

ESAME

14/01/25

① Volume di

$$A = \{(x, y, z) \in \mathbb{R}^3 \mid 3y^2 - 3 \leq 2x^2 + 7z^2 \leq 2y^2 + 5, y \geq 0\}$$

②  $f(x, y, z) = 3x + 2y - z^2$

zistette ad A -  $\{(x, y, z) \in \mathbb{R}^3 \mid 3x^2 + 4y^2 + 2z^2 = 12\}$

③  $f(x, y, z) = 4yz^2 - 5x^2z^2 + 2y^2 + 3z^2$

④  $f(x, y, z) = \frac{y^{x^2+2z}}{4} - \frac{x^{yz}}{2}$

$$\Gamma = \{(x, y, z) \in \mathbb{R}^3 \mid xyz^2 - x^2yz + y^2z^2 = 4\}$$

$$\hat{v} \in N_Q \Gamma \quad Q = (2, 1, 2) \quad \langle \hat{v}(Q), \hat{j} \rangle < 0$$

$$\frac{\partial f}{\partial \hat{v}}(Q) = ?$$

⑤  $f(x, y, z) = (3y - 5x^2y)\hat{i} + 3y^2\hat{j} - (2z + xy)\hat{k}$

$$\Gamma = \{(x, y, z) \in \mathbb{R}^3 \mid y = 5x^2 + 3z^2, 1 \leq y \leq 2\}$$

$$\langle \hat{v}, \hat{j} \rangle < 0 \quad \hat{v} \text{ orient. di } \Gamma$$

• div f?

• orient. del bordo  
in un punto

• parametriz. con dominio

• orientamento associato e compatibilità

• flusso di f su  $\Gamma$