,int ii,int tt){l=ll,r=rr,lca=zz,id=ii,time=tt;}
    friend bool operator<(Query a,Query b){</pre>
        if(block[a.1] == block[b.1]){
            if(block[a.r] == block[b.r])return a.time < b.time;</pre>
            return block[a.r] < block[b.r];</pre>
        }
        return block[a.1] < block[b.1];</pre>
    }
```

```
}query[N];
struct Change{
    int position,color,lastcolor;Change(){}
    Change(int pp,int cc,int ll){position=pp,color=cc,lastcolor=ll;}
void add(int x,int y){v[tot]=y,next[tot]=first[x],first[x]=tot++;}
void dfs(int x){
    for(int i=first[x];~i;i=next[i])if(v[i]!=fa[x][0])
        fa[v[i]][0]=x,deep[v[i]]=deep[x]+1,dfs(v[i]);
    stk[++top]=x;
    if(top==Block){
        for(int i=1;i<=top;i++)block[stk[i]]=cnt;</pre>
        top=0,cnt++;
    }
}
int lca(int x,int y){
    if(deep[x] < deep[y]) swap(x,y);</pre>
    for(int i=19;i>=0;i--)if(deep[x]-(1<<i)>=deep[y])x=fa[x][i];
    if(x==y)return x;
    for(int i=19;i>=0;i--)if(fa[x][i]!=fa[y][i])x=fa[x][i],y=fa[y][i];
    return fa[x][0];
}
void reverse(int x){
    if(vis[x])ans=(11)V[C[x]]*W[num[C[x]]],num[C[x]]=-;
    else num[C[x]]++,ans+=(11)V[C[x]]*W[num[C[x]]];
    vis[x]^=1;
}
void change_color(int x,int y){
    if(vis[x])reverse(x),C[x]=y,reverse(x);
    else C[x]=y;
}
void work(int x,int y){
    while(x!=y){
        if (deep[x] < deep[y]) swap(x,y);</pre>
        reverse(x), x=fa[x][0];
    }
}
int read(){
    char p=getchar();int x=0;
    while(p<'0'||p>'9')p=getchar();
    while (p>='0' \& p<='9') x=x*10+p-'0', p=getchar();
    return x;
}
int main(){
    memset(first,-1,sizeof(first));
    scanf("%d%d%d",&n,&m,&q);
    for(int i=1;i<=m;i++)V[i]=read();</pre>
    for(int i=1;i<=n;i++)W[i]=read();</pre>
    Block=pow(n,2.0/3.0)*0.5;
    for(int i=1;i<n;i++)xx=read(),yy=read(),add(xx,yy),add(yy,xx);</pre>
    deep[1]=1,dfs(1);
    for(int i=1;i<=top;i++)block[stk[i]]=cnt;</pre>
```

```
for(int j=1; j<=19; j++)</pre>
        for(int i=1;i<=n;i++)</pre>
            fa[i][j]=fa[fa[i][j-1]][j-1];
    for(int i=1;i<=n;i++)C[i]=read(),last[i]=C[i];</pre>
    for(int i=1;i<=q;i++){</pre>
        op=read(),xx=read(),yy=read();
        if(op){
            if(block[xx]>block[yy])swap(xx,yy);
            query[++cnt1] = Query(xx,yy,lca(xx,yy),cnt1,cnt2);
        else change[++cnt2]=Change(xx,yy,last[xx]),last[xx]=yy;
    }
    sort(query+1, query+1+cnt1);
    for(int i=1,T=0;i<=cnt1;i++){</pre>
           for(;T<query[i].time;T++)change_color(change[T+1].position,change[T+1].color)</pre>
         → for(;T>query[i].time;T--)change_color(change[T].position,change[T].lastcolor)
        if(i==1)work(query[i].1,query[i].r);
        else work(query[i-1].1,query[i].1),work(query[i-1].r,query[i].r);
        reverse(query[i].lca), Ans[query[i].id] = ans, reverse(query[i].lca);
    for(int i=1;i<=cnt1;i++)printf("%lld\n",Ans[i]);</pre>
}
```

8.4 Mo Sequence

```
//By SiriusRen
#include <cmath>
#include <cstdio>
#include <algorithm>
using namespace std;
const int N=1050000;
int n,m,a[N],cnt1,cnt2,Block,block[N],xx,yy,ans,sum[N],last[N],Ans[N];
char op[105];
struct Query{
    int L,R,time,id;
    Query(int LL,int RR,int TT,int II){
        L=LL,R=RR,time=TT,id=II;
    }Query(){}
}query[N];
struct Change{
    int position,color,lastcolor;
    Change(int II,int CC,int LL){
        position=II,color=CC,lastcolor=LL;
    }Change(){}
}change[N];
bool operator<(Query a,Query b){</pre>
    if(block[a.L] == block[b.L]){
        if(a.R!=b.R)return a.R<b.R;</pre>
        return a.time<b.time;</pre>
    }
```

```
return block[a.L] < block[b.L];</pre>
}
void update(int x,int f){
    if(f==1){if(!sum[x])ans++;sum[x]++;}
    else if(f==-1)\{if(sum[x]==1)ans--; sum[x]--;\}
}
int main(){
    scanf("%d%d",&n,&m);
    Block=(int)pow(n, 2.0/3.0);
    for(int i=1;i<=n;i++)scanf("%d",&a[i]),last[i]=a[i],block[i]=(i-1)/Block+1;</pre>
    for(int i=1;i<=m;i++){</pre>
        scanf("%s%d%d",op,&xx,&yy);
        if(op[0] == 'Q')query[++cnt1] = Query(xx,yy,cnt2,cnt1);
        else change[++cnt2]=Change(xx,yy,last[xx]),last[xx]=yy;
    }
    sort(query+1, query+1+cnt1);
    for(int L=1,R=0,i=1,T=0;i<=cnt1;i++){</pre>
        for(;T<query[i].time;T++){</pre>
             if (change [T+1].position>=L&&change [T+1].position<=R)
                 update(a[change[T+1].position],-1),update(change[T+1].color,1);
             a[change[T+1].position]=change[T+1].color;
        for(;T>query[i].time;T--){
             if(change[T].position>=L&&change[T].position<=R)</pre>
                 update(a[change[T].position],-1),update(change[T].lastcolor,1);
             a[change[T].position]=change[T].lastcolor;
        }
        for(;R<query[i].R;R++)update(a[R+1],1);</pre>
        for(;R>query[i].R;R--)update(a[R],-1);
        for(;L<query[i].L;L++)update(a[L],-1);</pre>
        for(;L>query[i].L;L--)update(a[L-1],1);
        Ans[query[i].id] = ans;
    }
    for(int i=1;i<=cnt1;i++)printf("%d\n",Ans[i]);</pre>
}
```